On the Impossibility of Cryptography Alone for Privacy-Preserving Cloud Computing

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Abstract

Cloud computing denotes an architectural shift toward thin clients and conveniently centralized provision of computing resources. Clients' lack of direct resource control in the cloud prompts concern about the potential for data privacy violations, particularly abuse or leakage of sensitive information by service providers. Cryptography is an oft-touted remedy. Among its most powerful primitives is *fully homomorphic encryption* (FHE), dubbed by some the field's "Holy Grail," and recently realized as a fully functional construct with seeming promise for cloud privacy.

We argue that cryptography alone can't enforce the privacy demanded by common cloud computing services, even with such powerful tools as FHE. We formally define a hierarchy of natural classes of private cloud applications, and show that no cryptographic protocol can implement those classes where data is shared among clients. We posit that users of cloud services will also need to rely on other forms of privacy enforcement, such as tamperproof hardware, distributed computing, and complex trust ecosystems.

1 Introduction

Cloud computing is a model of information processing, storage, and delivery in which highly centralized physical resources are furnished to remote clients on demand. Rather than purchasing actual physical devices—servers, storage, and networking equipment—clients lease these resources from a cloud provider as a outsourced service that abstracts away physical devices. By sharing infrastructure among tenants, a cloud provider achieves economies of scale and balances workloads, reducing per-unit resource costs and giving clients the ability to ratchet their resource consumption up or down. Cloud computing is flexible and portable in that it can be accessed anytime from anywhere. By using redundant sites and backup storage, cloud providers can also provide greater reliability than local computing systems.

For all the benefits of cloud computing, though, it deprives clients of direct control over the systems that manage their data. Thus arises a central concern of cloud computing: How can clients trust that a cloud provider will protect the privacy of their data, i.e., not leak their data or itself use their data inappropriately?

In this paper, we explore privacy protection in cloud architectures. In particular, we consider the challenge of having a cloud service run applications over client data while: (1) Not being able to learn any information itself and (2) Releasing output values to clients in accordance with an access-control policy. We argue that by itself, cryptography—and by implication, any logical layer information security tool—can't solve this problem in its full generality. Yet this privacy-preserving model is exactly the one ultimately desired for cloud applications involving multiple tenants, such as social networking, document sharing, and so forth. Given recent excitement over the potential of new, powerful constructs such as *fully homomorphic encryption* (FHE) [11] to support the privacy needs of cloud computing, we believe that our negative message is an important and sobering one.

1.1 Cloud Model

We treat a cloud for simplicity as a highly resourced, monolithic entity S. We denote each entity relying on S's resources as a *client* or *tenant*. (In usual parlance, a tenant is a relying entity; a client is a machine. We use the terms interchangeably.) We denote the set of n tenants of S by $\mathcal{C} = \{C_1, C_2, \ldots, C_n\}$.

In our model of cloud computing, clients are thin. They have limited local computation and storage, delegating as much as possible to a cloud provider. And they are not consistently on-line. They may deposit data in the cloud and go offline indefinitely. Consequently, a cloud provider assumes responsibility for processing data in the absence of its owners.

For the purposes of our exploration here, we treat the data of each player C_i as a static, private value x_i. C_i

stores x_i with S. S is tasked with executing various applications over $\{x_i\}$. The overarching goal of privacy preservation we explore in this paper dictates that in no case should S learn any portion of any piece x_i of private data. Applications that operate over the data of multiple clients respect access-control policies, as we explain.

1.2 Our Contribution

We explore the challenge of privacy preservation for clients in the cloud by proposing a (nested) hierarchy of three classes of privacy-preserving forms of computing. These classes are meant to characterize natural applications that S might be called upon to execute in the cloud over clients' sensitive data. We define privacy preservation here to mean that S itself should learn *no information* from any application execution, while select clients should learn limited output information. (We do not consider *bidirectional privacy* here, i.e., we do not consider the privacy of S.) The three classes, in order of increasing generality, are:

1. **Private single-client computing**: These applications execute over the data x_i of a given client C_i. Their access-control policy stipulates that only C_i may learn any output. Note that an access-control policy restricting C_i's access to outputs isn't meaningful: Since x_i belongs to C_i, revealing any function of x_i to C_i leaks no information.

   Example: A privacy-preserving tax-preparation program might be implemented via private single-client computing. The data x_i consists of the financial statements of C_i—to be hidden from S. The output of the program is a prepared tax return.

2. **Private multi-client computing**: These applications execute over the data $\{x_i\}_{i=1}^n$ of multiple clients $\{C_i\}_{i=1}^n$. Since clients may not be mutually trusting (and might collude with S), a multi-client application's access-control policy must stipulate release of information selectively to different clients. Such release may be asymmetric, i.e., for a given f, C_j may be granted permission to learn $f(x_i, x_j)$, while C_i isn't.

   Example: A social networking system might be designed as a private multi-client system. Here, x_i is the personal profile of client C_i. C_i adlso specifies which friends are entitled to what portions / functions of her data, i.e., gives an access-control policy.

3. **Stateful private multi-client computing**: These are private multi-client applications in which the access-control policy on a client's data is stateful, in the sense that it depends on the history of application execution by S.

   Example: A healthcare-research system might be implemented via stateful private multi-client computing in which a client is either a patient or a research facility. A patient C_i furnishes healthcare record x_i. A research facility C_i is permitted to learn certain aggregate statistics over the full set of healthcare records in the system. The access-control policy is stateful in the following sense, though: The aggregate information a research facility receives from the system should never be sufficient to reveal individually identifying data. (The system might enforce a standard privacy metric such as k-anonymity [25].)

Single-client private computing is realizable via FHE, as we explain below.

Private multi-client computing is an important class to consider because it provides natural cloud functionality that is fairly limited, but, as we prove, still not realizable by *any* cryptographic protocol. We prove that private multi-client computing implies general *program obfuscation*, which is provably unachievable in software alone [4]. (Special cases are realizable; our impossibility result applies to the class as a whole.) Thus private multi-client applications require *trustworthy computation* of some type. (Exactly how general such trustworthy computation needs to be is an open problem.) By trustworthy computation, we mean integrity-protected execution history and integrity-protected application of history to access control—i.e., functionality equivalent to a fully trusted party.

Stateful private multi-client applications are an important class to study, as they characterize the norm in the cloud. They include social networks (e.g., Facebook), shared applications (e.g., Google Apps), customer relationship management (e.g., Salesforce.com), etc. They are growing in prevalence. Stateful private multi-client functions clearly imply trustworthy computation in S.

Organization: In section 2, we discuss FHE and survey related work. We explore our three privacy-preserving application classes in detail in section 3, and prove that the class of private multi-client programs cannot be constructed. We conclude in section 4 with a discussion of practical approaches to cloud privacy.

2 Related Work

Privacy is a well recognized sticking point in the cloud. Garfinkel [9] discusses how Google Chrome OS realizes the thin-client / monolithic server model we explore here and the privacy concerns that the resulting data amalgamation and loss of infrastructural control bring to consumers. Enterprises too cite security and privacy as top challenges in cloud adoption, as shown in surveys, e.g., [1], and generally cautious industry adoption [24].

Researchers tend to advocate a consistent set of approaches to privacy enforcement in the cloud. Chow et al. [7] classify these approaches in three major categories: (1) "Information-centric" security, in which data objects are tagged with access-control policies—essentially the mode of operation envisioned in the multi-client classes of the private computing hierarchy we propose here; (2) Trusted computing; and (3) Privacy-preserving cryptographic protocols, which are, of course, the main focus of our work in this paper.

There are a number of privacy-preserving cryptographic protocols appropriate for specific cloud applications. Among these is Private Information Retrieval (PIR) [6], which allows a client to query a database without S learning which queries the client has submitted. Another example is searchable encryption; see, e.g., [23] for early work and [22] for more recent results. Searchable encryption allows the owner of a set of documents to authorize another party to conduct searches on a prespecified set of keywords, without revealing any additional information. These are special cases of private multi-player applications.

Proposed as a research challenge in 1978 [21], and long considered the "Holy Grail" of cryptography [19], Fully Homomorphic Encryption was first realized by Gentry in 2009 [11]. FHE enables computation over encrypted data. In a cloud environment, a client can store encrypted data on a server. The server can compute over this data without decrypting, and can send a ciphertext result to the client for decryption. Thus the server computes "under the covers" in a fully privacy-preserving way, never learning the client's data. While not yet efficient enough for practice, FHE in theory provides general privacy protection for a client-server relationship.

FHE provides a general solution for secure two-party computation, also called secure function evaluation (SFE) [28]. In this sense FHE is a special case of *secure multiparty computation* (SMC), first proposed in [12], and subsequently explored in an extensive literature. SMC allows a set of (multiple) players to compute an arbitrary (bounded complexity) function over private inputs. It realizes, as an interactive protocol, the ideal functionality provided by a trusted party (or piece of hardware). In its general form, however, SMC requires players to be online, and thus isn't suitable for client enforcement of privacy in thin-client cloud architectures.

3 Cloud-Application Class Hierarchy

3.1 Private Single-Client Computing

In the private single-client scenario, client C asks the cloud S to evaluate a function f over C's private input x. S should learn no information from the computation, so it is necessary that x, $f(x)$, and any intermediate values in the computation of $f(x)$ remain encrypted under C's public key p.[1]

More generally, C's private input x can be a composite $x = (x_1, \ldots, x_n)$ of different values $\{x_i\}_{i=1}^n$ supplied respectively by other clients $\{C_i\}_{i=1}^n$. Each x_i is encrypted under C's public key p to yield corresponding ciphertext c_i. Figure 1 depicts this more general scenario. The cloud S evaluates the resulting ciphertexts c_i via evaluation algorithm $\texttt{Eval}_{\mathcal{E}}$. The final result is a ciphertext c, an encryption of function value $f(x_S, x_1, \ldots, x_n)$ under p. Here $f(x_S, x_1, \ldots, x_n) = f(x_S, x)$ is f evaluated in C's private value x together with a value x_S supplied by $\mathcal{S}$.[2] The subscript $\mathcal{E}$ indicates that the evaluation algorithm $\texttt{Eval}_{\mathcal{E}}$ is associated with the encryption scheme $\mathcal{E}$, which consists of a key-generating, an encryption, and a decryption algorithm.

Note that the $\{x_i\}$ are private with respect to S, an important issue when we examine multi-client scenarios.

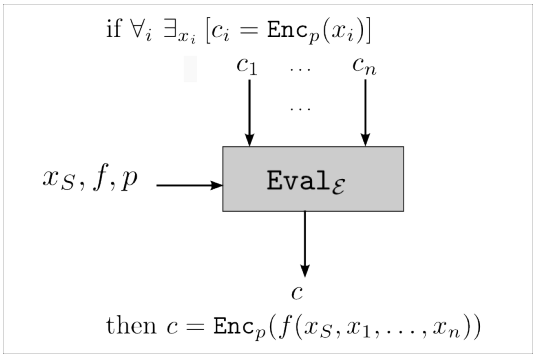

Figure 1: Private Single-Client Computing

It is possible to construct a semantically secure (against chosen plaintext attacks) encryption scheme $\mathcal{E}$ together with an evaluation algorithm $\texttt{Eval}_{\mathcal{E}}$ that satisfies the property shown in Figure 1. Gentry [11] constructed the first fully homomorphic encryption (FHE) scheme, which solves this problem. Non-homomorphic or partially homomorphic, i.e., ordinary encryption of data doesn't allow someone without knowledge of the secret decryption key to manipulate underlying data in a general way. In an FHE scheme, any f realizable as a (polynomial-size) circuit can be executed without leaking information about inputs, intermediate values, or outputs.

FHE can be used by a single client to outsource private computation to the cloud. But the range of cloud

[1] In single-client applications where only the client encrypts her data, symmetric-key encryption suffices, because a single entity encrypts and decrypts the data. If other entities contribute data, then public key encryption is necessary.

[2] Function f may discard x_S. Value x_S can also be encrypted input if the cloud also plays the role of another entity who contributes private data.

operations enabled by FHE is restricted to an encryption domain defined by the public key p of a single client. For more general cloud applications, we need to define a more general class.

3.2 Private Multi-Client Computing

The objective in a multi-client setting is to compute across data supplied by multiple clients, but also to reveal output values to multiple clients in a privacy-preserving way. To achieve this goal, we need a new primitive that has functionality beyond FHE. In particular, there are two new requirements:

1. **Access-controlled ciphertexts**: Because computation takes place across multiple clients, it's important that a client C_i be able to stipulate what functions may be computed on its private input x_i. If arbitrary computation is permitted, then x_i itself may be revealed to all other clients (and a colluding S). We refer to this privacy requirement as *functional privacy*.

2. **Re-encryption**: Privacy-protected transformation of a ciphertext under a key p' to a key p is required to enforce functional privacy. If the encryption keys p' and p are identical, then any client that can decrypt outputs can also decrypt and learn inputs, preventing any kind of access control.

In the private multi-client setting, then, S evaluates function f on private inputs $\{x_i\}$ encrypted under (potentially) different clients' public keys p_i. We let c_i denote the ciphertext of C_i. Functional privacy is enforced by allowing C_i to tag ciphertext c_i with access-control policy A_i that indicates whether x_i can be used as input to a given function f with output encrypted under public key p. We write $c_i = \texttt{Enc}_{p_i}(x_i, A_i)$. We model A_i as a membership circuit that takes as input triples (i, f, p). If $A_i(i, f, p) = \texttt{true}$, then client C_i allows x_i to be used as the ith input to f if its final result is encrypted under p. (Note that any client C_i can be a permitted receiver of output in this model, namely when $p = p_i$.)

Figure 2 depicts the new situation. If and only if access-control policies on all ciphertexts $\{c_i\}$ are met, the evaluation algorithm $\texttt{Eval}_{\mathcal{E}}$ returns a ciphertext $c = \texttt{Enc}_p(f(x_S, x_1, \ldots, x_n))$.

We now prove that private multi-client computing is in general unachievable using cryptography.

Two-player setting: For the purposes of our proof, it is simplest to consider a special case of the private multi-client computing class, namely a two-player setting as depicted in Figure 3. There is one sender and one receiver. The function f takes only two inputs, x_S and x_1. The sender uses a simple access-control policy $A_{(1,f,p)}$, a membership circuit that outputs $\texttt{true}$ only for input

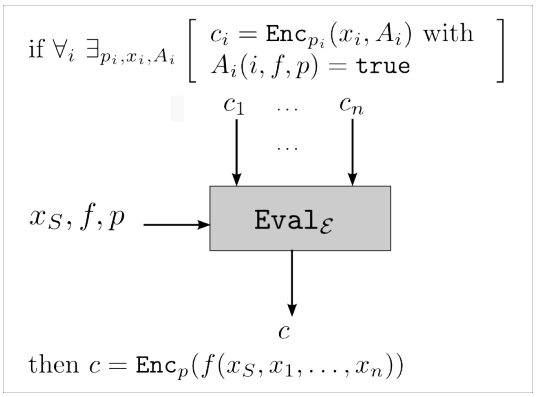

Figure 2: Private Multi-Client Computing

$(1, f, p)$, i.e., allows only one function f and one output key p. The receiver knows the secret key s corresponding to p and is able to decrypt the result and retrieve the function output $f(x_S, x_1)$ for any x_S. In this sense the receiver has oracle access to the function $x_S \to f(x_S, x_1)$. (Observe that this two-player scheme may be viewed as a multi-player application in which there are two clients and S learns the decryption key of or colludes with one client.)

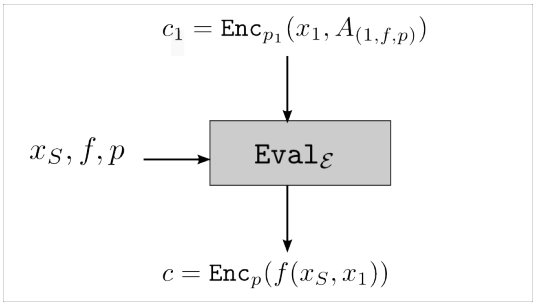

Figure 3: 2-Player Setting

Definition 1 *A two-player private computing scheme has* functional privacy *over circuits if: For all ppt adversaries $\mathcal{A}$, there exists a ppt simulator $\mathcal{S}$, and a negligible function α, such that for all $(p_1, s_1), (p, s) \leftarrow \texttt{Gen}(1^\lambda)$, for all circuits f, for all ciphertexts $c_1 \leftarrow \texttt{Enc}_{p_1}(x_1, A_{(1,f,p)})$ and for all poly-time computable binary predicates π,*

$$Pr[\mathcal{A}(p_1, f, p, c_1, s) = \pi(x_1)] \leq Pr[\mathcal{S}^{\{x_S \to f(x_S, x_1)\}}(1^\lambda) = \pi(x_1)] + \alpha(\lambda).$$

Here, λ is a security parameter; all asymptotics are in λ. $\mathcal{S}$ represents a simulator with oracle access to function $x_S \to f(x_S, x_1)$.

The definition formalizes the intuition that privacy means that an adversary learns no more about x_1 than a simulator can learn using oracle access to $x_S \to$

$f(x_S, x_1)$. That is, an adversary learns about x_1 only what the access control policy $A_{(1,f,p)}$ dictates.

Note that functional privacy does not imply semantic security. Two-player private computing —and by implication, full multi-client private computing—is not semantically secure against chosen-plaintext attacks. The receiver can distinguish between plaintexts by choosing x_1, x_1', x_S and f such that $f(x_s, x_1) \neq f(x_s, x_1')$.

Reducing two-player scheme to program obfuscation: Figure 4 shows a reduction from a two-player private computing scheme with functional privacy to an efficient circuit obfuscator $\mathcal{O}$ which takes any circuit g as input and outputs an obfuscated circuit $\mathcal{O}_g$. In this reduction, all circuit sizes and running times are polynomial in λ where λ is set as $|g|$, the circuit size of g.

The main idea (detailed in the appendix) is to create an execution environment that evaluates a given program g over an input x "under the covers," i.e., in the domain of encryption under key p_1. This is accomplished by feeding a representation $\langle g \rangle$ of g into $\texttt{Eval}_{\mathcal{E}}$ (expressed as an evaluation circuit[3]) in x_1 and setting input value $x = x_S$. The actual function evaluation $g(x)$ is performed by a "meta-circuit" F that takes as input x and $\langle g \rangle$, i.e., F is a generic circuit that runs *any* circuit g on any input value.[4] F is the homomorphically computed function here. (Ciphertext x_1 is tagged with access-control policy $A_{(1,F,p)}$, which permits application of F.) The computation result $g(x)$ is output by a decryption circuit.[5]

The set $BB = (p_1, F, p, c_1 = \texttt{Enc}_{p_1}(\langle g \rangle, A_{(1,F,p)}), s)$ of values circled in Figure 4 fully defines the execution environment, i.e., is all the data needed to realize it. The only variable value is the input x. Thus, running the two-player scheme on BB gives us a "black box" that takes input x and outputs $g(x)$—an obfuscated circuit $\mathcal{O}_g$ that executes g.[6]

By definition 1, it is easy to show that for execution of BB, we have

$$Pr[\mathcal{A}(\mathcal{O}_g) = \pi(g)] \leq Pr[\mathcal{S}^g(1^{|g|}) = \pi(g)] + \alpha(|g|).$$

That is, execution of BB obfuscates any (poly-size) program g, which we know is not achievable [4]. We conclude that general multi-client private computing based solely on cryptographical assumptions is impossible.

Remarks: Our proof technique is general: it can be used to prove the impossibility of multi-client computing schemes with functional privacy defined over Turing Machines (TM) or constant depth threshold circuits (TC0) (for which obfuscation impossibility results exist [4]).

While *general* program obfuscation is impossible, the literature does include positive results for *specific* forms of obfuscation, including point functions [18, 27, 13] and certain cryptographic primitives [15, 14].

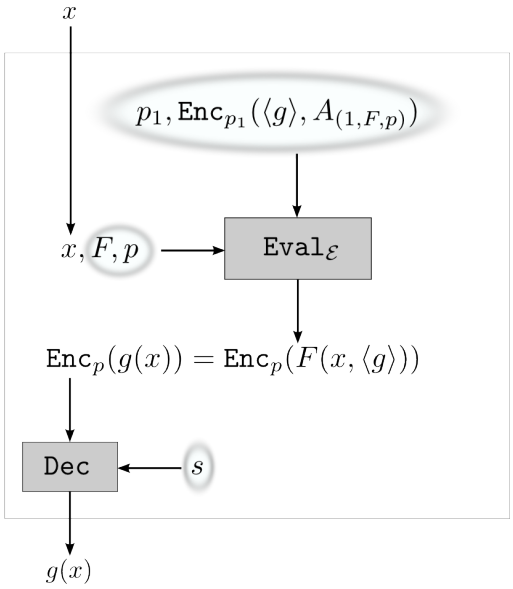

Figure 4: Obfuscated circuit $\mathcal{O}_g$

3.3 Private Stateful Multi-Client

Due to lack of space, we omit a formal definition of private stateful multi-client computing. We remark only that in this class, the access control policies for a ciphertext include *the full history of computation of* S over the data of the client C that owns the ciphertext. A trustworthy computation environment is clearly necessary to realize this class of applications. As remarked above, this class includes many important applications in the cloud.

A key question, then, regards the relationship between private multi-client computing and stateful private multi-client computing. We proved above that private multi-client computing cannot be realized with cryptography (i.e., software) alone; thus such applications require trusted state / execution of some sort. Are the two application classes equivalent, then, in the sense of having identical trusted execution requirements? This as an important open problem.

4 Conclusion: How to Get Cloud Privacy?

We have shown the limitations of cryptography alone in meeting the challenges of cloud privacy. So what practical options are there for trustworthy computation? One frequently advocated tool is *trusted computing*, i.e., privacy (and security) enforcement via tamper-resistant

[3] We assume that evaluation is compact, i.e., there exists a polynomial h such that for every value of λ, $\texttt{Eval}_{\mathcal{E}}$ can be expressed as a circuit E of size $|E| \leq h(\lambda)$.

[4] F can be constructed such that its size is polynomial in λ, i.e., polynomial in the size of its inputs.

[5] We assume that decryption `Dec` is compact.

[6] This procedure describes a circuit obfuscator $\mathcal{O}$, which is efficient in that $\mathcal{O}$ itself is a polynomial time algorithm, and its output $\mathcal{O}_g$ has circuit size polynomial in $|g|$.

hardware. The limitations of that approach too are legion. They include vulnerability to low-resource hardware attacks [2] and man-in-the-middle attacks during bootstrapping [20]. Even well-functioning hardware cannot guarantee system integrity. Trusted Platform Modules (TPMs) [26], the most prevalent form of trusted hardware, provide only a root of trust: They help ensure the execution of a given software stack, but don't protect against software vulnerabilities. Newer trusted computing technologies such as Intel TXT protect executables, but of course cannot ensure the trustworthiness of applications themselves [16]. Software introspection via, e.g., a trusted hypervisor, can help [10], but also falls far short of comprehensive security assurance.

Additionally, a meaningful trusted computing architecture for the cloud presumes an external entity that can verify the security and privacy posture of a provider. Cloud infrastructure providers are already developing architectures that presume such distributed trust: Trusted hardware and software logging tools generate attestations for consumption by an auditing or compliance-verification system [8].

An alternative to trust in a single provider is trust in a collection of providers. Clients can distribute their data across such a collection and delegate privacy enforcement to it. By executing applications via SMC, the providers can process client data in a privacy-preserving manner (in a stateful multi-client model). Correct execution is ensured given an honest majority. In its general form, though, SMC demands impractically intensive computation and communication. We believe that in the short-to-medium term, limited-capability distributed trust models will prevail. While as always helping demarcate trust boundaries, cryptography will also help verify specific security requirements of cloud deployments, e.g., correctly configured storage [3, 5, 17]. It will be one supporting component in a complex ecosystem of trust that depends on interlocking technical, regulatory, and commercial security and privacy enforcement approaches.

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