# On the relationship between azimuthal anisotropy from shear wave splitting and surface wave tomography

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Abstract. Seismic anisotropy provides essential constraints on mantle dynamics and continental evolution. One particular question concerns the depth distribution and coherence of azimuthal anisotropy, which is key for understanding force transmission between the lithosphere and asthenosphere. Here, we reevaluate the degree of coherence between the predicted shear wave splitting derived from tomographic models of azimuthal anisotropy and that from actual observations of splitting. Significant differences between the two types of models have been reported, and such discrepancies may be due to differences in averaging properties, or due to approximations used in previous comparisons. We find that elaborate, full waveform methods to estimate splitting from tomography yield generally similar results to the more common, simplified approaches. This validates previous comparisons and structural inversions. However, full waveform methods may be required for regional studies, and they allow exploiting the back-azimuthal variations in splitting that are expected for depth-variable anisotropy. Applying our analysis to a global set of SKS splitting measurements and two recent surface-wave models of upper-mantle azimuthal anisotropy, we show that the measures of anisotropy inferred from the two types of data are in substantial agreement. Provided that the splitting data is spatially averaged (so as to bring it to the scale of long-wavelength tomographic models and reduce spatial aliasing), observed and tomography-predicted delay times are significantly correlated, and global, angular misfits between predicted and actual splits are relatively low. Regional anisotropy complexity notwithstanding, our findings

imply that splitting and tomography yield a consistent signal that can be used for geodynamic interpretation.

# 1. Introduction

Earth's structure and tectonic evolution are intrinsically linked by seismic anisotropy in 1 the upper mantle and lithosphere, where convective motions are recorded during the for-2 mation of lattice-preferred orientation (LPO) fabrics under dislocation creep [e.g. Nico-3 las and Christensen, 1987; Silver, 1996; Long and Becker, 2010]. However, within the continental lithosphere, seismically mapped anisotropy appears complex [e.g. Fouch 5 and Rondenay, 2006. Transitions between geologically-recent deformation and frozen-6 in anisotropy from older tectonic motions are reflected in layering [e.g. *Plomerová et al.*, 7 2002; Yuan and Romanowicz, 2010] and the stochastic character of azimuthal anisotropy 8 in geological domains of different age [Becker et al., 2007a; Wüstefeld et al., 2009]. Regional studies indicate intriguing variations of azimuthal anisotropy with depth, which may 10 reflect decoupling of deformation, or successive deformation episodes recorded at different 11 depths [e.g. Savage and Silver, 1993; Pedersen et al., 2006; Marone and Romanowicz, 12 2007; Deschamps et al., 2008a; Lin et al., 2011; Endrun et al., 2011]. All of these observa-13 tions hold the promise of yielding a better understanding of the long-term behavior of a 14 rheologically complex lithosphere, including changes in plate motions and the formation 15 of the continents. 16

Ideally, one would like to have a complete, three-dimensional (3-D) model of the full (21 independent components) elasticity tensor for such structural seismology studies. Fully anisotropic inversions are feasible, in principle [cf. *Montagner and Nataf*, 1988; *Panning and Nolet*, 2008; *Chevrot and Monteiller*, 2009], particularly if mineral physics and petrological information are used to reduce the dimensionality of the model parameter

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<sup>22</sup> space [Montagner and Anderson, 1989; Becker et al., 2006a]. However, often the sparsity <sup>23</sup> of data requires, or simplicity and convenience demand, restricting the analysis to joint <sup>24</sup> models that constrain only aspects of seismic anisotropy, for example the azimuthal kind, <sup>25</sup> on which we focus here.

For azimuthal anisotropy, hexagonal crystal symmetry is assumed with symmetry axis 26 in the horizontal plane yielding a fast,  $v_{SV1}$ , and a slow,  $v_{SV2}$ , propagation direction for 27 vertically polarized shear waves. Surface (Rayleigh) wave observations can constrain the 28 anisotropic velocity anomaly,  $G/L = (v_{SV1} - v_{SV2})/v_{SV}$ , and the fast,  $\Psi$ , orientation for 29 shear wave propagation. Here, G and L are the relevant elastic constants and  $v_{SV}$  the 30 mean velocity, as defined in *Montagner et al.* [2000]. Given the dispersive nature of surface 31 waves, phase velocity observations from different periods can be used to construct 3-D 32 tomographic models for G/L and  $\Psi$ . Particularly in regions of poor coverage, tomographic 33 models can be affected by the trade-off between isotropic and anisotropic heterogeneity 34 Tanimoto and Anderson, 1985; Laske and Masters, 1998, which typically limits e.g. 35 the lateral resolution to many hundreds of km in global models [e.g. Nataf et al., 1984; 36 Montagner and Tanimoto, 1991; Debayle et al., 2005; Lebedev and van der Hilst, 2008]. 37

<sup>38</sup> This approach can then be contrasted with observations of shear wave splitting [e.g. <sup>39</sup> Ando et al., 1983; Vinnik et al., 1984; Silver and Chan, 1988], typically from teleseismic <sup>40</sup> SKS arrivals. A split shear wave is direct evidence for the existence of anisotropy. In its <sup>41</sup> simplest form, a splitting measurement provides information on the azimuthal alignment <sup>42</sup> of the symmetry axis,  $\phi$ , of a single, hexagonally anisotropic layer and the delay time <sup>43</sup> that the wave has accumulated between the arrival of the fast and the slow split S-wave <sup>44</sup> pulse,  $\delta t$ . With Fresnel zone widths of ~100 km, splitting measurements have relatively <sup>45</sup> good lateral, but poor depth resolution, suggesting that body and surface-wave based <sup>46</sup> anisotropy models provide complementary information (Figure 1).

An initial global comparison between different azimuthal anisotropy representations was 47 presented by Montagner et al. [2000] who compared the SKS splitting compilation of Silver [1996] with the predicted anisotropy,  $\phi'$  and  $\delta t'$ , based on tomography by Montagner 49 and Tanimoto [1991]. Montagner et al. found a poor global match with a bi-modal coher-50 ence,  $C(\alpha)$ , as defined by Griot et al. [1998], which suggested typical angular deviations, 51  $\alpha$ , between  $\phi$  from SKS and  $\phi'$  based on integration of  $\Psi$  and G/L from tomography of 52  $\alpha \sim \pm 40^{\circ}$ , where  $\alpha = \phi' - \phi$ . An updated study was conducted by Wüstefeld et al. [2009] 53 who used their own, greatly expanded compilation of SKS splitting results and compared 54 the coherence of azimuthal anisotropy with the predicted  $\phi'$  obtained from the model of 55 Debayle et al. [2005] on global and regional scales. Wüstefeld et al. conclude that the 56 global correlation between the two representations of anisotropy was in fact "substantial". 57 This improved match, with a more pleasing, single peak of C at zero lag,  $\alpha = 0$ , was at-58 tributed to improved surface-wave model resolution and better global coverage by SKS59 studies. Wüstefeld et al. [2009] also explore a range of ways to represent  $\phi$  from SKS. 60 Their best global coherence values were, however,  $C(0) \approx 0.2$ , which is only ~ 1.7 times 61 the randomly expected coherence at equivalent spatial representation. While no corre-62 lation values were provided, a scatter plot of actual  $\delta t$  and  $\delta t'$  from integration of G/L63 [Figure 9 of Wüstefeld et al., 2009] also shows little correlation of anisotropy strength. 64

One concern with any studies that perform a joint interpretation of splitting and anisotropy tomography is that the shear wave splitting measurement does not represent a simple average of the azimuthal anisotropy along the raypath [e.g. *Rümpker et al.*,

1999; Saltzer et al., 2000; Silver and Long, 2011]. Typically, the method proposed by 68 Montagner et al. [2000] for the case of small anisotropy and long period waves is used to 69 compute predicted splitting from tomographic models [e.g. Wüstefeld et al., 2009], and 70 this basically represents a vectorial averaging, weighing all layers evenly along the ray 71 path. In continental regions, fast orientations of azimuthal anisotropy and amplitudes 72 may vary greatly with depth over the top  $\sim 400$  km of the upper mantle. We therefore 73 expect significant deviations from simple averaging [Saltzer et al., 2000] and, moreover, 74 a dependence of both predicted delay time and fast azimuths of the splitting measure-75 ment on back-azimuth of the shear wave arrival [e.g. Silver and Savage, 1994; Rümpker 76 and Silver, 1998; Schulte-Pelkum and Blackman, 2003]. It is therefore important to test 77 the assumptions inherent in the *Montagner et al.* [2000] averaging approach, both to un-78 derstand the global coherence between body and surface-wave based models of seismic 79 anisotropy, and to verify that regional, perhaps depth-dependent, deviations between the 80

Here, we analyze two recent tomographic models of global azimuthal anisotropy and 82 show what kinds of variations in splitting measurements can be expected based on a 83 more complete treatment of predicted shear wave splitting that incorporates appropriate 84 depth-integration. We show that, overall, the simplified predictions are suitable, but 85 local variations between methods can be significant. We also reassess the match between 86 predicted and actual splitting and show that smoother representations of Earth structure 87 appear to match long-wavelength averaged splitting quite well, albeit at much reduced 88 amplitudes. 89

two are not partially an artifact of methodological simplifications.

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# 2. Splitting estimation methods

Our goal is to estimate the predicted shear wave splitting from a tomographic model 90 of seismic anisotropy in the Earth. In theory, this requires a 3-D representation of the 91 full elasticity tensor along the raypath of whichever shear wave is considered, for SKS92 from the core mantle boundary to the surface. In practice, we focus on the uppermost 93 mantle where most mantle anisotropy is focused [e.g. *Panning and Romanowicz*, 2006; 94 Kustowski et al., 2008], as expected given the formation of LPO under dislocation creep 95 [Karato, 1992; Becker et al., 2008; Behn et al., 2009]. We will also not consider lateral 96 variations of anisotropy on scales smaller than the Fresnel zone. This would require fully 97 three-dimensional wave propagation methods [e.g. Chevrot et al., 2004; Levin et al., 2007], 98 but is not warranted given the resolution afforded by tomographic models. 99

<sup>100</sup> The computation of shear wave splitting parameters from actual seismograms involves <sup>101</sup> estimating the fast "axes" (i.e. the apparent fast polarization direction) and the delay <sup>102</sup> time, and there are at least three ways of computing the equivalent, predicted  $\phi'$  and  $\delta t'$ <sup>103</sup> parameters from tomography: *Montagner et al.* [2000] averaging of G/L azimuthal anoma-<sup>104</sup> lies, computing splitting using the Christoffel matrix approach for an average tensor, and <sup>105</sup> full waveform synthetic splitting.

# 2.1. Montagner averaging of G/L azimuthal anomalies

In the case of small anisotropy and long period waves (period T > 10 s), the predicted splitting for a tomographic model can be computed as [Montagner et al., 2000]

$$\delta t' = \sqrt{f_c^2 + f_s^2} \quad \text{and} \quad \phi' = \frac{1}{2} \tan^{-1} \left( \frac{f_s}{f_c} \right), \tag{1}$$

where the vector components  $f_{c,s}$  are the depth integrals (assuming a vertical path)

$$f_{c,s} = \int_0^a \sqrt{\frac{\rho}{L}} \frac{G_{c,s}}{L} dz = \int_0^a \frac{1}{v_{SV}} \frac{G_{c,s}}{L} dz,$$
 (2)

*a* is the length of the path,  $v_{SV} = \sqrt{L/\rho}$ ,  $\rho$  density, and *c* and *s* indices indicate the azimuthal cos and sin contributions to anisotropy, as follows: The relevant components of the elasticity tensor that determine the splitting are G/L with  $G = \sqrt{G_c^2 + G_s^2}$ , and the ratios  $G_{c,s}/L$  relate to the typical parameterization of azimuthal-anisotropy tomography models

$$\frac{dv_{SV}}{v_{SV}} \approx A_0 + A_c \cos 2\Psi + A_s \sin 2\Psi \tag{3}$$

as

$$\frac{G_{c,s}}{L} = 2A_{c,s}.\tag{4}$$

Here,  $dv_{SV}$  is total the velocity anomaly with respect to a 1-D reference model,  $A_0$  the 106 isotropic velocity anomaly, and all higher order,  $4\Psi$ , terms are neglected. Assuming 107 vertical incidence and neglecting any effects due to isotropic anomalies  $A_0$ , the predicted 108 splitting at every location can then be approximated by integration of the  $A_{c,s}$  terms over 109 depth, z, as in eq. (2). To check if the assumptions of small anisotropy and long-period 110 filtering might be violated on Earth and in actual SKS measurements, and to estimate 111 the degree of variability of  $\phi'$  and  $\delta t'$  with back-azimuth, we also compute splitting using 112 two more elaborate methods. 113

#### 2.2. Christoffel matrix from averaged tensors

<sup>114</sup> We assume that the "real", anisotropic Earth can be approximated using the infor-<sup>115</sup> mation in the azimuthally-anisotropic surface wave models and convert the  $A_{c,s}$  factors <sup>116</sup> from tomography underneath each location into complete anisotropic tensors, C(z), as a

function of depth. To obtain C(z), we tested several approaches, most simply aligning a 117 best-fit, hexagonal approximation to an olivine-enstatite tensor in the horizontal plane, 118 and then scaling the anisotropy such that the effective, transversely isotropic ("splitting") 119 anomaly in the horizontal plane,  $\delta_{TI}^h$ , corresponds to  $2A_{c,s} = G/L$  from tomography at 120 that depth [using the decomposition of Browaeys and Chevrot, 2004]. We also consider 121 an identically aligned, but fully anisotropic, depth-dependent olivine-enstatite tensor [as 122 used in *Becker et al.*, 2006a], again scaled such that  $\delta_{TI}^h = 2A_{c,s}$ , which adds orthorhombic 123 symmetry components. Lastly, to explore the effect of dipping symmetry axes, we scaled 124 down the full, hexagonally approximated olivine-enstatite tensor anisotropy by a factor 125 of four to  $\delta_{TI}^{o}$ , and then aligned the tensor at a dip angle of  $\beta$  out of the horizontal plane 126 such that  $\cos(\beta)\delta_{TI}^o = \delta_{TI}^h = 2A_{c,s}$  matched the azimuthal anisotropy from tomography, 127 rescaling in an iterative step, if needed. The latter two approaches (non-hexagonal or dip-128 ping symmetry) are expected to yield a more complex splitting signal with back-azimuthal 129 variations [e.g. Schulte-Pelkum and Blackman, 2003; Browaeys and Chevrot, 2004]. 130

From this anisotropic model where, for each location under consideration, we have esti-131 mates of C(z) at each layer, we first compute a depth-averaged tensor  $\hat{C}$ , using arithmetic, 132 i.e. Voigt, averaging. From this average tensor, we then compute splitting as a function 133 of incidence and back-azimuth based on the Christoffel equation [e.g. Babuška and Cara, 134 1991] using the implementation of *Schulte-Pelkum and Blackman* [2003]. Differently from 135 the Montagner et al. [2000] averaging, this method not only yields  $\phi'$  and  $\delta t'$ , but also 136 simplified estimates of the variations of both parameters as a function of back-azimuth, 137  $\sigma_{\phi}$  and  $\sigma_{\delta t}$ . When computing back-azimuthal variations, we fix the incidence angle to 5°, 138 as a typical value for SKS. When averaging C(z) for the Christoffel approach, we use 139

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<sup>140</sup> constant weights for each layer, even though we expect surface-near regions to contribute <sup>141</sup> more strongly in reality [e.g. *Rümpker et al.*, 1999; *Saltzer et al.*, 2000], because such wave <sup>142</sup> propagation effects can be captured more fully by the method that is discussed next.

# 2.3. Full waveform, synthetic splitting

Lastly, we also follow the approach suggested by Hall et al. [2000] to obtain splitting 143 from geodynamic predictions of anisotropy, accounting for the full waveform complexities 144 given the depth-dependent C(z) model we can construct at each location using the method 145 described above. Following *Becker et al.* [2006b], we first use a layer matrix computation 146 that accounts for the depth-dependence of anisotropy by assigning a constant tensor for 147 each layer that the ray path crosses. This method assumes that lateral variations in 148 material properties are small on the wavelengths of a Fresnel zone. Our waveform modeling 149 approach is based on *Kennett* [1983], with extensions by *Booth and Crampin* [1985] and 150 Chapman and Shearer [1989], and yields a pulse train. This is then bandpass-filtered to 151 construct synthetic seismograms in SKS-typical bands of  $T \approx 7$  s center period. We 152 use mainly the cross-correlation method [e.g. Fukao, 1984; Bowman and Ando, 1987], 153 implemented following Levin et al. [1999], to automatically measure splitting from modeled 154 waveforms, scanning through the full back-azimuth of the incoming SKS waves. We 155 discard nulls and poor measurements and report both the mean ("best") and standard 156 deviations ( $\sigma_{\phi}$  and  $\sigma_{\delta t}$ ) of the inferred  $\delta t'$  and  $\phi'$  [see *Becker et al.*, 2006b, for details]. 157

The cross-correlation method is equivalent to the transverse-component minimization method [Silver and Chan, 1988] for a single horizontal layer in the absence of noise. However, cross-correlation should perform better in the case of multiple layers of anisotropy [Levin et al., 1999; Long and van der Hilst, 2005] as is the case for some locales where  $\Psi$ 

rotates quite widely with depth (Figure 2). While detailed results of the splitting measure-162 ment depend on analysis choices such as filtering, windowing, and measurement method, 163 general results are usually consistent [e.g. Long and van der Hilst, 2005; Wüstefeld and 164 Bokelmann, 2007]. However, to test this assumption in the framework of our automated 165 splitting setup, we also present some cases where splits were computed using the cross-166 convolution routine ah\_cross\_conv\_1 of Menke and Levin [2003], which has a slightly 167 different optimization strategy from our implementation of Levin et al. [1999] (all soft-168 ware and data used here are provided at http://geodynamics.usc.edu/ $\sim$ becker). More 169 importantly, we also experiment with the waveform filtering, allowing for longer periods 170 of  $T \approx 12.5$  s and  $T \approx 15$  s to test how the approximation of *Montagner et al.* [2000] is 171 affected. 172

#### 3. Azimuthal anisotropy observations and models

### 3.1. Shear wave splitting database

We maintain our own compilation of shear wave splitting measurements, mainly based 173 on the efforts by Silver [1996] and Fouch [2006], but subsequently updated by addition of 174 regional studies, and now holding 9635 entries. For this study, our database was merged 175 with that of *Wüstefeld et al.* [2009] which had 4778 entries as of May 2011, yielding a 176 total of 14,326 splits. Our compilation includes measurements carried out by many differ-177 ent authors, and individual studies differ in the measurement methods used, processing 178 choices such as event selection, filtering, windowing, and back-azimuthal coverage. Given 179 such methodological concerns and the possibly large back-azimuth variation of splitting 180 parameters if anisotropy is complex underneath a single station, it would be desirable to 181 have a consistent measurement and waveform filtering strategy, and to take into account 182

back-azimuth information. However, we only have event and method information for a 183 small subset of the splits which is why we discard this information subsequently. If we 184 station-average the splits (using an arithmetic, vectorial mean of all non-null splits, taking 185 the 180° periodicity of  $\phi$  into account), we are left with 5159 mean splitting values on 186 which we base our analysis (Figure 1). Such averaging is expected to also reduce the effect 187 of some of the inconsistencies of the splitting database, for example the mix between al-188 ready station-averaged and individual splits reported. (An electronic version of this SKS) 189 compilation can be found at http://geodynamics.usc.edu/ $\sim$ becker/.) 190

We will consider both this complete station-averaged data set and spatially averaged 191 versions of it. Several averaging and interpolation approaches for shear wave splitting 192 data have been discussed [e.g. Wüstefeld et al., 2009]. Here, we use one global basis-193 function approach and a simple averaging scheme that does not make any assumptions 194 about the statistical properties of the data. For a global, smoothed representation we use 195 generalized spherical harmonics as implemented by Boschi and Woodhouse [2006]. For 196 consistency with the tomographic models (see below), we use a maximum degree L = 20197 (individual degree  $\ell \in [2; L]$  for a  $2\Psi$  type of signal) and perform a least-squares fit to the 198 station-averaged splits (Appendix A). Such global representations assume that the field 199 represented by the splits is smooth (which it is not, but it may be seen as such by the 200 tomographic models), and will extrapolate into regions without data. 201

We therefore also use a simple, bin-averaged representation of  $\gamma$  resolution (say,  $\gamma = 5^{\circ}$ ). We compute the mean  $\delta t$  and  $\phi$  for all data within  $\gamma$  distance from the binning sites which are spaced  $\gamma$  in latitude,  $\lambda$ , ( $\lambda \in (-\pi, \pi)$ ) and with  $\gamma/\cos(\lambda)$  in longitude. The results X - 14

<sup>205</sup> of the damped, spherical harmonics representation and the bin-averaged splitting are <sup>206</sup> generally consistent in areas of good data coverage (compare Figures 1 and 2).

The regional characteristics of splitting have been discussed, for example, by Vinnik 207 et al. [1992], Silver [1996] and Wüstefeld et al. [2009], so we will not go into much detail. 208 However, we note that even updated SKS compilations remain strongly biased toward 209 continental, and particularly tectonically active, regions such as the western United States 210 (Figures 1 and 3). Figure 3a shows how the data and delay times are distributed in terms 211 of the GTR-1 tectonic regionalization [Jordan, 1981]. The regional bias is seen in the 212 prominence of the orogenic zones ( $\sim 75\%$  of the data) which include regions such as the 213 western US, and hence also dominate the global statistics. If we partially correct for the 214 data bias and consider the 5° averaged splitting (Figure 3b), there is almost no difference 215 in the mean delay times within continental regions ( $\langle \delta t \rangle_{\rm cont} \approx 0.77$  s), but some indication 216 of larger splitting underneath oceanic basins ( $\langle \delta t \rangle_{\rm ocean} \approx 0.96$  s), compared to the global 217 mean  $\langle \delta t \rangle \approx 0.84$  s. Even though  $\delta t$  distributions are typically (and necessarily) positively 218 skewed, differences between median and mean are relatively small (Figures 3a and b; also 219 see Figure 7a). Assuming normal distributions and independent sample values, the finding 220 of larger  $\langle \delta t \rangle$  in oceans compared to continents for Figures 3a and b can then be inferred 221 to be more than 97.5% and 99.9% significant, respectively, using Welch's *t*-test. 222

# 3.2. Comparison of tomographic models

<sup>223</sup> We contrast the *SKS* splits with the two most recent, global azimuthal anisotropy <sup>224</sup> models available to us, DKP2005 by *Debayle et al.* [2005] and LH08 by *Lebedev and* <sup>225</sup> van der Hilst [2008], from both of which we only use the  $2\Psi$  terms (Figure 2). Both <sup>226</sup> models use fundamental mode Rayleigh waves and overtones to constrain upper mantle SV structure, but their datasets, theoretical assumptions, and inversion choices, such as on regularization and parameterization, are quite different and have been discussed elsewhere [Debayle et al., 2005; Becker et al., 2007b; Lebedev and van der Hilst, 2008]. We here simply treat them as two alternative representations of the "true", 3-D anisotropic structure of the Earth, realizing that tomography represents regionally variably resolved, smoothed approximations of the actual structure.

For quantitative comparison purposes, we express both models in generalized spherical 233 harmonics [see *Becker et al.*, 2007b], and Figures 4a and b show heterogeneity spectra 234 at three layers in the upper mantle. The anisotropic heterogeneity amplitude decreases 235 strongly from 50 to 350 km depth for both models. However, DKP2005 shows a much 236 flatter decrease in power per spherical harmonic degree,  $\ell$ , than LH08, meaning that the 237 azimuthal anisotropy structure is more heterogeneous, even at the relatively smaller, re-238 gional scales. Such differences in the power spectra of tomography are expected given 239 different inversion choices, but they are more pronounced for anisotropic than for isotrop-240 ic models given the required additional choices as to how to regularize the inversions 241 [Becker et al., 2007b]. DKP2005's power continues to decrease roughly monotonically as 242 in Figure 4b down to  $10^{-4}$  at  $\ell \sim 30$ , but we will focus on relatively long-wavelength, 243 maximum degree L = 20 because LH08 has little meaningful power beyond that point. 244 Figure 4c shows the linear correlation per degree between DKP2005 and LH08 azimuthal 245 anisotropy (taking both azimuth and amplitude of  $2\Psi$  anomalies into account); it is sta-246 tistically significant at the 95% level for most  $\ell$ , but only above ~ 200 km depth. 247

Figure 5 shows how the tomographic models represent azimuthal anisotropy with depth; both display a concentration of anisotropy at  $\sim 100$  km (note range of depths where both

models are defined in Figure 5a), with DKP2005 having larger amplitudes of up to an 250 RMS,  $(v_{SV1} - v_{SV2})/v_{SV}$ , anomaly of 1.2%. To see how much radial change in structure 251 is mapped by these models, Figure 5b shows the total correlation up to  $\ell = 20, r_{20},$ 252 between two layers at  $z_{1,2} = z \pm 100$  km for the layer at z under consideration. DKP2005 253 has large change in structure at ~ 200 km depth [Debayle et al., 2005] whereas LH08 254 is also vertically very smooth (cf. Figure 2), presumably at this point mainly reflecting 255 choices as to the effective radial smoothing of the tomographic inversions. The overall 256 match between the models as a function of depth is shown in Figure 5c; it peaks at total 257 correlation values of  $r_{20} \sim 0.5$  at  $\sim 100$  km depth but falls below 95% significance at 258  $\sim 300$  km. 259

These differences in spectral character and the relatively poor match between models 260 reflect current challenges in finding consistent, anisotropic tomography models for the 261 upper mantle and the importance of regularization choices which differ between authors 262 [cf. Becker et al., 2007b, 2008]. To provide another point of comparison, we also compute 263 the correlation of azimuthal anisotropy from each surface wave model with the geody-264 namic flow modeling approach that was optimized by *Becker et al.* [2008] regarding its 265 match to entirely different, radial anisotropy tomography by Kustowski et al. [2008]. The 266 correlation with the geodynamic prediction peaks at  $\sim 0.3$  for DKP2005, and  $\sim 0.5$  for 267 LH08. The match between azimuthal anisotropy from LH08 and the geodynamic model 268 is thus overall better than the match between the seismological models, confirming that 269 the anisotropy inferred from mantle flow estimates provides a meaningful reference for 270 geodynamic interpretation [Long and Becker, 2010]. 271

# 4. Results

We proceed to describe the results from different predicted splitting methods, and when 272 predicted splitting is compared to actual data. If splitting is to be estimated at a certain 273 location, as in the case for the comparison with actual splitting observations, we interpo-274 late the original  $A_{c,s}$  values from the tomographic models to that location, assembling a 275 vertical, upper mantle stack of  $\mathsf{C}(z)$  tensors, and then compute  $\phi'$  and  $\delta t'$ . Alternatively, 276 if global estimates of statistical properties are required, we construct roughly  $2^{\circ} \times 2^{\circ}$  grid-277 ded representations of  $\phi'$  and  $\delta t'$  on regularly spaced sites on the surface of the globe, and 278 extract information from these. Given the smooth nature of LH08, the site-specific values 279 for predicted splitting are very similar to those that can be interpolated from the global 280 representations for LH08. However, as noted by Wüstefeld et al. [2009], the relatively more 281 heterogeneous model DKP2005 requires a finer representation. We therefore use global 282 representations for inter-tomography model comparisons, and geographic site-specific in-283 terpolations directly from  $A_{c,s}$  of tomography for comparisons with actual splits. We limit 284 all of our geographic analysis to polar-distant latitudes of  $\lambda \in [-80^\circ; 80^\circ]$  to ensure that 285 the uncertainty due to the smoothing of the anisotropy terms  $A_{c,s}$  in LH08 is not affecting 286 our analysis. 287

#### 4.1. Shear wave splitting from tomographic models

We now consider the global statistical deviations between different methods of estimating predicted splitting from tomographic models of azimuthal anisotropy. We first use the  $A_{c,s}$  terms of eq. (3) within the depth region in which both LH08 and DKP2005 are defined, from 75 to 410 km. We interpolate the original layers to a consistent, 25 km spaced representation and then compare results from *Montagner et al.* [2000] averaging with <sup>293</sup> the Christoffel matrix from averaged tensors, and the full wave-form, synthetic splitting <sup>294</sup> approach described above.

Figure 6 compares results obtained for predicted splitting using a vertically assembled, 295 C(z) models based on a horizontally aligned, hexagonal tensor oriented and scaled based 296 on  $A_{c,s}(z)$  terms, when expressed in generalized spherical harmonics up to L = 20. The 297 Christoffel matrix approach for a depth-averaged tensor leads to similar predictions to 298 the Montagner et al. [2000] average, particularly at the longest wavelengths, but back-299 azimuth variations due to effectively dipping symmetry axis lead to slight deviations at 300 shorter scales ( $r_{20} \approx 1.00$  and 0.99 for LH08 and DKP2005, respectively). The full wave-301 form results are broadly consistent with the simple averaging, but total correlations are 302 decreased to  $r_{20} \approx 0.90$  and 0.78 for the two models, respectively. Using the Christoffel 303 approach gives a slightly better match to full waveform splitting,  $r_{20} \approx 0.91$  and 0.82, 304 respectively. The relative agreement between methods is thus better for LH08 than for 305 DKP2005, which is expected given the more heterogeneous representation of Earth struc-306 ture of the latter model (Figures 2, 4, and 5). 307

The regional patterns of mismatch are strongly model-dependent and show no clear geographic association besides an indication for larger angular deviations,  $\Delta \alpha = \phi - \phi'$ , for the  $\phi/\phi'$  "axes" within continents, and under-predicted  $\delta t$  in young, spreadingcenter proximal regions when comparing *Montagner et al.* [2000] averages to full waveform splitting.

Expressed in perhaps more intuitive terms, the absolute angular mismatch,  $|\Delta \alpha|$  $(|\Delta \alpha| \in [0, 90^{\circ}])$ , between *Montagner et al.* [2000] averaging and the full waveform, synthetic splitting method are  $15 \pm 15^{\circ}$  and  $21 \pm 18^{\circ}$  for LH08 and DKP2005, respectively,

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with global mean  $\pm$  standard deviation indicated. These values reflect large spatial vari-316 ability in the mismatch, and the means are comparable to, and perhaps a bit larger than, 317 typical splitting measurement uncertainties in  $\phi$ ,  $\Delta \phi$  (median uncertainty is  $\Delta \phi = 15^{\circ}$ 318 in our compilation). The average and standard deviation of the delay time differences 319 are  $-0.05 \pm 0.08$  s and  $-0.07 \pm 0.13$  s for LH08 and DKP2005, respectively. The spatial 320 variability of the  $\delta t$  mismatch is therefore ~ 0.1 s, smaller than the typical delay time un-321 certainty of splits (median uncertainty 0.2 s in our compilation). Delay times themselves 322 from the Montagner et al. [2000] method and full waveform splits are correlated at the 0.94 323 and 0.82 level for LH08 and DKP2005, respectively, based on L = 20 expansions. (We 324 only quote linear, Pearson correlation coefficients here, but Spearman rank-order values 325 [see, e.g. Press et al., 1993, p. 636 and 640 for definitions] are generally very similar.) 326 Table 1 shows correlations and linear regression parameters between different, full wave-327 form, synthetic splitting methods and the *Montagner et al.* averaging. Results are broadly 328

independent of detailed choices of how anisotropy is represented, or how the measurement 329 is made on the waveforms. If longer period filtering is applied (making the measurement 330 more consistent with the assumptions inherent in *Montagner et al.* [2000]), correlations 331 are almost unchanged, but delay times increase. With moderate filtering between 7 and 332  $\sim 12$  s periods, the waveform methods predict between  $\sim 10$  and  $\sim 40\%$  larger delay times 333 than Montagner et al. averaging when the depth region between 75 and 410 km is consid-334 ered. The largest changes in correlation in Table 1 are seen when anisotropy is restricted 335 to the, perhaps best-constrained, depth regions between 25 and 250 km. In this case, 336 correlations are improved (and delay times relatively under-predicted by the waveform

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<sup>338</sup> methods). We will explore the depth dependence in a comparison with actual splitting <sup>339</sup> below.

With the caveat that tomography provides a lower bound for the degree of heterogeneity 340 in the Earth, the simplified method of relating tomography to shear wave splitting is 341 therefore generally valid, even if the assumptions inherent in the derivation of *Montagner* 342 et al. [2000] are not strictly fulfilled by actual splitting measurements [e.g. Silver and Long, 343 2011]. Typical differences in regional delay times are comparable to common uncertainties 344 in the individual measurement, and a bit larger for the more heterogeneous tomography 345 of *Debayle et al.* [2005]. This implies that the full waveform, synthetic splitting approach 346 might still be required for reliable estimates in settings with higher complexity. 347

# <sup>348</sup> 4.1.1. Regional variations of splitting complexity

An advantage of the full waveform method of predicting splitting is that the back-349 azimuthal variations of  $\phi$  and  $\delta t$  can, at least in theory, be used as additional information 350 [cf. Becker et al., 2006b]. For simplicity, we measure the back-azimuthal dependency of 351 variations in splitting by the standard deviation of  $\phi$  and  $\delta t$  when splits are computed for 352 all possible back-azimuths, here from 0° to 360° in steps of 2°, and call those "complexities" 353  $\sigma_{\phi}$  and  $\sigma_{\delta t}$ . The global mean values and standard deviations are  $\langle \sigma_{\phi} \rangle \sim 16 \pm 7^{\circ}$  and 354  $\langle \sigma_{\delta t} \rangle \sim 0.17 \pm 0.1$  s for both LH08 and DKP2005 (median values are close to the mean), 355 using the 75 to 410 km depth range for reference. The maximum complexities are  $\sigma_{\phi} \sim 50^{\circ}$ 356 and  $\sigma_{\delta t} \sim 1$  s, respectively, indicating that, regionally, such back-azimuth effects might 357 be important when comparing synthetics and real splitting. 358

<sup>359</sup> If we map this splitting complexity based on the full waveform splits for the two tomo-<sup>360</sup> graphic models considered, the regional variations are, again, not clearly associated with any tectonic or geographic features, and look quite different for the two tomographic models. One exception is  $\sigma_{\delta t}$  for LH08 which is larger (~ 0.2 s) for (young) oceanic regions, compared to continental regions (~ 0.11 s). No such relationship exists for synthetics from DKP2005.

Given that we expect splitting complexity, and the deviations between full waveform 365 splitting and *Montagner et al.* [2000] averaging, to be affected by local, depth-variable 366 anisotropy effects such as rotation of  $\Psi$  [e.g. Saltzer et al., 2000], it would be desirable 367 to have a simple metric to decide if full waveform treatments are needed. However, on a 368 global scale, we could not easily find such a metric. We tested the total, absolute rotation 369 of  $\Psi$  with depth, as well as a similar measure that scaled angular difference with depth 370 by the anisotropy strength for the particular layers. Only the latter measure showed 371 some predictive power, but global correlations with  $\sigma_{\delta t}$  and  $\sigma_{\phi}$  were low, of order 0.2 372 for DKP2005, and 0.45 for  $\sigma_{\phi}$  and 0.13 for  $\sigma_{\delta t}$  for LH08. If we restrict ourselves to the 373 perhaps better constrained depth regions of the tomographic models from 25 to 250 km, 374 the correlations between the scaled measure of rotation and splitting complexity are still 375 only  $\sim 0.3$  for DKP2500 and LH08. This somewhat surprising result implies that the non-376 linearity of the splitting measurement may not lend itself well to simplified estimates of 377 splitting complexity. 378

#### 4.2. Match between actual and predicted splitting

# <sup>379</sup> 4.2.1. Delay times

Figure 7 compares the delay times evaluated at the station-averaged splitting database (with globally uneven distribution as in Figures 1 and 3a) with those predicted from the two tomographic models using the simplified and full waveform approach. (The DKP2005

predictions from Figure 7b replicate Wüstefeld et al.'s [2009] results for a slightly different 383 database; they are consistent.) As expected from the analysis above, the two predicted 38 splitting methods in Figures 7b and c give broadly consistent answers. Based on the 385 reference depth-range of 75 to 410 km, median delay time predictions are  $\sim 50\%$  of the 386 original splits for DKP2005 and  $\sim 30\%$  for LH08, respectively. This reflects the differences 387 in the azimuthal anisotropy power in the two tomographic models (e.g. Figure 4), and 388 the general tendency of global tomographic models to under-predict actual amplitudes 389 given the necessary regularization choices. 390

In particular, predicted delay times are shifted toward zero ( $\sim 0.4$  s) (Figure 7c) com-391 pared to the actual splits which cluster at  $\sim 1.1$  s (Figure 7a). This shift is due to a 392 reduction in anomaly amplitudes because of the strong lateral and moderate vertical av-393 eraging (roughness damping, as in LH08, for example). In some tomographic inversions, 394 norm damping may also contribute, where the assumption is that of a Gaussian distri-395 bution of anisotropic anomalies around a zero mean. This may not be appropriate for 396 a description of seismic anisotropy in the upper mantle. Resulting amplitude differences 397 between predicted and actual splitting are less pronounced for regional comparisons of 398 azimuthal anisotropy models [e.g. Deschamps et al., 2008b]. 399

Figures 3c and d show the predicted splitting evaluated on the 5° bin-averaged splitting locations for LH08 and DKP2005, respectively, sorted into tectonic regions to test for geographic variations of typical delay times. The slight trend of larger average delay times for oceanic vs. continental regions as seen in actual splitting (Figure 3b) is stronger in predicted splitting for both models [as noted by *Wüstefeld et al.*, 2009, for DKP2005], and  $\delta t'$  is particularly large for the youngest oceanic lithosphere for LH08 (Figure 3c) and for orogenic zones in DKP2005 (Figure 3d).

#### 407 4.2.2. Fast polarization match

If we consider the spherical harmonics representation of our splitting database, the total 408 correlation with the predicted splits (using both  $\phi$  and  $\delta t$  information, as expressed by  $A_{c,s}$ 409 factors, see appendix A) computed for the full waveform method for LH08 and DKP2005 410 are  $r_{20} \sim 0.35$  and  $r_{20} \sim 0.25$ , respectively. However, when correlations are computed 411 per degree (as for the model comparison in Figure 4c), only the very longest wavelength 412 terms are above 95% statistical significance ( $\ell = 2$  for DKP2005,  $\ell = 2, 3$  for LH08). This 413 implies that, globally, the match between predicted splitting from tomography and actual 414 splits might only be recovered when the longest wavelengths are considered (cf. Figures 1 415 and 2). 416

Figure 2 compares the  $2\Psi$  fast propagation direction of the tomographic models, the 417 predicted splitting and variability, from the full waveform method, and the actual split-418 ting in the  $5^{\circ}$  degree averaged representation on global maps. These plots highlight the 419 differences in the tomographic models (cf. Figures 4 and 5) with resulting variations both 420 in the predicted splitting, and the back-azimuth variations thereof. From visual inspec-421 tion (Figure 2), it is apparent that the actual SKS splits are matched in some regions, 422 but not in others [cf. Montagner et al., 2000; Wüstefeld et al., 2009], and that there are 423 systematic, large-scale deviations in angle for LH08. 424

Table 2 lists the median and standard deviations of the absolute, angular misfit between full waveform, synthetic splitting and the station-averaged and 5° averaged representation of actual splits, when computed for different depth ranges and different tomographic

models. LH08 leads to overall slightly better predictions of the measured SKS splitting, 428 with typical values  $|\Delta \alpha| \sim 33^\circ$  compared to  $|\Delta \alpha| \sim 38^\circ$  for DKP2005. These misfits 429 are significantly smaller than the expected random value,  $|\Delta \alpha|_r = 45^\circ$ . There is a large 430 degree of spatial variability in the mismatch, as seen in the standard deviations for  $|\Delta \alpha|$ 431 which are  $\sim 25^{\circ}$ . Moreover, splitting predictions are somewhat improved in their match 432 to tomography if the crustal layers above 75 km are taken into account for LH08, or if 433 the integration is restricted to regions above 250 km (Table 2). This indicates that the 434 shallower layers of LH08 may be better constrained, and that crustal anisotropy in LH08 435 is reflected in the splitting signal. Any such trends with depth, if they exist, are less clear 436 for DKP2005. 437

Table 3 shows some of the regional and methodological variations of the mismatch between predicted and actual splitting and the 5° averaged splits (to partially account for the spatial bias inherent in the global splitting dataset, cf. Figures 1-3). We only use the well-constrained 25 to 250 km depth regions of LH08 for illustration where trends appear clearest. Comparing the global angular misfits, predictions are generally improved for full waveform estimates compared to the simplified, *Montagner et al.* [2000] averaging, but only marginally so.

# 445 4.2.3. Back-azimuth variations

Some of the mismatch between predicted and actual splitting (which is here based on station-averages of individual splits) might arise because of variations in apparent splitting with back-azimuth. We can account for this in an idealized fashion if we take the variability information afforded by the waveform method into account. We use the minimum  $|\Delta \alpha|$  that can be achieved by allowing  $\phi'$  for each site to vary within the range

 $\phi' \pm \sigma_{\phi}$ . The global, median misfit can then be reduced to 19° for the full waveform splits. This optimistic scenario  $|\Delta \alpha|$  is about as good as these comparisons get; 19° angular misfit is comparable or somewhat larger than the best match between geodynamic models and shear wave splitting [e.g. *Becker et al.*, 2006a; *Conrad and Behn*, 2010], and better than the match of geodynamic models to surface wave azimuthal anisotropy [e.g. *Gaboret et al.*, 2003; *Becker et al.*, 2003].

Uneven back-azimuthal coverage may also bias station-averaged splitting parameter 457 estimates in a general way. In the absence of back-azimuth information for most of 458 the splits in the database, we computed global maps of the theoretical back-azimuth 459 coverage that might be expected given natural seismicity and the location where a splitting 460 measurement is made [*Chevrot*, 2000]. Such maps can be constructed, for example, by 461 selecting, for each locale, the events within the SKS splitting typical distance-range from 462 90° to 145° with magnitude larger than 5.8 from the Engdahl et al. [1998] catalog between 463 1988 and 1997, as in *Chevrot* [2000]. We then sum these events into  $10^{\circ}$  back-azimuthal 464 angle bins and define completeness, f, by the number of bins with more than five events, 465 divided by the total number of bins. 466

To provide an idea of the spatial variability in, and robustness of, such maps, Figure 8 compares the resulting map for completeness with one where we selected all events in the Harvard/gCMT database [*Ekström et al.*, 2010] up to 2010 for the more restrictive range from 90 to 130° range instead. When broken into four regions of degree of completeness, neither the maps themselves, nor a combination with the back-azimuth variations from predicted splitting, showed robust trends regarding the misfit between predicted and actual splitting. This does not rule out that back-azimuthal variations, perhaps as predicted <sup>474</sup> from full waveform splitting, could be used to quantitatively explore the origin of the <sup>475</sup> misfit between predicted and real splits, but more information about the actual events <sup>476</sup> associated with each split is needed.

We also tested if the character of the tomographic model could be used to predict aver-477 age misfit values. Among the integrated rotation metrics considered above for prediction 478 of mismatch between *Montagner et al.* [2000] averaging and full waveform methods, only 479 the simple integration that did not weigh each layer rotation of  $\Psi$  by anisotropy strength 480 showed some spatial predictive power. Regions of high overall rotation show larger devia-481 tions than those with more coherent anisotropy (Table 3). For the scaled, depth-integrated 482 rotation (which had some, albeit small predictive power for the deviation between simple 483 averaging and waveform splitting), the case is reversed, and the larger integrated rotation 484 sites have a smaller median misfit. If we use the predicted, back-azimuth variability from 485 full waveform splitting,  $\sigma_{\phi}$ , to sort regions of misfit, the median  $|\Delta \alpha|$  is slightly higher in 486 those domains with the highest variability for the full waveform splitting results. (Misfit 487 values for low and high variability are inverted for the optimistic scenario where we allow 488  $\phi' \pm \sigma_{\phi}$  to vary to find the minimum misfit, as expected, because larger  $\sigma_{\phi}$  allows for larger 489 adjustment.) 490

# <sup>491</sup> 4.2.4. Wavelength dependence and smoothing

To evaluate the global relationship between predicted and real splitting further, we compute angular misfits and delay time correlations for different, bin-averaged representations of splitting to ensure we are not biased by the potential artifacts of spatial basis representations. Figure 9 explores different metrics for the match between predicted and actual splits for our simple, bin-averaging representation of the splitting database, for increasing <sup>497</sup> bin-size (or smoothing wavelength). At close-to-original representations of  $\gamma = 1^{\circ}$ , both <sup>498</sup> tomographic models predict median, absolute angular misfits,  $|\Delta \alpha|$ , of ~ 35° (Figure 9a), <sup>499</sup> but only LH08 shows a positive (small) correlation between  $\delta t'$  and  $\delta t$  (Figure 9b). If <sup>500</sup> we increase the averaging  $\gamma$  to ~ 25° at the equator, the median misfits for both LH08 <sup>501</sup> and DKP2005 are reduced, and delay time correlation for LH08 has a (positive) peak. <sup>502</sup> Consistent with the values shown in Table 3, the restriction to the depths between 25 and <sup>503</sup> 250 km (dotted lines) leads to a better match of splitting for both tomographic models.

While we find the delay time difference and angular misfit instructive, one can also consider the coherence function

$$C(\alpha) = \frac{\sum_{i=1}^{M} \sin^2 \Theta_i \, \delta t_i \delta t'_i \exp\left(-\left(\phi_i - \phi'_i + \alpha\right)^2 / (2D_c^2)\right)}{\sum_{i=1}^{M} \sin^2 \Theta_i \, (\delta t_i)^2 \sum_{i=1}^{M} \sin^2 \Theta_i \, (\delta t'_i)^2},\tag{5}$$

due to Griot et al. [1998] and used by Wüstefeld et al. [2009]. Here,  $C(\alpha)$  is expressed as 504 a summation for  $i = 1 \dots M$  of pairs of point data, provided at co-latitudes  $\Theta_i$ , as used 505 in comparing our splitting database (entries  $\phi_i$  and  $\delta t_i$ ) with synthetic splitting ( $\phi'_i$  and 506  $\delta t'_i$  from the tomographic models, and  $D_c$  is a constant correlation factor [cf. Wüstefeld 507 et al., 2009]. The coherence can be used for comparative purposes between studies, and 508  $C(\alpha)$  also allows detection of a systematic bias in orientations. We show the maximum of 509 the coherence,  $C_{max}$ , using  $D_c = 20^{\circ}$  in Figure 9, and the better match for LH08 rather 510 than DKP2005 as seen in the misfit values of Table 3 is reflected in respectively larger 511 maximum coherence. The corresponding  $C_{max}$  values are shown in Figure 9c for different 512 averaging lengths,  $\gamma$ , for the actual shear wave splitting. By comparison of the wavelength 513 dependence of  $C_{max}$ , it is clear that both a drop in mean angular misfit (Figure 9a) and 514 an increase in delay time correlation (Figure 9b) are the cause of the dramatic increase 515 of  $C_{max}$  for LH08 at larger averaging wavelengths. Maximum coherence for DKP2005 516

<sup>517</sup> remains fairly flat, mainly because of the poor correlation of predicted and actual delay <sup>518</sup> times.

Given that the  $C_{max}$  values in Figure 9c may well be found at  $\alpha$  offsets from zero-lag, we 519 show the lag dependence of  $C(\alpha)$  in Figure 10 for selected averaging bin sizes of  $\gamma = 1, 10, 10$ 520 and  $30^{\circ}$ . There is indeed a significant bias in LH08 toward a consistent misalignment of 521  $\alpha \sim -30^{\circ}$  for the shorter averaging lengths. Excluding North American splits from the full 522 database and recomputing  $C(\alpha)$  explains most of this shift toward negative  $\alpha$ , though the 523 culled dataset still leads to  $C_{max}$  at  $\alpha \sim -20^{\circ}$  lag. This highlights the spatially variable 524 character of the match between predicted and actual splitting (Figure 2), which was 525 discussed in a regional  $C(\alpha)$  analysis for DKP2005 by Wüstefeld et al. [2009]. However, 526 once larger averaging  $\gamma$  is applied, coherence is increased for LH08, and  $C_{max}$  is found at 527 roughly zero lag for  $\gamma = 30^{\circ}$  (Figure 10). 528

Eschewing further statistical geographic analysis, but rather considering the match to 529 actual splits when evaluated by geologically distinct regions, the inter-method differences 530 are somewhat larger, and oceanic regions are better predicted than continents (Table 3). 531 Within continents, the geologically young regions are matched better than older ones, 532 with up to 10° difference in median  $|\Delta \alpha|$  between orogenic zones and shields for the 533 full waveform approach. This is consistent with the notion of recent asthenospheric flow 534 leading to a simpler connection between convective anisotropy at depth compared to older 535 domains with complex, frozen-in structure as seen by splitting [cf. Becker et al., 2007a; 536 Wüstefeld et al., 2009]. 537

#### 5. Discussion

It is difficult to estimate the true amplitude and, especially, the scale of expected shear wave splitting heterogeneity from global models of seismic anisotropy. Yet, if the difference in lateral resolution of the two types of data is taken into account and treated quantitatively, the predicted and observed splitting parameters display significant agreement.

We find that the global distribution of azimuthal anisotropy is still represented very 543 differently in the most up-to-date tomographic models. Different data and inversion 544 choices lead to different representations of the Earth, as was discussed earlier by *Becker* 545 et al. [2007b] for Rayleigh wave phase-velocity maps. Generally, global models of seis-546 mic anisotropy are very smooth due to the unevenness of the azimuthal coverage given 547 the available broadband seismic data. In regions that are sampled relatively poorly, only 548 long-wavelength structure can be resolved accurately, which typically necessitates that 549 the entire model is smoothed strongly. Accumulation of seismic data from new stations 550 installed in the last few years, particularly in the oceans, can be expected to result in 551 a stronger agreement between anisotropic tomography models of a new generation, at 552 least at longer wavelengths, as has been seen for models of isotropic global structure [e.g. 553 Becker and Boschi, 2002]. 554

<sup>555</sup> Our results indicate that SKS-splitting delay times are severely under-predicted by both <sup>556</sup> tomographic models considered (too small compared to the actual splits by ~ half). One <sup>557</sup> explanation for this discrepancy is that anisotropy as measured by SKS splitting might <sup>558</sup> be accumulated in deeper mantle regions such as the transition zone [e.g. *Trampert* <sup>559</sup> and van Heijst, 2002], not (well) covered by the upper-mantle tomography models we

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tested here. However, we consider it unlikely that this is a large effect globally *Niu* 560 and Perez, 2004]. In some subduction zones, for example, it has been shown that the 561 uppermost mantle dominates the SKS splitting signal [e.g. Fischer and Wiens, 1996], 562 although some studies have identified a contribution to SK(K)S splitting from lower 563 mantle anisotropy in localized regions [e.g. Niu and Perez, 2004; Wang and Wen, 2007; 564 Long, 2009]. Dominance of uppermost mantle anisotropy for splitting is consistent with 565 the finding that most seismically-mapped azimuthal or radial anisotropy resides in the 566 as the nospheric regions above  $\sim 300$  km, where formation of LPO anisotropy for olivine in 567 the dislocation-creep regime can be quantitatively linked to anisotropy [Podolefsky et al., 568 2004: Becker, 2006: Becker et al., 2008: Behn et al., 2009]. 569

Assuming that the global shear wave splitting data set mainly reflects upper mantle 570 anisotropy, the mismatch between predicted and actual splitting delay time amplitudes 571 may partially be caused by methodological issues specific to the splitting measurements. 572 Monteiller and Chevrot [2010] discuss, for example, how the Silver and Chan [1988] 573 method may lead to a bias toward larger delay times in the presence of noise. Given 574 that this method is widely used, our compilation of splitting observations may thus re-575 flect such a bias compared to the synthetic splits. However, we do not consider such 576 methodological problems to be the main source of the discrepancy, but rather think that 577 the delay time mismatch gives some guidance as to how much azimuthal anisotropy am-578 plitudes might be under-predicted in global tomographic models. Such a reduction in 579 amplitude naturally results from the necessary regularization of inversions for isotropic 580 and anisotropic structure, but also choices as to the representation of Earth structure 581 that might lead to undue smoothing. Smoothness of tomography will also reduce the 582

predicted variations in synthetic splitting fast polarization and delay times as a function of back-azimuth that are seen when adjacent layers have different anisotropy orientations [e.g. *Silver and Savage*, 1994; *Chevrot et al.*, 2004], and such effects may in turn bias actual splitting databases toward larger delay time values.

<sup>587</sup> While computationally expensive, non-linear approaches to seismic anisotropy tomog-<sup>588</sup> raphy may be required to push such analysis further [cf. *Chevrot and Monteiller*, 2009], <sup>589</sup> particularly if regional, high resolution studies provide a more finely resolved represen-<sup>590</sup> tation of Earth structure. However, delay times between predicted and actual splitting <sup>591</sup> show positive correlation for one of the tomographic models, and it is encouraging that <sup>592</sup> the correlation is seen for the smoother (arguably, more conservative) of the models.

<sup>593</sup> The simple averaging approach which we applied to the original splitting dataset to <sup>594</sup> achieve a good match between LH08 and splitting at averaging lengths of  $\gamma \sim 25^{\circ}$  is <sup>595</sup> inconsistent with findings of strong variations of splits on the shortest, Fresnel zone length <sup>596</sup> [e.g. discussion in *Fouch and Rondenay*, 2006; *Chevrot and Monteiller*, 2009]. Yet, it <sup>597</sup> seems to capture the longest wavelength signal represented in the tomographic model. <sup>598</sup> This provides some confidence in the overall consistency of seismic anisotropy mapping <sup>599</sup> efforts at the longest wavelengths.

Global models, therefore, resolve large-scale patterns of azimuthal anisotropy associated, for example, with asthenospheric flow beneath oceanic plates. However, regional anisotropic tomography using data from dense broadband arrays is needed to provide more detailed information on the radial and lateral distribution of anisotropy. In this way, issues such as coupling between lithospheric deformation and asthenopsheric flow beneath tectonically complex areas can be addressed more fully.

# 6. Conclusions

Global tomographic models of azimuthal anisotropy provide guidance as to the lower bound of expected complexity in seismic anisotropy. For these models, simplified averaging approaches of computing predicted shear wave splitting are generally valid. Full waveform methods need not be applied to predict shear wave splitting from smooth tomographic models.

Full waveform approaches yield estimates of the back-azimuth variation of splitting, however, and accounting for such effects leads to dramatic drops in the median misfit between predicted and actual splitting. Consideration of actual patterns of back-azimuthal variations (observed and predicted) at individual stations may reconcile many of the remaining discrepancies.

Shear wave splitting predicted from smooth tomographic models is consistent with longwavelength representations of measured shear wave splitting, on global scales. For continents in particular, this implies that their lithosphere's heterogeneity, due to its geological assembly, is reflected in complex anisotropic structure, but simple, long-wavelength smoothed representations have a deterministic asymptote with geodynamic meaning.

Acknowledgments. We thank all seismologists who make their results available in electronic form, in particular M. Fouch, A. Wüstefeld and the numerous contributing authors for sharing their splitting compilations, and E. Debayle for providing his tomography model. The manuscript benefited from reviews by M. Savage, D. Schutt, and the associate editor, and comments by S. Chevrot. Most figures were created with the Generic Mapping Tools by *Wessel and Smith* [1998]. This research was partially supported by

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NSF-EAR 0643365, SFI 08/RFP/GEO1704, and computations were performed on John Yu's computer cluster at USC.

# Appendix A: Fitting generalized spherical harmonics to SKS splitting measurements

The azimuths and delay times as seen in global splitting databases display large variations on short spatial scales and are very unevenly distributed globally (Figure 1). However, long-wavelength averaging of splits leads to a significant improvement in the match between azimuthal anisotropy from SKS and surface wave tomography (Figure 9). This motivates our exploration of fitting global, generalized spherical harmonics (GSH) [e.g. Dahlen and Tromp, 1998, appendix C] with maximum degree L = 20 as basis functions to the SKS database [for details, see Boschi and Woodhouse, 2006; Becker et al., 2007b].

Assume that the M station-averaged splits at locations  $\mathbf{x}^i$  (i = 1...M) are expressed as a 2M dimensional vector holding M pairs of equivalent  $A_{c,s}$  parameters,  $\mathbf{A} = \{A_c^i, A_s^i\}$ . We then solve a regularized, least-squares inverse problem of type

$$\begin{pmatrix} \mathsf{Y} \\ \mathsf{R} \end{pmatrix} \cdot \mathbf{p} = \begin{pmatrix} \mathbf{A} \\ \mathbf{0} \end{pmatrix},\tag{A1}$$

for **p**, where the  $2M \times N$  matrix **Y** holds the real and imaginary GSH components at the M data locations, **p** holds the N = (2L + 6)(L - 1) GSH coefficients for degrees  $\ell \in [2; L]$  [see eqs. 8-10 of *Becker et al.*, 2007b], **0** is a N dimensional null vector, and **R**  $(N \times N)$  is a damping matrix. For norm damping, we use  $\mathsf{R}_n = \omega \mathsf{I}$  where  $\mathsf{I}$  is the identity matrix and  $\omega$  a damping factor; for wavelength-dependent, "roughness" damping, we use  $\mathsf{R}_r = \omega \frac{\ell(\ell+1)}{L/2(L/2+1)} \mathsf{I}$  [cf. *Trampert and Woodhouse*, 2003].

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To find an adequate representation of the actual splits, we conducted a standard tradeoff analysis, evaluating model complexity, expressed by the  $L_2$ -norm of  $\mathbf{p}$ ,

$$\nu = \|\mathbf{p}\|,\tag{A2}$$

against misfit, expressed as variance reduction,

$$\zeta = 1 - \|\mathbf{Y} \cdot \mathbf{p} - \mathbf{A}\| / \|\mathbf{A}\|, \tag{A3}$$

using various damping,  $\omega$ , values. Figure 11 shows the results for norm and roughness 642 damping of the station-averaged splitting dataset. Both approaches yield typical and 643 consistent "L-curves", indicating that a choice of  $\omega \sim 50$  (as indicated by the box symbols) 644 yields an appropriate compromise between representing the actual data and arriving at 645 a smooth model. For the analysis in the main text (including Figure 1), we therefore 646 chose  $\omega = 50$  and roughness damping to represent SKS splits in spherical harmonics. 647 That said, the variance reductions that can be achieved are relatively small ( $\zeta \sim 45\%$ ), 648 meaning that aspects of the heterogeneous nature of azimuthal anisotropy from SKS649 splits, expectedly, cannot be captured by our L = 20 GSH fit. However, once a  $1^{\circ} \times 1^{\circ}$ 650 averaging of the splitting database is performed, best  $\zeta$  values are increased significantly. 651

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Figure 1. Distribution of SKS splitting in our merged database (blue dots, with 5159 station-averaged entries) and damped, L = 20, generalized spherical harmonics representation of SKS splitting (yellow sticks, see Appendix A), shown on top of the 200 km depth  $2\Psi$  azimuthal anisotropy from *Lebedev and van der Hilst* [2008] (red sticks, eq. 3). Splitting measurements are mainly based on compilations by *Silver* [1996], *Fouch* [2006], and *Wüstefeld et al.* [2009], with additional references and data provided at http://geodynamics.usc.edu/~becker/. Plate boundaries here and subsequently are from *Bird* [2003]. (See online version for color.)



Figure 2. a) Depth variation (75 to 410 km shown) of  $2\Psi$  fast propagation direction in tomography model LH08 (sticks in background, see color-bar for depth), splitting predicted from tomography with the full waveform method (orange, with larger and smaller sticks and wedge sizes indicating back-azimuthal variability for  $\delta t' \pm \sigma_{\delta t}$  and  $\phi' \pm \sigma_{\phi}$ , reppectAvelyT, and vectorial average and average averag



Figure 3. a): Mean (filled boxes), standard deviation (error bars), and median (open boxes) of delay times,  $\delta t$ , in our station-averaged splitting database (Figure 1), sorted into GTR-1 [Jordan, 1981] tectonic regions. Orogenic zones are expected to be more geologically active than platforms, and shields are expected to be most stable and have the thickest lithosphere [cf. Becker et al., 2007a]. Number, N, of data for each region are listed underneath gray bars which indicate the relative frequency,  $N/N_0$ . b): Same as a), but for a 5° binned representation of the splitting data. c) Predicted splitting computed with the full waveform method for the depth regions 75 to 410 km in tomography model LH08 (see text), evaluated at the 5°-binned sites of b). d) Same as c), but predicted



Figure 4. Spatial wavelength-dependent comparison of azimuthal anisotropy ( $2\Psi$  anomaly signal for SV wave speeds) from the tomographic models by *Lebedev and van der Hilst* [2008] (LH08, a) and *Debayle et al.* [2005] (DKP2005, b). Plots a) and b) show power per degree and unit area (note log-scale) against spherical harmonic degree  $\ell$  at three layer depths as indicated. Plot c) shows the linear correlation per degree of azimuthal anisotropy between the two seismological models, along with the 95% significance level based on Student's *t*-test. All metrics are computed using generalized spherical harmonics based on the  $A_{c,s}$  terms of eq. (3) [see *Becker et al.*, 2007b, for details].



Figure 5. Depth-dependent properties of tomographic models of azimuthal anisotropy. a) Root mean square (RMS) of the  $2\Psi$  anomalies  $((v_{SV1} - v_{SV2})/v_{SV})$  in the models by *Lebedev and van der Hilst* [2008] (LH08) and *Debayle et al.* [2005] (DKP2005) as a function of depth, when both models are expressed in generalized spherical harmonics with maximum degree L = 20. b) Correlation up to  $\ell = 20$ ,  $r_{20}$ , between two layers of the same model at  $z_{1,2} = z \pm 100$  km, plotted as a function of depth z; 95% significance level shown (also see Figure 2). c) Cross-model correlation between the two seismological models, and of each with the best-fit geodynamic model of *Becker et al.* [2008].



Figure 6. Wavelength-dependent correlation between the predicted splitting  $\phi'$  and  $\delta t'$  computed using three different methods as described in sec. 2 based on tomography by *Lebedev and van der Hilst* [2008] (top) and *Debayle et al.* [2005] (bottom). Solid line: comparison between *Montagner et al.* [2000] averaging and Christoffel matrix from an averaged tensor approach; dashed line: *Montagner et al.* [2000] vs. full waveform split; dotted line: Christoffel matrix approach from averaged tensor vs. full waveform, synthetic splitting.

Table 1. Relationship between SKS splitting delay-time predictions based on vectorial averaging of azimuthal anisotropy tomography [Montagner et al., 2000] and full waveform approaches for the two tomographic models. Reference method uses scaled, purely hexagonal tensors C at all depths from 75 to 410 km, filtering with central period  $T \approx 7$  s, and the Levin et al. [1999] method. The best-fit slope, b, is computed from a linear regression (allowing for "errors" in both variables) such that  $\delta t'_{waveform} \approx a + b \ \delta t'_{Montagner}$ .

	LH08			DKP2005				
		linear reg	gression	linear regression				
type of computation	correlation	offset $a$	slope $b$	correlation	offset $a$	slope $b$		
reference	0.94	0	1.10	0.82	0	1.17		
$T \approx 12.5$ s filtering	0.93	-0.06	1.41	0.84	-0.03	1.33		
$T \approx 15$ s filtering	0.81	-0.11	1.86	0.84	-0.05	1.38		
$\operatorname{depth-dependent} C$	0.93	0	1.10	0.82	0	1.18		
${\rm depth-dependent}\ C,\ {\rm variable}\ {\rm dip}$	0.93	0	1.05	0.82	0	1.12		
Menke and Levin [2003]-method	0.94	0	1.23	0.84	0	1.02		
using $25$ to $250$ km depths	0.98	0	0.89	0.94	0	0.88		



Figure 7. Distribution of delay time in the station-averaged splitting database (a), if predicted from tomography using *Montagner et al.* [2000] averaging (b), and based on full waveform splits (c). Median values of distribution given along with  $q_1$  and  $q_2$  quartiles in parentheses.

Table 2. Median and standard deviation of the absolute, angular misfit,  $|\Delta \alpha|$  (random, average value is  $|\Delta \alpha|_r = 45^\circ$ ), between full waveform, synthetic splitting and our station-averaged *SKS* compilation, for the complete database and the 5°-binned representation in Figure 2. We show results for different tomographic models and depth ranges used for integration.

median  $\pm$  standard deviation of  $|\Delta \alpha|$  [°]

integration depth ranges

	75-	25-	10-	25-			
type of database	410 km	$250 \mathrm{~km}$	410 km	650 km			
	LH08						
all splits	$33 \pm 25$	$30 \pm 25$	$31\pm25$	$37 \pm 26$			
$5^{\circ}$ averaged	$34 \pm 26$	$32 \pm 26$	$31 \pm 26$	$34 \pm 26$			
		Dŀ	KP2005				
all splits	$39 \pm 25$	$38 \pm 26$	$37 \pm 25$	$40 \pm 25$			
5° averaged	$37 \pm 25$	$38 \pm 26$	$38 \pm 26$	$41\pm27$			

**Table 3.** Comparison of median, absolute angular misfit,  $|\Delta \alpha|$ , between predicted and actual *SKS* splitting based on a 5° averaged representation of our dataset and an integration of LH08 in the depth range from 25 to 250 km. We list median angular misfits for all data locations, and when sorted into, i), the tectonic regionalization of *Jordan* [1981] (cf. Figure 3), ii), the smallest and largest 25% of total, depth-integrated, nonamplitude scaled rotation of the tomographic fast direction,  $\Psi$ , and, iii), the smallest and largest 25% of estimated back-azimuth variability,  $\sigma_{\phi}$ , from full waveform splitting

# median of angular misfit $|\Delta \alpha|$ [°]

	global	oceanic	continental		$\Psi$ rotation			$\sigma_{\phi}$	
type of model			Orogenic	platforms	shields	low	high	low	high
Montagner et al. [2000] averaging	33	28	36	36	38	24	36	35	36
full waveform	32	27	30	35	41	24	36	32	35
full waveform, $\pm \sigma_{\phi}$	19	14	18	20	22	11	24	29	13



Figure 8. a) Back-azimuthal completeness for shear wave splitting, f, for all events above magnitude 5.8 in the *Engdahl et al.* [1998] catalog from 1988 to 1997 within the distance range between 90 and 145° [for comparison with *Chevrot*, 2000]. b) Completeness for all events in the gCMT catalog [*Ekström et al.*, 2010] up to 2010 and distance range 90 to 130°.



Figure 9. Misfit between predicted and actual splitting when expressed as the median, absolute angular deviation between  $\phi$  and  $\phi'$  (a), the delay time correlation between  $\delta t$ and  $\delta t'$  (b), and the maximum coherence,  $C_{max}$ , (for any lag,  $\alpha$ ), for  $D_c = 20^\circ$  (see eq. 5). All misfit values are shown as a function of bin-size,  $\gamma$ , of the averaged splitting; gray shades indicate different tomographic models. Solid lines are for the default depth range of 75 to 410 km, dashed for 25 to 250 km (cf. Table 3). Circle symbol size in a) and b) scales with the log<sub>10</sub> of the number of sites, N, used for analysis, N decreases from 2717 for  $\gamma = 1^\circ$  to N = 16 for  $\gamma = 50^\circ$ . Error bars (same for all tomographic models, but only shown for shallow, LH08 curves for simplicity) indicate the standard deviation around the mean for 250, random medium Monte-Carlo simulations.

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Figure 10. Coherence between predicted (full waveform, depth range 75 to 410 km) and actual splitting for  $D_c = 20^{\circ}$  and spatial averaging of the splitting database, solid line: bin-width  $\gamma = 30^{\circ}$ ; dashed:  $\gamma = 10^{\circ}$ , and dotted:  $\gamma = 1^{\circ}$  (cf. Figure 9c). Black: for LH08, gray: for DKP2005.



Figure 11. Trade-off curves for damped, least-square (eq. A1) fitting GSH basis functions to our global, station-averaged splitting database (as in Figure 1), expressed as model norm,  $\nu$  (eq. A2), as a function of variance reduction,  $\zeta$  (eq. A3), for norm ( $R_n$ ) and roughness ( $R_r$ ) damping with  $\omega = 50$  values indicated by squares. Plot also shows a roughness damping trade-off curve for a 1° × 1° averaged representation of the splitting database (see sec. 3.1).