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# ON THE RIESZ IDEMPOTENT OF CLASS $A$ OPERATORS

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*Abstract.* In this paper, we show that if $T$ is a class $A$ operator and $\lambda$ is a non–zero isolated eigenvalue of $\sigma(T)$, then $E\mathscr{H} = \ker(T-\lambda) = \ker(T-\lambda)^*$, where $E$ is the Riesz idempotent with respect to $\lambda$. In this case, $E$ is self–adjoint, i.e, it is an orthogonal projection.

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