## ON THE TIME-SENSE

## By Lefis T. Stevens.

The experiments which form the basis of this article have been in progress during the past two years: the greater portion of them were performed, under the supervision of Professor G. Stanley Hall, in the Psychophysical Laboratory of the Johns Hopkins University, Bailtimore; the results there obtained have received confirmation from additional experiments made in the Physiological Laboratory of Professor Henry P. Bowditch, at the Harvard Medical School, Boston. The method of experimenting was somewhat similar to that of Vierordt, ${ }^{1}$ and consisted, in a general way, in impressing upon the mind intervals of time by means of a metronome, and in reproducing the same after the metronome had been stopped.

The apparatus employed in the research was a horizontaldrum kymographion of Marey, with horizontal-screw attachment, by means of which was obtained a continuous spiral tracing. A delicate time-marker, writing upon the sooted-paper coating of the drum, was attached to the vertical support seated upon the horizontal screw, and by the revolution of the latter was made to proceed slowly from one end of the drum to the other. A tuning-fork, or a vibrating rod, ${ }^{2}$ and a resistancecoil were placed in the same electrical circuit with this timemarker. In a shorter circuit with the tuning-fork were placed a mercury-cup and a compound lever; this latter being so constructed that by depressing one end with the finger the other extremity (hook-shaped) was made to dip into the cup of mercury and thus close the circuit. When the hooked extremity was out of the mercary-cup, the time-marker registered the oscillations of the tuning-fork, bat by tapping the lever the fork was shifted into the shorter circuit, and its vibrations failed for a moment to be recorded. By tapping the lever, therefore, at the beginning and the end of an interval of time, the interval could be recorded upon the sooted paper, and its length be subsequently determined by counting the number of vibrations between two successive interruptions on the tracing. This end was attained at one stage of the investigation by inserting a Morse's key into the same circuit with the tuning-fork and the time-marker, and thas directly breaking the circuit; but the key possessed the disadvantages of requiring a considerable amount of muscular force to press it, and of

[^0]making, at the same time, a sharp click. What influence the introduction of muscular force into the experiment would exert upon the time-sense, beyond that of fatigue, is not definitely known; and the same can be said for the influence of sensory impressions. But it was desirable to exclude, as far as was possible, all probably complicating conditions from the method, and, consequently, for the Morse's key was substituted the compound lever, which worked noiselessly and with the least possible resistance.

The individual under experiment tapped the lever synchronously with the beats of a metronome. When he had become perfectly familiar with the given interval, the drum was set in motion and the first round of the tracing was taken, with the metronome still beating; the latter was then stopped, while the person kept on tapping the levar at the same rate. The average of the intervals recorded in the first line of the tracing was the standard time; the rest of the tracings gave successive reproductions of this standard.

At first, the duration of each experiment was from two to three minutes, but this brought on fatigue so rapidly that it wes impossible to obtain more than four or five experiments at one sitting. It was, therefore, reduced to one minute, under which condition ten or even more could be readily made at one time. In the discussion of the results, the reproductions for the first minate only will be considered in those cases where the experiments extended beyond that time.

Between two successive experiments there was an intermission of at least three minutes; in the majority of the series its length was from five to ten minutes.

In the majority of experiments the standard intervals ranged between 36 sec , and 1.5 secs .; there are several observations for $\cdot 27$ sec., and only one for $2 \cdot 9$ secs.

Experiments, to the number of 135 in all, were performed upon seven different individuals. Of these, 114 point to this fundamental principle:-That there is an interval of time (the value of which varies between 53 and -87 sec .) which can be reproduced with considerable accuracy; but with all other intervals an error is made, which is plus for those above and minus for those below the so-called indifference-point

These will be spoken of as the "regular" experiments.
The remaining 21 follow no recognised law, and, in contradistinction to the 114 , will be called the "irregular" experiments.

## A. Rogular Experiments.

The value of the standard interval being from $\cdot 53$ to -87 sec., and the duration of an experiment one minute, each experiment consists in reproducing the standard interval from about 40 to

150 times, according to its length. To condense the results for publication, a certain amount of averaging has been necessary. In the following Tables, the first figure in each column represents the value of the standerd, expressed in thousandths of a second; the second figure, the average of the reproductions of the standard for the first five seconds; the third, the average of the reproductions for the second five seconds; and so on, to the end of the experiment.

In Tables II., III. and IV. are given only a fraction of the total number of experiments performed upon the subjects; in these cases, those experiments are selected for publication which show the average amount of variation. In Tables I., V., VI. and VII., one or several regular experiments are omitted from each for the reason that they are mere repetitions of one or more of those which are given.
I.-O.S. 12 Experiments, all regular.

| 1.440 | 968 | 830 | $\cdot 740$ | 710 | -677 | 610 | . 590 | -480 | $\cdot 360$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.477 | 1.008 | -857 | $\cdot 748$ | $\cdot 728$ | 666 | 604 | $\cdot 582$ | $\cdot 474$ | $\cdot 348$ |
| 1.454 | -993 | . 860 | $\cdot 755$ | $\cdot 708$ | $\cdot 670$ | -590 | -564 | $\cdot 464$ | -346 |
| 1-500 | -990 | -853 | $\cdot 754$ | $\cdot 714$ | -672 | -382 | $\cdot 558$ | $\cdot 462$ | -348 |
| 1.515 | 1.038 | -860 | $\cdot 754$ | -708 | $\cdot 670$ | -584 | . 546 | $\cdot 452$ | -338 |
| 1.498 | 1013 | -853 | $\cdot 734$ | $\cdot 700$ | -678 | $\cdot 388$ | . 560 | $\cdot 448$ | -328 |
| $1 \cdot 536$ | 1000 | -850 | $\cdot 754$ | $\cdot 712$ | -668 | - 694 | -542 | -452 | -342 |
| 1.494 | 1032 | -870 | $\cdot 742$ | -714 | -680 | -578 | -544 | $\cdot 446$ | $\cdot 3.38$ |
| 1.522 | 1015 | -850 | -742 | -700 | -670 | $\cdot 580$ | -552 | $\cdot 446$ | -336 |
| $1 \cdot 510$ | 1028 | -875 | $\cdot 732$ | $\cdot 706$ | -654 | -588 | - 560 | $\cdot 444$ | -3.34 |
| 1.570 | 1.041 | -868 | $\cdot 768$ | -710 | 654 | 600 | -554 | - 440 | -332 |
| 1-543 | 1.048 | -882 | $\cdot 770$ | -722 | -674 | -590 | -556 | $\cdot 440$ | -332 |
| 1.580 | 1.008 | . 852 | $\cdot 764$ | $\cdot 714$ | -680 | -596 | . 548 | - 470 | -326 |

II.-I.I.H. 36 Experimente, of which 5 are irregular.

| 1.360 | 937 | $\cdot 730$ | 653 | . 593 | $\cdot 525$ | 492 | . 442 | 410 | .360 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $1 \cdot 448$ | 960 | 749 | $\cdot 637$ | -591 | . 522 | -481 | - 442 | -398 | $\cdot 351$ |
| $1-498$ | -908 | $\cdot 788$ | $\cdot 687$ | - 396 | - 520 | -491 | -432 | - 400 | - 31 |
| $1 \cdot 475$ | -939 | $\cdot 757$ | 641 | -593 | -542 | -486 | $\cdot 448$ | -403 | $\cdot 351$ |
| 1.470 | -985 | $\cdot 783$ | -663 | $\cdot 589$ | . 540 | -489 | $\cdot 445$ | - 400 | -351 |
| 1.547 | 1018 | -767 | 675 | $\cdot 600$ | $\cdot 540$ | 484 | $\cdot 456$ | - 408 | -349 |
| 1.548 | 1035 | $\cdot 783$ | -659 | -600 | -532 | -482 | $\cdot 438$ | -400 | -350 |
| 1.510 | 1065 | $\cdot 729$ | - 876 | $\cdot 600$ | - 519 | -490 | - 442 | $\cdot 405$ | -345 |
| 1.530 | 1068 | -757 | 870 | 611 | -524 | -491 | $\cdot 427$ | $\cdot 403$ | -352 |
| 1.485 | 1-101 | $\cdot 783$ | -670 | 600 | $\cdot 492$ | $\cdot 490$ | $\cdot 425$ | -389 | -349 |
| 1.487 | $1 \cdot 126$ | $\cdot 783$ | -689 | -600 | . 812 | $\cdot 490$ | - 422 | $\cdot 413$ | - 349 |
| 1.543 | $1 \cdot 153$ | -800 | 691 |  | . 510 | $\cdot 486$ | $\cdot 418$ |  | -351 |
| 1.525 | I-163 | -800 |  |  | -534 | -484 | - 426 |  | -347 |

III.-H.P.B. 38 Experiments, of which 6 are irregular.

| 1.250 | -900 | . 800 | 731 | 708 | 040 | -594 | . 560 | - 540 | 488 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $1 \cdot 263$ | -917 | - 817 | $\cdot 729$ | $\cdot 714$ | 831 | $\cdot 588$ | $\cdot 561$ | . 564 | $\cdot 480$ |
| 1-275 | -917 | - 800 | $\cdot 743$ | $\cdot 707$ | . 625 | -587 | -550 | -524 | $\cdot 475$ |
| 1.323 | -922 | -850 | -737 | $\cdot 693$ | 625 | - 578 | -563 | . 533 | $\cdot 487$ |
| 1.318 | -928 | -833 | $\cdot 734$ | $\cdot 714$ | -819 | . 389 | - 559 | . 520 | $\cdot 464$ |
| 1-268 | -980 | -850 | $\cdot 743$ | $\cdot 714$ | 625 | -598 | -656 | - 524 | -463 |
| 1.323 | -980 | -833 | . 729 | $\cdot 710$ | 825 | 601 | -561 | . 518 | -488 |
| $1 \cdot 350$ | -940 | -862 | 729 | $\cdot 719$ | -833 | 603 | -569 | $\cdot 550$ | -469 |
| $1 \cdot 367$ | -960 | -888 | $\cdot 757$ | $\cdot 789$ | 639 | 600 | $\cdot 570$ | $\cdot 520$ | $\cdot 476$ |
| $1 \cdot 400$ | 1.023 | -850 | $\cdot 757$ | $\cdot 700$ | -640 | 613 | -563 | - 520 | -490 |
| $1 \cdot 450$ | -994 | -867 | -817 | $\cdot 743$ | -639 | 635 | -589 | $\cdot 546$ | -488 |
| $1 \cdot 423$ | 946 | - 818 | $\cdot 817$ | $\cdot 729$ | -689 | -615 | -587 | $\cdot 328$ | $\cdot 474$ |
| $1 \cdot 433$ |  | -868 | . 808 | $\cdot 729$ | $\cdot 675$ |  | $\cdot 597$ | $\cdot 527$ | $\cdot 480$ |

IV.-F.S.L. 18 Experiments, of which 3 are irregular.

| 1467 | 1.100 | 875 | 822 | 746 | $\cdot 727$ | 882 | 820 | 478 | -387 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.517 | 1.109 | -883 | $\cdot 817$ | $\cdot 731$ | $\cdot 728$ | 660 | -628 | $\cdot 484$ | $\cdot 379$ |
| 1.577 | 1.168 | . 860 | -826 | $\cdot 714$ | -693 | -635 | -595 | -468 | $\cdot 377$ |
| 1.540 | 1.212 | -839 | -828 | -706 | $\cdot 700$ | $\cdot 608$ | -585 | $\cdot 463$ | $\cdot 366$ |
| 1.530 | 1-158 | -835 | -824 | $\cdot 737$ | 692 | -633 | -602 | $\cdot 466$ | -370 |
| 1.534 | 1-170 | -857 | 842 | $\cdot 718$ | ${ }^{6} 67$ | -616 | $\cdot 607$ | -458 | $\cdot 3.59$ |
| 1.572 | 1-166 | -831 | 799 | $\cdot 716$ | -692 | $\cdot 617$ | -595 | $\cdot 461$ | $\cdot 357$ |
| 1.501 | 1.095 | -855 | -833 | 733 | 688 | $\cdot 610$ | -598 | $\cdot 447$ | $\cdot 377$ |
| $1 \cdot 474$ | 1-163 | $\cdot 877$ | - 808 | $\cdot 739$ | 711 | 623 | $\cdot 603$ | $\cdot 449$ | -364 |
| 1-555 | $1 \cdot 140$ | -884 | $\cdot 788$ | $\cdot 736$ | $\cdot 712$ | 621 | -398 | $\cdot 467$ | $\cdot 357$ |
| 1.515 | $1 \cdot 140$ | -884 | 781 | $\cdot 710$ | $\cdot 716$ | -607 | -605 | $\cdot 454$ | $\cdot 362$ |
| 1.530 | $1 \cdot 129$ | $\cdot 883$ | 795 | 703 | 700 | ${ }^{6} 623$ | - 587 | $\cdot 455$ | -362 |
| $1 \cdot 473$ | $1 \cdot 150$ | $\cdot 925$ | $\cdot 791$ | 713 | $\cdot 708$ | -632 | -600 | $\cdot 456$ | . 354 |

V.-G.S.H. 9 Experiments, of which 2 are irregular.

| 1.535 | -828 | '721 | 638 | . 608 | -268 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1.670 | -823 | $\cdot 713$ | -613 | -492 | $\cdot 261$ |
| 1.687 | -821 | $\cdot 712$ | -608 | $\cdot 496$ | -259 |
| 1.573 | -802 | -697 | -620 | -488 | -262 |
| 1.677 | $\cdot 794$ | $\cdot 701$ | -618 | -505 | -261 |
| 1.680 | -849 | . 691 | -611 | $\cdot 492$ | -260 |
| 1.650 | -824 | -683 | 616 | -488 | -266 |
| 1.640 | -824 | $\cdot 705$ | 608 | $\cdot 479$ | -962 |
| 1.713 | -810 | $\cdot 702$ | 623 | $\cdot 499$ | $\cdot 269$ |
| 1-587 | -837 | 681 | 620 | -488 | $\cdot 271$ |
| 1876 | -802 | 681 | $\cdot 617$ | 472 | -262 |
| 1.763 | -834 | $\cdot 704$ | 628 | $\cdot 470$ | -268 |
| 1-703 | -801 | 694 | -604 | $\cdot 480$ | -264 |

VI.-Lit.S. 11 Experiments, of which 1 is irregular

| 1.480 | 750 | .744 | 660 | .690 | .600 | .360 | -260 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1.371 | .777 | .787 | .660 | .583 | .494 | .356 | -245 |
| 1.494 | .807 | .789 | .667 | .580 | .462 | .351 | -259 |
| 1.556 | .830 | .743 | -653 | .588 | .486 | .348 | -258 |
| 1.544 | .792 | .794 | .654 | .583 | .490 | .333 | .254 |
| 1.516 | .815 | .803 | .636 | .578 | .496 | .346 | .261 |
| 1.537 | .829 | .791 | .640 | .548 | .490 | .347 | .256 |
| 1.540 | .823 | .786 | .659 | .547 | .488 | .345 | .251 |
| 1.574 | .850 | .789 | .653 | .562 | .490 | .367 | .252 |
| 1.574 | .890 | .776 | .651 | .564 | .496 | .337 | .252 |
| 1.587 | .870 | .783 | .680 | .571 | .486 | .338 | .250 |
| 1.552 | .870 | .851 | .637 | .569 | .494 | .342 | .246 |
| 1.536 | .875 | -809 | .653 | .580 | .492 | .332 | .248 |
|  |  |  |  |  |  |  |  |

VII-H.H.D. 11 Experiments, of which 4 are irregular.

| 1458 | 979 | .730 | 600 | 472 | . 400 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1.488 | 1.006 | $\cdot 751$ | - 597 | $\cdot 462$ | -390 |
| $1 \cdot 436$ | $\cdot 970$ | $\cdot 718$ | 602 | $\cdot 458$ | - 394 |
| 1-589 | -998 | $\cdot 726$ | -588 | $\cdot 438$ | $\cdot 369$ |
| 1.602 | $\cdot 955$ | $\cdot 739$ | -596 | $\cdot 434$ | -385 |
| 1.694 | -941 | $\cdot 731$ | -600 | $\cdot 447$ | $\cdot 358$ |
| 1.693 | -994 | -734 | -605 | $\cdot 436$ | $\cdot 344$ |
| 1683 | 1050 | $\cdot 733$ | $\cdot 585$ | $\cdot 482$ | $\cdot 340$ |
| 1.582 | 1021 | -726 | $\cdot 596$ | -435 | $\cdot 335$ |
| 1.647 | -999 | $\cdot 732$ | -502 | $\cdot 442$ | $\cdot 333$ |
| 1683 | 1011 | -735 | -559 | $\cdot 442$ | -340 |
| 1.688 | -987 | $\cdot 718$ | -579 | $\cdot 434$ | $\cdot 335$ |
| 1819 | -971 | $\cdot 747$ | $\cdot 590$ | -442 | $\cdot 345$ |

A glance at these Tables shows that, in each case, short intervals are shortened and long intervals are still further lengthened in their reproduction; and that somewhere between the two extremes is an interval, in the reproduction of which there is made practically no error. These points are more plainly seen in the annexed series of carves, which represents, in detail, experiments 1, 2, 5, 8, 10 of Table I. Each mm. of ordinate represents 02 sec . The dotted line for each carve (opposite which the number of the experiment is placed) represents the level of the standard interval above the common base-line. The curve is obtained, in each case, by joining with straight lines the upper limits of the ordinates, the lengths of which represent the value of successive reproductions of the standard interval. The ordinates are separated from each other by a space of 1 mm . Where no error is made in reproducing the standard, the curve hugs the dotted line, as is the case with the middle one. Where an error is made, the curve recedes more and more from the dotted line, according to the amount of the error; and is above or below it, according as the error is plus or minus.


The amount of error made for each interval, and the position of the indifference-point, are better shown in the following Tables, which represent the experiments in a still more compact form. In the first column of each are placed the standard intervals; opposite these, in the second column, are the averages of the total number of reproductions for one minute ; and in the third column is shown the amount of error made in each case.

| I. | $\begin{aligned} & \text { Standard. } \\ & 1 * 440 \end{aligned}$ | Reproduced. $1 \cdot 517$ | Error. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | . 966 | 1018 | $+$ | 5-4 | " |
|  | $\cdot 830$ | -861 | $+$ | $3 \cdot 7$ | 0 |
|  | $\cdot 740$ | $\cdot 753$ | $+$ | 1.8 | " |
|  | $\cdot 710$ | $\cdot 711$ | $+$ | $\cdot 1$ | " |
|  | -677 | 670 | - | 10 | \% |
|  | 610 | - 590 | - | $3 \cdot 3$ | " |
|  | -590 | - 555 | - | 5.9 | " |
|  | $\cdot 480$ | $\cdot 454$ | - | $6 \cdot 3$ | " |
|  | -360 | -337 | - | 6.4 | " |
| II. | 1.360 | 1.508 | $+$ | 10.5 | " |
|  | -937 | 1043 | $+$ | 10.3 | " |
|  | $\cdot 730$ | $\cdot 773$ | $+$ | 6.9 | " |
|  | 653 | -669 | $+$ | $2 \cdot 4$ | " |
|  | -593 | -598 | + | -9 | " |
|  | -525 | -524 | - | - 8 | " |
|  | $\cdot 492$ | $\cdot 488$ | - | $\cdot 8$ | " |
|  | -442 | -435 | - | 18 | " |
|  | -410 | -408 | - | 20 | " |
|  | $\cdot 360$ | -350 | - | $2 \cdot 8$ | n |
| III. | 1.250 | 1.349 | $+$ | $7-9$ | " |
|  | -900 | -953 | $+$ | $6 \cdot 9$ | " |
|  | -800 | -845 | $+$ | 68 | " |
|  | $\cdot 731$ | $\cdot 758$ | $+$ | $3 \cdot 7$ | " |
|  | -708 | -717 | $+$ | 1.3 | " |
|  | 640 | +637 | - | -5 | " |
|  | -594 | -600 | $+$ | 10 | " |
|  | -569 | -569 |  | 00 | " |
|  | - 640 | -588 | - | $2 \cdot 2$ | " |
|  | -488 | $\cdot 474$ | - | 2.9 | " |
| IV. | $1 \cdot 467$ | 1.587 | $+$ | $4 \cdot 1$ | " |
|  | 1-100 | $1 \cdot 150$ | $+$ | $4 \cdot 5$ | " |
|  | . 875 | -868 | - | -8 | " |
|  | -828 | -818 | - | 1.2 | " |
|  | $\cdot 746$ | $\cdot 721$ | - | $3 \cdot 4$ | " |
|  | $\cdot 727$ | $\cdot 701$ | - | $3 \cdot 6$ | " |
|  | -862 | -684 | - | $5 \cdot 7$ | " |
|  | 680 | -590 | - | $3 \cdot 4$ | " |
|  | $\cdot 478$ | $\cdot 459$ | - | $3 \cdot 6$ | " |
|  | -387 | -365 | $\rightarrow$ | 5.7 | " |
| V. | $2.850{ }^{1}$ | 3.410 | $+$ | $19 \cdot 7$ | " |
|  | 1.535 | 1668 | $+$ | $8 \cdot 7$ | " |
|  | -826 | -819 | - | 9 | " |
|  | $\cdot 781$ | 697 | - | $3 \cdot 3$ | " |
|  | 636 | 618 | - | 32 | " |
|  | -508 | $\cdot 487$ | - | $4 \cdot 1$ | " |
|  | -268 | -264 | - | $1 \cdot 5$ | $\cdots$ |

${ }^{1}$ This experiment was not included in the preceding Tables, because of the impossibility of dividing it up into periods of $\overline{5}$ seconds.

| VI. | $1 \cdot 480$ | 1.548 | +46 per cent. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\cdot 750$ | . 838 |  | 11.5 | " |
|  | 744 | -798 | $+$ |  | " |
|  | 660 | 656 | - | . 8 | " |
|  | - 390 | -571 | - |  | " |
|  | -500 | -489 | - | 2-2 | " |
|  | -360 | -345 | - | $4 \cdot 8$ | " |
|  | $\cdot 260$ | -253 | - | $2 \cdot 7$ | " |
| VII. | 1.458 | 1.615 |  | 10.8 | " |
|  | $\cdot 979$ | .992 | + | 13 | " |
|  | $\cdot 730$ | $\cdot 733$ | + | $\cdot 4$ | " |
|  | -600 | -388 | - |  | " |
|  | $\cdot 472$ | $\cdot 446$ | - | $5 \cdot 5$ | " |
|  | $\cdot 400$ | -354 | - | 11.5 | n |

These Tables show very plainly the main point of the paper, namely, that the error made in the reproduction of the longer intervals is plus, of the shorter ones, minus; and that at some point between the two extremes the error approaches zero.

The value of this indifference-point is found not to be constant, but to vary for different individuals between 53 and 87 sec ., the average being aboat 71 sec . The position of the indifferencepoint is not so accurately defined in Case III as it is in the others. The reason for this is not evident. Of the six regular experiments made for intervals from 55 to 70 sec., the mean value of the standard interval is 61 sec ., and the average of the error of reproduction is 3 per cent., the individual variations not being, algebraically, more than 1 per cent.

With reference to the amount of variation, the number of experiments is, in the majority of cases, not sufficient to give the results a quantitative value. The amount of variation depends upon the fixedness of the attention on the work, and apon the experience which one has had in estimating and holding intervals of time. The complaint was made quite frequently by several of the gentlemen of their inability, at times, to keep their whole attention upon the experiment; and subsequent examination of such experiments showed that the error made was either contrary to the law above stated, or was in the proper direction but abnormally large in amount. The effect of practice was well seen in Case III., where a great number of observation swas made. In the first few experiments very large errors were made; but as the work proceeded, they gradually diminished in amount, until they reached, on the average, the size that is represented, for the various intervals, in the Tables. Tables I. and II. were obtained from gentlemen who are musicians by profession ; in the second case, where numerous experiments were made, the uniformity in the amount of variation was a noted feature from the very start. Moreover, in both these cases there was not that difficulty which was experienced by certain of the others, in grasping the longer intervals of time.

Diversion of attention and small experience are, therefore, regarded as the cause of the great irregularity in the size of the errors that is observed in the last four Tables.

The first three Tables, however, possess a certain quantitative as well as qualitative value; and in these it is observed that the error gradually increases in amount, as the indifference-point is moved from, in either direction. As to the manner of variation, examination of the curves (p. 398) reveals two remarkable points. (1) The constant zig-zag of individual records. This is a peculiarity which was observed in all the curves plotted. ${ }^{1}$ Of the series of curves published, the upper one shows about 19 cases only out of about 140 in which two sequent variations are in the same direction. This would seem to indicate that an interval is judged more correctly after it is completed than before, and that correction is made for its error in the next reproduction, according to a standard which the mind carries bat to which the hand (or perhaps the will during the interval) cannot be accurately true. The origin of this peculiarity would, therefore, appear to lie not in the judgment, but in the execution. (2) In all of the curves plotted, there were observed more or less distinctly still larger and more primary waves. The prominence of these varied greatly; in some of the curves they were apparently absent, in others they were decidedly marked. On p. 398, three such waves are plainly seen in the first, and one each in the second and fourth curves; in the third and fifth they are not so evident, but their existence is shown by enlarging these curves. Taking into consideration all of the carves that were plotted, it may be stated that these waves are no more prominent for one interval than for another, as the pablished curves would indicate. The length of these waves, expressed in fractions of a minute, varies, in the majority of cases, between 6 and 9 min ., and averages $73 \mathrm{~min}{ }^{2}$ This rhythmical variation seems to be not in the execution, but rather to have its origin in a rhythmical variation of the standard carried in the mind. That this is connected with the rhythmical changes in the nutritive condition of the cerebral centres, as produced by the vaso-motor rhythmical constriction of arterioles, it would be rash to deny or affirm, or, perhaps, even to suppose.

## B. Irregular Experiments.

The following are all of the irregular experiments, given in the form best adapted to show the direction and amount of variation:-

[^1]| II. | 8tanderd. | $\begin{aligned} & \text { A verage of the } \\ & \text { total number of } \\ & \text { reproductitons } \\ & -798 \\ & .535 \\ & .526 \\ & .523 \\ & .494 \end{aligned}$ | Error. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | -800 |  | - | - 3 per cent. |  |
|  | -515 |  | $+$ | $3-9$ | " |
|  | -506 |  | + | 40 | " |
|  | -500 |  | $+$ | 46 | " |
|  | $\cdot 471$ |  | $+$ | $4-9$ | " |
| IIL. | 960 | -960 |  | 0 | " |
|  | 933 | -929 | - | $\cdot 4$ | " |
|  | 647 | -681 | $+$ | 53 | " |
|  | -815 | 645 | $+$ | $4 \cdot 9$ | " |
|  | -588 | -819 | $+$ | 5.3 | " |
|  | $\cdot 493$ | - 510 | + | $3 \cdot 4$ | " |
| IV. | 980 | -908 | - | 1.3 | " |
|  | $\cdot 796$ | -862 | $+$ | $8 \cdot 3$ | " |
|  | $\cdot 734$ | $\cdot 783$ | $+$ | 6.7 | " |
| V. | $1 \cdot 115$ | 1078 | - | 39 |  |
|  | $\cdot 733$ | $\cdot 746$ | $+$ | 1.8 | " |
| VI. | 814 | 620 | + | 10 | " |
| VIL. | -638 | 657 | $+$ | 40 | " |
|  | -686 | 635 | $+$ | 1.4 | " |
|  | -358 | -591 | $+$ | 70 | " |

The irregularities consist in reproducing accurately long, in shortening long, and in lengthening short intervals. It must be stated that, in the attempt to get pure results, all those experiments were excluded in which fatigue or inattention spontaneously stated by the subject entered, but no others. The examination of such experiments, however, revealed the fact, that the effect of fatigue is to make the error for short intervals plus instead of minus, and to increase the amount of variation made in the reproduction of long intervals; and that individuals under experiment are apt, when inattentive, to shorten long and prolong short intervals. Some of these experiments, at least, are, therefore, regarded by the author as those in which fatigue and diversion of attention were existing but not acknowledged conditions. The accurate reproduction of long intervals is regarded as the chance result of the mataal neutralisation of the two opposing factors, the natural tendency to slow, and the effect of inattention.

The conclusion drawn in this paper, with reference to the direction of the variation made in estimating long and short intervals, is in direct opposition to that of previous investigators. Vierordt (1), receiving time-impressions from the beating of a metronome and after the lapse of a short while reproducing them,
foand that the reproduced interval was longer than the standard when this was small, shorter when it was great; and that between the two extremes was an interval which could be reproduced quite accurately. This indifference-point was not the same for different individuals, but varied between 1.5 and 3.5 secs. For himself, when the impressions were conveyed through the sense of taste, this interval was from 2.2 to 2.5 secs.; when through the sense of hearing, from 3 to 3.5 secs . These values were obtained when a short time elapsed between reception and reproduction; with the increase or dimination of this, the indiffer-ence-point was found to grow longer or shorter.

According to Mach (2), whose experiments were performed according to the method of just perceptible differences, the recognition of the inequality of two intervals of time, one interval following immediately upon the other, is the most delicate at about 37 sec.; and the further from this point the standard interval recedes, the greater must be the difference between the standard and the interval for comparison, in order that they be recognised as unequal. There is, however, considerable discord in his results, which detracts from the value of his conclusions.

Kollert (3) began the long series of experiments that have been performed in Wundt's laboratory. His experiments were performed according to the method of just perceptible differences. Two metronomes were used, the pendulum of each of which was placed in an electrical circuit along with an electro-magnet, so that by the momentary opening of the current a double vibration of the pendulum of the metronome could be effected, and thus an interval of time be marked out. One of the metronomes beat at a rate which was constant for a single series of observations; the other gave out various intervals for comparison with the standard. An intermission occurred between the two intervals, which in length was equal always to the standard. The pendulum of the second metronome was shortened, until a just perceptible difference was observed between its time and that of the first; after which it was elongated, until the subject detected a difference between the two. The mean of these two just perceptible differences gave the error made by the individual under experiment in his estimation of the constant interval. Experiments were made upon seven individuals for intervals extending from 4 to 1.5 sec . The majority of these experiments confirm the general law laid down by Vierordt, but fix the indifference-point between 7 and 8 sec . The remaining, which constitute about one-fourth of the total number of experiments, are called anomalous. In three of the five series of anomalous experiments, the tendency seems to be to bring the value of the indifference-point up to 1 to 1.2 secs.; in the other two, long intervals are prolonged and short ones still further shortened. Wrong decisions were chiefly made for 4 and 5 sec .

Estel (4) and Mehner (5) have extended these investigations, using, practically, the same method, and have incidentally fixed
the value of the indifference-point at 71 sec., as well as shown that the law of Vierordt is applicable, in general, to intervals considerably greater than 1.5 seconds. Their papers, however, deal mainly with the influence of contrast, the multiplicity of the indifference-point, and the validity of Weber's law for the timesense; their valuable conclusions will not be reported, inasmach as the experiments in question do not bear upon them.

From this short and very incomplete account of previous experiments, it will be seen that in all cases the conclusion is drawn, that the natural tendency is to subtract from long intervals and to add to short intervals, in reproducing or estimating them. The conclusion drawn in this paper is exactly the reverse. With reference to the value of the indifference-point, however, my results and those of recent investigators are in harmony.

I have no means of forming an opinion as to the cause of the discrepancy between my own results and those of others. The method used by Wundt's students is entirely different from mine. In one, comparison is made of two intervals, and the process is purely mental; while the other consists in catching an interval and reproducing the same, and, of course, in doing so, certain physiological and psychological moments (the exercise of the will, the origination of motor impulses and their transmission along efferent fibres, and the latent period of muscular contraction), in addition to the mental process, enter into the experiment. Whether these factors enter and, if so, how, or whether (as is barely suggested by the anomalous results) fatigue and inattention may have entered more largely into other methods in a way to account for the previous results, seems to require further study.

I regret that other duties prevent me from continuing the investigation, and I now publish my results, not with the intention of denying outright the correctness of previous conclusions, but with the hope that they will act as an incentive to others to proceed with the work, so as to obtain definite information of the possibly existing factors that are capable of so completely perverting the operations of our time-sense.

Before concluding, I have to thank Profs. G. Stanley Hall and Henry P. Bowditch for their advice and assistance; and also the other gentlemen who have kindly acted as subjects for experiment, or have otherwise assisted me.

## Referonces.

(1) Vierordt: Der Zeitsinnz, (1888) ; cp. Wundt's Phys. Psych., s. 781.
(2) Mach : Wundt's Physiol. Psychol (1te Aufl.), s. 785.
(3) Kollert: Philosophische Studicn, Bd. i., Heft. 1, s. 88.
(4) Estel: " $\quad$ : Bd. ii., Heft. 1, в. 37.
(5) Mehner : " $\quad$ Bd. ii., Heft. 4, s. 546.

Boston, January 10th, 1885.


[^0]:    ${ }^{1}$ See References at the end.
    ${ }^{2}$ In five out of the seven series of experiments to be reported, a tuningfork vibrating 50 times per sec. was used; in the renuaining two series, in order to render the task of counting out the tracings less tedions, a rod making 10 vibrations per sec. was employed.

[^1]:    ${ }^{1} 24$ in number, representing experiments from Cases I., IV., V., VI.
    ${ }^{3}$ The lengths of those detected in the curves obtained from Case I. vary between 63 and 86 min , and averaged 73 min . The average of 15 from Case IV. is 73 min .; of these 12 vary between 62 and 88 min ., and the values of the remaining 3 are $56,1 \cdot 06$, and 91 min . 11 waves from Case V. vary between 62 and 95 min., and average 72 min .9 from Case VI. vary between 61 and 89 min ., and average 73 min .

