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## ON TRAINING THE RECURRENT NEURAL NETWORK ENCODER-DECODER FOR LARGE VOCABULARY END-TO-END SPEECH RECOGNITION

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#### ABSTRACT

Recently, there has been an increasing interest in end-to-end speech recognition using neural networks, with no reliance on hidden Markov models (HMMs) for sequence modelling as in the standard hybrid framework. The recurrent neural network (RNN) encoderdecoder is such a model, performing sequence to sequence mapping without any predefined alignment. This model first transforms the input sequence into a fixed length vector representation, from which the decoder recovers the output sequence. In this paper, we extend our previous work on this model for large vocabulary end-to-end speech recognition. We first present a more effective stochastic gradient decent (SGD) learning rate schedule that can significantly improve the recognition accuracy. We then extend the decoder with long memory by introducing another recurrent layer that performs implicit language modelling. Finally, we demonstrate that using multiple recurrent layers in the encoder can reduce the word error rate. Our experiments were carried out on the Switchboard corpus using a training set of around 300 hours of transcribed audio data, and we have achieved significantly higher recognition accuracy, thereby reduced the gap compared to the hybrid baseline.

**Index Terms**: end-to-end speech recognition, deep neural networks, recurrent neural networks, encoder-decoder.

#### 1. INTRODUCTION

The neural network/hidden Markov model (NN/HMM) hybrid approaches have redefined state-of-the-art speech recognition [1, 2, 3]. In this framework, a neural network is used to estimate the posterior probabilities of HMM states, while the main sequential modelling is carried out by the HMM, incorporating context-dependent phone models, pronunciation models, and language models (LMs). The past few years have seen significant advancements in speech recognition based on this hybrid architecture including using different neural network architectures [4, 5, 6], sequence training [7, 8, 9] and speaker adaptation [10, 11, 12]. However, there has been relatively little focus on the fundamentals of the hybrid architecture. The main advantage of the hybrid approach is that it factorizes the speech recognition problem into several relatively independent subtasks based on a few assumptions and approximations; each module deals with only one of the sub-tasks, thus simplifying the objective. For instance, using neural networks to classify each acoustic frame into one of the HMM states based on the conditional independence assumption is much simpler compared to classifying a set of variable length sequences directly. However, the cost of this divideand-conquer strategy is that it is difficult to optimise all the modules jointly.

Recently, there has been an increasing interest in end-to-end speech recognition using neural networks without using HMM sequence modelling. One approach is based on the connectionist temporal classifier (CTC) that uses a recurrent neural network (RNN) for feature extraction [13], and competitive results have been achieved on a few tasks [14, 15, 16, 17]. CTC does not rely on a prior alignment between input and output sequences, but integrates over all possible alignments during the model training. The alignment is computed by the forward-backward algorithm as part of the model training. The key difference compared to HMMs is that the output labels can be letters or phonemes instead of the HMM states, and it introduces the blank label to discard those frames that are not informative or are noisy when computing the optimal output sequence. However, similar to HMMs, CTC still predicts labels for every frame, and relies on the conditional independence assumption.

Another approach is based on the RNN encoder-decoder which was firstly proposed for machine translation [18, 19], and has been applied to image captioning [20], as well as speech recognition [21, 22, 23, 24]. This model transforms the input sequence of variable length into a fixed dimensional vector representation using the RNN encoder, and the RNN decoder recovers the output sequence from this vector representation. Unlike CTC, this model does not require the alignments between the input and output tokens, and it does not rely on the conditional independence assumption. This model has achieved competitive phoneme recognition accuracy on the TIMIT database [21], and word recognition accuracy on WSJ [23]. Recently, Chan et al [24] obtained good results on the large scale Google Voice Search task. Previously, we investigated this approach for large vocabulary speech recognition on the Switchboard corpus [22], where we focused on architectural and speedup issues for this model. In this paper, we present training strategies that can significantly reduce the word error rate (WER). In particular, we show that improved scheduling of the SGD learning rates can significantly improve the recognition accuracy, and extending the memory of the RNN decoder can further reduce the WER. Finally, using multiple recurrent layers in the encoder can result in a higher recognition accuracy.

#### 2. RNN ENCODER-DECODER WITH ATTENTION

#### 2.1. The model

For sequence to sequence learning, the RNN encoder-decoder directly computes the conditional probability of the output sequence given the input sequence without assuming a fixed alignment. The

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key idea is to introduce the context vector obtained from the RNN encoder as a representation of the input sequence, so that the conditional probability can be approximated as

$$P(y_1, \dots, y_O | \mathbf{x}_1, \dots, \mathbf{x}_T) \approx \prod_{o=1}^{O} P(y_o | y_1, \dots, y_{o-1}, \mathbf{c}_o), \quad (1)$$

$$\mathbf{c}_o = \text{Encoder}(\mathbf{x}_1, \dots, \mathbf{x}_T). \quad (2)$$

$$\mathbf{c}_o = \operatorname{Encoder}(\mathbf{x}_1, \dots, \mathbf{x}_T).$$
 (2)

Note that the context vector  $\mathbf{c}_o$  is updated for each output token  $y_o$ . For speech recognition,  $\{\mathbf{x}_1, \dots, \mathbf{x}_T\}$  is usually a sequence of acoustic feature vectors, while  $\{y_1,\ldots,y_O\}$  is usually a sequence of class indices corresponding to the output units such as phonemes, letters, or words, etc. In practice, the output symbol  $y_0$  is usually represented as a vector  $\mathbf{y}_o$  which may be obtained from an embedding matrix. In the decoder, the posterior probability of  $y_0$  is computed using the softmax function after a recurrent hidden layer which takes both the embedding vector of the previous token  $\mathbf{y}_{o-1}$  and the current context vector  $\mathbf{c}_o$  as inputs, i.e.

$$P(y_o|y_1,\ldots,y_{o-1},\mathbf{c}_o) = \text{Softmax}(\mathbf{s}_o,\mathbf{c}_o)$$
(3)

$$\mathbf{s}_o = \text{Recurrent}(\mathbf{y}_{o-1}, \mathbf{s}_{o-1}, \mathbf{c}_o), \quad (4)$$

The recurrent layer in the decoder performs implicit language modelling, which can explain that the encoder-decoder can work without any language model. The function of the recurrent hidden state  $s_o$ is to remember the current decoding state, and fuse the information from  $\mathbf{y}_{o-1}$  and  $\mathbf{c}_o$ . As shown in 2.2,  $\mathbf{s}_o$  is also used to compute the attention weight in order to obtain the context vector. In the sofmax function Eq. (3), it is possible to remove  $c_0$  from the inputs, however, we obtain lower recognition accuracy (results are not given in this paper), indicating that  $s_0$  cannot capture all the information from  $\mathbf{c}_o$  by one recurrent hidden layer.

#### 2.2. Attention-based scheme

For the encoder-decoder, it is possible to use a global fixed context vector **c** in Eq. (1) as in the machine translation task [25, 18]. However, for long input sequences as in speech recognition, this approach usually does not work, especially when the dimension of c is relatively small. The more effective approach is to dynamically compute the context vector  $\mathbf{c}_o$  given the current decoding state  $\mathbf{s}_o$  by the attention-based scheme [19]. More precisely,  $\mathbf{c}_o$  is obtained as

$$\mathbf{c}_o = \sum_t \alpha_{ot} \mathbf{h}_t \tag{5}$$

where  $\alpha_{ot}$  is the attention weight with the constraint as  $\alpha_{ot} \in [0, 1]$ and  $\sum_t \alpha_{ot} = 1$ .  $\mathbf{h}_t$  denote the hidden state of the encoder RNN which transforms the input feature as

$$\mathbf{h}_t = \text{Recurrent}(\mathbf{x}_t, \mathbf{h}_{t-1}) \tag{6}$$

In this paper, we always use the bidirectional RNN [26] in the encoder, and we then concatenate the forward and backward hidden state as  $\mathbf{h}_t = (\overrightarrow{\mathbf{h}_t}, \overleftarrow{\mathbf{h}_t})$ . Since the conventional RNN only has limited power to capture the sequential information due to the vanishing gradient problem, in this work, we use the gated recurrent units (GRU) [18] in all the recurrent layers.

In Eq. (5), the weight  $\alpha_{ot}$  is computed by a learned alignment model for each  $c_o$ , which is implemented as a neural network such that

$$\alpha_{ot} = \frac{\exp(e_{ot})}{\sum_{t'} \exp(e_{ot'})} \tag{7}$$

$$e_{ot} = \mathbf{v}^{\top} \tanh(\mathbf{W} \mathbf{s}_{o-1} + \mathbf{U} \mathbf{h}_t),$$
 (8)

where  $e_{ot}$  is the relevance score of each hidden representation  $\mathbf{h}_t$ with respect to the previous hidden state of RNN decoder  $s_{n-1}$ . W and U are weight matrices, and v is a vector so that the output of  $e_{ot}$ is a scalar.

Since all the functions used in the encoder-decoder are differentiable, the model can be trained using SGD by maximising the average conditional log-likelihood over the training set as

$$\hat{\mathcal{M}} = \arg \max_{\mathcal{M}} \frac{1}{N} \sum_{n=1}^{N} \log P(y_1^n, \dots, y_O^n | \mathbf{x}_1^n, \dots, \mathbf{x}_T^n, \mathcal{M}),$$

where  $\mathcal{M}$  denotes the set of model parameters, and N is the number of training utterances. Unlike the hybrid model using the feedforward neural networks, this model is more complex in using different types of neural components. It leads to the problem that the dynamic range of the gradients for some weights varies significantly, which makes manually tuning the SGD learning rates challenging. Previously, we used the Adadelta algorithm [27] to aumatically tune the learning rate. However, it is still sub-optimal. The reason is that when we train the recurrent nets, we clipped the gradients as in [28] to avoid gradient explosion, but this makes the Adadelta algorithm unstable. This issue will be further investigated in section 3.

#### 2.3. Long memory decoder

As discussed before, the hidden state  $s_o$  in Eq. (3) has multiple functions, which may not be well realised by just using one recurrent layer. In this work, we investigate to improve the capacity of  $s_o$  by feeding in more informative features, which is again learned by a recurrent net. More precisely, we modify the decoder as

$$P(y_o|y_1, \dots, y_{o-1}, \mathbf{c}_o) = \text{Softmax}(\mathbf{s}_o, \mathbf{c}_o)$$
(9)

$$\mathbf{s}_o = \text{Recurrent}(\mathbf{p}_o, \mathbf{s}_{o-1}, \mathbf{c}_o) \tag{10}$$

$$\mathbf{p}_o = \text{Recurrent}(\mathbf{y}_{o-1}, \mathbf{p}_{o-1}) \tag{11}$$

where we introduce another recurrent layer as in Eq. (11) which only does the implicit language modelling and remembers the decoding history. We then replace  $\mathbf{y}_{o-1}$  by the recurrent hidden state  $\mathbf{p}_o$  as in Eq. (10) so that hidden state  $s_o$  can receive more information of the decoding history from the input features. This decoder is expected to have longer memory, and may work better without the language model. It is also possible to feed  $\mathbf{p}_o$  into the sofxmax layer as

$$P(y_o|y_1,\ldots,y_{o-1},\mathbf{c}_o) = \operatorname{Softmax}(\mathbf{s}_o,\mathbf{c}_o,\mathbf{p}_o), \tag{12}$$

however, it may over-weight the role of  $\mathbf{p}_o$ , and may not be suitable for the task of conversational speech recognition investigated in this paper, where the language pattern is more irregular.

#### 2.4. Comparison to CTC

CTC [13] does not directly compute the conditional probability of the output sequence given the input sequence. Instead, it compute the posterior probability of the label  $l_t$  for every frame  $\mathbf{x}_t$  similar to the hybrid model. In the case of using bi-directional RNN to transform the acoustic feature  $x_t$ , this probability is computed using only the softmax function without recurrent layer as

$$P(l_t|\mathbf{x}_t) = \operatorname{softmax}(\overrightarrow{\mathbf{h}_t}, \overleftarrow{\mathbf{h}_t}). \tag{13}$$

Since the classification is performed on the per-frame level, CTC needs to compute the alignment between the acoustic frames and output labels as part of the model training, and as observed in [14],

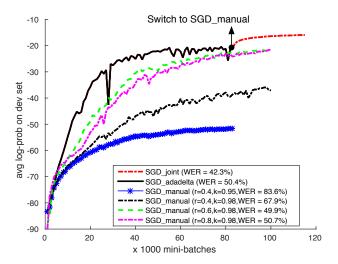


Fig. 1. Comparison of scheduling the SGD learning rate for training the RNN encoder-decoder. The results were obtained by using 24 dimensional FBANK static features. r denotes the initial learning rate and k is the learning rate decay factor. Since we have a large training set, we decay the learning rate for every 1000 mini-batches by a small factor as this is more stable and efficient compared to decaying the learning rate by a large ratio for every epoch.

it may be sensitive to the initial alignment. In order to guarantee that he lengths of the input and output sequences are the same, CTC replicates the output labels so that a consecutive frames can correspond to the same label. It then applies a rule to collapse the replicated labels during the decoding, while the RNN decoder does not have this problem. Finally, CTC still requires the independence assumption of the acoustic frames, which is not required in the RNN encoder-decoder approach.

#### 3. RESULTS AND DISCUSSION

#### 3.1. System setup

We report results using the Switchboard corpus of [29] released by LDC with the catalog number as LDC97S62. It has a 300 hour training set, and we show separate results for the Callhome English (CHE) and Switchboard (SWB) evaluation sets. The vocabulary size is around 30,000, and the number of training utterances in Switchboard is 192,701. In this work, we evaluated both the mel-frequency cepstral coefficients (MFCCs) and log-mel filterbanks (FBANKs) as acoustic features, which were obtained using the Kaldi toolkits [30]. In the frond-end, we performed the mean and variance normalisation on the per-speaker basis before we concatenating the features by a context window  $\pm 5$  frames. Following our previous practice [22], we uniformly subsample the spliced features for each utterance by a ratio of 1/3, which can significantly speedup the training. Interestingly, subsampling was also applied in the CTC-based system and it improved the recognition accuracy in [14]. In our experiments, the number of hidden units in the RNN encoder is 1000 unless specified otherwise, and the mini-batch size is 30 utterances.

#### 3.2. SGD learning rate

Manually searching the SGD initial learning rate and the learning rate decay factor — referred to SGD\_manual — may be expensive

**Table 1.** Comparison of SGD\_adadelta and SGD\_joint to schedule the SGD learning rates.

SGD learning rate	Feature	CHE	SWB	Avg
SGD_adadelta [22]	MFCC	59.9	38.8	49.4
SGD_joint	MFCC	55.0	36.2	45.6
SGD_adadelta	FBANK	56.8	34.7	45.8
SGD_joint	FBANK	48.2	26.8	37.6
SGD_joint	FBANK(static)	52.2	31.8	42.1

to train the model, In addition, the hyper-parameters may change when using different type of features and model configrations. Previously, we applied the Adadelta algorithm [27] to automatically tune the learning rate [22]. However, we found that it does not lead to the optimal solution similar to the observation in [21]. As discussed in Section 2.2, the Adadelta algorithm relies on the gradient to set the learning rate, however, in oder to tackle the gradient explosion problem in training the RNNs, we clipped the gradient which makes the Adadelta algorithm unstable. To address this problem, the authors in [21] proposed an approach to fix the gradient before applying Adadelta. In this work, we use the SGD\_joint approach, where we first run the Adadelta algorithm until convergence that usually takes around 10 - 15 epochs for our task, and we then switch to SGD\_manual with small initial learning rate (e.g. 0.01 - 0.02 used in this paper) to run another few epochs to fine tune the model. As shown in Table 1, we can achieve significant WER reduction by the fine tuning. Note that in these experiments, we used words as the output units in the softmax function in Eq. (3).

We also compared two different type of acoustic features, i.e. 39 dimensional MFCCs and 45 dimensional FBANKs both with delta and delta-delta coefficients. Note that in both cases, we spliced the features with the context window of  $\pm 5$ . Compared to the hybrid systems [31], we obtained much larger gains by using FBANK features, possibly due to that transforming the features by discrete cosine transform (DCT) in MFCCs makes it more difficult for RNNs to learn the sequential patterns. Since RNN can perform long temporal modelling and we have used long context window for feature splicing, we also did experiment with static FBANK features to evaluate if the dynamic features is still useful. Contrary to our exception, we obtained significantly higher WER without the dynamic features. In Figure 1, we increased the number of filterbanks from 15 to 24. We also show the convergence graphs of the three approaches to schedule the SGD learning rates. Again, SGD\_joint achieved much better result compared SGD\_adadelta, and it converges much faster then SGD\_manual. However, we did not obtain better results by using larger number of filterbanks. In the following experiments, we used 45 dimensional FBANKs with dynamic coefficients as features, and trained the model using SGD\_joint optimisation algorithm.

#### 3.3. Results of long memory decoder

We then evaluate if the long memory decoder approach discussed in section 2.3 can enhance the implicant language model and result in WER reduction. In our experiments, we set a smaller number of hidden units in recurrent layer in Eq. (11) which is 300, which is much smaller than the dimension of  $\mathbf{c}_o$ . The intuition is to emphasise the role of the context vector in the decoder hidden state in Eq. (10). As shown in Table 2, the long memory decoder described as Eq. (9) - (11) can improve the recognition accuracy by 1% absolute in case of using words as output units. However, the decoder as Eq. (12) did not work better, and we suspect that it is because the decoder may be biased toward the implicit language model. We then rescored the

**Table 2.** Results of language model rescoring and using long memory decoder. LongMem1 is referred to Eq. (9), and LongMem2 is referred to Eq. (12).

System	Output	CHE	SWB	Avg
EncDec no LM	word	48.2	26.8	37.6
EncDec + 3-gram rescoring	word	47.4	26.2	36.8
EncDec + LongMem1	word	46.5	26.3	36.4
+ 3-gram rescoring	word	46.0	25.8	36.0
EncDec + LongMem2	word	47.1	27.3	37.3
+ 3-gram rescoring	word	46.4	26.5	36.5
EncDec no LM	char	52.7	32.8	42.8
EncDec + 5-gram rescoring	char	51.9	32.6	42.3
EncDec + LongMem1	char	51.6	30.9	41.3
+ 5-gram rescoring	char	50.4	30.5	40.5

n-best list from the model using a 3-gram language model which was trained on Switchboard and Fisher transcriptions using the KenLM tookit [32]. However, we only obtained small improvement. Here, the size of n-best list to be 32, and similar to the observation in [24], increasing the size of n-best list did not further reduce the WER.

There are several problems of using word level output units, e.g. it can not generalise to words that are in the training set, and it may not work well for the low frequency words in the training set. In addition, for large vocabulary tasks, it has large number of model parameters in the softmax layer which may slow down the model training. Another approach is to use phonemes or characters as the output units. In this work, we prefer to use the characters so that we do not need to reply on the pronunciation dictionary, and it is possible to generalise to out-of-vocabulary words. The number of characters in our system is 35 including symbols as hyphen, slash, space, etc, and tokens corresponding to the noise as [noise], [vocalized-noise], [laughter]. In our experiments, we observed that the character level encoder-decoder model is more expensive to train since the lengths of the output sequences are much longer, which introduces more iterations to estimate the attention weights in Eq. (7). We also observe the character baseline system is worse than the corresponding word level system as predicting a longer output sequence is more challenging without any constraint. However, the long memory decoder can still bring more than 1% absolute again in this case.

#### 3.4. Depth of the encoder

In the previous experiments, we have only used 1 layer of RNN in the encoder after 1 hidden layer of feedforward neural network for feature extraction. In [22], we show that having more hidden layers in the feedforward neural network does not reduce the WER significantly. In this work, we investigate if having multiple layers of RNN in the encoder can improve the accuracy. As this will significantly increase the model size, limited by the size of the GPU memory, we only did the experiments with characters<sup>1</sup>. The results are given in Table 3. We observed that using multiple RNN layers in the encoder can significantly improve the recognition accuracy. However, the gain is smaller for the model with 1000 hidden units, which may be due to overfitting. As we mentioned before, we used the GRU [18] in all the recurrent layers which has 4 additional weight matrices compared to the conventional RNN that controls the forget and input

Table 3. Results of using multiple RNN layers in the encoder.

System	Output	Dim	CHE	SWB	Avg
EncDec – 1 layer	char	1000	52.7	32.8	42.8
EncDec – 2 layer	char	1000	50.3	29.1	39.7
EncDec – 1 layer	char	500	54.1	34.5	44.4
EncDec – 2 layer	char	500	48.4	28.8	38.7
EncDec – 3 layer	char	500	48.2	27.3	37.8

**Table 4.** Comparison to CTC and DNN-HMM hybrid systems. In [17], the LMs were trained using a corpus of 31 billion words, while in [16, 8], the LMs were trained using the Switchboard and Fisher transcriptions.

System	Output	CHE	SWB	Avg
DNN-HMM sMBR [8]	-	24.1	12.6	18.4
CTC no LM [17]	char	56.1	38.0	47.1
CTC+5-gram	char	47.0	30.8	39.0
CTC+7-gram	char	43.8	27.8	35.9
CTC+NNLM (1 hidden layer)	char	41.1	23.4	32.3
CTC+NNLM (3 hidden layers)	char	39.9	21.8	30.9
CTC+RNNLM (1 hidden layer)	char	41.7	24.2	33.0
CTC+RNNLM (3 hidden layers)	char	40.2	21.4	30.8
Deep Speech [16]	char	31.8	20.0	25.9
EncDec no LM	word	46.5	26.3	36.4
EncDec no LM	char	48.2	27.3	37.8

gates respectively. Having one more layer of GRU-RNN can significantly increase the number of model parameters, especially in the case of bi-directional RNN as in this work. After reducing the number of hidden units to be 500, we can achieved significantly lower WER with multiple RNNs in the encoder. In the future, we shall evaluate the long memory decoder with multiple of RNN layers in the encoder.

#### 3.5. Comparison to CTC

In Table 4, we compare our results to those obtained using CTC reported in [16, 17] using the same dataset. In the CTC systems [16, 17], a strong LM was applied during the decoding, and according to [17], the LM can significantly improve the recognition accuracy of CTC. Without any LM, the encoder-decoder approach can achieve much higher recognition accuracy compared to CTC, however, we can only obtain marginal improvement by LM rescoring. In the future, we shall incorporate the LM into the decoder. We also refer to the publicly reported hybrid baseline in [8]. We see that there is still a big gap between the end-to-end and hybrid systems on this dataset, but we also note that in [14], CTC outperformed the hybrid baseline on the Google voice search task.

#### 4. CONCLUSIONS

In this paper, we present the improvements obtained for the RNN encoder-decoder based end-to-end speech recognition on the large vocabulary task. We show a simple yet efficient and effective approach to schedule the SGD learning rates which achieves large gain in our experiments. In principle, the encoder-decoder approach does not need to rely on a language model given enough training data, and we proposed an approach to extend the decoder with long memory to enhance its power for implicit language modelling. Finally, using multiple recurrent layers in the encoder can significantly reduce the WER. In the future, we shall investigate using multiple recurrent layers and incorporating a language model in the decoder.

Training this model requires large memory since all the hidden states  $(\overrightarrow{h_t}, \overleftarrow{h_t})$  for each frame in a minibatch are kept in the memory in order to dynamically compute the context vector  $\mathbf{c}_o$ .

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