

Opinion Dynamics and Communication Networks

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Abstract

This paper examines the interplay of opinion exchange dynamics and communication network formation. An opinion formation procedure is introduced which is based on an abstract representation of opinions as k -dimensional bit-strings. Individuals interact if the difference in the opinion strings is below a defined similarity threshold d_I . Depending on d_I , different behaviour of the population is observed: low values result in a state of highly fragmented opinions and higher values yield consensus. The first contribution of this research is to identify the values of parameters d_I and k , such that the transition between fragmented opinions and homogeneity takes place. Then, we look at this transition from two perspectives: first by studying the group size distribution and second by analysing the communication network that is formed by the interactions that take place during the simulation. The emerging networks are classified by statistical means and we find that non-trivial social structures emerge from simple rules for individual communication. Generating networks allows to compare model outcomes with real-world communication patterns.

Introduction

Many societal processes are ultimately based on the mutual interactions among individuals with diverse opinions, attitudes and lifestyles. The processes of inter-personal communication and opinion exchange play a crucial role in the formation of social structures and networks. Examining the interplay of opinion exchange and communication network formation is the main issue addressed by this study.

Therefore, an opinion formation model inspired by the abstract agent model presented in [6] is introduced. Opinions are represented as a series of k bits, which we find an interesting approach to the modelling of attitudes and beliefs, since human thinking can be represented in terms of polarities (yes/no, good/bad, young/old, etc.). And moreover, we are used to measuring information in bits.

Such an abstract bit-string approach has been used in the simulation of consumer-producer behaviour [6] as well as in the context of labour market analysis [5] where bit-strings represent products (or job offers) and needs (worker skills). Here, each bit-string represents an agent opinion and a procedure of agent-agent interaction is specified based on assumptions from social comparison theory [15] and in opinion formation models [7, 12, 3, 26, 27].

This paper is organized in the following way. We start reviewing previous approaches to the modelling of opinion exchange dynamics. After this, we give an explanation of our model. This is followed by a numerical analysis, in which the opinion evolution is considered before looking at the emerging networks of communication activity. A discussion of the results concludes this work.

Related Work

The most important observation from studying computer models of social influence and opinion dynamics is probably that interaction rules by which interacting agents tend to become more alike in their beliefs do not necessarily lead to a population in which all the individuals share the same opinion. To put it in Axelrod's words ([7], p.223): »Local convergence can lead to global polarization.« This dynamic effect which contrasts common intuition has been shown and analysed in a large number of different opinion formation models (e.g., [7, 10, 12, 26, 3, 18]).

All these models are based on two principles: (1.) two individuals are more likely to communicate with one another if they already share a number of opinion features (i.e., their opinions are similar); and (2.) communication further increases this number of shared features (i.e., individuals become even more alike). Approaches differ mainly in their representation of opinion. Some models use continuous representations (e.g., [12, 3]) whereas others assume opinions to be a set of features which can take different (discrete) values [7, 10]. Also populations in which agents may have only two possible choices (yes/no) have been studied frequently (e.g., [26, 16, 29, 30, 19]).

Depending on the control parameters, opinion models give rise to quite a variety of population structures, from a highly fragmented population in which only few individuals share the same opinion, to homogeneity or, in between these two regimes, to a stable state with several differently sized groups. These three *behaviour classes*¹ have been reported in several previous studies on opinion dynamics (e.g., [7, 10, 12, 26, 3, 18, 30]). Moreover, in the transition regime, group sizes were found to follow a power law distribution [10]. For a detailed report with particular focus on such statistical properties of social dynamics processes the reader is referred to [9].

The social network structure which is assumed to underlie the opinion exchange dynamics is another important aspect. In opinion formation studies as well as in other disciplines, often a static network determining which agents may interact with one another is imposed. In social influence models this is referred to as an agent's neighbourhood. Only recently, the co-evolution of agent states and networks formed by processes (based on the states) receive more attention

¹Behaviour classes refer to qualitative different behaviours that potentially result from a simulation model.

(see [17] for an inter-disciplinary, recent review). Simultaneously, adaptive network approaches that focus on the interplay of opinion dynamics and network formation have been further developed [18, 30, 25, 4].

In reference [18], a parameter is used to determine whether agents form their opinion based on the opinions of connected agents or if they re-link to an agent having the same opinion. This simple model was found to undergo the same phase transition from diverse to homogeneous opinions as reported above. The effect of giving agents the possibility of cutting links, if they do not achieve agreement with their neighbours, is also studied in [30]. The study presented in [4] starts from a random network determining the possible communication links between the agents. The similarity between two linked agents (which evolves in time since the opinions of interacting agents are updated) is used to assign a frequency of interaction. In this way, dynamic network structures emerge without the need for specifying conditions for cutting social links.

In this paper, we also avoid introducing further assumptions for re-wiring the network. Instead, the network design is based on the communication that effectively takes place among the agents.

Model Definition

The opinion formation model implemented for this study bases on a bit-string representation as used in [6] concerning the simulation of consumer-producer behaviour and in [5] for the analysis of labour market dynamics. In these examples, bit-strings represent products (or, respectively, work offers) and needs (skills). The exchange is based on the matching of these two strings. Here, this concept is used in the modelling of opinion exchange where a series of k bits represents an agent opinion, and interaction between agents takes place if their opinion strings are similar. Two agents are willing to interact with one another if the matching of their opinion strings is below (or equal to) a certain similarity threshold denoted by d_I . The interaction process is illustrated in Fig. 1.

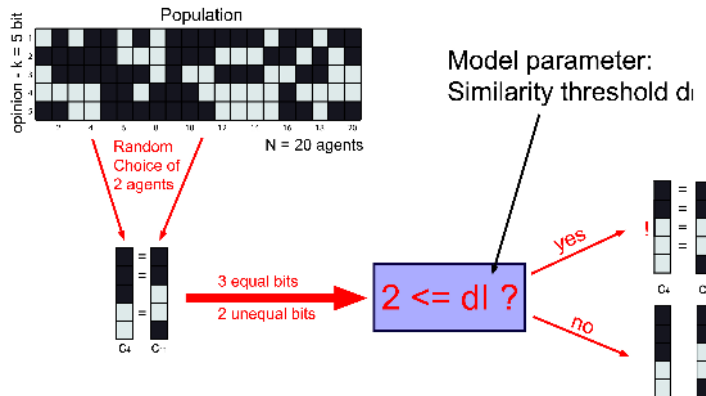


Figure 1: Illustration of the interaction process.

In the beginning N agents are generated and a random bit-string is assigned to them. In the interaction process, two agents, say c_4, c_{11} according to Fig. 1, meet at random. But they are only willing to communicate about an issue (one

element of the bit-string), if the number of unequal bits (i.e., the hamming distance h) is below or equal to a similarity threshold d_I . If the hamming distance between the two agents is below the threshold ($h(c_4, c_{11}) \leq d_I$), they exchange ideas about an issue. As a result of that the agent chosen first (c_4 in the example) adopts the opinion of the c_{11} concerning that issue by flipping the respective bit.² In this way the principles of similarity and imitation which form the basis of most opinion models (e.g., [7, 10, 12, 26, 3, 18]) are integrated.

The model is implemented so that during a single time step all the agents have the chance to interact with one another. Therefore one time step of the model corresponds to N interactions of pairs of randomly chosen agents c_i, c_j . We exclude self-interaction ($c_i = c_j$), but we do not force all agents to be chosen exactly one time (with the result that some may be chosen twice and other ones are not chosen at all in that iteration).

In order to understand better the opinion exchange dynamics among the agents, we keep track of the interactions that take place in the course of the simulation. We introduce an interaction matrix I which stores all the interaction activity. I is of size $N \times N$ and the element i_{ij} saves the number of times c_i and c_j interacted in some way. Therefore, each time two chosen agents c_i, c_j are sufficiently similar ($h(c_i, c_j) \leq d_I$), we increase i_{ij} and i_{ji} by one. Note that i_{ij} and i_{ji} are also increased if agents already share the same opinion. The matrix I corresponds to a weighted graph, in which edges represent the communication lines between different agents. Additional information about who imitates who, and which agents are imitated is stored separately.

To summarize. Starting from an initial random population, at each time step N pairs of agents (c_i, c_j) are chosen, and if the distance is below the threshold ($h(c_i, c_j) \leq d_I$), the agent c_i switches one of the bits that have been unequal. In other words, if individuals are close enough they have the opportunity to become even closer. Otherwise, they just do not communicate at all. As they split apart groups are formed. In the next section, we discuss the characteristics of the groups that emerge from this process.

Behaviour Classification

In order to obtain a classification of the general dynamic behaviour of the model, a series of systematic tests has been performed. For this purpose, we looked at different numbers of dimensions k used in the opinion representation and respectively different threshold values d_I . Note that considering the ratio of the two parameters $\frac{d_I}{k}$ might also be of interest, since it accounts for the relative similarity required for two agents to interact. It would also be favourable as the number of model parameters would be reduced.

However, in order to be clear about the interdependence of the two parameters, we first tested all the configurations $k = 1 \dots 32$ and respectively $d_I = 1 \dots k$, and looked at the number of groups of individuals that share exactly the same opinion (denoted by N_G). A group in this sense can be formalized as

$$G_o = \{c_i : h(c_i, o) = 0\}, \quad (1)$$

²Since the probability of an agent to be the first one is equal for all individuals during the iteration process, all the agents have an equal chance to imitate or to be imitated. The same assumption about who imitates who is made by Axelrod in [7].

where o is the reference opinion string shared by all the members c_i of the group G_o . A particular group G_o comprises all the agents c_i , whose opinions equals o , (that is the hamming distance $h(c_i, o) = 0$). Consequently, N_G is defined as the number of groups G_o with at least one member. With groups defined in this way, the maximum number of possible groups is

$$\max(N_G) = \min(N, 2^k). \quad (2)$$

As opinions are represented as a series of k bits, there are 2^k possible opinion strings. But in the case that the number of agents is below that number ($N < 2^k$), then the maximum number of groups with at least one member is equal to N (i.e., $\max(N_G) = N$).

The model behaviour can be classified by using N_G as an indicator for different kinds of behaviour. The case where N_G is near the theoretical maximum ($N_G \approx N$ or respectively $N_G \approx 2^k$ as described above) represents the cases in which the public opinion remains highly fragmented, since there are many groups with only few members (or even just a single one). The other extreme is represented by $N_G = 1$ in which case all the agents belong to a single giant group, that is: the society of agents reaches global consensus.

In Fig. 2 this classification of the model behaviour with respect to k and d_I is shown using a 32×32 parameter grid formed by $k = 1 \dots 32$ and $d_I = 1 \dots k$. $N = 1000$ agents have been used for the experiments and five simulation runs have been performed for each parameter configuration.³ The two additional grids represent the iteration number required to reach the stable state (middle) and the variance of N_G (r.h.s) observed over the five realizations. Note that the stable state, in which no further opinion exchange is possible, is always reached, though the number of iterations required to reach it differs tremendously.

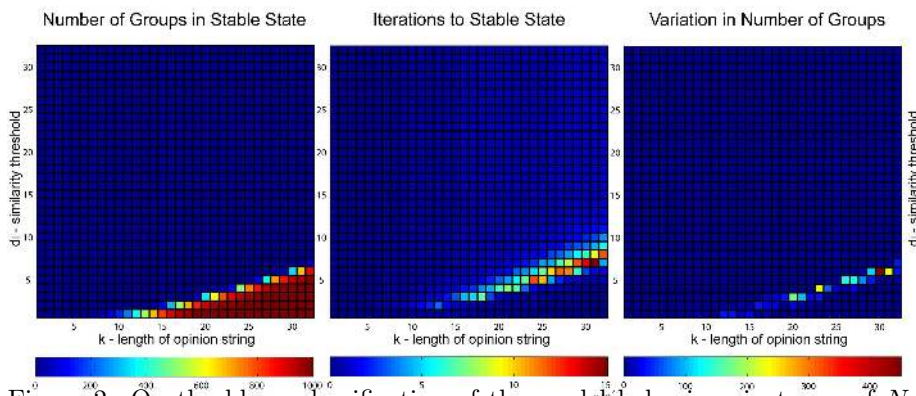


Figure 2: On the l.h.s., classification of the model behaviour in terms of N_G with respect to k and d_I for 1000 agents. The middle image shows the iteration number required to reach the stable state, and on the r.h.s. the variation of N_G is shown. Average of 5 simulation runs.

Fig. 2 makes clear that a transition takes place from a population in which all opinions are the same (blue region with $N_G \approx 1$) to a population in which basically all the agents have different opinions (dark red with $N_G \approx 1000$). The third and in fact most interesting behaviour is observed in the area of transition

³On the whole, 5×528 runs with $N = 1000$ agents have been performed.

in between these two extremes. It will be considered using a specific parameter constellation in the following section.

Group Size Distribution

In order to get a better idea of the model behaviour in transition, we concentrate on the example $N = 1000$ and $k = 20$ in the following two sections. The influence of the population size N is studied after that. From the images in Fig. 2 we assume that the critical behaviour can be observed for $d_I = 3$, where an average number of groups $N_G \approx 400$ was found with a very high variance. In a second series of systematic experiments, now using 100 simulation runs, we subsequently increase the threshold from $d_I = 1 \dots 5$ and look at the distribution of group sizes in stable state. The results are presented in Fig. 3.

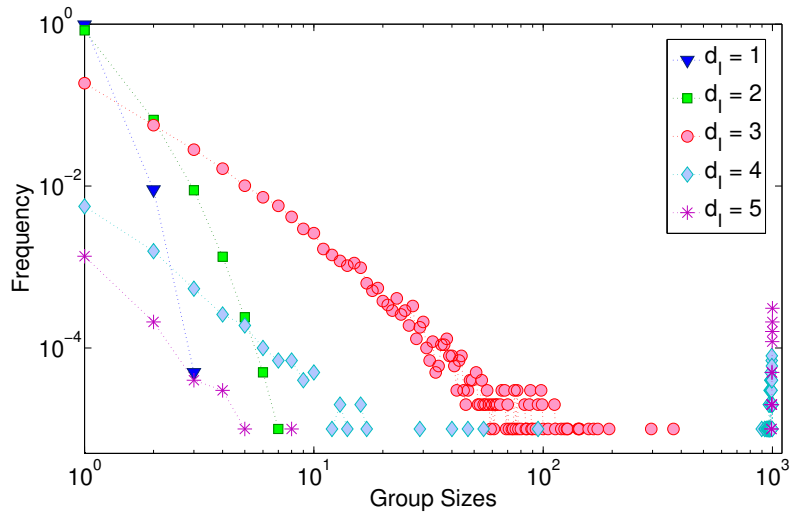


Figure 3: Group size distribution in stable state for $k = 20$ and $d_I = 1 \dots 5$ based on 100 simulation runs.

It becomes clear that, for $N = 1000$ and $k = 20$, $d_I = 3$ is indeed at the border between the two qualitatively different behaviours: homogeneity and fragmentation. It therefore displays the model behaviour in the phase transition. Moreover, Fig. 3 shows that groups scale according to a power law for $d_I = 3$, which was also reported in the phase transition of the Axelrod model in [10].

For $d_I < 3$ only very small groups are present, whereas for $d_I > 3$ the likeliness of small groups to form subsequently decreases and agents are very likely to meet in a single giant group (global consensus). Note, however, that for $d_I = 4$ several intermediate group sizes are also observed that show a power law scaling for group sizes up to 20 members.

Communication Networks

The analysis of the groups that consist of individuals sharing the same opinion is an interesting issue, looking at the communication activities that led to this

state, on the other hand, can reveal important additional information of how a certain state is reached. From the network point of view, we can consider that agents are the nodes of a communication network and that edges represent communication lines. In order to keep track of the communication activity within such a network, we introduced the interaction matrix I which stores all the interactions that take place in the course of the simulation. We also compute the adjacency matrix A , the elements of which are $a_{ij} = 0$ if $i_{ij} = 0$ and $a_{ij} = 1$ if $i_{ij} > 0$. Matrix A accounts for communication lines between the agents, but not for the intensity (i.e., the frequency) of communication between them.

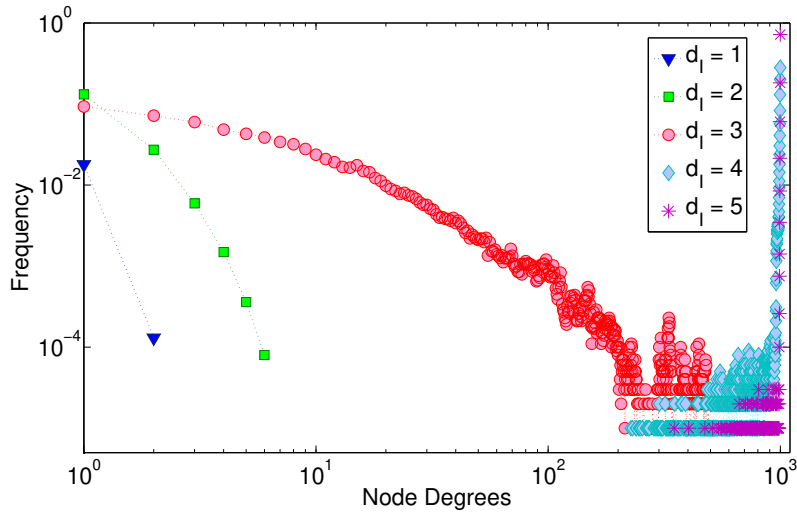


Figure 4: Log-log plot of the degree distribution for $N = 1000$, $k = 20$, and different $d_I = 1 \dots 5$. The distribution for $d_I = 3$ displays the behaviour in the phase transition.

In Fig. 4 the degree distribution of the communication network computed on the basis of A is visualised. Degree distributions are used frequently in the classification of complex networks (e.g., [2, 8, 17, 13]). The data displayed in Fig. 4 represents the same 100 realisations performed for the group size analysis shown in Fig. 3.

The distribution shows that for $d_I = 1$ the frequency with which node degrees of one or two (represented by the blue triangles) have been observed is around 0.02, which makes clear that the great majority of the nodes has a zero degree, i.e., they are isolated nodes. For $d_I = 2$, still, the majority of nodes is isolated, but there are agents connected to up to six others. All in all, for low values of d_I the differences between the agents maintain, because initially, the distance between most agents is larger than d_I . Therefore, interaction becomes unlikely and the communication network is very weakly connected.

The degree distributions for $d_I = 4$ and $d_I = 5$ are quite different from the prior examples. They display the characteristics of a highly connected (quasi-complete) network. In the course of 100 simulations no node with a degree below 200 was found which means that the weakest connected agent is still connected to more than 200 other agents. Moreover, the larger d_I is chosen, the more close

the final network is to the complete graph.⁴ This is because potentially all the agents are allowed to interact with all the others (complete graph), and with an increased threshold value more of these interactions really take place since the condition $h(c_i, c_j) \leq d_I$ is more likely to be satisfied.

An interesting property is observed when comparing the degree distribution for $d_I = 4, d_I = 5$ to the group size distribution in Fig. 3 as it results using the same values d_I . As shown in Fig. 3, small minority groups of agents may form in these cases, although these agents interacted with at least 200 others (as we know from Fig. 4), i.e., they are not isolated at all. We conclude that intensive communication behaviour does not automatically make agents adopt the opinion of the largest group, agents (or small groups of agents with up to ten members) may have an individual »outsider« opinion even though the communication activity involved many agents from different groups.

From the network point of view the phase transition from highly fragmented opinions to global consensus as reported above now becomes the transition from a weakly connected network (i.e., reduced communication activity for $d_I = 1, 2$) to a complete network (in which all the agents communicate with all the others for $d_I = 4, 5$). The degree scaling behaviour in between these two regimes ($d_I = 3$) represents the model behaviour in the phase transition.

The distribution of the degrees for $d_I = 3$ as shown in Fig. 4 displays the characteristics of a non-trivial network structure (compare also the network shown in Fig. 8). The distribution is significantly different from distributions found in random networks. Fig. 4 indicates that the scaling of the degrees is according to a power law, at least for the upper tail with degrees below 100. This means that the network is scale-free. For connectivities around 100 slight deviations are visible and for degrees in the region from 300 to 500 we cannot any longer assume a power law behaviour.

Further analysis using a larger number of experiments⁵ might reveal the reasons for these irregularities, and they will also make us more confident about the power law distribution indicated by Fig. 4. Another equally important issue to provide us with a more complete picture of the model behaviour is the influence of the populations size.

Influence of the Population Size

In order to be able to compare the model outcomes for realizations using different numbers of agents (N), it is convenient to use the relative number of groups after stabilization given by $\frac{N_G}{N}$. In the case of opinion fragmentation $\frac{N_G}{N} \approx 1$ since $N_G \approx N$. In the case a global consensus is reached we have $N_G = 1$ and therefore $\frac{N_G}{N} = \frac{1}{N} \approx 0$. For the intermediate states the relative number of groups stays between zero and one ($0 < \frac{N_G}{N} < 1$).

In the l.h.s. of Fig. 5, the relative number of groups in stable state is shown for $N = 100, 500, 1000, 5000$ and 10000 as a function of the threshold d_I . In all simulations an opinion string of length $k = 20$ is used. Each data point in Fig. 5 represents the average of $\frac{N_G}{N}$ determined over 10 repeated simulation runs. Let's call d_I^* the threshold values at which the transition from fragmentation to consensus takes place. With each increase of the population size from $N =$

⁴For $d_I = 6$ the percentage of node degrees smaller than 900 was 0.08%.

⁵In the physics literature (e.g., [10, 18]) often 10^4 realizations are used.

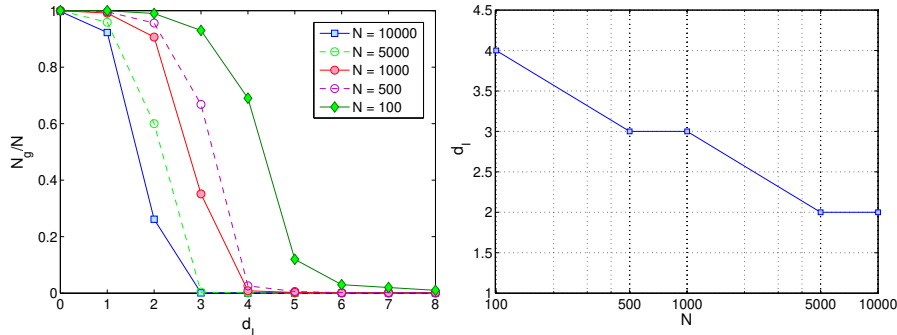


Figure 5: Dependence of the model behaviour on the population size N . L.h.s.: The relative number of groups after stabilisation ($\frac{N_g}{N}$) is shown for different population sizes N . R.h.s.: The critical values d_I^* at which transition behaviour is observed with respect to the population size. Results for 10 realizations and $k = 20$.

100 to $N = 10000$ the values at which transition behaviour is observed (d_I^*) decreases.

The r.h.s of Fig. 5 makes this clear. It shows the »critical« values d_I^* as a function of the population size. For a certain N , d_I^* has been chosen to correspond to those 10 repeated simulation runs in which the variance in the values of $\frac{N_g}{N}$ is maximal, as a high variance is a suitable indicator for transition behaviour (compare also Fig. 2). The r.h.s of Fig. 5 shows the decrease of the d_I^* with the population size N . Note the logarithmic scale used for the number of agents N on the horizontal axis. As the N grows 10 times larger, the critical threshold decreases by one.

In Fig. 5 the influence of N on the model behaviour is evaluated on the basis of the average value and the variance of a series of relative numbers of groups, $\frac{N_g}{N}$. A further interesting aspect is the influence of the population size on the group sizes in stable state and the interaction network formed as the result of the opinion exchange process. For $N = 1000$, $d_I = 3$ and $N = 10000$, $d_I = 2$ (both displaying the characteristics of transition behaviour) the group size and the degree distributions are presented and compared in Fig. 6.

We observe in Fig. 6 that there is no remarkable difference between the groups formed in a population of 10000 agents compared to the example of 1000 agents considered previously. The degree distribution shown in the inset of Fig. 6 displays the same scaling behaviour for both cases as well. This indicates that in the phase transition the observed interaction patterns as well as the statistical properties of the grouping behaviour after stabilisation is invariant to changes of the population size. Moreover, observing the same power law scaling of the degrees for $N = 1000$ and $N = 10000$ confirms that the opinion exchange process as presented in this paper yields scale-free communication networks.

The observed power law scaling can be an interesting issue for the validity of the model, since such a behaviour is shown to be a property of many real-world networks (compare [2, 8, 11, 23, 22, 20]). The invariance of the communication patterns to the population size N (as indicated by Fig. 6) is another important issue for the comparison with real-world network data, since empirical network studies often consider a large number of participants (up to several millions).

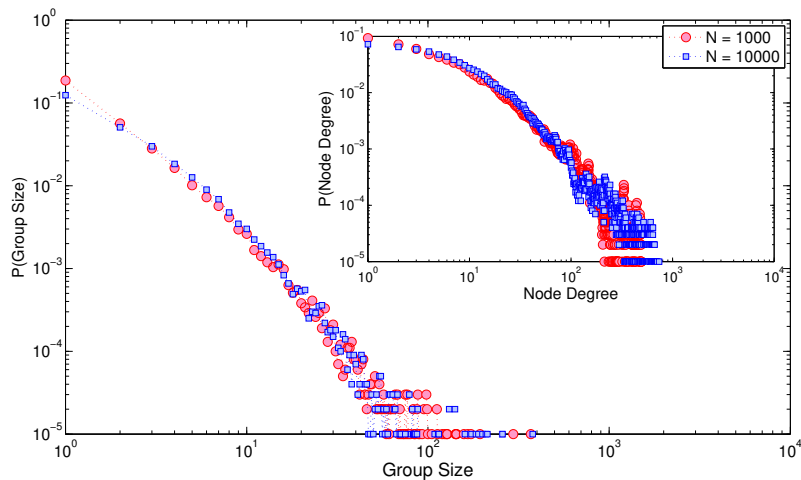


Figure 6: Group size and degree (inset) distributions for $N = 1000$, $d_I = 3$ and $N = 10000$, $d_I = 2$ with $k = 20$ in both cases. The distributions for $N=1000$ and $N=10000$ are based on, respectively, 100 and 10 repeated simulation runs.

Networks as a Link to Reality

Recently, a critical account by Sobkowicz ([28]) revealed that among the vast literature on opinion formation models, there are very few attempts to link the simulation results to real-world data. The main reason for this is that high-quality data of opinion spread in real societies is not available. However, recent analyses of real-world communication networks ([23, 22, 20]) have led to a better understanding of human communication activity. The network view on opinion exchange processes introduced in this paper, enables that simulation outcomes be compared to this new insights. This may be of great value in the refinement and calibration of opinion models.

One example of networks that can be adequate in the comparison are phone call networks (e.g., [1, 23, 22]). As in our model, these networks are constructed by one-to-one communication. In [23] and [22], Onnela et al. extensively analyse the structure of a mobile phone network constructed by observing the communication activity of several million users during 18 weeks. They explain that the data serves as »a proxy for the underlying social network« ([23], p. 3) and therefore of human communication patterns. For any opinion model to be of explanatory value (as an explanatory candidate in the words of Epstein [14]), it is necessary that realistic network structures (macro-behaviour) are formed by the interaction process implemented in the model, so that simulated communication patterns compare to the real-world exchange processes.

In a qualitative sense, the degree distributions of the interaction networks in the phase transition shown throughout this paper (Fig. 4 and 6) relate to observations made on real-world communication networks. A scaling according to a power law as shown for call graphs by Onnela et al. in [23, 22] (compare Fig. 1A in [22]) as well as by Aiello et al. in [1] (Fig. 1 and 2), is observed in the present model of opinion exchange. Another confirming observation is the percentage of nodes in the largest connected component. In the mobile

network study ([23, 22]) it consists of 84% of the nodes and in our networks this percentage is found to be in between 75 and 85%. The qualitative similarity may be a useful starting point for future calibration of the opinion model.

One has to take into account in such a comparison that the real-world examples consist of several millions of nodes (e.g., 3.9 million in [23, 22]) and that the largest network created in the course of this study has (only) 10000 participants. However, as the previous section revealed, the degree scaling did not change with an increasing population size.

The emergence of very complex, non-trivial social structures from simple opinion exchange processes becomes also visible in the example network presented at the very end of this paper (in Fig 8). Agents do not have any knowledge of the global properties of the network nor is there any routine by which they urge to improve their position in the network. Nevertheless, we observe the formation of various clusters that among themselves are strongly connected, and also the emergence of individuals that connect between different clusters becomes visible. Having a high centrality, but only a small number of social contacts to sustain, such nodes are considered to have a high importance in the social network (compare [17] and references therein).

While the generation of networks provides us with the possibility of linking the simulation model and reality at the level of global structure, the use of bit-strings in the opinion representation allows for a connection of agent opinions and real survey data. For instance, questions like »are you currently satisfied with the work of politician X?« or »which of the following issues you think should be regulated/not regulated by the government?« can be used to set up an agent population with opinions distributed according to the results of a questionnaire. Repeated surveys might even allow for comparison of real data to the simulated opinion exchange dynamics.

Future Developments

Besides being scale-free, real-world networks are typically characterized by some other statistical properties. Many possess a relatively small average diameter (small-world property) and a high clustering. So far our analysis did not consider these properties in the analysis of the emerging network of opinion exchange activity. Classifying the networks using additional statistical network measures, such as betweenness centrality, diameter and clustering measures like the continuous clustering coefficient introduced in [24], is one essential issue to be addressed in the future.

Looking at opinion dynamics from the perspective of networks allows for a series of additional analyses, one of which is shown in Fig. 7. The data stored during the 100 simulation runs for $N = 1000$ and $d_I = 3$ is used in this analysis. In Fig. 7, the number of opinion changes is plotted with respect to the degree of the nodes. Surprisingly, we observe strong irregularities in the exchange behaviour. For node degrees around 100 and around 320 significantly more opinion exchange is observed than for neighbouring degrees. This might be an indication that a critical connectivity level exists, and that the nodes once they reached this connectivity enter a larger community of agents which gives them a whole group of new communication partners. Such a reasoning may also explain the scaling of the degree distribution for degrees larger than 100. Future

research has to clarify these effects.

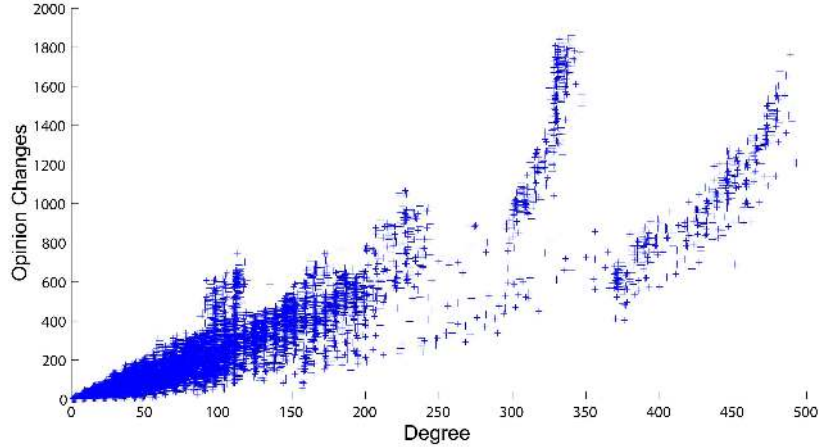


Figure 7: Number of opinion changes to the degree.

Due to the high flexibility of the bit-string description adopted in this work, a series of model refinements can be implemented without much effort. For instance, splitting the string into two and using one sub-string for (say) the private life and the other for the professional relations will allow to generate two different networks and to study the interrelation between the two. Considering parts of the string as fixed, accounting for fixed attributes like gender, can also be a reasonable extension to the model. And along this line, a recent study showed that cross-gender communication is more frequent and more intensive than communication among the same gender [20], which reveals that besides similarity also differences attract in some cases. An adaptation of the interaction rule such that for a part of the bit-string difference is more appealing than similarity is another candidate for future refinement of the model.

Another future development will concern the validation of the opinion dynamics model. Initial assumptions of the model can be grounded on previous research and on literature, and they can also be validated through some empirical studies. In this case, the assumptions of similarity and imitation follow Axelrod’s well-known and discussed dissemination of culture model. The model outcomes which are the communication network and the group sizes will be the subject of future research, aiming to compare them to some real-world networks and group configurations as outlined in the previous section.

Conclusions

Like other authors in the opinion formation field, we explore the mechanisms through which similarity leads to interaction and interaction leads to still more similarity. Network properties seem a natural way to describe the structural patterns that come out from those multi-agent interactions. In this context, the main purpose of this paper is to discuss the potential of networks to emerge endogenously from local interactions without explicitly specifying rules for network linking. This facilitates comparisons of model results to real-world social networks.

We show that complex network structures emerge from a simple process of communication between individuals that have no information on the global properties of the network. This indicates that a crucial role in the formation of social structures and associations is played by the mutual interactions among individuals with diverse opinions, attitudes and lifestyles.

In the context of opinion dynamics, considering which networks result from simulations with different model parameters made visible that the phase transition from highly fragmented public opinion to homogeneity in models of social influence is due to the communication activity that is allowed by a certain parameter constellation. A few critical values play the fundamental role.

We have followed a biological inspiration, where opinion change compares to a mutation mechanism that allow for the adoption of a new position with respect to a certain issue in the agents mind. Such an abstract bit-string approach has been used in the context of labour market analysis [5] where bit-strings represent job offers and worker skills. It was also applied to model innovation in a market-oriented context where producers and consumers try to improve their matching in what concerns products and needs [6]. We envision that the application of the notion of opinion exchange presented in this paper could bring relevant improvement to the way the underlying population structures were represented in those earlier approaches.

Acknowledgements

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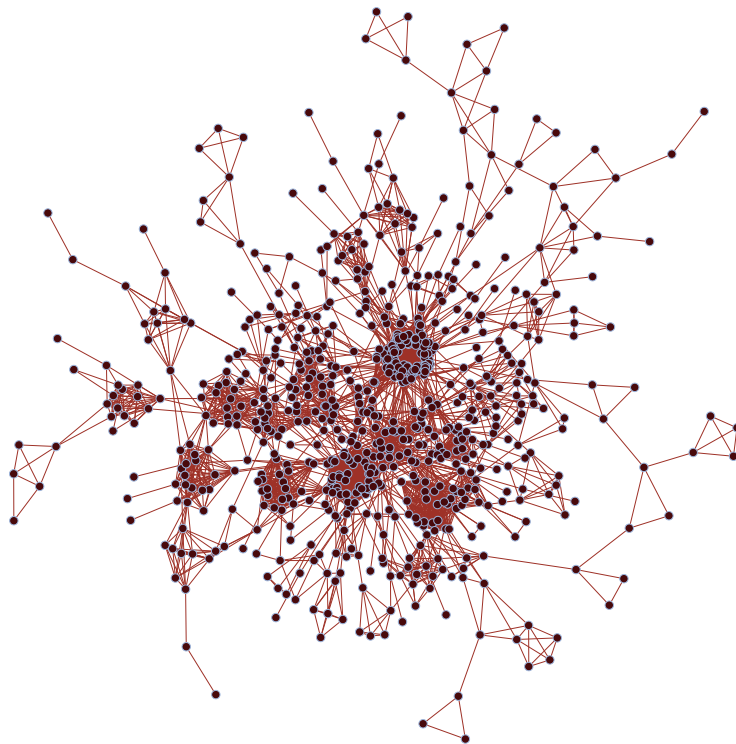


Figure 8: A network of communication formed by the interaction of 1000 agents ($k = 20$ and $d_I = 3$). We can observe the formation of various clusters that among themselves are strongly connected. We also observe the emergence of individuals that connect between clusters which gives them a high importance in the social network. All in all, this shows that very complex social structures can emerge from opinion exchange processes and individual communication. Image produced with the Network Workbench Tool [21].