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# Optical extinction efficiency measurements on fine and accumulation mode aerosol using single particle cavity ring-down spectroscopy

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A new experiment is presented for the measurement of single aerosol particle extinction efficiencies,  $Q_{\text{ext}}$ , combining cavity ring-down spectroscopy (CRDS,  $\lambda = 405$  nm) with a Bessel beam trap ( $\lambda = 532$  nm) in tandem with phase function (PF) measurements. This approach allows direct measurements of the changing optical cross sections of individual aerosol particles over indefinite time-frames facilitating some of the most comprehensive measurements of the optical properties of aerosol particles so far made. Using volatile 1,2,6-hexanetriol droplets,  $Q_{\text{ext}}$  is measured over a continuous radius range with the measured  $Q_{\text{ext}}$  envelope well described by fitted cavity standing wave (CSW) Mie simulations. These fits allow the refractive index at 405 nm to be determined. Measurements are also presented of  $Q_{\text{ext}}$  variation with RH for two hygroscopic aqueous inorganic systems ( $(\text{NH}_4)_2\text{SO}_4$  and  $\text{NaNO}_3$ ). For the PF and the CSW Mie simulations, the refractive index,  $n_\lambda$ , is parameterised in terms of the particle radius. The radius and refractive index at 532 nm are determined from PFs, while the refractive index at 405 nm is determined by comparison of the measured  $Q_{\text{ext}}$  to CSW Mie simulations. The refractive indices determined at the shorter wavelength are larger than at the longer wavelength consistent with the expected dispersion behaviour. The measured values at 405 nm are compared to estimates from volume mixing and molar refraction mixing rules, with the latter giving superior agreement. In addition, the first single-particle  $Q_{\text{ext}}$  measurements for accumulation mode aerosol are presented for droplets with radii as small as  $\sim 300$  nm.

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## 1. Introduction

Aerosol can interact directly with solar radiation, perturbing how much solar energy reaches the Earth's surface. Knowledge of the complex refractive index (RI),  $m$ , is central to determining the scattering and absorption cross sections of aerosol particles and the collective impact of the aerosol ensemble on radiative forcing; the magnitude of the real component,  $n$ , influences the scattering of light, whereas the imaginary component,  $k$ , quantifies light absorption. Atmospheric aerosols also affect climate indirectly by acting as cloud condensation nuclei (CCN), impacting on the size, composition and lifetime of clouds.<sup>1</sup> Quantifying the equilibrium partitioning of water between an aerosol particle and the gas phase, and the condensational growth that results as the relative humidity increases, is critical in describing the size distribution and composition of atmospheric aerosol. The primary motivation for the work presented

here is to report the development of a new technique for reducing the uncertainties associated with the direct interaction of light with aerosol. The extinction cross section of a particle,  $\sigma_{\text{ext}}$ , has contributions from the scattering cross section,  $\sigma_{\text{scat}}$ , and the absorption cross section,  $\sigma_{\text{abs}}$ .<sup>2</sup> The ratio of  $\sigma_{\text{ext}}$  to the geometric cross section  $\sigma_{\text{geo}}$  is referred to as the extinction efficiency,  $Q_{\text{ext}}$ .

Ensemble cavity ring-down spectroscopy (E-CRDS) is a well-established technique used routinely in the measurement of  $Q_{\text{ext}}$  for aerosol particles with sub-micron radii.<sup>3–5</sup> E-CRDS involves measuring  $Q_{\text{ext}}$  by studying the extinction of light by a collection of hundreds to thousands of particles introduced into an optical cavity formed by two highly reflective mirrors at a separation of  $\sim 1$  m. In laboratory measurements, the cloud of particles is generated using an atomiser before some degree of size selection is performed prior to admitting the aerosol to the optical cavity. Rudich and co-workers reported studies of absorbing aerosols using E-CRDS at a variety of visible and UV wavelengths.<sup>4,6,7</sup> By fitting Mie theory scattering simulations to their measured  $Q_{\text{ext}}$  trends, the authors reported trends in both the real and imaginary components of the RI. Mellon *et al.* measured  $Q_{\text{ext}}$  for a range of spherical and non-spherical

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aerosol particles at a wavelength of 1520 nm using an E-CRDS technique.<sup>8</sup> Meanwhile, Mason *et al.* used E-CRDS to study the size and relative humidity (RH) dependence of  $Q_{\text{ext}}$  for sodium nitrate particles, and assessed the limitations inherent to E-CRDS.<sup>3</sup> Most importantly, although size selection is commonplace in the E-CRDS experiments described in the literature, some inevitable polydispersity in size will remain which can be difficult to characterise. For all the drawbacks of E-CRDS, it has proven to be a robust technique that can be used in either the laboratory or the field, and is used routinely to probe aerosol with sub-micron radii from  $\sim 500$  nm down to  $\sim 100$  nm, *i.e.* the size regime bearing most atmospheric relevance in terms of loading and light extinction.

Studying a single particle, instead of an ensemble, by combining CRDS with an independent, nanometre-resolution method for determining particle size should improve the accuracy of  $Q_{\text{ext}}$  measurements. Further, to satisfy the needs of the atmospheric research community, any new technique for measuring  $Q_{\text{ext}}$  should retain the ability to study sub-micron particles. The motivation for studying aerosol in this regime is to reduce the uncertainty associated with the influence of aerosol on Earth's radiative balance.<sup>9</sup> The variations of  $\sigma_{\text{ext}}$ ,  $\sigma_{\text{geo}}$  and  $Q_{\text{ext}}$  with radius for spherical water droplets ( $n = 1.335$  at  $\lambda = 532$  nm) are well known.<sup>2</sup> Importantly, the  $Q_{\text{ext}}$  curve peaks at approximately 500 nm radius, highlighting the need to perform measurements in the sub-micrometre regime.

The application of new techniques for the isolation and characterisation of single aerosol particles is crucial in understanding aerosol processes at a fundamental level.<sup>10</sup> Well established techniques include electrodynamic balances<sup>11,12</sup> and optical tweezers,<sup>13,14</sup> both of which are limited to confining single particles larger than 2–5  $\mu\text{m}$  in radius. We have previously shown that a zeroth-order Bessel laser beam (BB)<sup>15–17</sup> optical trap can be used in the measurement of single particle processes, such as evaporation and hygroscopic response, for particle radii ranging from  $\sim 5$   $\mu\text{m}$  to as small as  $\sim 350$  nm.<sup>18–21</sup> Our experience has shown that BBs can be used to trap particles smaller than 350 nm, but the size of these particles cannot be determined reliably using visible light. Illuminating a particle with the core of a BB will result in a radiation pressure force acting on the particle, while optical gradient forces act in transverse directions to retain the particle within the core. For stable confinement, the radiation pressure force may be balanced by a second counter-propagating BB, although the stability of the alignment for such a system is poor.<sup>18,22–24</sup> Instead, we have opted for a more robust and versatile method using a counter-propagating gas flow, which exerts a Stokes drag force on a particle and renders all forces balanced.<sup>19,20,25</sup>

We have recently demonstrated that optical extinction measurements on single particles can be made using a BB ( $\lambda = 532$  nm) to control the position of a single aerosol particle within a CRD beam.<sup>20,25,26</sup> By observing how the presence of a particle in the centre of the CRD beam changes the rate of decay of light from the high finesse optical cavity formed by two highly reflective mirrors,  $\sigma_{\text{ext}}$  values for aerosols have been determined at a laser wavelength of 532 nm. In tandem with

size determination from angular light scattering measurements, the variation of  $Q_{\text{ext}}$  was measured for the simple case of slowly evaporating 1,2,6-hexanetriol droplets<sup>25</sup> and for the more complicated case of hygroscopic growth of sodium chloride droplets.<sup>20</sup> Not only does optical confinement of a single particle remove the assumptions inherent in E-CRDS measurements and improve the size determination accuracy, but it also allows the same single particle to be studied over a long period of time. This latter advantage permits the optical cross section to be studied as a particle changes size or composition due to, for example, the evaporation of semi-volatile species, the uptake of water if the RH in the chamber increases, or even the chemical transformation accompanying heterogeneous aging.

Our previous publications<sup>20,25</sup> are based on experiments using a CRD beam wavelength of 532 nm, which was chosen in part for experimental convenience but also because it is close to the measured maximum in the solar spectrum at sea level. Measurements were limited to particles with radii larger than  $\sim 750$  nm, outside the atmospherically-relevant accumulation mode regime ( $< 500$  nm). It is important that the range of wavelengths for which  $Q_{\text{ext}}$  is measured is extended to the UV and IR regions of the spectrum, to assess the impact of aerosols on the radiative balance at these wavelengths, and that measurements be made for accumulation mode particles. At shorter wavelength and, thus, larger size parameter, the number of features in a  $Q_{\text{ext}}$  resonance spectrum increases, improving the accuracy with which RI determinations can be made. At longer wavelengths (towards the IR region), water begins to absorb significantly, possibly allowing the effect of the imaginary RI component on the  $Q_{\text{ext}}$  spectrum to be explored. Further, our previous studies for hygroscopic growth of aerosols containing inorganic species did not report independent fits of the RI, but instead employed the parameterisations of Tang and Munkelwitz. Although providing a validation of previous results, this approach did not represent a strategy for determining the optical properties and hygroscopic response of aerosol of completely unknown RI and composition.<sup>27</sup>

The purpose of this publication is many fold. A new experiment is presented: although broadly similar to our single particle 532 nm CRDS apparatus detailed previously,<sup>20,25</sup> CRDS measurements are performed at a wavelength of 405 nm allowing us to quantify the dispersion in RI between 532 and 405 nm. This new set-up is benchmarked by determination of  $Q_{\text{ext}}$  variation for 1,2,6-hexanetriol droplets; comparison with cavity standing wave (CSW) Mie theory calculations allows the constant RI of hexanetriol at  $\lambda = 405$  nm to be extracted. Further, we describe a new method of fitting both the angular variation in elastically scattered light and the CRDS data for hygroscopic growth measurements to determine the RI of aerosol particles directly with no prior assumptions. Subsequently, CRDS measurements and RI determinations for the hygroscopic growth of ammonium sulfate and sodium nitrate droplets are presented. The resulting independent determinations of RI as a function of RH are compared with previous literature parameterisations, in addition to volume fraction and molar refraction mixing rules. Finally, using the previously described 532 nm CRDS apparatus<sup>20,25</sup> with a



reduced BB core, the first single particle measurements of  $Q_{\text{ext}}$  for droplets with radii as small as  $\sim 250$  nm are reported.

## II. Experimental

The experimental apparatus for the 532 nm CRDS system has been described elsewhere;<sup>20,25</sup> the new 405 nm CRDS system is similar in design, and is described here and summarised in Fig. 1. The beam from a 35 mW, single mode 405 nm diode laser (IQ Series, Power Technology Incorporated) was passed through an acousto-optic modulator (AOM, Brimrose) which split the beam into a series of diffraction spots. The first order diffraction spot was selected and injected into an optical cavity, while the zeroth and higher order spots were directed into a beam dump. The optical cavity was constructed from two highly reflective mirrors (Layertec) with reflectivities greater than 99.96% at 405 nm and radii of curvature of 1 m, separated by a distance of 0.8 m. One mirror was mounted on a piezo ring actuator (Piezomechanik), driven with a triangular waveform of amplitude 20 V at a fixed frequency in the range 10–20 Hz. Build-up of light inside the cavity was monitored using a photodiode (RedWave Labs, D101), and the intensity escaping the cavity was measured as an output voltage which was sent to both a Compuscope 12-bit digitizer (GaGe, Octopus CS8222) and a digital delay generator (Quantum Composers, Sapphire 9200). The digital delay generator sent a 5 V TTL pulse to the AOM when the voltage reached a pre-selected threshold, causing the first order diffraction beam from the AOM to extinguish, hence initiating a ring-down decay.

To reduce the impact of light scattering by airborne dust particles on ring-down times (RDTs) and to prevent the mirrors getting dirty, nitrogen gas purge flows were directed across the faces of the cavity mirrors and through flow tubes which extended from the mirror faces to the trapping cell at the centre of the

cavity. The cavity was aligned such that the  $\text{TEM}_{00}$  mode was preferentially excited; as a result, higher order modes with lower coupling efficiencies, and hence lower amplitude ring-down events, could be discriminated against in the data collection. The subsequent  $\text{TEM}_{00}$  mode ring-down traces of photodiode voltage ( $V$ ) vs. time ( $t$ ) were fitted to a single exponential function of the form  $V = V_0 \exp(-t/\tau) + b$  where  $b$  accounts for any baseline offset, and  $\tau$  is the RDT, which was recorded at a rate of between 5 and 10 Hz. In the case of the empty cavity purged with  $\text{N}_2$  gas, this RDT is denoted  $\tau_0$ , and typically has a value of  $14.5 \pm 0.5$   $\mu\text{s}$  depending on the cleanliness of the two cavity mirrors and their alignment, although remains constant over the course of a measurement with a typical standard deviation  $< 0.1$   $\mu\text{s}$ .

A 532 nm Gaussian laser beam (Laser Quantum 2W Opus) was passed through a  $2^\circ$  axicon (Altechna) to produce a Bessel beam. Immediately after the axicon, the BB core diameter was measured to be 55  $\mu\text{m}$ , which is too large to trap micron-sized aerosol particles.<sup>18</sup> Hence, a pair of lenses was used to reduce the core diameter to  $\sim 5.5$   $\mu\text{m}$ . This beam was propagated vertically into the trapping cell using a  $45^\circ$  mirror. The mirror and the trapping cell were mounted on a translation stage. The radiation pressure exerted by this vertically propagating BB on a trapped particle was balanced by a humidified nitrogen gas flow of 100–200 sccm, the RH of which could be controlled. This gas flow was also used to purge the cell of excess aerosol. The RH inside the trapping cell was monitored using a capacitance probe (Honeywell). A camera coupled to a  $20\times$  long working distance objective with a numerical aperture (NA) of 0.42 was used to capture the angular variation of elastically scattered light (phase function) with  $s$ -polarisation from a single trapped aerosol particle. Aerosol particles were introduced into the cell *via* a medical nebuliser (Omron). If multiple particles were trapped, the trapping cell was evacuated and aerosol was again nebulised into the cell. This process was repeated until only a single particle was trapped.

Once a single aerosol particle was optically trapped, its position was optimised to obtain a minimum in the measured RDTs. The position could be tuned in both transverse directions to the CRD beam, in the vertical direction by changing the laser power and in the horizontal direction by scrolling the translation stage on which the trapping cell was mounted. When the particle was centred in the CRD beam, laser feedback control was initiated to keep the particle in the centre over the course of the measurement, and RDTs were collected for the particle in the CRD beam, denoted by  $\tau$ . Typically, the power of the laser required modulating between 400 and 2000 mW over the course of an experiment, depending on the size and composition range of the droplet levitated. From measured  $\tau$  and  $\tau_0$  values, the optical cross section was calculated using eqn (1), in which  $L$  is the cavity length,  $c$  is the speed of light and  $w$  is the CRD beam waist.<sup>20,28</sup>

$$\frac{1}{\tau} - \frac{1}{\tau_0} = \frac{2c\sigma_{\text{ext}}^*}{L\pi w^2} \quad (1)$$

Although  $w$  can be predicted using geometric optics (see Kogelnik and Li<sup>29</sup>), giving an approximate value,  $w$  is in practice treated as a fitting parameter in all  $\sigma_{\text{ext}}$  simulations. Note that the asterisk in  $\sigma_{\text{ext}}^*$  indicates the measured extinction cross section in a cavity

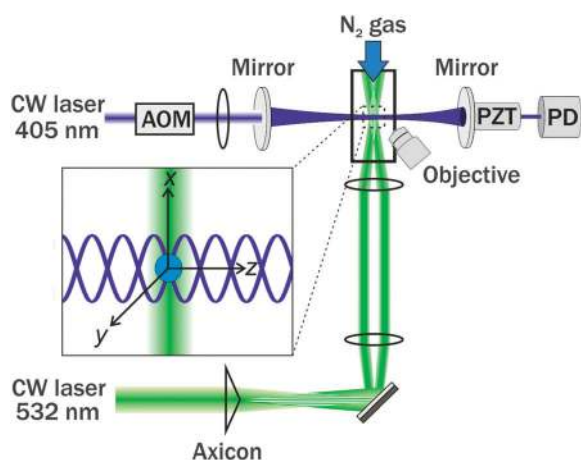


Fig. 1 Schematic diagram of the apparatus used to perform CRDS on single aerosol particles optically trapped in a BB. AOM is an acousto-optic modulator, PZT is a piezoelectric transducer, PD is a photodiode. The inset defines the coordinate system used in CSW Mie theory calculations and shows a particle confined in a BB core intersected with the intra-cavity standing wave.



standing wave, as opposed to a travelling wave which is assumed in Mie theory. Miller and Orr-Ewing calculated the effect of the standing wave on the observed scattering cross section of an aerosol particle.<sup>30</sup> They showed that the effect of the standing wave on the measured extinction cross section  $\sigma_{\text{ext}}^*$  is encapsulated in a phase parameter,  $\zeta$ , which relates  $\sigma_{\text{ext}}^*$  to the Mie theory value,  $\sigma_{\text{ext}}$ :

$$\sigma_{\text{ext}}^* = \zeta(m, a, z_0) \sigma_{\text{ext}} \quad (2)$$

Here,  $\zeta$  is a function of the position of the particle with respect to the phase of the standing wave,  $z_0$ , as well as the RI and size of the particle. Miller and Orr-Ewing showed how  $\zeta$  may be calculated when a particle is centred on a node and on an anti-node of an intra-cavity standing wave, which form the two limiting cases in the distribution of measured  $\sigma_{\text{ext}}^*$  data.<sup>30</sup> Here, we refer to this modification of Mie theory as cavity standing wave (CSW) Mie theory. Experimental verification of the effect of the standing wave on the measured  $\sigma_{\text{ext}}^*$ , and the importance of taking into account CSW Mie theory were demonstrated by Mason and co-workers.<sup>25,26</sup>

Once the optical cross section has been determined, the radius of the particle must be measured to calculate  $Q_{\text{ext}}$ . The radius of the particle is determined from the phase function (PF) image, which is analysed to give the one dimensional relative intensity distribution with scattering angle. This distribution is affected not only by particle radius but also by the RI of the particle. Measuring the angular variation in the scattered intensity and simulating the measured distribution using Mie theory provides a method of obtaining the particle size and RI, even for sub-micron aerosol particles.<sup>31</sup>

### III. Optical extinction measurements for 1,2,6-hexanetriol droplets

To benchmark the experiment and assess its capability, it is important to measure  $\sigma_{\text{ext}}^*$  for a spherical particle of constant composition (RI) over a continuous size range and determine whether the data can be described using CSW Mie theory. Hexanetriol is a semi-volatile organic compound that is relatively non-hygroscopic, particularly when compared to the water uptake of inorganic species such as sodium chloride in high RH environments. Although having no atmospheric relevance, it serves as an ideal system to benchmark our experiment, and has been studied extensively in previous work.<sup>19,20,25,26</sup> A hexanetriol droplet was optically trapped at low RH (<10%), and its position in the CRD beam optimised. The RDTs and PFs were subsequently measured over  $\sim 2$  hours as the particle evaporated.

The radius,  $a$ , and constant RI of a droplet were determined from the PFs by comparing to a computed library of Mie-theory simulated PFs over a defined radius range for a constant value of the real component of the RI,  $n_{532}$ . The Pearson correlation coefficient,  $C$ , between each of the simulated and measured PFs was calculated. For each measured PF, the simulation with the highest correlation defined the best-fit radius of the particle for the corresponding value of  $n_{532}$ . Once the radii were determined

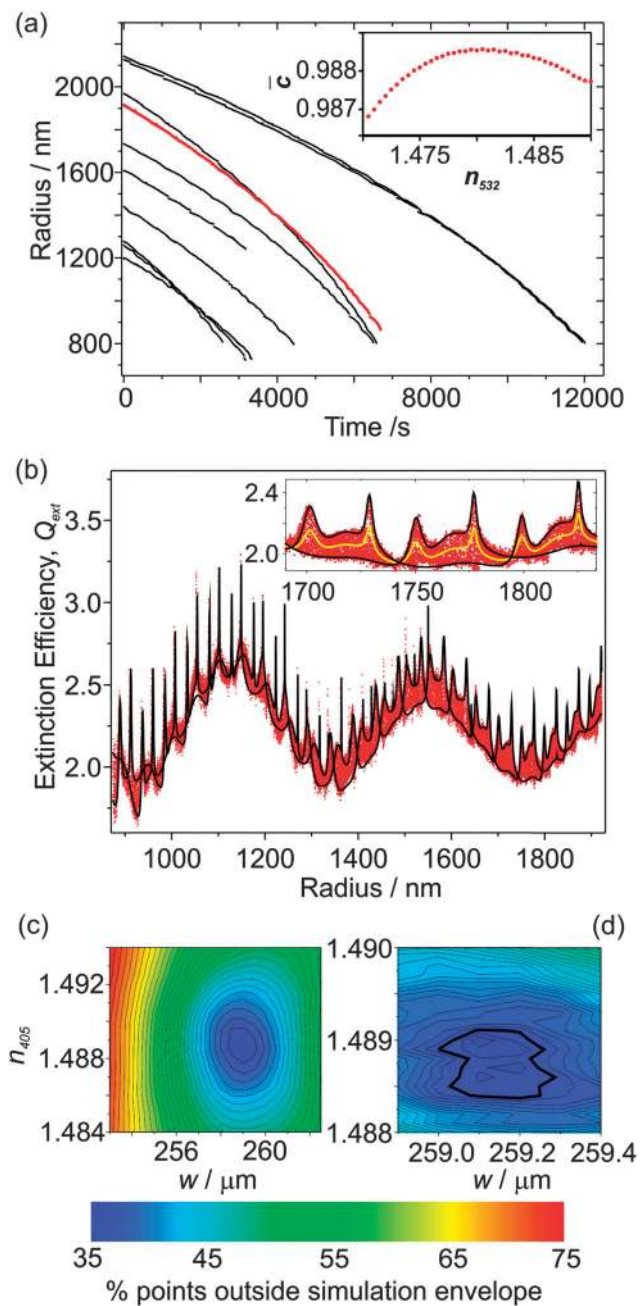
for all the measured PFs in an entire data set, the mean correlation coefficient  $\bar{C}$  is calculated for the value of  $n_{532}$  of the first iteration before varying  $n_{532}$  in a stepwise manner. Note that  $\bar{C}$  is defined as the arithmetic mean of the collection of Pearson correlation coefficients calculated for the entire data set for the particular trial value of  $n_{532}$ . Then, by identifying the  $n_{532}$  that yielded the maximum  $\bar{C}$  calculated over the full range of trial values of  $n_{532}$ , the best-fit constant RI for hexanetriol was determined.

The radius data for 10 such measurements are shown in Fig. 2(a); the largest droplet was initially trapped at a radius of 2140 nm, and the smallest droplet evaporated to a size of 725 nm. The inset shows how the mean correlation coefficient,  $\bar{C}$ , between the experimental and simulated PFs varies with  $n_{532}$  for one of the droplets (plotted using red data points). For this particular droplet, the best fit  $n_{532}$  peaks at  $\sim 1.481$ ; the average determined RI for all 10 droplets is  $1.477 \pm 0.004$  where the error represents one standard deviation. This value of  $n_{532}$  for hexanetriol is consistent with previous measurements using either single aerosol particle CRDS ( $1.4782 \pm 0.0007$ )<sup>25</sup> at 532 nm, or a combination of radiation pressure and PF measurements ( $1.482 \pm 0.001$ ).<sup>19</sup> We will now focus on the particle that has been highlighted in more detail.

Fig. 2(b) shows the  $Q_{\text{ext}}$  values inferred from the CRDS measurements at 405 nm as a function of particle radius, with the radius and geometric cross section determined from the PF measurements. The CSW Mie simulations of  $Q_{\text{ext}}$  are performed for the two limiting cases of the particle centred at a node and anti-node. These simulations depend on the RI at 405 nm; although  $n_{532}$  is known from the PF fitting,  $n_{405}$  is not known but can be determined by varying it as a fit parameter. In addition, the CRDS beam waist is varied, which has the effect of scaling the measured  $Q_{\text{ext}}$  data to larger or smaller values (*i.e.*, an amplitude shift in  $Q_{\text{ext}}$ ) as would be expected after inspection of eqn (1). We define a residual as the fraction of the measured  $Q_{\text{ext}}$  points that fall outside the simulation envelope, and this residual is minimised by varying  $w$  and  $n_{405}$ . Accordingly, Fig. 2(b) shows the best fit CSW Mie theory simulations for the limiting node and anti-node cases. The inset to Fig. 2(b) shows an expanded portion of these  $Q_{\text{ext}}$  data accompanied with a conventional Mie theory simulation (solid yellow line). This inset emphasises how the measured  $Q_{\text{ext}}$  data are broadened by the impact of the cavity standing wave, with the  $Q_{\text{ext}}$  being scaled in equal proportion to higher and lower values about this Mie theory curve. It also emphasises how well the CSW Mie theory simulations describe the boundaries of this broad  $Q_{\text{ext}}$  envelope. Note that in previous publications where both the PF and the CRD data were measured at the same wavelength (532 nm), the droplet radius was scaled using an empirical formula when the RI was varied to correct for using an inaccurate RI in the PF fitting.<sup>25</sup> This method cannot be used here because the PF and CRD data are measured at different wavelengths. Nonetheless, the agreement in the peak positions between the measured  $Q_{\text{ext}}$  data and the CSW Mie simulations is remarkable, indicating that the radius determination from the PF fitting is more accurate than for our previous single particle CRDS measurements.<sup>25</sup>

Fig. 2(c) shows a contour plot of the residual variation with  $n_{405}$  and  $w$  used in the CSW Mie simulations, with a region





**Fig. 2** (a) The measured radius vs. time for ten 1,2,6-hexanetriol droplets. The inset shows the mean correlation coefficient,  $\bar{C}$ , between the measured and simulated PFs as a function of  $n_{532}$  for the radius data plotted with red data points. (b) The measured  $Q_{\text{ext}}$  for the radius data plotted in red in (a), along with the best fit CSW Mie simulation. The inset shows an expanded portion, highlighting the good agreement between the boundaries in the measured  $Q_{\text{ext}}$  and the CSW Mie simulations, along with a conventional Mie simulation (solid yellow line). (c) A contour plot of the percentage of points outside the CSW Mie simulation envelope as a function of the two fitting parameters,  $n_{405}$  and  $w$ . (d) An expanded portion of the contour plot in (c).

where the residual is minimised. Fig. 2(d) shows an expanded portion of this contour plot in which a finer grid search was performed. In this expanded portion, local minima can be seen because of the noise inherent in the measured  $Q_{\text{ext}}$  data.

The best fit is defined as the midpoint of the contour where the residual rises above the baseline noise (shown by the thicker line in the figure). The best fit has 34.5% of points lying outside the simulated envelope, and gives  $w = 259.15 \pm 0.2 \mu\text{m}$  and  $n_{405} = 1.48875 \pm 0.0005$ . Note that only the real component of the RI is varied, and  $k$  is set to zero. The determined beam waist is in good agreement with the prediction of  $253 \mu\text{m}$  obtained using theory for symmetrical resonators.<sup>29</sup> The large value for the minimum in the residual is due to large contributions where the envelope in  $Q_{\text{ext}}$  narrows; where the CSW Mie simulations for the limiting node and anti-node cases cross, there is scatter in  $Q_{\text{ext}}$  deriving from noise in both  $\tau$  and  $\tau_0$ .

Each of the radius-time data sets in Fig. 2(a) has corresponding RDT data, which were analysed to determine  $w$  and  $n_{405}$  for all 10 particles. The mean value of  $n_{405}$  is  $1.4906 \pm 0.0012$ , while the mean value of  $w$  is  $264.4 \pm 4.4 \mu\text{m}$ , where the errors represent one standard deviation in the measured values. The former mean value is in good agreement with previous determinations of  $n_{405}$  for hexanetriol using radiation pressure measurements, which gave a value of  $1.485 \pm 0.006$ .<sup>19</sup> The percentage error in  $w$  is much larger than that in  $n_{405}$ , which is expected; from one day to the next, the cavity alignment can drift and needs re-alignment. The measured  $n_{405}$  values are larger than the  $n_{532}$  values measured from the PFs and those reported previously by Mason and co-workers ( $1.4782 \pm 0.0007$ ), in accordance with the dispersion trends exhibited by most substances.<sup>25</sup> Further, both the  $n_{405}$  and  $n_{532}$  values are higher than refractometer (Misco, Palm Abbe II) measurements which give a bulk RI of 1.4758 at a wavelength of 589.6 nm.

#### IV. Fitting refractive index for hygroscopic inorganic species

The analysis of the PF and RDT data for hexanetriol was relatively straightforward: each droplet has a composition (and hence RI) that does not change over time, assuming the RH remains constant at 0%. In this section, we look at measurements and the analysis of the PF and RDT data for hygroscopic inorganic salts as the ambient RH is varied. A changing RH results in the condensation or evaporation of water from a hygroscopic droplet. As a consequence, both the size and composition of the droplet change, leading to a size dependent RI. An aqueous inorganic salt solution with a typical solute concentration of  $100 \text{ g L}^{-1}$  was nebulised into the trapping cell, and a single aqueous droplet optically trapped in the BB core at a high RH ( $>70\%$ ). The position of the droplet was optimised until it was located at the centre of the  $\lambda = 405 \text{ nm}$  CRD beam. The PFs and RDTs were collected while the RH was lowered steadily over time. In the following sections, we initially describe our PF fitting strategy for the determination of both radius and RI for hygroscopic growth measurements before demonstrating the ability to retrieve the RI at wavelengths of 405 nm and 532 nm for ammonium sulfate and sodium nitrate aerosol droplets. Finally, we test common literature mixing rules to assess their validity in predicting the variations of RI with relative humidity.



#### IV. a Strategy for fitting PFs for hygroscopic growth measurements

Previous radius determinations from PFs in the literature used either a fixed RI, or modelled a varying RI by linking the composition of a particle to its radius or the RH of the surrounding environment<sup>19,20</sup> using the parameterisations of Tang and Munkelwitz.<sup>27</sup> However, with recent improvements in the acquisition of PFs (in particular, noise reduction), as well as computational advances in fitting the PFs to Mie theory, we are now in a position to fit both the RI and the particle radius.<sup>32</sup> In principle, a suitable approach to characterising a trapped particle is to find values of  $a$  and  $n$  that maximise the correlation between experimental and simulated PFs. In practice, even when a particle is homogeneous and spherical, this method yields best-fits that contain high uncertainties. Typically, the poor quality of the fits is noticeable when the analysis is applied to a series of PFs measured under experimental conditions where both  $a$  and  $n$  should change slowly over time. When these measurements are fitted and the results are plotted as a function of time, both  $a$  and  $n$  can be scattered and contain discontinuities that are contrary to the expectation that their change over time should be smooth. Needless to say, analysis and interpretation of these types of data are difficult.

To reduce, or perhaps eliminate, the above problem, an alternative fitting scheme is implemented here. For a PF data set acquired for one droplet over a long time frame, the Pearson correlation coefficient  $C$  is maximised with respect to  $a$  over the whole data set, constraining the relationship between radius and  $n$  by the equation:

$$n = n_0 + \frac{n_1}{a^3} + \frac{n_2}{a^6} + \dots + \frac{n_k}{a^{3k}} \quad (3)$$

Of these parameters, only  $n_0$  is known beforehand (the refractive index of pure water at the wavelength of the measurement), while  $n_1, n_2, \dots, n_k$  must still be determined. These additional terms are found by maximising the mean correlation coefficient  $\bar{C}$  across an entire set of PFs (for experiments performed here, there will typically be several thousand PFs in a data set). Maximised correlation coefficients between experimental and simulated PFs are found by fixing  $n_1, n_2, \dots, n_k$  across all PFs and varying  $a$  in fitting each individual PF in the set. The resulting set of maximised correlation coefficients is then used to calculate  $\bar{C}$  for the chosen parameter set and represents one point on the  $k$ -dimensional space formed by  $n_1, n_2, \dots, n_k$ . The goal is to find the point in this space that maximizes  $\bar{C}$  and, in this work, a grid-search is used to accomplish this task.<sup>33</sup> After each calculation of  $\bar{C}$ , one of the parameters  $n_1, n_2, \dots, n_k$  is incremented using a chosen step size and  $\bar{C}$  is calculated once more. This process is repeated until a maximum in the correlation coefficient is located. The point in the  $k$ -dimensional grid that maximises  $\bar{C}$  corresponds to the best-fit values for parameters  $n_1, n_2, \dots, n_k$  (the values of  $a$  for each PF are found during the calculation of  $\bar{C}$  for this point). During testing, this method was found to reduce both noise and discontinuities in  $a$  and  $n$ . Note that the quality of the fits is also found to improve when both the lower and upper values of the angular range for the measured

PFs are allowed to vary for each individual PF by  $1.5^\circ$  to account for changes in the computer-determined positions of the droplet edges during image processing.

When the particle radius is infinitely large (*i.e.* at infinite RH or dilution of solutes), eqn (3) simplifies to  $n = n_0$ ; thus  $n_0$  corresponds to the RI value for a pure water droplet, which is 1.335 at 532 nm. The terms  $n$  and  $n_0, n_1, n_2, \dots, n_k$  are wavelength dependent and will be denoted as  $n_\lambda, n_{0,\lambda}, n_{1,\lambda}, n_{2,\lambda}, \dots, n_{k,\lambda}$  from this point forward. The  $n_{k,\lambda}$  values will vary from one experiment to another depending on the mass of solute in the droplet, while the number of terms required to model accurately the RI will also vary, although typically only  $n_{1,\lambda}$  and  $n_{2,\lambda}$  are required. Initial ranges are set for  $n_{1,532}$  (typically between 0 and  $1 \times 10^9 \text{ nm}^3$  for radii  $< 2 \mu\text{m}$ ) and  $n_{2,532}$  (between  $-3$  and  $3 \times 10^{18} \text{ nm}^6$ ), with  $n_{1,532}$  optimised initially while  $n_{2,532}$  is set to zero.  $\bar{C}$  is determined for every iteration of  $n_{1,532}$ , with the highest  $\bar{C}$  corresponding to the optimum value of  $n_{1,532}$ . Next,  $n_{2,532}$  is varied with  $n_{1,532}$  set to its optimum value. After these initial optimisations, refining grid search cycles are performed with the steps in the grid search being reduced by 50% after every search cycle.

#### IV. b Hygroscopic growth measurements for ammonium sulfate

Our initial discussion focuses on a hygroscopic growth measurement for an ammonium sulfate droplet, which was trapped at  $\sim 80\%$  RH; the ambient RH was subsequently lowered to  $\sim 38\%$ , at which point the droplet fell out of the trap following crystallisation. Fig. 3(a) shows how  $\bar{C}$  changes as  $n_{1,532}$  (red squares) and  $n_{2,532}$  (blue circles) are varied during their initial optimisation stages. The  $\bar{C}$  values for the  $n_{2,532}$  optimisation stage are higher as a result of  $n_{1,532}$  having been optimised, and  $n_{2,532}$  representing a small perturbation of the curve in  $n_{532}/a^{-3}$  space. Fig. 3(b) shows the final radius-time determination (after the refining grid search cycles) corresponding to  $\bar{C} = 0.9701$ , accompanied by the variation in the RH over the measurement. The inset shows the final, best-fit RI curve as a function of  $a^{-3}$ , and the impact of the variation of the  $n_{2,532}$  term can be clearly seen by the curvature in this plot. The values of  $n_{1,532}$  and  $n_{2,532}$  for this particular droplet are  $8.84 \times 10^8 \text{ nm}^3$  and  $-2.12 \times 10^{18} \text{ nm}^6$  respectively. Note that a small perturbation from a third-order term,  $n_{3,532}$ , was also applied with a value of  $2.00 \times 10^{27} \text{ nm}^9$  in order to refine further the RI description. The uncertainties in these values are difficult to quantify. However, we show later that the determined RI description behaves as expected when compared to parameterisations by Tang *et al.*<sup>27,34</sup> The radius-time data decrease smoothly with very little experimental noise, and only exhibit a couple of discontinuities in the droplet radius, each with a magnitude of  $< 5 \text{ nm}$ . The low noise and smooth variation in the radius suggest that the improvements in the PF acquisition and subsequent Mie theory fitting procedure have resulted in better-quality radius determination compared to other published determinations from PFs of sub- $2 \mu\text{m}$  droplets.<sup>19,20,35</sup>

Now the radius of the particle has been determined,  $Q_{\text{ext}}$  may be calculated from the RDT data for a trial beam waist,



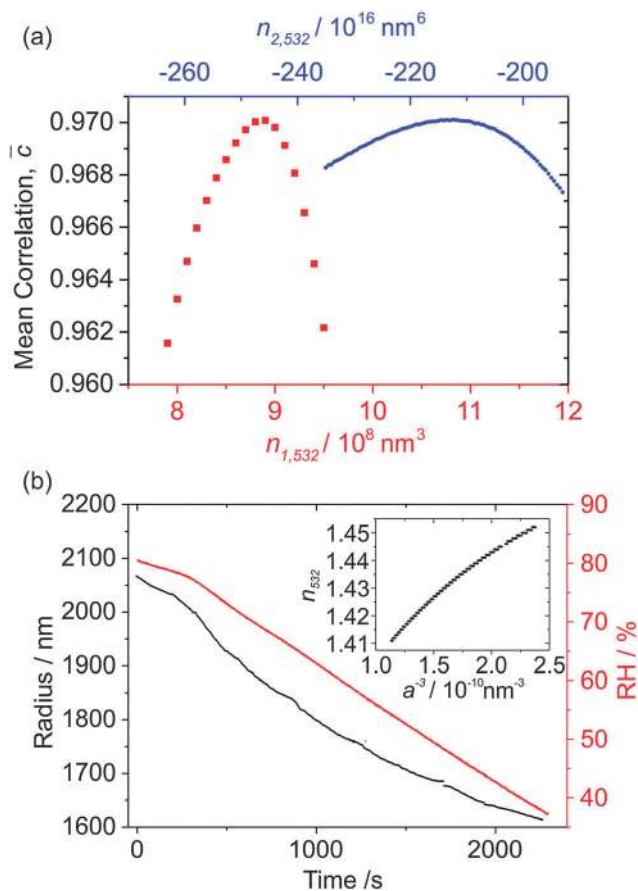


Fig. 3 (a) The mean correlation,  $\bar{c}$ , as a function of  $n_{1,532}$  (red squares) and  $n_{2,532}$  (blue circles) during the initial stages of their optimisation through PF fitting for a hygroscopic growth measurement of ammonium sulfate. (b) The measured RH vs. time and determined radius vs. time for the ammonium sulfate droplet in (a). The inset shows how the determined RI at 532 nm varies with  $a^{-3}$ .

which will later be treated as a fitting parameter. Knowing for certain the droplet size, simulating the  $Q_{\text{ext}}$  data with CSW Mie theory allows a retrieval of the variation in  $n_{405}$  with particle radius, leading to direct measurements of the dispersion in RI. We generate another expression of the form of eqn (3), but instead of using a value of  $n_{0,532} = 1.335$ , we now fix the RI of water to the known value of  $n_{0,405} = 1.343$ .<sup>36</sup> Further, instead of fitting  $n_{1,405}$  and  $n_{2,405}$ , we use:

$$n_{405} = n_{0,405} + \frac{n_{1,532} + \Delta n_1}{a^3} + \frac{n_{2,532} + \Delta n_2}{a^6} + \frac{n_{3,405}}{a^9} \quad (4)$$

where  $n_{1,532}$ ,  $n_{2,532}$  and  $n_{3,532}$  have been determined by the PF fitting procedure, and small offsets to these first-order ( $\Delta n_1$ ) and second-order ( $\Delta n_2$ ) coefficients are applied with the fitting at 532 nm thereby providing excellent first estimates of the values. Therefore, fitting the  $Q_{\text{ext}}$  data to CSW Mie simulations requires a three parameter fit, varying  $w$ ,  $\Delta n_1$  and  $\Delta n_2$  using a grid searching approach. Owing to the computational time needed to perform this fitting, no offset is applied to the third order  $n_{3,532}$  term.

Unlike the experiments involving hexanetriol, as the RH variation is not perfectly linear in hygroscopic growth measurements (particularly evident at the beginning of the measurement in Fig. 3(b)), the ‘density’ of the measured  $Q_{\text{ext}}$  data points is not uniform in the radius domain. To ensure there is no bias in the fitting of CSW Mie simulations to higher density regions of  $Q_{\text{ext}}$  data, the values of  $Q_{\text{ext}}$  are collected into 1 nm bins and each point that falls outside the envelope is weighted by dividing by its associated bin’s number count. The result of the fitting of CSW Mie theory simulations to the  $Q_{\text{ext}}$  data is shown in Fig. 4(a). Not only is there excellent agreement in the resonance peak positions of the measured  $Q_{\text{ext}}$  and CSW Mie simulations (further indicating accurate size determination of the droplet from PF analysis), but there is also a good description of the underlying contour of the data (indicating good determination of the variation in  $n_{405}$  over the measurement).

Fig. 4(b) shows a contour plot of the residual in terms of  $\Delta n_1$  and  $\Delta n_2$ , which exhibits a definite minimum, with several local minima resulting from noise in the  $Q_{\text{ext}}$  data. The values of  $\Delta n_1$  and  $\Delta n_2$  corresponding to a minimum in the residual are  $(0.95 \pm 0.03) \times 10^8 \text{ nm}^3$  and  $(4.4 \pm 0.2) \times 10^{16} \text{ nm}^6$ ,<sup>17</sup> respectively, with uncertainties determined by the distance to the contour where the residual rises above the baseline noise. Note that the well in the residual is diagonal in shape, implying that  $\Delta n_1$  and  $\Delta n_2$  are inversely correlated, while the uncertainties in  $\Delta n_1$  and  $\Delta n_2$  may also be correlated. In a similar way,  $w$  is found to be  $251.5 \pm 0.5 \mu\text{m}$ .

The parameterisation of the variation of  $n_{532}$  and  $n_{405}$  with RH may be of value for applications in environmental research. Therefore, polynomial fits to the measured  $n_{405}$  and  $n_{532}$  variation with water activity,  $a_w$ , used eqn (5), where  $C_i$  are polynomial coefficients, the values of which are reported in Table 1:

$$n_\lambda = \sum_{i=0}^4 C_i a_w^i \quad (5)$$

The uncertainties quoted in  $\Delta n_1$  and  $\Delta n_2$  allow the uncertainty envelope in  $n_{405}$  to be calculated. When parameterising  $n_{405}$  in the RH domain, these uncertainties in  $\Delta n_1$  and  $\Delta n_2$  are negligible when compared to the errors associated with the RH measured ( $\pm 2\%$ ). This point is emphasised in Fig. 4(c) which shows the dependence of  $n_{405}$  (purple solid line) and  $n_{532}$  (black data points) on RH. The narrow red envelope represents the uncertainty in  $n_{405}$  if we only consider the errors obtained by fitting the  $Q_{\text{ext}}$  data, while the broad grey envelope takes into account the uncertainty in the RH probe measurement. Clearly, the  $\pm 2\%$  uncertainty in the RH probe measurement is the dominant source of error in any RI–RH parameterisation. A comparison is also made to the parameterisation of Tang *et al.* (red solid line) determined at a wavelength of 632.8 nm.<sup>27,34</sup> The measured  $n_{532}$  curve from the PF measurements is shifted towards higher RI compared to the Tang parameterisation, while the  $n_{405}$  curve is shifted towards higher RI relative to  $n_{532}$  (as expected given typical wavelength dispersion behaviour). Further, the separation between the  $n_{405}$  and  $n_{532}$  curves



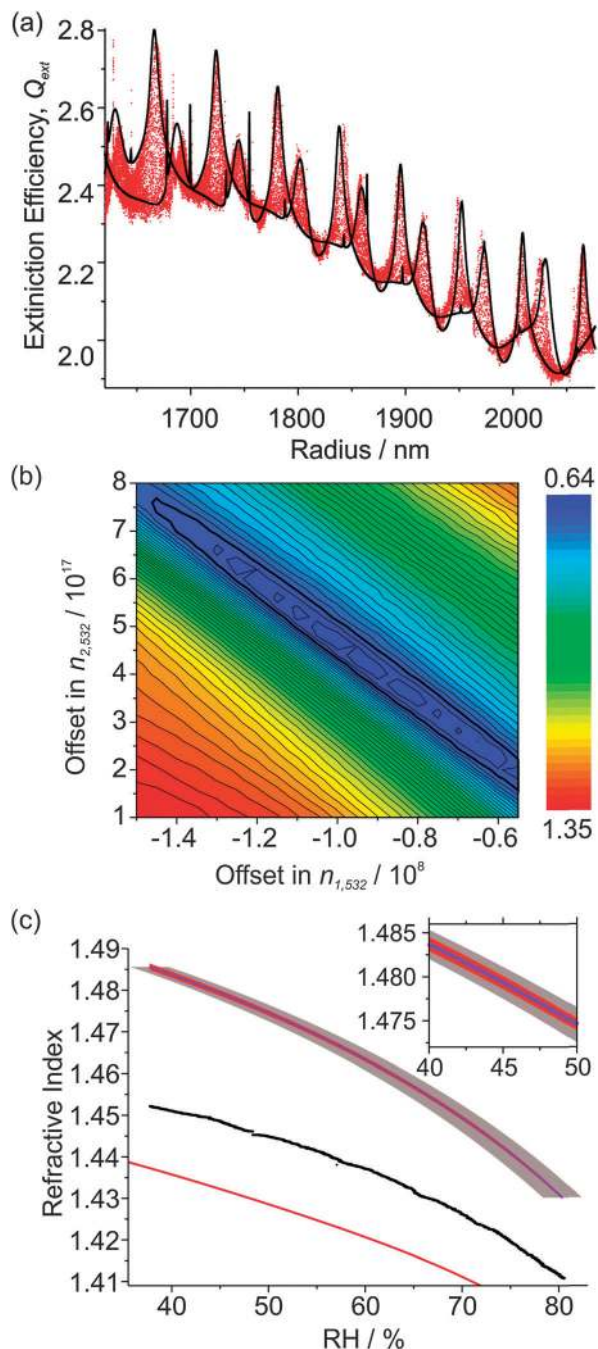


Fig. 4 (a) The measured  $Q_{\text{ext}}$  variation with particle radius for the hygroscopic growth of the  $(\text{NH}_4)_2\text{SO}_4$  droplet in Fig. 3 (red data points) and best-fit CSW Mie simulations (black lines). (b) Contour plot of the dependence of the residual on  $\Delta n_1$  and  $\Delta n_2$ . (c) RH dependence of  $n_{532}$  (black data points) and  $n_{405}$  (purple line), with a comparison to the parameterisation of Tang *et al.* ( $\lambda = 633$  nm, red line).<sup>27,34</sup> The red envelope shows the uncertainty in  $n_{405}$  resulting from uncertainties in  $\Delta n_1$  and  $\Delta n_2$ . The larger grey envelope shows the uncertainty caused by uncertainty in the RH measurement. The inset shows an expanded portion of these envelopes.

increases as the RH is lowered and the droplet composition tends to that of the solute, which is also expected given the higher chromatic dispersion of inorganic salts compared to water.

Table 1 Summary of the determined coefficients for calculating the RI from water activity,  $a_w$ , using eqn (5) for the inorganic species  $(\text{NH}_4)_2\text{SO}_4$  and  $\text{NaNO}_3$ , at illuminating wavelengths of 405 and 532 nm

	$(\text{NH}_4)_2\text{SO}_4$		$\text{NaNO}_3$	
	$\lambda = 532$ nm	$\lambda = 405$ nm	$\lambda = 532$ nm	$\lambda = 405$ nm
$C_0$	1.476	1.526	1.481	1.504
$C_1$	$-9.748 \times 10^{-2}$	$-1.547 \times 10^{-1}$	$-1.166 \times 10^{-1}$	$-9.947 \times 10^{-2}$
$C_2$	$1.501 \times 10^{-1}$	$2.032 \times 10^{-1}$	$-1.233 \times 10^{-1}$	$-2.184 \times 10^{-1}$
$C_3$	$-1.621 \times 10^{-1}$	$-1.973 \times 10^{-1}$	$3.490 \times 10^{-1}$	$4.973 \times 10^{-1}$
$C_4$	—	—	$-2.613 \times 10^{-1}$	$-3.482 \times 10^{-1}$

#### IV. c Hygroscopic growth measurements for sodium nitrate

Sodium nitrate aerosol is another atmospherically relevant system;  $\text{NaNO}_3$  particles form by the reaction of sea salt aerosol with nitric acid and  $\text{NO}_x$ , and can impact the radiative forcing in marine environments.<sup>37</sup> There is ongoing debate over the hygroscopic properties and the RH at which  $\text{NaNO}_3$  droplets effloresce, with Gysel *et al.* not observing any efflorescence at RHs as low as  $\sim 6\%$  using an ensemble technique.<sup>38</sup> Thus, single  $\text{NaNO}_3$  droplets were confined within a Bessel laser beam and placed into the centre of our 405 nm CRD beam for the measurement of  $Q_{\text{ext}}$  with variations in RH.

Fig. 5(a) shows the measured  $Q_{\text{ext}}$  variation with radius for one droplet which fell from the trap at  $\sim 12\%$  RH, although the particle loss may not be a consequence of efflorescence. Instead, the combination of both the small size of the droplet and its RI may have rendered the forces acting on it too weak for stable trapping. The measured  $Q_{\text{ext}}$  is again very well described by CSW Mie theory. Both the resonance peak positions and the underlying contour of the  $Q_{\text{ext}}$  curve agree well with the CSW Mie simulations. This agreement is indicative of correct size determination of the particle by PF analysis at 532 nm, as well as good determination of the variation of  $n_{532}$  and  $n_{405}$  with changing RH. The values of  $n_{1,532}$ ,  $n_{2,532}$  and  $n_{3,532}$  for this particular droplet are  $2.28 \times 10^8 \text{ nm}^3$ ,  $-3.28 \times 10^{16} \text{ nm}^6$  and  $1.20 \times 10^{25} \text{ nm}^9$  respectively. The values of  $\Delta n_1$  and  $\Delta n_2$  corresponding to the minimum in the contour plot of Fig. 5(b) are  $(4.48 \pm 0.03) \times 10^7 \text{ nm}^3$  and  $(-3.2 \pm 0.1) \times 10^{16} \text{ nm}^{17}$  respectively. Fig. 5(c) compares the  $n_{532}$  determined from our measurement with Tang's parameterisation ( $\lambda = 633$  nm), with an expected shift in  $n_{532}$  towards higher RI not observed.<sup>27</sup> Further, the  $n_{405}$  variation with RH is displaced to higher values compared to the  $n_{532}$  curve, as expected. The similarity in the  $n_{532}$  and  $n_{633}$  curves suggests that the refractive index dispersion is a weak function of wavelength until the blue region of the spectrum is reached. Again, a polynomial was fitted to the measured  $n_{405}$  and  $n_{532}$  variation with water activity using eqn (5), and the coefficients are presented in Table 1 along with those for  $(\text{NH}_4)_2\text{SO}_4$ .

#### IV. d Comparison of determined RIs with literature mixing rules

Fig. 6 summarises the variation of  $n_{405}$  with RH for both the  $(\text{NH}_4)_2\text{SO}_4$  and  $\text{NaNO}_3$  droplets studied (purple solid lines).





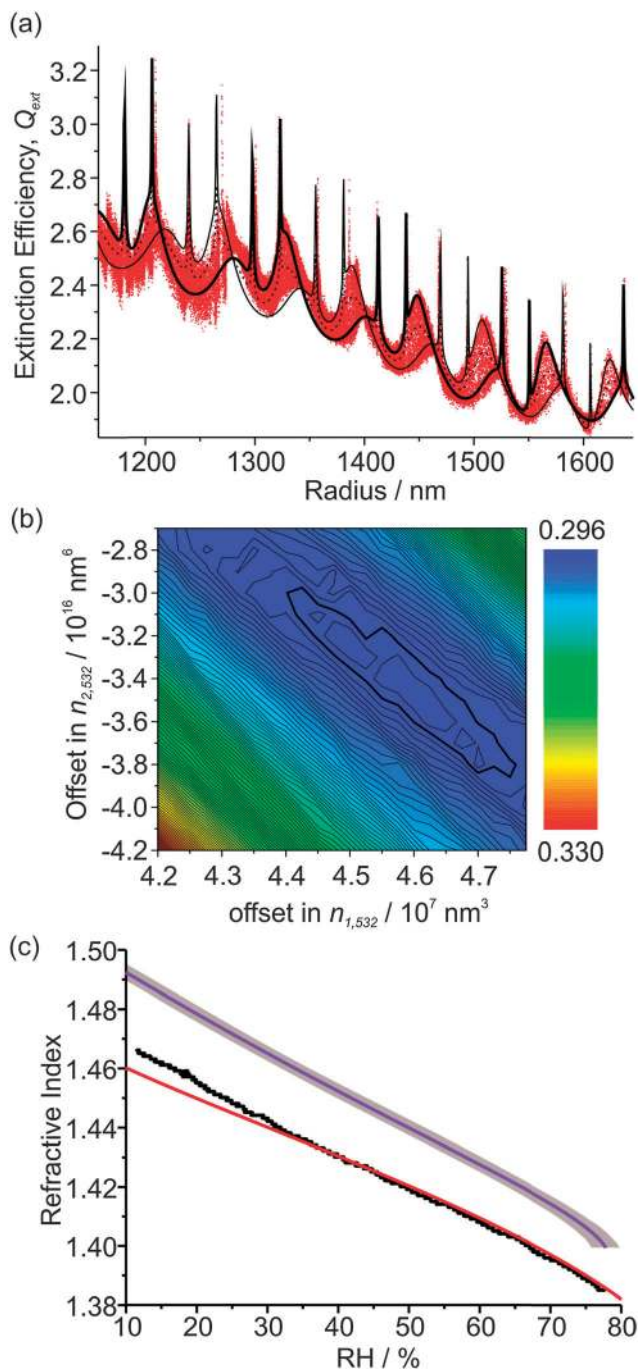


Fig. 5 (a) The measured  $Q_{\text{ext}}$  variation with particle radius for the hygroscopic growth of a  $\text{NaNO}_3$  droplet (red data points) and best-fit CSW Mie simulations (black lines). (b) Contour plot of the dependency of the residual on  $\Delta n_1$  and  $\Delta n_2$ . (c) The determined RH dependence of  $n_{532}$  (black data points) and  $n_{405}$  (purple line), with a comparison to the parameterisation of Tang *et al.* ( $\lambda = 633$  nm, red line).<sup>27,34</sup> The large grey envelope shows the uncertainty caused by uncertainty in the RH measurement.

These variations can be compared with predictions from refractive index mixing rules, with the two most common being the volume fraction weighting and the molar refraction methods. The volume fraction mixing rule is widely encountered,<sup>39,40</sup> and uses a volume fraction weighting of the pure solute,  $n_s$ , and pure

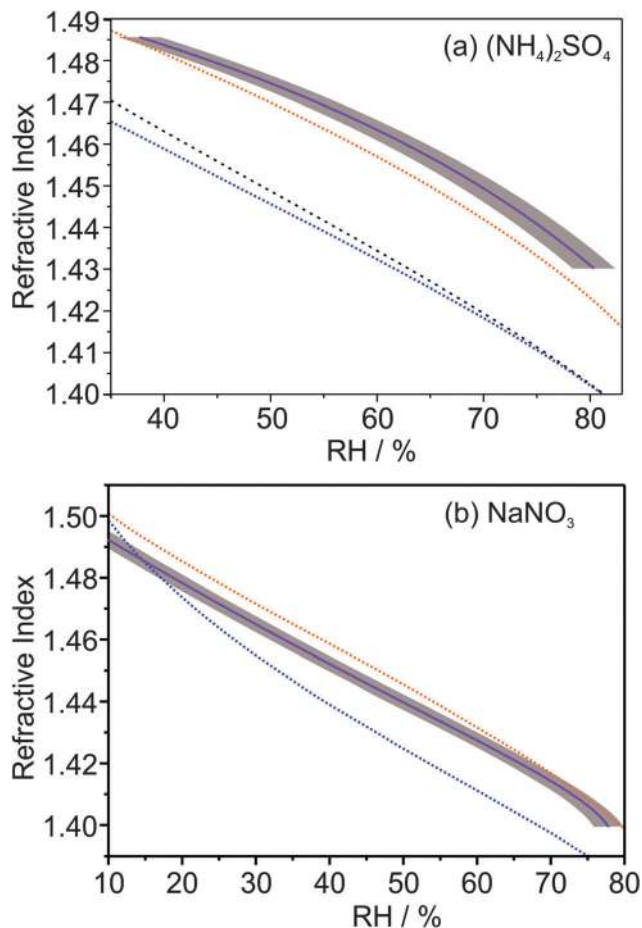


Fig. 6 Comparison of predictions from mixing rules with the measured  $n_{405}$  variation with RH (solid purple line) for (a) ammonium sulfate and (b) sodium nitrate. The grey envelopes show a  $\pm 2\%$  uncertainty in the RH probe measurement. The dashed orange lines show the predictions of the molar refraction mixing rule, while the dashed blue lines show the conventional volume fraction mixing rule predictions, taking  $n_{405}$  of water to be 1.343 and  $n_{405}$  for the pure, inorganic liquid melt to be equal to the corresponding  $C_0$  value in Table 1. The densities of the pure, inorganic melt are described using the model of Clegg and Wexler.<sup>41</sup> The dashed black line in (a) shows the prediction of the volume fraction mixing rule when the crystalline ammonium sulfate density ( $1.769$  g  $\text{cm}^{-3}$ ) is used with the ADIENT value of  $n_{405}$  (1.54) for pure ammonium sulfate.<sup>43</sup>

water,  $n_w$ , RIs as shown in eqn (6) where  $\phi_s$  is the volume fraction of solute.

$$n = \phi_s n_s + (1 - \phi_s) n_w \quad (6)$$

The volume fraction of solute can be calculated from the mass fraction of solute,  $m_s$ , provided the densities of the pure solute,  $\rho_s$ , and pure water,  $\rho_w$ , are known.

$$\phi_s = \frac{m_s \rho_w}{m_s (\rho_w - \rho_s) + \rho_s} \quad (7)$$

Although  $\rho_w$  is well known at  $25$  °C, the densities of pure liquid inorganic substances at  $25$  °C and atmospheric pressure cannot be measured. However, Clegg and Wexler calculated these values for numerous inorganic solutes, including  $(\text{NH}_4)_2\text{SO}_4$  and  $\text{NaNO}_3$ .<sup>41</sup> The variation of  $n_{405}$  with  $m_s$  can now be calculated,



taking  $n_{405}$  for water to be 1.343 and  $n_{405}$  for the pure solute to be the value of  $C_0$  in Table 1 (*i.e.* the extrapolated value from the measured  $n_{405}$  curve to RH = 0%). Finally, the Extended Aerosol Inorganics Model (E-AIM) is used to relate  $m_s$  to the RH.<sup>42</sup>

The molar refraction mixing rule uses a mole fraction,  $x$ , weighting of the molar refraction,  $R$ , as described by eqn (8) and (9) where  $M$  is the molecular mass.<sup>39</sup>

$$R = x_s R_s + (1 - x_s) R_w \quad (8)$$

$$R = \frac{(n^2 - 1)M}{(n^2 + 2)\rho} \quad (9)$$

Again, the value of  $n_{405}$  for water is taken as 1.343 and  $n_{405}$  for the pure solute as the appropriate  $C_0$  in Table 1. Further, the Clegg and Wexler model<sup>41</sup> is used to describe the variation in density with  $m_s$ , while the E-AIM model is used to relate mass fraction to the RH.<sup>42</sup> The RH-dependencies of these two mixing rule models are presented in Fig. 6 for both  $(\text{NH}_4)_2\text{SO}_4$  and  $\text{NaNO}_3$ , and compared against the respective measured variation of  $n_{405}$ . The dashed black line in Fig. 6 for  $(\text{NH}_4)_2\text{SO}_4$  is the RH variation of  $n_{405}$  predicted by the volume fraction mixing rule when density and pure component  $n_{405}$  are taken as the typical values implemented in radiative transfer models. In this case, the crystalline  $(\text{NH}_4)_2\text{SO}_4$  density ( $1.769 \text{ g cm}^{-3}$ ) is used, while  $n_{405}$  for pure  $(\text{NH}_4)_2\text{SO}_4$  is taken as 1.54, based on values recommended for radiative transfer modelling by the appraising direct impacts of aerosol on climate (ADIENT) database.<sup>43</sup> There are no recommended values of RI for  $\text{NaNO}_3$ . Clearly, the molar refraction mixing rule gives a very good description of  $n_{405}$  for both inorganic systems, while the conventional volume fraction mixing rule gives a poor description.<sup>39</sup> The molar refraction mixing rule is self-consistent with the Lorentz–Lorenz relation, a fundamental description of how the RI of a bulk material is related to its polarisability, while the volume fraction mixing rule has no physical basis.

#### IV. e Further investigation of sodium nitrate's behaviour at low (<10%) RH

In this section, we demonstrate that sodium nitrate aerosol does not always effloresce at low (< 10%) RH. The reproducibility in  $Q_{\text{ext}}$  can therefore be studied by cycling the RH between high (> 60%) and low values, which is of particular interest at low RH because the viscosity of sodium nitrate aerosol might reach appreciably high values. Thus, another aqueous  $\text{NaNO}_3$  droplet was subjected to detailed study, although in this instance the CRDS data were acquired at a wavelength of 532 nm using the apparatus described in previous publications.<sup>20,25,26</sup> As shown in the inset of Fig. 7(a), the trapping cell RH was initially at ~75% and was subsequently lowered and then held at an RH of ~2% for ~40 minutes. Over this measurement period, size determination from the PFs was reasonable (also shown in the inset to the figure) albeit with ~20 nm jumps in the particle radius at regular intervals, and the droplet radius steadily reduced. During the ~40 minute period at low RH, the droplet did not undergo efflorescence and remained trapped, with the size of the droplet stable. The RH was increased to high (~66%)

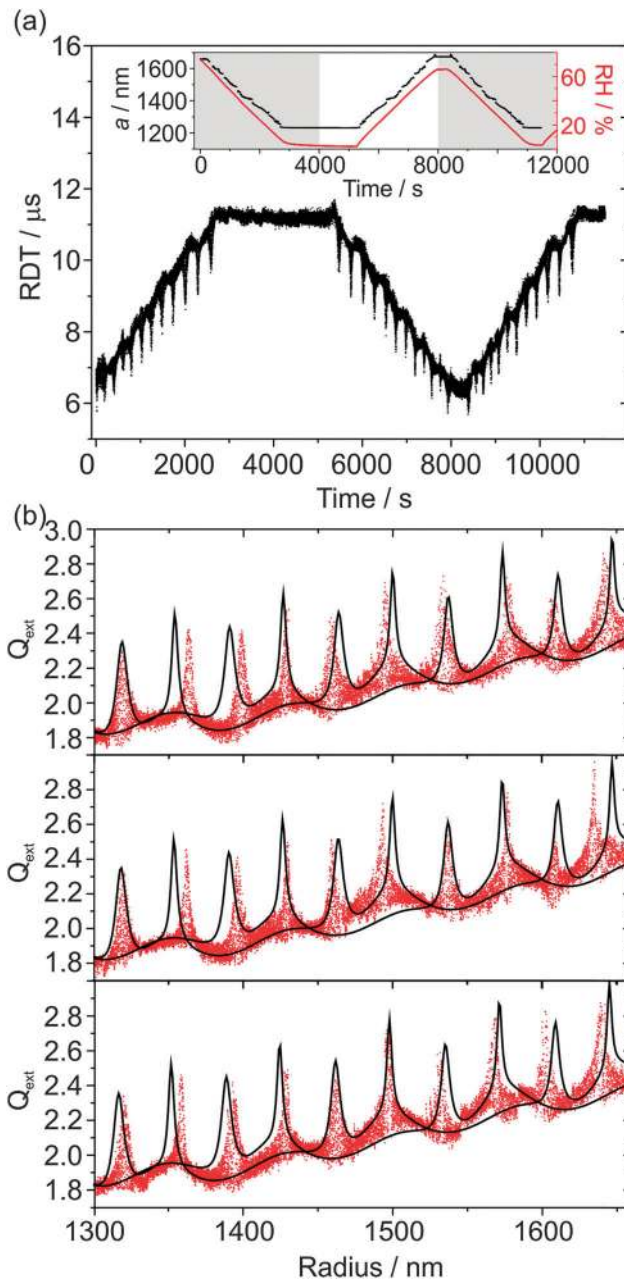


Fig. 7 (a) The measured RDTs over time for a  $\text{NaNO}_3$  droplet in an experiment in which the RH was cycled between low and high RH. The inset shows how the RH and droplet radius varied over time, while the shaded panels demark regions where the  $Q_{\text{ext}}$  were determined separately. (b) The determined  $Q_{\text{ext}}$  as a function of radius for the three regions highlighted in the inset of (a), with accompanying CSW Mie simulations.

RH, and then back to low RH to investigate the possibility that there might be hysteresis in the droplet's RDT and  $Q_{\text{ext}}$  data, in particular at the high viscosities anticipated at low RH. The cycling of the RH also allows us to examine the reproducibility in the determination of the optical properties of the aerosol. The resulting RDT values are shown as a function of time in the main panel of Fig. 7(a).

There is clear symmetry in the RDTs as the RH is cycled between high and low RH. The three different phases to the RH



cycling are now separately analysed in more detail, although the radius was determined from analysing all the PFs together for the three phases. These three phases are the first 4000 s during which the RH is initially lowered; 4000–8000 s in which the RH is subsequently increased; and 8000 s to the end of the measurement, for which the RH is once again lowered to  $\sim 3\%$ . These three phases are shown in the three panels of Fig. 7(b). There are a few mismatches in resonance peak locations in all cases resulting from the  $\sim 20$  nm jumps in the radius data, although there is reasonable agreement between the underlying contours of the measured  $Q_{\text{ext}}$  and the CSW simulations, implying that the fitted  $n_{532}$  is good. There is no noticeable hysteresis in the measured  $Q_{\text{ext}}$ , so there is no effect of inhibition of water transport between the droplet and the gas phase because of increases in viscosity on the timescales of RH variation performed here. The droplet finally fell from the trap at  $\sim 3\%$  RH upon the second RH reduction phase. This particle loss could be attributed to efflorescence, but could equally be due to the particle randomly exiting the trap through instability.

## V. Measurement of $Q_{\text{ext}}$ for accumulation mode aerosol

Up until this point we have only presented results for droplets which were larger than  $\sim 800$  nm in radius. As was discussed in the introduction, the most important aerosol particle size regime in terms of atmospheric optics is that for particles with radii  $> 200$  nm but  $< 1000$  nm. In this section, we report the first single particle  $Q_{\text{ext}}$  measurements, and companion CSW Mie theory simulations, for particles with radii ranging from 650 nm to as small as  $\sim 250$  nm. For these measurements, aerosol particles were optically trapped in a BB with a core diameter of  $\sim 3$   $\mu\text{m}$  and positioned in the centre of a  $\lambda = 532$  nm CRD beam for the measurement of  $Q_{\text{ext}}$ .

Fig. 8(a) shows the time-dependence of the measured radius (black data points) for a hexanetriol droplet evaporating from a radius of 1040 nm to  $\leq 300$  nm. As the radius of the droplet approaches the wavelength of the illuminating beam (532 nm), size determination of the droplet is unreliable as the PFs become featureless, giving 50–100 nm jumps in the fitted radius. Because the evaporation of hexanetriol is well described by the Maxwell mass-flux equation,<sup>10,19</sup> we fit a third order polynomial through the portion of the data which has been sized well using Mie theory (*i.e.*, for droplet radii  $> 400$  nm) and project the radius forwards in time, as shown by the solid red line in Fig. 8(a). The measured  $Q_{\text{ext}}$  data for this droplet, along with CSW Mie theory simulations, are shown in Fig. 8(b). The agreement between the CSW Mie theory simulations and the measured  $Q_{\text{ext}}$  data is excellent, with near-perfect agreement in the positions of resonance peaks even at droplet radii  $< 400$  nm. This good agreement at small particle sizes is emphasised in the inset, which shows an expanded portion of the data in the range 450–600 nm, and indicates that the use of

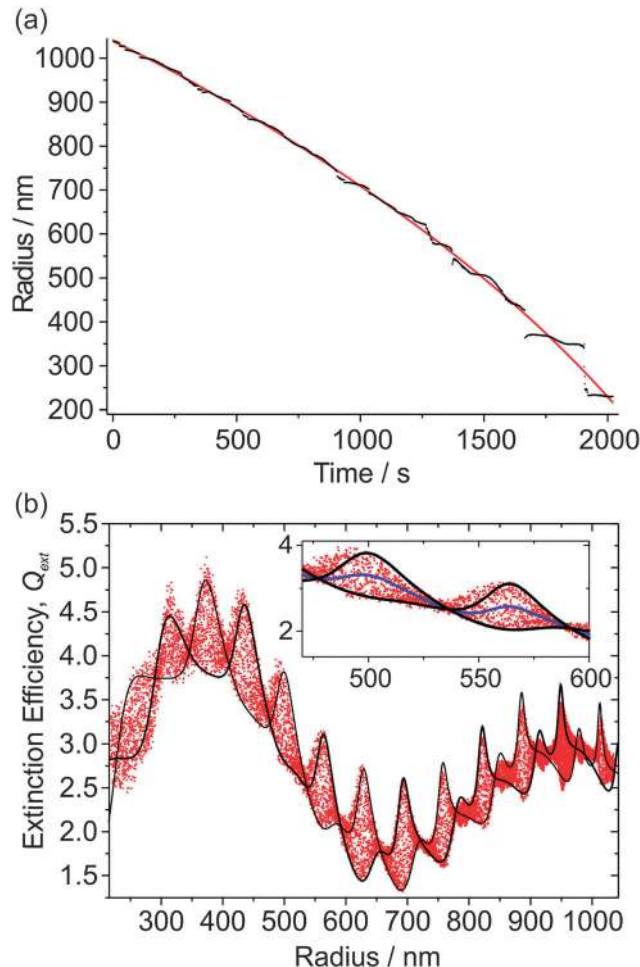


Fig. 8 (a) The determined radius as a function of time for a hexanetriol droplet which evaporates to accumulation mode sizes. A 3rd order polynomial is fitted to data  $> 400$  nm, and extrapolated to smaller radii (longer times). (b) The result of  $Q_{\text{ext}}$  fitting to CSW Mie simulations, using the radius determination from the third order polynomial fit.

a polynomial fit to predict the radius for small sizes was adequate in describing the size of the particle.

These results represent the first published single particle measurements of  $Q_{\text{ext}}$  for accumulation mode aerosol. The fitted  $n_{532}$  (which takes a constant value for this single-component system) is  $1.4823 \pm 0.0002$ , which is in reasonable agreement with previous single particle CRDS measurements for hexanetriol at  $\lambda = 532$  nm of  $1.4782 \pm 0.0007$ .<sup>25</sup> The value measured here agrees particularly well with the determined  $n_{532}$  from previously published radiation pressure measurements, which found  $n_{532}$  to be  $1.482 \pm 0.001$ .<sup>19</sup> Reasons for the difference in these values might be variations in the RH at which the measurements were performed; however the exact RH probe measurements were not reported in these previous publications.

The same experimental set-up was used to examine the hygroscopicity of a sub-650 nm aqueous  $\text{NaNO}_3$  droplet at  $\sim 68\%$  RH which evaporated to a radius  $< 500$  nm at low ( $\sim 2\%$ ) RH, as shown in Fig. 9(a). Because the droplet is so



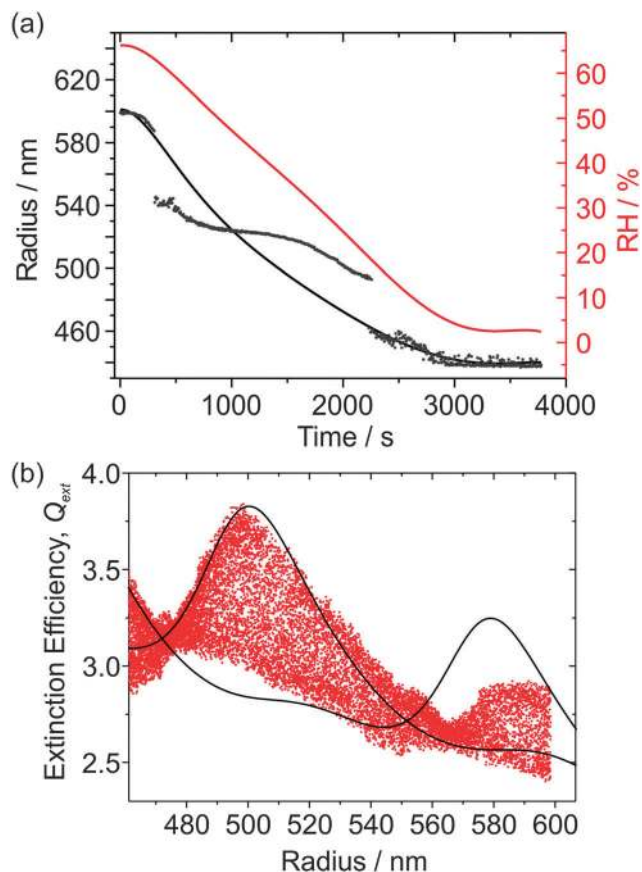


Fig. 9 (a) Plot of the measured radius vs. time (grey data points) for a hygroscopic growth experiment on a small sodium nitrate droplet, with the RH variation also plotted (red solid line). Also shown is a fit of a Kappa-Köhler curve to the radius data (black solid line). (b) Measured  $Q_{\text{ext}}$  with accompanying best fit CSW Mie theory simulations.

small, angular light scattering becomes featureless and sizing accuracy becomes poor. There are two  $\sim 50$  nm jumps in the determined radius, as well as unphysical undulations, despite smooth RH variation. Simply, the variation in scattering intensity with angle as recorded in the PF becomes increasingly featureless as the size diminishes, providing little constraint in the fitting of radius and RI. To describe the time variation in the droplet radius in a way which is more representative of the true radius evolution, a Kappa-Köhler dependence of the form:

$$a = a_0 \left( 1 + \kappa \frac{a_w}{1 - a_w} \right)^{1/3} \quad (10)$$

is fitted to the RH dependence of the size, where  $a_0$  is the radius of the particle at 0% RH,  $a_w$  is the activity of water (which is equal to the RH if the droplet is at equilibrium), and  $\kappa$  is a hygroscopicity parameter. Both  $\kappa$  and  $a_0$  were varied in a least squares fit of eqn (10) to the measured radius and this curve is shown as the black solid line in Fig. 9(a). Using this description of radius as a function of RH and thus time, the measured  $Q_{\text{ext}}$  were calculated for a given  $w$ , and fitted to CSW Mie simulations by varying  $w$ ,  $n_{1,532}$  and  $n_{2,532}$ . The best-fit measured  $Q_{\text{ext}}$  variation with size and corresponding CSW Mie simulations are

plotted in Fig. 9(b). The CSW Mie simulations give a reasonable description of the  $Q_{\text{ext}}$  variation, with the positions of resonance peaks and troughs in  $Q_{\text{ext}}$  well located. The underlying contour is well described at large particle sizes, but the description becomes poorer at small sizes, indicating that the RI or radius determination is not as well characterised as in previous hygroscopic growth measurements. This trend is expected at small particle sizes as we approach the experimental limits of the measurement where accurate determinations of RI and radius are not possible because the droplet radius is smaller than the illuminating wavelength used for PF acquisition. The accuracy of RI and radius determinations from PFs can be improved for sub-500 nm radius droplets by using a  $\sim 400$  nm illuminating wavelength, as demonstrated in our previous publication.<sup>19</sup>

## VI. Conclusions

A new experimental approach has been presented for the measurement of single aerosol particle  $Q_{\text{ext}}$  at a wavelength of 405 nm, combining CRDS ( $\lambda = 405$  nm) with BB optical confinement ( $\lambda = 532$  nm) in tandem with PF measurements. This technique has been benchmarked using semi-volatile droplets of 1,2,6-hexanetriol, allowing  $Q_{\text{ext}}$  to be measured over a continuous radius range. The measured distribution of  $Q_{\text{ext}}$  derives from the particle moving within the BB trap over a few microns, traversing several nodes and anti-nodes of the cavity standing wave, with the limits in  $Q_{\text{ext}}$  accounted for using CSW Mie theory. A residual is defined as the percentage of data points that fall outside the CSW Mie-theory simulation envelope and is minimized to obtain  $n_{405}$ . Repeat measurements for 10 evaporating hexanetriol droplets give a mean value for  $n_{405}$  of  $1.4906 \pm 0.0012$ , in good agreement with previous determinations from radiation pressure measurements ( $1.485 \pm 0.006$ ).<sup>19</sup>

For hygroscopic inorganic aerosol particles exposed to a decreasing RH, both particle radius and RI change as water partitions from the aerosol particle into the gas phase. A parameterisation of  $n_\lambda$  in terms of the particle radius is presented, consisting of 2 or 3 fit parameters (depending on the inorganic species) which are optimised to maximise the mean correlation between the measured PFs and Mie theory simulations. Radius and RI determinations from PFs ( $\lambda = 532$  nm) for both an aqueous  $(\text{NH}_4)_2\text{SO}_4$  and a  $\text{NaNO}_3$  droplet are presented. For both these systems, the determined  $n_{532}$  variation with RH agrees well with previous parameterisations by Tang *et al.*, indicating correct  $n_{532}$  determination.<sup>27,34</sup> Best-fit  $Q_{\text{ext}}$  variation to CSW Mie simulations allows  $n_{405}$  to be evaluated. For these simulations,  $n_{405}$  was fitted using a parameterisation relating  $n_{405}$  to the droplet radius in the same way as performed in the PF fitting procedure. The results show excellent agreement between the resonance peak positions of the measured  $Q_{\text{ext}}$  and CSW Mie simulations and a good description of the underlying contour of the data. This indicates accurate size determination from fitting the PFs and good  $n_{405}$  determination by CRDS. There are no literature parameterisations for the



variation in  $n_{405}$  with RH for either  $(\text{NH}_4)_2\text{SO}_4$  or  $\text{NaNO}_3$  with which to compare our results. However,  $n_{405}$  is shifted to higher values of RI compared to  $n_{532}$ , as expected given typical dispersion behaviour for most materials. Polynomials of the form of eqn (5) were fitted to the measured  $n_{405}$  and  $n_{532}$  variation with water activity,  $a_w$ , for both  $(\text{NH}_4)_2\text{SO}_4$  and  $\text{NaNO}_3$ . Table 1 summarises the coefficients obtained in these fits. The measured  $n_{405}$  variations for both a  $(\text{NH}_4)_2\text{SO}_4$  droplet and a  $\text{NaNO}_3$  droplet were compared with those predicted using two commonly encountered mixing rules. The volume fraction mixing rule gives poor agreement with the measured  $n_{405}$  data, even though extrapolated solute melt densities are used. However, the molar refraction mixing rule gives good agreement with the measured  $n_{405}$  data.

Although the first  $\text{NaNO}_3$  droplet reported here was observed to fall out of the BB trap at  $\sim 12\%$  RH, many subsequent droplets remained trapped to as low as  $\sim 2\%$  RH without undergoing crystallisation. When the RH was kept at  $\sim 2\%$  for  $\sim 40$  minutes, and subsequently increased to high RH and to low RH once more, no hysteresis was observed in the measured  $Q_{\text{ext}}$ , indicating that there is no inhibition of water transport from the aerosol particle to the gas phase on the timescales of the RH variation.

We present the first single particle measurements of  $Q_{\text{ext}}$  for accumulation mode aerosol. The measured  $Q_{\text{ext}}$  variation is shown for a sub-micron hexanetriol droplet evaporating from an initial radius of 1040 nm to  $\leq 300$  nm, which is well within the accumulation mode regime. The radius below  $\sim 400$  nm is poorly determined because the droplet radius is less than the wavelength of light. The evaporation of hexanetriol is described by the Maxwell mass flux equation, allowing extrapolation of a third order polynomial fitted to the  $>400$  nm radius data. The agreement between the measured  $Q_{\text{ext}}$  and the fitted CSW Mie simulations is good, even at small radii where the droplet radius has been predicted using the polynomial extrapolation. Finally, the hygroscopicity of a sub-650 nm  $\text{NaNO}_3$  droplet is studied as it evaporates and shrinks to a radius  $< 500$  nm at low ( $\sim 2\%$ ) RH. The radius determination by PF analysis is poor in this size regime. Using the measured RH variation, a Kappa Köhler curve is fitted to the radius data to describe the radius evolution. Using this description for radius, the  $Q_{\text{ext}}$  variation with size is presented along with best fit CSW Mie simulations. These simulations give a reasonable description of the measured  $Q_{\text{ext}}$  variation. The limitations in the radius determination by PF analysis might be improved by using a shorter wavelength laser source to illuminate the droplet.

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