Article

# Optimal Allocation Method for Energy Storage Capacity Considering Dynamic Time-of-Use Electricity Prices and On-Site Consumption of New Energy 

Wei Hu ${ }^{\mathbf{1 , 2}}$, Xinyan Zhang ${ }^{1, *}$, Lijuan Zhu ${ }^{\mathbf{1 , 2}}$ and Zhenen Li ${ }^{1}$<br>1 School of Electrical Engineering, Xinjiang University, Urumqi 830017, China; huwei96301@163.com (W.H.); qingyouloveyue@163.com (L.Z.); lizhenenlut@163.com (Z.L.)<br>${ }^{2}$ School of Mechanical and Electrical Engineering, Xinjiang Institute of Technology, Aksu 843100, China<br>* Correspondence: xjcxzxy@126.com

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#### Abstract

Configuring energy storage devices can effectively improve the on-site consumption rate of new energy such as wind power and photovoltaic, and alleviate the planning and construction pressure of external power grids on grid-connected operation of new energy. Therefore, a dual layer optimization configuration method for energy storage capacity with source load collaborative participation is proposed. The external model introduces a demand-side response strategy, determines the peak, flat, and valley periods of the time-of-use electricity price-based on the distribution characteristics of load and new energy output, and further aims to maximize the revenue of the wind and solar storage system. With the peak, flat, and valley electricity price as the decision variable, an outer optimization model is established. Based on the optimized electricity price, the user's electricity consumption in each period is adjusted, and the results are transmitted to the inner optimization model. The internal model takes the configuration power and energy storage capacity in the wind and solar storage system as decision variables, establishes a multi-objective function that comprehensively considers the on-site consumption rate of new energy and the cost of energy storage configuration, and feeds back the optimization results of the inner layer to the outer layer optimization model. Use ISSA-MOPSO algorithm to solve the optimized configuration model. Finally, the rationality of the proposed model and algorithm in terms of on-site consumption rate and economy of new energy is verified through numerical examples.


Keywords: dynamic electricity price; demand-side response; on site consumption of new energy; new energy; energy storage; absorption

## 1. Introduction

With the intensification of the energy crisis, renewable energy represented by wind and solar has been vigorously developed. However, the intermittent fluctuation of wind and solar has affected the security and stability of the grid and increased the cost of grid transformation [1,2]. Energy storage can enhance the value of wind and solar resources due to its fast response and flexible charging and discharging characteristics.

At present, the cost of energy storage is relatively high, and it is necessary to reasonably optimize configuration capacity and fully coordinate the availability and economy of energy storage. Currently, the issue of optimizing the configuration of energy storage has received widespread attention from scholars at home and abroad [3-5]. Li et al. [6] comprehensively considered the multi-objective optimization configuration method for energy storage with minimal comprehensive cost and load fluctuation and proposed an improved fast non-dominated sorting genetic algorithm for model solving. Khezri et al. [7] proposed a configuration scheme for grid-connected rooftop photovoltaic systems, discussing two scenarios: independent grid connection and joint energy storage grid connection. The impact of different factors such as grid constraints, load demand, roof space, and energy
storage subsidies on the configuration results was analyzed in detail, providing practical solutions for users to configure their photovoltaic storage capacity. Wu et al. [8] used cloud model theory combined with the k-means method to obtain typical scenarios of charge-discharge curves and studied the configuration of wind farm energy storage capacity. El-Bidairi et al. [9] established a multi-objective optimization method to reduce microgrid fuel consumption and greenhouse gas emissions and proposed an energy storage configuration method based on a combination of expert fuzzy system and grey wolf optimization algorithm. Kong et al. [10] proposed a multi-objective optimization method that considers economy, technology, and environment and analyzed the relationship between the proportion of renewable energy and energy storage configuration. Cai et al. [11] aiming at improving the utilization of wind energy, proposed a method based on wind power consumption timing scenario to establish a battery energy storage configuration model, and verified the effectiveness of the method with the actual data validation of the power grid. Barrera-Santana et al. [12] studied the capacity planning scheme of an island power system, discussed in detail different energy composite patterns such as renewable energy, energy storage, electric vehicles, and HVDC transmission, and concluded that energy storage has an important impact on power generation capacity planning and operation. Naderipour et al. [13] focused on the optimal ratio of photovoltaic energy, wind power, inverters, and energy storage capacity for hybrid energy systems in remote areas. With the goal of optimizing the system's economy, an improved grasshopper algorithm is proposed to solve the optimization model, and the impact of interest rates on the model is emphasized. Nazir et al. [14] studied the optimization configuration of energy storage capacity under wind farm prediction errors to increase the reliability of wind farm output power and analyzed the benefits of energy storage facilities under different confidence levels. Pires et al. $[15,16]$ studied the optimal allocation strategy of wind and solar storage capacity in microgrid scenarios and established a multi-objective model for system economy and carbon emissions. The above literature mainly analyzes the important role of energy storage configuration in the planning and operation of wind and solar systemsand establishes a configuration plan that includes wind and solar storage as the main facility. However, it lacks the exploration of demand-side flexibility resources in the system and ignores the beneficial impact of source load interaction on energy storage optimization configuration.

In recent years, under the background of power market reform, demand-side management policies based on electricity prices, incentives, etc. have been gradually promoted. As an important and flexible adjustment method, demand response has been introduced into the research of optimal allocation of energy storage. Kou et al. [17] proposed to reduce the capacity allocation of energy storage by stimulating demand response, which improved the economy of grid-connected system. In order to improve energy utilization, Yan et al. [18] discussed the use of price-based demand response to reduce the investment cost of energy storage system. V. et al. [19] analyzed the impact of demand-side response on the system environment and economy when optimizing the configuration of hybrid energy sources such as wind power, photovoltaic, energy storage, and distributed power generation. Honarmand et al. [20] studied the planning of an energy hub system with renewable energy and introduced the price-based demand response into the optimization model to smooth the load curve and reduce the system operation cost. The results show that the scheme can effectively reduce the allocation capacity of energy storage. Kiptoo et al. [21,22] has studied the scale of energy storage and other equipment in the cost minimization scheme under different demand-side response resource allocation strategies the results show that the demand response strategy can improve the flexibility of the system and the economy of energy storage configuration. References [17-22] studied energy storage configuration models from multiple perspectives, such as energy storage configuration scenarios and demand-side responses. At present, the speed of new energy construction in the region exceeds the absorption capacity, and the power grid construction is not coordinated with new energy construction. The local consumption of new energy is still the most economical way. Some scholars have investigated [23], but at present, there is little research on methods
of applying demand response strategy to energy storage configuration around the local consumption of new energy.

Therefore, this article constructs a two-layer nested model for source load storage coordination optimization. The outer model is based on the optimized time-of-use period, with the time-of-use electricity price as the decision variable, and the objective function is established to maximize the revenue of the wind and solar storage system. The inner model takes the configured power and capacity of energy storage in the wind and solar storage system as the decision variables and establishes a multi-objective function that comprehensively considers the on-site consumption rate of new energy and the cost of energy storage configuration. The combination of sparrow algorithm and multi-objective particle swarm optimization algorithm is used to solve the model and the optimization results of new energy local consumption rate and economy of the system under different electricity prices and energy storage configurations are obtained. Further, the impact of different penalty factors on energy storage configuration scheme is discussed.

## 2. Structure of Wind and Solar Energy Storage System

Wind power, photovoltaic cells, and energy storage systems are connected to wind and solar storage systems through their respective converters and connected to the external power grid. According to the characteristics of electricity consumption, loads can be divided into two categories: fixed load and flexible load. In grid-connected wind and solar energy storage systems, wind and solar power are prioritized for supplying local loads, and excess electricity can be sent to the external power grid. When the power supply is insufficient, electricity is purchased from the external power grid to meet the electricity needs of local users. The wind and solar storage system studied in this article is shown in Figure 1.


Figure 1. Wind and solar storage system.

## 3. Demand Response Model Considering Time Division and Price Optimization

### 3.1. Time Period Division Based on Fuzzy C-Means Clustering

With the gradual advancement of China's power market reform policy, the demand response mechanism on the user side plays an increasingly important role in the safe and economic operation of the power grid, and the time-sharing price has been widely used in demand-side management. Renewable energy wind power, photovoltaic power generation, and their loads are constantly fluctuating due to factors such as wind speed, light, and temperature. The division of time periods in traditional time-of-use electricity prices is generally calculated by the power department based on experience, and the division of time periods is generally fixed throughout the year, which does not fully reflect the
characteristics of wind and photovoltaic power generation changes in different seasons. A fixed time-of-use electricity price is not conducive to the consumption of renewable energy. In order to fully tap into the flexible adjustment ability of demand-side resources, this article adopts dynamic time-of-use electricity prices, which update peak, flat, and valley periods based on the typical daily renewable energy generation and load electricity consumption throughout the year. The difference between the predicted load power and the wind and light output power is defined as the net load $P_{\text {net }}$, i.e., $P_{\text {net }}=P_{\text {load }}-P_{\mathrm{PV}}-P_{\mathrm{WT}}$, and the set of predicted net load power is obtained as $P_{\text {net }}=\left\{q_{1}, q_{2}, \cdots, q_{23}, q_{24}\right\}$. This article uses the fuzzy C-means method to determine the peak, flat, and valley periods.

The peak and valley membership of each time period is calculated using larger and smaller semi trapezoidal membership functions, as shown in (1).

$$
\left\{\begin{array}{l}
\xi_{i}^{\mathrm{p}}=\frac{q_{i}-\min \left(q_{i}\right)}{\max \left(q_{i}\right)-\min \left(q_{i}\right)}  \tag{1}\\
\tilde{\xi}_{i}^{1}=\frac{\max \left(q_{i}\right)-q_{i}}{\max \left(q_{i}\right)-\min \left(q_{i}\right)}
\end{array}\right.
$$

In the formula, $q_{i}$ is the net load of the $i$-th period.
According to the sample set $\xi=\left\{\tilde{\zeta}_{1}^{\mathrm{p}}, \xi_{1}^{1} ; \xi_{2}^{\mathrm{p}}, \xi_{2}^{1} ; \cdots ; \xi_{24}^{\mathrm{p}}, \xi_{24}^{1}\right\}$, the cluster center is set as $C_{k}(k=1,2,3)$, and $u_{k i}$ is used to represent the membership degree of the $i$ th sample belonging to the $k$ class. Then the fuzzy C-means clustering of $\xi$ is the minimum value for solving the loss function $J$.

$$
\left\{\begin{array}{l}
\min J\left(\xi, C_{1}, C_{2}, C_{3}\right)=\sum_{i=1}^{24} \sum_{k=1}^{3}\left(u_{k i}\right)^{m}\left\|\xi_{i}-C_{k}\right\|^{2}  \tag{2}\\
0 \leq u_{k i} \leq 1 \\
\sum_{k=1}^{3} u_{k i}=1
\end{array}\right.
$$

In the formula, $m$ refers to the fuzzy weighted index, generally $m=2$ [24].
The necessary condition for obtaining the minimum value of $J\left(\xi, C_{1}, C_{2}, C_{3}\right)$ is that both $\partial J / \partial u_{k i}$ and $\partial J / \partial C_{k}$ are zero, i.e.,:

$$
\begin{gather*}
u_{k i}=\frac{1}{\sum_{j=1}^{3}\left(\frac{\left\|\xi_{i}-C_{k}\right\|}{\left\|\xi_{i}-C_{j}\right\|}\right)^{\frac{2}{m-1}}}  \tag{3}\\
C_{k}=\frac{\sum_{i=1}^{24} u_{k i}^{m} \cdot \xi_{i}}{\sum_{i=1}^{24} u_{k i}^{m}} \tag{4}
\end{gather*}
$$

The initial membership matrix and clustering termination conditions are set and Equations (3) and (4) are iteratively collected to finally output the clustering results for each period of peak-valley leveling. To improve the smoothness of demand-side response load operation, it is stipulated that each time period shall not be less than 2 h , and any time period that does not meet the division requirements shall be corrected.

### 3.2. Price Setting

The establishment of appropriate time-of-use price can actively guide users to change their electricity consumption behavior, thus helping to play a greater role in demand response in reducing the pressure of system peak shaving and improving the consumption of new energy. In order to reflect the relationship between electricity prices and user electricity
demand, the concept of demand price elasticity coefficient in the field of economics is often introduced [25,26], which is

$$
\begin{gather*}
\varepsilon_{i j}=\frac{\Delta P(i)}{P_{\text {out0 } 0}(i)}\left(\frac{\Delta p_{1}(j)}{p_{0}(j)}\right)^{-1}  \tag{5}\\
\Delta P(i)=P_{\text {out1 }}(i)-P_{\text {out } 0}(i)  \tag{6}\\
\Delta p(j)=p_{1}(j)-p_{0}(j) \tag{7}
\end{gather*}
$$

In the formula, $P_{\text {out } 0}(i)$ and $P_{\text {out } 1}(i)$ are the load values before and after the electricity price adjustment for period $i$, and $p_{0}(j)$ and $p_{1}(j)$ are the electricity prices before and after adjustment in period $j$; when the moments $i$ and $j$ are equal, $\varepsilon_{i j}$ is the self-elastic coefficient; otherwise it is the cross-elastic coefficient. The elasticity matrix based on the time-of-use electricity price is

$$
E=\left[\begin{array}{cccc}
\varepsilon_{11} & \varepsilon_{12} & \cdots & \varepsilon_{1 t}  \tag{8}\\
\varepsilon_{21} & \varepsilon_{22} & \cdots & \varepsilon_{2 t} \\
\vdots & \vdots & \vdots & \vdots \\
\varepsilon_{t 1} & \varepsilon_{t 2} & \cdots & \varepsilon_{t t}
\end{array}\right]
$$

After implementing the time-of-use electricity price, the electricity consumption in the period $i$ with a daily cycle is

$$
\begin{equation*}
P_{\text {out1 }}(i)=P_{\text {out } 0}(i)\left[1+\varepsilon_{i i} \frac{p_{1}(i)-p_{0}(i)}{p_{0}(i)}+\sum_{j=1, j \neq i}^{24} \varepsilon_{i j} \frac{p_{1}(j)-p_{0}(t)}{p_{0}(t)}\right] \tag{9}
\end{equation*}
$$

## 4. Build a Coordinated Optimization Model for Time-of-Use Electricity Prices and Energy Storage Capacity

The user load distribution changes due to demand response, which affects the energy storage configuration and dispatching results of the wind-solar storage system. Different energy storage configurations also affect different time-sharing pricing strategies. In response to the coordination optimization problem of energy storage configuration and dynamic time-of-use electricity price in wind and solar storage systems, this section adopts a double-layer optimization model, with the time-of-use electricity price as the decision variable and the problem of maximizing the revenue of the wind and solar storage system as the objective. The configuration power and capacity of energy storage in the wind and solar storage system are used as the decision variables, and the problem of considering the on-site consumption rate of new energy such as wind and solar and the configuration cost of energy storage is described in the inner layer. The construction architecture of the two-layer optimization model is shown in Figure 2.

### 4.1. External Revenue Model Considering Demand-Side Response

### 4.1.1. Objective Function

The outer layer aims to maximize the revenue of the wind and solar energy storage system, which can be expressed as:

$$
\begin{equation*}
\max F \tag{10}
\end{equation*}
$$

In the formula, $F$ represents the revenue of the wind and solar energy storage system. The benefits of the wind and solar energy storage system can be calculated by Equation (11):

$$
\begin{equation*}
F=I_{\text {sell }}+I_{\text {line-grid }}-C_{\text {grid-line }}-C_{\text {ope }}-C_{\text {line }}+I_{\text {lc }} \tag{11}
\end{equation*}
$$

$$
\begin{align*}
& \left\{\begin{array}{l}
I_{\text {sell }}=\sum_{t=1}^{24} p_{1}(t) P_{\text {out1 }}(t) \\
I_{\text {line-grid }}=\sum_{t=1}^{24}\left[p_{\text {line-grid }} P_{\text {line-grid }}(t)\right] \\
C_{\text {grid-line }}=\sum_{t=1}^{24} p_{\text {grid-line }} P_{\text {grid-line }}(t) \\
C_{\text {line }}=K_{\text {line }} \frac{1}{24} \sum_{t=1}^{24}\left(\left|P_{\text {line }, t}\right|-\frac{1}{24} \sum_{t=1}^{24}\left|P_{\text {line }, t}\right|\right)^{2} \\
I_{\mathrm{lc}}=\sum_{t=1}^{24}\left[P_{\mathrm{PV}}(t)+P_{\mathrm{WT}}(t)\right] r_{c} p_{c}
\end{array}\right.  \tag{12}\\
& p_{1}(t)=\left\{\begin{array}{l}
p_{g} t \in T_{g} \\
p_{f} t \in T_{f} \\
p_{p} t \in T_{p}
\end{array}\right. \tag{13}
\end{align*}
$$



Figure 2. Architecture of the bilevel programming model.
In the formula, $I_{\text {sell }}$ represents the system's electricity sales revenue to users; $I_{\text {line-grid }}$ represents the revenue from selling electricity to the external power grid of the system; $C_{\text {grid-line }}$ represents the cost of purchasing electricity from the solar energy storage system to the external power grid; $C_{\text {ope }}$ represents the daily operating cost of energy storage; $C_{\text {line }}$ represents the penalty cost for power fluctuations in the interconnection line; $I_{\text {IC }}$ represents low-carbon benefits. Carbon trading is a mechanism for reducing carbon dioxide emissions in a market environment, which is an important way to develop a low-carbon economy. Here, low-carbon benefits are quantified and included in the benefits of wind and solar energy storage systems; $p_{1}(t)$ represents the electricity price sold by the optimized wind
and solar storage system to users; $P_{\text {out1 }}(t)$ represents the power after users participate in demand response; $P_{\text {line-grid }}(t)$ is the selling power of the solar energy storage system to the external power grid, and $p_{\text {line-grid }}$ is the purchasing electricity price of the external power grid; $P_{\text {grid-line }}(t)$ is the purchasing power of the solar energy storage system from the external power grid, and $p_{\text {grid-line }}$ is the selling electricity price of the external power grid; $P_{\text {line }}(t)$ and $K_{\text {line }}$ respectively represent the power of the interconnection line and its fluctuation penalty coefficient; $r_{\mathrm{c}}$ represents the carbon emissions that can be reduced per unit of renewable energy generation, and $p_{\mathrm{c}}$ represents the carbon trading price; $P_{\mathrm{WT}}(t)$ and $P_{\mathrm{PV}}(t)$ are the grid power of wind power and photovoltaic power, respectively; $p_{p}$. $p_{f}$ and $p_{g}$ respectively represent peak, flat, and valley electricity prices; $T_{p}, T_{f}$, and $T_{g}$ represent peak, flat, and valley periods, respectively.

### 4.1.2. Constraints

(1) The total load after the user participates in demand response will remain unchanged, and the load change in any time period will be controlled within a certain range to ensure the power demand of the user.

$$
\begin{gather*}
\sum_{t=1}^{24} P_{\text {out } 1}(t)=\sum_{t=1}^{24} P_{\text {out } 0}(t)  \tag{14}\\
|\Delta P(t)| \leq \Delta P_{\max }(t) \tag{15}
\end{gather*}
$$

(2) The implementation of time-of-use tariff has changed users' electricity consumption habits to a certain extent and reduced their comfort. Therefore, it is necessary to ensure the economy of users' participation in demand response, so as to mobilize users' enthusiasm for electricity consumption. It is stipulated that the total electricity cost before users' participation in demand response should not be greater than the total electricity cost when users do not participate in demand response.

$$
\begin{equation*}
\sum_{t=1}^{24} p_{1}(t) P_{\text {out } 1}(t) \leq \sum_{t=1}^{24} p_{0}(t) P_{\text {out } 0}(t) \tag{16}
\end{equation*}
$$

(3) Improper time-of-use electricity prices can lead to peak-valley inversion or insufficient response, so it is necessary to constrain the peak-valley electricity price ratio.

$$
\begin{gather*}
k_{1} \leq \frac{p_{p}}{p_{g}} \leq k_{2}  \tag{17}\\
0 \leq p_{g}<p_{f}<p_{p} \leq p_{\max } \tag{18}
\end{gather*}
$$

In the formula, the range of peak-to-valley electricity price ratio is usually taken as $2-5$ [27], and $k_{1}=2$ and $k_{2}=5$ are taken; $p_{\max }$ is the upper limit of peak electricity price in this paper.
(4) Marginal cost constraint in valley time

$$
\begin{equation*}
p_{\mathrm{g}} \geq C_{0} \tag{19}
\end{equation*}
$$

where, $C_{0}$ is the marginal cost of the valley period.

### 4.2. Internal Multi-Objective Model Considering the Daily Life Loss Cost of Energy Storage

Based on the load data optimization results of the outer time-of-use electricity price model, with the goal of maximizing the on-site consumption rate of new energy and minimizing the cost of energy storage configuration, appropriate capacity and power are allocated for the energy storage equipment in the wind and solar storage system. The daily operating
cost of the entire life cycle of the energy storage system is further established, and the inner optimization results are fed back to the outer optimization problem for further solving.

### 4.2.1. Energy Storage Cycle Life Loss Model

In the optimization configuration of energy storage that takes into account the entire life cycle, initial investment cost and cycle life are important factors to consider, while the life loss during energy storage is mainly determined by the discharge depth [28]. Different charging and discharging depths restrict the different recyclable times of energy storage, thereby affecting the length of energy storage cycle life. Among various energy storage materials, lithium batteries have high charging and discharging efficiency as well as high specific energy and power. This article selects lithium battery energy storage as the research object.
(1) Battery discharge depth

$$
\begin{align*}
& \operatorname{DOD}(t)=1-\operatorname{SOC}(t)  \tag{20}\\
& \mathrm{SOC}(t)=\frac{E(t)}{E_{\mathrm{ESS}}^{\mathrm{R}}} \times 100 \% \tag{21}
\end{align*}
$$

In the formula, $\mathrm{SOC}(t)$ and $\mathrm{DOD}(t)$ respectively represent the state of charge and discharge depth at time $t ; E(t)$ is the amount of electricity stored at the time $t$ of energy storage; $E_{\mathrm{ESS}}^{\mathrm{R}}$ is the rated capacity of energy storage.
(2) Equivalent number of cycles model

The cycle life of energy storage [29] is shown in (22):

$$
\begin{equation*}
N_{\text {life }}=N_{0}(\mathrm{DOD})^{-\mathrm{k}_{\mathrm{p}}} \tag{22}
\end{equation*}
$$

In the formula, $N_{\text {life }}$ represents the number of cycles in the energy storage life cycle; $N_{0}$ represents the number of life cycle cycles corresponding to energy storage at $100 \%$ discharge depth; DOD represents the actual discharge depth of energy storage; both $N_{0}$ and $K_{p}$ are known parameters given by the energy storage battery manufacturer.

Each time the energy storage battery is charged and discharged, it cannot be guaranteed that the discharge depth remains unchanged. It needs to be converted to a unified standard for statistics. Generally, it is converted according to the equivalent $100 \%$ discharge depth. The number of equivalent cycles $n_{\mathrm{eq}}(t)$ for a single time can be calculated using Equation (23):

$$
\begin{gather*}
n_{\mathrm{eq}, t}^{100} \approx[\Delta \mathrm{DOD}(t)]^{k_{p}}  \tag{23}\\
\Delta \mathrm{DOD}(t)=\frac{E_{a}(t)}{E_{\mathrm{ESS}}^{\mathrm{R}}}  \tag{24}\\
E_{a}(t)=\left[\eta_{\text {cha }} P_{\text {cha }}(t)+\eta_{\text {dis }}-1 P_{\text {dis }}(t)\right] \Delta t \tag{25}
\end{gather*}
$$

In the formula, $\eta_{\text {cha }}$ and $\eta_{\text {dis }}$ are the charging and discharging efficiency, respectively; $P_{\text {cha }}(t)$ and $P_{\text {dis }}(t)$ are, respectively, charging and discharging power; $E_{a}(t)$ is the charging and discharging capacity of energy storage during period $t ; \mathrm{DOD}(t)$ represents the discharge depth of energy storage during period $t$.

The daily equivalent cycle number $N_{\text {eq }}$ of energy storage batteries can be obtained from Equation (26):

$$
\begin{equation*}
N_{\mathrm{eq}}^{\mathrm{day}}=\sum_{t \in \mathrm{cha}} n_{\mathrm{eq}}^{100, \mathrm{cha}}(t)+\sum_{t \in \mathrm{dis}} n_{\mathrm{eq}}^{100, \mathrm{dis}}(t) \tag{26}
\end{equation*}
$$

In the formula, when the energy storage battery is in the charging or discharging state during period $t$, the equivalent number of cycles during that period is represented by $n_{\mathrm{eq}}^{100, \text { cha }}(t)$ and $n_{\mathrm{eq}}^{100, \text { dis }}(t)$, respectively.
(3) The equivalent cycle life of energy storage is

$$
\begin{equation*}
T_{\mathrm{cyc}}=\frac{N_{0}}{365 \cdot N_{\mathrm{eq}}^{\mathrm{day}}} \tag{27}
\end{equation*}
$$

(4) The daily cycle life loss cost of energy storage is

$$
\begin{gather*}
C_{\text {loss }}=\left(c_{\mathrm{P}} P_{\mathrm{ESS}}^{\mathrm{R}}+c_{\mathrm{E}} E_{\mathrm{ESS}}^{\mathrm{R}}\right) \frac{\beta(1+\beta)^{T_{\mathrm{cyc}}}}{365 \cdot(1+\beta)^{T_{\mathrm{cyc}}}-1}  \tag{28}\\
K_{\mathrm{ESS}}^{\mathrm{D}}=\frac{\beta(1+\beta)^{T_{\mathrm{cyc}}}}{365 \cdot(1+\beta)^{T_{\mathrm{cyc}}}-1} \tag{29}
\end{gather*}
$$

In the formula, $c_{\mathrm{P}}$ and $c_{\mathrm{E}}$ are the cost per unit power and per unit capacity of the energy storage system, respectively; $\beta$ is the discount rate; $K_{\mathrm{ESS}}^{\mathrm{D}}$ is the isodiurnal coefficient; $E_{\mathrm{ESS}}^{\mathrm{R}}$ and $P_{\mathrm{ESS}}^{\mathrm{R}}$ represent the rated capacity and power of the energy storage configuration, and they are the internal decision variables.

### 4.2.2. Daily Cost of Energy Storage throughout Its Entire Life Cycle

The daily operating cost $C_{\text {ope }}$ of the entire life cycle of the energy storage system is composed of the daily investment cost $C_{\text {investment }}$, daily operation and maintenance cost $C_{\text {maintenance, }}$ and daily loss cost $C_{\text {loss }}$. The calculation formula is shown in Equation (32).

$$
\begin{gather*}
C_{\text {investment }}=\left(c_{\mathrm{P}} P_{\mathrm{ESS}}^{\mathrm{R}}+c_{\mathrm{E}} E_{\mathrm{ESS}}^{\mathrm{R}}\right) \frac{\beta(1+\beta)^{\gamma_{\mathrm{a}}}}{365 \times(1+\beta)^{Y_{\mathrm{a}}}-1}  \tag{30}\\
C_{\text {maint }}=\frac{c_{\text {maint }} E_{\mathrm{ESS}}^{\mathrm{R}}}{365}  \tag{31}\\
C_{\text {ope }}=C_{\text {investment }}+C_{\text {maintenance }}+C_{\text {loss }} \tag{32}
\end{gather*}
$$

In the formula, $Y_{\mathrm{a}}$ is the investment period of the energy storage system; $C_{m a i n t}$ is the average annual maintenance cost per unit capacity of energy storage.

### 4.2.3. Objective Function

In the formula, $f_{1}$ is the on-site consumption rate of new energy; $f_{2}$ is the configuration cost of energy storage, $P_{\mathrm{SC}}(t) . P_{\mathrm{bat}}(t)$ represents the new energy consumed by the load and energy storage at time $t$.

$$
\left\{\begin{array}{l}
\max f_{1}  \tag{33}\\
f_{1}=\left[\begin{array}{c}
\left.\frac{\sum_{t=1}^{24}\left(P_{\mathrm{SC}}(t)+\left|P_{\mathrm{bat}}(t)\right|\right)}{\sum_{t=1}^{24}\left(P_{\mathrm{PV}}(t)+P_{\mathrm{WT}}(t)\right)}\right] \times 100 \%, P_{\mathrm{SC}}(t)=\min \left\{P_{\mathrm{PV}}(t)+P_{\mathrm{WT}}(t), P_{\mathrm{out}}(t)\right\} \\
\min f_{2} \\
f_{2}=c_{\mathrm{E}} \times E_{\mathrm{ESS}}^{\mathrm{R}}+c_{\mathrm{P}} \times P_{\mathrm{ESS}}^{\mathrm{R}}
\end{array}\right.
\end{array}\right.
$$

### 4.2.4. Constraints

(1) Power balance constraints

$$
\left\{\begin{array}{l}
P_{\mathrm{WT}}(t)+P_{\mathrm{PV}}(t)+P_{\mathrm{ESS}}(t)-P_{\text {line }}(t)=P_{\text {load }}(t)  \tag{34}\\
0 \leq P_{\mathrm{WT}}(t) \leq P_{\mathrm{WTY}}(t) \\
0 \leq P_{\mathrm{PV}}(t) \leq P_{\mathrm{PVY}}(t) \\
0 \leq P_{\text {load }}(t) \leq P_{\text {load }}(t) \\
P_{\text {loss }}(t)=P_{\text {load }}(t)-P_{\text {load }}(t) \\
P_{\text {waste }}(t)=P_{\mathrm{WTY}}(t)+P_{\mathrm{PVY}}(t)-P_{\mathrm{WT}}(t)-P_{\mathrm{PV}}(t)
\end{array}\right.
$$

In the formula, $P_{\mathrm{WT}}(t)$ and $P_{\mathrm{PV}}(t)$ are the actual grid power of wind power and photovoltaic power during time $t$, respectively; $P_{\text {load }}(t)$ is the actual load power supplied by the system during period $t ; P_{\mathrm{WTY}}(t)$ and $P_{\mathrm{PVY}}(t)$ are the predicted power of wind power and photovoltaic power during the $t$ period, respectively; $P_{\text {load }}(t)$ is the load power transmitted from the outer layer to the inner layer during the $t$ period; $P_{\mathrm{ESS}}(t)$ is the energy storage charging and discharging power during period $t ; P_{\text {loss }}(t)$ is the power loss during period $t ; P_{\text {waste }}(t)$ represents the excess power of wind and solar power during the $t$ period.
(2) Transmission power constraints of interconnection lines

$$
\begin{equation*}
P_{\text {line }}^{\min }<P_{\text {line }}(t)<P_{\text {line }}^{\max } \tag{35}
\end{equation*}
$$

In the formula, $P_{\text {line }}^{\max }$ and $P_{\text {line }}^{\min }$ are the upper and lower limits of the transmission power of the interconnection line, respectively.
(3) Energy storage operation constraints

During any period of time, the charging and discharging power of the energy storage system is limited to

$$
\begin{equation*}
0 \leq P_{\text {cha }}(t), P_{\text {dis }}(t)<P_{\text {max }} \tag{36}
\end{equation*}
$$

In the formula, $P_{\text {cha }}(t)$ and $P_{\text {dis }}(t)$ respectively represent the charging and discharging power during the energy storage period $t$, and $P_{\max }$ represents the maximum charging and discharging power.

$$
\left\{\begin{array}{l}
E_{\mathrm{b}}(t+\Delta t)=E_{\mathrm{b}}(t)+P_{\mathrm{cha}}(t) \Delta t \times \eta_{\mathrm{cha}}-P_{\mathrm{dis}}(t) \Delta t / \eta_{\text {dis }}  \tag{37}\\
P_{\text {cha }}(t) P_{\text {dis }}(t)=0
\end{array}\right.
$$

In the formula, $E_{\mathrm{b}}(t)$ is the energy storage capacity at time $t$. To avoid overcharging and discharging of energy storage, then

$$
\left\{\begin{array}{l}
\operatorname{SOC}(t)=\frac{E_{\mathrm{b}}(t)}{E_{\mathrm{ESS}}}  \tag{38}\\
\operatorname{SOC}_{\min }<\operatorname{SOC}(t)<\operatorname{SOC}_{\max }
\end{array}\right.
$$

In the equation, $\mathrm{SOC}_{\text {max }}$ and $\mathrm{SOC}_{\text {min }}$ are the maximum and minimum values of SOC .
To ensure the sustainability of the scheduling cycle of the energy storage system, the state of charge is consistent throughout a cycle, i.e.,

$$
\begin{equation*}
\operatorname{SOC}(0)=\operatorname{SOC}(24) \tag{39}
\end{equation*}
$$

(4) Limited by factors such as investment funds and site conditions, the power and capacity of energy storage are constrained

$$
\begin{align*}
& P_{\mathrm{ESS}}^{\min }<P_{\mathrm{ESS}}^{\mathrm{R}}<P_{\mathrm{ESS}}^{\max }  \tag{40}\\
& E_{\mathrm{ESS}}^{\min }<E_{\mathrm{ESS}}^{\mathrm{R}}<E_{\mathrm{ESS}}^{\max } \tag{41}
\end{align*}
$$

In the formula, $P_{\mathrm{ESS}}^{\max }, P_{\mathrm{ESS}}^{\min }, E_{\mathrm{ESS}}^{\max }$, and $E_{\mathrm{ESS}}^{\min }$ are the boundary values of the configured power and capacity of the energy storage system allowed by the installation conditions.

### 4.2.5. Optimal Scheduling Strategy for Wind and Solar Energy Storage Systems

In the operation of the wind and solar storage grid-connected system, a strategy of joint interaction between the energy storage system and the external power grid is adopted to balance the output of new energy such as wind and solar in the system and the electricity demand of users. The optimization control strategy proposed in this article is shown in Appendix A Figure A1. $P_{\text {net }}$ is the net load, that is, $P_{\text {net }}=P_{\text {load }}-P_{\mathrm{PV}}-P_{\mathrm{WT}}$, which detects the difference between $P_{\text {net }}$ and the energy storage system SOC, and determines the magnitude of $t$ period $P_{\text {net }}(t)$ and the rated power $P_{\mathrm{ESS}}^{\mathrm{R}}$ of the energy storage system, then adjusts accordingly to balance the main body of the fluctuation in wind and solar energy storage power. When $P_{\text {net }}(t)$ is greater than $P_{\mathrm{ESS}}^{\mathrm{R}}$, the external power grid is mainly used to supply the power demand of the load, and the portion exceeding the power limit of the tie line is supplied by the energy storage system for the load. If $P_{\text {net }}(t)$ is within the power supply capacity of the interconnection line, the external power grid should consider charging the energy storage system while supplying electricity; When $P_{\text {net }}(t)$ is less than zero or greater than zero and less than $P_{\mathrm{ESS}}^{\mathrm{R}}$, this situation mainly relies on the energy storage system to maintain the balance of $P_{\text {net }}(t)$. If $P_{\text {net }}(t)$ is less than zero, first consider charging the energy storage system, then consider selling the remaining electricity to the external power grid. If $P_{\text {net }}(t)$ is less than zero, the energy storage system is first considered to be charged, and the remaining electricity is considered to be sold to the external power grid. If $P_{\text {net }}(t)$ is greater than zero and less than $P_{\mathrm{ESS}}^{\mathrm{R}}$, priority will be given to discharging the energy storage system, and for the part with insufficient electricity, external grid electricity will be purchased. In the entire control strategy, the charging and discharging of energy storage should be dynamically adjusted based on the SOC state to avoid the problem of energy storage system SOC exceeding the limit. When $\operatorname{SOC}(t-1)$ is in the boundary state $\mathrm{SOC}_{\min }$, the energy storage system does not perform discharge operation, and when $\operatorname{SOC}(t-1)$ is in the boundary state $\mathrm{SOC}_{\text {max }}$, the energy storage system does not perform charging operation. If the energy storage system exceeds the boundary state $P_{\text {cha }}(t)$ or $P_{\text {dis }}(t)$ after charging and discharging with $\mathrm{SOC}_{\text {min }}$ or $\mathrm{SOC}_{\text {max }}$, the charging and discharging power needs to be corrected according to Equations (42) and (43).

$$
\begin{gather*}
P_{\text {cha }}^{\prime}(t)=\frac{S O C_{\max }-S O C(t-1)}{\eta_{\text {cha }}} E_{\mathrm{ESS}}^{\mathrm{R}}  \tag{42}\\
P_{\text {dis }}^{\prime}(t)=\left[S O C(t-1)-S O C_{\text {min }}\right] E_{\mathrm{ESS}}^{\mathrm{R}} \eta_{\text {dis }} \tag{43}
\end{gather*}
$$

## 5. Model Solving Algorithms and Processes

### 5.1. Solution Algorithm

The model solving algorithms in this article include the improved sparrow algorithm and the multi-objective particle swarm optimization algorithm, among which the ISSA algorithm can refer to reference $[30,31]$. The basic concepts of multi-objective particle swarm algorithm are as follows.

### 5.1.1. Multi-Objective Particle Swarm Optimization Algorithm

The multi-objective particle swarm optimization algorithm, like the sparrow algorithm, is also a biomimetic algorithm where individuals in the population participate in
cooperation and competition using a velocity displacement model to guide optimization searches. The evolutionary process is as follows:

$$
\left\{\begin{array}{l}
v_{i, j}^{k+1}=w \times v_{i, j}^{k}+c_{1} r_{1} \times\left(p_{i, j}^{k}-x_{i, j}^{k}\right)+c_{2} r_{2} \times\left(g_{i, j}^{k}-x_{i, j}^{k}\right), j=1,2, \cdots n  \tag{44}\\
x_{i, j}^{k+1}=x_{i, j}^{k}+v_{i, j}^{k+1} \\
w=w_{\max }-\frac{\left(w_{\max }-w_{\min }\right) \times k}{K_{\max }}
\end{array}\right.
$$

In the formula, $n$ is the number of individuals in the population; $w$ is the inertia weight used for manipulating algorithm development and exploration scales, $K_{\max }$ is the number of iterations, $w_{\text {max }}, w_{\text {min }}$ are artificially set empirical values, and $k$ is the current algebra; $c_{1}$, $c_{2}$ is the learning factor; $r_{1}$ and $r_{2}$ are random numbers within $[0,1] ; v_{i, j}^{k}$ and $x_{i, j}^{k}$ correspond to the individual's position and speed respectively; $p_{i, j}^{k}$ and $g_{i, j}^{k}$ are individual extreme value and global extreme value determined by fitness function respectively.

The above internal function Equation (33) can be summarized as the following multiobjective model:

$$
\begin{align*}
& \left\{\begin{array}{l}
\max f(E, P) \\
\min R(E, P)
\end{array}\right. \\
& \text { s.t. }\left\{\begin{array}{r}
g(E, P)=0 \\
h(E, P) \leq 0
\end{array}\right. \tag{45}
\end{align*}
$$

In the formula, $F(E, P)$ and $R(E, P)$ are the objective functions of the on-site consumption rate of new energy and the purchase cost of energy storage, respectively; $g(E, P)$ and $h(E, P)$ represent equality and inequality constraints, respectively; $E$ and $P$ represent the configured capacity and configured power of energy storage.

For $F(E, P)$ and $R(E, P)$, the two objective functions interact and constrain each other, making it difficult for them to achieve optimal results simultaneously. Instead, they are replaced by the Pareto optimal solution [32,33]. These solutions are mapped by functions $F(E, P)$ and $R(E, P)$ to form the optimal frontier of Pareto. The solution to Equation (45) is to find a sufficient number of optimal solutions for Pareto and try to distribute the optimal frontier diagram evenly, in order to provide reference for power practitioners.

### 5.1.2. Choosing the Compromise Optimal Solution

After obtaining the Pareto optimal solution set, the optimal compromise solution is determined using fuzzy mathematics [34]. Using fuzzy membership functions to characterize the satisfaction of the solution set elements corresponding to various dimensional functions:

$$
\mu_{i}^{m}= \begin{cases}1 & f_{i}^{m} \leq f^{m, \text { min }}  \tag{46}\\ \frac{f^{m, m a x}-f_{i}^{m}}{f^{m, m a x}-f_{m, m i n}}, & f^{m, \min }<f_{i}^{m}<f^{m, \max } \\ 0 & f_{i}^{m} \geq f^{m, \text { max }}\end{cases}
$$

In the equation, $f_{i}^{m}$ is the objective function, $m \in\left\{1,2, \cdots, N_{o b j}\right\} ; f^{m, \max }$ and $f^{m, \min }$ are the maximum and minimum values corresponding to $f_{i}^{m}$, respectively.

The satisfaction calculation of each Pareto optimal solution is shown in Equation (47), and the corresponding solution when it reaches its maximum is considered the optimal compromise solution.

$$
\begin{equation*}
\mu_{i}=\frac{\sum_{m=1}^{N_{\text {obj }}} \mu_{i}^{m}}{\sum_{i=1}^{N_{c}} \sum_{m=1}^{N_{\text {obj }}} \mu_{i}^{m}} \tag{47}
\end{equation*}
$$

In the equation, $N_{\mathrm{c}}$ is the number of Pareto optimal solutions.

### 5.2. Energy Storage Charging and Discharging Verification

Inner-layer optimization belongs to the multi-time period coupling optimization problem, which means that the operating state of energy storage is not only constrained by its capacity and maximum charging and discharging power but also related to multiple other time periods. The constraint of equal starting and ending energy during the daily operation cycle of energy storage, as shown in Equation (38), is not easy to implement. To this end, a backstepping method is proposed to verify and adjust the capacity status of each period of energy storage, as follows:
(1) First, based on the decision variables of energy storage capacity and maximum charging and discharging power at the lower level, and on the principle that the initial state of charge $\operatorname{SOC}(0)$ of energy storage is equal to the end time $\operatorname{SOC}(24)$, the maximum state of charge $\mathrm{SOC}_{t}^{\max }$ and minimum state of charge $\mathrm{SOC}_{t}^{\min }$ that should be constrained for each time period $\operatorname{SOC}(23), \mathrm{SOC}(22) \ldots \mathrm{SOC}(t)$ are derived.

$$
\begin{gather*}
\mathrm{SOC}_{t}^{\max }=\min \left[0.5+(24-t) \cdot P_{\mathrm{d}}^{\mathrm{R}} /\left(\eta_{\mathrm{d}} \cdot E_{\mathrm{ess}}^{\mathrm{R}}\right), 0.9\right]  \tag{48}\\
\mathrm{SOC}_{t}^{\min }=\max \left[0.5-(24-t) \cdot \eta_{\mathrm{c}} \cdot P_{\mathrm{c}}^{\mathrm{R}} / E_{\mathrm{ess}}^{\mathrm{R}}, 0.2\right] \tag{49}
\end{gather*}
$$

(2) Detect and correct $P_{\mathrm{c}}^{t}$ and $P_{\mathrm{d}}^{t}$

$$
\left\{\begin{array}{l}
P_{\mathrm{d}}^{t}=\min \left\{\mathrm{x},\left[\mathrm{SOC}(t-1)-\mathrm{SOC}_{t}^{\min }\right] \cdot\left(\eta_{\mathrm{d}} \cdot E_{\mathrm{ess}}^{\mathrm{R}}\right)\right\}  \tag{50}\\
\text { s.t. } \operatorname{SOC}(t)<\mathrm{SOC}_{t}^{\min } \\
P_{\mathrm{c}}^{t}=\max \left\{\mathrm{x},\left[\mathrm{SOC}(t-1)-\mathrm{SOC}_{t}^{\max }\right] \cdot E_{\mathrm{ess}}^{\mathrm{R}} / \eta_{\mathrm{c}}\right\} \\
\text { s.t. } \operatorname{SOC}(t)>\mathrm{SOC}_{t}^{\max }
\end{array}\right.
$$

In the formula, x represents other constraints that need to be comprehensively considered during the energy storage charging and discharging process.
(3) Detect and correct $P_{\mathrm{c}}^{t+1}$ and $P_{\mathrm{d}}^{t+1}$ based on, $\mathrm{SOC}_{t+1}^{\max }, \mathrm{SOC}_{t+1}^{\min }$, until $\operatorname{SOC}(24)$ equal SOC(0).

### 5.3. Solution Flowchart

The improved sparrow algorithm is used to solve the outer layer of the model to optimize electricity price. Users actively respond to the electricity price policy and transfer the load after participating in demand response to the inner layer. The inner layer uses the common multi-objective particle swarm optimization algorithm to solve the problem. The objective function is to coordinate and optimize the capacity and maximum charging and discharging power of the energy storage system, taking the on-site consumption rate of new energy and the optimization configuration cost of energy storage as the objective functions. The optimization results are fed back to the outer layer to participate in the optimization of the outer layer decision variables. The solving process of the double-layer multi-objective model is shown in Appendix A Figure A2.

## 6. Example Analysis

### 6.1. Example Parameter Description

To verify the rationality of the model proposed in this article, a simplified wind and solar energy storage grid-connected system is used as an example to study the optimization configuration of energy storage capacity. The relevant parameters are shown in Table 1.

Table 1. Simulation parametersis.

| Parameter | Numerical Value | Parameter | Numerical Value |
| :---: | :---: | :---: | :---: |
| Penalty cost coefficient | 0.1 | Cross elasticity coefficient | 0.03 |
| Ciscounted rate | 5\% | $c_{p}(\mathrm{RMB} / \mathrm{kW})$ | 1085 |
| $\mathrm{K}_{\mathrm{p}}$ | 2 | $P_{\text {line }}^{\max }(\mathrm{kW})$ | 600 |
| Maximum number of charges and disCharges for energy storage | 5000 | $P_{\text {line }}^{\text {min }}(\mathrm{kW})$ | -600 |
| Carbon trading price ( $\mathrm{RMB} / 1000 \mathrm{~kg}$ ) | 15 | $\mathrm{c}_{\mathrm{E}}(\mathrm{RMB} / \mathrm{kW})$ | 3224 |
| $\eta_{\mathrm{c}}, \eta_{\mathrm{d}}$ | 0.95 | Operation and maintenance Costs (RMB/kW h) | 50 |
| $\mathrm{SOC}_{\max }$ | 0.9 | $E_{\text {ESS }}{ }^{\text {ax }}$ | 2500 |
| $\mathrm{SOC}_{\text {min }}$ | 0.2 | $P_{\text {ESS }}^{\text {max }}$ | 500 |
| SOC initial value | 0.5 | Carbon reduction per unit of New energy ( $\mathrm{kg} / \mathrm{kW} \cdot \mathrm{h}$ ) | 0.16 |
| Electricity selling price | 0.58 | $\mathrm{C}_{0}(\mathrm{RMB} / \mathrm{kW} \cdot \mathrm{h})$ | 0.12 |
| Electricity purchase price | 0.69 | $p_{\text {max }}(\mathrm{RMB} / \mathrm{kW} \cdot \mathrm{h})$ | 1.2 |
| Coefficient of self elasticity | -0.2 | $Y_{\text {a }} /$ Year | 20 |

Wind power, photovoltaic power, and load are all selected according to the typical daily power curve according to the season. Due to the close relationship between wind, light, and load power curves in spring and autumn, the situation in autumn is not considered, and spring is referred to as the transitional season, as shown in Appendix A Figure A3. The initial electricity price is shown in Table 2.

Table 2. Initial time-of-use tariff table.

| Parameter | Period of Time | Electricity Price (RMB/kW $\mathbf{h}$ ) |
| :---: | :---: | :---: |
| Peak period | $07: 00-11: 00,17: 00-21: 00$ | 0.96 |
| Peacetime period | $12: 00-16: 00,22: 00-23: 00$ | 0.58 |
| Valley period | $00: 00-6: 00$ | 0.27 |

Based on the example data combined with the mathematical model described earlier, the solution algorithm can be used to optimize the model. The subsequent analysis of the results will mainly optimize the expressions based on the three objective functions mentioned in the previous text, namely Equations (2), (11) and (33). The division of time periods for dynamic time-of-use electricity prices mainly relies on functional Equation (2). The calculation of the electricity price value, energy storage power and capacity, on-site consumption rate of wind and solar energy, and economic cost of wind and solar energy storage systems for dynamic time-of-use electricity prices is mainly based on the final optimization solution results of outer objective Equation (11) and inner optimization objective Equation (33).

### 6.2. Optimization Configuration Results under Different Typical Weather Conditions

Due to the different distribution characteristics of net load in different seasons and time periods, it is necessary to divide the peak-to-valley electricity prices into three scenarios, as shown in Figure 3. From the figure, it can be seen that the electricity prices under three typical daily scenarios are different in size and distribution during peak-to-valley periods. Taking peak electricity prices as an example, the highest electricity price is in summer, with a peak value of $0.91 \mathrm{RMB} / \mathrm{kW} \cdot \mathrm{h}$, and the peak electricity prices in transition season and winter are $0.75 \mathrm{RMB} / \mathrm{kW} \cdot \mathrm{h}$ and $0.73 \mathrm{RMB} / \mathrm{kW} \cdot \mathrm{h}$, respectively.


Figure 3. Optimization results of time-of-use electricity prices in different seasons.
Figure 4 and Table 3 show the optimization solution results under different seasonal scenarios. From this, it can be concluded that the energy storage capacity configuration scale in summer is the largest, reaching $1194 \mathrm{~kW} \cdot \mathrm{~h}$, and the energy storage configuration power in spring is the largest, reaching 210 kW . When configuring the energy storage capacity of the system, the energy storage configuration results of the typical day with the highest demand are considered the energy storage planning standard of the system. Therefore, based on the energy storage configuration results of three typical scenarios, the final energy storage scale configured in this combined power generation system is $1194 \mathrm{~kW} \cdot \mathrm{~h}$ capacity and 210 kW power.


Figure 4. Configuration of energy storage in different seasons.

Table 3. Optimization results of typical days in three seasons.

| Typical Daily Scenario | On Site Consumption Rate of <br> New Energy | Energy Storage Capacity/(kW $\cdot \mathbf{h})$ | Energy Storage Power/(kW) |
| :---: | :---: | :---: | :---: |
| Peak period | $07: 00-11: 00,17: 00-21: 00$ | 285 | 210 |
| Peacetime period | $12: 00-16: 00,22: 00-23: 00$ | 1194 | 136 |
| Valley period | $00: 00-6: 00$ | 826 | 192 |

To study the coordination relationship between energy storage configuration and electricity price in wind and solar energy storage systems, typical summer days are selected as the energy storage configuration carriers, and the following scenarios are set up for further comparative analysis:

Scenario 1: Revenue from wind and solar systems (excluding energy storage) and on-site consumption of new energy without implementing dynamic time-of-use electricity prices.

Scenario 2: Implementation of dynamic time-of-use electricity prices for wind and solar systems (excluding energy storage) and on-site consumption of new energy.

Scenario 3: Revenue and internal multi-objective optimization of wind and solar energy storage systems without implementing dynamic time-of-use pricing.

Scenario 4: Implementing the revenue and internal multi-objective optimization of wind and solar energy storage systems under dynamic time-of-use electricity prices.

### 6.3. Analysis of Simulation Results

### 6.3.1. Analysis of On-Site Consumption of New Energy

Table 4 shows the results of energy storage configuration scale and on-site consumption rate under four different scenarios. From Table 4, it can be seen that compared to Scenario 1, the on-site consumption rate of new energy in Scenario 2 has increased by $4.12 \%$, indicating that implementing the time-of-use electricity price can improve the distribution characteristics of the initial predicted load and enhance the absorption capacity of the wind and solar storage system for new energy. Compared with Scenario 1, the on-site consumption rate of new energy in Scenario 3 has increased by $2.34 \%$, indicating that the system is equipped with energy storage facilities to store excess local wind and solar resources, thereby reducing the electricity output of new energy from the wind and solar storage system to the external power grid. Scenario 4 has the highest on-site consumption rate of new energy, as the optimized time-of-use electricity price through the outer layer provides the inner layer with a load that has undergone demand-side response. The peak-valley difference and volatility of the load curve are reduced, and the flexible adjustment ability of the system's new energy is further improved through the charging and discharging actions of energy storage in the inner layer. Figure 5 depicts the relationship between the energy storage configuration and the on-site consumption rate of new energy in Scenarios 3 and 4. It can be seen from the figure that when the wind and solar storage system achieves the same on-site consumption rate of new energy, Scenario 3 needs to be configured with a larger energy storage capacity. This further demonstrates that the optimized time-of-use electricity price is conducive to further improving the on-site consumption rate of new energy.

Table 4. Optimization results of typical days in three Seasons.

| Scene | On Site Consumption Rate of <br> New Energy/\% | Energy Storage Capacity/(kW $\mathbf{h}$ ) | Energy Storage Power/(kW) |
| :---: | :---: | :---: | :---: |
| 1 | $91.55 \%$ | 0 | 0 |
| 2 | $95.67 \%$ | 0 | 0 |
| 3 | $93.89 \%$ | 1194 | 210 |
| 4 | $97.93 \%$ | 1194 | 210 |



Figure 5. Configuration of energy storage before and after demand response.
Table 5 and Figure 6 show the characteristic changes in typical daily load in summer before and after participating in demand response. From Table 5 and Figure 6, it can be concluded that users have a high demand for electricity from 11:00-14:00 and from 18:00-21:00, with insufficient wind and photovoltaic output and net load in the peak range. Therefore, these periods are divided into peak periods. Users consume less electricity during the period from 1:00 to 8:00, wind power has a higher output during this period, and the net load takes a smaller value during the day. This period is divided into valley periods, and the rest of the period is divided into regular periods. According to the net load, the peak-tovalley electricity price periods are further optimized, and the optimized electricity prices for valley, flat, and peak periods are $0.28 \mathrm{RMB} / \mathrm{kW} \cdot \mathrm{h}, 0.42 \mathrm{RMB} / \mathrm{kW} \cdot \mathrm{h}$, and $0.91 \mathrm{RMB} / \mathrm{kW} \cdot \mathrm{h}$, respectively. The optimized load curve reduces the peak-valley difference, the peak load decrease by 17.3 kW , and the valley load increases by 88.4 kW . From the calculation results and Figure 6, it can be seen that the demand response strategy can effectively stabilize the load peak-valley difference and the net load peak-valley difference. The total load before users' participation in demand response remains unchanged, and Table 4 shows that the total price before users' participation is $14,301 \mathrm{RMB}$, and the total price after response is $13,238 \mathrm{RMB}$, which meets the constraint setting requirements of demand response in the model, and the reduced power cost helps to improve the enthusiasm and feasibility of users' participation in demand response.


Figure 6. Summer electricity price optimization and source load changes.

Table 5. Demand response effect.

| Before and after <br> Optimization | Maximum Load/kW | Minimum Load/kW | Peak-Valley Difference <br> of Load/kW | Net Load Peak Valley <br> Difference/kW |
| :---: | :---: | :---: | :---: | :---: |
| Before optimization | 1356.3 | 458.6 | 897.7 | 646.9 |
| After optimization | 1339 | 547 | 792 | 411.4 |
| Variation | -17.3 | 88.4 | -105.7 | -235.5 |

Figure 7 shows optimization scheduling results under four different scenarios. Figure 8 shows the energy storage charging and discharging power and charging state of each period in Scenario 3 and Scenario 4. The initial charging state of the energy storage is 0.5 , and it recovers to 0.5 at the end of one cycle, meeting the sustainability of the energy storage system scheduling cycle. According to the scheduling strategy mentioned earlier, the non-on-site consumption period of new energy is distributed during the period when the wind and solar output exceeds the load demand. From Figure 7a, it can be seen that the non-on-site consumption period of new energy is from 1:00 to 8:00, as well as at 22:00 and 24:00. From Figure 7 b , it can be seen that the user load after demand response increases at these moments, thus reducing the surplus of the scenery. As shown in Figure 7c,d, when energy storage devices are installed in the new energy system, energy storage will absorb a portion of excess wind and solar new energy during the remaining hours of 1:00-3:00 and 22:00, thereby improving the on-site consumption rate of new energy.


Figure 7. Optimization scheduling results for four scenarios.


Figure 8. Energy storage charge and discharge power and state of charge for Scenarios 3 and 4.

### 6.3.2. Economic Analysis

Table 6 shows the system benefits under four scenarios. Compared with Scenario 2, Scenario 1 has an increase of 1560 RMB in system revenue. As users participate in the demand response policy, the revenue from selling electricity to users in the system has decreased by 1063 RMB, but in Scenario 2, the penalty for contact line fluctuation has decreased by 2519.6 RMB, and in Scenario 2, the system revenue has increased. Although there is a small difference between Scenario 1 and Scenario 2 and the settlement amount of purchasing and selling electricity from the external network, the scale of single purchasing and selling electricity in Scenario 1 is larger than that in Scenario 2. This also verifies the conclusion that demand response policy can improve the local consumption rate of new energy. Compared with Scenario 1, Scenario 3 showed a decrease of 3307.6 RMB in system revenue. This difference is mainly due to the daily loss cost of energy storage equipment in the system and the penalty for contact line fluctuations. As a result, the reduction in electricity purchase revenue from the grid also indicates that Scenario 3 with energy storage facilities has improved the on-site consumption rate of new energy compared to Scenario 1 without energy storage facilities. Compared with Scenarios 1 and 3, Scenario 4 has the highest system revenue, mainly due to the significant reduction in penalties for tie line fluctuations. This indicates that the method proposed in this article can better suppress power fluctuations in the interconnection line. This method has the lowest electricity sales revenue for the power grid, which minimizes the sales of new energy to external power grids. This reduces the impact of integration fluctuations between new energy and external power grids in wind and solar energy storage systems, and improves the safe and stable operation of the power grid. Compared with Scenario 2, the decrease in system revenue in this scenario mainly comes from the daily loss cost of energy storage, but the on-site consumption of new energy in Scenario 4 is better than that in Scenario 2.

Table 6. Economic analysis under different scenarios (Unit:RMB).

| Scene | System <br> Benefits | Consumer <br> Electricity <br> Consumption | Revenue from <br> Selling Electricity to <br> the Power Grid | Cost of Purchasing <br> Electricity from the <br> Power Grid | Penalty for <br> Contact Line <br> Fluctuations | Daily Loss Cost <br> of Energy <br> Storage |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 10,354 | 14,301 | 1124.9 | 1514.9 | 3612.1 | 0 |
| 2 | 11,914 | 13,238 | 576.17 | 863.19 | 1092.5 | 0 |
| 3 | 7046.4 | 14,301 | 985.51 | 1426.3 | 5197.7 | 1670.9 |
| 4 | 10,527 | 13,238 | 276.12 | 560.53 | 856.43 | 1625.7 |

### 6.3.3. Optimization Results of Different Penalty Factors

To study the impact of power fluctuation penalties on interconnection lines, three different penalty values, $0.1,0.01$, and 0.001 , are set. The solution results under different scenarios are shown in Table 7. From the table, it can be seen that in scenarios 1 to 4 , for
each scenario with the same on-site consumption rate and energy storage configuration scale of new energy, the system revenue is maximum at a penalty factor of 0.001 , and minimum at a penalty factor of 0.1.

Table 7. EffectSystem returns and contact line fluctuation penalties under different penalty factors.

| Different Scenarios | Returns and Volatility <br> Penalties | Different Penalty Factors |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | $\mathbf{0 . 1}$ | $\mathbf{0 . 0 1}$ | $\mathbf{0 . 0 0 1}$ |
| Scenario 1 | Volatility Penalties | 10,354 | 13,605 | 13,930 |
|  | System benefits | 3612.1 | 361.21 | 12,914 |
| Scenario 2 | Volatility Penalties | 1092.5 | 109.25 | 12,995 |
|  | System benefits | 7046.4 | 11,725 | 10.93 |
| Scenario 3 | Volatility Penalties | 5197.7 | 519.77 | 12,192 |
|  | System benefits | 10,527 | 11,297 | 51.98 |
|  | Solatility Penalties | 856.43 | 85.64 | 11,374 |

The inner model is solved under the set control strategy. When the load transmitted from the outer layer to the inner layer is the same and the energy storage configuration scale of the inner layer is the same, the variables in the inner layer of the model obtain the same results, The main change at this point comes from the power fluctuation penalty of the interconnection line. When the penalty coefficient is large, the system revenue will correspondingly decrease. Under the penalty factors of 0.001 and 0.01 , the revenue in Scenario 1 is the largest, and the revenue in Scenario 4 is the smallest. This indicates that some users participate in demand response, reducing the revenue of the system, and the system configured with energy storage also increases the energy storage loss, which is greater than the loss caused by the system reducing the power fluctuation of the tie line. When the penalty factor is 0.1 , the fluctuation penalty cost of Scenario 1 and Scenario 2 is relatively large, which greatly reduces system revenue. At this time, Scenario 4 has the largest system revenue, because this scenario has the smallest power fluctuation of tie lines under the influence of demand response and energy storage configuration.

## 7. Conclusions

This article studies the allocation of energy storage capacity considering electricity prices and on-site consumption of new energy in wind and solar energy storage systems. A nested two-layer optimization model is constructed, and the following conclusions are drawn:
(1) The distribution of source load power curves varies for typical days in different seasons. Using dynamic time-of-use electricity prices can more flexibly obtain the capacity configuration scale of energy storage. The article adopts the capacity and maximum power values of energy storage configuration in each season, which can meet the demand for energy storage capacity in each season. The optimization of park electricity prices can slightly increase the on-site consumption rate of new energy, while energy storage can significantly increase the consumption rate of new energy, but the cost of energy storage configuration is relatively high. This article proposes a coordinated optimization method for energy storage and electricity prices in the park, which can achieve maximum on-site consumption of new energy while improving the economy of energy storage to a certain extent.
(2) This article adopts a joint optimization model of load demand-side response and energy storage configuration, which can effectively improve the revenue of wind and solar storage systems and the on-site consumption rate of new energy, and greatly reduce the fluctuation penalty of connecting lines.
(3) The energy storage daily loss model proposed in this article can accurately reflect the operational loss of energy storage, and the proposed backstepping method can effectively verify and adjust the capacity status of each period of energy storage, ensuring that the optimization of energy storage has equal states of charge from beginning to end.
(4) This article does not consider user satisfaction factors and does not analyze the impact of typical day prediction errors on energy storage configuration results when participating in demand-side response. The next step can focus on this point.

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## Appendix A



Figure A1. Optimization operation strategy for wind and solar storage system.


Figure A2. Double layered multi-objective optimization calculation process.


Figure A3. Predicted values of solar and load power before the day.

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