Carousel Optimal Arrangements of Cartridges in (Type Mass Storage Systems

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Optimal arrangements of cartridges and file partitioning schemes are examined in carousel type mass storage systems using Markov decision theory. It is shown that the Organ-Pipe Arrangement is optimal under different storage configurations for both the anticipatory as well as the non-anticipatory versions of the problem. When requests arrive as per an arbitrary renewal process this arrangement is also shown to minimize the mean queweing delay and the time spent in the system by the requests.

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1. INTRODUCTION

A large number of applications such as multimedia databases, document retrieval and scientific databases, require high-capacity mass storage systems that can hold multigigabytes or even terabytes of data. These systems contain a hierarchy of storage devices typically consisting of large robotic tape libraries, optical disks and magnetic disks. In such systems, files are automatically migrated across the storage hierarchy such that the more frequently used files reside on the faster and more expensive (in terms of dollars per byte) storage media. In this paper we analyse data placement strategies on a carousel type robotic tape library. Such devices are quite commonly found in mass storage systems, for example Magnus Jukebox Library and Lago Systems LS/300L are carousel type devices that use 8 mm tape cartridges with a total capacity of 270 GB (Ranade, 1992).

The carousel type mass storage system is a configuration found in systems catering for low to medium tertiary storage requirements. The system usually has a number of storage locations for cartridges arranged on the inner periphery of a carousel (see Figure 1). The system responds to a request for loading a cartridge by the movement of the carousel to align the required cartridge in front of a read/write head, and a robot does the actual loading or unloading. The problem addressed in this paper is the optimal allocation of cartridges to the storage locations and files to the cartridges.

A similar problem has been solved recently in the context of determining warehouse storage by Fujimoto (1991). Using a Markovian model, Fujimoto proves the optimality of the Organ-Pipe Arrangement when only one cartridge is stored per location. An Organ-Pipe Arrangement (OPA) is one in which cartridges, or more generally items, are first sorted in the descending order of

the probability that they will be requested. The first item is allotted to the central location (for a circular storage device such as a carousel, the choice of this location is location. The picture made by the graph of the probabilities with respect to locations resembles an non-anticipatory based on a terminology introduced in King (1990). In the non-anticipatory case the storage device is not permitted to be repositioned between requests even if time is available for doing so; whereas in the anticipatory case the controller can reposition the device between requests. In Fujimoto's terminology bi-directional system. Singe refers to the number of Fujimoto gives an extensive literature survey in the area of warehousing and also refers to papers on optimal Groosman and Silverman, 1973; Yue and Wong, 1973 and Karp et al., 1975). None of these directly address the specific Fujimoto concludes that the closest paper that solves the carousel problem is that of Lim et al. (1985), where the analysis. Fujimoto adds a missing step in Bergmans' proof for the case when only one cartridge (item) can be stored per location, and conjectures the optimality of the OPA arrangement for the case when more than one cartridge can be stored per storage location but does not arbitrary). Then the remaining items are placed alternatively to the left and right of the central organ-pipe. The model solved by Fujimoto is called the mass storage carousel is a single dimensional direction. problem of allocation of storage space in carousels. S caronsel bi-directional as it can be rotated in either of OPA is proved based on 1972; (Bergmans, and the prove the optimality of this policy. location permutations cartridges per optimality spatial

The case of a mass storage system is a bit different, because depending on the load, it is possible to reposition the carousel before another request arrives. This is the

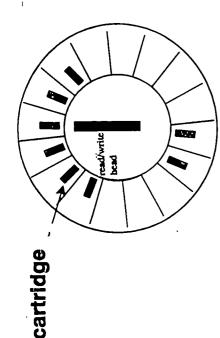


FIGURE 1. A carousel with one read/write head.

anticipatory case as defined above. Anticipatory policies for disk arm control are offered as a good strategy by King (1990). A well known example of such a policy is the greedy policy of 'nearest head' shown to be optimal for a disk with two read heads by Hofri (1983). In that work the head which does not serve the current request is allowed to 'jockey' to an optimal location in anticipation of the next request.

In this paper, we use a Markovian model for the carousel problem, and show that for both the anticipatory and non-anticipatory versions of the problem, the optimal arrangement is the Organ-Pipe Arrangement when there is a single read/write head. The results are then extended to the case when two heads are provided. Finally we extend the results to the case where requests arrive as per an arbitrary renewal process and show that for the non-anticipatory case the OPA arrangement minimizes both the mean queueing delay as well as the average time spent in the system by the requests.

2. MODEL

and bin packing type of limitations. From experience will need to incorporate caching). When extending the results to file allocation at most m files. This is a simplification because file sizes contend with random and non-stationary sizes of files however, it is seen that storing larger files in the tertiary So the file migration policies may tend to even out the size below can be extended to the case of continuous variables representing the items stored and thus are not The carousel is modeled as having n storage locations. One cartridge can be placed in each of the locations. We will assume that there are at most n cartridges to be we will model the cartridge as capable of accommodating need not be the same and file migration policies could dictate the size distribution of files found in the mass storage system. However the simplification enables the solution of a problem which otherwise will have to distribution. In any case, the operating policies described system leads to a better retrieval performance. necessarily of limited usefulness in practice. loaded (else the problem

In order to model the demand process, it is assumed at the probability a particular cartridge will be

of cartridges is less than n then the remaining probabilities are set to zero. Unless specified, in all cases the number of read/write heads is one. A similar is linear and the shortest distance to travel will be realized. The objective throughout is to minimize to mean delay to service a request and except in propositiक्र one another. The last assumption is reasonable for mass requests is physically possible but not found in currest 7, it is always assumed that requests do not interfere wi聶 storage systems and the ability to reposition in between Thus the request pattern forms a Markov chain with state probabilities, p_i , the probability that the next cartridge requested will be i and $\sum_{i=1}^{n} p_i = 1$. If the number model will be used for the file allocation problem. The Markovian assumption is reasonable considering that the mass storage system does not actively participate in user processing and is more like a library or repository in its functions. In the non-anticipatory case, called case I, the carousel cannot be moved to a specific location in anticipation of a request—whereas in the anticipatory case, termed case II, the carousel can be repositione between requests. It will be assumed that the travel ting requests past independent of the requested next is systems.

Number the locations on the carousel as 1 through a Assume that cartridge $\pi(i)$ is stored in location i. In case I, as we have a finite state space for the Markov chain, of follows that there exists a unique stationary distribution of the position at which arriving requests find the carousel (see Wolff, 1990 for example). Direct verification shows that the (stationary) probability that a request will find the read head at location i is equal to the probability, $p_{\pi(i)}$, that the cartridge stored at location is will be requested.

In dealing, with the file allocation model in case $\frac{n}{n}$, there are two levels of decision. First the files must be allocated to cartridges. Then the cartridges must be arranged in storage locations. Once the file allocation has been carried out, the request probability for a particular cartridge is fixed by the sum of the probabilities of requests for files allotted to the cartridge. It follows that the above stationary distribution holds goodonce the request probability for cartridges has been computed.

In case I, using the above notation, cartridge $\pi(i)^{NS}$ stored in location *i*, the expected travel distance, $ED(\pi)$, per request is given by (see Wolff, 1990 for example):

$$ED(\pi) = \sum_{i} p_{\pi(i)} \sum_{j} p_{\pi(j)} d(i,j)$$

where d(i,j) is the shortest rotational distance between locations i and j. By substituting any function f of the distances d(i,j) in the above formula we also obtain the expected value of that function, i.e.

$$Ef[D_{(\pi)}] = \sum_{i} p_{\pi(i)} \sum_{i} p_{\pi(j)} f[d(i,j)]$$

This fact will be used in proposition 1.

OPTIMAL ARRANGEMENTS OF CARTRIDGES

In case II, we do not need to use the Markov chain at all. This is because in the anticipatory case it is assumed that the read head can be positioned very quickly to a given position before a request arrives. Given that requests are independent of one another, the optimal repositioning strategy will be stationary and deterministic. Therefore the read head will always be positioned at the same place before a request arrives; a fact that allows us to search within this class of policies in determining the optimal allocation scheme. Thus, if the read head is always repositioned between requests at location i, then the expected distance traveled per request (ignoring the repositioning distance) will be given by:

$$ED(\pi) = \sum_{i} p_{\pi(j)} d(i,j)$$

Note that the expected repositioning distance is also equal to the above value.

3. THE OPTIMALITY OF THE ORGAN-PIPE ARRANGEMENT

An Organ-Pipe Arrangement is one in which the cartridges are placed in an alternating arrangement. The cartridges are ranked in descending order as per their request probability. Let cartridge #i be the one with the ith largest request probability and let the storage locations be numbered in clockwise fashion. Then cartridge #1 is placed in location l cartridge #2 in location l, l in location l, l in location l, l in location l, l in location l arrangement proves to be optimal under a variety of modeling assumptions as described in this section.

 $X \geqslant_H Y$, if Prob $(X > t) \leqslant \text{Prob}(X > t)$ for an t. In Wolff (1990) it is shown that $X \geqslant_H Y$ is equivalent to the left side of this line be larger than the sum on the right speaking we expect that the request probability for cartridge i should be larger than for cartridge j in the optimal arrangement. This property is called the pairwise Majorization Property (PMP) by Fujimoto. In case I, in ines. And not very coincidentally the OPA possesses this A sketch of the proof (partly provided by Fujimoto) follows but with a strengthening of the result. we start out nitially with the stationary distribution of the Markov chain, then OPA minimizes the distance traveled at each equal to Y in the stochastic ordering sense, denoted by The basic condition for optimality of an arrangement Let the sum of request probabilities for cartridges on the [ignoring the location(s) bisected]. Let i and j be the cartridges stored in mirror image location on the left and right sides of the line respectively. Then intuitively transition in the sense of stochastic order. By definition, if X and Y are random variables, then X is larger or is obtained by imagining that a line of symmetry (of any fact a necessary and sufficient condition for an arrangenent to be optimal is that PMP holds over all symmetry orientation) is drawn across the carousel, see Figure 2. for any non-decreasing function, The strengthening is in the sense that if $\mathbb{E}[f(X)] \geqslant E[f(Y)].$ condition that property.

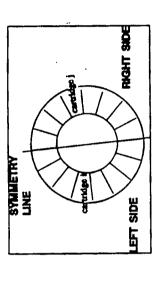


FIGURE 2. The pairwise majorization property.

Proposition 1. (Bergmans, 1972 and Fujimoto, 1991. The OPA arrangement is optimal in case I and also in the stochastic sense described above.

Proof. Let there be a line of symmetry over which the pairwise majorization property is violated. We will call the side that has the higher sum of probabilities as the left side. Assume that the symmetrical dividing line is vertical. Denote a violating assignment to be one where a cartridge on the left side has a lower request probability than the one in the mirror image location on the right. For example, the fourth cartridge on the left of the symmetry line has a smaller request probability compared to the fourth one on the right side of the line.

due to the interchange is exactly the distance by which line. Consider the impact of cost in (iii) with respect to lu (iii) can be proved by the following argument: fix an un-interchanged cartridge location. The distance by another cartridge has moved closer to this location. The argument can be formalized by denoting the locations on the left of the symmetry line from which the cartridges must be interchanged to be $\{11, 12, 13, ..., 1k\}$ and the mirror image locations on the right (where they must be placed) to be $\{r1, r2, r3, ..., rk\}$. Let lu and ru stand for the mirror image locations of two uninterchanged cartridges, on the left and right sides of the symmetry and ru. The change in cost with respect to these two We will show that this arrangement can be improved assignments This helps because (i) the cost with themselves is unchanged, (ii) the cost with respect to the while (iii) the interaction between the interchanged and un-interchanged cartridges leads to lower cost. The case which a cartridge has moved away from this location respect to the un-interchanged cartridges considered by interchanged cartridges by themselves is unaffected violating interchanging all pairs of ocations is given by: simultaneously.

$$P_{\pi(h)} \left[\sum_{j=1}^{k} P_{\pi(l_j)} d(lu, l_j) + \sum_{j=1}^{k} P_{\pi(r_j)} d(lu, r_j) \right] -$$

$$P_{\pi(h)} \left[\sum_{j=1}^{k} P_{\pi(r_j)} d(lu, l_j) + \sum_{j=1}^{k} P_{\pi(l_j)} d(lu, r_j) \right] +$$

$$P_{\pi(n)} \left[\sum_{j=1}^{k} P_{\pi(l_j)} d(lu, l_j) + \sum_{j=1}^{k} P_{\pi(r_j)} d(lu, r_j) \right] -$$

$$\begin{aligned} & p_{\pi(n)} \left[\sum_{j=1}^{k} p_{\pi(r_j)} d(lu, l_j) + \sum_{j=1}^{k} p_{\pi(l_j)} d(lu, r_j) \right] \\ &= \left(p_{\pi(l\omega)} - p_{\pi(r\omega)} \right) \sum_{j=1}^{k} \left(p_{\pi(l_j)} - p_{\pi(r_j)} \right) (d(lu, l_j)) \\ &- d(lu, r_j)) \geqslant 0 \end{aligned}$$

assumption, $p_{\pi(lu)} \ge p_{\pi(ru)}$ as the cartridges in these two positions satisfied PMP, and $d(lu, l_j) \le d(lu, r_j)$. The last step follows from the fact that $p_{\pi(l_j)} < p_{\pi(r_j)}$ as PMP is violated at the symmetric locations l_j and r_j by

the arguments carry over to the carousel rotational time rather than rotational distance, because the time is an increasing function of the distance. The importance of sense of stochastic order. In our case, this implies that all in the proof given above. This shows that the interchange reduces the distance traveled at each transition in the demonstrating this ordering must be noted. This artifice and will be used in a queueing context in proposition 7. the above any increasing function of the distance. To verify this does not affect costs averaged over a long period of time, argument holds when the distances are substituted by substitute each distance d(x, y) by the function f[d(x, y)]out with the stationary distribution Fujimoto argued as above. However

side. Then that side has to have the larger sum of probabilities else PMP will be violated. But #2 can be interchanged with the cartridge immediately on the left label the cartridge placed in the OPA location instead as #j. Draw a symmetry line such that #j and #(k+1) are in mirror image locations on this line. There are three cases to consider. (i) If #j is closer to cartridge #1, the are equidistant from cartridge #1 then k must be an even number. Draw a symmetry line through cartridge #1. The sum of probabilities on #js side must be higher as kis an even number and so cartridge #2 is on its side of the line. (iii) The case where #(k+1) is closer to cartridge #1 cannot occur. This completes the proof of the Next it is necessary to show that only an OPA has the PMP over all symmetry lines. Here we deviate from Fujimoto and use a proof by induction. Order the cartridges in decreasing value of request probabilities. Place cartridge #1 in location 1. If cartridge #2 is not placed in location 2 or n then pass a symmetry line adjacent to the location in which #2 has been placed such that #1 is on the opposite side of #2. Let #1 be on the left of the symmetry line which is a contradiction. Let the first k cartridges be placed in OPA, starting with #2 in location 2. If the cartridge #(k+1) is not placed in OPA sum of probabilities on #js side of the line is greater. This leads to a contradiction. (ii) If both #j and (#k+1)proposition

The OPA arrangement is optimal in the anticipatory case too. Proposition 2.

anticipatory position of the head should be at location with the maximum $p_{\pi(i)}$. of possible rotational distances as the weights w, in follows that the OPA arrangement is optimal and the sum: $\sum_{i=1}^{n} w_i p_{\pi(i)}$ is the one that forms each term in the above sum by multiplying the j^{th} largest value of the p_i 's with the j^{th} smallest value of w_i 's. If we fix the position of given two sequences w_1, \ldots, w_n and p_1, \ldots, p_n , of all permutations π of the p_l 's, the one that minimizes the the head at a particular location, exactly one cartridge at most two at distance 1 etc. If we consider our sequence In the anticipatory case, by the independence property we will always position the head at the same cartridge is essentially assigned a travel distance on a will be at distance 0 (distance measured in units of $2\pi/n$), permanent basis. By the inequality of Hardy et al. (1991), between requests (ignoring ties). So location

Remark. The proof assumes that either the move to reposition the head is completed before the next request arrives, or the move is always completed regardless of whether a request has arrived. The latter case assumes no interruptions are allowed during the rotation of the carousel towards its anticipatory position.

cartridge can hold m equi-sized files and requeserence by probabilities are given for each file. This is analogous and pages, however the method of proof here is different use a direct interchange argument whereas In the next proposition we consider the case that each to Theorem 1.3.1 of Wong83 which deals with records Wong83 uses Schur functions. Proposition 3. The OPA policy is optimal for the non-anticipatory case and when there are m files stored per cartridge. Proof. The OPA arrangement in this case is obtained by sorting mn files in descending order of request probabilities and grouping the first m in bundle #1, the second m in bundle #2 etc. Then the bundles are placed in forward extension of proposition 1. Let the OP® property not hold for the optimal arrangement. But by OPA fashion. The proof of optimality is a straighter forward extension of proposition 1. Let the OPA before) be larger. Call these mirror image locations on the left side *i* and that on the right *j*. What the violation implies is that the probability that a cartridge in location proposition I the property has to hold with respect to the bundles of files. Without loss of generality let the property not hold for files in two mirror image locations say across a given symmetry line. Also let the sum of probabilities on the left side of the symmetry line (as i will be requested can be made larger by interchanging abel the files in location i as l through m and those in location j as (m+l) through 2m. Label the sorted order files between locations i and j. Without loss of generality, in descending

probability as l' through 2m'. Consider bundling l' through m' into location i and the rest in location j. Note that this interchange does not affect the cost of interaction between other locations. Also the interactions between other locations and interchanged files leads to a decrease in cost as in (iii) of proposition 1. We thus are left with comparing

$$\sum_{i=1}^{m} p_i \sum_{i=m+1}^{2m} p_i \text{ and } \sum_{i=1}^{m'} p_i \sum_{i=m'+1}^{2m'} p_i.$$

The minimality of the second expression obtained from a simple interchange argument. To see this, let $p_l < p_{m+1}$. Then interchanging these two alone leads to the difference:

$$-p_{m+1} \sum_{i=2}^{m} p_i - p_i \sum_{i=m+2}^{2m} p_i + p_{m+1} \sum_{i=m+2}^{2m} p_i + p_1 \sum_{i=2}^{m} p_i$$

$$= (p_{m+1} - p_1) \left(\sum_{i=m+2}^{2m} p_i - \sum_{i=2}^{m} p_i \right)$$

$$\sum_{i=m+1}^{m} p_i - \sum_{i=m+1}^{2m} p_i \geqslant 0 \text{ and}$$

$$p_{m+1} > p_1 \Rightarrow \sum_{i=m+2}^{2m} p_i - \sum_{i=2}^{m} p_i < 0$$
(1)

(1) and (2) together with the hypothesis shows that the interchange of the two files is beneficial. The proof then is completed by showing that only by sorting the files and bundling them can we avoid any violation of the OPA arrangement as defined initially. But this is easy, because (i) the files are first sorted and so the bundles have descending sums of probabilities. So if two mirror image locations violate the OPA property with respect to files then all the files in the two locations need to be interchanged. But the bundles are in OPA order leading to a contradiction. And (ii) if the files were not sorted then an interchange is always possible.

(ED

Proposition 4. The OPA order is optimal for the anticipatory case when m files can be placed per cartridge.

Proof. Similar to proposition 2.

Proposition 5. When there are two read heads placed symmetrically opposite one another, the optimal anticipatory policy is OPA on each half of the carousel.

Proof. We need to define this ordering and will do so shortly. The basic idea is that the repositioning is the same between requests. So the anticipatory action allots a permanent distance to be traveled to each file. If the

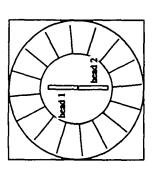


FIGURE 3. A carousel with two read/write heads symmetrically positioned.

number of storage locations is even, say 2x, then the available values for the distance are 2m zeros, 2m ones,... By the Hardy, Littlewood, Polya inequality an optimal arrangement is to order the files per descending request probability and place files #1 through #m in location 1, files #(m+1) through #(2m) in location (x+l) etc. In between requests, the strategy is to bring the carousel with locations 1 and (x+1) aligned with the heads. The case of odd number of storage locations is similarly solved.

OED

The case of two read heads and non-anticipatory type of operations is more difficult. The problem is which way should the carousel rotate? First, let us assume that there are an even number of cartridge locations on the carousel; in which case the direction of rotation is immaterial as far as the next request is concerned. In the next proposition we show that for even number of cartridge locations the nearest head policy combined with OPA on each half of the carousel will be optimal. Interestingly, this is not optimal for odd number of locations as we show in the next example.

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Consider the carousel schema of Figure 4 with five cartridge locations. In this case, to ensure that the heads are aligned with some cartridge locations, the smaller angle between the two heads is $4\pi/5$ (and the big one $6\pi/5$). Let us assume that each of the request probabilities of cartridges at locations 1, 2 and 4 are a and that of cartridges at locations 3 and 5 are each 0.5-3a/2. The carousel is currently at the position shown in Figure 4a when a request to read cartridge at location 5 arrives. When the value of a tends to zero, it is clear that rotating the carousel to the position of Figure 4c (the black head serving the request) is optimal as the two heads are now positioned such that with probability 1-3a, the expected rotational distance for serving the stream of future requests is 0. On the other hand, the nearest head policy will lead to oscillations between 4a and 4b at each future step probability arbitrarily close to 0.5. positions of Example.

Proposition 6. When there are an even number of locations, OPA is optimal.

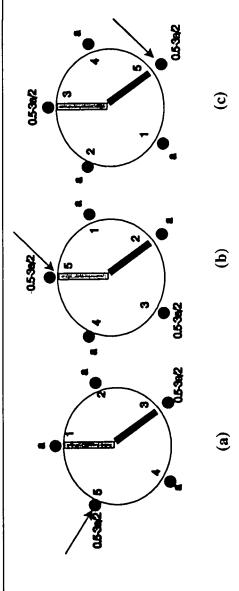


FIGURE 4. (a) Current position of carousel, when cartridge at location 5 is requested. (b) Nearest head policy, carousel rotates $2\pi/5$ in the clockwise direction, grey head serves the request (c) optimal policy carousel rotates $4\pi/5$ in the counter-clockwise direction, black head serves the request. policy carousel rotates $4\pi/5$ in the counter-clockwise direction, black head serves the request.

optimal Therefore the problem can be reduced to the case when there are n/2 locations to be filled each capable of holding two cartridges. Proposition the nearest head policy is rotational strategy. 3 provides the result. The Proof.

QED

The optimality in propositions 3 and 6 can be extended to hold in the stochastic sense as done in proposition 1. Remark.

the mass storage system are queued and serviced on a first In many practical multiuser applications, the requests to come first served basis (FCFS). In the next proposition we utilize two powerful theorems from Stoyan (1983) to show that OPA is optimal in this case as well.

OPA minimizes the average queueing delay as well as the Proposition 7. For the non-anticipatory case, for any of the three models of proposition 1, 3, and 6, when requests arrive as per a general renewal process and they are attended on a first come first served (FCFS) basis, time spent in the system.

proof follows from the fact that by 3, and 6, when starting out with the stationary distribution, the time to serve a request is the smallest in the stochastic sense under the OPA order. The rest of the proof can be found in theorems 5.2.1 and 6.2.1 The propositions 1, (Stoyan, 1983).

QED

4. SIMULATION RESULTS

also In this section we use simulation to (i) investigate the case a repositioning (anticipatory) between when successive requests for cassettes can be correlated obtain answers to the questions of how much improve-We there is interference requests. As a by product of the analysis, and (ii) determine how when performs policy

Arrangement over a random placement of cassettes in the carousel and what is the extent of savings due to the savings of an anticipatory policy.

4.1. A Markov chain model for requests probabilities

Successive requests for cassettes will not be independent in any practical situations. A plausible modelings approach in such situations is to use a Markov chain to model the dependence between successive requests. Markov chain is given by solving the equation p = pP. It may be verified that if anticipation is not permitted, then will be given by p_{ij} , where $\Sigma_{j=1}^{n}p_{ij}=1$. We assume that the transition matrix $P=(p_{ij})$ is irreducible and that the steady state probability vector, ${\pmb p}=(p_1,p_2\dots,p_n)$ for the the optimal arrangement of cassettes is still OPA based case is very different now, as it is possible to do state dependent anticipation, i.e. depending on what the last for the next request. Moreover given the arrangement (of can be determined simply by computing the expected cost of travel using the transition probabilities. Fotto We assume that given the current cassettes requested is i, anticipatory case will carry over. But the anticipatory request was we can reposition the reading head optimally. cassettes) there is an optimal anticipation point which the probability that the next cassette requested will be $j_{eta}^{ ilde{\omega}}$ example if the cassette i were placed in the position π_i , \dots, n , and if the last request was for cassette j, on p, and therefore all the previous results for the noncost of travel using the transition probabilities. then the optimal repositioning should be done at i = 1, 2,

$$\min_{k} \sum_{i=1}^{n} p_{ji} d(\pi_k, \pi_i)$$

i is placed. Unfortunately, determining the optimal arrangement of cassettes is a very hard problem (it can where $d(\pi_k, \pi_l)$ is the distance between the locations at which cassette k is placed and the location where cassette be shown to be in the class of NP-Complete problems). Therefore we tackled the optimal arrangement problem through simulation. OPTIMAL ARRANGEMENTS OF CARTRIDGES

2 based on p and reposition the reading head between requests, called OPADYN for dynamic OPA (as against using OPA and a non-anticipatory policy), (ii) use each of the vectors $(p_{ij}, j = 1, 2, ..., n)$, i = 1, 2, ..., n to determine n different organ pipe arrangements, compute the expected cost with repositioning between requests cost, i.e. if the organ pipe arrangement is given by π_i , assigned these to be an $n \times n$ matrix and normalized their arrangement of cassettes, we used brute force search over the (n-1)! possibilities. This limited the size of the matrices. To obtain the OPA arrangement for the case when no anticipation was permitted, we solved for the be applied to larger problems (a typical carrousel would have n = 40 cassettes). A simple lower bound can be order depending on the state. For example, if the last then we use the pij, = 1, 2, ..., n to rearrange the cassettes. This clearly provides us with a lower bound. We show this lower bound in Tables 1(a-d). We also tested three heuristics: assume that the cassettes are placed in OPA order ments, denoted as GREEDY and (iii) using the OPA based on p compute which request leads to the highest = 5, 6, 7, 8, 9, 10. For each matrix of size $n \times n$, we sum across rows to be unity. To determine the optimal steady state probabilities through recursive convolution of the transition probability matrix. This gave the steady state vector p. We also wished to obtain a good lower bound for the minimum cost as well as heuristics that can rearranged between requests and put into the OPA being allowed and choose the best of these n arrange-We generated random transition matrices of size nxn, variables. can cassettes uniformly generated random assuming that the request was for cassette i, $= 1, 2, \ldots, n$, then find þ generated n^2 obtained

$$\max_{j} \left\{ p_{j} \left[\min_{t} \sum_{i=1}^{n} p_{j,i} d(\pi_{k}, \pi_{i}) \right] \right\}$$

call this row h. Then use an anticipatory policy and OPA based on the transition probabilities, p_{hj} , $j=1,2,\ldots,n$.

This heuristic is called HICOST. We investigate the case where there is only one read head.

the average 13-17% of travel time. These findings are optimality of the heuristics and the savings from using It is seen that the lower bound gets progressively worse as n increases. The GREEDY heuristic performed well in the best, and that the degree of sub-optimality is on the below 5.5%. The other interesting finding from these experiments was that an anticipatory policy can save on also summarized in Figure 5 showing the average sub-9 6 9 findings. We see that the GREEDY heuristic performed average <3.2%. The worst case performance was also the best heuristic arrangement and an anticipatory policy ducted 20 trials for n = 5, 6 and only 10 trials for the rest. these experiments. In Table 1e we summarize these ≰ Tables 1a-d summarize our simulations. over OPA without anticipation.

4.2. Effect of interference of requests on anticipatory policies

ing the reading head will add some overhead because of In practical situations it is of interest to know when to use anticipatory policies when requests arrive as per some random process. Reposition--so when does the trade-off between these two effects favor repositioning? In the commercial systems available today, it is not possible to change the command for moving to a position while the command is being cannot change our mind once having given a command to before that command mitigating this effect. One method would be to reposition one location at a time, for example if we are currently at a we could do the repositioning in two steps, first to the travel time for moving the head to an anticipatory position, but repositioning saves on subsequent travel proposition 7, we restricted our attention to nonposition i and would like to reposition to location i + executed. There are several options available executed. This creates a situation where we reposition and request arrives anticipatory policies. time-.8

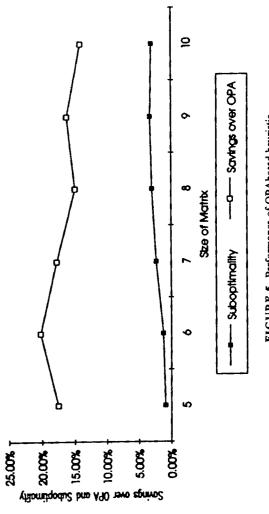


FIGURE 5. Performance of OPAbased heuristic.

0/47:07	0/ 07:1		61	1	Totals			<u>-</u>					
%\$1.0Z	%05.1 %98.1	0	61 1	0	22211.1	17421.1	£87 <u>60.1</u>	111522	L9861.1	L9E61 [.] 1	1,40259	70	
	%18.0	0	1	0	41151.1	12791.1	1.12201	41151.1	81822.1	94880.I	7233E.1	61	
%18.02	%18.0	0	I.	0	1.13063	1.14226	1.11623	1.13063	90712.1	61 1 90.1	1.382.1	81	
%97.27			0	ī	1,14346	1.21456	82921.1	££\$71.1	34541.1	£1880.1	1,25994	LI	
%61.01	%0S.1	0	Ū	0	28660.1	24981.1	28660.1	28660.1	17552.1	88070.1	6674£.1	91	
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23.85%	%00.0	0	1	•	\$6890°I	1,10605	61110.1	61110.1	21890.1	9+0026.0	£7£0£.1	εī	
%86.87	%00 .0	0	l .	0	61110.1	1.0963			660£1.1	1.0250.1	1.24912	71	
12.52%	%00.0	0	ł .	0	60011.1	£6591.1	60011.1	60011.1		\$9\$7L6.0	28602.1	II	
16.39%	%00.0	0	į.	0	1.03949	1.12086	1.03949	1.03949	S >6 E1.1				
15.39%	% <i>L</i> S``Z	0	I	0	1.14204	1.16834	7211.1	1.14204	722.1	1.06524	1.28349	01	
%26.4I	%20.2	0	I	0	1.1634	1.20937	1.13994	1.1634	1.21445	91511.1	755.1	6	
%08.21	%99'7	0	I	0	1.17622	8402.1	£6441.1	1.17622	1.25318	82880.1	1.36207	8	
%9Z.T£	%£Z.£	0	I	0	112478.0	0.918299	292948.0	112478.0	<i>LL</i> £966.0	468167.0	1,20036	L	
%1 <i>5.</i> 72	%77° <i>†</i>	0	Į.	0	1.05066	1.06633	1.00632	990£0.1	82890.1	672726.0	696EE.1	9	
%6 <i>L</i> .81	%00.0	0	I	0	1.19612	123151	1.19612	1.1961.1	47212.1	281-81.1	1,42086	Ş	
% 1 8.97	%80.2	I	1	0	11960.1	11960.1	1.07332	11960.1	1.20023	8£820.1	1.39028	Þ	
% bb .92	%00.0	0	Ī	0	1.03424	1.08734	1.03424	1.03424	1.14352	922756.0	9970£.1	3	
14.25%	%00.0	0	Ţ	0	1.10995	6L0L1.1	1.10995	1.10995	1.16885	1.03782	71892.I	7	
%ZÞ.6I	%\$9°I	0	I	0	1.15723	1.18465	1.13812	£2721.1	1.20419	1.05927	1.38192	I .	
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% > L'01	%00.0	Ī	Ţ	0	67 4 868.0	67 4 868.0	67 1 868.0	67 1 -868.0	701749.0	819178.0	286466.0	LI	
20.17%	% <i>LL</i> `I	0	Ţ	0	208556.0	1.00139	15719.0	208559.0	946338	8£9978.0	1.12213	91	
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%EÞ.11	%\$L"T	0	ī	Ţ	2.01539	2.08531	≯ 1096'1	2.01539	2.01723	78197.1	2.24565	7	
24.81%	%11.8	0	ī	0	1.89382	\$98061	£1 <i>L6L</i> 1	28E98.1	2.01192	16672.1	7636.2	٤	
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ZYNEOPA	DENN %	HICOST	GKEEDY	OPADYN?	€ Yo ru™	LSOOIH	OPTIMAL	CKEEDY	OPADYN	TOMBD	TATZA90	גוָסן
15.22%	7.22%	0	Ī	0	2.01376	2.07533	90696.1	2.01376	2.13392	1.82401	2.32026	9
%\$0°6	3.15%	0	τ	0	2.0138	2.08705	1.95038	2.0138	2,06198	79397. I	2.19595	L
% t \$'6	%98.7	0	ī	0	1.9546	2.03759	1.89633	1.95246	2.03842	٤٢.١	17851.2	8
%L9.81	%£7.£	0	Ţ	0	1.9699.1	19889.1	L0968.1	12696.1	2.01925	<u>,</u> 1969`I	12872.2	6
%9 5 .8	7.51%	0	I	0	2.0478	2.10834	1.99639	87 Þ 0.2	2.0915	1.82538	2.223	01
%E6.E1	%66.2	0	10	0	alatoT							

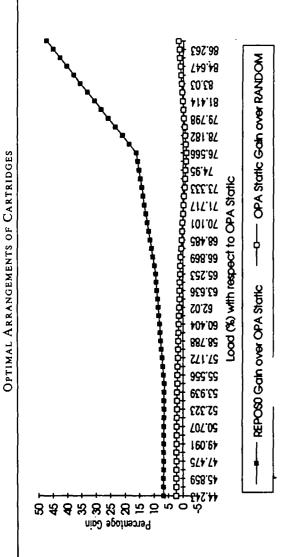


FIGURE 6. Performance of OPA static versus REPOSO & RANDOM, number of locations = 10.

1989). We assume that the cassette request probabilities ocation i+1 and then to location i+2. Even such a provision is unavailable today. We assume therefore that once a command to reposition has been given, it has to be executed and only then subsequent commands can be taken up for execution. We also assume that requests are served in the first come first served (FCFS) order. We assume that the arrival process of requests can be modelled by using a Poisson process. Given that a large number of users will be making infrequent requests to a tertiary storage system, this is a reasonable assumption make (for example see Gnedenko and Kovalenko, are such that 70% of the requests are for 10% of the cassettes, 20% for 20% of cassettes and the remaining 70% of the cassettes. If files that are rarely are put into tertiary storage, then based on practical experience this assumption would be valid. 10% for accessed 2

We assume that the original model for cassette requests holds, i.e. requests are independent of one another and that the request probabilities do not change over time. We investigate the case when there is only one read head. Given these assumptions we ask: does repositioning yield any benefits? How much benefit do

we get from using an OPA arrangement over a random arrangement of cassettes?

simulation results for the case n = 10. The cassettes are carousel from 10 to 40 cassettes in steps of 10. The of n, medium load class, i.e. 20% of n and low load class example, if n = 10, the request probabilities were set to be: 0.7, 0.1, 0.1, 0.0142857, 0.0142857, 0.0142857, reading time from the tape was assumed to be uniformly distributed over [0, 2] and the rotational time between two adjacent locations to be 0.1. In Table 2a we show the arranged as per OPA in all except the columns labeled repositioning policy. In STATIC OPA, we do not allow in Tables 2a-d. In these experiments we varied the load on the system from 30% to 95% and the size of the request probabilities were assigned as follows: given n = 10, 20, 30, 40 break up *n* into high load class i.e. 10% consisting of 70% of the n cassettes. We then assign Note that the average service time will answer these questions and their results are summarized depend on the arrangement of cassettes as well as simulation experiments 0.0142857, 0.0142857, 0.0142857 and 0.0142857. request probabilities uniformly within each class. several conducted RANDOM.

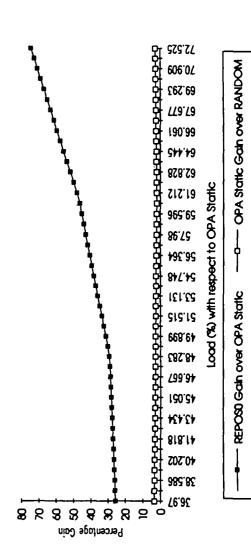


FIGURE 7. Performance of OPA static versus REPOS0 & RANDOM, number of locations = 20.

(KAI)	(KEPOSØ)
01 = 20	. Number of tape location

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1.5443.1	12410.0	21673	1498000	760222	68£.7	715.1	8£7.7	TEE.1	36.2	\$04.I	\$6\$°L	19.26	£2£.1	T.(
766.42TI	6,016893	186.4	8.19911	8.6664	724.2	1.302	795.2	82E.1	3.448	804.1	2.468	92.9 <i>L</i>	1.321	9.
1.259124	0.028529	2.084	3.926	3.093	1.332	882.I	<i>L94</i> .1	1.374	₽ / 9'I	704.1	75.1	99	1.32	ç.(
226032.0	6.052503	£20.1	1.529	24£.1	618.0	82.1	726.0	1.393	186.0	1.412	298.0	53	1.325	þ ′(
976295.0	707530.0	669.0	698.0	187.0	812.0	1.264	£68.0	901·I	\$19.0	614.1	155.0	27.9£	225.1	£.(
<i>I</i> -(<i>I</i>)/(ε)	I-(Z)/(I)	thir 20 Trials	thir 20 Trials	(٤)	<i>(z)</i>	əmi∏	mətey2 ni	smiT.	in System	əmiT	(I)	(%)	∍nüT	Saie
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18.2481	SEE700.0	60°L	<i>L</i> 91 <i>L</i> 1	1.7808	3.272	2.1	28E.E	1.233	196.₽	6LZ.1	3.296	<i>L.</i> ₽8	12.1	L'(
LZ6947.0	0.028145	2.208	₽£9. č	3.127	147.1	861.I	678.1	1.249	2.2	1.281	6L.1	2T.2T	1.212	9.0
0.463282	0.020352	1.291	≯66°I	19°I	180.1	681.I	991.1	1.261	1.269	1.282	1.103	L.03	1.214	٤.(
0.292244	0.02849	687.0	190.1	££6.0	207.0	1.182	≯ LL.0	LZ.1	₱08.0	1.282	22 <i>T</i> .0	48.55	1.213	4.(
\$952530	922250.0	412.0	7£9.0	282.0	24. 0	LI.I	102.0	₽72.I	18.0	182.1	994.0	££.8£	1.2.1	£.(
' Ι-(Ι)/(ε)	I-(Z)/(I)	thir 20 Trials	slairT 02 ri	(E)	(2)	5miT	mətey2 ni	əmiT	mətey2 ni	smiT	(I)	(%)	∍ เกมัT	Rate
шориоу	Static OPA	mosm niM	ирәш хрүү	тэзгүг и	msizyZ ni	Setvice	лэqшN	Service	мтрег	Service	məteyZ ni	mərs4S	Service	Arrival
Static OPA over	KEZLOZO ongl			1эqum _N	Number	uvəşy	Mean	Mean	wegy	Mean	лэ <i>фит</i> ү	ио роо7	nns M	
Gain	Gain			Mean	Mean						Mean			
			pəopjd λημι	Tapes randor	Аздигэ ио	Repositi	ј изум и	Reposito	מ מןאמאז	Repositio	əpu yd	O siatic		
			(SlairT OS	(KANDOM :	(ØSO	(Ber	(150	(BEL	(SOa	(BE	(VdO	oiiviS)		
				0ζ = ε	ape locations	To radmu	VBLE 2b. N	T		· · · · · •				
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782£6Þ.0	<i>L\$L</i> 10.0	4.326	198.7	cc0. 9	₹86.€	1.09	4.026	790.1	60£.₽	1.105	4.054	22.78	1.094	8.0
912691.0	68110.0-	2.054	2.798	2.416	2.102	₹80.1	2.132	1.099	2.186	901.1	2.077	88.9 <i>T</i>	1.094	T.0
6 1 £\$60.0	81010.0	80£.1	res.1	614.1	LLZ. I	180.1	215.1	1.102	1.354	1.106	1.29	4 9.89	1.094	9.0
979 1 90.0	6,019653	68.0	L66 [.] 0	6£6.0	£88.0	770.1	£68.0	1.104	706.0	701.1	288.0	T.42	1.094	٤.ر
Þ £Þ£90.0	0.023569	109.0	€69.0	6 1/ 9.0	468.0	£70.1	\$19.0	\$01.1	129.0	701.1	809.0	9L.£4	1.094	4.(
Ι-(1)/(ε)	I-(z)/(I)	slairT 02 ni	in 20 Trials	(٤)	(7)	snúT.	mətey2 ni	snúT	in System	smiT.	(I)	(%)	sniT	Raie
шориру	Static OPA	msm niM	уу ах шеан	mətey2 ni	mətey2 ni	Setvice	19qumN	Service	Number	Service	mətey2 ni	System	Service	lovitth
Static OPA over	RESPOSO over			15qmnN	Number	Mean	Mean	Mean	Mean	Mean	Number	uo poo7	Mean	
Gain	Gain			Mean	Mean						Меап			
			named Ann	Tapes randor	Aidum uo	nisodəy	า นอนุค น	Reposito	sypwin no	Repositio	opu ya	Static O		
				:WOUNT)	(ØSO		(,50		(SOd			(צומווָכ		

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			(; 20 Trials) omly placed		ksoli) OSO)			(KEP	ekdwid in (ŜOc	(KEI Kepositio	opru y d (VdO)			
Gain Static OPA over monasa (%) I–(I) (£)	Gain Static OPA (1) (2)-1 (%)	% in 30 Min mean % ShirT OS ni	% msm xaM zlaivT O2 ri	Mean Munber in System (5)	Mean Mumber in System (2)	Mean Service SmiT	Mean TədmuM mətsy2 ni	Mean Service SmiT	nosM 19dmuN mstev2 ni	Mean Service snaT	Mean Number is System (1)	(%) Weisks Wood on	Mean Service smiT	Arrival Rate
98004.0	£47190.0	14.0	8£2.0	č. 0	725.0	225.1	96£.0	LLS'I	904.0	282.1	ree.0	29.04	1.452	2.0
9.642036	662070.0	££8.0	1,105	Ī	695.0	1.326	L9 .0	2E2.1	707.0	1.554	609.0	45.9	£4.1	€.0
886£00.1	1201-50.0	74E.1	2.593	10.2	£6.0	275.1	£60.1	812.1	212.1	955.1	1.003	80.7 <i>c</i>	724.1	₽.0
27640.01	11270.0-	3.566	6L.86	70	789. I	1.402	9\$6'l	1.502	712.2	1.563	18.1	T.1T	1.434	2.0
81503.2	9 \$1 00.0—	18406	L080S9	320230	744.E	214.1	6\$1.4	894.1	14.6	655.1	626.€	38.28	164.1	9.0
p.978271	14250.0-	₱66LEL	7947000	1827000	10.922	82Þ. I	£11.11	8 44 .1	9.2558	rss.1	898.01	872.1 4 6	1.433	99.0

TABLE 24. Tape locations = 20

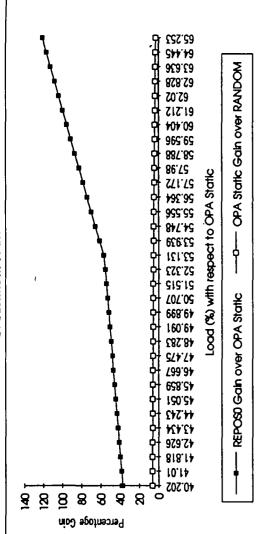


FIGURE 8. Performance of OPA static versus REPOSO & RANDOM, number of locations = 30.

with load almost back to the STATIC OPA case, and on top of probability. In REPOSI, we reposition when there is one ₩e that suffer a penalty whenever repositioning interferes with the next request.) This demonstrates the trade off between repositioning overhead and the reduction in the which as seen from the table adds tremendous overhead to the mean service time because the carousel always rotates back to the cassette with the highest request request and give the repositioning command when that cassette is taken up for service. That is at the time of command for repositioning, which is always executed. This adds decreasing amount of overhead as the load reposition when the system is empty. This adds overheads once in a while, but that overhead is not shown in the table as it was difficult to adjust the simulator to compute the overhead added to the request that arrived while the carousel was being repositioned. However note because less and less repositioning gets done as the load increases. (If repositioning is not done frequently we are reference to this policy. In REPOS we always reposition, taking up for service the (lone) request we add as seen from Table 2a. In REPOS0 that the mean service time increases with the and the system load is computed repositioning increases,

OSO & RANDOM, number of locations = 30.

mean service time. Finally, we generated 20 differents random arrangements of cassettes and assumed that not repositioning was done in these 20 cases. We show the number of requests over the 20 cases. For each policy arrangement we give the average number of requests in the system over a suitable length of simulation. The in the system wag collected for each time interval of 1000 units to get $\ddot{\mathbb{R}}$ standard error for the average number in the system ove the entire run. The run length of the simulations was adjusted to keep this standard error within 1-2% of the average number in the system for the entire length of simulation. The standard errors are not shown in the Tables. The simulation was coded in f77 and run on a network of SUN workstations at the Leonard N. Stertiff give the mean, maximum and minimum of the average simulation runs were for 10000 to 9000000 time units results from these arrangements under RANDOM, and school of Business, New York University. The average number of requests

The results show that REPOS is not a good strategy REPOS0 is the best strategy we have discovered. But even REPOS0 gave at the most 9% improvement over OPA STATIC and that too at low loads. This is shown in the graphs in Figures 6-9. The remarkable fact from

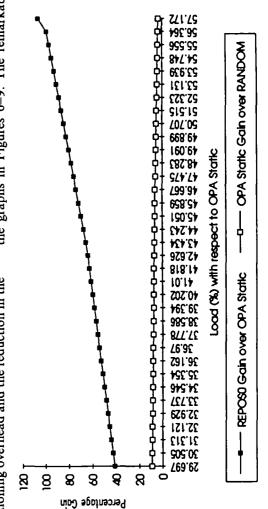


FIGURE 9. Performance of OPA static versus REPOSO & RANDOM, number of locations = 40

OPTIMAL ARRANGEMENTS OF CARTRIDGES

outperforms ncreases, the gain in performance becomes better and caronsel STATIC the as OPA and that significantly .s simulations RANDOM

use of OPA reduces the average service time. The extent of the reduction in service time will depend on the size of the carousel, because RANDOM has a greater chance to Jeviate from the optimal arrangement as the size increases. Another factor that influences the percentage eduction in the average service time is the ratio between the average time to read from a cassette and the average ravel time to move to the cassette location. This atio would get progressively small as the size of the arousel increases. Thus the relative improvement in the average service time will increase (by using OPA over The explanation for the improvement in performance over RANDOM, lies almost entirely in the fact that the RANDOM).

CONCLUSIONS

of carousel type robotic tape library. The this paper we studied organization schemes eartridges on a carousel type robotic ta following Table summarizes the results:

	Anticipatory	Non-Anticipatory
One head/Single File	Proposition 2	Fujimoto (1991), Proposition 1
Two heads/Single File	Proposition 5	Proposition 6 (even number of
One head/Multiple Files	Proposition 4	locations) Proposition 3
Two heads/Multiple Files	Proposition 5	Proposition 6
		(even number of locations)

we showed that by using the concept of stochastic ordering, all the above results can also be environment extended to the queueing In addition, policy.

Some questions raised by this work are:

(i) Varying file sizes. In the file allocation problem we assumed that the files are of equal size. If the file sizes are not the same, we will have packing limitation based on file size and cartridge capacity. This leads to an NP-complete problem as shown in Wong83. Based on files as per the request probability per unit of size and ordering them in OPA the results in this paper a good heuristic can constructed by first ranking files as per the requ based on these modified probabilities. on file size and cartridge capacity.

(ii) Other queueing disciplines. We have ignored schedulng problems in proposition 7 by assuming a FCFS

some advantage in attending to requests that need smaller files 12. there vary, sizes discipline. When file on a priority basis.

picks four parallel drives. Optimal arrangements of cartridges (iii) Analysis of other robotic devices. The carousel is only one type of robotic device, other architectures include cabinets with multiple shelves such as the EXB-120 (by cartridges from the shelves and places them in up to in such architectures and efficient mount schedules of the robotic arm Exabyte Corporation) where the parallel drives are of interest.

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