Optimising Quantity of Manufacturing and Remanufacturing in an Electric Vehicle Battery Closed-loop Supply Chain

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Abstract

Purpose – Batteries installed on electric vehicles (EVs) should normally be removed when their capacity falls to 70-80%, but they are still usable for other purposes, such as energy storage. This paper studies an EV battery closed-loop supply chain (CLSC) consisting of a battery manufacturer and a remanufacturer. The manufacturer produces new batteries by using natural resources, while the remanufacturer collects returned batteries and makes decisions based on the return quality, that is, to reuse or recycle. The purpose of this research is to maximise the individual profits through optimising the amount of manufacturing and remanufacturing respectively, and optimising the purchase price of returned batteries.

Design/methodology/approach – Based on the Nash equilibrium, this paper develops a three-period model in the CLSC. In period 1, batteries are made from raw materials; in period 2, returned batteries from period 1 are sorted into low quality and high quality. Some high-quality returns can be reused for other purposes while those non-reusable returns are recycled into materials. In period 3, all the returns are recycled into materials. The analytical results are derived.

Findings – The result of the analyses suggest that (a) among the variables that affect the (re-)manufacturing decision, the purchase price for returned batteries plays a critical role. In particular, the price of low-quality returns has more influence than the price of high quality returns. (b) Interestingly, the higher purchase price for re-usable returns does not necessarily lead to a higher return rate of reusable returns. (c) The manufacturer's profit is normally higher than the remanufacturer's. This suggests the need to design incentives to promote the remanufacturing sector. (d) Although it is appreciated that maximising the utilisation of batteries over the life-cycle would benefit the environment, the economic benefit needs further investigation.

Originality/value – Although the CLSC has been widely studied, studies on the EV battery CLSC are scarce. The EV battery CLSC is particularly challenging in terms of the reusability of returns because used EV batteries cannot be reused for the original purpose, which complicates CLSC operations. This paper explores the interrelationship between manufacturer and remanufacturer, explaining the reasons why recycling is still underdeveloped, and suggests the possibility of enhancing remanufacturing profitability.

Key words – Closed-loop supply chain, Electric vehicle battery, Recycle, Reuse, Purchasing price, Profit

Paper type – Research paper

1. Introduction

With the aim of achieving sustainable development, electric vehicles (EVs) are considered one of the future directions for the automotive industry. One of the earliest studies regarding EV's history, progress and advantages can be found in Turner and Heusinger (1984). In the 21st century, the EV industry is developing and the uptake of EVs is increasing rapidly. According to the International Energy Agengy (2016), from 2005 to 2010 the number of EV sales, including pure battery EVs and plug-in hybrid EVs (PHEVs), increased from 1670 to 12,480 worldwide. Since then, the number of new-energy vehicles has been increased even more sharply. By 2015, the stock of EVs was 1,256,900, which is almost 752 times higher than 10 years ago.

One of the most important components of an EV is the battery. The high uptake of EVs leads to a high demand for EV batteries. The battery's operating life affects the EV's mileage directly. For example, Tesla model S P90D's battery duration is 430km with an embedded 95kWh battery (Tesla, 2016). The working mileage of an EV battery may affect the desirability to customers of buying an EV. Unlike gasoline vehicles, EVs cannot use their batteries until they reach the end of their life-cycle. Instead, the batteries have to be removed when their capacity fall to around 70-80% due to performance and safety concerns (McIntire-Strasburg, 2015). In early 2010, the US National Renewable Energy Laboratory undertook a project on EV battery reuse (Neubauer and Pesaran, 2010). The report shows that a recycled battery can be reused in the following ways: (a) grid-based stationary, for example energy time shifting, renewables capacity firming; (b) off-grid stationary, for example backup power and remote installations; and (c) mobile, for example commercial idle management or public transportation. Those applications for EV second use could significantly increase the total lifetime value of money, and thus reduce the cost to the electric automotive user.

Most of the research studying the reuse of EV batteries has focused on the technical aspects (e.g. Lih et al., 2012; Neubauer and Pesaran, 2011; Patten et al., 2011; Yu et al., 2013). How reuse of EV batteries affects the operational performance and profit of the closed-loop supply chain (CLSC) remains untouched. From an operations management point of view, research lags behind the industry. In response to automotive batteries being banned from landfill or incineration, EV battery collection and recycling networks have been built. Nevertheless, most of the returned batteries are recycled into materials rather than being reused. To deal with this issue, some industrial initiatives exist, for instance in North America, Tesla, working with Kinsbursky Brothers, recycled about 60% of its battery packs; in Europe, Tesla started working with Umicore on recycling (Kelty, 2011); and Nissan and Volkswagen require their EV customers to return used batteries to licensed points or local authority battery collection schemes (Nissan, 2015; Volkswagen, 2016). Now more and more EV manufacturers are involved in reusing EV batteries. For example, BMW and Nissan are expected to reuse returned batteries as home energy storage (Ayre, 2016; Dalton, 2016). Chevrolet has set up an energy storage station by using used EV batteries at the General Motors facility in Michigan (Voelcker, 2016).

Inspired by these applications, we built a three-period model to describe the EV CLSC process. There are two participants in the model: the manufacturer, who produces new EV batteries (over the three periods); and the remanufacturer, who collects used batteries and sorts them into reusable and recyclable based on the quality of the returns in period 2. The reused batteries will be recycled in period 3. In period 1, batteries are *only* made from raw materials. There are no returned or recycled batteries in this period. In period 2, returned batteries are sorted into low quality and high quality. The high-quality returns are further sorted into reusable and recyclable. The recyclable returns will be recycled into materials. In period 3, those reused batteries reach the end of their life and will be collected and recycled into materials.

The paper is organised as follows. The next section reviews some relevant literature and clarifies our contribution to the literature. Section 3 describes the model and derives the optimal quantity, the optimal purchase price and the maximised profit for manufacturer and remanufacturer, respectively. Section 4 conducts a numerical study. Finally, Section 5 concludes our findings and discusses the limitations as well as future research.

2. Closely related literature

The model developed in this paper is related to EV battery reuse and recycling in a multi-period CLSC. In this section, the relevant literature on battery reuse and multi-period SC is reviewed. The purpose is to justify the differences between our model and existing models, and hence our contribution to the literature.

Most research discusses how EV batteries can be reused from a technical point of view. There are very few studies focusing on economic benefits. Patten et al. (2011) discuss how EV batteries can be used in a wind storage system to improve utilisation and make more efficient use of EV batteries prior to recycling. Assuncao et al. (2016) built a model of how repurposed EV batteries can be used to support solar energy. The model is analysed from both technical and economic aspects. In their model, they allow users to generate energy and inject it into the grid for economic benefits. As shown in that paper, the used batteries could be reused for more than 10 years and will bring a good payback to customers. Ahmadi et al. (2014) and Aziz et al. (2015) studied the performance of reused EV batteries in rebalancing the electricity grid. They state that if repurposed batteries are used to store off-peak electricity to serve peak demand, carbon dioxide (CO₂) emissions will be reduced by around 56%. However, some people have different views. Although used EV batteries could be a potential enhancement of cost-effective energy storage, Neubauer and Pesaran (2011) argue that even though the second use of the batteries is not expected to significantly affect PHEV/EV price, longterm battery degradation and second-use applications need to be investigated in more detail.

The CLSC is a well-studied yet challenging area in particular when it becomes a multi-period model. There are several papers that study a two-period model (Atasu et al., 2008; Ferguson and Toktay, 2006; Mitra and Webster, 2008; Webster and Mitra, 2007; Majumder and Groenevelt, 2001), most of which focus on the relationship and

decision making between manufacturer and remanufacturer. For instance, Majumder and Groenevelt (2001) study a two-period competition model between an original equipment manufacturer (OEM) and a local remanufacturer by fixing the total cost for dealing with the returned items. The model developed by Mitra and Webster (2008) analyses the regulation of remanufacturing activities. Moreover, from the multi-period aspect, Ferrer and Swaminathan (2010) analyse the (re)manufacturer monopoly environment from a two-period to a multi-period planning horizon, and develop a strategy for optimising price for the firm in the model.

The literature review suggests that the existing multi-period CLSC models do not reflect the practices of used EV battery reuse and recycling and the characteristics of such CLSC; that is, unlike normal goods, EV batteries cannot be reused for their original purpose, which complicates normal CLSC operations. Therefore, the contribution of this study is to fill the CLSC research gap in EV battery recycling and reuse. This paper explores the interrelationship between EV battery manufacturer and remanufacturer, explains the reasons why recycling is still underdeveloped.

Our study is closely related to two models. The first is a general two-period model designed by Bulmus et al. (2014), which involves an OEM and an independently operating remanufacturer (IO). In period 1, only the OEM is included, while in period 2 both OEM and IO are included in competition. The authors analyse the manufacturing/remanufacturing optimal quantity and profit under Nash equilibrium conditions. Relationships between these and several different parameters – that is, market size, (re)manufacturing cost in each period, return rate and so on – are discussed in their model. In this paper, we expand the model from a two-period to a three-period model, where returned batteries are reused before being recycled into materials in period three. This is moreover similar to Cai et al. (2014), whose model studies the optimal acquisition and production policy in a hybrid manufacturing and remanufacturing system including high-quality core remanufacturer and low-quality core remanufacturer. In our model, we further classify the returned batteries into high quality, low quality and reusable returns.

3. Model description and formulation

We consider a three-period model to describe an EV battery manufacturing/ remanufacturing system as shown in Figure 1.

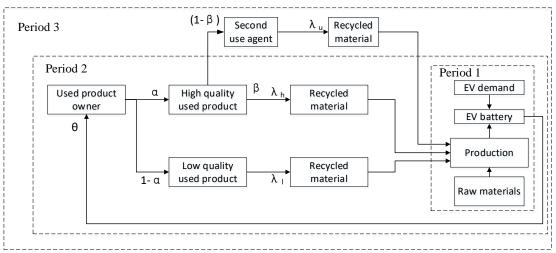


Figure 1: A three-period model in a manufacturing/remanufacturing system

• In period 1, all EV batteries are made from raw materials. The battery manufacturing quantity is based on the EV demand.

• In period 2, the batteries are made from raw materials and recycled materials from returned batteries, both high and low quality. A proportion, θ , of used EV batteries is returned. According to Erp-batteries (2012) and Gaines and Singh (1995), recycled batteries have different conditions so their values are different. We classify returns into two levels: α refers to the proportion of high-quality returns and $(1-\alpha)$ to low-quality returns. Then, high-quality returns will be sorted further. β refers to the proportion that is recycled into materials, and $(1-\beta)$ the proportion that is reused in other places for a certain period. This means that these reused batteries will not be recycled in period 2. Furthermore, because there will be a loss in the process, we set λ_1 and λ_h as the remanufacturing rates for low- and high- quality returns, respectively. We assume that the remanufacturing cost for low-quality returns is higher than that for high-quality returns, that is, $c_{2h} < c_{2l}$.

• In period 3, the reused batteries reach the end of their life and they will be recycled as well. Hence, in this period batteries are made from raw materials and recycled materials from high- and low- quality returns as well as reused batteries. The recycling rate for reused batteries is λ_{μ} .

General parameters					
$M_{EVi}; i = 1, 2, 3$	Potential EV market size in period <i>i</i>	Α	Coefficient between battery material quan- tity and EV quantity: $q_i = Aq_{EVi}, (A > 0)$		
δ_m	Coefficient between EV sale price and material price: $p_i = \delta_m p_{EVi}, (0 < \delta_m < 1)$	$k_{EVi}; i = 1, 2, 3$	For simplification, we define $k_{EVi} = \delta_m / (AM_{EVi})$		
θ	Battery return yield	α	Proportion of high quality returns among total returns		

All the notations used are listed in Table 1. Table 1: Notations

$1-\beta$	Reusable rate among high	C _{nature}	Cost of purchasing raw
	quality returns	naure	materials
C_n	Manufacturing cost of new	c_h	Remanufacturing cost
	battery		of high-quality returns
c_l	Remanufacturing cost of	C_{u}	Remanufacturing cost
	low-quality returns		of reused battery
λ_h	High-quality returns' recy-	λ_l	Low-quality returns
	cling rate into materials		recycling rate
	$(0 < \lambda_h < 1)$		$(0 < \lambda_l < 1)$
λ_{μ}	Reused EV battery recy-	$p_{FVi}; i = 1, 2, 3$	EV price in period <i>i</i>
LL	cling rate $(0 < \lambda_u < 1)$	I Lyt	
$q_{EVi}; i = 1, 2, 3$	Quantity of EV demand in		
$q_{EVi}, r = 1, 2, 3$	period <i>i</i>		
Decision varia	L -	1	1
$p_i; i = 1, 2, 3$	Battery selling price in pe-	$q_i; i = 1, 2, 3$	Total amount of bat-
1 [, , , ,	riod <i>i</i>	11, , , ,	tery needed in period
			i
$q_{in}; i = 1, 2, 3$	Amount of battery made	$q_{il}; i = 2, 3$	Quantity of recycled
	from raw material in pe-		materials from low
	riod <i>i</i>		quality returns in pe-
			riod i
$q_{ih}; i = 2, 3$	Quantity of recycled mate-	$s_{il}; i = 2, 3$	Price of purchasing
	rials from high quality re-		low-quality returns in
	turns in period <i>i</i>		period i
$s_{ih}; i = 2, 3$	Price of purchasing high-	<i>S</i> _{3<i>u</i>}	Price of purchasing re-
	quality returns in period i		used batteries in period
			3
q_{3u}	Quantity of batteries re-	$\Pi_{in}; i = 1, 2, 3$	Profit for new battery
	manufactured from reused		manufacturing in pe-
	batteries in period 3		riod <i>i</i>
$\Pi_{il}; i = 2, 3$	Profit for low-quality re-	$\Pi_{ih}; i=2,3$	Profit for high quality
	turns remanufacturing in		returns remanufactur-
	period <i>i</i>		ing in period <i>i</i>
Π_{3u}	Profit for re-used battery		
	remanufacturing in period		
	3		

For simplification, we assume that each of the initial parameters is the same over the three periods.

3.1 Nash equilibrium in period 1

This study discusses EV battery, and its manufacturing quantity is based on EV market. Assume EV market size is M_{EV1} , its sale price is p_{EV1} . Customer's willingness to pay for the EV is v. We assume that p_{EV1} and v have a uniform distribution between 0 and 1, i.e., $v \in [0,1]$ and $p_{EV1} \in [0,1]$. By adopting the same utility-based approach as Ferguson and Toktay (2006), Bulmus et al. (2014) and Debo et al. (2005), customer utility of buying EVs is $U = v - p_{EV1}$. The quantity of EVs sold in this period becomes

$$q_{EV1} = M_{EV1}(1 - p_{EV1})$$
(1)

Assume that the demand for battery material is $q_1 = Aq_{EV1}$, (A > 0) and the price of an EV battery for each EV is $p_1 = \delta_m p_{EV1}$, $(0 < \delta_m < 1)$, where A and δ_m are coefficients. As in period 1, all EV batteries are made from raw materials, that is $q_1 = q_{1n}$. Hence, through substituting q_1 and p_1 into (1), we have

$$q_{1n} = AM_{EV1}(1 - p_1 / \delta_m)$$
(2)

Let $k_1 = \delta_m / (AM_{EV1})$ and, through formula transformation, the battery price in period 1 is

$$p_1 = \delta_m - k_1 q_{1n} \tag{3}$$

Battery manufacturer's profit is the sale price minus both the raw materials purchasing cost and the manufacturing cost, then multiplied by the quantity of batteries sold. Through substituting (3), the profit can be expressed as:

$$\Pi_{1n} = (p_1 - c_n - c_{nature})q_{1n} = (\delta_m - k_1 q_{1n} - c_n - c_{nature})q_{1n}$$
(4)

To make the study non-trivial and allow profitable manufacturing, we let $0 < (c_n + c_{nature}) < p_1 < 1$ to ensure the profit for the battery manufacturer is positive; that is $\Pi_{1n} > 0$.

As
$$\frac{\partial^2 \Pi_{1n}}{\partial q_{1n}^2} = -2k_1 < 0$$
, Π_{1n} is a convex function. Therefore, the maximised profit

that the battery manufacturer will achieve at $\frac{\partial \Pi_{1n}}{\partial q_{1n}} = 0$. So, the optimal quantity for

manufacturer q_{1n}^* in period 1 is:

$$q_{1n}^{*} = \frac{\delta_m - c_n - c_{nature}}{2k_1}$$
(5)

We have $q_{1n}^* > 0$ as $0 < (c_n + c_{nature}) < \delta_m$. From Equation (5), we can conclude that the optimal quantity for the new battery manufacturer has negative relationship with c_n and c_{nature} . This also means that, with the increase in the raw materials price and the manufacturing cost, the optimal quantity for manufacturing a new EV battery is decreasing. Meanwhile, as can be seen in Equation (3), the lower the manufacturing quantity, the higher the sale price p_1 , reflecting the theory of market leverage.

3.2 Nash equilibrium in period 2

Similar to period 1, the demand for EVs depends on market size and EV price in period 2:

$$q_{EV2} = M_{EV2}(1 - p_{EV2})$$
(6)

With $q_2 = Aq_{EV2}$ and $p_2 = \delta_m p_{EV2}$, the quantity of EV batteries required in this period is:

$$q_2 = AM_{EV2}(1 - p_2 / \delta_m)$$
(7)

And letting $k_2 = \delta_m / (AM_{EV2})$, we can derive the EV battery price function by the inverse of (7):

$$p_2 = \delta_m - k_2 q_2 \tag{8}$$

In this period, θ of batteries will be returned. These returned batteries will be sorted into three classes: reusable, high-quality and low-quality. As shown in Figure 1, reusable returns will be reused in other places, for instance, for energy storage. Only highquality and low-quality returns will be recycled into materials. Therefore, in period 2, the materials needed for producing batteries come from three parts: raw material, material recycled from high-quality returns and material recycled from low-quality returns. The demand for raw materials is the total demand for materials minus the quantity of recycled materials:

$$q_{2n} = q_2 - q_{2l} - q_{2h} \tag{9}$$

We can derive the inverse of demand function (9) by substituting (8) as follows:

$$p_2 = \delta_m - k_2(q_{2n} + q_{2l} + q_{2h})$$
(10)

The total return at period 2 is the return rate θ multiplied by the quantity of existing battery material in the previous period, $A\theta q_{FV1}$.

Applying the utility-based concepts as described in period 1, assuming that the purchasing price for returns, both high quality and low quality, obeys a uniform distribution [0,1], we derive the return quantity for high and low quality in Equation (11):

$$\begin{cases} q_{2h} = A\theta q_{EV1}\alpha\beta(1-s_{2h}) \\ q_{2l} = A\theta q_{EV1}(1-\alpha)(1-s_{2l}) \end{cases}$$
(11)

Because of different values for different qualities, we have $s_{2h} > s_{2l}$.

The quantity of materials made from different classes of return is the return quantity multiplied by the returned batteries salvageable rate, λ_h and λ_l . The profit for manufacturer and remanufacturer is defined as battery sales revenue minus recycling cost and returned battery purchase price. Hence, by substituting (10), profit functions for manufacturer and remanufacturer (e.g. both low-quality and high-quality) are:

$$\begin{cases} \Pi_{2n} = (p_2 - c_n - c_{nature}) q_{2n} = (\delta_m - k_2 (q_{2n} + q_{2l} + q_{2h}) - c_n - c_{nature}) q_{2n} \\ \Pi_{2l} = (\lambda_l p_2 - c_l - s_{2l}) q_{2l} = (\lambda_l (\delta_m - k_2 q_{2n} - k_2 q_{2l} - k_2 q_{2h}) - c_l - s_{2l}) q_{2l} \\ \Pi_{2h} = (\lambda_h p_2 - c_h - s_{2h}) q_{2h} = (\lambda_h (\delta_m - k_2 q_{2n} - k_2 q_{2l} - k_2 q_{2h}) - c_h - s_{2h}) q_{2h} \end{cases}$$
(12)

We also assume $p_2 > c_n + c_{nature}$, $\lambda_l p_2 > c_l + s_{2l}$ and $\lambda_h p_2 > c_h + s_{2h}$ to ensure a positive profit. In addition, due to the higher loss in the recycling process for low-quality returns, we have $\lambda_l < \lambda_h$.

Through the second-order condition, we find that Π_{2n}, Π_{2l} and Π_{2h} are all convex functions:

$$\frac{\partial^2 \Pi_{2n}}{\partial q_{2n}^2} = -2k_2 < 0; \\ \frac{\partial^2 \Pi_{2l}}{\partial q_{2l}^2} = -2\lambda_l k_2 < 0; \\ \frac{\partial^2 \Pi_{2h}}{\partial q_{2h}^2} = -2\lambda_h k_2 < 0$$
(13)

So, they all have the maximum profit which can be achieved by using the first-order condition, that is, $\frac{\partial \Pi_{2n}}{\partial q_{2n}} = \frac{\partial \Pi_{2l}}{\partial q_{2l}} = \frac{\partial \Pi_{2h}}{\partial q_{2h}} = 0$:

$$\begin{cases} \delta_{m} - 2k_{2}q_{2n}^{*} - k_{2}q_{2l}^{*} - k_{2}q_{2h}^{*} - c_{n} - c_{nature} = 0\\ \lambda_{l} \left(\delta_{m} - k_{2}q_{2n}^{*} - 2k_{2}q_{2l}^{*} - k_{2}q_{2h}^{*} \right) - c_{l} - s_{2l} = 0\\ \lambda_{h} \left(\delta_{m} - k_{2}q_{2n}^{*} - k_{2}q_{2l}^{*} - 2k_{2}q_{2h}^{*} \right) - c_{h} - s_{2h} = 0 \end{cases}$$

$$\tag{14}$$

Proof of the existence of a unique Nash equilibrium can be found in Appendix A. Combining Equation (11) and (14), the optimal values are shown as:

$$s_{2l}^{*} = \frac{\left(2c_{l} - J_{21}\lambda_{l} + J_{22} \begin{pmatrix} (3 + \alpha \left(\beta + c_{h}\beta + \beta J_{21}\lambda_{h} - 3\right))\lambda_{l} \\ +4k_{2}J_{23}q_{EV1} - 3c_{l}\alpha\beta\lambda_{h} \end{pmatrix} \right)}{3J_{22}J_{24} + 4J_{22}J_{23}k_{2}q_{EV1} - 2}$$
(15)

$$s_{2h}^{*} = \frac{\left(2c_{h} - J_{21}\lambda_{h} + J_{22}\begin{pmatrix}(\alpha - 1)(3c_{h} - J_{21}\lambda_{h})\lambda_{l} \\ +((1 + c_{l})(1 - \alpha) + 3\alpha\beta)\lambda_{h} + 4k_{2}J_{23}q_{EV1}\end{pmatrix}\right)}{3J_{22}J_{24} + 4J_{22}J_{23}k_{2}q_{EV1} - 2}$$
(16)

Where $J_{21} = (c_n + c_{nature} + \delta_m)$, $J_{22} = Ak_2\theta q_{EV1}$, $J_{23} = A(\alpha - 1)\alpha\beta\theta\lambda_h\lambda_l$

 $J_{24} = \left(\alpha\beta\lambda_h + \lambda_l - \alpha\lambda_l\right).$

(

$$q_{2n}^{*} = \frac{\lambda_h s_{2l}^{*} + \lambda_l s_{2h}^{*} + \lambda_l c_h + \lambda_h c_l + \lambda_l \lambda_h \left(\delta_m - 3c_n - 3c_{nature}\right)}{4k_2 \lambda_h \lambda_l}$$
(17)

$$q_{2l}^{*} = \frac{-3\lambda_{h}s_{2l}^{*} + \lambda_{l}s_{2h}^{*} + \lambda_{l}c_{h} - 3\lambda_{h}c_{l} + \lambda_{l}\lambda_{h}\left(\delta_{m} + c_{n} + c_{nature}\right)}{4k_{2}\lambda_{h}\lambda_{l}}$$
(18)

$$q_{2h}^{*} = \frac{\lambda_{h} s_{2l}^{*} - 3\lambda_{l} s_{2h}^{*} + \lambda_{h} c_{l} - 3\lambda_{l} c_{h} + \lambda_{l} \lambda_{h} \left(\delta_{m} + c_{n} + c_{nature}\right)}{4k_{2} \lambda_{h} \lambda_{l}}$$
(19)

From Equations (15) and (16), we can see that the decision on optimal purchasing prices mainly depends on remanufacturing cost, but also is influenced by other factors such as EV market size, return yield and salvageable rate.

In Equations (17)-(19), only s_{2h}^* and s_{2l}^* are the decision variables; the rest are input constants. Therefore, we focus on how these two decision variables affect q^* . Observing the above equations, knowing that $\lambda_h > \lambda_l$, it suggests that the decision on the optimal purchasing price for low-quality returns is more influenced by s_{2l}^* than s_{2h}^* . But this fact is less prominent in deciding the optimal q_{2h}^* . In general, Equations (17)-(19) suggest the following:

- The higher the purchase price of returns, the less motivation for remanufacturing because of reduced profit. Hence, using raw materials becomes a favourable choice, as shown in Equation (17).
- The lower the purchase price of low-quality returns, s_{2l}^* , the higher the remanufacturing of low-quality returns, q_{2l}^* , as shown in Equation (18), which leads to the following point.
- The need for remanufacturing of high-quality returns is reducing, because the total $q_{2l}^* + q_{2h}^* + q_{2n}^*$ is meant to cover the total demand for battery. Hence, the higher q_{2l}^* , the lower q_{2n}^* and q_{2h}^* .

We then use $q_{2l}^* + q_{2h}^*$ to present the total optimal remanufacturing amount, and $q_{2l}^* + q_{2h}^* + q_{2n}^*$ to mean the total optimal amount of manufacturing and remanufacturing. The purpose is to understand the influence of the purchase price on the (re-)manufacturing operations as a whole. From Equation (17)-(19), we have

$$q_{2l}^* + q_{2h}^* = \frac{-\lambda_h s_{2l}^* - \lambda_l s_{2h}^* - \lambda_l c_h - \lambda_h c_l + \lambda_l \lambda_h \left(\delta_m + c_n + c_{nature}\right)}{2k_2 \lambda_h \lambda_l}$$
(20)

$$q_{2}^{*} = q_{2l}^{*} + q_{2h}^{*} + q_{2n}^{*} = \frac{-\lambda_{h} s_{2l}^{*} - \lambda_{l} s_{2h}^{*} - \lambda_{l} c_{h} - \lambda_{h} c_{l} + \lambda_{l} \lambda_{h} \left(3\delta_{m} - c_{n} - c_{nature} \right)}{4k_{2} \lambda_{h} \lambda_{l}}$$
(21)

Observing Equations (20) and (21), we find that both s_{2h}^* and s_{2l}^* have a negative relationship between both $q_{2l}^* + q_{2h}^*$ and $q_{2l}^* + q_{2h}^* + q_{2n}^*$.

- Equation (20) suggests that the higher the return purchase price, the lower the remanufacturing quantity.
- Nevertheless, the total amount of manufacturing and remanufacturing in period 2 is decided by other factors other than purchase price alone. In this case, the cost of producing new batteries and the purchase price of raw materials play important roles, as shown in Equation (21).

In summary, if we use +/- to represent a positive/negative correlation relationship, the relationship between quantity and the returned battery purchase prices is shown in Table 2 below:

Tuble 2. Relationship between optimal quantities and purchase price in period 2					
Input variable Decision variable	s_{2h}^{*}	s [*] ₂₁			
$q_{2l}^{ *}$	+	_			
$q_{2h}^{}^{*}$	_	+			
$q_{2n}^{ *}$	+	+			
$q_{2l}^{*} + q_{2h}^{*}$	_	_			
$q_{2l}^{*} + q_{2h}^{*} + q_{2n}^{*}$	_	_			

Table 2: Relationship between optimal quantities and purchase price in period 2

3.3 Nash equilibrium in period 3

Similarly, the EV quantity desired in period 3 is

$$q_{EV3} = M_{EV3}(1 - p_{EV3})$$
(22)

With $q_3 = Aq_{EV3}$ and $p_3 = \delta_m p_{EV3}$, the demand for EV batteries in this period is:

$$q_3 = AM_{EV3}(1 - p_3 / \delta_m)$$
(23)

And letting $k_3 = \delta_m / (AM_{EV3})$, we can achieve the price function deriving from Equation (23):

$$p_3 = \delta_m - k_3 q_3 \tag{24}$$

In this period, the battery material consists of raw materials, high and low quality returns and end-of-life reused battery returns. The quantity of demand for new batteries equals the total market demand minus all EV batteries made from returns:

$$q_{3n} = q_3 - q_{3l} - q_{3h} - q_{3u}$$
(25)

And the price:

$$p_3 = \delta_m - k_3(q_{3n} + q_{3l} + q_{3h} + q_{3u})$$
(26)

The return quantity in period 3 is new batteries manufactured in period 2 multiplied by the return rate which is $A\theta q_{EV2}$. In this period, all returns in all three classes will be recycled with the quantities:

$$\begin{cases} q_{3l} = A\theta q_{EV2}(1-\alpha)(1-s_{3l}) \\ q_{3h} = A\theta q_{EV2}\alpha\beta(1-s_{3h}) \\ q_{3u} = A\theta q_{EV2}\alpha(1-\beta)(1-s_{3u}) \end{cases}$$
(27)

The profits for manufacturer and remanufacturer (e.g. low-quality, high-quality and reused batteries) are:

$$\begin{cases} \Pi_{3n} = (p_3 - c_n - c_{nature}) q_{3n} = (\delta_m - k_3(q_{3n} + q_{3l} + q_{3h} + q_{3u}) - c_n - c_{nature}) q_{3n} \\ \Pi_{3l} = \lambda_l q_{3l} p_3 - (c_l + s_{3l}) q_{3l} = \lambda_l q_{3l} (\delta_m - k_3(q_{3n} + q_{3l} + q_{3h} + q_{3u})) - (c_l + s_{3l}) q_{3l} \\ \Pi_{3h} = \lambda_h q_{3h} p_3 - (c_h + s_{3h}) q_{3h} = \lambda_h q_{3h} (\delta_m - k_3(q_{3n} + q_{3l} + q_{3h} + q_{3u})) - (c_h + s_{3h}) q_{3h} \\ \Pi_{3u} = \lambda_u q_{3u} p_3 - (c_u + s_{3u}) q_{3u} = \lambda_u q_{3u} (\delta_m - k_3(q_{3n} + q_{3l} + q_{3h} + q_{3u})) - (c_u + s_{3u}) q_{3u} \end{cases}$$

$$(28)$$

The profits above are all convex because of:

$$\frac{\partial^2 \Pi_{3n}}{\partial q_{3n}^2} = -2k_3 < 0; \\ \frac{\partial^2 \Pi_{3l}}{\partial q_{3l}^2} = -2\lambda_l k_3 < 0; \\ \frac{\partial^2 \Pi_{3h}}{\partial q_{3h}^2} = -2\lambda_h k_3 < 0; \\ \frac{\partial^2 \Pi_{3u}}{\partial q_{3u}^2} = -2\lambda_u k_3 < 0; \\ (29)$$

Using first-order condition to acquire the optimal profit for each agent:

$$\begin{cases} \delta_{m} - k_{3}(2q_{3n} + q_{3l} + q_{3h} + q_{3u}) - c_{n} - c_{nature} = 0\\ \lambda_{l}\delta_{m} - \lambda_{l}k_{3}(q_{3n} + 2q_{3l} + q_{3h} + q_{3u}) - c_{l} - s_{3l} = 0\\ \lambda_{h}\delta_{m} - \lambda_{h}k_{3}(q_{3n} + q_{3l} + 2q_{3h} + q_{3u}) - c_{h} - s_{3h} = 0\\ \lambda_{u}\delta_{m} - \lambda_{u}k_{3}(q_{3n} + q_{3l} + q_{3h} + 2q_{3u}) - c_{u} - s_{3u} = 0 \end{cases}$$
(30)

Proof of the existence of a unique Nash equilibrium can be found in Appendix B. Combining Equations (27) and (30):

$$s_{3l}^{*} = \frac{\left(2c_{l} - J_{31}\lambda_{l} + J_{32} \left(-3\alpha c_{l}J_{33} + \alpha J_{32} + \lambda_{l} \left(3 + \alpha \left(J_{33} + J_{31}J_{33} - 2\right)\right)\right)\right)}{J_{32} \left(3J_{35} + \alpha J_{32}J_{36} + 5\alpha k_{3}J_{32}J_{34}q_{EV2}\right) - 2}$$
(31)

$$s_{3h}^{*} = \frac{\left(2c_{h} - J_{31}\lambda_{h} + J_{32} \left(3c_{h} \left(\lambda_{l}J_{37} + \alpha\lambda_{u}J_{38}\right) + \lambda_{h}J_{311} + J_{32} \alpha \left(J_{38}\lambda_{u}J_{312} - J_{313} + 5k_{3}J_{34}q_{EV2}\right)\right)\right)}{J_{32} \left(3J_{35} + \alpha J_{32}J_{36} + 5\alpha k_{3}J_{32}J_{34}q_{EV2}\right) - 2}$$
(32)

$$s_{3u}^{*} = \frac{\left(2c_{u} - J_{31}\lambda_{u} + J_{32}\left(-3c_{u}\left(\alpha\beta\lambda_{h} - \lambda_{l}J_{37}\right) + \lambda_{u}J_{314} + J_{32}\alpha\left(5k_{3}J_{34}q_{EV2} + J_{45} + J_{316}\right)\right)\right)}{J_{32}\left(3J_{35} + \alpha J_{32}J_{36} + 5\alpha k_{3}J_{32}J_{34}q_{EV2}\right) - 2}$$
(33)

Where
$$J_{31} = (c_n + c_{nature} + \delta_m)$$
, $J_{32} = Ak_3\theta q_{EV2}$, $J_{33} = \beta(\lambda_h - \lambda_u) + \lambda_u$,
 $J_{34} = A(\alpha - 1)\alpha(\beta - 1)\beta\theta\lambda_h\lambda_l\lambda_u$, $J_{35} = (\lambda_l + \alpha(J_3 - \lambda_l))$,
 $J_{36} = 4(\alpha - 1)\beta\lambda_h\lambda_l + 4(\beta - 1)(\alpha\beta\lambda_h + \lambda_l - \alpha\lambda_l)\lambda_u$, $J_{37} = (\alpha - 1)$, $J_{38} = (\beta - 1)$,
 $J_{39} = \beta\lambda_h\lambda_l(\alpha(3 + c_uJ_{38} + \beta) - 4)$,
 $J_{310} = ((4 + \alpha\beta(1 + c_h) + \alpha\beta J_{31}\lambda_h - 4\alpha)\lambda_l - 4c_l\alpha\beta\lambda_h)$,
 $J_{311} = (1 - c_lJ_{37} + 2\alpha\beta + (c_n + c_{nature})\lambda_l - \alpha J_1(\lambda_l + \lambda_uJ_{38}) + \delta_m\lambda_l - \alpha c_uJ_{38})$,
 $J_{312} = ((4\alpha\beta - (1 + c_l)J_{37})\lambda_h + J_{37}(4c_h - J_1\lambda_h)\lambda_l)$, $J_{313} = J_{37}\lambda_h\lambda_l(c_uJ_{38} - 3\beta - 1)$,
 $J_{314} = (1 - c_lJ_{37} - \lambda_lJ_{31}J_{37} + \alpha(2 + \beta(c_h + J_{31}\lambda_h - 2)))$,
 $J_{315} = \beta\lambda_h(\lambda_u(c_lJ_{37} - 3\alpha + 4\alpha\beta - 1) - 4\lambda_lc_uJ_{37})$,
 $J_{316} = \lambda_u\lambda_lJ_{37}(4 + \beta(c_h + J_{31}\lambda_h - 3))$.
 $q_{3n}^* = \frac{(\lambda_u\lambda_hs_{3l}^* + \lambda_u\lambda_ls_{3h}^* + \lambda_h\lambda_ls_{3h}^*}{5k_3\lambda_h\lambda_k}$ (34)

$$q_{3l}^{*} = \frac{\begin{pmatrix} -4\lambda_{u}\lambda_{h}s_{3l}^{*} + \lambda_{u}\lambda_{l}s_{3h}^{*} + \lambda_{h}\lambda_{l}s_{3u}^{*} \\ +\lambda_{h}\lambda_{l}c_{u} - 4\lambda_{u}\lambda_{h}c_{l} + \lambda_{u}\lambda_{l}c_{h} + \lambda_{u}\lambda_{l}\lambda_{h}\left(c_{n} + c_{nature} + \delta_{m}\right) \end{pmatrix}}{5k_{3}\lambda_{h}\lambda_{l}\lambda_{u}}$$
(35)

$$q_{3h}^{*} = \frac{\begin{pmatrix} \lambda_{u}\lambda_{h}s_{3l}^{*} - 4\lambda_{u}\lambda_{l}s_{3h}^{*} + \lambda_{h}\lambda_{l}s_{3u}^{*} \\ +\lambda_{h}\lambda_{l}c_{u} - 4\lambda_{u}\lambda_{l}c_{h} + \lambda_{u}\lambda_{h}c_{l} + \lambda_{u}\lambda_{h}\lambda_{l}\left(c_{n} + c_{nature} + \delta_{m}\right) \end{pmatrix}}{5k_{3}\lambda_{h}\lambda_{l}\lambda_{u}}$$
(36)

$$q_{3u}^{*} = \frac{\begin{pmatrix} \lambda_{u}\lambda_{l}s_{3h}^{*} + \lambda_{u}\lambda_{h}s_{3l}^{*} - 4\lambda_{h}\lambda_{l}s_{3u}^{*} \\ -4\lambda_{h}\lambda_{l}c_{u} + \lambda_{u}\lambda_{h}c_{l} + \lambda_{u}\lambda_{l}c_{h} + \lambda_{u}\lambda_{l}\lambda_{h}\left(c_{n} + c_{nature} + \delta_{m}\right) \end{pmatrix}}{5k_{3}\lambda_{h}\lambda_{l}\lambda_{u}}$$
(37)

In Equations (31)-(33), the decision on optimizing return purchase prices (e.g. lowquality, high-quality and reused batteries) is rather complicated. It is influenced by various factors, but certainly remanufacturing costs play a crucial role. Equations (34)-(37) appear to have the same pattern. In general, the higher the purchase price for that class, the lower the remanufacturing quantity for that specific class. This makes perfect sense. Because remanufacturer's decision on the production quantity must be based on the maximizing profit. With relatively fixed remanufacturing cost, the higher purchasing price, the less profit.

In more detail, from Equations (34)-(37), with a focus on how s_{3h}^* , s_{3l}^* , s_{3u}^* influence the decision variables, we assume that $\lambda_h > \lambda_u > \lambda_l$; $4\lambda_u \lambda_h > \lambda_u \lambda_h > \lambda_h \lambda_l > \lambda_u \lambda_l$; $4\lambda_h \lambda_l > \lambda_u \lambda_h > \lambda_u \lambda_l$; $\lambda_h > \lambda_u \lambda_l > \lambda_u \lambda_l$. This suggests:

• s_{3l}^* has more influence than s_{3h}^* and s_{3u}^* on q_{3n}^* , and it also has more impact on q_{3l}^* .

• s_{3h}^* has more influence on q_{3h}^* and s_{3u}^* has more influence on q_{3u}^* ; With the addition of Equations (34)-(37), we have the following:

$$q_{3l}^{*} + q_{3h}^{*} + q_{3u}^{*} = \frac{\left(\frac{-2\lambda_{u}\lambda_{h}s_{3l}^{*} - 2\lambda_{u}\lambda_{l}s_{3h}^{*} - 2\lambda_{h}\lambda_{l}s_{3u}^{*}}{-2\lambda_{u}\lambda_{l}c_{l} - 2\lambda_{u}\lambda_{l}c_{l} - 2\lambda_{u}\lambda_{l}c_{h} + 3\lambda_{u}\lambda_{l}\lambda_{h}\left(c_{n} + c_{nature} + \delta_{m}\right)\right)}{5k_{3}\lambda_{h}\lambda_{l}\lambda_{u}}$$
(38)

$$q_{3}^{*} = q_{3l}^{*} + q_{3h}^{*} + q_{3u}^{*} + q_{3n}^{*} = \frac{\begin{pmatrix} -\lambda_{u}\lambda_{h}s_{3l}^{*} - \lambda_{u}\lambda_{l}s_{3h}^{*} - \lambda_{h}\lambda_{l}s_{3u}^{*} \\ -\lambda_{h}\lambda_{l}c_{u} - \lambda_{u}\lambda_{h}c_{l} - \lambda_{u}\lambda_{l}c_{h} + \lambda_{u}\lambda_{l}\lambda_{h}\left(-c_{n} - c_{nature} + 4\delta_{m}\right) \end{pmatrix}}{5k_{3}\lambda_{h}\lambda_{l}\lambda_{u}}$$

(39)

Equation (38) presents the total optimal remanufacturing amount, and Equation (39) the total optimal amount of manufacturing and remanufacturing in period 3. Comparing with period 2, there is one more decision variable which is s_u^* . The result suggests the following:

- The higher return purchasing price $(s_{3l}^*, s_{3h}^*, s_{3u}^*)$, the lower remanufacturing quantity, as shown in (38);
- Because of $\lambda_u \lambda_h > \lambda_h \lambda_l > \lambda_u \lambda_l$, s_{3l}^* plays more important roles in both total optimal amount of remanufacturing and total optimal amount of manufacturing and remanufacturing, compared with s_{3h}^* and s_{3u}^* . Moreover, s_{3h}^* impacts less on those two optimal amounts while the impact of s_{3u}^* is between them.

To summarise, the relationship between quantity and returned battery purchase price in period 3 is shown Table 3:

Input variable Decision variable	s_{3h}^{*}	s [*] _{3l}	S_{3u}^{*}
q_{3l}^{*}	+	_	+
q_{3h}^{*}	_	+	+
q_{3u}^{*}	+	+	_

Table 3: Relationship between optimal quantities and purchase price in period 3

q_{3n}^{*}	+	+	+
$q_{3l}^{*} + q_{3h}^{*} + q_{3u}^{*}$	_	_	_
$q_{3l}^* + q_{3h}^* + q_{3u}^* + q_{3n}^*$	_	_	_

4. Numerical study

4.1 Numerical example

In this section, we come up with a numerical example to demonstrate the model. According to International Energy Agency (2017), EV market size is predicted to 18,000,000 in 2020, i.e. $M_{EV} = 18,000,000$. And EV battery price accounts for around 30% of electric car price i.e. $\delta_m = 0.3$.

According to Lambert (2017) and Mark (2014), taking Tesla Model as example, the nature resources for each battery on EV costs £8200 with manufacturing cost £3500. According to Binks (2016) and Will Date (2015), it averagely costs £860 to process a used battery. We assume the low-quality used battery recycling processing cost is £950, high-quality is £850 and reusable battery is £800. To normalize the cost into the same scale, without losing generality, we set $c_{nature} = 0.1$ as benchmarking, other costs other costs against the benchmark $c_1 = 0.1*950/8200 = 0.012$,

 $c_{\rm h}=0.1*850\,/\,8200=0.011\,,\ c_{\rm u}=0.1*800\,/\,8200=0.01\,,$

 $c_n = 0.1 * 3550 / 8200 = 0.043$.

The parameters are shown in Table 4 below:

$M_{EV} = 18,000,000$	<i>A</i> = 4	$\delta_m = 0.3$	$\theta = 0.8$	$\alpha = 0.6$
$\beta = 0.7$	$\lambda_l = 0.5$	$\lambda_h = 0.8$	$\lambda_u = 0.65$	$c_{nature} = 0.1$
$c_n = 0.043$	$c_l = 0.012$	$c_h = 0.011$	$c_{u} = 0.01$	

Table 4: Numerical example parameters

In **Period 1**, applying Equations (1)-(5), the optimal quantity for battery raw materials (which is also the optimal total quantity) is $q_1^* = q_{1n}^* = 1.8 \times 10^7$. The optimal sale price is $p_1^* = 0.221$. The optimal profit that the battery manufacturer will achieve is $\Pi_{1n}^* = 1.49 \times 10^6$.

In **period 2**, we substitute $q_{EV1}^* = 4.72 \times 10^6$ as the initial parameter by applying Equation (1). Through applying Equation (15)-(19), the optimal values are shown below:

$s_{2l}^* = 0.076$ $s_{2h}^* = 0.13$ $q_{2l}^* = 5.58 \times 10^6$	$q_{2h}^* = 5.51 \times 10^6$ $q_{2n}^* = 1.33 \times 10^7$			
Total quantity of battery material	$q_2^* = 2.22 \times 10^7$			
Optimal sale price for EV battery	$p_2^* = 16236$			
Profit for low-quality EV battery remanufacturer	$\Pi_{2l}^* = 64926$			
Profit for high-quality EV battery remanufacturer	$\Pi_{2h}^* = 101560$			
Profit for new EV battery manufacturer	$\Pi_{2n}^* = 740030$			

Table 5: Optimal values in period 2

In **period 3**, through Equation (6), we substitute $q_{EV2}^* = 6.11 \times 10^6$ as the initial EV quantity in this period. The optimal values are derived by using Equations (31)-(37), as in Table 6:

$s_{3h}^* = 0.113$	$s_{3u}^* = 0.102$			
$q_{3h}^* = 7.28 \times 10^6$	$q_{3u}^* = 4.72 \times 10^6$	$q_{3n}^* = 1.00 \times 10^7$		
Entire quantity for the battery material				
Optimal sale price for EV battery		$p_3^* = 14596$		
Profit for low quality EV battery remanufacturer				
Profit for high quality EV battery remanufacturer				
Profit for re-used EV battery remanufacturer				
Profit for new EV battery manufacturer				
	$q_{3h}^* = 7.28 \times 10^6$ ry material attery ttery remanufacturer attery remanufacturer y remanufacturer	$g_{3h}^{*} = 7.28 \times 10^{6}$ $q_{3u}^{*} = 4.72 \times 10^{6}$ ry material $q_{3}^{*} = 2.93 \times 10^{7}$ attery $p_{3}^{*} = 14596$ ttery remanufacturer $\Pi_{3l}^{*} = 87427$ attery remanufacturer $\Pi_{3h}^{*} = 138820$ y remanufacturer $\Pi_{3u}^{*} = 20443$		

Table 6: Optimal values in period 3

4.2 Analysis

In this section, we study the relationship between the parameters (i.e. $\theta, \alpha, \beta, \lambda_l, \lambda_h$, λ_u) and (re)manufacturer's profit in each period. The first column in Figures 2-7 shows profit in period 2; the second column shows profit in period 3; and the third column compares the total profit in periods 2 and 3.

In order to better study the parameters' features, we keep the market size among three periods fixed. The initial input variables are given in Table 7:

Table 7: Value of parameters

$M_{_{EV}} = 18,000,000$	<i>A</i> = 4	$\delta_m = 0.3$	$\theta = 0.8$	$\alpha = 0.6$
$\beta = 0.7$	$\lambda_l = 0.5$	$\lambda_h = 0.8$	$\lambda_u = 0.65$	$c_{nature} = 0.1$
$c_n = 0.043$	$c_l = 0.012$	$c_h = 0.011$	$c_{u} = 0.01$	

1) Analysis of return rate and sorting proportion (θ, α, β)

We set $\theta \in [0.1 \ 0.9]$ while fixing other parameters as shown in Table 7.

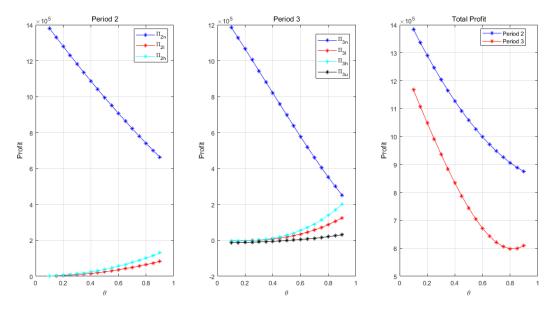
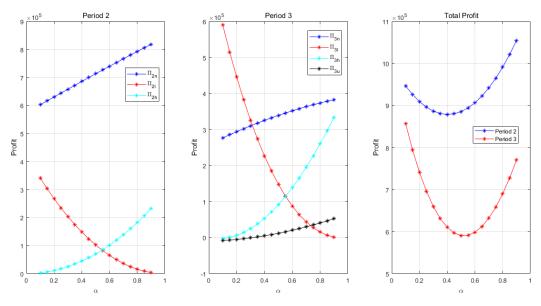


Figure 2: heta vs Profit in Period 2 and Period 3

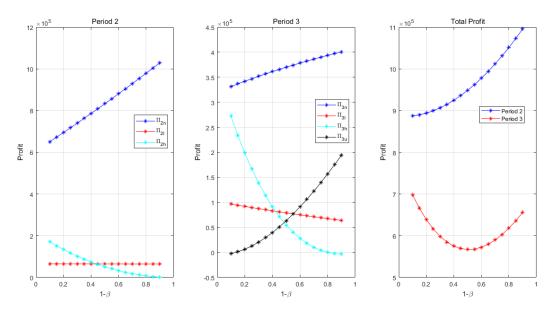
With the return rate θ increasing, the profit for the manufacturer is decreasing while the profit for the remanufacturer is increasing. The profit for manufacturer is always greater than that for the remanufacturer. It can be found that the profit on high quality returns is greater than that for low-quality returns. The profit achieved from reused battery recycling is the lowest. Furthermore, through comparing the varying trend of profits between periods 2 and 3 in Figure 2, for θ , the profits for manufacturer, low quality return remanufacturer, high quality return remanufacturer are more sensitive in period 3. Furthermore, the higher θ , the less total profit in period 2 and 3. But the total profit for period 3 is increasing when $\theta > 0.8$.

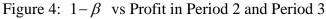
Now we discuss the high-quality return rate α . The results are shown in Figure 3. In general, with increasing α , (which also means a higher low-quality return rate), the profit for high quality remanufacturing increases, which is opposite trend to low quality remanufacturer. In period 3, both manufacturer and 'reused' remanufacturer's profits are insensitive to α although slight increase can be observed. However, low quality remanufacturer's profit is getting less and less, with α =0.9, its profit (Π_l^*) is even close to 0. On the contrary, the profit for high quality remanufacturer, Π_h^* , is increasing. Because low quality remanufacturer cannot make profit if they don't have returned batteries when α close to 1, while in this case, high quality remanufacturer will have more returns to make profit. Base on this, total profit is decreased when α is low but it increases when α is high.





The reusable battery return rate, $(1-\beta)$, has limited impact on low quality return's remanufacturer (Π_l^*) . In period 3, the more the reusable battery, the higher the profit for manufacturer (Π_n^*) and for the reusable battery remanufacturer (Π_u^*) as well, but less profit for high-quality returned battery remanufacturer (Π_h^*) . Furthermore, higher reusable battery return will lead to high total profit in period 2. But in period 3, with increasing of $(1-\beta)$, the total profit in period 3 shows a tendency to decrease first and then increase afterwards.





2) Analysis of remanufacturing rate $(\lambda_l, \lambda_h, \lambda_u)$

As can be seen in Figure 5, with the increasing of low quality returned battery remanufacturing rate λ_l , Π_{2h}^* and Π_{3u}^* is constant. Meanwhile, Π_{2n}^* , Π_{2l}^* , Π_{3n}^* and Π_{3l}^* are increasing slowly. The total profit in both period 2 and period 3 are keep increasing.

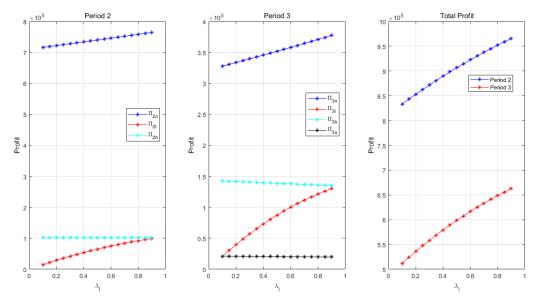


Figure 5: λ_l vs Profit in Period 2 and Period 3

Considering λ_h , high quality returned battery remanufacturing rate, as shown in Figure 6, when it increases, profits are increasing except Π_{2l}^* (Π_{2l}^* keeps constant as there is no relationship between them). However, in period 3, all profits are decreased (but a tiny increase in low λ_h). This results from the increasing returned batteries' purchase price. Combining these two, the total profit in period 2 is rising while the profit in period 3 is increasing first and keep dropping down when $\lambda_h > 0.4$.

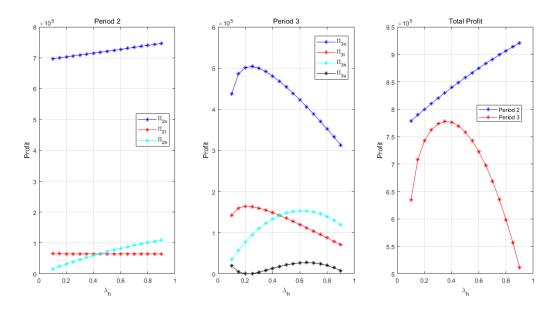


Figure 6: λ_h vs Profit in Period 2 and Period 3

The reused battery remanufacturing rate λ_u only works in period 3. As we can find in Figure 7, with the condition of low λ_u , profits for manufacturer and remanufacturer are even negative. Meanwhile, the higher the remanufacturing rate for reused batteries, the higher the profit to both manufacturer and remanufacturer.

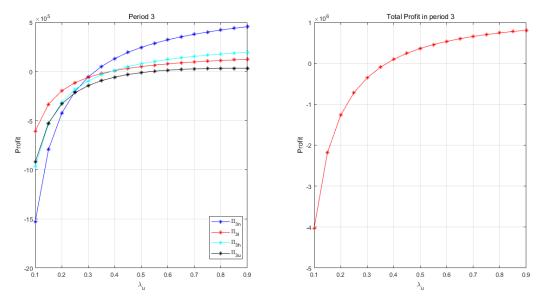


Figure 7: λ_u vs Profit in Period 3

In summary, different parameters have different sensitivities and variation tendencies for each (re)manufacturer's profit in different periods.

- The manufacturer normally gets more profit than the remanufacturer (except the case about low high-quality return rate in period 3).
- All parameters are more sensitive in period 3 than period 2.
- With the increase of θ , the remanufacturer's profit increases.
- Increasing α will result in more profit for the manufacturer, high-quality remanufacturer and re-usable remanufacturer, but less profit for the low-

quality returns remanufacturer.

Recycling rates (λ_l, λ_h, λ_u) have less sensitivity than the sorting rate (θ, α, (1-β)). Except for λ_h in period 3, profits for each participant in this model show a small increase or remain the same.

One of the most significant findings, from observing the above figures is that the total profit in period 3 is always smaller than that in period 2. The reason is that, because of the increase in returned batteries over these periods, the profit for the battery manufacturer (which occupies the majority of total profit) is decreasing and this has a direct impact on total profit.

Therefore, to maintain the profit balance between manufacturer and remanufacturer, and to promote battery recycling, the government should pay close attention to policy and incentive mechanisms to enhance the total battery return rate (θ) and the high-quality return rate (β). Some technologies also need to be developed to improve recycling efficiency, which will improve the total profit for the whole supply chain.

5. Conclusion

In this paper, we develop a three-period EV battery recycling and reuse model. We determine the unique Nash equilibrium among new EV battery manufacturer, low quality battery remanufacturer and high-quality battery remanufacturer as well as re-used battery remanufacturer. The purpose is to maximize individual's profit through optimal purchase price and production quantity.

We also analyze the influencing factors for the optimal (re)manufacturing quantity. The result of the analyses suggests that: (a) among the variables that have an impact on the (re-)manufacturing decision, the purchase price of returned batteries plays a critical role. Particularly, the price of low-quality returns has more influence than that of high-quality returns. (b) Interestingly, a higher purchasing price for re-usable returns does not necessarily lead to higher return rate of reusable returns. (c) The manufacturer's profit is always higher than remanufacturer's. This suggests the need to design incentives to promote the remanufacturing sector. (d) Although it is appreciated that maximising the utilisation of a battery over its life-cycle would benefit the environment, the economic benefit needs further investigation.

Implication of the research results to practitioners have threefold: (1) Special attention needs to be paid on low-quality returns as it has more significant impact on total profit; (2) Although high-quality return is encouraged, monetary incentive to obtain high-quality returns may not necessarily work; (3) To sustain recycling business, government support is vitally important to keep the business going.

This paper develops the model based on the reality that most manufacturers and remanufacturers make decisions based on their own interests, the profit. There is a lack of coordination among the participants to achieve the maximized total profit for the EV battery CLSC. This leads to our suggestion for future research. In addition, our model suggests that reusing returned batteries does not bring economic benefits. How to realize the benefits for the environment and the economy at same time needs further investigation.

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Appendix A

Proof of exitance and uniqueness of Nash equilibrium in period 2

Combining equations (11) and (14), we have simultaneous equations

$$\begin{cases} -2k_{2}q_{2n} - k_{2}q_{2l} - k_{2}q_{2h} = c_{n} + c_{nature} - \delta_{m} \\ -\lambda_{l}k_{2}q_{2n} - 2\lambda_{l}k_{2}q_{2l} - \lambda_{l}k_{2}q_{2h} - s_{2l} = c_{l} - \lambda_{l}\delta_{m} \\ -\lambda_{h}k_{2}q_{2n} - \lambda_{h}k_{2}q_{2l} - 2\lambda_{h}k_{2}q_{2h} - s_{2h} = c_{h} - \lambda_{h}\delta_{m} \\ q_{2h} + A\theta q_{EV1}\alpha\beta s_{2h} = A\theta q_{EV1}\alpha\beta \\ q_{2l} + A\theta q_{EV1}(1-\alpha)s_{2l} = A\theta q_{EV1}(1-\alpha) \end{cases}$$
(A1)

The simultaneous equations above can be rewritten as

AX = B

Where

$$A = \begin{bmatrix} -2k_2 & -k_2 & -k_2 & 0 & 0 \\ -\lambda_l k_2 & -2\lambda_l k_2 & -\lambda_l k_2 & -1 & 0 \\ -\lambda_h k_2 & -\lambda_h k_2 & -2\lambda_h k_2 & 0 & -1 \\ 0 & 0 & 1 & 0 & A\theta q_{EV1} \alpha\beta \\ 0 & 1 & 0 & A\theta q_{EV1} (1-\alpha) & 0 \end{bmatrix}$$
(A3)

$$X = \begin{bmatrix} q_{2n} & q_{2l} & q_{2h} & s_{2l} & s_{2h} \end{bmatrix}'$$
 (A4)

$$B = \begin{bmatrix} c_n + c_{nature} - \delta_m \\ c_l - \lambda_l \delta_m \\ c_h - \lambda_h \delta_m \\ A \theta q_{EV1} \alpha \beta \\ A \theta q_{EV1} (1 - \alpha) \end{bmatrix}$$
(A5)

Based on Linear algebra, it can be found that the rank for A and B has relationship r(A) = r(B) = 5 (A6)

So, there is a solution and the only solution for simultaneous equations. Hence, period 2 has an exitance and uniqueness of Nash equilibrium.

End.

Appendix B

Proof of exitance and uniqueness of Nash equilibrium in period 3 Combining equations (27) and (30), we have

AX = B

$$\begin{cases} -2k_{3}q_{3n} - k_{3}q_{3l} - k_{3}q_{3h} - k_{3}q_{3u} = c_{n} + c_{nature} - \delta_{m} \\ -\lambda_{l}k_{3}q_{3n} - 2\lambda_{l}k_{3}q_{3l} - \lambda_{l}k_{3}q_{3h} - \lambda_{l}k_{3}q_{3u} - s_{3l} = c_{l} - \lambda_{l}\delta_{m} \\ -\lambda_{h}k_{3}q_{3n} - \lambda_{h}k_{3}q_{3l} - 2\lambda_{h}k_{3}q_{3h} - \lambda_{h}k_{3}q_{3u} - s_{3h} = c_{h} - \lambda_{h}\delta_{m} \\ -\lambda_{u}k_{3}q_{3n} - \lambda_{u}k_{3}q_{3l} - \lambda_{u}k_{3}q_{3h} - 2\lambda_{u}k_{3}q_{3u} - s_{3u} = c_{u} - \lambda_{u}\delta_{m} \\ q_{3l} + A\theta q_{EV2}(1-\alpha)s_{3l} = A\theta q_{EV2}(1-\alpha) \\ q_{3h} + A\theta q_{EV2}\alpha\beta s_{3h} = A\theta q_{EV2}\alpha\beta \\ q_{3u} + A\theta q_{EV2}\alpha(1-\beta)s_{3u} = A\theta q_{EV2}\alpha(1-\beta) \end{cases}$$
(B1)

The simultaneous equations above can be rewritten as

Where

$$A = \begin{bmatrix} -2k_3 & -k_3 & -k_3 & 0 & 0 & 0 \\ -\lambda_l k_3 - 2\lambda_l k_3 & -\lambda_l k_3 & -\lambda_l k_3 & -1 & 0 & 0 \\ -\lambda_h k_3 - \lambda_h k_3 - 2\lambda_h k_3 & -\lambda_h k_3 & 0 & -1 & 0 \\ -\lambda_u k_3 - \lambda_u k_3 & -\lambda_u k_3 - 2\lambda_u k_3 & 0 & 0 & -1 \\ 0 & 1 & 0 & 0 & A\theta q_{EV2}(1-\alpha) & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & A\theta q_{EV2}\alpha\beta & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & A\theta q_{EV2}\alpha(1-\beta) \end{bmatrix}$$
(B3)

$$X = \begin{bmatrix} q_{3n} & q_{3l} & q_{3h} & q_{3u} & s_{3l} & s_{3h} & s_{3u} \end{bmatrix}'$$
 (B4)

$$B = \begin{bmatrix} c_n + c_{nature} - \delta_m \\ c_l - \lambda_l \delta_m \\ c_h - \lambda_h \delta_m \\ c_u - \lambda_u \delta_m \\ A \theta q_{EV2} (1 - \alpha) \\ A \theta q_{EV2} \alpha \beta \\ A \theta q_{EV2} \alpha (1 - \beta) \end{bmatrix}$$
(B5)

Based on Linear algebra, it can be found that the rank for A and B has relationship r(A) = r(B) = 7 (B6)

So, there is a solution and the only solution for simultaneous equations. Hence, period 3 has an exitance and uniqueness of Nash equilibrium.

End.