

# Optimization and Optimal Control

# Series on Computers and Operations Research

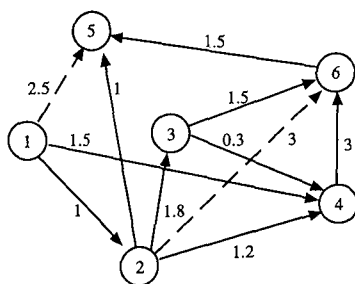
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*eds. P. M. Pardalos, I. Tseveendorj and R. Enkhbat*

# Optimization and Optimal Control



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*In memory of a dear teacher and friend*  
*Oleg V. Vasiliev*

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## Preface

Numerous mathematical models in many diverse fields of science and engineering lead to the formulation of optimization or optimal control problems. In optimization we often solve problems in finite dimensional spaces. On the other hand, in optimal control problems we often deal with infinite dimensional spaces where the solution is described by a curve instead of a finite vector. Optimization and optimal control has flourished in the last half century. In this book we cover a small subset of recent important topics in optimization and optimal control with emphasis on recent theoretical developments and applications.

An international conference on *Optimization and Optimal Control* was held during August 13-17, 2002 at Ulaanbaatar, Mongolia. The conference was endorsed by France Télécom R&D, the Mongolian Mathematical Society, the Mongolian Academy of Sciences, the Mongolian State University, DAAD and the Center for Applied Optimization at the University of Florida. The conference provided a forum for researchers working on different aspects of optimization and optimal control to present their recent discoveries, and to initiate scientific collaborations. This volume contains a selective collection of carefully refereed papers based on talks presented at this conference. The two themes of *optimization* and *optimal control* pervade this book.

The target audience of the book includes graduate students in engineering and operations research, academic researchers, as well as practitioners, who use optimization and optimal control methods for their specific needs and applications.

We would like to take this opportunity to thank the sponsors, the authors of the papers, the anonymous referees, and World Scientific, for making the publication of this book possible.

P.M. Pardalos, I. Tseveendorj, and R. Enkhbat  
June 2003

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## Contents

A. Antipin, <b>Extragradient Approach to the Solution of Two Person Non-Zero Sum Games</b>	1
N. Bouhmala, T. Natvig, and M. Jakobsen, <b>A Multilevel Construction Algorithm for the Traveling Salesman Problem</b>	29
M. Bouhtou, M. Diallo, and L. Wynter, <b>Fair Network Resource Allocation and Link Pricing: A Numerical Study</b>	37
S. Budnyam, <b>Nonlinear Phenomena in Economics</b>	59
V.P. Bulatov and D. Ganhyuag, <b>Necessary Optimality Conditions and Methods of Global Optimization</b>	69
R. Enkhbat, <b>On Some Theory, Methods and Algorithms for Concave Programming</b>	79
D. Fortin and I. Tseveendorj, <b>Maximum Clique Regularizations</b>	103
M. Kamada, T. Kawahito, and R. Enkhbat, <b>Optimal Synthesis of Handwritten Letters from Their Characteristic Points</b>	121
D.W. Katzner, <b>The Role of Optimization in Economics</b>	141
O. Khamisov, <b>A Global Optimization Approach to Solving Equilibrium Programming Problems</b>	155
L. Liberti, <b>Comparison of Convex Relaxations for Monomials of Odd Degree</b>	165
P. Mbunga, <b>Structural Stability of Vector Optimization Problems</b>	175
H. Nakayama, M. Arakawa, and K. Washino, <b>Optimization for Black-Box Objective Functions</b>	185
T.Q. Nguyen, M. Bouhtou, and J.-L. Lutton, <b>D.C. Approach to Bilevel Bilinear Programming Problem: Application in Telecommunication Pricing</b>	211

S. Saito and H. Ishii, <b>Fuzzy Optimization Problems Concerning Oil Equations of <math>L</math>-Fuzzy Numbers</b>	233
S. Saito, <b>A Genetic Algorithm by Use of Virus Evolutionary Theory for Combinatorial Problems</b>	251
V.A. Srochko, <b>New Variants of Gradient Type Methods in Optimal Control Problems</b>	269
U. Badam, <b>A Simple Model of Improving Survival in Economical Systems</b>	287
O.V. Vasiliev, <b>Controlled Systems with Distributed Parameters: Optimality Conditions and Optimization Methods in Class of Smooth Restricted Controls</b>	297
G. Wanka, R.I. Boş, and E. Vargyas, <b>Duality for the Multiobjective Location Model Involving Sets as Existing Facilities</b>	307
V.I. Zorkaltsev, <b>The Points of a Linear Manifold Nearest to a Given Vector</b>	335
A. Strekalovsky, <b>Some Remarks on D.C. Programming</b>	347