

Optimizing feed force for turned parts through the Taguchi technique

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Abstract. The objective of the paper is to obtain an optimal setting of turning process parameters (cutting speed, feed rate and depth of cut) resulting in an optimal value of the feed force when machining EN24 steel with TiC-coated tungsten-carbide inserts. The effects of the selected turning process parameters on feed force and the subsequent optimal settings of the parameters have been accomplished using Taguchi's parameter design approach. The results indicate that the selected process parameters significantly affect the selected machining characteristics. The results are confirmed by further experiments.

Keywords. Cutting parameters; turning process; feed force; Taguchi technique; EN24 steel; coated carbide inserts.

1. Introduction

To provide satisfaction to customers and to deliver in a competitive market, a producer has to acknowledge that considerable advantage can be obtained by controlling quality at the design stage itself instead of at the manufacturing stage or by the inspection of finished products. This is basic idea of off-line quality control; Taguchi's method is one of the most comprehensive and effective systems of off-line quality control.

Taguchi has built upon W E Deming's observation that 85% of poor quality is attributable to the manufacturing process and only 15% to the worker (Roy 1990). Thus, his attempt has been to develop robust manufacturing systems that are insensitive to daily and seasonal variations of environment, machine wear etc.

Taguchi recommends a three-stage process to achieve desirable product quality by design – system design, parameter design and tolerance design. While system design helps to identify working levels of the design parameters, parameter design seeks to determine parameter levels that provide the best performance of the product or process

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under study. The optimum condition is selected so that the influence of uncontrollable factors (noise factors) causes minimum variation to system performance. Orthogonal arrays, variance and signal to noise analysis are the essential tools of parameter design. Tolerance design is a step to fine-tune the results of parameter design (Ross 1996).

EN24 is a medium-carbon low-alloy steel and finds its typical applications in the manufacturing of automobile and machine tool parts. Properties of EN24 steel, like low specific heat, and tendency to strain-harden and diffuse between tool and work material, give rise to certain problems in its machining such as large cutting forces, high cutting-tool temperatures, poor surface finish and built-up-edge formation. This material is thus difficult to machine (Mottram & WoolMan 1966; Nakayama & Shaw 1967; Komanduri 1982; Sarmah 1988). Nakayama & Shaw (1967) investigated the machining of EN24 steel with HSS tools and carbide tools. They found large forces during machining which may result in tool fracture and high cutting temperatures. Lo & Chen (1977) studied tool life in DC hot machining of EN24 steel using carbide tools in the speed range of 35–230 m/min. They used response surface methodology for design of experiments. Kalnth *et al* (1978) applied electric resistance heating technique to get optimal results for reduction in cutting forces. They recommended an optimum heating current of 200 amperes for machining EN24 steel at 80 m/min. Sarmah (1988) carried out some investigations into performance of CVD-coated indexable carbide inserts in machining of austenitic 18-8 stainless steel, incoloy 800 and EN24 alloy steel. The quality of surface finish was found to improve with reduction of cutting force. Abdulla (1994) studied the performance of six coated-carbide inserts in machining of EN24 steel. He used response surface methodology for experimentation. Owing to its wide application EN24 steel has been selected as the work material in this case study. Recently developed tool materials such as coated carbides have improved productivity levels of difficult-to-machine materials.

The literature survey reveals that the machining of difficult-to-machine materials like EN24 is relatively a less researched area. There is also a complete dearth of interaction studies. The objective of this case study is to obtain optimal settings of turning process parameters – cutting speed, feed rate and depth of cut, to yield optimal feed force while machining EN24 steel with TiC-coated carbide tools. Taguchi's parameter design approach has been used to accomplish this objective.

2. Turning process parameters

In order to identify the process parameters affecting the selected machining quality characteristic of turned parts, an Ishikawa cause-effect diagram was constructed as shown in figure 1. The identified process parameters are the cutting tool parameters – tool geometry, tool material, physical and mechanical properties, the cutting parameters – cutting speed, feed rate, depth of cut, work piece-related parameters – hot-worked, cold-worked, difficult-to-machine, and environment parameters – dry cutting, wet cutting.

The following process parameters were thus selected for the present work: Cutting speed – (A), feed rate – (B), depth of cut – (C), tool material – Widadur TG inserts, work material – EN24 steel, and environment – dry cutting.

The selection of parameters of interest was based on some preliminary experiments and earlier studies by the authors (Singh & Kumar 2000, 2003–2005). The following parameters were kept fixed during the entire experimentation:

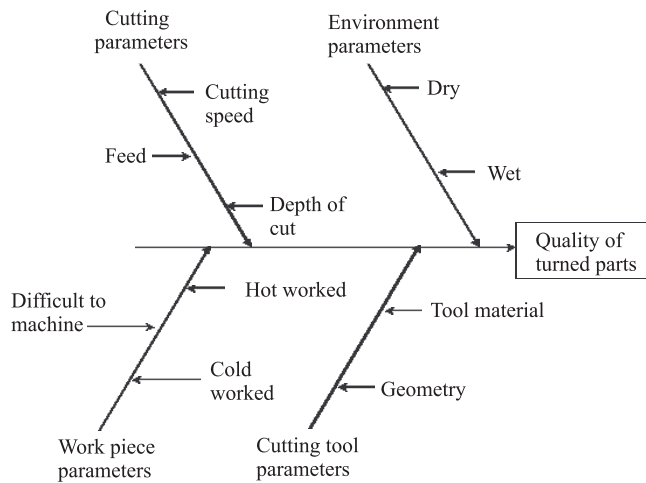


Figure 1. Ishikawa cause-effect diagram of a turning process.

- (a) Work material : EN24 steel
- (b) Cutting tool material : Widadur TG
- (c) Insert geometry : SPUN 120308 (ISO designation)
- (d) Tool holder : CSBPR 2525 H 12 (ISO designation)
- (e) Cutting conditions : Dry

3. Selection of orthogonal array (OA)

The nonlinear relationship among the process parameters, if it exists, can only be revealed if more than two levels of the parameters are considered (Byrne & Taguchi 1987). Thus each selected parameter was analysed at three levels. The process parameters and their values at three levels are given in table 1.

It was also decided to study the two-factor interaction effects of process parameters on feed force while turning EN24 steel with carbide inserts. Interactions considered were between cutting speed and feed rate ($A \times B$), feed rate and depth of cut ($B \times C$), and cutting speed and depth of cut ($A \times C$).

The total degrees of freedom (DOF) for three parameters, each at three levels, and the three two-factor interactions are eighteen (Ross 1996). So, a three level OA with at least eighteen DOF was to be selected. The L_{27} OA (DOF = 26) was thus selected for the present case study.

Table 1. Process parameters with their values at 3 levels.

Parameters designation	Process parameters	Level 1	Level 2	Level 3
A	Cutting speed (m/min)	190	250	310
B	Feed rate (mm/rev)	0.14	0.16	0.18
C	Depth of cut (mm)	0.70	0.85	1.00

Table 2. $L_{27}(3^{13})$ Orthogonal array with process parameters and interactions assigned to columns.

Trial	Column												
	A 1	B 2	A × B 3	A × B 4	C 5	A × C 6	A × C 7	B × C 8	– 9	– 10	B × C 11	– 12	– 13
1	1	1	1	1	1	1	1	1	1	1	1	1	1
2	1	1	1	1	2	2	2	2	2	2	2	2	2
3	1	1	1	1	3	3	3	3	3	3	3	3	3
4	1	2	2	2	1	1	1	2	2	2	3	3	3
5	1	2	2	2	2	2	2	3	3	3	1	1	1
6	1	2	2	2	3	3	3	1	1	1	2	2	2
7	1	3	3	3	1	1	1	3	3	3	2	2	2
8	1	3	3	3	2	2	2	1	1	1	3	3	3
9	1	3	3	3	3	3	3	2	2	2	1	1	1
10	2	1	2	3	1	2	3	1	2	3	1	2	3
11	2	1	2	3	2	3	1	2	3	1	2	3	1
12	2	1	2	3	3	1	2	3	1	2	3	1	2
13	2	2	3	1	1	2	3	2	3	1	3	1	2
14	2	2	3	1	2	3	1	3	1	2	1	2	3
15	2	2	3	1	3	1	2	1	2	3	2	3	1
16	2	3	1	2	1	2	3	3	1	2	2	3	1
17	2	3	1	2	2	3	1	1	2	3	3	1	2
18	2	3	1	2	3	1	2	2	3	1	1	2	3
19	3	1	3	2	1	3	2	1	3	2	1	3	2
20	3	1	3	2	2	1	3	2	1	3	2	1	3
21	3	1	3	2	3	2	1	3	2	1	3	2	1
22	3	2	1	3	1	3	2	2	1	3	3	2	1
23	3	2	1	3	2	1	3	3	2	1	1	3	2
24	3	2	1	3	3	2	1	1	3	2	2	1	3
25	3	3	2	1	1	3	2	3	2	1	2	1	3
26	3	3	2	1	2	1	3	1	3	2	3	2	1
27	3	3	2	1	3	2	1	2	1	3	1	3	2

The L_{27} OA is given in table 2. This array specifies twenty-seven experimental runs and has thirteen columns. Using a linear graph for L_{27} OA (Peace 1993), the interacting columns were identified and parameters were assigned to specific columns accordingly. The assignment of process parameters and interactions to columns is also done in table 2.

4. Experiment, analysis and discussion

EN24 steel rods of 90 mm diameter and 500 mm length were turned on an H-22 centre lathe (HMT). Titanium carbide-coated tungsten carbide inserts (Widia India Limited) were used to machine the work material (EN24 steel) of mean hardness 220 BHN. Three specimens were turned for each trial condition given in table 2. Using the randomization technique, eighty-one specimens were thus turned and the feed force was measured with a three-dimensional turning dynamometer, with four extended half rings machined from a single block of CI. The tangential force places the lower elements of half rings under compression and the upper ones under tension. The feed force subjects all elements to shearing while the radial force subjects all the half rings to compression. The dynamometer was calibrated on a vertical milling machine by using a proving ring. The calibration curve is shown in figure 2.

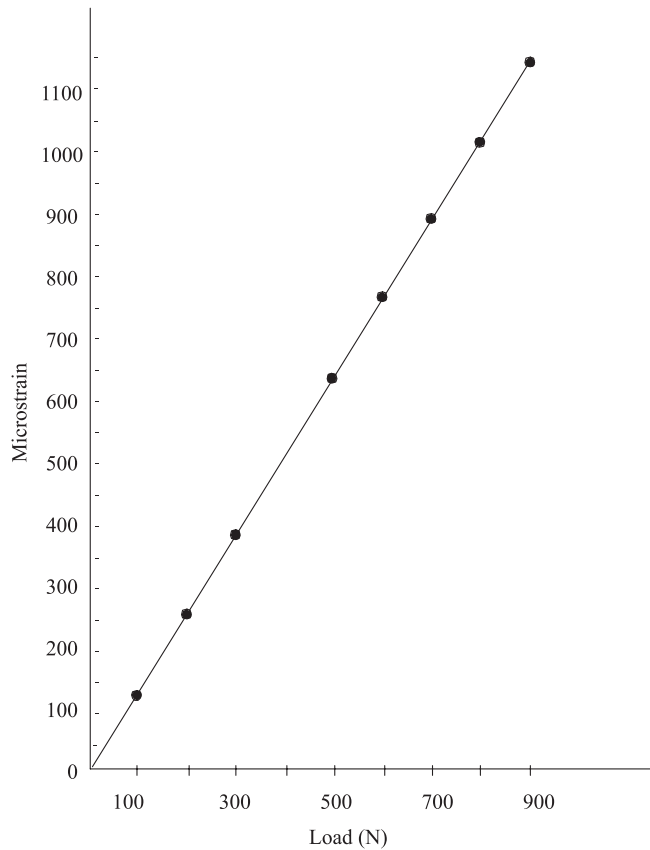


Figure 2. Calibration curve for tool dynamometer – feed force

Experimental data for the feed force have been reported in table 3. Feed force being a ‘lower the better’ type of machining quality characteristic, the S/N ratio for this type of response was used and is given below (Roy 1990).

$$S/N \text{ ratio (dB)} = -10 \log \left[\frac{1}{n} (y_1^2 + y_2^2 + \dots + y_n^2) \right], \quad (1)$$

where y_1, y_2, \dots, y_n are the responses of the machining characteristic, the feed force, for a trial condition repeated n times. The S/N ratios were computed using (1) for each of the twenty-seven trials and the values are reported in table 3 along with the raw data for feed force.

The mean response refers to the average value of the performance characteristic for each parameter at different levels. The average values of feed force for each parameter at levels 1, 2 and 3 are calculated and given in table 4. The main effects, i.e. the effects of process parameters on the response characteristic when the process parameters change from one level to another are also given in table 4 and are plotted in figures 3a–c. The average values of S/N ratios of various parameters at different levels are reported in table 5 and plotted in figures 3a–c along with the raw data. The interaction graphs, both for raw data and S/N data, are plotted in figures 4a–c.

Table 3. Experimental data of feed force.

Trial No.	Feed force (N)			<i>S/N</i> ratio (dB)
	R1	R2	R3	
1	210	190	190	-45.88
2	205	185	210	-46.03
3	240	215	215	-46.99
4	200	205	205	-46.16
5	230	250	215	-47.31
6	250	240	250	-47.84
7	225	200	220	-46.66
8	245	255	235	-47.79
9	275	250	235	-48.09
10	185	175	190	-45.27
11	240	190	205	-46.56
12	240	190	175	-46.17
13	175	195	190	-45.43
14	250	210	230	-47.26
15	230	230	190	-46.75
16	190	210	215	-46.25
17	280	240	255	-48.26
18	240	220	255	-47.56
19	185	170	175	-44.95
20	190	190	200	-45.73
21	250	260	230	-47.85
22	195	175	180	-45.27
23	215	220	210	-46.65
24	235	250	240	-47.67
25	200	185	190	-45.66
26	230	235	235	-47.36
27	290	255	250	-48.48
Total	6100	5790	5790	

$$\bar{T}_{FF} = \text{overall mean of feed force} = 218.27 \text{ N}$$

4.1 Analysis of results

It is evident from the figure 3 that feed force is minimum at the first level of feed (B) and the first level of depth of cut (C). The effect of cutting speed is not very clearly defined in figure 3a.

The interaction analysis in figure 4 clearly shows that B_1C_1 and A_3C_1 are the optimal combinations. Thus, the third level of cutting speed, first level of feed and first level of depth of cut represent the optimal levels of various turning process parameters to yield an optimal value of the feed force.

In order to quantify the influence of process parameters and interactions on the selected machining characteristic, the feed force, analysis of variance (ANOVA) was performed. The pooled ANOVA of the raw data (feed force) is given in table 6. The *S/N* pooled ANOVA is given in table 7.

It is evident from the pooled ANOVA tables 6 and 7 for raw data and *S/N* data that feed rate, depth of cut and interaction between cutting speed and depth of cut ($A \times C$), are all significant at 95% confidence level in both ANOVAs, and thus affect the average value of feed force as

Table 4. Average values and main effects (raw data: feed force).

Process parameter designation	Average values of feed force (N)			Main effects (N)	
	L1	L2	L3	L2-L1	L3-L2
A	223.9	214.6	216.3	-9.3	1.7
B	203.7	217.2	233.9	13.5	16.7
C	193.5	224.3	237	30.8	12.7
A × B	216.9	220.5	217.4	3.6	-3.1
B × C	221.6	214.3	219	-7.3	4.7
A × C	221.2	216.1	217.5	-5.1	1.4

well as its variation. Cutting speed (A) and the interaction between feed rate and depth of cut (B × C) are significant at 95% confidence level in S/N pooled ANOVA only, thus affecting the only variation in feed force. The ANOVAs also suggest that the interaction between cutting speed and feed rate (A × B) is insignificant and does not affect anything (Ross 1996).

The percent contributions of parameters as quantified under column P of tables 6 and 7 reveal that the influence of depth of cut in affecting feed force is significantly larger than the

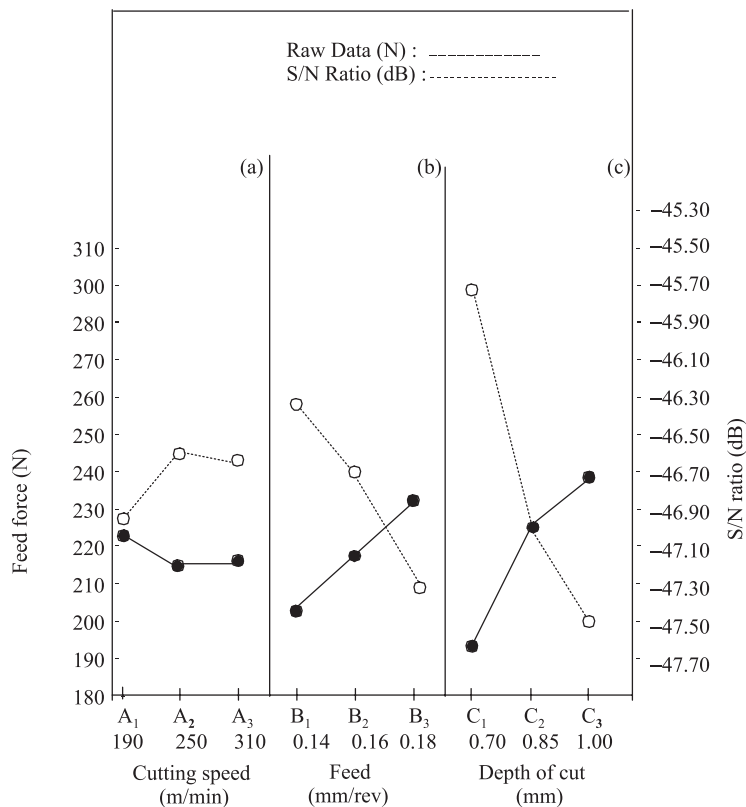


Figure 3. Effects of process parameters on feed force (raw data) and S/N ratio. (a) Cutting speed, (b) feed, (c) depth of cut.

Table 5. *S/N* average values and main effects (raw data: feed force).

Process parameter designation	<i>S/N</i> average values (dB)			Main effects (dB)	
	L1	L2	L3	L2-L1	L3-L2
A	-46.97	-46.61	-46.62	0.36	-0.01
B	-46.16	-46.71	-47.35	-0.55	-0.64
C	-45.73	-46.99	-47.49	-1.26	-0.5
A × B	-46.69	-46.82	-46.70	-0.13	0.12
B × C	-46.85	-46.58	-46.78	0.27	-0.2
A × C	-46.87	-46.64	-46.69	0.23	-0.05

feed rate, cutting speed and interaction between cutting speed and depth of cut. It is also clear from table 6 that the relative strength of the interaction between cutting speed and depth of cut ($A \times C$: 10.23%) is significant as compared with the relative strength of feed rate (B: 18.75%)

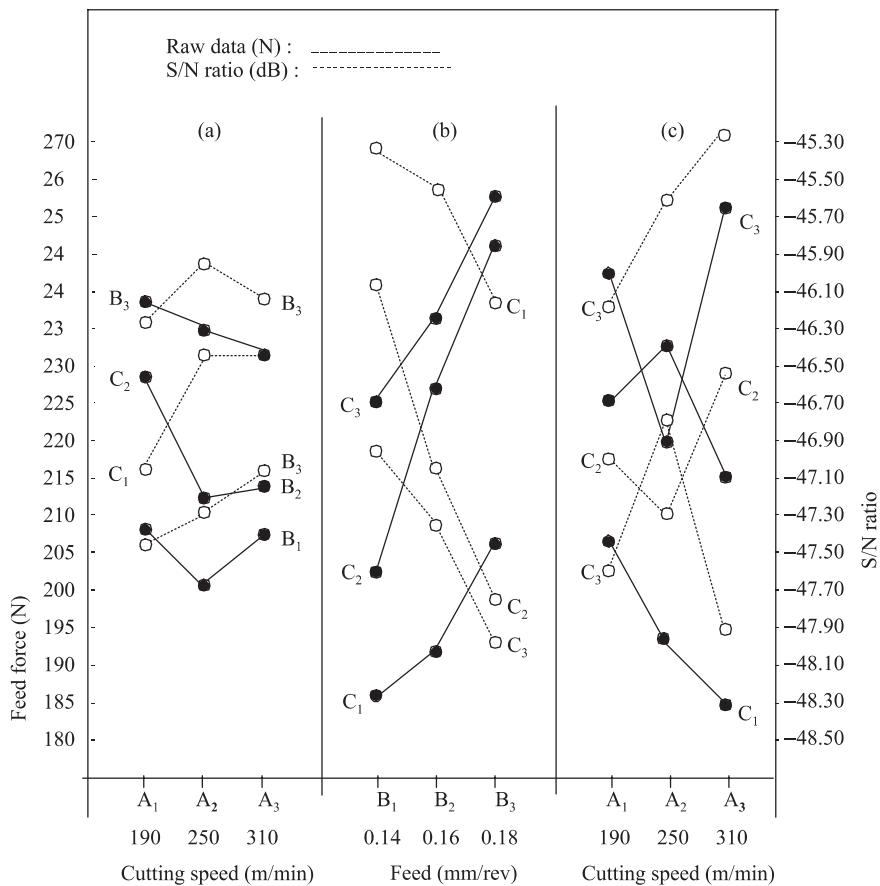


Figure 4. Effects of process parameters interactions on feed force (raw data) and *S/N* ratio. (a) and (c) Cutting speed, (b) feed.

Table 6. Pooled ANOVA (raw data: feed force).

Source	SS	DOF	V	F ratio	SS'	P
A	(1315.4)	(2)	–	Pooled	–	–
B	12345	2	6172.5	26.39*	11916.948	18.75
C	27019	2	13509.5	57.77*	26590.948	41.84
A × B	(647.5)	(4)	–	Pooled	–	–
B × C	(1604.9)	(4)	–	Pooled	–	–
A × C	7356.6	4	1839.15	7.86*	6500.4968	10.23
T	63558	80			63558	100.00
e (pooled)	(16837.4)	(72)	233.85278		18549.606	29.18

SS = sum of squares, DOF = degrees of freedom, V = variance, T = total; SS' = pure sum of squares, P = percent contribution, e = error, Tabulated F-ratio at 95% confidence level: $F_{0.05;2;72} = 3.13$; $F_{0.05;4;72} = 2.50$

*Significant at 95% confidence level

and depth of cut (C: 41.84%). Thus, to estimate mean value, the interaction between cutting speed and depth of cut (A × C) is also considered. The parameters and their selected levels are given in table 8.

5. Estimation of optimum value of feed force

To obtain the best estimate of a mean value when there is an interaction, trials that include the specific treatment condition (here, A_3C_1) should be averaged. By considering the interaction as one item that has good additivity to other non-interacting items (here, B_1), an estimate of mean value may be made (Ross 1996).

From table 2, it is clear that the A_3C_1 combination is included in the trials 19, 22 and 25. These trials are thus averaged to get, $A_3C_1 = 183.89$ N (table 3).

The estimated mean of the response characteristic can be computed as (Ross 1996):

$$\mu_{FF} = \overline{A_3C_1} + \overline{B_1} - \overline{T_{FF}} \tag{2}$$

Table 7. S/N pooled ANOVA (raw data: feed force).

Source	SS	DOF	V	F ratio	SS'	P
A	0.764	2	0.382	8.90*	0.70775	2.63
B	6.337	2	3.1685	73.83*	6.28075	23.33
C	14.904	2	7.452	173.64*	14.84775	55.15
A × B	(0.290)	(4)		Pooled	–	–
B × C	0.712	4	0.178	4.15*	0.5995	2.23
A × C	3.692	4	0.923	21.51*	3.5795	13.29
T	26.924	26			26.924	100.00
e (pooled)	(0.515)	(12)	7.0429166		0.90875	3.37

Tabulated F-ratio at 95% confidence level: $F_{0.05;2;12} = 3.89$; $F_{0.05;4;12} = 3.26$

*Significant at 95% confidence level.

Table 8. Parameters and their selected levels (for optimal feed force).

Parameter designation	Process parameters	Optimal levels
A	Cutting speed	3 (310 m/min)
B	Feed rate	1 (0.14 mm/rev)
C	Depth of cut	1 (0.70 mm)

where $\overline{T_{FF}}$ = overall mean of feed force = 218.27 N (table 3) and \overline{B}_1 = average value of feed force at the first level of feed = 203.7 N (table 4).

Hence $\mu_{FF} = 169.32$ N.

A confidence interval for the predicted mean on a confirmation run can be calculated using the following equation (Ross 1996):

$$CI = \left(F_{\alpha; (1, f_e)} V_e \left[\frac{1}{n_{\text{eff}}} + \frac{1}{R} \right] \right)^{1/2}, \quad (3)$$

where $F_{\alpha; (1, f_e)}$ = F ratio required for α , α = risk, f_e = error DOF, V_e = error variance, n_{eff} = effective number of replications = $N / \{1 + [\text{Total DOF associated in the estimate of mean}]\}$,

R = number of repetitions for confirmation experiment, N = total number of experiments.

Using the values $V_e = 233.85278$ and $f_e = 72$ from table 6, the confidence interval is calculated.

Total DOF associated with the mean (μ_{FF}) = $2 \times 2 + 2 = 6$, total trials = 27, $N = 3 \times 27 = 81$

$$n_{\text{eff}} = 81 / (1 + 6) = 11.57, \alpha = 0.05, F_{0.05; (1, 72)} = 3.98 \text{ (tabulated).}$$

The calculated CI is: $CI = \pm 19.77$.

The predicted mean of feed force is: $\mu_{FF} = 169.32$ N.

The 95% confidence interval of the predicted optimal feed force is: $[\mu_{FF} - CI] < \mu_{FF} < [\mu_{FF} + CI]$ i.e. $149.55 < \mu_{FF}(N) < 189.09$.

6. Confirmation experiments

The confirmation experiment is the final step in verifying the conclusions drawn based on Taguchi's parameter design approach. The optimum conditions are set for the significant factors (the insignificant factors are set at economic levels) and a selected number of tests are run under constant specified conditions. The average of the results of the confirmation experiment is compared with the anticipated average based on the parameters and levels tested. The confirmation experiment is a crucial step and is highly recommended by Taguchi to verify the experimental conclusions (Ross 1996). Three confirmation experiments were thus conducted at the optimal settings of the turning process parameters recommended by the investigation. The average value of feed force while turning EN24 steel with TiC-coated carbide inserts was found to be 176.67 N. This result was within the 95% confidence interval of the predicted optimal value of the selected machining characteristic (feed force). Hence the optimal settings of the process parameters, as predicted in the analysis, can be implemented.

7. Limitations of case study

The results are valid within the specified range of the process parameters and for the specified work-tool combination. Any extrapolation must be confirmed by experiments.

8. Conclusions

The following conclusions can be drawn from the case study.

- (1) The percent contributions of depth of cut (55.15 %) and feed rate (23.33 %) in affecting the variation of feed force are significantly larger (95 % confidence level) as compared to the contribution of the cutting speed (2.63 %).
- (2) Interaction between cutting speed and depth of cut is significant at 95% confidence level in affecting the mean and variation of feed force, while the interaction between feed and depth of cut affects only the variation in the feed force.
- (3) Optimal settings of various process parameters for turned parts to yield optimal feed force are: cutting speed = 310 m/min; feed rate = 0.14 mm/rev; depth of cut = 0.70 mm.
- (4) The predicted range of the optimal feed force is:

$$149.55 < \mu_{FF}(N) < 189.09$$

References

- Abdulla A A 1994 *Performance of some coated carbide inserts in machining of EN24 steel*. Ph D thesis, University of Roorkee, Roorkee
- Byrne D M, Taguchi S 1987 The Taguchi approach to parameter design. *Quality Progress*: 19–26
- Kalnh G S, Sachdeva S C, Choudhary A P 1978 An experimental investigation into hot machining of EN24 steel. *Proc. AIMTDR Conference*, IIT, Bombay, p. 285
- Komanduri R 1982 Catastrophic shear instability in high speed machining of AISI 4340 steels. *Trans. ASME., J. Eng. Ind.* 104: 121–128
- Lo K C, Chen N S S 1977 Prediction of tool life in hot machining of alloy steels. *Int. J. Prod. Res.* 15: 47–63
- Mottram R A, WoolMan J 1966 *The mechanical and physical properties of the British Standard EN steels* vol. 2, EN21–EN39, p. 72
- Nakayama K, Shaw M C 1967 Machining high strength materials. *Ann. CIRP* 15: 456–459
- Peace G S 1993 *Taguchi methods: A hands-on approach* (New York: Addison Wesley)
- Roy R K 1990 *A primer on Taguchi method* (New York: Van Nostrand Reinhold)
- Ross P J 1996 *Taguchi techniques for quality engineering* (New York: McGraw-Hill)
- Sarmah B P 1988 *Some investigations into performance of CVD-coated indexable carbide inserts in machining of difficult to machine materials*. Ph D thesis, University of Roorkee, Roorkee
- Singh H, Kumar P 2000 Multicriteria optimization of machining parameters using the concept of fuzzy set logics. *Proc. 16th Nat. Convention of Mechanical Engineers* University of Roorkee, Roorkee, India, pp. 516–521
- Singh H, Kumar P 2003 Quality optimization of turned parts (En 24 steel) by Taguchi method. *Prod. J.* 44: 43–49
- Singh H, Kumar P 2004 Tool wear optimization in turning operation by Taguchi method. *Indian J. Eng. Mater. Sci.* 11: 19–24
- Singh H, Kumar P 2004 Effect on power consumption for turned parts using Taguchi technique. *Prod. J.* 45: 231–238
- Singh H, Kumar P 2005 Optimizing cutting force for turned parts using Taguchi's parameter design approach. *Indian J. Eng. Mater. Sci.* 12: 97–103