Orbital-selective Mott transitions in the anisotropic 2-band Hubbard model at finite temperatures

Nils Blümer

Outline

Motivation: OSMTs in $Ca_{2-x}Sr_xRuO_4$

Complementing QMC with high-frequency expansions

Mott transition in frustrated 1-band Hubbard model

High-precision ground state estimates from QMC

Orbital-selective Mott transitions in 2-band Hubbard model

Summary

Motivation: OSMTs in $Ca_{2-x}Sr_xRuO_4$



 $Ca_{2-x}Sr_xRuO_4$: isostructural to $La_{2-x}Sr_xCuO_4$

 Sr_2RuO_4 : quasi-2d FL, spin-triplet superconductor





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[Nakatsuji et al., PRL 90, 137202 (2003)]

saturation moment, susceptibility

 $\rightsquigarrow S = 1/2$ system for $x \gtrsim 0.2$ (not S = 1)

strongly anisotropic magnetoresistance

orbital-selective Mott metal-insulator transitions for $x\approx 0.5,\,x\approx 0.2$?

high-precision methods needed!

Complementing QMC with high-frequency expansions



Complementing QMC with high-frequency expansions



QMC: discretization $\beta = \Lambda \Delta \tau$, Trotter decoupling, discrete Hubbard-Stratonovich transformation

$$\longrightarrow \bigwedge^{*}_{*} \bigoplus^{*}_{*} \bigoplus$$

Metropolis MC importance sampling over auxiliary Ising field, 2^{Λ} configurations, $50 \lesssim \Lambda \lesssim 400$

+ numerically exact — effort scales as T^{-3}

- no info for $\omega\gtrsim\omega_{
m Nyquist}~~
ightarrow$ problems with Fourier transforms



 $1^{\rm st}$ solution: correct unphysical behavior for $|\omega|\lesssim\omega_{\rm Nyquist}$ by transformation [UImke]

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2^{nd} solution: interpolate G_{QMC}(\tau) by cubic splines [Jarrell, Krauth, ...]
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but: natural boundary conditions not appropriate for $G(\tau)$:

- adjust bc's [Oudovenko]
- spline-fit only difference w.r.t. reference problem:
 - IPT [Jarrell]



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- adjust bc's [Oudovenko]
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 - IPT [Jarrell]
 - high-frequency expansion for Σ + fit-param. [Knecht, NB]





Sensitive test: self-energy $\Sigma(i\omega_n)$ for insulating phase (T = 0.1, U = 5.0)

Rapid convergence at all frequencies for "QMC + $1/\omega$ " DMFT solver

Mott transition in frustrated 1-band Hubbard model





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High-precision ground state estimates from QMC

QMC (+ high-frequency expansion) vs. strong-coupling PT for insulating phase



Excellent agreement at U = 6.0, deviations below.

Higher resolution plots: differences w.r.t. 10^{th} order PT



ePT: extrapolation of PT to infinite order [NB, Kalinowski, Phys. Rev B **71**, 195102 (2005)] \rightsquigarrow critical interaction U_{c1} , critical exponents, benchmark ($\Delta E \lesssim 10^{-6}$)

QMC algorithm has passed only available authoritative (1-band) test!

Metallic phase: differences w.r.t. 2^{nd} order weak-coupling PT for E and D



QMC-fit consistent with ePT for insulator; larger deviations of PSCT, DMRG, and PQMC. 4^{th} order PT coefficient corrected by QMC ($-62 \rightarrow +5$)

Orbital-selective Mott transitions in 2-band Hubbard model





Orbital-selective Mott transitions in 2-band Hubbard model



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Orbital-selective Mott transitions in 2-band Hubbard model



two distinct MITs for $J_z = J_\perp = U/4$ [Koga *et al.*, PRL **92**, 216402 (2004)] single MIT or two OSMTs for $J_\perp = 0$, $J_z = U/4$?

Earlier DMFT-QMC results: single Mott transition in J_z model ($J_{\perp} = 0$)

quasiparticle weight $Z_i = m/m_i^*$

discrete QMC estimate:

$$Z_i \approx \left[1 - \mathrm{Im}\Sigma(i\pi T)/\pi T\right]^{-1}$$



$$J_z = 0.2, \ U' = U - 0.4$$



Earlier DMFT-QMC results: single Mott transition in J_z model ($J_{\perp} = 0$)



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Test for multiband-QMC: quasiparticle weights $Z = m/m^*$ in 2-band model



Test for multiband-QMC: quasiparticle weights $Z = m/m^*$ in 2-band model



Very small dependence on discretization $\Delta \tau$ (here for T = 1/32).

Conclusion in 3/2005: New algorithm clearly exposes (single) metal-insulator transition (MIT) But: wide band still "quite metallic" for $U > 2.0 - 2^{nd}$ transition?

Ratio of quasiparticle weights $r=Z_{ m narrow}/Z_{ m wide}$





kinks indicate $2^{\rm nd}$ transition at $U \approx 2.5$

Low-frequency analysis of self-energy



for regular self-energy: $\omega\Sigma(\omega) \xrightarrow{\omega \to 0} 0$

singularities (\sim gap) for $U\gtrsim 2$ in narrow band $U\gtrsim 2.5$ in wide band

Spectral function (interacting DOS)



Clear indications for second singularity

Wide band remains metallic at $U \approx 2.0$

→ two orbital-selective Mott transitions [Knecht, NB, van Dongen, cond-mat/0505106, to appear in PRB RC] same conclusions from slave-spin approximation [de' Medici, Georges, Biermann, cond-mat/0503764]

Comparison at T = 1/32 with Liebsch, PRB **70**, 165103 (2004)

triggered by Comment [Liebsch, cond-mat/0506138] on our preprint



Numerical noise in Liebsch's QMC data obscures second transition

Liebsch's relative errors > 100% at both transitions [our error: $\mathcal{O}(1\%)$]

[Knecht, NB, van Dongen, cond-mat/0506450]

Determination of critical temperature for narrow-band transition



Systematic study: effect of inter-orbital coupling (preliminary results)

$$H = \sum_{m=1}^{2} \left[-\sum_{\langle ij \rangle \sigma} t_m c_{im\sigma}^{\dagger} c_{jm\sigma} + U \sum_i n_{im\uparrow} n_{im\downarrow} \right] + \alpha \sum_{i\sigma\sigma'} (U/2 - \delta_{\sigma\sigma'} U/4) n_{i1\sigma} n_{i2\sigma'}$$

$$I = \frac{1}{40} \int_{\alpha=0.0}^{\alpha=0.0} \frac{1}{\alpha=0.2} \int_{\alpha=0.1}^{\alpha=0.0} \frac{1}{\alpha=0.2} \int_{\alpha=0.1}^{\alpha=0.0} \frac{1}{\alpha=0.2} \int_{\alpha=0.1}^{\alpha=0.0} \frac{1}{\alpha=0.2} \int_{\alpha=0.3}^{\alpha=0.1} \frac{1}{\alpha=0.2} \int_{\alpha=0.3}^{\alpha=0.3} \frac{1}{\alpha=0.3} \int_{\alpha=$$

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Summary

Improved DMFT-QMC scheme using high-frequency expansion of $\Sigma(\omega)$

Mott transition in frustrated 1-band Hubbard model

High-precision ground state estimates from QMC

Critical exponents from (infinite-order) ePT

Orbital-selective Mott transition in 2-band Hubbard model J_z model: minimal model for OSMTs in Ca_{2-x}Sr_xRuO₄ narrow-band transition 1st order for $T \lesssim 0.02$ wide-band transition 1st order for small J_z , U'

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