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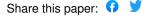
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## OSSOS. VII. 800+ Trans-Neptunian Objects—The Complete Data Release

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#### Abstract

The Outer Solar System Origins Survey (OSSOS), a wide-field imaging program in 2013–2017 with the Canada-France-Hawaii Telescope, surveyed 155 deg<sup>2</sup> of sky to depths of  $m_r = 24.1 - 25.2$ . We present 838 outer solar system discoveries that are entirely free of ephemeris bias. This increases the inventory of trans-Neptunian objects (TNOs) with accurately known orbits by nearly 50%. Each minor planet has 20–60 Gaia/Pan-STARRS-calibrated astrometric measurements made over 2-5 oppositions, which allows accurate classification of their orbits within the trans-Neptunian dynamical populations. The populations orbiting in mean-motion resonance with Neptune are key to understanding Neptune's early migration. Our 313 resonant TNOs, including 132 plutinos, triple the available characterized sample and include new occupancy of distant resonances out to semimajor axis  $a \sim 130$  au. OSSOS doubles the known population of the nonresonant Kuiper Belt, providing 436 TNOs in this region, all with exceptionally high-quality orbits of a uncertainty  $\sigma_a \le 0.1\%$ ; they show that the belt exists from  $a \ge 37$  au, with a lower perihelion bound of 35 au. We confirm the presence of a concentrated low-inclination  $a \simeq 44$  au "kernel" population and a dynamically cold population extending beyond the 2:1 resonance. We finely quantify the survey's observational biases. Our survey simulator provides a straightforward way to impose these biases on models of the trans-Neptunian orbit distributions, allowing statistical comparison to the discoveries. The OSSOS TNOs, unprecedented in their orbital precision for the size of the sample, are ideal for testing concepts of the history of giant planet migration in the solar system.

*Key words:* Kuiper belt: general – surveys *Supporting material:* tar.gz files

#### 1. Introduction

We present the full data release of the Outer Solar System Origins Survey (OSSOS) as part of an ensemble of four surveys that together have found 1142 trans-Neptunian objects (TNOs) with well-measured discovery biases. We provide a software suite that allows models of the orbital distributions of the

trans-Neptunian populations to be "observed" by OSSOS and the other three well-characterized surveys, imposing their observational biases. The biased models can then be statistically tested against the detected outer solar system, i.e., the precisely classified TNO discovery sample. Potential dynamical histories of our planetary system can be comprehensively tested.

The dynamical structure of the trans-Neptunian population is complex and intricate (e.g., Chiang et al. 2003; Gladman et al. 2008, 2012; Petit et al. 2011 and references therein), a signature of shaping by multiple processes over the last 4.5 Gyr. How the TNOs that reside in orbital resonances with Neptune were emplaced is intimately related to how and where the giant planets formed and migrated (Fernandez & Ip 1984; Kaula & Newman 1992; Malhotra 1993, 1995; Chiang & Jordan 2002; Thommes et al. 2002; Kortenkamp et al. 2004; Hahn & Malhotra 2005; Tsiganis et al. 2005; Levison et al. 2008; Nesvorný 2015b; Kaib & Sheppard 2016; Pike & Lawler 2017). Models of planetary migration result in different distributions of today's resonant objects in (1) the various "types" of libration, (2) the libration amplitude of the resonance angle  $(\phi)$ , (3) their eccentricities (e.g., Murray-Clay & Chiang 2005; Pike & Lawler 2017), (4) the fraction of resonant TNOs also experiencing Kozai resonance (Lawler & Gladman 2013), and (5) the relative population of different resonances. As an example, considering the 2:1 mean-motion resonance with Neptune, rapid planetary migration results in fewer objects librating around  $\phi \sim 90^{\circ}$  than about the other asymmetric island near  $\phi \sim 270^{\circ}$ , with the fraction depending on the pace and duration of Neptune's early wandering through the solar system (Murray-Clay & Chiang 2005). The population ratios between particular resonances differ if Neptune's orbital evolution is modeled as a smooth migration (Chiang et al. 2003; Hahn & Malhotra 2005) or as scattered and damped (Levison et al. 2008), e.g., between the 2:1, 3:2, and 5:2 resonances (Gladman et al. 2012). Three possible mechanisms for resonant capture—large-scale migration of Neptune (e.g., Malhotra 1995; Hahn & Malhotra 2005), chaotic capture of scattered objects (Levison et al. 2008), and capture of scattered objects through fast secular evolution (Dawson & Murray-Clay 2012)—may also result in different libration amplitudes and resonance occupation ratios.

The present set of minor planets suitable for testing models of the solar system's dynamical history is still small. Observational surveys of the trans-Neptunian region need to have detailed parameterizations, which make the surveys' discoveries useful for cosmogonic mapping (Kavelaars et al. 2008). The surveys must have precisely measured detection efficiencies and track essentially all their discoveries in order to avoid ephemeris bias. This bias is an insidious loss of unusual orbits from the detected TNO sample. It happens when the assumed orbit fit to a short (\( \left( month-long \)) arc of observations is used to predict the future sky location of a TNO for recovery observations made many months later (Jones et al. 2006; Kavelaars et al. 2008; Jones et al. 2010). TNOs discovered with well-quantified discovery biases are key, as they are appropriate to use to understand the intrinsic population distributions. As of 2018 January 15, the Minor Planet Center (MPC) database<sup>26</sup> contained 1796 TNOs with orbits known from observations on multiple oppositions (excluding the 167 OSSOS-credited discoveries released to the MPC prior to this date). The MPC database is built from the discoveries of more than 60 individual surveys, with a wide variety of inherent and typically unpublished bias characteristics. Three surveys provide half of the MPC sample. The two largest past surveys are the Deep Ecliptic Survey (DES, 1998-2005; Elliot et al.

2005), which provided 478 MPC designations, of which 316 had sufficient observational arc for their orbits to be classified within populations, with 304 secure classifications (Adams et al. 2014), and the Canada–France Ecliptic Plane Survey and its High Ecliptic Latitude extension (CFEPS, 2003–2006: Jones et al. 2006; Kavelaars et al. 2009; Petit et al. 2011; HiLat, 2006–2009: Petit et al. 2017), which provided 190 secure orbits. The Pan-STARRS1 survey (2010–ongoing; Chambers et al. 2016) has provided 370 new objects thus far (Holman et al. 2015, 2017; Weryk et al. 2016), but these are still without quantification of their observational biases (Holman et al. 2018).

We designed OSSOS to discover and track many hundreds of distant minor planets, with careful quantification of the bias effects inherent in the observing and analysis of TNOs (see Bannister et al. 2016b). A core theme of OSSOS was to find the fraction of resonant TNOs and map out the filigreed structure of the resonances. OSSOS operated as the top-ranked Large Program on the Canada–France–Hawaii Telescope (CFHT) from 2013A through 2016B, with additional observing through 2017. Our design was based on experience from CFEPS and the survey of Alexandersen et al. (2016, hereafter A16). We surveyed 155.3  $\deg^2$  of sky near the invariable plane at a range of heliocentric longitudes to moving-target limiting magnitudes ( $m_r$ ) ranging from  $m_r = 24.1$  to 25.2. Three-quarters of the survey goes deeper than the forthcoming Large Synoptic Survey Telescope will reach in single observations (Jones et al. 2016).

Our full survey data release focuses on the products from our 5 yr of observations, 2013 January through 2017 December. The calibration and analysis of the images are given in Section 2. The entire survey's discoveries of TNOs are detailed in Section 3. Of our TNOs, 840 were bright enough to have detailed bias-characterization analysis. Of these, 838 have received tracking observations that ensure that the objects can never be lost, while merely two close Centaurs were lost. No previous survey has ever achieved such a high rate of success in tracking TNOs to good orbits. Our established survey simulator is expanded and improved from that in Petit et al. (2011). It permits assessment of models of the trans-Neptunian populations against a calibrated and carefully tracked set of TNO detections. We provide simulator files detailing the observations and the characterized detections (1142 in total) from an ensemble of four bias-characterized surveys with CFHT: CFEPS, HiLat, A16, and OSSOS (Section 4). This framework is ideal for investigating the processes at work during the formation and early evolution of the solar system. We conclude by highlighting the orbital properties of our discoveries, with comparison to the MPC inventory (Section 5).

#### 2. Data Acquisition and Calibration

All observations were acquired with the 0."184 pixel<sup>-1</sup> MegaCam imager (Boulade et al. 2003) of CFHT on Maunakea, Hawai'i. Bannister et al. (2016a, Section 2) detailed the survey design; here we provide a brief summary. OSSOS surveyed the distant solar system objects present in eight regions of sky ("blocks," each ~20 deg²). The spatial relationship of these pointings to one of the target resonant TNO populations, the plutinos (3:2 mean-motion resonance with Neptune), is shown in Figure 1. The full geometry of the survey is in Table 1.

The OSSOS blocks were placed on the sky at a range of low latitudes chosen relative to the invariable plane of the solar system (Souami & Souchay 2012), rather than to the ecliptic

<sup>26</sup> https://minorplanetcenter.net/iau/lists/TNOs.html, https://minorplanetcenter.net/iau/lists/Centaurs.html, https://minorplanetcenter.net/iau/lists/NeptuneTrojans.html



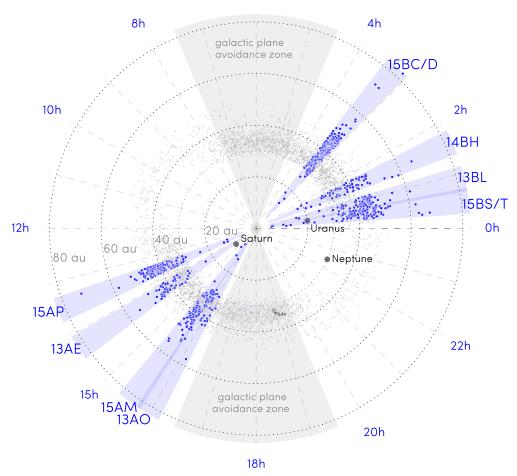
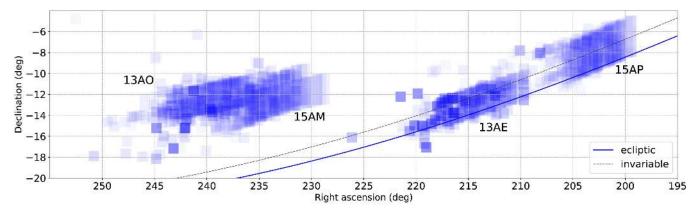


Figure 1. Spatial relationship of the regions of sky targeted by OSSOS to the geometry of the outer solar system. The eight sky blocks are indicated by blue wedges, flattened from their low  $0^{\circ}-10^{\circ}$  inclinations into the plane (the on-sky projection is shown in Figure 2). The blocks were placed to avoid the dense star fields of the galaxy (schematically indicated by gray shading). Gray dots show the predicted position density of the observable fraction ( $m_r < 24.7$ ) of objects in the 3:2 resonance with Neptune, as modeled by Gladman et al. (2012). Blue dots are the 840 characterized OSSOS discoveries (Table 3), which were found at heliocentric distances between 6 and 83 au. The sensitivity of OSSOS to distant moving objects extends beyond the figure boundaries to  $\sim 100-130$  au and is discussed in Section 2.9.

Table 1
Areas of the Sky Observed for Discovery by OSSOS

Block	R.A. (hr)	Decl. (deg)	Epoch (MJD)	Field Layout	Area (deg²)	Filling Factor	Filter	$m_{\text{limit}}$ (3" hr <sup>-1</sup> )	TNOs Detected
15BS	00:30:08.35	+06:00:09.5	57274.42965	2 × 5	10.827	0.9223	R.MP9602	25.12	67
15BT	00:35:08.35	+04:02:04.5	57273.42965	$2 \times 5$	10.827	0.9223	R.MP9602	24.93	54
13BL	00:52:55.81	+03:43:49.1	56596.22735	$3 \times 7  (-1)$	20.000	0.9151	R.MP9601	24.42	83
14BH	01:35:14.39	+13:28:25.3	56952.27017	$3 \times 7$	21.000	0.9103	R.MP9601	24.67	67
15BC	03:06:18.32	+15:31:56.3	57332.33884	$1 \times 4$	4.331	0.9215	R.MP9602	24.78	
15BD	03:12:58.36	+16:16:06.4	57333.35377	$2 \times 4$	8.662	0.9211	R.MP9602	25.15	146
15BC	03:22:09.15	+17:15:44.0	57332.33884	$2 \times 4$	8.662	0.9215	R.MP9602	24.78	104
15AP	13:30:22.11	-07:47:23.0	57125.36971	$4 \times 5$	21.654	0.9186	R.MP9602	24.80	147
13AE	14:15:28.89	-12:32:28.5	56391.36686	$3 \times 7$	21.000	0.9079	R.MP9601	24.09	49
15AM	15:34:41.30	-12:08:36.0	57163.31831	$4 \times 5$	21.654	0.9211	R.MP9602	24.87	87
13AO	15:58:01.35	-12:19:54.2	56420.45956	$3 \times 7$	21.000	0.9055	R.MP9601	24.40	36

**Note.** The filling-factor correction is discussed in Section 2.9: it incorporates the true pixel area, the small overlap area due to the new shape of the CCD in discovery blocks from 2015, and the few incompletely searched chips. It is used in the survey simulator (Section 4) when testing the visibility of model objects by their location on the sky. The survey simulator uses a single date for each block, as that is statistically equivalent: the simulator produces a statistical ensemble that is representative of the detections, and the approximation provides computational efficiency. Note that 15BC is in two parts (Section 2.6) and thus appears twice in this table; however, its detections are given once as a total. Limiting magnitude is given for sources with a sky motion rate of 3" hr<sup>-1</sup>: for comprehensive details across the full range of motion rates, see Section 2.9 and Table 2. TNO detections are discussed in Section 3. (This table is incorporated in machine-readable form with fully specified polygons inside the survey simulator, linked in Section 4.)



(a) OSSOS survey blocks with April-May oppositions.

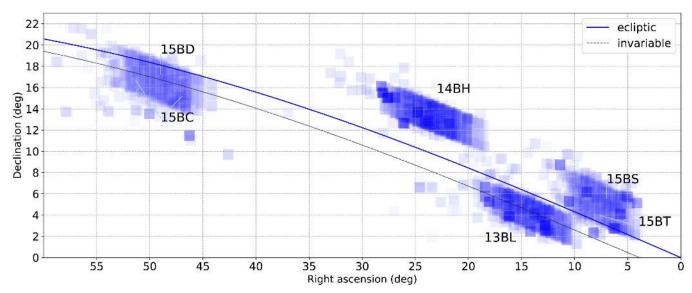


Figure 2. Sky locations of the OSSOS survey blocks, showing all CFHT MegaCam imaging 2013-2017 (blue shading).

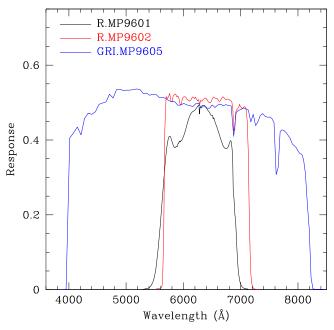
(Figure 2). The choice of reference plane when siting survey regions is important for low-latitude surveys. The inclination distributions of the dynamical populations of TNOs are well described by overlapping Gaussians of various widths (Brown 2001): the narrowest, that of the cold classical Kuiper Belt, has a mere  $\sigma \sim 2^{\circ}$  (Gulbis et al. 2010; Petit et al. 2011). The mean plane of the Kuiper Belt is certainly not the ecliptic, nor is it precisely the invariable plane, and it is not consistently flat with increasing semimajor axis (Brown 2001; Chiang & Choi 2008; Volk & Malhotra 2017). However, the invariable plane provides a reasonable proxy for the purpose of large-area survey design. As the spacing on the sky between the ecliptic and invariable planes varies with longitude by up to  $\sim 4^{\circ}$ , proximity to a given plane will affect the detection rates of the cold classical population. Each OSSOS block was a rectangular grid, arranged to best tessellate MegaCam's  $\sim 0.9 \text{ deg}^2$  field of view parallel to the invariable plane and reduce shear loss of TNOs (Figure 2).

Discovery observations were made when each block of sky came to opposition, and they set the limiting magnitudes of the survey. OSSOS observed in the r-band ( $\lambda \sim 640$  nm) MegaCam filters R.9601 and R.9602, which approximate the r-band Sloan Digital Sky Survey (SDSS) response (Fukugita et al. 1996), and in a "w" wide-band filter, GRI.MP9605, all of which are specified in Section 2.8.3 and Figure 3. Each of the

fields in a block was observed with a triplet of exposures in an *r*-band MegaCam filter, spaced over 2 hr. The image quality (IQ) of this discovery triplet<sup>27</sup> was crucial: the depth reached in the discovery images set the detectable flux limit of TNO discoveries for OSSOS, which, in combination with the tracking efficiency, determined each block's characterization limits. These derived brightness- and sky motion rate-dependent limiting magnitudes for OSSOS are given in Table 2.

OSSOS was designed to provide the necessary orbital accuracy of its TNOs via (a) a dense cadence, with observations in every available dark run over 2 consecutive yr, and (b) the elimination of systematic errors in astrometry catalogs (discussed in Section 2.8). As in the A16 survey, the observations in the first year targeted only each block's large grid of pointings. We offset the sky position of the discovery fields throughout the observing semester at a rate consistent with the mean rate of motion for TNOs expected to be detectable in the field. This observing technique maximized observations of the TNOs that would be present in the block at opposition and ensured that the TNOs were imaged at least

<sup>&</sup>lt;sup>27</sup> The CFHT image IDs of the images used in the discovery triplet for each block are provided in the Supplemental Materials. See footnote 28 for image access details.



**Figure 3.** Filter responses for the CFHT MegaCam filters used in OSSOS. Discovery imaging was made exclusively in the two very similar r filters (Table 1). Most tracking images were made with the wide GRI.MP9605 filter, which we refer to in our astrometric measurement lines as w. The detailed data for the filter response curves are available at http://www.cadc-ccda.hia-iha.nrc-cnrc.gc.ca/en/megapipe/docs/filt.html.

several times each lunation. Our avoidance of estimating follow-up ephemerides from short observational arcs removed ephemeris bias.

The high astrometric precision and numerous observations in the first year ensured that ephemeris predictions in the second year generally had uncertainties smaller than 1', allowing observations to use targeted pointings instead of a grid. The pointings were designed to recover all objects as they slowly sheared further apart; the TNOs were still clustered close enough on the sky to frequently observe multiple TNOs in each pointing. Tracking observations were first made in an r-band filter, then, after 2015 August, in the "w" GRI.MP9605 wideband filter (Section 2.8). The additional observations refined the TNOs' orbital parameters until they were better than a quality threshold: we required a fractional semimajor axis uncertainty  $\sigma_a < 0.1\%$  (see Section 3.3).

Considering purely the overall data set of images, the dense OSSOS cadence provided 20–60 epochs across 2–5 yr, each to an r- or w-band  $\sim 3\sigma$  depth of magnitudes 24.1–25.3 across a substantial region of sky:  $\sim 170~{\rm deg^2}$  in the vicinity of the ecliptic. The density of visits is indicated by shading in Figure 2. More than 8000 images were acquired, making OSSOS one of the most data-rich surveys yet made with CFHT. The depth of the combined imaging if stacked would approach  $m_r \sim 26.3$  across large areas. All of the calibrated survey images are available 28 from the Canadian Astronomy Data Centre (CADC).

Bannister et al. (2016b) described the observations of the first two blocks (13AE and 13AO) in 2013–2015. We now describe the observations of the remaining six blocks, which had their discovery observations in the semesters 2013B, 2014B, 2015A, and 2015B (Sections 2.1–2.6). We also detail

observations made for OSSOS with CFHT in 2014–2017 outside of the Large Program (Section 2.7). We then discuss our astrometric and photometric calibration of the images (Section 2.8) and quantify our analysis pipeline's TNO detection efficiency (Section 2.9).

#### 2.1. Block 13BL Observations

The 13BL block was a  $3 \times 7$  grid of MegaCam fields that overlaid the invariable plane, centered at  $0^h.55'$ ,  $4^o.00'$  (Figure 2). The 13BL discovery observations were made in median IQ of 0.75 with the R.MP9601 filter. Half the block was acquired on 2013 September 29, and the other half was acquired on 2013 October 31. A complete triplet sequence was acquired on 20 MegaCam fields (one fewer than in the 21-field block design). Uranus was about  $1^\circ$  away during discovery acquisition but did not contribute any scattered light. Tracking observations within the discovery lunation and in the lunations on either side were smoothly acquired. Pointed tracking observations were made from 2014 July through 2015 January, all with the R.MP9601 filter.

## 2.2. Block 14BH Observations

The 14BH block was a  $3 \times 7$  grid of pointings  $2^{\circ}-5^{\circ}$  off the invariant plane, centered at 1.29, 12.58 (Figure 2). Poor weather during the 2013 October opposition prevented observation of a valid discovery triplet for the whole H block. Only six fields received a survey-quality  $m_r \sim 24.5$  depth triplet on 2013 November 1. Fortunately, the multiyear nature of the Large Program allowed the discovery observations for the H block to be deferred to the next year's opposition. Also, the CFHT mirror was re-aluminized in 2014 July, a process that increases optical throughput. The full 21 fields of 14BH received discovery triplet observations on a single night, 2014 October 22, in the R.MP9601 filter. All discoveries at Kuiper Belt distances found in the six-field 2013 triplet were rediscovered in the 2014 triplet. The capriciousness of weather meant the designed OSSOS survey cadence was modified for this block: there were two semesters of only tracking the 14BH grid, with the discovery triplet observed in the second. The cadence and strategy remained successful under this strain. During analysis, the density of the 2013 observations permitted immediate linking out of each TNO's orbit from the arcs in the 2014 discovery semester to "precovery" arcs throughout 2013B. Despite the unorthodox observing, only minimal cleanup observations with pointed ephemerides were needed in 2014 December and 2015 January. These secured the orbits of a small fraction of <30 au discoveries, which had moved to areas of sky outside the grid of the block that was observed in 2013-2014.

## 2.3. Block 15AP Observations

The 15AP block was a  $4 \times 5$  grid of pointings spanning the invariant plane and centered at  $13^h30'$ ,  $-7^\circ45'$  (Figure 2). Its positioning, lower in R.A. than 13AE, centers it more on the invariant plane while avoiding potential scattered light from  $\alpha$  Vir. The 15AP block was acquired for discovery on 2015 April 12 in 0."6 seeing in the R.MP9602 filter (discussed below).

A new set of filters was introduced for CFHT's MegaPrime in 2015. The new filters allowed the use of four chips that have been on MegaCam since its commissioning but were vignetted out. This changed the MegaCam focal plane from 36 chips

<sup>&</sup>lt;sup>28</sup> doi:10.11570/18.0001

Table 2
Characterization Limits for Each Survey Sky Region (Block) of OSSOS

Motion Rate						
(arcsec hr <sup>-1</sup> )	$\eta_o$	c	$\sigma$	$m_0$	$m_{50\%}$	$m_{ m limit}$
		13	AE			
0.5-8.0	0.8877	0.0276	0.1537	24.1423	23.95	24.09
8.0-11.0	0.8956	0.0231	0.1571	24.0048	23.86	23.85
11.0-15.0	0.8658	0.0212	0.1555	23.8811	23.74	23.73
		13	AO			
0.5-7.0	0.8414	0.0205	0.1107	24.5497	24.36	24.40
7.0–10.0	0.8776	0.0188	0.1217	24.4187	24.28	24.26
10.0–15.0	0.8639	0.0188	0.1453	24.2575	24.10	24.10
0.5.2.5	0.9524		BL 0.1480	24 5212	24.25	24.45
0.5–2.5 2.5–8.0	0.8524 0.8883	0.0168 0.0133	0.1489 0.1453	24.5213 24.4793	24.35 24.36	24.45 24.42
8.0–12.0	0.8841	0.0133	0.1433	24.3311	24.30	24.42
12.0–15.0	0.8683	0.0002	0.1544	24.2243	24.12	24.10
12.0 13.0	0.0003		ВН	21.2213	21.12	21.10
0.5-2.0	0.9359	0.0088	0.1769	24.6522	24.57	24.66
$2.0-6.0^{a}$	0.9025	0.2820	0.7796	24.7967	24.54	24.67
6.0-8.0	0.8997	0.0101	0.1713	24.5681	24.45	24.55
8.0-10.0	0.8932	0.0113	0.1663	24.5113	24.40	24.39
10.0-12.0	0.8784	0.0113	0.1670	24.4454	24.32	24.32
12.0-15.0	0.8663	0.0140	0.1674	24.3540	24.21	24.21
			AP			
0.5–2.0	0.9479	0.0117	0.1837	24.7797	24.66	24.77
2.0-5.0	0.9270	0.0131	0.1780	24.7708 24.6999	24.64	24.80
5.0–8.0 8.0–10.0	0.8990 0.8775	0.0124 0.0125	0.1744 0.1749	24.6332	24.56 24.49	24.66 24.49
10.0–12.0	0.8600	0.0123	0.1749	24.0332	24.49	24.49
12.0–15.0 <sup>a</sup>	0.8258	0.3112	0.9109	24.6297	24.28	24.32
12.0 10.0	0.0200		AM	2110277	220	252
0.5-2.0	0.9382	0.0107	0.1561	24.9223	24.82	24.91
2.0-6.0	0.9168	0.0127	0.1490	24.9023	24.78	24.87
6.0-8.0	0.8903	0.0131	0.1485	24.8419	24.71	24.79
8.0-10.0	0.8810	0.0136	0.1462	24.7839	24.64	24.63
10.0–12.0	0.8654	0.0145	0.1482	24.7113	24.56	24.55
12.0–15.0	0.8455	0.0149	0.1518	24.6220	24.45	24.45
0.5.20	0.0502		BS 0.2064	25 2025	25.20	25.20
0.5-2.0 2.0-6.0	0.9593 0.9353	0.0066 0.0072	0.2064 0.1985	25.3835 25.3351	25.29 25.23	25.39 25.15
6.0-8.0	0.9353	0.0072	0.1963	25.2459	25.23	25.23
8.0–10.0	0.9103	0.0073	0.1804	25.1959	25.06	25.07
10.0–12.0	0.8965	0.0091	0.1706	25.1040	24.98	24.97
12.0–15.0	0.8711	0.0104	0.1697	24.9981	24.84	24.85
		15	BT			
0.5-2.0	0.7794	0.0096	0.1543	25.0931	24.88	25.00
2.0-6.0	0.7337	0.0070	0.1764	25.0357	24.79	24.97
6.0-8.0	0.7045	0.0072	0.1792	24.9767	24.69	24.85
8.0–10.0	0.6822	0.0068	0.1694	24.9149	24.62	24.68
10.0–12.0	0.6802	0.0099	0.1690	24.8709	24.50	24.59
12.0–15.0	0.6548	0.0096	0.1756	24.7751	24.35	24.47
0.5-2.0	0.9333	0.0122	BC 0.1300	24.8779	24.78	24.86
$2.0-6.0^{a}$	0.9333	0.0122	0.7915	24.9270	24.68	24.78
6.0-8.0	0.8632	0.0108	0.1364	24.7044	24.58	24.67
8.0–10.0	0.8440	0.0125	0.1456	24.6313	24.49	24.48
10.0–12.0	0.8126	0.0114	0.1313	24.5264	24.38	24.37
12.0-15.0	0.7847	0.0129	0.1457	24.3944	24.21	24.22
			BD			
0.5-2.0	0.9526	0.0072	0.1517	25.2270	25.15	25.23
2.0-6.0	0.9305	0.0093	0.1713	25.1766	25.06	25.15
6.0-8.0	0.9093	0.0111	0.1559	25.0603	24.94	25.03
8.0–10.0	0.8898	0.0116	0.1607	24.9649	24.82	24.82
10.0–12.0	0.8778	0.0118	0.1532	24.8430	24.71	24.70
12.0–15.0	0.8522	0.0144	0.1584	24.6762	24.50	24.51

**Note.** See text for details of  $\eta_o$ , c,  $\sigma$ ,  $m_0$ ,  $m_{50}$ , and  $m_{\text{limit}}$ . Fits were made with Equation (4), except those marked as follows.

to 40 chips, which required rearranging the OSSOS grid to a 4  $\times$  5 tessellation. All 2015A observations, including the discovery triplets, were acquired in MegaCam's new

R.MP9602 filter. Section 2.8.3 discusses how R.MP9602 has a very similar bandpass but 0.13 mag higher throughput than the R.MP9601 used in previous years (Figure 3). Use of R.MP9602 maintained consistency in the discovery bandpass across the whole of OSSOS. Section 4 discusses how TNO colors can thus be modeled.

The new wide-band filter for MegaCam, GRI.MP9605, spans 4000–8200 Å and is very flat in transmission. We discuss its characteristics in Section 2.8 (Figure 3). Observations in GRI.MP9605 are referred to as w in our observations reported to the MPC. We used the GRI.MP9605 filter exclusively for all of our tracking observations after it became available in 2015 August: it added an extra  $\sim$ 0.7 mag of depth (Section 2.8.3), ideal for recovery of fainter TNOs near the characterization limit.

Good weather in the 15A semester allowed pointed recoveries in GRI.MP9605 on the TNOs discovered in 15AP to proceed without incident from 2016 January through late July. Two observations, spaced by a week to 10 days, were made each lunation.

#### 2.4. Block 15AM Observations

The off-plane 15AM block was a 4 × 5 grid of pointings nestled next to the earlier 13AO block (Bannister et al. 2016b) at a slightly lower ecliptic latitude, centered at 15<sup>h</sup>.30', -12°20' (Figure 2). The multiyear nature of our Large Program permitted advance observations: we predicted the 2014 location of model Kuiper Belt objects that would be within the desired region of sky at opposition in 2015. In 2014, we imaged 21  $deg^2$  (arranged in the 36 chip 3 × 7 grid layout) with a triplet in R.MP9601, with half on 2014 May 29 in 0"5-0"7 seeing and the remainder on 2014 June 1 in similar IQ. In 2015, a successful discovery triplet in the new R.MP9602 filter (see Section 2.3) saw 0".5 IQ on each half, observed on 2015 May 24 and 25. Despite the change in the grid layout (see Section 2.3) and the comparatively higher dispersal rate on the sky of TNOs on more inclined and eccentric orbits, the 2014 observations were able to provide precovery for more than half of the 15AM discoveries. Tracking throughout 16A in the new GRI.MP9605 filter proceeded smoothly (see Section 2.3).

### 2.5. Block 15BS-15BT Observations

The 15B observations provide the deepest areas of sky observed by OSSOS, with discovery observations in Mega-Cam's new filters R.MP9602 and tracking observations in GRI. MP9605 (see Section 2.3) in a semester featuring exceptionally good weather.

The 15BS block was a  $4 \times 5$  grid of pointings placed above the invariant plane to sample inclinations midway between those observed by 13BL and 14BH and centered at  $0^h.30'$ ,  $+05^\circ00'$  (Figure 2). Its discovery triplet acquisition in R.MP9602 in 2015B was in two halves, split parallel to the plane. Both were observed in excellent seeing. However, the half observed on 2015 September 9 had better IQ than that on 2015 September 8, and the half acquired on September 8 had a small pointing shift error for one image of the triplet. For characterization, we thus regard it as two adjacent blocks of equal size: 15BS, the southern half, shallower and closer to the invariant plane, and 15BT, deeper and higher-latitude, as shown in Figure 2.

<sup>&</sup>lt;sup>a</sup> Which were fit with Equation (5).

The tracking acquisitions in GRI.MP9605 in 2015B proceeded smoothly. However, 2016B saw several dark runs become near-total losses due to weather. A quarter of the 2015B discoveries from 15BS/15BT received insufficient tracking for high-precision orbit determination and were targeted for additional 2017 observation.

#### 2.6. Block 15BC-15BD Observations

The 15BD block was a  $4 \times 5$  grid of pointings centered on the invariant plane at  $03^{\rm h}.15'$ ,  $+16^{\circ}.30'$  (Figure 2). As with the 15AM block (Section 2.4), advance planning allowed acquisition of precovery imaging in 2014. This included acquisition on 2014 November 17 of a lengthened, 400 s exposure triplet in R.MP9601 on 11 deg<sup>2</sup> of the block. Designed to be the deepest block OSSOS would acquire, the 2015 discovery triplet's exposure times were lengthened to 400 s in R.MP9602. We redesigned the acquisition cadence to ensure that a triplet spanning 2 hr could still be successfully acquired on a large enough area of sky. Notable variation in IQ occurred between the two nights of observation: 0."6 IQ on 2015 November 6 and 0."45 IQ on 2015 November 7. The characterization on this block is therefore also split in two, forming the adjacent 15BC and 15BD areas (Figure 2). Both have the same latitude coverage. The shallower 15BC is in two parts: a  $1 \times 4 \text{ deg}^2$ column and a  $2 \times 4 \text{ deg}^2$  area, as shown in Figure 2. These bracket the contiguous  $2 \times 4 \text{ deg}^2$  area of 15BD, which is the deepest area imaged by OSSOS.

Similar to that for block 15BS (see Section 2.5), the tracking observations in GRI.MP9605 in 15B were well sampled. The 15BD block was buffered against the sparse observing that occurred in 2016B (see Section 2.5) by the partial-coverage observations in 2014. Exposure times for the GRI.MP9605 tracking observations were increased to 450 s to retain the deep discoveries.

## 2.7. Additional Observations

After 2 yr of intensive observation, a small fraction of TNOs either had orbits still classifying them as insecure or were securely resonant but had large libration amplitude uncertainties. These were targeted with a few extra observations in GRI. MP9605: at minimum two, and in some cases three or four epochs, at times far from opposition that provided the greatest parallax. In 2017, these observations were provided via a Director's Discretionary (17A) and regular-time (17B) proposal. The CFHT mirror was re-aluminized in 2017 August, again producing slightly deeper images.

Additional observations came from a Director's Discretionary program with CFHT MegaCam in 2014–2017, which simultaneously observed a magnitude-limited  $m_r < 23.6$  sample of OSSOS TNOs together with Gemini North for Colours of OSSOS (Col-OSSOS; e.g., Fraser et al. 2015). The program observed a uniform r–u–r filter sequence, with the two 300 s r-band images separated by 1.5 hr. The r filter was R.MP9601 in 2014B-2015A and R.MP9602 after 2015 August. The Col-OSSOS imaging covered most of the area of 13AE, 13AO, 13BL, 14BH, 15BS, and 15BT (M. T. Bannister et al. 2017, in preparation). Its r-band observations are folded into the OSSOS analysis.

The targeted imaging and that for Col-OSSOS produced substantial amounts of serendipitous observing of the TNOs nearby on the sky due to the large MegaCam field of view. The orbits (Section 3) in this paper thus update those given in Bannister et al. (2016b) for the discoveries from blocks 13AE and 13AO.

#### 2.8. Astrometric and Photometric Calibration

OSSOS required high-precision, coherent astrometric calibration to produce TNO orbits of the desired quality (Section 3.3). During the 2013 February–2016 October tracking of each TNO, we acquired observations and then reclassified the newly improved orbit to determine if additional observations were required to secure the orbit. The image calibration during this time used an iterative approach with the 2MASS and UCAC4 catalogs, described in Bannister et al. (2016a, Section 3). Since the *Gaia* Data Release 1 was published in late 2016, all OSSOS data have been astrometrically calibrated using *Gaia*. At the end of the Large Program observations, all earlier OSSOS images were recalibrated using *Gaia*. The orbits that we report here (Section 3) and to the MPC are based on this calibration.

#### 2.8.1. Astrometric Calibration

The *Gaia* Data Release 1 (*Gaia*-DR1; Gaia Collaboration et al. 2016) was used for the principal astrometric reference catalog. The *Gaia*-DR1 catalog extends to a magnitude of  $g \sim 20$ . The astrometric uncertainties are typically 10 mas and do not include estimates of proper motion. However, since OSSOS observed from 2013 to 2017, no observation is more than 2 yr from the *Gaia*-DR1 epoch of 2015.0, so proper motion is unlikely to cause significant systematic effects. The majority of the OSSOS images were calibrated directly with *Gaia*-DR1.

For 201 of the more than 8000 OSSOS images, the Gaia catalog was insufficiently dense to compute an accurate plate solution. In these cases, we used the Pan-STARRS Data Release 1 catalog (PS-DR1; Magnier et al. 2016). The PS-DR1 extends 2-3 mag deeper than Gaia, with a corresponding increase in source density. It was calibrated with the 2MASS catalog (Skrutskie et al. 2006), leading to significant zonal errors. Just before the PS-DR1 release, the coordinates were corrected. The quality of this correction is generally good: for most fields, the typical residuals between PS-DR1 and Gaia-DR1 are on the order of 10 mas. However, there exist several patches of sky in PS-DR1 where there is a considerable offset between PS-DR1 and Gaia. For each of the 201 OSSOS images calibrated with PS-DR1, we examined the residuals between PS-DR1 and Gaia-DR1. Only two images had an unacceptable match and were instead calibrated with 2MASS; their astrometric accuracy is significantly worse.

To measure the astrometric errors, the positions of the sources in every overlapping pair of images were compared. The residuals give an indication of the astrometric errors. The results are 29 mas for R.MP9601, 21 mas for R.MP9602, and 49 mas for GRI.MP9605. The difference in accuracy between the two r filters can be explained by two factors. The installation of vents in the dome of CFHT in late 2013 (Bauman et al. 2014) improved the median seeing in r by  $\sim$ 0."1 (Devost et al. 2016) relative to earlier CFHT imaging (Salmon et al. 2009). Additionally, the new R.MP9602 filter has better throughput (Section 2.8.3), resulting in deeper images. The comparatively worse residuals for the GRI.MP9605 wide filter are due to differential chromatic refraction (DCR).

#### 2.8.2. The Effects of Differential Chromatic Refraction

The effects of DCR are about 10 times as great on the 4000 Å wide GRI.MP9605 as on either of the two r filters. However, while DCR affected the positions of individual stars by tens of mas, the net effect on the plate solution was virtually nil. On average, the plate solution was shifted by 1-2 mas, far smaller than the above-noted random errors. The effects of DCR could only be detected due to the high precision of *Gaia*-DR1. The earlier calibration done in Bannister et al. (2016b) was with respect to 2MASS and UCAC4 (Zacharias et al. 2013), and the random errors in 2MASS overwhelmed the effects of DCR.

We investigated if it would be possible to roughly determine the color of our TNOs from their astrometry, as DCR will systematically shift the measured positions of the TNOs with respect to their true positions. The amplitude of the positional shift from DCR depends on airmass. The direction depends on color: toward the zenith (along the complement of the parallactic angle) if bluer than the average star, toward the horizon if redder. The amplitude of the shift as a function of zenith angle, z, can be computed theoretically using an atmospheric model (Allen 1976) if one has full knowledge of the throughput of the telescope, camera, and filter system, as well as the spectral energy distribution of each observed source. The atmospheric model would need to incorporate the hourly weather conditions and the pointing azimuth and altitude to compute the temperature/pressure profile as a function of altitude along the line of sight. We chose instead to measure DCR empirically, in terms of arcseconds of shift per magnitude of g - i relative to the mean g - i color of stars. The DCR increases linearly with tan(z). We found the slope for the GRI.MP9605 filter to be 75 mas  $mag^{-1}$  per unit tan(z). The amplitude of the slope is 7 mas  $mag^{-1}$  per unit tan(z) for the two r-band filters. The bulk of our observations were made at an airmass <1.4 (or, equivalently, tan(z) < 1). The known range of colors of TNOs is smaller than the range of colors of stars: about  $\pm 0.5$  mag centered on g - i = 1.2 (Sheppard 2012; Wong & Brown 2016), which turns out to also be roughly the mean color of stars. The shift in sky position for a TNO with a color toward the edges of the color distribution is typically 30-40 mas, while TNOs with more median colors will have a smaller shift. Thus, the effect of DCR on the OSSOS measurements is dwarfed by the median 124 mas centroid uncertainties of each TNO observation, and our astrometry cannot be used to infer the color of the TNOs.

## 2.8.3. Photometric Calibration

The filter responses for the three OSSOS filters are shown in Figure 3. These filter responses include the full system of the telescope and camera (including mirror, lenses, and the quantum efficiency of the detector), 1.25 airmasses of atmosphere, and the transmission of the filters themselves. The newer r-band filter (R.MP9602) is slightly wider than the older r-band filter (R.MP9601) and has higher transparency over a wider wavelength range. Images taken in R.MP9602 are on average 0.13 mag deeper than those taken with R.MP9601. Images taken in the wide filter (GRI.MP9605) are on average 0.71 mag deeper than those taken in R.MP9601.

Previously, the photometric calibration was based on the SDSS (Fukugita et al. 1996; Ahn et al. 2014). As described in Bannister et al. (2016a, Section 3), images taken on the

footprint of the SDSS were directly calibrated using the SDSS catalog converted into the MegaCam system. For images off the SDSS footprint, the procedure was more intricate. First, we computed the zero-point variation across the focal plane of MegaCam. Then, for each photometric night, all images on the SDSS were used to compute a nightly zero point. Images taken on photometric nights were calibrated using this zero point. Images taken on nonphotometric nights were calibrated by transferring the zero point from images taken on photometric nights using a bootstrapping system.

With the release of PS-DR1, this system was replaced with a much simpler system. Each image was calibrated using the PS-DR1 photometric catalog. The Pan-STARRS photometry was converted to the MegaCam photometric system,

$$R.MP9601 = r + 0.002 - 0.017x + 0.0055x^{2} - 0.00069x^{3},$$
(1)

$$R.MP9602 = r + 0.003 - 0.050x + 0.0125x^{2} - 0.00699x^{3},$$
 (2)

GRI.MP9605 = 
$$r + 0.005 + 0.244x - 0.0692x^2 - 0.00140x^3$$
, (3)

where r refers to  $r_{\text{Pan-STARRS}}$  and x = g - i in the Pan-STARRS system. This third-order polynomial expression of color terms in g - i follows the convention in Finkbeiner et al. (2016). The transformation for GRI.MP9605 is only valid for g - i < 1.4. Sources redward of this limit were not used, and only stars (not galaxies) were used. The transformed Pan-STARRS stellar photometry was used to calibrate each CCD of each image separately. Occasionally, the number of stars on a CCD was insufficient to robustly calibrate that CCD. In these cases, the zero point was determined for the focal plane as a whole, and that zero point was applied to the individual CCD. Magnitudes were measured through two circular apertures whose size depends on the seeing; the diameters are  $2\times$  and  $5\times$ the full width at half maximum (FWHM) of the point-spread function (PSF). An average correction of the small aperture to the large aperture is computed for bright stars, and this correction is then applied to the smaller aperture magnitudes.

Stellar catalogs from overlapping images were used to check the photometry. The photometry of two overlapping images was consistent to 0.005 mag for the two r bands, comparable to the quoted accuracy of the PS-DR1 photometry. However, the photometry of the GRI.MP9605 band was found to be good to only 0.02 mag. This is due to two factors. First, the transformation between the Pan-STARRS g, r, and i filters and our wide filter is complex, with nonnegligible scatter. Second, the wide filter causes the PSF to vary depending on the spectral energy distribution of the stars: bluer stars will have larger PSFs, since seeing is worse at blue wavelengths, and DCR (Section 2.8.2) will stretch some stars away from the horizon.

## 2.9. TNO Detection Efficiency

We first consider the total area of sky that OSSOS surveyed. The on-sky footprint of the eight blocks described in Sections 2.1 through 2.6 (Figure 2) is a total of 169.62 deg<sup>2</sup>. The total searched area for OSSOS is 155.3 deg<sup>2</sup>, with a geometry that is summarized in Table 1. This slightly smaller region accounts for both the true pixel area of the MegaCam

field of view and the few incompletely searched chips. Active pixels fill 91.64% of the region inside the outer boundary of the MegaCam mosaic: each of the 36 or 40 chips is  $2048 \times 4612$  pixels, and with the 0.118689 pixel plate scale, the field of view is 0.9164 or 1.018 deg Rare pipeline failures occurred in 1%-2% of cases. They were caused by bright stars or large galaxies that elevated the background light levels and reduced point-source detections to a level that precluded our automated PSF construction process. This rate is consistent with the sky coverage of the background contaminants. The effects are quantified by the "filling factor" in Table 2.

The TNO discovery pipeline and analysis techniques for OSSOS are exhaustively described in Sections 4 and 5 of Bannister et al. (2016b). The depth of each discovery triplet of images was quantified by planting PSF-matched sources in copies of each image at magnitudes  $m_r = 21.0-25.5$ . We planted 44k sources in each of 13AE and 13AO (Bannister et al. 2016b), of order 2 million sources in 13BL and 14BH, 700k sources in 15AP, and 400k sources in 15AM and all 15B blocks. We found empirically that about 10k sources per CCD were required to (a) provide the resolution needed to precisely determine the efficiency as a function of motion rate and (b) accurately measure the pipeline's ability to correctly determine the true flux of a source as a function of magnitude. (Sources were planted and candidates recovered in iterative loops to avoid planting saturation.) This substantial increase in the number of artificial sources meant that we could not vet 100% of all artificial candidates (as was done in Bannister et al. 2016b). Instead, we audited a subset of about 1000 artificial candidates per field (about 20,000 per block). For every frame examined, we performed an audit of the planted sources that we used in calibrating the detection system. These audited sources were treated identically to the detections from the actual data frames and used to verify our planting and search processes. To achieve a precise measurement of the structure of the detection threshold and the fill factor, we use the full sample of planted sources. We conducted tests to ensure that the vetting process did not introduce an additional bias by examining all planted sources for some blocks. These tests revealed that above about the 30% detection threshold (Petit et al. 2004), the vetting process does not remove valid detections. Our quantification of our false-positive rate is detailed in Bannister et al. (2016a, Section 5.1) and was 0 for 13AE and 13AO; in the later six blocks, we also have a negligible false-positive rate. Our falsenegative rate is  $\sim 0.75\%$ . However, the process of vetting all artificial sources did introduce fatigue, which can affect the vetting. The increase in the number of planted sources and subsequent alteration of our review process was the only material change in our detection and tracking process.

OSSOS provides precisely quantified TNO detection efficiencies. The rate of recovery of sources planted in the images as a function of magnitude is modeled by the functional form given in Bannister et al. (2016b):

$$\eta(m) = \frac{\eta_o - c(m-21)^2}{1 + \exp\left(\frac{m-m_0}{\sigma}\right)},\tag{4}$$

where  $\eta_o$  is the peak efficiency, c is the strength of the quadratic drop,  $\sigma$  is the width of the transition from a quadratic to an exponential form, and  $m_0$  is the approximate magnitude of the transition. The peak efficiency  $\eta_o$  is roughly the efficiency at m = 21, in the case where  $\exp((21 - m_0)/\sigma) \ll 1$ . A few of

the efficiency functions could not be fit correctly with the functional form of Equation (4), as the simplex minimization did not converge with the square function. They were instead fit with a double hyperbolic tangent,

$$\eta(m) = \frac{\eta_o}{4} \left[ 1 - \tanh\left(\frac{m - m_0}{\sigma}\right) \right] \left[ 1 - \tanh\left(\frac{m - m_0}{c}\right) \right], \tag{5}$$

as described in Jones et al. (2006) and are marked as such in Table 2. The efficiency function is determined using the intrinsic flux from the source, i.e., the planted source magnitude. The variation in the measured flux from the intrinsic value (caused by noise in the measurement process) is modeled as a function of source flux for each block. This variation is accounted for during our survey simulation process (see Bannister et al. 2016b, Appendix A). For completeness, we list  $m_{50\%}$ , the r-band magnitude at which the efficiency function drops to 50%, which was often used in earlier surveys. However, the key limiting magnitude used throughout OSSOS is instead  $m_{\text{limit}}$ , the slightly deeper, but no fainter than  $m_{40\%}$ (Petit et al. 2004), characterization limit: per Bannister et al. (2016b), "the magnitude above which we have both high confidence in our evaluation of the detection efficiency, and find and track all brighter objects." The efficiency function parameters are given for all of OSSOS in Table 2 and are distributed in machine-readable form in our Survey Simulator (see Section 4).

Detectability and the effective area of survey sky coverage are a function of the distant minor planets' sky motion rate. For each block, we report multiple efficiency curves in Table 2, each for a range of rate of motion. These different efficiency curves account for the changes in effective area, as fastermoving objects are more likely to shear off a given chip between the exposures of the discovery triplet. This produces a variation in area coverage as a function of rate, which is only  $\sim$ 2% less for motion rates >10" hr<sup>-1</sup>. The flux limit for each rate is also different: trailing of fast-moving objects makes the flux sensitivity poorer, as the source is spread over more pixels in each exposure, pushing faint sources into the noise. We set an upper limit of  $15'' \,\mathrm{hr}^{-1}$ , as the survey's focus is on discoveries at heliocentric distances ≥10 au; at rates faster than this, the object would also feature significant trailing within an exposure, causing reduced detection efficiency (partly due to reduced signal-to-noise and partly due to our pipeline being optimized for roughly circular sources). The survey simulator (Section 4) accounts for this variation in sensitivity as a function of TNO sky motion rate.

## 2.9.1. TNO Tracking Efficiency

Our detected and tracked sample is a fair representation of the orbital distribution in the Kuiper Belt. Of the 840 TNOs brighter than the characterization limit, 99.8% were recovered outside of their discovery triplet and tracked to fully classifiable arcs (Section 3.3).

All of the  $\sim$ 37,000 tracking observations that comprise the arcs were individually inspected. Aperture photometry was measured with daophot (Stetson 1987) with a typical 4–5 pixel aperture, corrected to a 20–25 pixel aperture using bright-star aperture corrections, and the sky measured in a 10 pixel

wide annulus with an inner edge of about 30 pixels. While all images are calibrated to Pan-STARRS/*Gaia* (Section 2.8.3) and standard MPC flags<sup>29</sup> were assigned throughout to indicate any photometric irregularities, the arc measurements were optimized for astrometry rather than precision photometry. Thus, care should be taken if using the bulk arcs to infer TNO light curves or variability.

The superlative tracking fraction removes ephemeris bias from the survey. Only two detections could not be tracked, both with estimated distances interior to 20 au: o5p002nt and o5s03nt in Table 3 (characterized). These two detections are brighter than the characterization limit and have rates of motion within the survey limits; i.e., they are characterized discoveries. The loss of these two objects is not magnitude-dependent. Both moved onto the corner of their blocks only during the night of the discovery triplet, so there were no additional observations with which to track them. The loss of these two objects is accounted for using the rate-dependent tracking fraction parameter in our survey simulator (Section 4), which applies an accurate reproduction of the OSSOS survey tracking success.

#### 2.9.2. Sensitivity as a Function of Heliocentric Distance

The maximum distance sensitivity of a survey is set by the temporal spacing of the discovery exposures, the elongation of the target field, and the length of the exposures. For OSSOS, it varies across the range of blocks: each has a unique set of delays between our three exposures and a unique field elongation. Additionally, the trailing of sources results in poorer sensitivity to fast-moving sources (i.e., inside 20 au distance). To determine our distance sensitivity, we examine the efficiency curves for the slowest rate bin for each block (Table 2). The 0.75 hr<sup>-1</sup> threshold to which we search implies a detectable distance limit of  $\sim$ 300 au. However, taking flux into account, our 50% threshold for large  $H_r = 4$  TNOs ranges between a detectable distance of 100 au for 13AE and 130 au for 15BD. Having considered temporal spacing/elongation and flux, we additionally take into account the steep size distribution of TNOs. In our sample, we have few detections beyond 60 au. Our most distant detection was at 82.5 au,  $H_r = 5.6$ , in 15BC (Figure 1). One might be inclined to infer that this indicates an intrinsic lack of TNOs between 60 au (our decrease in detections) and 100 au (our practical limit for detection of TNOs with  $H_r > 4$ ). However, in the entire OSSOS survey, we have only 2% of our sample drawn from objects with  $H_r < 6$  and only one object with  $H_r < 4$  (Table 3). Thus, our lack of distant >60 au detections is more a manifestation of the steep luminosity function of TNOs and the area coverage of OSSOS than of our flux or rate of motion sensitivity.

## 2.9.3. Sensitivity to Retrograde Orbits and Interstellar Objects

The OSSOS detection pipeline efficiency is independent of the nature, Sun-bound or interstellar, of the trajectories of the minor planets in the field of view. The detection process is driven only by the angular rate and direction of each source on the sky. We consider in turn the cases of retrograde orbits and interstellar trajectories.

For both retrograde and prograde orbits bound to the solar system, the component of reflex motion from the Earth's orbital

 Table 3

 Description of the Survey Discovery Catalogs

Description

Column Name

Unit

Table: Characterized OSSOS minor planets (840 rows)

Table: Uncha	aracterized OSSOS	6 detections (109 rows)
		ed minor planets from four surveys (1142 rows)
cl		Orbital population/class
p		Additional class-dependent detail
j		Resonant object is in the <i>j:k</i> resonance
k		Resonant object is in the $j:k$ resonance
sh		Orbit classification status (secure/insecure)
object		Survey object designation
mag	mag	Mean magnitude during the discovery triplet, excluding flagged observations
$mag_e$	mag	Uncertainty in mag
Filt	mug	Filter used in discovery observation
$H_{\rm sur}$	mag	Surmised absolute magnitude <i>H</i> , in discovery
11 Sur	mug	filter
dist	au	Object distance at discovery
$\operatorname{dist}_e$	au	Uncertainty in dist.
$N_{ m obs}$		Number of observations available
time	yr	Length of measured orbital arc
$av_{xres}$	arcsec	Mean orbit-fit residual, R.A.
$av_{yres}$	arcsec	Mean orbit-fit residual, Decl.
$\max_x$	arcsec	Maximum orbit-fit residual, R.A.
$\max_y$	arcsec	Maximum orbit-fit residual, Decl.
a	au	Semimajor axis
$a_e$	au	Uncertainty in a
e		Eccentricity
$e_e$		Uncertainty in e
i	deg	Inclination to the ecliptic
$i_e$	deg	Uncertainty in i
Ω	deg	Longitude of ascending node
$\Omega_e$	deg	Uncertainty in $\Omega$
$\omega$	deg	Argument of perihelion
$\omega_e$	deg	Uncertainty in $\omega$
$T_{ m peri}$	days	Modified Julian Date of osculating perihelion passage
Tperi <sub>e</sub>	days	Uncertainty in tperi
R.A.	deg	Right ascension (J2000) at mean time of discovery
Decl.	deg	Declination (J2000) at mean time of discovery
JD		Central Julian Date of first discovery image
Rate	arcsec hr <sup>-1</sup>	Angular rate of sky motion at discovery
MPC		MPC object designation (packed format)
		c coject designation (packed format)

**Note.** All orbital elements are J2000 ecliptic barycentric coordinates. MPC packed format is defined at <a href="http://www.minorplanetcenter.net/iau/info/PackedDes.html">http://www.minorplanetcenter.net/iau/info/PackedDes.html</a>. (This table is available in its entirety in FITS format.)

velocity dominates the direction of sky motion in our imaging. Orbits that are retrograde will move about 10% faster on the sky than prograde TNOs at the same distance. Our coverage both before and after the discovery night provides tracking that covers all possible orbit motion ranges, removing nearly 100% of ephemeris bias. Of our detected sources brighter than our characterization limit, 99.8% were tracked to full orbits, and the 0.2% tracking loss rate of very close objects was not due to orbit assumptions (Section 2.9). Thus, although none of the minor planets that we detected were on retrograde orbits, we can conclude that if such objects had been present in our fields and fell inside our rate and direction cuts, we would have detected and tracked them. We note that our algorithm

<sup>&</sup>lt;sup>29</sup> minorplanetcenter.net/iau/info/ObsNote.html

continues that of CFEPS, which detected the first retrograde TNO (Gladman et al. 2009). Because we chose the ensemble of rates and directions to cover all bound solar system orbits beyond  $\sim \! 10$  au, we are confident that no retrograde orbits brighter than our survey limits were within our detection volume. An upper limit for the retrograde population could be created, which would be highly dependent on the assumed distribution of a, q, and H, and we defer that to future work.

OSSOS has less sensitivity to unbound interstellar interlopers like 1I/'Oumuamua (Meech et al. 2017). Interstellar objects have very large heliocentric velocity vectors; cf. the 26 km s<sup>-1</sup> of 1I/'Oumuamua. For most of the part of their inbound and outbound trajectory when they are close enough to be brighter than our flux limit, unbound orbits could be moving in almost any direction on the sky. Thus, interstellar objects would mainly be outside our rate cuts, though they could be detectable if within our rate cuts.

### 3. Discoveries

OSSOS detected 949 objects within the eight survey blocks. We present the catalog of their discovery and orbital properties in three machine-readable tables, which are separated by their quality of usefulness as samples for modeling the structure of the outer solar system. The content of each table is summarized in Table 3. In the following section, we discuss the quality of our TNO orbits and their classification into different dynamical populations, including the small fraction of our discoveries that were linked to previously known objects.

## 3.1. Discoveries to Use for Testing Models

The OSSOS primary discovery set is 840 TNOs, given in the catalog described in Table 3: characterized OSSOS minor planets. These minor planets were found at brightnesses and rates of sky motion that mean that they have fluxes brighter than our tracking limit, with well-quantified detection efficiencies. (This includes two close objects that were not tracked; see Section 2.9). The characterized discoveries are the set that should be used for modeling solar system structure. We summarize their orbital populations in Table 4.

# 3.2. Discoveries with Poorly Determined Discovery Efficiency and Some Incomplete Tracking

For completeness, we list all 109 remaining detections in the catalog referenced in Table 3 as uncharacterized OSSOS detections. In this machine-readable catalog, there are three TNOs that have detection efficiencies that are quantifiable but differ from the efficiencies provided here for the main survey. They are designated with the prefix Col3N and were fast-moving discoveries in the incomplete first attempt at a discovery triplet on the 14BH block in 2013 (Section 2.2).

Table 3 (uncharacterized) also catalogs 106 TNOs from all blocks that are designated with the prefix u. These exceptionally faint objects have a detection efficiency that is poorly quantified, as their faintness at discovery placed them below their block's rate-of-motion-dependent characterization limit. The uncharacterized objects are severely afflicted by unquantifiable observational biases. The lack of quantified detection efficiency means that the only aspect of the tracked, uncharacterized TNOs that we can be sure of is their orbits. Of the uncharacterized TNOs, 21 could not be tracked beyond the  $\sim$ 2 hr arc of their discovery triplet; these are designated

 Table 4

 Orbital Populations of the Characterized Discoveries of OSSOS

Dynamical				
Class	a (au)	Secure	Insecure	Comments
Jupiter-coupled		5	0	q < 7.35 au and
				$T_j < 3.05$
Centaur	a < 30	15	0	Insecure one
				is nt
Scattering		29	9	$\delta a > 1.5$ au in
				10 Myr
Inner-belt	a < 39.4	11	0	
Main-belt	39.4 < a < 47.7	391	30	
Outer-belt	a > 47.7	4	0	e < 0.24
Detached-	a > 47.7	10	21	e > 0.24
component				
Total		465	60	+2 nt
nonresonant				discoveries

Neptune M	ean-motion Reso	nant (n:m) O	rdered by	Increasing a
1:1	30.1	4	0	Neptune Trojan
4:3	36.4	10	0	
3:2	39.4	131	1	
5:3	42.3	13	1	
7:4	43.7	31	8	
9:5	44.5	1	1	
2:1	47.7	34	0	
5:2	55.4	17	3	Volk
				et al. (2016)
3:1	62.5	6	1	
7:2	69.3	1	1	
4:1	75.7	1	2	
9:2	81.9	0	1	Bannister et al. (2016a)
5:1	87.9	0	1	
9:1	130.1	2	0	Volk
				et al. (2018)
Others		19	23	
Total resonant		270	43	
Total (all)		735	103	+2 nt discoveries

**Note.** Classifications similar to those in Gladman et al. (2008), with the difference that resonant status is declared if the best-fit clone resonates even if the two extremal clones do not. We check all objects thoroughly for meanmotion resonances with Neptune; we additionally check low-a objects for 1:1 mean-motion resonances with Saturn and Uranus. The semimajor axes given for resonances are approximate.

with the suffix nt. It is possible that some of the untrackable nt sample may actually be false positives; see Section 5.1 of Bannister et al. (2016b) for an evaluation of the false-positive rate of our analysis. We recommend exceptional caution in any use of the Table 3 uncharacterized TNOs and strongly advise against simply combining them with the characterized discoveries when modeling solar system structure.

### 3.3. Orbit Quality and Population Classifications

To fully exploit the discovery of a TNO, we must know both its discovery circumstances and its precise orbit. Extensive tracking is often required before such precise orbits can be determined; this is especially critical for resonant objects. The resonant orbits require extreme orbital precision (fractional semimajor axis uncertainty roughly <0.01%) in order to

determine the resonance libration amplitude, which is a diagnostic of the resonance capture mechanism. An additional classification to those in Bannister et al. (2016b) is for Jupiter-coupled objects; these are defined by a combination of perihelion distance and Tisserand parameter,

$$T_J = a_J / a_{\text{TNO}} + 2\sqrt{(a_J / a_{\text{TNO}})(1 - e_{\text{TNO}}^2)} \cos(i_{\text{TNO}}).$$
 (6)

We do not attempt orbital classifications for the nt discoveries or objects with an arc only within their discovery lunation.

As described in Bannister et al. (2016b), we classify the TNOs into different dynamical populations (Gladman et al. 2008) based on a 10 Myr integration of clones of the best-fit orbit and two extremal orbits, which are determined from the available astrometry using the orbit-fitting method of Bernstein & Khushalani (2000). When all three clones show consistent dynamical behavior, we declare the object's classification to be secure. Precisely determining how long an observing arc, or the frequency of observations, is required to secure an orbit is not strictly possible because it depends on the TNO's dynamical behavior. The trans-Neptunian region is riddled with chaos and complex boundaries in orbital phase space. Orbits near the boundaries of resonances must be very precisely determined before the dynamical evolution can be accurately presented. In contrast, secure classifications for orbits farther from the resonance boundaries can be achieved with less precision. We do not know in advance where a given object's orbit is relative to these boundaries.

The high-precision and well-sampled tracking of OSSOS has allowed 734 of the 840 characterized orbits to be securely classified with the arcs we present here. This is summarized by population in Table 4. Additional arc was required to further refine the orbits for some insecurely classified objects. The orbits of the o3e and o3o TNOs that were initially reported in Bannister et al. (2016b) now have an additional two oppositions of more sparsely sampled OSSOS arc and accordingly updated classifications. Once an object was securely classified, we discontinued target tracking (occasionally, further serendipitous observations may have occurred, which we measure and include; see Section 2).

At the completion of the 2013–2017 observations, 103 characterized discoveries with well-observed arcs remain insecurely classified. The chaotic nature of the resonance boundaries means these objects' dynamical classifications might never become secure, because they transition between resonant and nonresonant behavior during the 10 Myr of the classification integration.

#### 3.4. Previously Discovered TNOs

Fewer than 3% of the OSSOS discoveries were previously known, largely because of the greater depth of OSSOS compared to previous wide-field surveys. We designate 23 TNOs in Table 3 (characterized OSSOS) with the suffix PD, which indicates that during their tracking (Section 2), we made use of available pre-OSSOS astrometry to assist in securing their orbits. Pre-OSSOS astrometry was located in two ways. After the discoveries from each block were made, we checked against the predicted location of all MPC-listed TNOs that were within the sky coverage. We also tested for linkages to the short-arc discoveries by CFEPS (Petit et al. 2011).

There are OSSOS objects with pre-OSSOS data that we do not designate as PD. Several OSSOS discoveries were

subsequently given MPC designations earlier than 2013–2015 on submission, due to linkages that the MPC was able to provide to unlisted or exceptionally sparse earlier astrometry, e.g., o3128 (2006 QE<sub>181</sub>). These do not have the suffix PD. Additionally, some objects were independently discovered during our survey. Object o3139 (2016 BP<sub>81</sub>) was found in *Kepler* space telescope observations of the K2 Campaign 8 superstamp field of Uranus (Molnár et al. 2018), and o3118 (2010 RE<sub>188</sub>) was reported by Pan-STARRS (Holman et al. 2015; Weryk et al. 2016). The orbits of these TNOs were already securely classified with our observed arcs by the time the other astrometry became available, and we do not designate them with PD.

The high cadence and astrometric precision of OSSOS maintains our sample uniformity across all our discoveries, including those designated PD. We tested for the effect of the prior astrometry on our classifications by integrating our arcs both with and without the earlier observations. Our orbital classifications are independent of the possibility that an object might be a PD: no classifications changed in class, though a few shifted between secure and insecure. Note that none of the PD objects are on high-perihelion, exceptionally large-a orbits (Section 5.4), where instead the observed length of arc would become the dominant source of orbital uncertainty. The PD TNOs are consistent in quality with the rest of the data set, rather than exhibiting greater orbital precision. This held true even in cases where the earlier astrometry extended the orbital arcs to a decade or more in length.

Our linkages to earlier discoveries show that for sparsely sampled arcs, even multi-opposition orbits in the MPC are sometimes misleading. An interesting case is o5p064PD (2001 FL<sub>193</sub>). The 2001 discovery by the Deep Ecliptic Survey (Elliot et al. 2005) was with a pair of observations on March 27 and 28. Fourteen years later, 2001 FL<sub>193</sub> was recovered in three single observations in 2015 by the Dark Energy Survey (Gerdes et al. 2017). Having only six measured points defined 2001 FL<sub>193</sub>'s orbit with high uncertainty, despite its 14 yr arc. The orbit was a rare low-inclination,  $a \sim 50$  au, outer-belt TNO beyond the 2:1 (see Table 6 of Bannister et al. 2016b). The OSSOS discovery o5p064PD links back to this previous data. However, we find instead that o5p064PD = 2001 FL<sub>193</sub> is correctly on an a = 43.1 au, e = 0.04, i = 1.8 orbit, which is that of a standard cold classical TNO.

A few MPC-listed objects were nominally within our coverage but fell in chip gaps during our discovery observations (e.g., 2000 FA<sub>8</sub> was in a chip gap during the 2015 April 12 discovery observations for the 15AP block). We recovered and reported astrometry where these TNOs were serendipitously included in our tracking observations.

# 4. The Survey Ensemble: A Framework for Testing Models of the Solar System's Dynamical History

We provide a survey simulator,<sup>30</sup> described in detail in Bannister et al. (2016a, Section 5.2), that can assess model trans-Neptunian populations against the OSSOS orbit sample. With this piece of software, one can take a model of the outer solar system and submit it to an observed survey's detection characterization. The model needs to provide a set of small outer solar system bodies defined by their orbital elements and

<sup>&</sup>lt;sup>30</sup> doi:10.5281/zenodo.591435; ongoing development and the most recent survey files are at https://github.com/OSSOS/SurveySimulator.

physical characteristics, e.g., intrinsic absolute magnitude and colors.

The survey simulator allows the user to model multiple well-characterized surveys performed using up to 10 different filters, as well as populations of objects that may vary in color (Bannister et al. 2016b). Each model object given to the survey simulator needs to be specified with its intrinsic absolute magnitude, given in a bandpass filter, X, and an array of colors between the various survey filters that each survey used and the reference X band. Thus, the variation of colors inside and across the various dynamical populations can be modeled when combining surveys performed through different filters.

For each object, the survey simulator computes the object's position in the sky, its apparent motion, and its apparent magnitude, accounting for the Poisson noise in the measured flux. The survey simulator models the observing conditions (IQ, attenuation, star crowding) through the use of the detection efficiency function (Section 2.9). Then it decides if the object was detected and tracked, determining what a given survey would have detected had the outer solar system been the model. The orbital and physical characteristics of the model "detections" can then be compared to the discovered TNO sample to assess the viability of the model.

In a previous version of the survey simulator, we used rectangles with edges along the R.A. and decl. axes to describe the footprint of the blocks on the sky, which was appropriate for the R.A.—decl. grid-aligned survey blocks of CFEPS and A16. We had to balance between the number of rectangles (more rectangles slow down the computation) and the accuracy of the simulation (fewer rectangles imply less accurate representation of a nonrectangular shape). We now describe the footprint of the blocks by polygons; the areas are given in Table 1. This allows us to accurately represent the shape of the observed region while still being numerically efficient. The shape accuracy is particularly important for large, staggered blocks like those in OSSOS that straddle the plane of the Kuiper Belt.

The simulator that we provide here includes four characterized surveys with well-measured discovery biases (Table 5): CFEPS, HiLat, A16, and OSSOS, all made with CFHT's MegaCam. Only the colors g-X, r-X, and R-X need to be specified to the simulator when modeling this full set of surveys, and only r-X when modeling OSSOS, HiLat, and A16. The "ensemble" of surveys covers in total 1224 deg<sup>2</sup> of sky, at a wide range of ecliptic latitudes and longitudes, to depths of  $m_r = 23.5-25.2$ . There are 1142 TNOs in the ensemble discovery sample from a wide range of TNO dynamical populations. We provide them in the same format as for the OSSOS discoveries (Table 3). They are collated in the catalog referenced in Table 3 as the ensemble. This is by far the largest sample with quantified biases currently available for investigating the structure of the trans-Neptunian populations. We observed the insecurely classified TNOs from the earlier surveys several times during the observations of OSSOS, which has improved some of the orbital classifications from those at the time of their discovery surveys' publication. In the six cases where TNOs from earlier surveys in the ensemble were rediscovered by OSSOS, they are listed twice in Table 3: ensemble, in both cases with the OSSOS object designation.

Future characterized surveys can easily be added to the simulator. We provide an example template in the

Table 5
The Ensemble of Surveys Described by the OSSOS Survey Simulator

Survey	Bandpass	Characterized Detections
CFEPS <sup>a</sup>	G.MP9601	210
HiLat <sup>b</sup>	R.MP9601	21
A16 <sup>c</sup>	R.MP9601	77
OSSOS	R.MP9601/R.	840
	MP9602	
Total (distinct detections)		1142

**Notes.** There are six characterized detections in CFEPS that were refound in OSSOS. All detections are provided in the machine readable catalog of Table 3: ensemble.

Supplementary Materials for the formatting of the characterization information and TNO discovery sample.

# 5. An Overview of the Trans-Neptunian Populations from Characterized Discoveries

The orbits of our discoveries reveal new and complex detail in the known trans-Neptunian populations. Here we provide a broad overview of the strengths of the OSSOS sample relative to that present in the MPC. Where relevant, we consider the sample available by combining the characterized discoveries of four surveys (all available in the survey simulator): CFEPS, HiLat, A16, and OSSOS, which we refer to as the "ensemble" (Section 4). We focus on the dynamical properties of the characterized ensemble sample (Table 3), which is graphically presented in Figures 4 and 5. We also draw attention to individual OSSOS objects on unusual orbits (Sections 5.2.1 and 5.4).

## 5.1. Minor Planets on Transient Orbits

The Centaur (a < 30 au) population and the  $q \lesssim 30$  portion of the scattering population undergo strong gravitational interactions with the giant planets, making them an unstable, transient population. The larger q portion of the scattering population also interacts with Neptune and undergoes significant orbital evolution as a result, but the more distant encounters allow for longer dynamical lifetimes. These unstable orbits are a mixture of a slowly decaying remnant of a vast population emplaced early in the solar system's history when the Oort cloud was built and a steady-state intermediary population leaking from a more stable Kuiper Belt or Oort cloud reservoir (Duncan & Levison 1997; Gomes et al. 2008; Dones et al. 2015). OSSOS provides 21 objects classed as Jupiter-coupled and Centaurs, and 38 scattering TNOs. Shankman et al. (2016) considered the size distribution of the scattering TNOs using 22 objects: 13 from CFEPS, two from A16, and the first seven OSSOS scattering discoveries. The available ensemble sample has now more than doubled. Lawler et al. (2018b) and Shankman (2017) found a break in the scattering size distribution and an intrinsic population of  $9 \times 10^4$  for  $H_r < 8.66$  (D > 100 km), with the Centaur population two orders of magnitude smaller at 111<sup>+59</sup><sub>-44</sub> (Lawler et al. 2018a).

<sup>&</sup>lt;sup>a</sup> Jones et al. (2006), Kavelaars et al. (2009), Petit et al. (2011).

<sup>&</sup>lt;sup>b</sup> Petit et al. (2017).

<sup>&</sup>lt;sup>c</sup> Alexandersen et al. (2016).

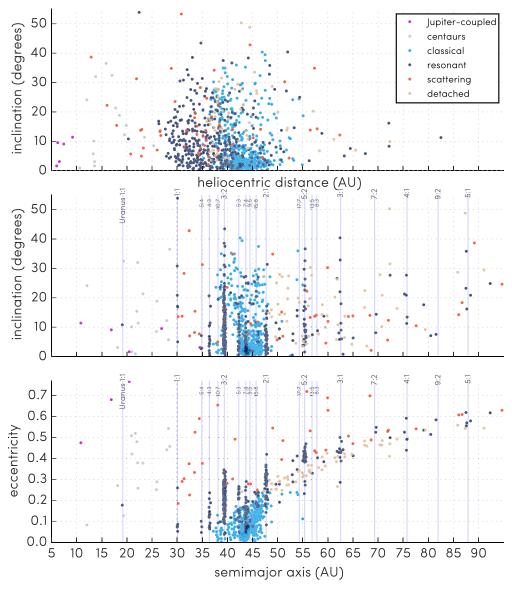


Figure 4. Orbital parameters and discovery distances of the 1142 characterized minor planets from the four surveys of the ensemble, OSSOS, CFEPS, HiLat, and A16 (Table 3: ensemble), displaying the subset with parameters within these a/e and a/i axis ranges. All uncertainties are smaller than the point size. The pale blue vertical lines show the approximate semimajor axis locations of the resonance centers for resonances with detections.

## 5.2. The Nonresonant TNOs

The OSSOS survey has acute sensitivity to all objects exterior to the orbit of Saturn and thus provides a strong sampling of the inner-belt component of the TNO population in 37 au  $\lesssim a \lesssim 39$  au. OSSOS detected 11 inner-belt TNOs above our characterization thresholds. Given our thorough ability to detect objects interior to 37 au and the complete absence of nonresonant/nontransient objects in the range 30 au < a < 37 au, we find that the present-day inner belt does not extend inward of  $a \sim 37$  au (Figure 5, top left). It is noteworthy that the strong lower perihelion bound of  $q \sim 35$  au is consistent across the entire Kuiper Belt. Only one TNO with a semimajor axis in the region  $36 \,\mathrm{au} < a < 48 \,\mathrm{au}$  has a perihelion dipping just below, to q = 34.6 au (Figure 5, top left). The main structure visible within the inclination distribution in the inner belt is that of the  $\nu_8$  secular resonance, which destabilizes orbits in this semimajor axis range that have  $i \lesssim 15^{\circ}$  (Kavelaars et al. 2009). After accounting for this instability zone, the distribution of inner-belt inclinations

continues to be consistent with being drawn from the same dynamically excited population as is present in the main belt. Further examination of the architecture of the inner belt and its relation to the main belt (J.-M. Petit et al. 2018, in preparation) is likely to provide significant insight into the processes that resulted in the currently observed structure (e.g., Nesvorný 2015b).

As of 2016 October, the MPC listed 484 TNOs with arcs where orbits as fit showed no resonance, with 42 au < a < 48 au and  $\sigma_a <$  5%, from surveys other than those in the ensemble (Volk & Malhotra 2017). The ensemble presented here has 530 such main-belt objects, of which 421 are from OSSOS, and they have  $\sigma_a <$  0.1%; the orbital precision is substantially better, allowing for much more secure dynamical classifications. We show these in Figure 5. In the main belt, even the first two blocks of OSSOS were able to independently confirm the existence of the cold classical "kernel" (Bannister et al. 2016b), which was first described in Petit et al. (2011). With the full ensemble sample, the kernel is starkly visible in Figure 5. The tight parameter space of the kernel constrains the processes that are

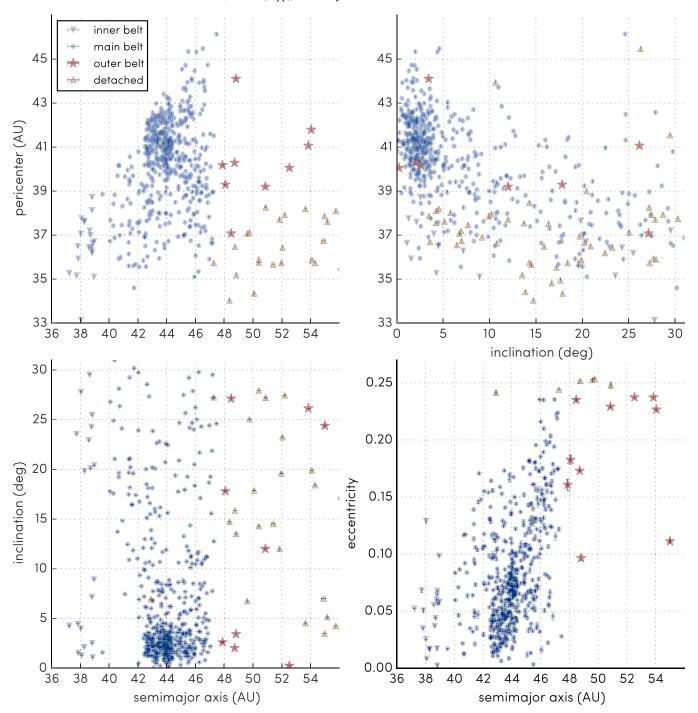


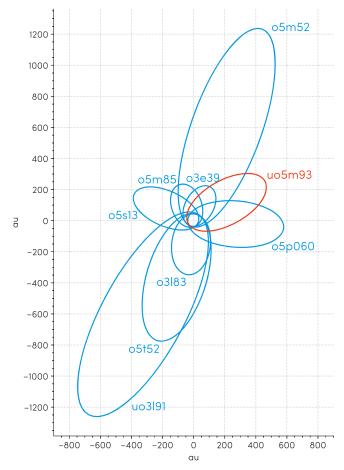
Figure 5. Nonresonant Kuiper Belt and detached component as observed by the four surveys of the ensemble: OSSOS, CFEPS, HiLat, and A16 (Table 3: ensemble). Inner, main, and outer Kuiper Belt and detached TNOs are distinguished by symbol shape based on their orbital classifications (Section 3.3). The main Kuiper Belt (blue circles) shows a strong concentration of low-i orbits with  $a \simeq 44$  au, a feature known as the kernel (Petit et al. 2011; Bannister et al. 2016b). The outer belt (red stars) continues at low inclinations beyond the 2:1 mean-motion resonance with Neptune ( $a \sim 47.7$  au). All orbital elements are barycentric, with  $1\sigma$  uncertainties shown.

viable candidates for its sculpting out of the primordial disk (Gomes et al. 2018) or its emplacement (Nesvorný 2015a).

# 5.2.1. The Cold Classical Population Extends Beyond the 2:1 Resonance with Neptune

OSSOS confirmed that the cold classical population extends beyond the 2:1 resonance (Bannister et al. 2016b), which places a significant new condition on the creation or emplacement of low-inclination orbits in this region. Only six TNOs are known in this elusive population. The ensemble

sample has four outer-belt objects that orbit on inclinations of only a few degrees, with q>40 au and semimajor axes beyond the 2:1 mean-motion resonance with Neptune: 0.3e45, 0.4h47, 0.5d115PD from OSSOS, and 2011 US<sub>412</sub> from A16 (Figure 5). The other nonresonant outer-belt TNOs just beyond the 2:1 have more substantial inclinations of  $12^{\circ}.7-36^{\circ}$  (Figure 5). We rediscovered two previously known TNOs related to this low-inclination population. OSSOS confirms the outer-belt orbit of 0.5d115PD, which is (48639) 1995 TL8, and rules out that of 0.5p0.64PD (2001 FL193); it is instead a standard main-belt cold classical (see Section 3.4). The others



**Figure 6.** Ecliptic plane projection of the orbits of the nine q>30, a>150 au TNOs discovered by OSSOS. The biases affecting discovery of the distant TNO population in OSSOS are quantified in Shankman et al. (2017), which lists the TNOs with orbits in blue. Newly reported in this work is uo5m93 (orbit in red), in Table 3: catalog of uncharacterized OSSOS discoveries. These nine TNOs are consistent with being detected from a distribution of orbits that are intrinsically uniform in the angles  $\omega$  and  $\Omega$ .

listed in the MPC are 2003 UY<sub>291</sub> (Gladman et al. 2008) and 2012 FH<sub>84</sub> (Sheppard et al. 2016). We report a new member of the outer belt. With  $i=3^{\circ}.4$  and a=48.83 au, q=44.10 au, 04h47 is indisputably linked to the cold classical population. It has the lowest eccentricity and highest perihelion yet seen for a cold classical beyond the 2:1 (see Table 6 of Bannister et al. 2016b).

## 5.2.2. The Detached Component

The a>50 au OSSOS sample is particularly valuable due to the exceptional certainty of its orbit classifications. In the range 50 au  $\leqslant a \leqslant 150$  au, there are 135 apparently nonresonant TNOs with da/a < 5% orbits in the MPC from other surveys. This contrasts with 76 in the ensemble, 48 of which are from OSSOS. A major nonresonant a>50 au population is on orbits that are detached: stable, with large a and e, but with perihelia large enough that they are not now strongly interacting with Neptune. The exact perihelion distance required to prevent significant orbital evolution due to distant encounters with Neptune depends on semimajor axis, so classification as "detached" can only be determined by numerical integration (Lykawka & Mukai 2007; Gladman et al. 2008). OSSOS provides 31 TNOs orbiting in the detached component (those

with a below the limits of the axes are shown in Figure 4). The fractional increase in the nonresonant a > 50 au sample from OSSOS is less pronounced than it was for the nonresonant Kuiper Belt. However, the OSSOS sample is far more secure than the MPC TNOs in this range; it is entirely possible that many objects listed in the MPC are inaccurately classified as nonresonant due to their low-precision orbits. Additionally, the ensemble sample has well-characterized biases, which is particularly important for the large-a population.

#### 5.3. Resonant TNOs

OSSOS provides a substantive additional sample of TNOs in mean-motion resonances with Neptune (Figure 4). The four new and secure Neptune Trojans from OSSOS exhibit the known wide range of inclinations of this population (Chiang et al. 2003; Sheppard & Trujillo 2006, 2010; Parker et al. 2013; Alexandersen et al. 2016), discussed further in H. W. Lin et al. (2018, in preparation). A spectacular 132 plutinos (3:2 resonance) dominate the resonant detections of OSSOS; combined with the survey simulator, the detailed debiased distribution will provide the information needed to study and constrain resonance capture conditions and plutino mobility over the age of the solar system (K. Volk et al. 2018, in preparation).

Observational biases make the TNOs in more distant resonances progressively harder to detect, as they spend a larger fraction of each orbit at greater heliocentric distances, where they are fainter. For example, OSSOS found only 34 TNOs in the 2:1 resonance. However, early OSSOS findings support earlier findings that the total population in the more distant resonances may rival or exceed those of the nonresonant Kuiper Belt (Gladman et al. 2012). Volk et al. (2016) found that the OSSOS o3e and o3o discoveries imply that the 5:2 resonance ( $a \sim 55$  au) is much more heavily populated than had previously been suggested from migration models. The significant number of objects OSSOS has observed in some of the resonances will enable detailed modeling of their dynamical structure and relative populations, providing detailed constraints on Neptune's migration history. For example, the o3e and o3o discoveries confirmed that the objects in the 2:1 have a colder inclination distribution (Gladman et al. 2012) than the population of objects in the 3:2 (Volk et al. 2016). This is now visually obvious in Figure 4 and is discussed further in Y. T. Chen et al. (2018, in preparation).

The number of distant resonant objects beyond the 2:1 listed in the MPC from other surveys is  $\sim$ 103, contrasting with 68 in the ensemble, of which 48 are from OSSOS. Table 4 highlights that OSSOS provides the first TNOs found in a number of distant resonances. These include occupancy in the  $a\sim$ 82 au 9:2 resonance and the most distant securely resonant TNOs yet seen, in the  $a\sim$ 130 au 9:1 resonance (Volk et al. 2018). OSSOS has also found additional TNOs in other rarely seen distant resonances: seven in the 3:1 and three in the 4:1 resonances (Chiang et al. 2003; Alexandersen et al. 2016). The largest TNO found by OSSOS, the  $H_r$  = 3.6  $\pm$  0.1 dwarf planet candidate  $\circ$ 5  $\circ$ 68 (2015 RR<sub>245</sub>), is in the 9:2 resonance (Bannister et al. 2016a); its long-term behavior suggests that a large metastable population is cycling between the scattering population and high-order resonances.

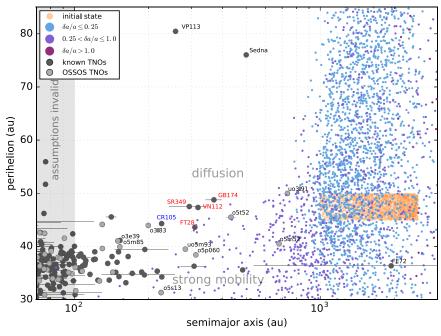


Figure 7. Semimajor axis evolution demonstrating diffusion in large-a TNOs with  $q \lesssim 50$  au, updated from Figure 5 in Bannister et al. (2017). Known TNOs are shown with OSSOS discoveries (light gray) and the multi-opposition MPC TNOs (dark gray), together with the outcome of a model simulating a Gyr of evolution of particles started on orbits in the inner Oort cloud (start: orange; outcome: blue through purple). The nine q > 30, a > 150 au OSSOS TNOs are named, as are the relevant MPC TNOs; 2000 CR<sub>105</sub> (name shown in blue) is in a high-order resonance, while the four red-labeled MPC TNOs exhibit diffusion in the integrations in Bannister et al. (2017).

## 5.4. Extreme TNOs

The OSSOS discoveries include nine TNOs with q > 30 au and a > 150 au, eight of which have q > 38 au. Their orbits are shown in Figure 6. Pronounced biases affect the discovery of minor planets on such distant orbits; the sensitivity of OSSOS to this population is quantified in Shankman et al. (2017). There has been recent interest in the apparent angular clustering of the MPC-listed TNOs with a > 150 au orbits, which some have hypothesized as evidence for a massive distant planet (Trujillo & Sheppard 2014; Batygin & Brown 2016). The sensitivity of OSSOS was applied to a distribution of simulated orbits that are uniform in their angles  $\omega$ ,  $\Omega$ , and  $\varpi$  to test if the detected OSSOS sample is consistent with being drawn from a uniform distribution. In an analysis of the orbit distribution of the first eight of these TNOs, Shankman et al. (2017) found that the OSSOS sample is consistent with being detected from that uniform distribution.

We report a new minor planet in the  $q>30\,\mathrm{au}$ ,  $a>250\,\mathrm{au}$  population. The TNO uo5m93, an object in the uncharacterized OSSOS sample (Table 3), was eventually tracked to a well-sampled four-opposition arc and found to have an orbit with  $q=39.5\,\mathrm{au}$  and  $a=283\,\mathrm{au}$  (Figure 6). Thorough inspection of the complete detection sample has minimized the possibility that any further  $q>30\,\mathrm{au}$ ,  $a>150\,\mathrm{au}$  orbits remain concealed among the OSSOS nt discoveries: fewer than 16 (with  $d>30\,\mathrm{au}$ ) of the 111 uncharacterized objects were untrackable (see Table 3: uncharacterized, nt designations). The spatial orientation of uo5m93's orbit lies in an angular direction that is distinct from the hypothesized clustering, further weakening the evidence for a lurking presence of intrinsic angular clustering.

Although this object is from the uncharacterized part of the sample, where our completeness limits are less well known, we reperformed the full statistical analysis of Shankman et al.

(2017); the results are unchanged, and the OSSOS q > 30 au, a > 150 au nine-TNO sample is still consistent with being detected from a distribution of orbits that are intrinsically uniform in the angular elements.

Formation mechanisms for this distant population are not yet clear, and it remains an area of active investigation (e.g., Lawler et al. 2016; Nesvorny et al. 2017). However, all of the extreme TNO discoveries of OSSOS are consistent with a formation by random diffusion in semimajor axis due to weak kicks at perihelion by Neptune from orbits with semimajor axes in the inner fringe of the Oort cloud, as proposed in Bannister et al. (2017). This is shown in Figure 7, which updates Figure 5 in Bannister et al. (2017): the OSSOS discoveries are in the phase spaces that can be populated by the combined mechanisms of diffusion, scattering, and capture into weak distant resonances. We refer the reader to Bannister et al. (2017) for detailed discussion.

## 6. Summary

OSSOS acquired 8 TB of wide-field images of  $\sim 170~{\rm deg}^2$  of sky in 2013–2017 with CFHT's MegaCam. These publicly available data are calibrated to Data Release 1 from *Gaia* and Pan-STARRS. Our analysis of the images has provided more than 37,000 astrometric measurements on the orbital arcs of 949 detections at heliocentric distances between 6 and 83 au; all points have been individually inspected for quality control. From these detections, we present 840 discoveries of minor planets with precise quantification of their observational biases, ideal for use in testing models of TNO populations. The orbital quality of 97% of the 840 characterized discoveries is  $\sigma_a < 0.1\%$ . This provides a significant improvement in both number per population and orbital quality over the sample in the MPC.

We highlight several key results thus far from the OSSOS discovery sample and analysis papers.

- 1. The scattering disk has an intrinsic population of  $9 \times 10^4$  for  $H_r < 8.66$  (D > 100 km), and the Centaur population is two orders of magnitude smaller.
- 2. The inner Kuiper Belt has  $a \gtrsim 37$  au, and its inclinations are consistent with those in the main belt.
- 3. Perihelia are consistently q > 35 au throughout the nonresonant Kuiper Belt.
- 4. The low-inclination cold classicals have a "kernel" of population concentration in a tight parameter space at  $a \sim 42.5$ –44.5 au.
- 5. The low-inclination cold classical belt extends beyond the 2:1 resonance with Neptune to at least 49 au.
- 6. TNOs in the 2:1 resonance have a colder inclination distribution than those in the closer 3:2 resonance.
- 7. The distant a > 50 au resonances are more heavily populated than current Neptune migration models predict.
- 8. Securely occupied resonances exist out to at least  $a \sim 130\,\mathrm{au}$ . Their long-term behavior on timescales of more than 100 Myr suggests that a large metastable population is cycling between the scattering disk and high-order resonances.
- 9. Our nine q>30, a>150 au TNOs are consistent with being detected from an orbit distribution intrinsically uniform in the angles  $\omega$  and  $\Omega$  and with formation via the mechanisms of diffusion, scattering, and capture into distant resonances.

In contrast, the MPC sample is from a variety of surveys, largely without bias characterization. Thus, the OSSOS minor planets form a unique set: a sample that is half as large as the entire MPC inventory, yet with perfect tracking efficiency for trans-Neptunian orbits and quantifiable biases. We provide a survey simulator that includes the specifications of OSSOS and three other smaller surveys with well-quantified biases for a total discovery sample of 1142 bias-characterized TNOs with which to test population models. We look forward to seeing the community use this powerful tool for diagnosing the inventory and history of our solar system.

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Facility: CFHT (MegaPrime).

Software: Astropy (The Astropy Collaboration et al. 2013), matplotlib (Hunter 2007), scipy (Jones et al. 2001), GNU parallel (Tange 2011), SExtractor (Bertin & Arnouts 1996), IRAF (Tody 1986), DAOphot (Stetson 1987), WCStools, SuperMongo.

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#### References

Adams, E. R., Gulbis, A. A. S., Elliot, J. L., et al. 2014, AJ, 148, 55
Ahn, C. P., Alexandroff, R., Allende Prieto, C., et al. 2014, ApJS, 211, 17
Alexandersen, M., Gladman, B., Kavelaars, J. J., et al. 2016, AJ, 152, 111
Allen, C. W. 1976, Astrophysical Quantities (London: Athlone), 124
Bannister, M. T., Alexandersen, M., Benecchi, S. D., et al. 2016a, AJ, 152, 212
Bannister, M. T., Kavelaars, J. J., Petit, J.-M., et al. 2016b, AJ, 152, 70
Bannister, M. T., Shankman, C., Volk, K., et al. 2017, AJ, 153, 262
Batygin, K., & Brown, M. E. 2016, AJ, 151, 22
Bauman, S. E., Benedict, T., Baril, M., et al. 2014, Proc. SPIE, 9149, 91491K
Bernstein, G., & Khushalani, B. 2000, AJ, 120, 3323

```
Bertin, E., & Arnouts, S. 1996, A&AS, 117, 393
Boulade, O., Charlot, X., Abbon, P., et al. 2003, Proc. SPIE, 4841, 72
Brown, M. E. 2001, AJ, 121, 2804
Chambers, K. C., Magnier, E. A., Metcalfe, N., et al. 2016, AJ, submitted
   (arXiv:1612.05560)
Chiang, E., & Choi, H. 2008, AJ, 136, 350
Chiang, E. I., & Jordan, A. B. 2002, AJ, 124, 3430
Chiang, E. I., Jordan, A. B., Millis, R. L., et al. 2003, AJ, 126, 430
Dawson, R. I., & Murray-Clay, R. 2012, ApJ, 750, 43
Devost, D., Moutou, C., Manset, N., et al. 2016, Proc. SPIE, 9910, 991015
Dones, L., Brasser, R., Kaib, N., & Rickman, H. 2015, SSRv, 197, 191
Duncan, M. J., & Levison, H. F. 1997, Sci, 276, 1670
Elliot, J. L., Kern, S. D., Clancy, K. B., et al. 2005, AJ, 129, 1117
Fernandez, J. A., & Ip, W. H. 1984, Icar, 58, 109
Finkbeiner, D. P., Schlafly, E. F., Schlegel, D. J., et al. 2016, ApJ, 822, 66
Fraser, W. C., Bannister, M., Pike, R., et al. 2015, in AAS/Division for
  Planetary Sciences Meeting Abstracts 47, 211.15
Fukugita, M., Ichikawa, T., Gunn, J. E., et al. 1996, AJ, 111, 1748
Gaia Collaboration, Brown, A. G. A., Vallenari, A., et al. 2016, A&A, 595, A2
Gerdes, D. W., Sako, M., Hamilton, S., et al. 2017, ApJL, 839, L15
Gladman, B., Kavelaars, J., Petit, J.-M., et al. 2009, ApJL, 697, L91
Gladman, B., Lawler, S. M., Petit, J.-M., et al. 2012, AJ, 144, 23
Gladman, B., Marsden, B. G., & Van Laerhoven, C. 2008, in The Solar System
   Beyond Neptune, ed. M. A. Barucci et al. (Tucson, AZ: University of
   Arizona Press), 43
Gomes, R., Nesvorny, D., Morbidelli, A., Deienno, R., & Nogueira, E. 2018,
   Icar, 306, 319
Gomes, R. S., Fern Ndez, J. A., Gallardo, T., & Brunini, A. 2008, in The Solar
   System Beyond Neptune, ed. M. A. Barucci et al. (Tucson, AZ: University
   of Arizona Press), 259
Gulbis, A. A. S., Elliot, J. L., Adams, E. R., et al. 2010, AJ, 140, 350
Hahn, J. M., & Malhotra, R. 2005, AJ, 130, 2392
Holman, M. J., Chen, Y.-T., Lin, H.-W., et al. 2015, in AAS/Division for
   Planetary Sciences Meeting Abstracts 47, 211.12
Holman, M. J., Payne, M. J., Fraser, W., et al. 2018, ApJL, 855, L6
Hunter, J. D. 2007, CSE, 9, 90
Jones, E., Oliphant, T., Peterson, P., et al. 2001, SciPy: Open source scientific
  tools for Python, http://www.scipy.org/
Jones, R. L., Gladman, B., Petit, J.-M., et al. 2006, Icar, 185, 508
Jones, R. L., Jurić, M., & Ivezić, Ž. 2016, in IAU Symp. 318, Asteroids: New
   Observations, New Models, ed. S. R. Chesley et al., 282
Jones, R. L., Parker, J. W., Bieryla, A., et al. 2010, AJ, 139, 2249
Kaib, N. A., & Sheppard, S. S. 2016, AJ, 152, 1
Kaula, W. M., & Newman, W. I. 1992, AdSpR, 12, 3
Kavelaars, J., Jones, L., Gladman, B., Parker, J. W., & Petit, J.-M. 2008, in The
   Solar System Beyond Neptune, ed. M. A. Barucci et al. (Tucson, AZ:
   University of Arizona Press), 59
Kavelaars, J. J., Jones, R. L., Gladman, B. J., et al. 2009, AJ, 137, 4917
```

Kortenkamp, S. J., Malhotra, R., & Michtchenko, T. 2004, Icar, 167, 347

Lawler, S. M., & Gladman, B. 2013, AJ, 146, 6

```
Lawler, S. M., Kavelaars, J. J., Alexandersen, M., et al. 2018a, Frontiers in
  Astronomy and Space Sciences: Fundamental Astronomy, submitted
Lawler, S. M., Shankman, C., Kaib, N., et al. 2016, AJ, 153, 33
Lawler, S. M., Shankman, C., Kavelaars, J. J., et al. 2018b, AJ, in press
Levison, H. F., Morbidelli, A., Van Laerhoven, C., Gomes, R., & Tsiganis, K.
  2008, Icar, 196, 258
Lykawka, P. S., & Mukai, T. 2007, Icar, 186, 331
Magnier, E. A., Schlafly, E. F., Finkbeiner, D. P., et al. 2016, AJ, submitted
  (arXiv:1612.05242)
Malhotra, R. 1993, Natur, 365, 819
Malhotra, R. 1995, AJ, 110, 420
Meech, K. J., Weryk, R., & Micheli, M. 2017, Natur, 552, 378
Molnár, L., Pál, A., Sárneczky, K., et al. 2018, ApJS, 234, 37
Murray-Clay, R. A., & Chiang, E. I. 2005, ApJ, 619, 623
Nesvorný, D. 2015a, AJ, 150, 68
Nesvorný, D. 2015b, AJ, 150, 73
Nesvorny, D., Vokrouhlický, D., Dones, L., et al. 2017, ApJ, 845, 27
Parker, A. H., Buie, M. W., Osip, D. J., et al. 2013, AJ, 145, 96
Petit, J.-M., Holman, M., Scholl, H., Kavelaars, J., & Gladman, B. 2004,
           3. 347, 471
Petit, J.-M., Kavelaars, J. J., Gladman, B. J., et al. 2011, AJ, 142, 131
Petit, J.-M., Kavelaars, J. J., Gladman, B. J., et al. 2017, AJ, 153, 236
Pike, R. E., & Lawler, S. M. 2017, AJ, 154, 171
Salmon, D., Cuillandre, J.-C., Barrick, G., et al. 2009, PASP, 121, 905
Shankman, C. 2017, PhD thesis, Univ. Victoria
Shankman, C., Kavelaars, J. J., Bannister, M. T., et al. 2017, AJ, 154, 50
Shankman, C., Kavelaars, J. J., Gladman, B. J., et al. 2016, AJ, 151, 31
Sheppard, S. S. 2012, AJ, 144, 169
Sheppard, S. S., Trujillo, C., & Tholen, D. J. 2016, ApJL, 825, L13
Sheppard, S. S., & Trujillo, C. A. 2006, Sci, 313, 511
Sheppard, S. S., & Trujillo, C. A. 2010, Sci, 329, 1304
Skrutskie, M. F., Cutri, R. M., Stiening, R., et al. 2006, AJ, 131, 1163
Souami, D., & Souchay, J. 2012, A&A, 543, A133
Stetson, P. B. 1987, PASP, 99, 191
Tange, O. 2011, login: The USENIX Magazine, 36, 42
The Astropy Collaboration, Robitaille, T. P., Tollerud, E. J., et al. 2013, A&A,
  558, A33
Thommes, E. W., Duncan, M. J., & Levison, H. F. 2002, AJ, 123, 2862
Tody, D. 1986, Proc. SPIE, 627, 733
Trujillo, C. A., & Sheppard, S. S. 2014, Natur, 507, 471
Tsiganis, K., Gomes, R., Morbidelli, A., & Levison, H. F. 2005, Natur,
  435, 459
Volk, K., & Malhotra, R. 2017, AJ, 154, 62
Volk, K., Murray-Clay, R., Gladman, B., et al. 2016, AJ, 152, 23
Volk, K., Murray-Clay, R., Gladman, B. G., et al. 2018, ApJL, submitted
  (arXiv:1802.05805)
Weryk, R. J., Lilly, E., Chastel, S., et al. 2016, Icar, submitted (arXiv:1607.
Wong, I., & Brown, M. E. 2016, AJ, 152, 90
Zacharias, N., Finch, C. T., Girard, T. M., et al. 2013, AJ, 145, 44
```