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Research Article

Otsu Based Optimal Multilevel Image Thresholding Using Firefly Algorithm

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Histogram based multilevel thresholding approach is proposed using Brownian distribution (BD) guided firefly algorithm (FA). A bounded search technique is also presented to improve the optimization accuracy with lesser search iterations. Otsu's between-class variance function is maximized to obtain optimal threshold level for gray scale images. The performances of the proposed algorithm are demonstrated by considering twelve benchmark images and are compared with the existing FA algorithms such as Lévy flight (LF) guided FA and random operator guided FA. The performance assessment comparison between the proposed and existing firefly algorithms is carried using prevailing parameters such as objective function, standard deviation, peak-to-signal ratio (PSNR), structural similarity (SSIM) index, and search time of CPU. The results show that BD guided FA provides better objective function, PSNR, and SSIM, whereas LF based FA provides faster convergence with relatively lower CPU time.

1. Introduction

In imaging science, image processing plays a vital role in the analysis and interpretation of images in fields such as medical discipline, navigation, environment modeling, automatic event detection, surveillance, texture and pattern recognition, and damage detection. The development of digital imaging techniques and computing technology increased the potential of imaging science.

During the image processing operation, a photograph or a video frame is analyzed with a chosen signal processing technique and the outcomes such as processed image, data, and/or parameters related to image are further investigated to extract the desired information from the raw input image.

Image segmentation is one of preprocessing techniques used to regulate the features of an image. It is also judged to be an important procedure for significant examination and interpretation of input images [1].

Over the years, several techniques for segmentation have been proposed and implemented in the literature [2–10]. In segmentation, the input image is separated into nonoverlapping, homogenous regions containing similar objects. Based on the performance appraisal process, the segmentation methods are classified into two groups such as supervised and unsupervised evaluation. Unsupervised methods are preferable in real-time processing because they do not require a manually segmented image [11].

Thresholding is considered the most desired procedure out of all the existing procedures used for image segmentation, because of its simplicity, robustness, accuracy, and competence [12]. If the input image is divided into two classes, such as the background and the object of interest, it is called bilevel thresholding. Bilevel thresholding is extended to multilevel thresholding to obtain more than two classes [11, 13, 14].

The thresholds can be derived at a local or global level [15]. In local thresholding, a different threshold is assigned for each part of the image. In global thresholding, a single global threshold in the probability density function of the grey level histogram is obtained using parametric or nonparametric approach to find the thresholds. In the parametric approaches, the statistical parameters of the classes in the image are estimated. They are computationally expensive, and their performance may vary depending on the initial conditions. In the nonparametric approaches, the thresholds are determined by maximising some criteria, such as betweenclass variance [16] or entropy measures.

The methods such as Kapur, Tsallis, and Otsu are widely adopted by most of the researchers to find solution for multilevel image segmentation problems [17–20]. In general, Kapur and Otsu based thresholding techniques proved their better shape and uniformity measures for the bilevel and multilevel thresholding problems [1].

Traditional methods work well for a bilevel thresholding problem, when the number of threshold level increases, complexity of the thresholding problem also will increase and the traditional method requires more computational time. Hence, in recent years, soft computing algorithm based multilevel image thresholdingprocedure is widely proposed by the researchers.

Recent literature illustrates that the heuristic and metaheuristic algorithms such as particle swarm optimization (PSO) [20-25], bacterial foraging algorithm (BFO) [1, 13, 17, 18], differential evaluation (DE) [19, 26-28], artificial bee colony (ABC) [11, 29], cuckoo search (CS) [12, 30], watershed algorithm [31], fuzzy logic [32], hybrid method [33], and self-adaptive parameter optimization algorithm [34] are widely considered for optimal multilevel image segmentation problem to enhance the outcome.

In this work, the FA, initially proposed by Yang, is considered [35, 36]. From the recent literature, it is observed that the FA offers better optimal solution for variety of engineering problems [37–48]. In this work, recently proposed Brownian distribution guided firefly algorithm (BDFA) by Sri Madhava Raja et al. [49] is adopted for solving multilevel thresholding image segmentation problem using Otsu's between-class variance method. The proposed technique is tested on twelve standard test images and compared with the traditional FA and Lévy flight guided firefly algorithm (LFFA).

The paper is organized as follows. Section 2 presents the Otsu based multilevel thresholding problem. Section 3 presents the overview of the FA, and the implementation of Otsu guided FA is discussed in Section 4. Experimental results are evaluated and discussed in Section 5. Conclusion of the present research work is given in Section 6.

2. Methodology

The classical and optimization algorithm based thresholding methods existing in the literature are employed to find the best possible threshold in the segmented histogram by satisfying some guiding parameters. Otsu based image thresholding is initially proposed in 1979 [50]. This method presents the

optimal values by maximizing the objective function. In the present work, Otsu's nonparametric segmentation method known as between-class variance is considered. A detailed description of the between-class variance method could be found in [1, 11].

In bilevel thresholding (for m = 2), input image is divided into two classes such as C_0 and C_1 (background and objects, or vice versa) by a threshold at a level "t." The class C_0 encloses the gray levels in the range 0 to t-1 and class C_1 encloses the gray levels from t to L-1. The probability distributions for the gray levels C_0 and C_1 can be expressed as

$$C_0 = \frac{p_0}{\omega_0(t)} \cdots \frac{p_{t-1}}{\omega_0(t)}, \qquad C_1 = \frac{p_t}{\omega_1(t)} \cdots \frac{p_{L-1}}{\omega_1(t)}, \quad (1)$$

where $\omega_0(t) = \sum_{i=0}^{t-1} p_i$, $\omega_1(t) = \sum_{i=t}^{L-1} p_i$, and L = 256. The mean levels μ_0 and μ_1 for C_0 and C_1 can be expressed

$$\mu_0 = \sum_{i=0}^{t-1} \frac{ip_i}{\omega_0(t)}, \qquad \mu_1 = \sum_{i=t}^{L-1} \frac{ip_i}{\omega_1(t)}. \tag{2}$$

The mean intensity (μ_T) of the entire image can be represented as

$$\mu_T = \omega_0 \mu_0 + \omega_1 \mu_1, \qquad \omega_0 + \omega_1 = 1.$$
 (3)

The objective function for the bilevel thresholding problem can be expressed as

Maximize
$$J(t) = \sigma_0 + \sigma_1$$
, (4)

where $\sigma_0 = \omega_0 (\mu_0 - \mu_T)^2$ and $\sigma_1 = \omega_1 (\mu_1 - \mu_T)^2$.

The above discussed procedure can be extended to a multilevel thresholding problem for various "m" values as follows.

Let us consider that there are "m" thresholds (t_1, t_2, \dots, t_m) , which divide the input image into "m" classes: C_0 with gray levels in the range 0 to t-1, C_1 with enclosed gray levels in the range t_1 to $t_2 - 1, ...,$ and C_m with gray levels from t_m to L-1.

The objective function for the multilevel thresholding problem can be expressed as

Maximize
$$J(t) = \sigma_0 + \sigma_1 + \dots + \sigma_m$$
, (5)

where $\sigma_0 = \omega_0 (\mu_0 - \mu_T)^2$, $\sigma_1 = \omega_1 (\mu_1 - \mu_T)^2$,..., $\sigma_m =$ $\omega_m(\mu_m - \mu_T)^2$. (Note that, in the proposed work, objective functions are assigned for m = 2, m = 3, m = 4, and m = 5.)

3. Firefly Algorithm

Firefly algorithm is a nature inspired metaheuristic algorithm initially proposed by Yang [35, 36]. This algorithm is developed by imitating the flashing illumination patterns generated by invertebrates such as glowworm and firefly. They generate chemically produced light from their lower abdomen. This bioluminescence with varied flashing patterns generated by glowworm/firefly is used to establish communication between two neighboring insects, to search for prey and also to find mates.

The classical FA is developed by taking the following conditions into account [37–40].

- (i) All the fireflies are unisex and one firefly will be attracted to the nearest firefly regardless of their sex.
- (ii) The attractiveness between two fireflies is proportional to the luminance. For any couple of flashing fireflies, the firefly with the brighter luminance will attract the firefly with lesser luminance. The attractiveness between two fireflies mainly depends on the Cartesian distance and is proportional to the brightness which decreases with increasing distance between fireflies. In a region, if all the fireflies have lesser luminance, then they will move randomly in the "D" dimensional search space until they find a firefly with brighter luminance.
- (iii) The brightness of a firefly is somehow related to the analytical form of the objective function assigned to guide the search process.

The overall performance (exploration time, speed of convergence, and optimization accuracy) of the FA depends on the cost function, which monitors the optimization search. For a maximization problem, luminance of a firefly is considered to be proportional to the value of cost function (i.e., luminance = objective function).

3.1. Fundamentals. The chief parameters which decide the efficiency of the FA are the variations of light intensity and attractiveness between neighboring fireflies. These two parameters will be affected by the increase in the distance between fireflies [23].

Variation in luminance can be analytically expressed by the following Gaussian form:

$$I(r) = I_0 e^{-\gamma d^2},\tag{6}$$

where I is the new light intensity, I_0 is the original light intensity, and γ is the light absorption coefficient.

The attractiveness to the luminance can be analytically represented as

$$\beta = \beta_0 e^{-\gamma d^2},\tag{7}$$

where β is the attractiveness coefficient and β_0 is the attractiveness at r = 0.

The above equation describes a characteristic distance $\Gamma = 1/\sqrt{\gamma}$ over which the attractiveness changes significantly from β_0 to $\beta_0 e^{-1}$. The attractiveness function $\beta(d)$ can be any monotonically decreasing functions such as the following form:

$$\beta(d) = \beta_0 e^{-\gamma d^m}, \quad (m \ge 1). \tag{8}$$

For a fixed γ , the characteristic length becomes

$$\Gamma = \gamma^{-1/m} \longrightarrow 1, \quad m \longrightarrow \infty.$$
 (9)

Conversely, for a given length scale Γ , the parameter γ can be used as atypical initial value (i.e., $\gamma = 1/\Gamma m$).

The Cartesian distance between two fireflies i and j at x_i and x_j , in the n-dimensional search space, can be mathematically expresses as

$$d_{ij}^{t} = \left\| X_{j}^{t} - X_{i}^{t} \right\|_{2} = \sqrt{\sum_{k=1}^{n} \left(X_{j,k} - X_{i,k} \right)^{2}}.$$
 (10)

In FA, the light intensity at a particular distance d from the light source X_i^t obeys the inverse square law. The light intensity of a firefly I reduces, as the distance d increases in terms of $I \propto 1/d^2$. The movement of the attracted firefly i towards a brighter firefly j can be determined by the following position update equation:

$$X_{i}^{t+1} = X_{i}^{t} + \beta_{0} e^{-\gamma d_{ij}^{2}} \left(X_{i}^{t} - X_{i}^{t} \right) + \Psi, \tag{11}$$

where X_i^{t+1} is the updated position of firefly, X_i^t is the initial position of firefly, $\beta_0 e^{-\gamma d_{ij}^2} (X_j^t - X_i^t)$ is the attraction between fireflies, and Ψ is the randomization parameter.

From (11), it is observed that updated position of the ith firefly depends on initial position of the firefly, attractiveness of firefly to the luminance, and the randomization parameter. In this paper randomization parameters such as $\alpha \varepsilon i$ [36] and α sign (rand - 1/2) Lévy [37, 51] are considered. Lévy flight based randomization parameter helps to achieve faster convergence compared to other randomization parameters existing in the literature.

3.2. Working Principle. The working principle of the traditional FA is demonstrated in this section using a two-dimensional optimization problem. The total number of fireflies is assigned as six. When the algorithm is initialized, all the fireflies are randomly distributed in the two-dimensional search space. In this problem, it is assumed that the search space has two local best values and a global best value.

During the initial search, some fireflies move towards the local best (LB) values and some reach the global best (GB) value as illustrated in Figure 1(a). From Figure 1(a), it is observed that firefly 1 (FF1) is at LB1, firefly 4 (FF4) is at GB, and firefly 5 (FF5) is at LB2. FF2 lies between LB1 and GB, FF3 lies between GB and LB2, and FF6 is between GB and LB2. The light intensity produced by FF4 is brighter than the light intensity by FF1 and FF5. At this condition, FF2 moves towards LB1 or GB based on the Cartesian distance "d" (8). In this problem, the distance between FF1 and FF2 (D1) is short compared to D2; hence FF2 moves towards LB1. Similarly, the Cartesian distance between FF4 and FF3 (D3) is shorter than D4, and FF3 is more likely attracted to GB than LB2. The Cartesian distance between FF6 and FF5 (D5) is shorter than D6, and FF6 is likely attracted to LB2.

Figure 1(b) shows the second stage of search process. When the search iteration increases, the firefly at the GB is retained. The attraction signal between the fireflies at the local best value is exponentially decreased with the increase in search iteration and the entire fireflies move towards the GB. Finally a considerable amount of fireflies are gathered at the global best value as shown in Figure 1(c) at the end of optimization search.

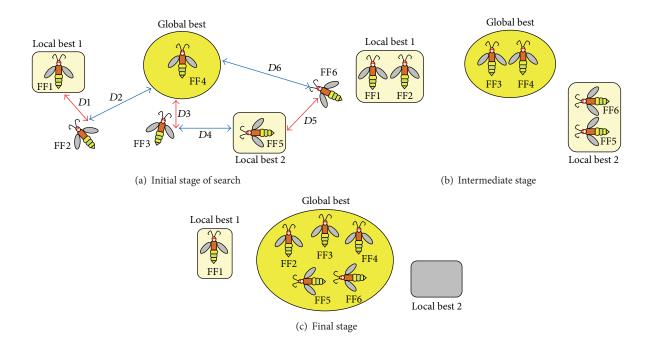


FIGURE 1: Various stages of firefly search.

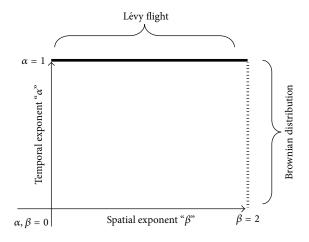


FIGURE 2: Relation between LF and BD.

3.3. Lévy Flight and Brownian Distribution. In recently developed nature inspired methods such as firefly and cuckoo algorithm, optimization search process is guided by Lévy flight (LF) strategy [35].

LF is a random walk with a sequence of arbitrary steps and is conceptually similar to the search path of a foraging animal [52]. In LF, the flight span and the length between two successive changes in direction are drawn from a probability distribution. Similar to LF, Brownian distribution (BD) is also in the family of random walks. Figure 2 shows the relationship between LF and BD. Based on the temporal exponent (α) and spatial exponent (β) values, LF and BD

can be realized from the random walks [53]. A detailed justification of LF and BD is discussed in the book by Yang [35]. Lévy flight is superdiffusive Markovian process, whose step length is drawn from the Lévy distribution in terms of a simple power-law formula:

$$L(s) \sim |s|^{-1-\beta}$$
, where $0 < \beta \le 2$. (12)

The Brownian walk is a subdiffusive non-Markovian process, which obeys a Gaussian distribution with zero mean and time-dependent variance. In (12), the ratio of exponents α/β provides the relationship between sub- and superdiffusion. When $\beta < 2\alpha$, the continuous random walk is superdiffusive, and for $\beta > 2\alpha$ it is subdiffusive. For $\beta = 2\alpha$, the search process exhibits the same scaling as ordinary Brownian motion [52, 54].

Figures 3(a) and 3(b) depict the search patterns of a single firefly with LF and BD in a two-dimensional search space. Figure 3(a) shows that Lévy flight guided FA is very efficient in exploring unknown search space with minimal number of iterations, because of its large step size. Figure 3(b) shows that the BD guided FA explores the search space with smaller step size and provides the best possible solution. In this work, the following formulae are considered:

Lévy flight:
$$L_F(s) = A \cdot |s|^{1/\beta}$$
 (13)

Brownian distribution:
$$B(s) = A \cdot |s|^{\alpha/2}$$
 (14)

$$A = \beta \Gamma(\beta) \sin\left(\frac{\beta \pi}{2}\right) \frac{1}{\pi},\tag{15}$$

where *A* is the random variable, β is the spatial exponent, α is the temporal exponent, and $\Gamma(\beta)$ is a Gamma function.

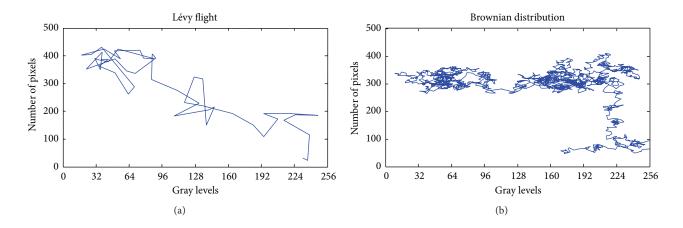


FIGURE 3: (a) Search pattern of a firefly with LF. (b) Search pattern of a firefly with BD.

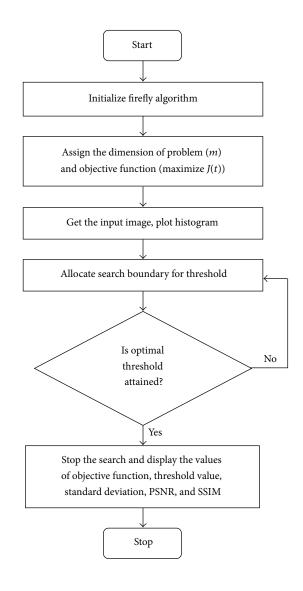


FIGURE 4: Flow chart of proposed method.

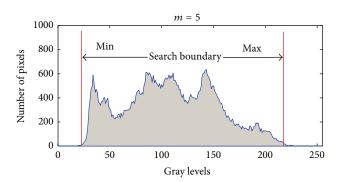


FIGURE 5: Histogram with possible search boundaries.

Equations (13) and (14) are formed as discussed in [49]. The random variable presented in (15) is chosen based on the article by Gandomi et al. [51].

4. Implementation

The multilevel thresholding problem deals with finding optimal thresholds within the gray scale range [0, L-1] that maximize a fitness criterion J(t). Otsu's between-class variance function is employed to find the threshold values. The search dimension of the optimization problem is assigned based on the number of thresholds (m) considered. In this paper, optimal multilevel thresholding has been carried out by an unsupervised global-level nonparametric approach. In the proposed approach, the efficiencies of BDFA, LFFA, and FA are tested separately, and their performances have been compared.

Figure 4 depicts the flow chart of the proposed work. The firefly algorithms are employed to find the optimal threshold values by maximizing the objective function.

In metaheuristic algorithm based optimization methods, the bounded search technique helps to achieve better values with lesser iterations [49]. In the proposed work, the

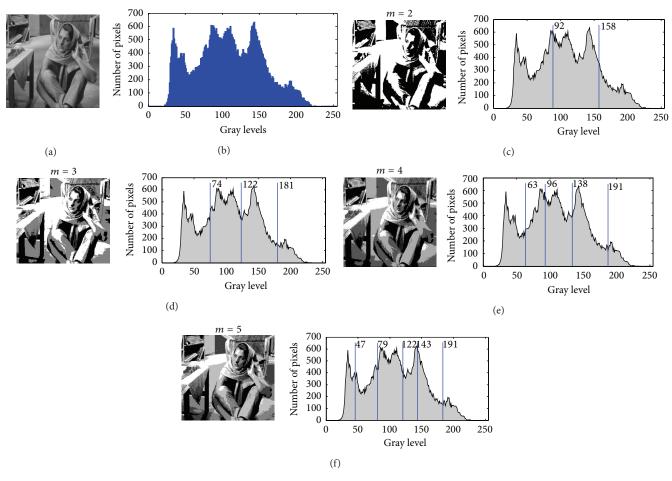


FIGURE 6: (a) Original Barbara image, (b) histogram, and (c)–(f) segmented Barbara image with various "m" levels and corresponding optimal threshold values.

dimension of the search varies from 2 to 5 based on the "m" values. When m=2, it is a simple two-dimensional optimization problem and an unbounded search may offer better result with lesser iterations. When "m" value increases, the complexity of the optimization problem also will increase.

In this paper we introduced a bounded search technique for the image segmentation problem. Instead of initializing the search operation with a range of gray levels [0, L-1], we propose a search boundary as

Figure 5 shows the histogram of the Barbara image. The value of "m" is five; hence it is a five-dimensional optimization problem (i.e., the number of threshold to be identified is five). The search boundary for the threshold is assigned as 20 < gray levels < 220. During the boundary based search, the optimization algorithm explores the gray levels situated between 20 and 220 and ignores the rest of the gray levels. This bounded search technique will provide better solution with lesser iterations.

The performance of the Otsu guided firefly algorithms is evaluated using the well-known parameters such as peak-to-signal ratio (PSNR) and structural similarity indices (SSIM) [11].

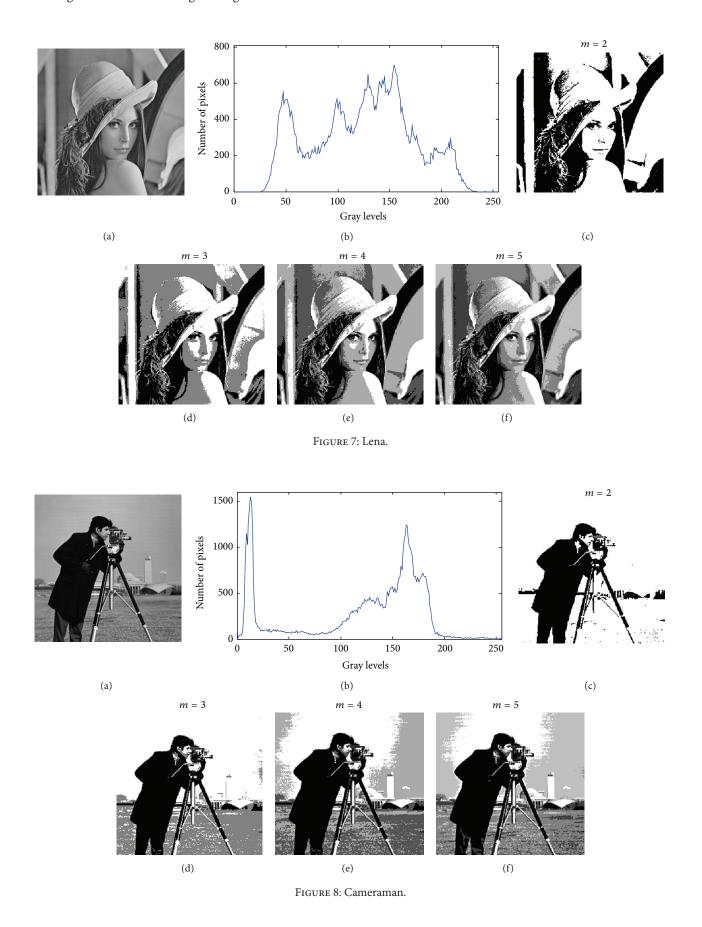
The PSNR is mathematically represented as

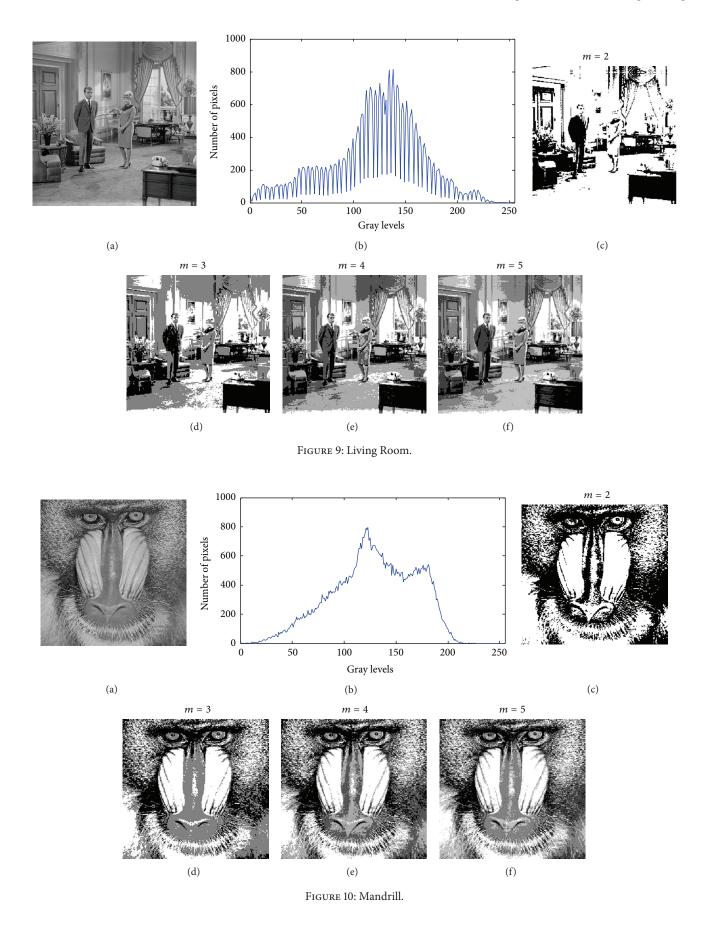
PSNR
$$(x, y) = 20 \log_{10} \left(\frac{255}{\sqrt{\text{MSE}(x, y)}} \right).$$
 (17)

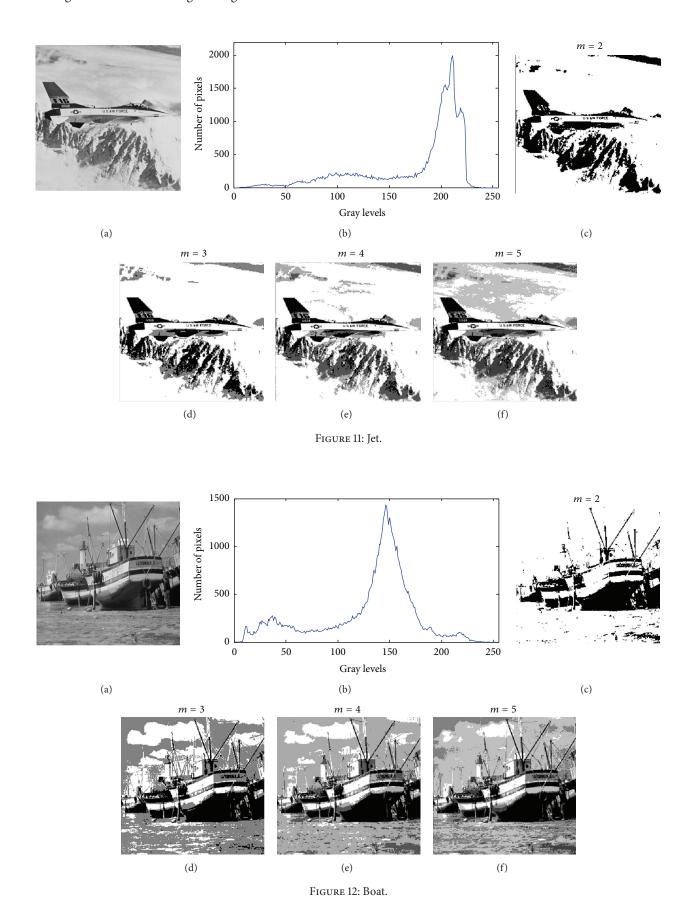
The SSIM is normally used to estimate the image quality and interdependencies between the original and processed image. SSIM index combines luminance comparison, contrast comparison, and structure comparison and satisfies symmetry, boundedness, and unique maximum properties:

SSIM
$$(x, y) = \frac{(2\mu_x \mu_y + C_1)(2\sigma_{xy} + C_2)}{(\mu_x^2 + \mu_y^2 - C_1)(\sigma_{x^2} + \sigma_{y^2} + C_2)}.$$
 (18)

Otsu guided firefly algorithm based multilevel thresholding techniques have been tested on different standard test images such as Barbara, where μ_x is the average of x, μ_y is the average of y, σ_x^2 is the variance of x, σ_y^2 is the variance







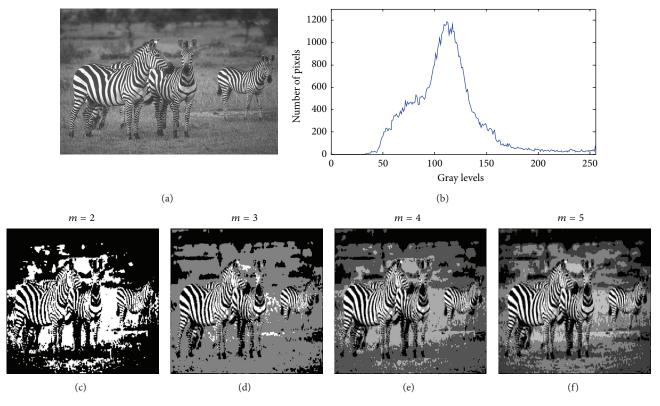


Figure 13: Zebra.

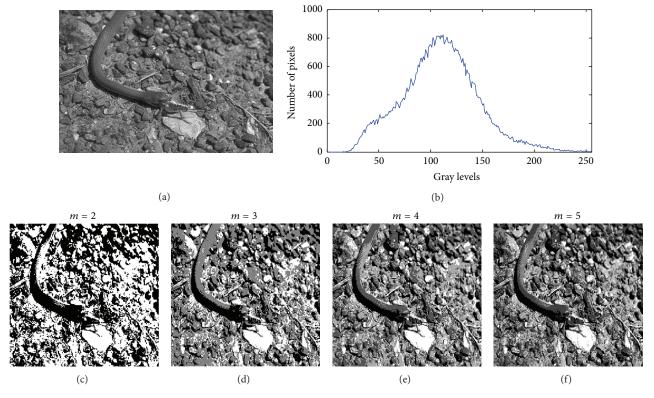
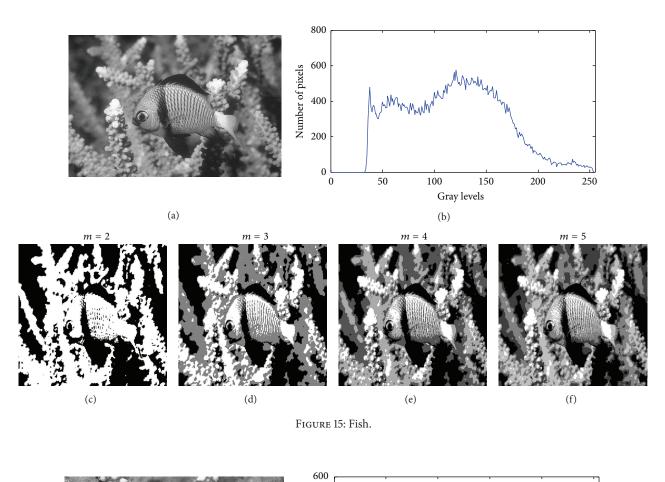


Figure 14: Snake.



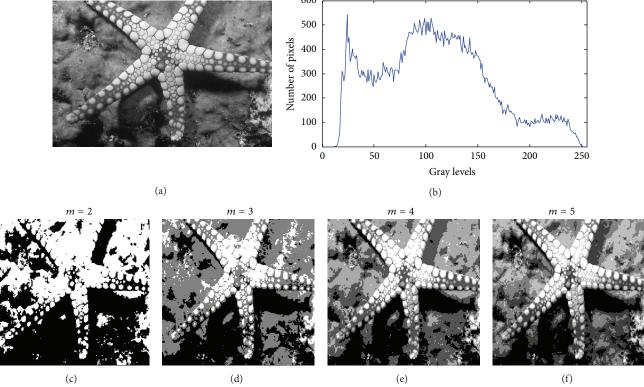


Figure 16: Star Fish.

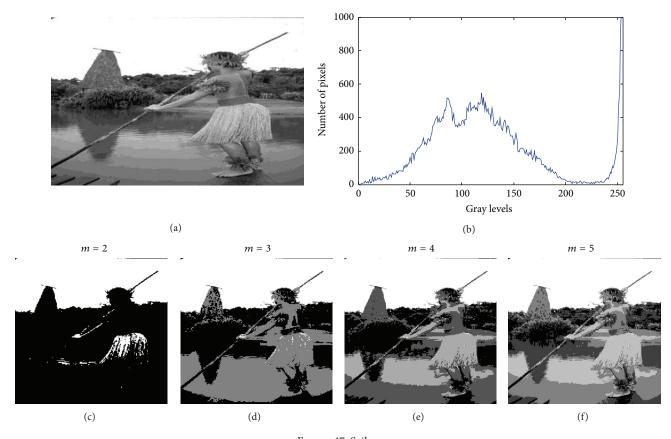


Figure 17: Sailor

of y, σ_{xy} is the covariance of x and y, $C_1 = (k_1 L)^2$ and $C_2 = (k_1 L)^2$ stabilize the division with weak denominator, L = 256, $k_1 = 0.01$, and $k_2 = 0.03$.

Like SSIM, structural dissimilarity (DSSIM) is also a measure of the processed image quality and it can be expressed as

$$DSSIM(x, y) = \frac{1 - SSIM(x, y)}{2}.$$
 (19)

In this work, PSNR and SSIM are considered to evaluate the performance of firefly algorithms.

5. Results and Discussion

The images Lena, Cameraman, Living Room, Mandrill, Jet, and Boat are obtained from the database available at [55]. The remaining five images, Zebra, Snake, Fish, Star Fish, and Sailor, were taken from the Berkeley Segmentation Dataset [56]. The entire image has an inimitable grey level histogram. All the test images are converted into a 256×256 sized gray scale image before the analysis. In the test images, most of them are difficult to segment because of their multimodal histograms. Images such as Barbara and Lena show multiple peaks and valleys whereas the Living Room image shows abruptly changing pixel levels. Other images such as Mandrill, Boat, Zebra, Snake, Fish, and Star Fish

show a smooth distribution in gray level compared to the Cameraman and Jet.

All the experiments were performed on a work station with an AMD C70 Dual Core 1 GHz CPU with 4 GB of RAM and equipped with MATLAB R2010a software.

The firefly algorithm parameters are assigned as discussed in [51]; the number of fireflies is as follows: (n) = 25, β_0 = 1, γ = 5, and α_0 = 0.5 (gradually reduced to 0.1 in steps of 0.01 as iterations proceed), and the total number of run is chosen as 5000.

During the experiment, each image is examined with a number of thresholds such as m=2 to 5. The simulation study is repeated 20 times individually and the best value among the search is recorded as the optimal threshold value. In Figures 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, and 17, (a) represents the original image, (b) represents the histogram for a 256 \times 256 image, and (c) to (f) represent the segmented images of Otsu guided BDFA for m=2 to 5.

During the optimization exploration, the search boundaries for the images are assigned as follows.

 $\label{eq:lemma} Lena=20 < gray \ levels < 220, \ Cameraman=50 < gray \ levels < 200, \ Living \ Room=0 < gray \ levels < 230, \ Mandrill \ 30 < gray \ levels < 210, \ Jet=50 < gray \ levels < 220, \ Boat=50 < gray \ levels < 200, \ Zebra=50 < gray \ levels < 200, \ Snake=20 < gray \ levels < 200, \ Fish=30 < gray \ levels < 230, \ Star \ Fish=30 < gray \ levels < 230, \ and \ Sailor=10 < gray \ levels < 210.$

Table 1: Comparison of objective values achieved with Otsu guided various FAs.

Test images	m	Objective function values			Optimal threshold values					
		BDFA	LFFA	FA	BDFA	LFFA	FA			
Barbara	2	912.23	1023.28	1038.18	92, 158	90, 157	90, 156			
	3	961.89	1523.21	1300.15	74, 122, 181	77, 124, 183	73, 120, 178			
	4	1053.12	1593.82	1872.19	63, 96, 138, 191	61, 93, 137, 194	63, 96, 138, 191			
	5	2428.05	1735.34	2164.01	47, 79, 122, 143, 191	46, 81, 119, 140, 193	44, 81, 120, 147, 188			
Lena	2	1105.92	952.36	1052.66	90, 148	92, 149	92, 148			
	3	1823.25	1271.83	1382.71	63, 119, 171	64, 117, 168	59, 111, 172			
	4	1858.92	1639.26	1429.52	55, 100, 133, 183	57, 102, 138, 179	51, 98, 142, 176			
	5	2017.63	1753.92	1742.08	49, 98, 124, 150, 185	53, 95, 128, 153, 187	49, 103, 128, 152, 186			
Cameraman	2	1757.03	2071.36	1949.28	70, 148	70, 148	71, 148			
	3	1941.42	2418.92	2023.41	51, 119, 163	54, 120, 158	53, 118, 162			
	4	2056.55	2508.48	2205.20	49, 117, 144, 182	50, 113, 148, 174	49, 112, 148, 171			
	5	2592.04	2691.82	2533.75	38, 91, 137, 170, 201	42, 93, 138, 169, 198	44, 92, 140, 173, 204			
Living Room	2	1053.87	925.83	1104.07	84, 152	82, 155	84, 152			
	3	1103.72	1053.62	1311.94	86, 141, 192	84, 138, 189	86, 141, 192			
	4	1376.21	1329.02	1482.10	61, 107, 148, 189	64, 105, 140, 187	66, 109, 146, 191			
	5	1855.16	1753.41	2153.12	62, 110, 129, 174, 195	66, 106, 138, 162, 203	61, 102, 135, 166, 198			
Mandrill	2	903.63	1067.36	942.01	90, 147	88, 148	87, 148			
	3	1053.01	1271.53	1101.83	101, 148, 193	102, 153, 178	100, 148, 182			
	4	1187.49	1480.99	1359.22	70, 104, 133, 182	71, 109, 144, 175	71, 112, 138, 184			
	5	1609.61	1622.76	1472.94	71, 111, 134, 167, 187	69, 104, 141, 156, 183	74, 102, 138, 158, 181			
Jet	2	836.42	753.36	1102.53	90, 213	98, 210	91, 213			
	3	1063.26	933.92	1491.25	93, 139, 203	98, 140, 211	96, 138, 215			
	4	1293.84	1077.32	1870.55	63, 111, 142, 199	66, 108, 142, 205	58, 112, 138, 203			
	5	1419.27	1121.66	2015.99	77, 92, 123, 151, 210	76, 96, 118, 149, 212	72, 95, 131, 148, 206			
Boat	2	933.16	1047.83	1036.00	99, 176	98, 178	100, 181			
	3	1076.37	1154.34	1204.36	60, 119, 183	64, 121, 178	61, 124, 182			
	4	1192.01	1293.51	1528.04	48, 81, 138, 188	51, 86, 131, 184	52, 91, 133, 176			
	5	1302.33	1504.18	1597.61						
	2	1392.22	1073.25	1530.03	39, 67, 110, 158, 187 94, 151	42, 65, 109, 153, 183 94, 149	46, 72, 116, 148, 189			
							91, 148			
Zebra	3	1503.87	1482.39	1677.92	82, 119, 188	81, 128, 185	78, 119, 189			
Snake	4	1893.2	1629.06	1853.33	70, 115, 132, 185	73, 110, 135, 204	69, 98, 128, 187			
	5	2019.11	1865.35	2289.01	61, 95, 122, 153, 187	66, 93, 114, 146, 198	64, 97, 109, 145, 189			
	2	1398.36	1811.76	1195.21	77, 146	75, 147	74, 144			
	3	1639.22	2071.04	1584.73	61, 114, 166	68, 110, 153	61, 121, 169			
	4	1763.93	2191.55	1965.05	59, 93, 122, 175	54, 85, 123, 175	55, 76, 135, 182			
	5	1973.06	2305.04	2100.46	52, 84, 121, 144, 189	48, 82, 130, 152, 182	51, 81, 128, 151, 179			
Fish	2	925.38	825.25	733.25	102, 182	98, 182	100, 184			
	3	955.26	1063.82	792.47	83, 143, 194	87, 144, 197	82, 139, 188			
	4	1005.03	1205.13	1052.35	72, 125, 162, 203	63, 118, 172, 202	65, 122, 164, 198			
	5	1052.77	1311.74	1360.35	57, 88, 134, 178, 197	48, 79, 141, 175, 202	54, 91, 127, 168, 206			
Star Fish	2	1402.32	2061.65	1785.50	81, 159	82, 162	81, 158			
	3	1611.54	2095.16	2106.76	62, 109, 181	59, 116, 187	65, 111, 175			
	4	1638.02	2105.32	2201.45	57, 108, 142, 186	53, 112, 149, 178	48, 109, 138, 183			
	5	1977.28	2411.77	2311.86	47, 88, 123, 157, 192	44, 83, 127, 163, 188	53, 78, 120, 152, 176			
Sailor	2	600.23	854.05	831.06	53, 175	51, 178	50, 172			
	3	712.93	1052.69	953.72	48, 126, 161	52, 132, 174	47, 136, 178			
	4	730.18	1172.07	1106.35	41, 84, 142, 181	38, 91, 138, 178	41, 84, 142, 181			
	5	826.24	1202.22	1290.60	39, 98, 127, 154, 186	41, 87, 122, 164, 192	45, 88, 133, 184, 203			

 ${\it Table 2: Comparison of the standard deviation, PSNR, SSIM, and CPU time obtained for test images.}$

		Standard deviation			DCNID (AD)			CCIM			CPU time (sec)		
Test images	m					PSNR (dB)		DDEA	SSIM	ГА			
		BDFA	LFFA	FA	BDFA	LFFA	FA 22.0627	BDFA	LFFA	FA	BDFA	LFFA	FA 47.05
Barbara	2	0.00914	0.02582	0.01457	20.0652	25.1241	23.0627	0.8068	0.7540	0.7882	100.46	26.15	47.05
	3	0.07482	0.06925	0.06679	22.0239	25.2267	24.1197	0.8371	0.8201	0.8300	163.05	41.26	43.14
	4	0.50224	0.62528	0.27874	21.7727	23.1895	22.0257	0.8553	0.8227	0.8285	187.25	57.31	50.42
	5	0.62903	0.80425	0.70422	24.8064	24.9632	25.0159	0.8368	0.8113	0.8328	258.15	45.25	73.02
Lena	2	0.02891	0.16251	0.07539	23.2027	27.1066	25.1176	0.8208	0.8011	0.8116	102.36	18.02	25.14
	3	0.04903	0.27180	0.13850	20.9014	22.0823	20.9964	0.8489	0.8246	0.8310	142.47	31.78	61.03
	4	0.31176	0.52319	0.38196	24.1167	25.2476	25.5752	0.8606	0.8165	0.8206	204.52	56.23	71.32
	5	0.58319	0.83251	0.61698	23.2251	24.1466	23.2257	0.8847	0.8542	0.8729	291.02	69.22	108.13
Cameraman	2	0.00176	0.27810	0.07972	25.2568	25.7741	25.8820	0.8258	0.7736	0.8211	104.15	37.28	42.05
	3	0.11874	0.29826	0.31709	23.2942	26.0523	24.0368	0.8432	0.7302	0.8400	131.42	51.35	60.15
	4	0.73652	0.52111	0.37073	25.1117	27.2476	25.8852	0.8478	0.7533	0.8218	128.26	58.13	62.34
	5	0.90362	0.70728	0.74130	26.0004	27.1168	26.4773	0.8633	0.8154	0.8206	142.43	55.28	70.51
Living Room	2	0.03782	0.12671	0.19542	22.0778	22.9625	23.1843	0.8004	0.7699	0.7804	305.35	118.15	136.04
	3	0.07293	0.16729	0.21073	20.2699	22.9952	21.0424	0.8105	0.7811	0.7915	461.55	132.03	130.33
	4	0.38791	0.50981	0.49611	24.9426	26.0731	25.5817	0.8422	0.8102	0.8200	604.46	146.21	172.49
	5	0.82522	0.92351	0.99218	26.0774	26.4426	26.9936	0.8259	0.8246	0.8216	822.50	165.15	190.22
Mandrill	2	0.26681	0.38199	0.28541	23.1159	24.0052	24.1111	0.8077	0.7745	0.7835	89.37	52.11	54.27
	3	0.27916	0.51029	0.39510	21.0002	22.1842	21.2943	0.8322	0.8004	0.8125	114.50	51.58	64.03
	4	0.63441	0.73416	0.73170	24.1883	25.2952	24.7160	0.8421	0.7953	0.8386	172.24	59.13	72.44
	5	0.83551	0.91282	0.90525	21.2683	22.0673	23.0662	0.8257	0.8104	0.7993	166.39	71.35	69.51
Jet	2	0.43203	0.69100	0.28023	23.9864	24.1578	24.0622	0.8414	0.8011	0.8268	79.03	43.35	41.50
	3	0.55871	0.69261	0.63321	21.8552	21.9994	22.0523	0.8528	0.7793	0.8280	82.33	51.29	48.04
	4	0.58352	0.83515	0.70527	26.0316	26.1481	26.1963	0.8234	0.7922	0.8003	97.15	74.22	84.52
	5	0.62253	0.92614	0.88038	25.3806	26.0437	25.5280	0.8943	0.8317	0.8552	133.07	94.25	77.06
Boat	2	0.00256	0.13872	0.02923	23.7731	24.9962	25.0063	0.8018	0.7935	0.7825	59.35	42.55	51.12
	3	0.02361	0.20018	0.06377	20.2579	21.2579	22.0774	0.8280	0.7847	0.7899	63.19	50.32	46.24
	4	0.18389	0.41993	0.21950	21.6589	23.1843	24.1116	0.8146	0.8003	0.8002	89.04	62.13	70.13
	5	0.20871	0.61923	0.37424	25.0227	26.7428	25.8125	0.8593	0.8331	0.8236	107.23	71.35	81.30
Zebra	2	0.10198	0.41092	0.20850	26.0424	27.3566	26.9431	0.8405	0.7999	0.8332	125.31	48.01	72.52
	3	0.18378	0.57708	0.31114	27.1157	27.8841	27.3215	0.8305	0.8110	0.8206	91.26	50.19	42.16
	4	0.18992	0.72119	0.50019	25.6428	27.0053	25.9092	0.8288	0.7845	0.8005	124.20	61.34	71.24
	5	0.39346	0.90371	0.74930	25.7431	27.1579	26.0853	0.8500	0.8003	0.8367	152.43	73.15	80.26
Snake	2	0.00278	0.21309	0.04859	25.0723	25.1589	26.2786	0.8267	0.7945	0.8025	110.52	59.21	61.25
	3	0.07820	0.40192	0.15428	20.6437	20.6318	21.2578	0.8725	0.8264	0.8226	136.11	62.25	82.19
	4	0.13891	0.51223	0.28420	24.0628	24.9132	24.3337	0.8259	0.8077	0.8024	131.35	71.39	59.18
	5	0.20182	0.98801	0.49110	22.1118	23.0075	22.9524	0.8551	0.8205	0.8366	148.52	83.11	93.40
Fish	2	0.00991	0.34992	0.00163	20.0732	22.7737	21.9966	0.8049	0.7883	0.7832	98.01	44.27	54.17
	3	0.01831	0.71027	0.02679	24.0224	24.8512	25.0222	0.8166	0.7935	0.7903	105.39	51.44	67.35
	4	0.01926	0.71027	0.03922	22.7874	24.8312	23.1570	0.8552	0.7955	0.8277	129.56	41.35	82.05
	5	0.01920	0.90172	0.03722	25.0861	25.1119	25.0063	0.8729	0.8553	0.8260	131.03	77.51	90.18
Star Fish													
	2	0.02813 0.06321	0.11162	0.01944	20.0004	22.5775	21.7269	0.8428	0.8032	0.8246	91.43	58.51 58.03	45.44
	3		0.30992	0.03792	20.4882	21.1583	22.0133	0.8333	0.8004	0.8022	116.30	58.03	77.02
	4	0.21739	0.70018	0.13270	21.0632	22.2257	24.5721	0.8510	0.7994	0.8365	108.39	44.00	72.45
	5	0.51910	0.92732	0.42680	23.1567	25.5004	26.1489	0.8371	0.8177	0.8024	111.59	81.25	69.30
Sailor	2	0.12763	0.93471	0.37703	20.7738	22.1268	21.2311	0.8248	0.8210	0.7937	93.51	46.29	55.03
	3	0.28711	0.90182	0.52893	25.9125	25.9984	26.1489	0.8537	0.8422	0.8325	141.38	51.49	50.17
	4	0.48291	0.98271	0.72279	23.3532	23.9552	25.1362	0.8440	0.8001	0.8228	127.51	70.14	68.47
	5	0.71032	0.99013	0.93321	24.0284	25.0061	24.9958	0.8206	0.7990	0.7993	130.09	65.39	82.37

For all the test images, the histogram (Figure b) and Otsu guided BDFA based processed images for m = 2, 3, 4, and 5 are presented (Figures (c) to (f)) for all the considered test images. The quality of image segmentation is better for all the images when m = 5 compared to lesser "m" values.

The objective values and optimal threshold values for Otsu guided BDFA, LFFA, and FA are presented in Table 1. The other quality measures such as standard deviation, PSNR, SSIM, and CPU time are depicted in Table 2. From Table 1, it is seen that the BDFA offers better objective function values for most of the test images compared to the LFFA and FA.

6. Conclusion

In this paper, optimal multilevel image thresholding problem is addressed using Otsu guided firefly algorithms. The proposed histogram based bounded search technique helps in reducing the computation time. Further, the performances of the BDFA, LFFA, and FA are evaluated using parameters such as objective function, standard deviation, PSNR, SSIM, and search time of CPU. When the assigned threshold level is two (m = 2), all the FAs provide approximately similar threshold values. When "m" increases, the search time taken by the BDFA regularly increases compared to LFFA and FA. From the result, it is evident that, for m > 3, Brownian distribution based FA provides better objective function, PSNR, and SSIM, whereas Lévy flight based FA shows faster convergence with relatively lower CPU time. To analyze the permanence of the algorithms, the standard deviations of 20 runs have been presented in Table 1 for Otsu's between-class variance. The PSNR and the SSIM presented in Table 2 also prove the efficiency of the proposed Brownian distribution guided firefly algorithm. Due to the smaller search step, the BD guided firefly algorithm's run time is considerably larger than Lévy flight guided firefly and the traditional FAs.

Conflict of Interests

The authors declare that there is no conflict of interests regarding the publication of this paper.

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