



# Article (refereed) - postprint

Ritchie, Paul D.L.; Clarke, Joseph J.; Cox, Peter M.; Huntingford, Chris. 2021. **Overshooting tipping point thresholds in a changing climate.** *Nature*, 592 (7855). 517-523. <u>https://doi.org/10.1038/s41586-021-03263-2</u>

© The Author(s), under exclusive licence to Springer Nature Limited 2020

# For use in accordance with Nature Research's Terms of Reuse of archived manuscripts

This version is available at <a href="http://nora.nerc.ac.uk/id/eprint/530416/">http://nora.nerc.ac.uk/id/eprint/530416/</a>

Copyright and other rights for material on this site are retained by the rights owners. Users should read the terms and conditions of use of this material at <u>https://nora.nerc.ac.uk/policies.html#access</u>.

This document is the authors' final manuscript version of the journal article, incorporating any revisions agreed during the peer review process. There may be differences between this and the publisher's version. You are advised to consult the publisher's version if you wish to cite from this article.

The definitive version is available at <a href="https://www.nature.com/">https://www.nature.com/</a>

Contact UKCEH NORA team at <u>noraceh@ceh.ac.uk</u>

The NERC and UKCEH trademarks and logos ('the Trademarks') are registered trademarks of NERC and UKCEH in the UK and other countries, and may not be used without the prior written consent of the Trademark owner.

- 1 Overshooting Tipping Point Thresholds in A Changing Climate
- 3 Paul D. L. Ritchie<sup>1</sup>, Joseph J. Clarke<sup>1</sup>, Peter M. Cox<sup>1</sup>, Chris Huntingford<sup>2</sup>

<sup>1</sup> College of Engineering, Mathematics and Physical Science, University of Exeter, EX4 4QF, UK
 <sup>2</sup> UK Centre for Ecology and Hydrology, Wallingford, Oxon OX10 8BB, UK

7

2

4

8 9 Paleo-records suggest that the climate system has tipping points, where small changes in forcing 10 cause substantial and irreversible alteration to Earth system components called tipping elements. 11 As atmospheric greenhouse gas concentrations continue to rise due to fossil fuel burning, human 12 activity could also trigger tipping. These would be difficult for society to adapt to. Previous studies 13 report low global warming thresholds above pre-industrial conditions for key tipping elements such 14 as ice-sheet melt. If so, high contemporary rates of warming imply that the exceedance of these 15 thresholds is almost inevitable. It is widely assumed that this means we are now committed to 16 suffering these tipping events. We show that this conventional wisdom may be flawed, especially 17 for slow onset tipping elements in our rapidly changing climate. Recently developed theory 18 indicates that a threshold may be temporarily exceeded without prompting a change of system 19 state, if the overshoot time is short compared to the effective timescale of the tipping element. To 20 demonstrate this, we consider transparently simple models of tipping elements with prescribed 21 thresholds, driven by global warming trajectories that peak before returning to stabilise at 1.5°C of 22 global warming.

23

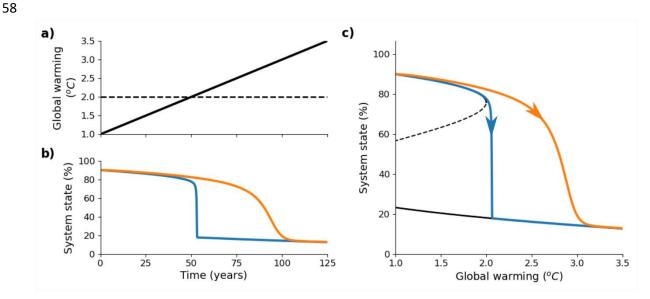
# 24 Introduction

Multiple strands of evidence indicate that components of the Earth System, called Tipping Elements<sup>1</sup>, 25 26 are capable of large and rapid changes in response to relatively small changes to forcings<sup>2</sup>. Tipping 27 Elements are often irreversible over multiple human generations: the original system state is not 28 recovered when the forcing is brought back to its original value. The point beyond which a Tipping 29 Element changes state is called a Tipping Point<sup>3,4</sup>. Tipping points are evident in paleoclimate records<sup>5,6</sup>, 30 as well as in future projections made with Earth System Models<sup>7</sup>. Tipping points are normally 31 characterised by the global warming levels at which they occur. These tipping point thresholds (hereafter thresholds) are often estimated to be at low levels of global warming<sup>8-12</sup>, and it is these 32 33 assessments that in part have led to the societal aspiration to restrict global warming to low levels 34 such as 2.0°C or even 1.5°C above the pre-industrial period<sup>10,13,14</sup>. However, current emission levels 35 and measured warming rates suggest that keeping below these global warming levels will be difficult for society to achieve<sup>15,16</sup>. It is therefore important to ask if thresholds could be briefly overshot 36 without triggering the transition to an alternative state. Despite the pressing requirement to answer 37 this question, very few assessments exist of whether the overshoot of thresholds is possible, and if so 38 what magnitudes and timescales are safe<sup>17-19</sup>. Nevertheless, dynamical systems theory shows that 39 temporary tipping point overshoot is both possible and can be quantified<sup>20,21</sup>. We combine this theory 40 41 with transparently simple models of four potential tipping elements to determine the possible global 42 warming trajectories that allow for a safe overshoot of the prescribed thresholds.

43

# 44 The importance of timescales

Of greatest relevance here are tipping points that may occur in response to a change in global temperature. Such warming might be over long paleo periods, or as of interest here, at a faster decade-to-century timescale, largely driven by the human burning of fossil fuels and rising atmospheric greenhouse gas concentrations<sup>22</sup>. Once global warming passes a threshold for the system, the current state of the system starts to undergo a transition to an alternative state, where such a state might be vastly different. This transition may occur relatively quickly - we refer to these as having a fast tipping onset, and hypothetical examples include Amazon forest dieback<sup>23</sup> and disruption to monsoons<sup>24</sup>. Other transitions may take much longer, and these slow onset cases include ice sheet loss<sup>25</sup> and the collapse of the Atlantic Meridional Overturning Circulation (AMOC)<sup>26</sup>. A transgression of a tipping point threshold does not necessarily cause an instantaneous transition, especially for slow onset tipping elements, as illustrated schematically in Figure 1 (and animated with stability landscapes in **Video 1**). Instead the system lives on borrowed time<sup>27</sup> before tipping occurs, and such inertia might allow for a temporary 'safe' global warming overshoot.



**Figure 1: Comparison between slow and fast onset tipping elements**. **a**) Idealised time series of a linear increase in global warming above pre-industrial levels that crosses an illustrative threshold of 2°C (dashed line). **b**) Time series of system state for a fast onset tipping system (blue) and slow onset tipping system (orange), with the same threshold and the same global warming forcing as in **a**). **c**) System state vs global warming for the fast onset tipping element (blue) and slow onset tipping element (orange). Both systems have a desired state, which is the upper solid black curve and represent contemporary conditions. An undesired stable state, given by the lower solid black curve, coexists with the desired state for warming levels below the 2°C threshold, separated by an unstable state (black dashed curve). Above the threshold, only the undesired equilibrium state remains.

59 Figure 1a considers a scenario where global warming increases linearly with time. We assume two 60 tipping elements of the climate system which have the same threshold of 2°C of global warming, 61 denoted by the horizontal black dashed line. Figure 1b displays the time series response of the system 62 state to this linear warming increase for a fast-onset tipping element (blue) and a slow-onset tipping element (orange). Despite both tipping elements having the same threshold, which is transgressed 63 64 after 50 years, only the fast system experiences rapid tipping. In contrast, the slow system maintains 65 the initial system state for much longer, with full tipping not occurring until about year 100. Figure 1c presents these trajectories, and the equilibrium states, as a function of global warming. Stable states 66 67 are represented by black solid curves and the unstable state by the black dashed curve. For warming 68 levels below the threshold, the system is bistable, with a desirable upper stable branch (representing 69 current conditions) and an undesirable lower stable system state coexisting. Importantly, beyond the 70 threshold, only the undesirable state persists. The trajectories of both the fast and slow systems 71 closely track the equilibrium state initially. Once the equilibrium state disappears at the threshold, the 72 fast system tips nearly instantaneously, whereas the slow system at first appears unaware of the 73 disappeared state. For the parameters in this illustrative example, it is not until the warming has 74 exceeded 2.5°C that the slow system begins to tip. We assess if this delay in tipping can be exploited 75 to enable safe overshoots of thresholds that do not result in the system tipping to the undesired state. 76 Similar delayed tipping phenomena has been observed in numerical runs of an Energy Balance 77 Model<sup>28</sup>. A ghost state, also known as an attractor relic, can be another reason for tipping to be

- delayed<sup>29,30</sup>. Features not included here such as internal variability and seasonal cycles will also have
   an influence on the size of delay.
- 80
- 81 In our analysis we consider global warming overshoot trajectories,  $\Delta T$ , introduced by Huntingford et 82 al. (2017)<sup>31</sup>:

 $\Delta T = \Delta T_0 + \gamma t - (1 - e^{-\mu t})[\gamma t - (\Delta T_{Lim} - \Delta T_0)], \qquad \mu(t) = \mu_0 + \mu_1 t.$ (1)

These temperature trajectories contain five parameters. Parameter  $\Delta T_0$ , is the absolute warming since 84 85 the preindustrial period. Parameter  $\Delta T_{Lim}$ , is an eventual stabilisation temperature, set to be the longterm Paris target of 1.5°C<sup>14</sup>. An exponential decay term characterises the transition that moves away 86 87 from the current linear growth (and towards stabilisation). The transition timescale,  $\mu(t)$ , can change 88 linearly in time, described by the parameters,  $\mu_0$  and  $\mu_1$ . Such a time-dependency captures if society 89 places more effort to lower global warming rates in the near term, or instead many decades ahead. 90 For relatively slower transitions, the profiles initially overshoot  $\Delta T_{Lim}$ , as used in this study. The 91 parameter,  $\gamma$ , is chosen to ensure a realistic rate of global warming in the recent past, given the chosen 92 values of the other parameters. These global temperature trajectories are designed to allow varying 93 levels of temperature overshoot for varying periods of time, while also matching the contemporary 94 rate of global warming and asymptoting to the long-term Paris target of 1.5°C.

95

Steffen et al.  $(2018)^{11}$  characterised global warming ranges at which the climate tipping elements would undergo state changes if exceeded for sufficiently long. However, the models for the climate tipping elements we consider in this study (detailed in Boxes 1 and 2) have their individual forcing parameters and thresholds that cause the systems to undergo state changes if exceeded for sufficiently long. For clarity, these forcing parameters are: local temperature for forest dieback; solar constant for ice cap loss; planetary albedo for monsoon disruption; and freshwater forcing for AMOC collapse. We assume that each of these forcing parameters p are proportional to the global warming T therefore

103 *T*, therefore

$$T = T_{TP} + (p - p_{TP}) \frac{T_{TP} - T_{ref}}{p_{TP} - p_{ref}},$$

104

where the subscript TP refers to the threshold (for temperature these are chosen at the centre of the ranges given by Steffen et al. (2018)<sup>11</sup>). The subscript ref is a reference level related to the current climate.

108

109 We now move to specific examples of tipping elements. Figure 2 (animated with stability landscapes 110 in **Video 2**) demonstrates the concept of overshooting a threshold for a model of the AMOC<sup>32-34</sup> – see 111 Box 2 for details of the AMOC model. The potential collapse of the AMOC is one example of a slow 112 tipping onset where the transitional timescale is assumed to be of the order of centuries<sup>1</sup>. Steffen et 113 al. (2018)<sup>11</sup> have characterised the critical global warming for the collapse of the AMOC to be in the 114 range of 3-5°C. In our model, we set the threshold to be at the centre of this warming range, namely 115 at 4°C of global warming above pre-industrial.

116

In Figure 2a we consider two different overshoots of the AMOC threshold; the first trajectory (blue curve) represents a relatively small peak overshoot of 1°C but takes approximately 3,500 years to stabilise at 1.5°C. The second trajectory (orange curve) overshoots the threshold by 2°C but stabilises much faster (1,150 years) at the same level. Conventional wisdom suggests that both trajectories would lead to the AMOC tipping to the 'off' state, because in both cases the threshold has been exceeded. However, these trajectories have very different and rather counterintuitive risks of tipping when timescales are taken properly into account.

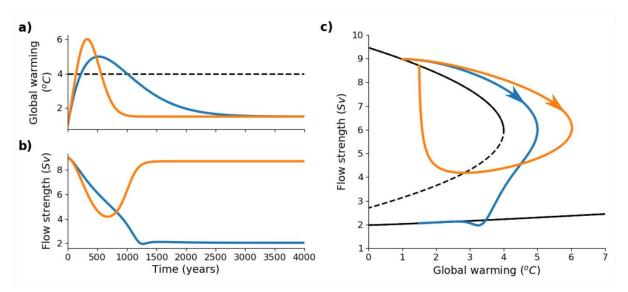


Figure 2: Illustration of overshooting a threshold in a model for the Atlantic Meridional Overturning Circulation (AMOC). a) Two time series of contrasting sample overshoot trajectories are shown in global warming given by Equation (1). The blue curve (parameter values:  $\mu_0 = 1.8 \times 10^{-3}$ ,  $\mu_1 = 2.0 \times 10^{-7}$  per year,  $\gamma = 0.0191^{\circ}$ C per year) is a small and long overshoot, while the orange curve (parameter values:  $\mu_0 = -1.3 \times 10^{-3}$ ,  $\mu_1 = 7.0 \times 10^{-6}$  per year,  $\gamma = 0.02065^{\circ}$ C per year) is a much larger yet quick overshoot. The black dashed line indicates the threshold, above which if global warming is fixed, the AMOC would eventually collapse. b) Time series response of ocean flow strength corresponding to the warming overshoot trajectories presented in a). c) Flow strength vs global warming for short, long overshoot and big fast overshoot (colours as in a) and b)). An AMOC 'on' state (upper solid black curve) and an AMOC 'off' state (lower solid black curve) both coexist for warming levels below the threshold of 4°C and are separated by an unstable state (black dashed curve). Above the threshold only the AMOC 'off' state remains.

- 125 The AMOC is characterised by its north-south flow strength, measured in Sverdrups (Sv). In Figure 2b
- 126 the blue time series shows that a small but long-lasting overshoot does not prevent the system tipping,
- 127 and instead causes the flow strength to drop from 9Sv to only 2Sv, indicating a sustained collapse of
- 128 the circulation. The flow rate remains severely weakened, even as global warming decreases. In
- 129 contrast, the larger but shorter overshoot allows the flow strength to recover after a strong initial
- 130 weakening (orange time series). The AMOC has been able to recover in this scenario because the
- 131 reversal in global warming has been sufficiently fast.
- 132

133 Plotting this as a function of warming (Figure 2c), reveals a clearer picture of the underlying dynamics 134 taking place. For the small overshoot (blue trajectory), the substantial amount of time spent over the 135 threshold means that once global warming is back below the threshold, the circulation has almost 136 reached its collapsed state. Hence the circulation does not recover and is destined to remain 'off' 137 regardless of how far warming is further reduced. For the faster reversal in global warming (orange 138 trajectory), resulting in less time over the threshold once warming is brought back below 4°C the 139 collapsed state has yet to be reached. Therefore, with a continued fast reduction in warming, the 140 trajectory is able to cross the unstable state (black dashed curve) – also known as a melancholia 141 state<sup>28</sup>, after which the flow strength begins to recover, preventing the tipping. It is important to note, 142 in Figure 2c, that such crossing occurs at a warming below 4°C. Hence safely returning to the initial 143 state requires a period of time when global warming is below the threshold.

144

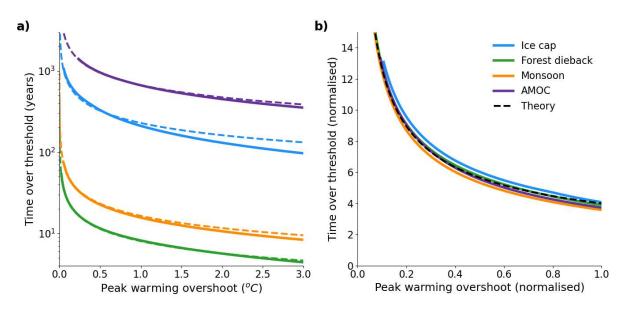
### 145 Theoretical basis

- 146 We now provide a more theoretical basis to the numerical findings presented in Figure 2. For a fixed
- 147 stabilisation level, there are two attributes that determine whether a system can safely overshoot a

148 threshold. These are the amount by which the threshold is exceeded relative to the difference between the threshold and the stabilisation level,  $\chi$ , and the time spent over that threshold,  $t_e$ . For 149 symmetric parabolic overshoots, it has been shown that a system will not tip if  $\chi < 16 \tau^2 / t_e^2$ , where 150  $\tau$  is the effective timescale of the system<sup>20</sup>. Here we define the effective timescale of a tipping element 151 as the recovery time from perturbations in the equilibrium state at 1.5°C global warming. The effective 152 153 timescale depends on the distance to the threshold and can be determined from the lag-1 autocorrelation statistic (see Ritchie et al., 2019<sup>20</sup> for further details). In Figure 3 we show how the 154 155 theory compares against four tipping elements of the climate system<sup>1,11</sup>: collapse of the AMOC<sup>32</sup>; 156 melting of the ice cap<sup>35</sup>; disruption to the Indian Summer Monsoon<sup>24</sup>; and forest dieback<sup>23</sup>. The simple 157 models used to represent these fast tipping elements and slow tipping elements are presented in 158 Boxes 1 and 2 respectively.

159

160 Figure 3a shows the boundaries of safe and unsafe overshoots for each of these potential tipping 161 elements, in a regime diagram defined by the peak overshoot and exceedance time of each threshold. 162 There is a clear separation between tipping elements that can be classified as fast onset and those 163 classified as slow onset tipping elements. The slower onset tipping elements are ice cap melt and 164 AMOC collapse, and it is possible to safely overshoot their thresholds for multiple centuries before 165 returning and stabilising at the 1.5°C level. In contrast, for the faster onset tipping elements of 166 monsoon disruption and Amazon forest dieback, overshoot is possible only for decades or even just years before tipping would be induced. In Figure 3a, we present the boundaries derived numerically 167 168 from the temperature overshoots defined by Huntingford et al. (2017)<sup>31</sup> (solid curves) and analytically 169 from the inverse square theory (dashed curves). Normalising the time over the threshold with the 170 effective timescale of each system, and also the peak warming overshoot with the distance from the 171 threshold at 1.5°C, collapses the theoretical curves onto a single curve (Figure 3b). This panel shows a



**Figure 3: Boundary curves separating safe and unsafe overshoots that start at current warming levels and return to stabilise at the 1.5°C Paris Climate Agreement Target. a)** Four climate tipping elements are shown (as marked), based on the peak warming overshoot and time over individual thresholds. Above and right of boundary curves represents where tipping occurs while below and left provides the safe overshoots of the threshold for each tipping element. Solid boundary curves are calculated numerically and give the exact boundary, and dashed curves represent the inverse square law theory. b) Same as a) but with the peak warming overshoot normalised by the threshold distance beyond the 1.5°C Paris Target and the time over the threshold normalised by the effective timescale of the individual systems. Presented in this way, the theoretical curves for each tipping element collapse onto one curve given by the black dashed curve.

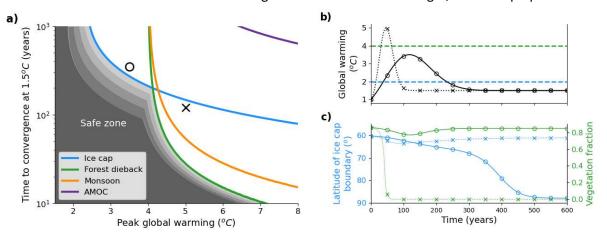
- 172 good agreement between the boundary calculated numerically for our temperature overshoots and
- 173 the theoretical inverse square boundary (which assumes a parabolic overshoot), for all four climate
- 174 tipping elements.
- 175

## 176 Safe and unsafe overshoots

177 Instead of considering the peak and time over the specific thresholds, Figure 4a displays the numerical 178 boundaries of safe overshoots for absolute peak global warming and time to stabilisation at the Paris 179 Climate Agreement target of 1.5°C. The grey shaded region indicates all overshoots of the 1.5°C target 180 that would not result in tipping for any of the four chosen tipping elements of the climate system. 181 Figure 4a indicates that the ice cap could be preserved if peak warming is limited to 3°C instead of the 182 more conventional 2°C threshold (i.e. an overshoot of 1°C) if the time taken to stabilise at 1.5°C is 183 under 400 years. It is important to note that, overshooting slightly more than intended can be offset 184 by stabilising at some lower level. Similarly, the AMOC can be maintained up to a peak warming of 6°C 185 provided the time to converge to 1.5°C is less than 1,200 years, despite the assumed 4°C threshold. 186 Significantly, for the faster onset tipping elements, there is little opportunity for safe overshoot.

187

188 We present a more detailed comparison between a slow onset tipping element (ice cap melt) with a 189 low threshold, and a fast onset tipping element (Amazon forest dieback) with a higher threshold in 190 Figure 4c. We consider two overshoot scenarios, as marked by a cross and a circle in Figure 4a, of the 191 1.5°C target before returning to stabilise at that level. The time evolution of these scenarios is shown 192 in Figure 4b. One scenario considers a peak global warming of 3.5°C that stabilises at 1.5°C after 350 193 years (solid curve with circles) and the other has a higher peak warming of 5°C but takes 120 years to 194 converge to 1.5°C (dotted curve with crosses). The responses to these overshoot scenarios are 195 displayed in Figure 4c, where colour differentiates between the latitude of the ice cap boundary (blue) 196 and vegetation fraction characterising forest dieback (green), and the line style and marker separates 197 the overshoot scenarios. For a small but long overshoot of the 1.5°C target, the ice cap tips to an ice-



**Figure 4: Boundaries of safe overshoots for multiple tipping points. a)** Boundary curves separating safe and unsafe overshoots for four climate tipping elements considered (see Boxes 1 and 2), based on the peak global warming and time to stabilisation at 1.5°C warming. Above and right of the individual coloured boundary curves represents where tipping is not avoided, whilst below and left provides the safe zone for each particular tipping element. The grey shaded region indicates the safe zone for all tipping elements. Each different grey shade indicates the boundary of this safe zone if the threshold for all tipping elements were 0.1°C lower. Cross and circle markers indicate parameter values of contrasting sample warming overshoot trajectories considered in **b**) and **c**). **b**) Time series of sample overshoot trajectories in global warming, differentiated by line type and marker. Horizontal blue and green dashed lines denote thresholds for the ice cap and forest dieback respectively. **c**) Time series of ice cap boundary (blue) and Amazon vegetation fraction (green) response to the two overshoot trajectories presented in **b**). Line type and symbols identical between **b**) and **c**).

198 free state because its threshold has been transgressed for a sufficiently long time. However, in this 199 scenario, there has been no forest dieback simply because its threshold has not been crossed. 200 However, the opposite behaviours are observed for a higher peak global warming with a quick 201 convergence to 1.5°C. In this scenario the ice cap boundary is maintained at close to 60°N. Although 202 there is a large exceedance of the threshold it is possible to return to the initial state because the time 203 over that threshold is sufficiently short compared to the effective timescale of the system. Forest 204 dieback is induced due to the fast onset of the tipping permitting only very limited overshoots of the 205 threshold. Scenarios with a high peak warming and a fast convergence to the 1.5°C stabilisation level 206 do however imply a fast reduction in temperature, which may not be possible with available 207 technologies. The 'point of no return' is therefore also practically constrained by the rate at which 208 global warming can be reduced.

# 210 Discussion

Our analysis reveals that for many climate tipping points it is possible to cross a threshold temporarily without triggering tipping to a new state. This finding is particularly relevant for potential slow-onset tipping elements such as ice-sheet melt or collapse of the AMOC. Hence, the 'point of no return' for a slow onset tipping element is not the threshold but a point beyond the threshold. How far this point

215 is beyond the threshold is determined by three factors: 1) the effective timescale of the system 2) how

216 fast global warming can be reduced and 3) the level at which warming stabilises.

217

209

218 In this study we have used transparently simple models for four climate tipping elements, with a 219 prescribed choice of threshold in each case based-on previous studies<sup>11</sup>. In particular, with the 220 exception of the monsoon model, the models used are first order with a single timescale. Further work 221 is required to demonstrate that similar behaviour is present in more complex models, in which 222 multiple variables act on multiple timescales and the dynamics around the threshold is much more 223 complex. While the thresholds for climate tipping points are highly uncertain, we have assumed the central estimates as published by Steffen et al. (2018)<sup>11</sup> and focussed specifically on the impact of 224 225 timescales on top of these prescribed thresholds. The tipping element with the earliest threshold is 226 also the one with the longest timescale (ice sheet melt), whereas faster tipping elements tend to have 227 higher thresholds (e.g. tropical forest dieback). This means that safe levels of peak warming are set by 228 faster onset tipping points, but the safe stabilisation warming level is set by the slower onset tipping 229 points.

230

In our analysis we have considered the safe and unsafe boundaries for each tipping element individually. However, recently it has been proposed that tipping elements are coupled and that tipping cascades are possible<sup>36,37</sup>. The timescales and coupling strength between tipping elements, could result in the overall threshold being lower. Therefore, further research is required to calculate 'safe' overshoots for coupled tipping elements.

236

This study highlights the importance of timescales for possible tipping points in a changing climate. Slow onset tipping elements permit temporary overshoots of a threshold without triggering tipping to a new state. Both the approach rate to any tipping point threshold, and actions taken to reverse warming once over that threshold, will therefore determine if climate remains safe from unwelcome

- warming once over thestate changes. state
- 242
- 243
- 244
- 245
- 246
- 247
- 248

249	References					
250						
251	1	Lenton, T. M. et al. Tipping elements in the Earth's climate system. Proceedings of the				
252		national Academy of Sciences <b>105</b> , 1786-1793 (2008).				
253		This paper was the first study to identify potential tipping elements in the climate system.				
254	2	Lenton, T. M. Environmental tipping points. Annual Review of Environment and Resources				
255		<b>38</b> , 1-29 (2013).				
256	3	Scheffer, M. et al. Early-warning signals for critical transitions. Nature 461, 53-59 (2009).				
257	4	Lenton, T. M. Early warning of climate tipping points. Nature Climate Change 1, 201-209				
258		(2011).				
259	5	Dakos, V. et al. Slowing down as an early warning signal for abrupt climate change.				
260		Proceedings of the National Academy of Sciences <b>105</b> , 14308-14312 (2008).				
261		This paper presents evidence of tipping points in paleoclimate records.				
262	6	Ditlevsen, P. D. & Johnsen, S. J. Tipping points: early warning and wishful thinking.				
263		Geophysical Research Letters <b>37</b> (2010).				
264	7	Drijfhout, S. et al. Catalogue of abrupt shifts in Intergovernmental Panel on Climate Change				
265		climate models. Proceedings of the National Academy of Sciences 112, E5777-E5786 (2015).				
266		This study illustrates that tipping points are found in future projections with complex Earth				
267		System Models.				
268	8	Nobre, C. A. & Borma, L. D. S. 'Tipping points' for the Amazon forest. Current Opinion in				
269		Environmental Sustainability <b>1</b> , 28-36 (2009).				
270	9	Robinson, A., Calov, R. & Ganopolski, A. Multistability and critical thresholds of the				
271		Greenland ice sheet. Nature Climate Change 2, 429-432 (2012).				
272	10	Schellnhuber, H. J., Rahmstorf, S. & Winkelmann, R. Why the right climate target was agreed				
273		in Paris. Nature Climate Change <b>6</b> , 649-653 (2016).				
274	11	Steffen, W. et al. Trajectories of the Earth System in the Anthropocene. Proceedings of the				
275		National Academy of Sciences 115, 8252-8259 (2018).				
276		This paper estimates tipping point thresholds (central estimates used here).				
277	12	Kriegler, E., Hall, J. W., Held, H., Dawson, R. & Schellnhuber, H. J. Imprecise probability				
278		assessment of tipping points in the climate system. Proceedings of the national Academy of				
279		Sciences <b>106</b> , 5041-5046 (2009).				
280	13	Lenton, T. M. et al. Climate tipping points - too risky to bet against. Nature 575, 592-595,				
281		doi:10.1038/d41586-019-03595-0 (2019).				
282	14	UNFCCC, V. Adoption of the Paris agreement. Proposal by the President (2015).				
283	15	Raftery, A. E., Zimmer, A., Frierson, D. M., Startz, R. & Liu, P. Less than 2°C warming by 2100				
284		unlikely. <i>Nature climate change <b>7</b>,</i> 637 (2017).				
285	16	Tong, D. <i>et al.</i> Committed emissions from existing energy infrastructure jeopardize 1.5°C				
286		climate target. <i>Nature</i> <b>572</b> , 373-377 (2019).				
287	17	Alkhayuon, H., Ashwin, P., Jackson, L. C., Quinn, C. & Wood, R. A. Basin bifurcations,				
288		oscillatory instability and rate-induced thresholds for Atlantic meridional overturning				
289		circulation in a global oceanic box model. Proceedings of the Royal Society A 475, 20190051				
290		(2019).				
291	18	Jackson, L. & Wood, R. Hysteresis and Resilience of the AMOC in an Eddy-Permitting GCM.				
292		Geophysical Research Letters <b>45</b> , 8547-8556 (2018).				
293	19	Kaszás, B., Haszpra, T. & Herein, M. The snowball Earth transition in a climate model with				
294		drifting parameters: Splitting of the snapshot attractor. Chaos: An Interdisciplinary Journal of				
295		Nonlinear Science <b>29</b> , 113102 (2019).				
296	20	Ritchie, P., Karabacak, Ö. & Sieber, J. Inverse-square law between time and amplitude for				
297		crossing tipping thresholds. Proceedings of the Royal Society A 475, 20180504 (2019).				
298		This study describes the mathematical theory for how much and how long a tipping point				
299		threshold can be exceeded without causing tipping.				

300 301 302	21	O'Keeffe, P. E. & Wieczorek, S. Tipping Phenomena and Points of No Return in Ecosystems: Beyond Classical Bifurcations. <i>SIAM Journal on Applied Dynamical Systems</i> <b>19</b> , 2371-2402 (2020).
303 304 305	22	Pachauri, R. K. et al. Climate change 2014: synthesis report. Contribution of Working Groups I, II and III to the fifth assessment report of the Intergovernmental Panel on Climate Change. (Ipcc, 2014).
306 307	23	Cox, P. M. <i>et al.</i> Amazonian forest dieback under climate-carbon cycle projections for the 21st century. <i>Theoretical and applied climatology</i> <b>78</b> , 137-156 (2004).
308 309	24	Zickfeld, K., Knopf, B., Petoukhov, V. u. & Schellnhuber, H. Is the Indian summer monsoon stable against global change? <i>Geophysical Research Letters</i> <b>32</b> (2005).
310	25	Walker, G. The tipping point of the iceberg. Nature 441, 802-805, doi:10.1038/441802a
311		(2006).
312 313	26	Stocker, T. F. & Wright, D. G. Rapid transitions of the ocean's deep circulation induced by changes in surface water fluxes. <i>Nature</i> <b>351</b> , 729-732 (1991).
314	27	Hughes, T. P., Linares, C., Dakos, V., Van De Leemput, I. A. & Van Nes, E. H. Living
315 316		dangerously on borrowed time during slow, unrecognized regime shifts. <i>Trends in ecology</i> & <i>evolution</i> <b>28</b> , 149-155 (2013).
317	28	Lucarini, V. & Bódai, T. Transitions across melancholia states in a climate model: Reconciling
318		the deterministic and stochastic points of view. <i>Physical review letters</i> <b>122</b> , 158701 (2019).
319	29	Wernecke, H., Sándor, B. & Gros, C. Attractor metadynamics in terms of target points in
320		slow-fast systems: adiabatic versus symmetry protected flow in a recurrent neural network.
321		Journal of Physics Communications <b>2</b> , 095008 (2018).
322	30	Medeiros, E. S., Caldas, I. L., Baptista, M. S. & Feudel, U. Trapping phenomenon attenuates
323		the consequences of tipping points for limit cycles. <i>Scientific reports</i> <b>7</b> , 42351 (2017).
324	31	Huntingford, C. et al. Flexible parameter-sparse global temperature time profiles that
325		stabilise at 1.5 and 2.0° C. (2017).
326		This article defines the temperature overshoot profiles used in this study.
327	32	Cessi, P. A simple box model of stochastically forced thermohaline flow. <i>Journal of physical</i>
328		oceanography <b>24</b> , 1911-1920 (1994).
329	33	Dijkstra, H. A. Nonlinear climate dynamics. (Cambridge University Press, 2013).
330	34	Stommel, H. Thermohaline convection with two stable regimes of flow. <i>Tellus</i> <b>13</b> , 224-230
331		(1961).
332	35	Herald, C. M., Kurita, S. & Telyakovskiy, A. S. Simple Climate Models to Illustrate How
333		Bifurcations Can Alter Equilibria and Stability. Journal of Contemporary Water Research &
334		Education <b>152</b> , 14-21 (2013).
335	36	Dekker, M. M., Von Der Heydt, A. S. & Dijkstra, H. A. Cascading transitions in the climate
336		system. Earth System Dynamics 9, 1243-1260 (2018).
337	37	Wunderling, N., Donges, J. F., Kurths, J. & Winkelmann, R. Interacting tipping elements
338		increase risk of climate domino effects under global warming. Earth System Dynamics
339		Discussions, 1-21 (2020).
340	38	Levermann, A., Schewe, J., Petoukhov, V. & Held, H. Basic mechanism for abrupt monsoon
341		transitions. Proceedings of the National Academy of Sciences <b>106</b> , 20572-20577 (2009).
342	39	North, G. R. The small ice cap instability in diffusive climate models. Journal of the
343		atmospheric sciences <b>41</b> , 3390-3395 (1984).
244		

# Box 1: Models of fast tipping elements

# Forest dieback model

Forest dieback is represented by a modified version of the TRIFFID model<sup>23</sup> for a single vegetation type. Vegetation fraction v is modelled by a Lotka-Volterra equation:

$$\frac{dv}{dt} = gv(1-v) - \gamma v,$$

where  $\gamma$  is a disturbance rate and g is a growth term which is assumed to be parabolic in the local temperature,  $T_l$ :

$$g = g_0 \left[ 1 - \left( \frac{T_l - T_{opt}}{\beta} \right)^2 \right]$$

There is an optimal temperature  $T_{opt}$  for which growth is maximal and equal to  $g_0$ . The parameter  $\beta$  determines the temperature half-width for which vegetation grows. A negative growth-rate implies additional tree mortality. However, there is an additional feedback on the local temperature,  $T_l$ , a decline in vegetation results in an increase in temperature:

$$T_l = T_f + (1 - v)\alpha.$$

The temperature  $T_f$  is used as the forcing parameter and defines the temperature if there was total forest cover. The temperature difference between total forest and bare soil is defined by the parameter  $\alpha$ . Table 1 lists all the parameters and their values used in the forest dieback model.

Table 1: Table of parameters used in vegetation dieback model

Parameter	Value	Unit	Description	
α	5	٥C	difference between surface temperature of bare-soil and forest	
β	10	٥C	half-width of the growth versus temperature curve	
${\boldsymbol{g}}_{0}$	2	$yr^{-1}$	maximum growth-rate	
γ	0.2	$yr^{-1}$	disturbance rate	
T <sub>opt</sub>	28	٥C	optimal temperature for plant growth	

# Indian Summer Monsoon model

The summer temperature gradient generates monsoon winds over the Indian subcontinent which hold moisture having emanated from the Indian Ocean. Once over the land the moisture falls as precipitation, which in turn releases heat, amplifying the temperature gradient and generating stronger winds<sup>38</sup>. This key feedback mechanism of the monsoon is captured in a reduced form model introduced by Zickfeld et al.  $(2005)^{24}$ . Zickfeld et al.  $(2005)^{24}$  identified a threshold in the planetary albedo  $A_{sys}$ , such that if it was exceeded for sufficiently long, the monsoon season would be disrupted. Ritchie et al. (2019) made further reductions to the model though retained the key mechanisms of the monsoon. We adopt the same version of the model as Ritchie et al.  $(2019)^{20}$ , which models the time evolution of the land temperature T, and specific humidity Q:

$$\begin{aligned} \frac{dQ}{dt} &= \frac{E(Q,T) - P(Q) + A_v(Q,T)}{I_Q}, \\ \frac{dT}{dt} &= \frac{\mathcal{L}\big(P(Q) - E(Q,T)\big) + F_\downarrow\big(1 - A_{sys}\big) - F_\uparrow(T) + A_T(Q,T)}{I_T}. \end{aligned}$$

For further details of variables and a table of the parameter values used, we ask the reader to refer to Ritchie et al. (2019)<sup>20</sup>. The increase in planetary albedo required to cause a tipping in the monsoon is arguably more likely to occur due to increases in reflective anthropogenic aerosols rather than increases in greenhouse gases. We follow Steffen et al. (2018)<sup>11</sup> in assuming that this threshold corresponds to about 4°C of global warming.

# Box 2: Models of slow tipping elements

# Ice cap model

North  $(1984)^{39}$  devised a model to offer an interpretation of the small ice cap instability. It was found that simple climate models, which employ heat diffusion and the ice-albedo feedback, show that ice caps smaller than a finite size are unstable. Specifically, for a given range in the solar constant  $S_0$  (a proxy for temperature) a large ice cap state and an ice-free state could coexist. The small ice cap instability is assumed to play a key role in the formation of large ice sheets such as Greenland. In this study we use a model, introduced by Herald et al.  $(2013)^{35}$ , that models the sine of the latitude of the ice cap boundary x, and captures the key mechanisms of the North model, namely the bistable regime:

$$\frac{dx}{dt} = -0.003 + (1-x) \left[ \frac{S_0}{4} - 355 + 3 \left( \frac{x - 0.89}{0.09} \right)^2 \right].$$

# Atlantic Meridional Overturning Circulation (AMOC) model

Analysing the flow between two boxes of water connected by an overflow and a capillary tube, Stommel  $(1961)^{34}$  devised the first model of the AMOC. The model measures the evolution of salinity and temperature fluxes between the two boxes, where one box was used to represent the cold salty waters of the North Atlantic and the other the warm fresh waters of the Tropics. Cessi  $(1994)^{32}$  made the additional assumption that the diffusion timescale is much larger than the temperature restoring timescale. This assumption means that temperature can be assumed constant and so the model can simply be written in terms of a rescaled salinity flux, y:

$$\frac{dy}{dt} = F - y[1 + \mu^2(1 - y)^2],$$

where  $\mu^2$  is the ratio of the diffusive and advective timescales. The AMOC is a temperature and salinity driven circulation and hence, the rescaled salinity flux y acts as a proxy for the strength of the flow Q:

$$Q = \frac{\eta V [1 + \mu^2 (1 - y)^2]}{t_d}$$

See Table 2 for a description of the parameters and their values, which are the same as those used in Dijkstra  $(2013)^{33}$ . The freshwater forcing F represents freshwater added to the North Atlantic and has a threshold such that maintained freshwater forcing above this level will eventually lead to a collapse of the AMOC.

 Table 2: Table of parameters used in AMOC model.

Parameter	Value	Unit	Description
$\mu^2$	6.2	1	Ratio of diffusive and advective timescales
$t_d$	180	yr	Diffusion timescale
V	$300 \times 4.5 \times 8,250$	km <sup>3</sup>	Ocean volume
η	$3.17 \times 10^{-5}$	Sv yr km <sup>-3</sup>	Scaling factor

345

346

347

348

349

350

351

# 352 Acknowledgments

- This work was supported by the European Research Council 'Emergent Constraints on Climate-Land feedbacks in the Earth System (ECCLES)' project, grant agreement number 742472 (P.D.L.R., J.J.C. and P.M.C.). P.M.C. was also supported by the European Union's Framework Programme Horizon 2020 for Research and Innovation under Grant Agreement No. 821003, Climate-Carbon Interactions in the Current Century (4C) project. C.H. acknowledges the Natural Environment Research Council National
- 358 Capability Fund awarded to the UK Centre for Ecology and Hydrology.
- 359

# 360 Author Contributions

- P.D.L.R., and P.M.C. designed and directed the research. All authors helped to shape the research and
   drafted the manuscript through weekly virtual meetings. P.D.L.R. performed the analysis and
   produced the figures and animations.
- 364

### 365 **Competing interests**

366 The authors declare no competing interests.