# Parallelizing the Camellia and SMS4 Block Ciphers

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# Outline of Talk



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- 3 Definitions and Preliminaries
- Practical Security Evaluation of GF-NLFSR against DC and LC
- 5 Application
  - Parallelizing Camellia
  - Parallelizing SMS4

### 6 Conclusion

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Motivation	

- Object of interest: Parallelizable *n*-cell GF-NLFSR structures
- Encryption speed faster by up to n times
- SDS versus SPN round functions
  - SDS: Too complex and not suitable for space and speed efficient implementation
  - SPN: Use relatively less resources
- $\Rightarrow$  Meanginful to investigate GF-NLFSR (with SPN) security against DC and LC

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# Our Contribution

- Provide a neat and concise proof of the result that for a 2nr-round parallelizable *n*-cell GF-NLFSR structure with an SPN round function having branch number  $\mathcal{B}$ , the number of differential active S-boxes  $\geq r\mathcal{B} + \lfloor \frac{r}{2} \rfloor$
- Parallelizing Camellia and SMS4: p-Camellia and p-SMS4
- Ensure that p-Camellia and p-SMS4 are secure against other block cipher cryptanalysis
- Hardware implementation advantages: Achieves higher maximum frequency with lower area and power demands
- ullet  $\Rightarrow$  Well suited for applications that require a high throughput

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SPN round function	

- *F*-function comprises: key addition layer, *S*-function, *P*-function.
- Neglect the effect of the round key since by assumption, the round key consists of independent and uniformly random bits, and is bitwise XORed with data
- *S*-function: non-linear transformation layer with *m* parallel *d*-bit bijective S-boxes
- P-function is a linear transformation layer

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SPN round function	

• Throughout, assume S-function and P-function bijective

$$S : GF(2^{d})^{m} \to GF(2^{d})^{m}, X = (x_{1}, \dots, x_{m}) \mapsto Z = S(X) = (s_{1}(x_{1}), \dots, s_{n}(x_{n}))$$
  

$$P : GF(2^{d})^{m} \to GF(2^{d})^{m}, Z = (z_{1}, \dots, z_{m}) \mapsto Y = P(Z) = (y_{1}, \dots, y_{n})$$
  

$$F : GF(2^{d})^{m} \to GF(2^{d})^{m}, X \mapsto Y = F(X) = P(S(X))$$

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### Differential and Linear Probabilities

#### Definition

Let  $x, z \in GF(2^d)$ . Denote the differences and the mask values of x and z by  $\Delta x$ ,  $\Delta z$ , and,  $\Gamma x$ ,  $\Gamma z$  respectively. The differential and linear probabilities of each S-box  $s_i$  are defined as:

$$DP^{s_i}(\Delta x \to \Delta z) = \frac{\#\{x \in GF(2^d) | s_i(x) \oplus s_i(x \oplus \Delta x) = \Delta z\}}{2^d},$$
$$LP^{s_i}(\Gamma z \to \Gamma x) = (2 \times \frac{\#\{x \in GF(2^d) | x \cdot \Gamma x = s_i(x) \cdot \Gamma z}{2^d} - 1)^2.$$

### Differential and Linear Probabilities

### Definition

The maximum differential and linear probabilities of S-boxes are defined as:

$$p_{s} = \max_{i} \max_{\Delta x \neq 0, \Delta z} DP^{s_{i}}(\Delta x \to \Delta z),$$
$$q_{s} = \max_{i} \max_{\Gamma x, \Gamma z \neq 0} LP^{s_{i}}(\Gamma z \to \Gamma x).$$

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### **Branch Number**

#### Definition

Let  $X = (x_1, x_2, \cdots, x_m) \in GF(2^d)^m$ . Then the Hamming weight of X is denoted by  $H_w(X) = \#\{i|x_i \neq 0\}$ .

#### Definition

The branch number  $\mathcal{B}$  of linear transformation  $\theta$  is defined as follows:

$$\mathcal{B} = \min_{x \neq 0} (H_w(x) + H_w(\theta(x))).$$

- Differential case:  ${\cal B}$  taken to be the *differential* branch number
- I.e.  $\mathcal{B} = \min_{\Delta X \neq 0} (H_w(\Delta X) + H_w(\Delta Y))$
- $\Delta X$  is an input difference into the *S*-function,  $\Delta Y$  is an output difference of the *P*-function

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- Linear case:  $\mathcal B$  is taken to be the *linear* branch number
- I.e.  $\mathcal{B} = \min_{\Gamma Y \neq 0} (H_w(P^*(\Gamma Y)) + H_w(\Gamma Y))$
- ΓY is an output mask value of the P-function
- *P*<sup>\*</sup> is a diffusion function of mask values concerning the *P*-function
- Throughout,  $\mathcal{B}$  is used to denote differential or linear branch number, depending on the context

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Number of active S-boxes

#### Definition

A differential active S-box is defined as an S-box given a non-zero input difference. Similarly, a linear active S-box is defined as an S-box given a non-zero output mask value.

#### Theorem

Let  $\mathcal{D}^{(r)}$  and  $\mathcal{L}^{(r)}$  be the minimum number of all differential and linear active S-boxes for a r-round Feistel cipher respectively. Then the maximum differential and linear characteristic probabilities of the r-round cipher are bounded by  $p_s^{\mathcal{D}^{(r)}}$  and  $q_s^{\mathcal{L}^{(r)}}$  respectively.

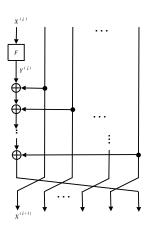
### Kanda's result

#### Theorem

The minimum number of differential (and linear) active S-boxes  $\mathcal{D}^{(4r)}$  for 4r-round Feistel ciphers with SPN round function is at least  $r\mathcal{B} + \lfloor \frac{r}{2} \rfloor$ .

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### Structure of *n*-cell GF-NLFSR



- Proposed in "Cryptographic Properties and Application of a Generalized Unbalanced Feistel Network Structure", ACISP 2009
- *n*-cell extension of the outer function *FO* of the KASUMI block cipher which is a 2-cell structure
- Parallelizable, up to *n* times

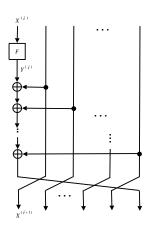
#### Figure: *i*-th round of GF-NLFSR

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Parallelizing the Camellia and SMS4 Block Ciphers

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### Structure of *n*-cell GF-NLFSR



• X<sup>(i)</sup>, Y<sup>(i)</sup> : input and output data to the *i*-th round function

$$X^{(i+n)} = Y^{(i)} \oplus X^{(i+1)} \oplus \cdots \oplus X^{(i+n-1)}$$
  
for  $i = 1, 2, \cdots$ .

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Figure: *i*-th round of GF-NLFSR

Huihui Yap, Khoongming Khoo and Axel Poschmann

Parallelizing the Camellia and SMS4 Block Ciphers

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# Practical Security against DC

- Aim: To investigate the upperbound of the maximum differential characteristic probability of GF-NLFSR cipher
- $\bullet\,\Rightarrow\,{\sf Need}$  to find lower bound for  ${\cal D}^{(r)}$
- I.e. number of differential active S-boxes for *r* consecutive rounds

#### Lemma

For n-cell GF-NLFSR cipher, the minimum number of differential active S-boxes in any 2n consecutive rounds satisfies  $\mathcal{D}^{(2n)} \geq \mathcal{B}$ .

### Practical Security against DC

### Proof.

- Assume that the 2*n* consecutive rounds run from the first round to the 2*n*-th round
- For  $j = 1, \cdots, n$ , at least one of  $\Delta X^{(j)} \neq 0$

• Let *i* be the smallest integer such that  $\Delta X^{(i)} \neq 0$ , where  $1 \leq i \leq n$ . Then

$$\mathcal{D}^{(2n)} \geq H_w(\Delta X^{(1)}) + H_w(\Delta X^{(2)}) + \cdots + H_w(\Delta X^{(2n)})$$

Practical Security against DC

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- For  $j = 1, \cdots, n$ , at least one of  $\Delta X^{(j)} \neq 0$

• Let *i* be the smallest integer such that  $\Delta X^{(i)} \neq 0$ , where  $1 \leq i \leq n$ . Then

$$\begin{aligned} \mathcal{D}^{(2n)} &\geq H_w(\Delta X^{(1)}) + H_w(\Delta X^{(2)}) + \dots + H_w(\Delta X^{(2n)}) \\ &\geq H_w(\Delta X^{(i)}) + H_w(\Delta X^{(i+1)}) \dots + H_w(\Delta X^{(i+n)}) \end{aligned}$$

Practical Security against DC

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$$\begin{aligned} \mathcal{D}^{(2n)} &\geq H_w(\Delta X^{(1)}) + H_w(\Delta X^{(2)}) + \dots + H_w(\Delta X^{(2n)}) \\ &\geq H_w(\Delta X^{(i)}) + H_w(\Delta X^{(i+1)}) \dots + H_w(\Delta X^{(i+n)}) \\ &\geq H_w(\Delta X^{(i)}) + H_w(\Delta X^{(i+1)} \oplus \dots \oplus \Delta X^{(i+n)}), \end{aligned}$$

Practical Security against DC

### Proof.

- Assume that the 2*n* consecutive rounds run from the first round to the 2*n*-th round
- For  $j = 1, \cdots, n$ , at least one of  $\Delta X^{(j)} \neq 0$

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$$\begin{aligned} \mathcal{D}^{(2n)} &\geq H_w(\Delta X^{(1)}) + H_w(\Delta X^{(2)}) + \dots + H_w(\Delta X^{(2n)}) \\ &\geq H_w(\Delta X^{(i)}) + H_w(\Delta X^{(i+1)}) \dots + H_w(\Delta X^{(i+n)}) \\ &\geq H_w(\Delta X^{(i)}) + H_w(\Delta X^{(i+1)} \oplus \dots \oplus \Delta X^{(i+n)}), \\ &= H_w(\Delta X^{(i)}) + H_w(\Delta Y^{(i)}) \end{aligned}$$

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Practical Security against DC

### Proof.

- Assume that the 2*n* consecutive rounds run from the first round to the 2*n*-th round
- For  $j = 1, \cdots, n$ , at least one of  $\Delta X^{(j)} \neq 0$

• Let *i* be the smallest integer such that  $\Delta X^{(i)} \neq 0$ , where  $1 \leq i \leq n$ . Then

$$\begin{aligned} \mathcal{D}^{(2n)} &\geq H_w(\Delta X^{(1)}) + H_w(\Delta X^{(2)}) + \dots + H_w(\Delta X^{(2n)}) \\ &\geq H_w(\Delta X^{(i)}) + H_w(\Delta X^{(i+1)}) \dots + H_w(\Delta X^{(i+n)}) \\ &\geq H_w(\Delta X^{(i)}) + H_w(\Delta X^{(i+1)} \oplus \dots \oplus \Delta X^{(i+n)}), \\ &= H_w(\Delta X^{(i)}) + H_w(\Delta Y^{(i)}) \\ &\geq \mathcal{B}. \end{aligned}$$

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# Practical Security against DC

### Remark

- With probability  $1 \frac{1}{M}$ , where *M* is the size of each cell, i.e. most of the time,  $\Delta X^{(1)} \neq 0$
- $\Rightarrow$  Able to achieve at least  $\mathcal{B}$  number of differential active S-boxes over (n + 1)-round most of the time

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### Practical Security against DC

With the previous lemma, straightforward to prove:

#### Theorem

The minimum number of differential active S-boxes for 2nr-round n-cell GF-NLFSR cipher with bijective SPN round function satisfies

$$\mathcal{D}^{(2nr)} \geq r\mathcal{B} + \lfloor \frac{r}{2} \rfloor.$$

# Practical Security against DC

### **Observations:**

- When n = 2,  $\mathcal{D}^{(4r)} \ge r\mathcal{B} + \lfloor \frac{r}{2} \rfloor$
- $\bullet \Rightarrow$  Similar security against DC as Feistel ciphers with bijective SPN round function
- 2-cell GF-NLFSR has added advantage: parallelizable
- To investigate practical security of 2-cell GF-NLFSR against LC

### Practical Security against LC

- Need to find lower bound for  $\mathcal{L}^{(r)}$
- I.e. number of differential active S-boxes for *r* consecutive rounds

#### Lemma

For 2-cell GF-NLFSR cipher with bijective SPN round function and linear branch number  $\mathcal{B} = 5$ , the minimum number of linear active S-boxes in any 4 consecutive rounds satisfies  $\mathcal{L}^{(4)} \geq 3$ .

# Practical Security against LC

### Outline of proof:

- ΓX<sup>(i)</sup> and ΓY<sup>(i)</sup>: input, output mask values to the *i*-th round
   F function
- Assume that the 4 consecutive rounds run from the first round to the 4th round
- Duality between differential characteristic and linear approximation:  $\Gamma X^{(i+1)} = \Gamma Y^{(i-1)} \oplus \Gamma Y^{(i)}$ , for i = 2 and 3

• 
$$\mathcal{L}^{(4)} = H_w(\Gamma Y^{(1)}) + H_w(\Gamma Y^{(2)}) + H_w(\Gamma Y^{(3)}) + H_w(\Gamma Y^{(4)})$$

- Go through all possible cases
- $\mathcal{L}_{i}^{(r)}$ :number of linear active S-boxes over r rounds for case i:

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Practical Security against LC

With the previous lemma, straightforward to prove:

#### Theorem

For 2-cell GF-NLFSR cipher with bijective SPN round function and linear branch number B = 5, we have

**1** 
$$\mathcal{L}^{(8)} \geq 7$$
,

② 
$$\mathcal{L}^{(12)} \ge 11$$
,

3 
$$\mathcal{L}^{(16)} \ge 15$$
,

where  $\mathcal{L}^{(r)}$  is the minimum number of linear active S-boxes over r rounds.

Parallelizing Camellia Parallelizing SMS4

### Camellia

- Jointly developed by NTT and Mitsubishi Electric Corporation
- Uses an 18-round Feistel structure for 128-bit key, and a 24-round Feistel structure for 192-bit and 256-bit keys,
- Additional input/output whitenings and logical functions, FL-function and  $FL^{-1}$ -function, inserted every 6 rounds
- Bijective SPN F-function
- S-function: 8 S-boxes in parallel
- P-function: bytewise exclusive-ORs

• 
$$B = 5; p_s, q_s = 2^{-6}$$

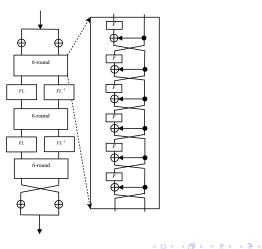
Practical Security Evaluation of GF-NLFSR against DC and LC Application p-Camellia: "Parallelizable" Camellia

- Replace the Feistel network of Camellia with the 2-cell GF-NLFSR block cipher structure instead
- Other components such as number of rounds, *S*-function, *P*-function and the key schedule etc remain unchanged

Parallelizing Camellia Parallelizing SMS4

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### Figure of p-Camellia block cipher



Huihui Yap, Khoongming Khoo and Axel Poschmann Parallelizing the Camellia and SMS4 Block Ciphers

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DC of p-Camellia	

- *p*: Maximum differential characteristic probabilities reduced to 16-round
- Over 16 rounds  $\Rightarrow$  four 4-round blocks

• Recall: 
$$\mathcal{B}=5$$
,  $p_s=2^{-6}$ 

• By previous results, minimum number of differential active S-boxes =  $4 \times 5 + 2 = 22$ 

• 
$$\Rightarrow p \le (2^{-6})^{22} = 2^{-132} < 2^{-128}$$

 $\bullet \Rightarrow \mathsf{Secure} \text{ against } \mathsf{DC}$ 

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LC of p-Camellia	

- *q*: Maximum linear characteristic probabilities reduced to 16-round
- By previous results, minimum number of linear active S-boxes is 15

• 
$$\Rightarrow q \leq (2^{-6})^{15} = 2^{-90}$$

- $\Rightarrow$  Attacker needs to collect at least 2<sup>90</sup> chosen/known plaintexts to mount an attack, which is not feasible in practice
- $\bullet \ \Rightarrow \mathsf{Secure} \ \mathsf{against} \ \mathsf{LC}$

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 Other Attacks on p-Camellia

- Boomerang attack: Can be shown that for 16 rounds, probability of finding a boomerang distinguisher ≤ 2<sup>-180</sup> ⇒ Secure against boomerang attack
- Impossible differential attack: Maximum length of impossible differential distinguisher is 4
   ⇒ Full cipher secure against impossible differential attack

- Integral attack: Maximum length of integral distinguisher is 4 and attacker can extend by at most 3 rounds
   ⇒ Full cipher secure against impossible differential attack
- Slide attack: *FL* and *FL*<sup>-1</sup>-functions provide non-regularity across rounds, and different subkeys used for every round ⇒ Unlikely to work

- Higher order differential attack: Algebraic degree reach maximum degree of 127 after 6th round ⇒ Unlikely to work
- Interpolation attack: After passing through many S-boxes and P-functions, cipher becomes a complex function which is a sum of many multi-variate monomials over GF(2<sup>8</sup>) ⇒ Unlikely to work

Table: Comparison of the implementation results of the round function of Camellia and p-Camellia on UMC *180 nm* ASIC technology.

	Camellia			p-Camellia				
	1 roι	und	2 ro	unds	1 roι	und	2 ro	unds
	abs.	%	abs.	%	abs.	%	abs.	%
Area (GE)	4877	100	9754	200	4877	100	9754	200
power* (mW)	2.65	100	8.38	316.5	2.65	100	5.2	196.2
max Freq. (MHz)	229.4	100	117.8	51.4	229.4	100	221.2	96.5
max T'put (Gbps)	29.4	100	30.2	103	29.4	100	56.6	192.9

\*at a frequency of 100 MHz and a supply voltage of 1.8V.

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SMS4	

- Underlying block cipher used in WAPI standard (Chinese national standard for Wireless Local Area Networks)
- 128-bit key
- 32-round generalized Feistel structure
- Each round transforms four 32-bit words  $X_i$ , i = 0, 1, 2, 3:

 $(X_0,X_1,X_2,X_3,\textit{rk})\mapsto (X_1,X_2,X_3,X_0\oplus T(X_1\oplus X_2\oplus X_3\oplus \textit{rk})),$ 

where *rk* denotes the round key

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SMS4	

 Non-linear function T in sequence: 32-bit subkey addition, S-box Subsitution (layer of four 8-bit S-boxes), a 32-bit linear transformation L

• 
$$\mathcal{B} = 5; \ p_s, q_s = 2^{-6}$$

• Key schedule similar structure to main cipher with slight differences

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- Replace the generalized Feistel network of SMS4 with the 4-cell GF-NLFSR block cipher structure instead
- Modify key schedule too so that same structure as the main cipher: also parallelizable in hardware
- Other components such as number of rounds, *S*-function, *P*-function etc remain unchanged

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Parallelizing Camellia Parallelizing SMS4

# Security of p-SMS4 against block cipher attacks

- Follows similar analysis to p-Camellia
- $\bullet\,$  E.g. Can be shown differential characteristic probability over 29 rounds  $\leq 2^{-108}$
- $\Rightarrow$  Attacker needs to collect at least 2<sup>108</sup> chosen plaintext-ciphertext pairs
- $\bullet\,$  Can be shown linear characteristic probability over 29 rounds  $\leq 2^{-90}\,$
- $\Rightarrow$  Attacker needs to collect at least 2<sup>90</sup> chosen plaintext-ciphertext pairs

Table: Comparison of the implementation results of the round function of SMS4 and p-SMS4 on UMC *180 nm* ASIC technology.

	SMS4			p-SMS4				
	1 round		4 rounds		1 round		4 rounds	
	abs.	%	abs.	%	abs.	%	abs.	%
Area (GE)	2924	100	11546	394.9	2924	100	11574	395.9
power* (mW)	1.81	100	11.38	627.5	1.39	76.8	5.9	322.3
max Freq. (MHz)	288.2	100	73.1	25.4	290.7	100.9	267.4	92.8
max T'put (Gbps)	36.9	100	37.4	101.4	37.2	100.9	136.9	371.1

\*at a frequency of 100 MHz and a supply voltage of 1.8V.

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Conclusion	

- Proposed the use of *n*-cell GF-NLFSR structure to parallelize (Generalized) Feistel structures
- Used two examples, p-Camellia and p-SMS4, and showed that they offer sufficient security against various known existing attacks
- Hardware implementations achieve a maximum frequency that is *n* times higher, where *n* is the number of Feistel branches, while having lower area and power demands
- ⇒ n-cell GF-NLFSRs are particularly well suited for applications that require a high throughput

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