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Passivity-based Control of Euler-Lagrange Systems

Mechanical, Electrical and Electromechanical Applications

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