

Peristaltic flow with inclined magnetic field and convective boundary conditions

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Abstract. Peristaltic flow of viscous fluid in an asymmetric inclined channel with heat transfer and inclined magnetic field is examined. The convective boundary conditions have been handled. Complexity of emerging equations is simplified by utilizing long wavelength and low Reynolds number approximation. Variation of emerging parameters embedded in flow system are discussed. It is observed that an increase in Brikman number increases the temperature profile. Further, it is seen that temperature distribution is an increasing function of Biot number at lower wall.

Keywords: Convective boundary conditions, inclined magnetic field, heat transfer, peristaltic flow, exact solutions

1. Introduction

The study of Peristaltic mechanism has become popular among the researchers during the last four decades because of its vital and extensive applications in physiology and industry. Some of these applications incorporate chyme movement in gastrointestinal tract, swallowing food through esophagus, chyme movement in the gastrointestinal tract, urine transport from kidney to bladder through the ureter, vasomotion of blood vessels in capillaries and arterioles. Since the seminal work of Latham [1] several theoretical and experimental investigations have been carried out in order to understand the peristaltic flows of hydrodynamic fluids under varied assumptions of long wave length, low Reynolds number, small wave amplitude etc. Although the literature on the topic is extensive but few recent investigations can be mentioned by the studies [2–10].

Influence of magnetohydrodynamic (MHD) on peristaltic flow problems have gained significance on the

basis of engineering and biomedical applications. Bio-magnetic fluid dynamics in medical science has wide range of applications such as stoppage of bleeding during surgeries, cancer tumor treatment, cell separation, targeted transport of drug using magnetic particles as drug carriers etc. Agarwal and Anwaruddin [11] has studied the peristaltic flow of a blood under long wave length and low Reynolds number assumption. Mekheimer [12] reported peristaltic flow of blood under effect of magnetic field in anon-uniform channel. Eldabe et al. [13] analyzed the induced magnetic field effect on peristaltic transport of biviscosity fluid in a non-uniform tube. Mekheimer and Elmaboud [14] had reported the influence of heat and magnetic field on peristaltic transport of Newtonian fluid in a vertical annulus. Vajravelu et al. [15] discussed the combined influence of velocity slip, temperature and concentration jump conditions on MHD peristaltic transport of a Carreau fluid in a non-uniform channel.

The purpose of present research is to discuss the simultaneous effects of an inclined magnetic field and heat transfer with connective boundary conditions [16–20]. To best of our knowledge, this problem has not been investigated yet. The paper is arranged as follows. Sections two and three provides the mathematical

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formulation. Graphical discussion is presented in section four while the concluding remarks are given in section five.

2. Basic equations

The Cauchy stress tensor is

$$\bar{\mathbf{T}} = -p\mathbf{I} + \mu\bar{\mathbf{A}}_1, \quad (1)$$

in which p is pressure, \mathbf{I} is identity tensor, μ is dynamic viscosity and the first Rivlin Ericksin tensor is

$$\bar{\mathbf{A}}_1 = \bar{\mathbf{L}} + \bar{\mathbf{L}}^T, \quad \bar{\mathbf{L}} = \text{grad } \bar{\mathbf{V}}, \quad (2)$$

where $\bar{\mathbf{V}}$ indicates the velocity.

The following equations can govern the flow under consideration

Continuity equation

$$\nabla \cdot \mathbf{V} = 0. \quad (3)$$

Equation of motion

$$\rho \frac{d\mathbf{V}}{dt} = \text{div } \mathbf{T} - \sigma B_0^2 \cos \beta (\bar{U} \cos \beta - \bar{V} \sin \beta) + \rho g \sin \epsilon \quad (4)$$

Energy equation

$$\rho C_p \frac{dT}{dt} = \kappa \nabla^2 T + \mathbf{T} \cdot \mathbf{L}. \quad (5)$$

where T the temperature, κ the thermal conductivity, C_p the specific heat, B_0 the applied magnetic field, g is acceleration due to gravity, β and ϵ are inclination angles of magnetic field and channel respectively. The channel walls for heat transfer satisfy convective conditions.

3. Mathematical formulation

Peristaltic motion of an incompressible viscous fluid in an inclined asymmetric channel of width $d_1 + d_2$ is investigated. A sinusoidal wave with speed c is propagating on the channel walls. The fluid is electrically conducting and an inclined magnetic field is taken into consideration. The channel walls are non-conducting. We choose rectangular coordinates (\bar{X}, \bar{Y}) with \bar{X} in the direction of wave propagation and \bar{Y} transverse to it. The geometry of the wall surfaces are

$$\begin{aligned} \bar{h}_1(\bar{X}, \bar{t}) &= \bar{d}_1 + \bar{a}_1 \cos \left(\frac{2\pi}{\lambda} (\bar{X} - c\bar{t}) \right), \quad \text{upper wall,} \\ \bar{h}_2(\bar{X}, \bar{t}) &= -\bar{d}_2 - \bar{a}_2 \cos \left(\frac{2\pi}{\lambda} (\bar{X} - c\bar{t}) + \phi \right), \quad \text{lower wall.} \end{aligned} \quad (6)$$

In above equations \bar{a}_1 and \bar{a}_2 are the wave amplitudes. The phase difference ϕ varies in the range $0 \leq \phi \leq \pi$. The case $\phi = 0$ corresponds to the symmetric channel with waves out of phase and for $\phi = \pi$ the waves are in phase. Further \bar{a}_1 , \bar{a}_2 , \bar{d}_1 , \bar{d}_2 and ϕ satisfy the condition $\bar{a}_1^2 + \bar{a}_2^2 + 2\bar{a}_1\bar{a}_2 \cos \phi \leq (\bar{d}_1 + \bar{d}_2)^2$, λ is the wavelength and \bar{t} is the time. The system is stressed by a constant transverse magnetic field of strength B_0 . The velocity field is written as

$$\mathbf{V} = [\bar{U}(\bar{X}, \bar{Y}, \bar{t}), \bar{V}(\bar{X}, \bar{Y}, \bar{t}), 0], \quad (7)$$

where \bar{U} and \bar{V} are the velocity components in the \bar{X} and \bar{Y} directions respectively.

The transformations between the laboratory and wave frames are given by

$$\begin{aligned} \bar{x} &= \bar{X} - c\bar{t}, & \bar{y} &= \bar{Y}, \\ \bar{u}(\bar{x}, \bar{y}) &= \bar{U} - c, & \bar{v}(\bar{x}, \bar{y}) &= \bar{V}, \end{aligned} \quad (8)$$

where (\bar{u}, \bar{v}) are the velocity components in the wave frame.

With the help of Eqs. (7) and (8), the resulting two-dimensional flow equations become

$$\frac{\partial \bar{u}}{\partial \bar{x}} + \frac{\partial \bar{v}}{\partial \bar{y}} = 0, \quad (9)$$

$$\begin{aligned} \rho \left(\bar{u} \frac{\partial}{\partial \bar{x}} + \bar{v} \frac{\partial}{\partial \bar{y}} \right) \bar{u} + \frac{\partial \bar{p}}{\partial \bar{x}} &= \mu \left(\frac{\partial^2 \bar{u}}{\partial \bar{x}^2} + \frac{\partial^2 \bar{u}}{\partial \bar{y}^2} \right) - \sigma B_0^2 \cos \beta (\bar{U} \cos \beta \\ &- \bar{V} \sin \beta) + \rho g \sin \epsilon, \end{aligned} \quad (10)$$

$$\begin{aligned} \rho \left(\bar{u} \frac{\partial}{\partial \bar{x}} + \bar{v} \frac{\partial}{\partial \bar{y}} \right) \bar{v} + \frac{\partial \bar{p}}{\partial \bar{y}} &= \mu \left(\frac{\partial^2 \bar{v}}{\partial \bar{x}^2} + \frac{\partial^2 \bar{v}}{\partial \bar{y}^2} \right) + \sigma B_0^2 \sin \beta (\bar{U} \cos \beta \\ &- \bar{V} \sin \beta) - \rho g \cos \epsilon, \end{aligned} \quad (11)$$

$$\begin{aligned} & \rho C_p \left[\bar{u} \frac{\partial}{\partial \bar{x}} + \bar{v} \frac{\partial}{\partial \bar{y}} \right] \bar{T} \\ &= \kappa \left[\frac{\partial^2 \bar{T}}{\partial \bar{x}^2} + \frac{\partial^2 \bar{T}}{\partial \bar{y}^2} \right] + \mu \left[2 \left\{ \left(\frac{\partial^2 \bar{u}}{\partial \bar{x}^2} \right)^2 \right. \right. \\ & \quad \left. \left. + \left(\frac{\partial^2 \bar{v}}{\partial \bar{y}^2} \right)^2 \right\} + \left(\frac{\partial \bar{u}}{\partial \bar{y}} + \frac{\partial \bar{v}}{\partial \bar{x}} \right)^2 \right]. \end{aligned} \quad (12)$$

The exchange of heat by Newtons law of cooling is given by [19, 20]

$$\begin{aligned} \kappa \frac{\partial \bar{T}}{\partial y} &= -\eta_1 (\bar{T} - T_1) \quad \text{at} \quad y = h_1 \\ \kappa \frac{\partial \bar{T}}{\partial y} &= -\eta_0 (T_0 - \bar{T}) \quad \text{at} \quad y = h_2 \end{aligned} \quad (13)$$

where η_1 , η_0 , T_1 and T_0 are Biot numbers and temperatures at upper and lower walls respectively. The dimensionless variables and parameters are defined by

$$\begin{aligned} x &= \frac{\bar{x}}{\lambda}, \quad y = \frac{\bar{y}}{d_1}, \quad t = \frac{c\bar{t}}{\lambda}, \quad p = \frac{d_1 \bar{p}}{c\lambda\mu}, \\ d &= \frac{d_2}{d_1}, \quad \gamma = \frac{\bar{T} - T_0}{T_1 - T_0}, \quad a = \frac{\bar{a}_1}{d_1}, \\ \delta &= \frac{2\pi d_1}{\lambda}, \quad u = \frac{\bar{u}}{c}, \quad v = \frac{\bar{v}}{c}, \\ Br &= Ec Pr, \quad Pr = \frac{\mu}{C_p \kappa}, \quad M = \sqrt{\frac{\sigma}{\mu}} B_0 d_1 \\ Re &= \frac{cd_1 \rho}{\mu}, \quad b = \frac{a_2}{d_1}, \quad Fr = \frac{c^2}{gd_1}, \\ h_1 &= \frac{\bar{h}_1}{d_1}, \quad h_2 = \frac{\bar{h}_2}{d_1}, \quad Z_2 = \frac{\eta_0 d_1}{k}, \\ Ec &= \frac{c^2}{C_p (T_1 - T_0)}, \quad Z_1 = \frac{\eta_1 d_1}{k}, \quad u = \frac{\partial \Psi}{\partial y}, \quad v = -\delta \frac{\partial \Psi}{\partial x}, \end{aligned} \quad (14)$$

in which Ec , Pr , δ , Re , M and Z_1 , Z_2 are the Eckert, Prandtl, wave, Reynolds, Hartman and Biot numbers respectively. Here p is the pressure, Ψ is the stream function. Moreover T_0 and T_1 are the temperatures at $y = h_1$ and $y = h_2$ respectively.

Dimensionless form of Eq. (6) is

$$\begin{aligned} h_1 &= 1 + a \cos(2\pi x), \\ h_2 &= -d - b \cos(2\pi x + \phi), \end{aligned} \quad (15)$$

where a , b , ϕ and d satisfy $a^2 + b^2 + 2ab \cos \phi \leq (1 + d)^2$.

Under the application of Eq. (14), equation. (9) is satisfied identically. Eqs. (10) – (13), under assumption of long wavelength and low Reynolds number yield:

$$\frac{\partial p}{\partial x} = \frac{\partial^3 \Psi}{\partial y^3} - M^2 \cos \beta \left(\frac{\partial \Psi}{\partial y} + 1 \right) \cos \beta + \frac{Re}{Fr} \sin \epsilon, \quad (16)$$

$$\frac{\partial p}{\partial y} = 0, \quad (17)$$

$$\frac{\partial^2 \gamma}{\partial y^2} + Br \left(\frac{\partial^2 \Psi}{\partial y^2} \right)^2 = 0, \quad (18)$$

where Eq. (18) shows that $p \neq p(y)$ and therefore $p = p(x)$. Application of Eq. (18) on Eq. (17) gives :

$$\frac{\partial^4 \Psi}{\partial y^4} - M^2 \cos^2 \beta \frac{\partial^2 \Psi}{\partial y^2} = 0, \quad (19)$$

The dimensionless boundary conditions of the problem are

$$\begin{aligned} \Psi &= \frac{F}{2}, \quad \frac{\partial \Psi}{\partial y} = -1, \quad \frac{\partial \gamma}{\partial y} + Z_1 \gamma = 0 \quad \text{at} \quad y = h_1, \\ \Psi &= -\frac{F}{2}, \quad \frac{\partial \Psi}{\partial y} = -1, \quad \frac{\partial \gamma}{\partial y} - Z_2 (\gamma - 1) = 0 \quad \text{at} \quad y = h_2, \end{aligned} \quad (20)$$

where F is the dimensionless time mean flow rate in the wave frame. If θ is the dimensionless time mean flow rate in the laboratory frame then

$$\theta = F + 1 + d$$

with

$$F = \int_{h_2}^{h_1} \frac{\partial \Psi}{\partial y} dy. \quad (21)$$

The above set of equations are solved exactly using the the symbolic software Mathematica by DSolve Command. The resulting expressions for stream function Ψ , pressure gradient $\frac{dp}{dx}$ and temperature γ are given as follows

$$\Psi = \frac{1}{B_0} \left[\left(\cosh(\sqrt{B}y) - \sinh(\sqrt{B}y) \right) \left(2(F + h_1 - h_2)(\cosh(\sqrt{B}(h_1 + h_2)) + \sinh(\sqrt{B}(h_1 + h_2))) \right) \right. \\ \left. 2(F + h_1 - h_2)(\cosh(2\sqrt{B}y) + \sinh(2\sqrt{B}y)) - (2 + \sqrt{BF})(h_1 + h_2 - 2y)(\cosh(\sqrt{B}(y + h_1)) \right. \\ \left. + \sinh(\sqrt{B}(y + h_1))) - (-2 + \sqrt{BF})(h_1 + h_2 - 2y)(\cosh(\sqrt{B}(y + h_2)) + \sinh(\sqrt{B}(y + h_2))) \right], \quad (22)$$

$$\frac{dp}{dx} = -2BB_0 \cosh(\sqrt{B}h_1) - B^{3/2} B_0 F \cosh(\sqrt{B}h_1) + 2BB_0 \cosh(\sqrt{B}h_2) - B^{3/2} B_0 F \cosh(\sqrt{B}h_2) \\ - 2BB_0 \sinh(\sqrt{B}h_1) - B^{3/2} B_0 F \sinh(\sqrt{B}h_1) + 2BB_0 \sinh(\sqrt{B}h_2) - B^{3/2} B_0 F \sinh(\sqrt{B}h_2) \\ - B + \frac{\text{Re} \sin \epsilon}{Fr}, \quad (23)$$

$$\gamma = B_1 [\cosh(2\sqrt{B}(h_1 + h_2 + y)) - \sinh(2\sqrt{B}(h_1 + h_2 + y))(-4Z_1(1 + h_2Z_2 - yZ_2) \\ (\cosh(2\sqrt{B}(y + h_1 + h_2)) + \sinh(2\sqrt{B}(y + h_1 + h_2))) - 2B^{3/2} B_0^2 Br(F + h_1 + h_2)^2 \\ (2 + h_1Z_1 - yZ_1 + h_2Z_2 - yZ_2)(\cosh(2\sqrt{B}(y + 2h_1 + h_2)) - \cosh(2\sqrt{B}(y + h_1 + h_2))) \\ + \sinh(2\sqrt{B}(y + 2h_1 + h_2)) - \sinh(2\sqrt{B}(y + 2h_1 + h_2))) - BB_0^2 Br(F + h_1 - h_2)^2 \\ (-Z_1 + Z_2 + h_1Z_1Z_2 - h_2Z_1Z_2)(\cosh(4\sqrt{B}(h_1 + h_2)) - \cosh(2\sqrt{B}(y + 2h_1 + h_2))) \\ - \cosh(2\sqrt{B}(y + h_1 + 2h_2)) + \cosh(2\sqrt{B}(2y + h_1 + h_2)) + \sinh(4\sqrt{B}(h_1 + h_2)) \\ - \sinh(2\sqrt{B}(2h_1 + h_2 + y))], \quad (24)$$

$$B_0 = 2((-2 + \sqrt{B}h_1 - \sqrt{B}h_2)(\cosh(2\sqrt{B}h_1) + \sinh(2\sqrt{B}h_1)) + (2 + \sqrt{B}h_1 - \sqrt{B}h_2) \\ (\cosh(2\sqrt{B}h_2) + \sinh(2\sqrt{B}h_2))), \quad (25)$$

$$B_1 = \frac{1}{4(-Z_1 + Z_2 + h_1Z_1Z_2 - h_2Z_1Z_2)}, \quad B = M^2 \cos^2 \beta. \quad (26)$$

The dimensionless expressions of pressure rise ΔP_λ is

$$\Delta P_\lambda = \int_0^1 \frac{dp}{dx} dx. \quad (27)$$

4. Discussion

Our interest in this section is to examine the variations of Brinkman number Br , channel inclination ϵ , Hartman number M , phase difference ϕ , inclined magnetic field parameter β and wave amplitude a on the pressure gradient dp/dx , pressure rise ΔP_λ , temperature distribution γ and velocity u . For this purpose the Figs. 1(a-c)-4(a-f) have been plotted.

The behaviors of β , ϵ and a on the axial pressure gradient is shown in Fig. 1(a-c). It is evident that magnitude of dp/dx has an opposite effects for β and ϵ .

It decreases when β increases. It is also clear that dp/dx is directly proportional to a . Further, Fig. 1(a-c) depict that in the wider part of channel the pressure gradient is small and flow can easily pass without the application of large pressure gradient. However in the narrow part of the channel a much larger pressure gradient is required to maintain the same flux to pass it.

The variation of pressure rise ΔP_λ against mean flow rate θ for different values of β , a and M is plotted in Fig. 2(a-c). Pumping action is due to the dynamic pressure exerted by the walls on the fluid trapped between the contraction region. Inclined magnetic field parameter β has opposite behavior on pressure rise when compared with the Hartman number M . Figure 2b shows that influence of a on Δp_λ is similar to that of M . It is noticed that an increase in M causes an increase in the pressure rise (Fig. 2c). In the pumping region

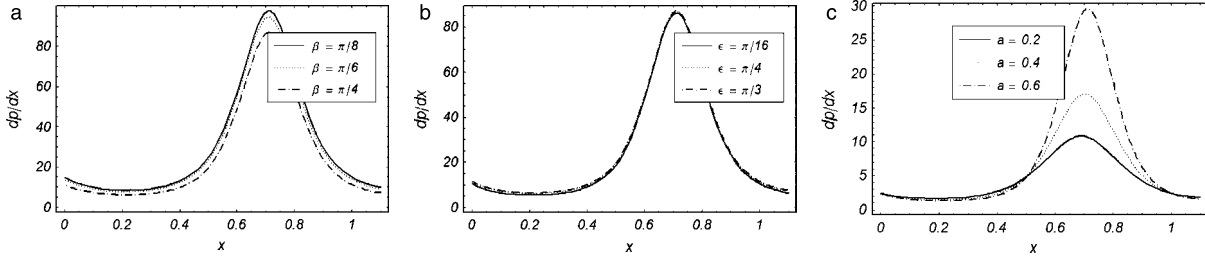


Fig. 1. a) The pressure gradient dp/dx versus x for $\phi = \pi/6$, $\theta = 5.5$, $a = 0.6$, $b = 0.5$, $M = 2$, $\epsilon = \pi/4$, $Re = 2$, $Fr = 1.3$ and $d = 1.1$. b) The pressure gradient dp/dx versus x for $\phi = \pi/6$, $\theta = 5.5$, $a = 0.6$, $b = 0.5$, $M = 2$, $\beta = \pi/8$, $M = 2$, $Re = 2$, $Fr = 1.3$ and $d = 1.1$. c) The pressure gradient dp/dx versus x for $\phi = \pi/6$, $\theta = 5.5$, $\epsilon = \pi/4$, $b = 0.5$, $a = 0.6$, $\beta = \pi/4$, $Re = 2$, $Fr = 1.3$ and $d = 1.1$.

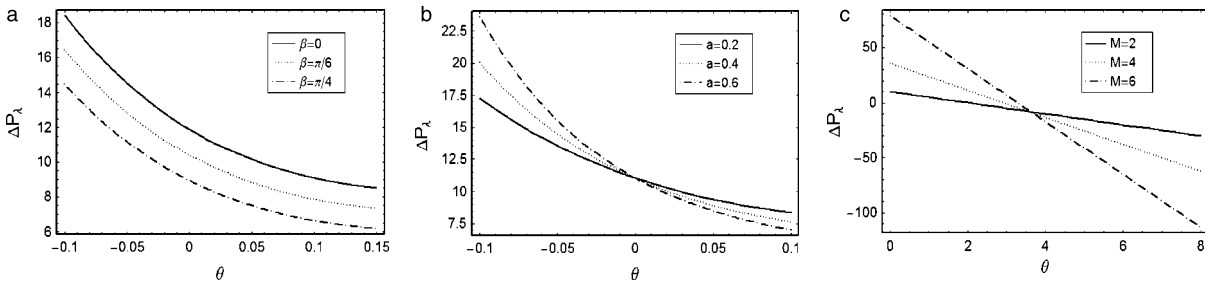


Fig. 2. a) The pressure rise ΔP_λ versus θ for $\phi = \pi/6$, $\theta = -5.5$, $a = 0.6$, $b = 0.5$, $M = 2$, $\epsilon = \pi/4$, $Re = 2$, $Fr = 1.3$ and $d = 1.1$. b) The pressure rise ΔP_λ versus θ for $\phi = \pi/6$, $\theta = 5.5$, $\epsilon = \pi/4$, $b = 0.5$, $M = 2$, $\beta = \pi/4$, $M = 2$, $Re = 2$, $Fr = 1.3$ and $d = 1.1$. c) The pressure rise ΔP_λ versus θ for $\phi = \pi/6$, $\theta = -5.5$, $\epsilon = \pi/4$, $b = 0.5$, $a = 0.6$, $\beta = \pi/4$, $Re = 2$, $Fr = 1.3$ and $d = 1.1$.

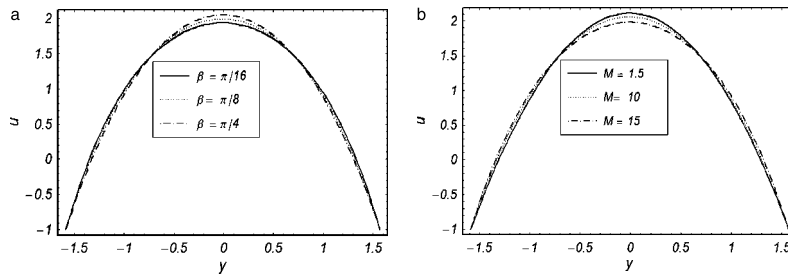


Fig. 3. a) The velocity function u versus y $a = 0.6$, $\theta = 5.5$, $\phi = \pi/6$, $b = 0.5$, $x = 0.2$, $M = 1.5$ and $d = 1.1$. b) The velocity function u versus y for $a = 0.6$, $\theta = 5.5$, $\phi = \pi/6$, $b = 0.5$, $x = 0.2$, $M = 1.5$ and $d = 1.1$.

($\Delta p_\lambda > 0$) the pumping rate increases by increasing M . The free pumping rate ($\Delta p_\lambda = 0$) increases by increasing M . In copumping ($\Delta p_\lambda < 0$) the pumping rate decreases by increasing M .

Figure 3(a,b) has been plotted in order to study the effects of β and M on the velocity function u . Figs. 3a depicts that the magnitude of velocity function u increases by increasing β parameter at the centre of channel. Figure 3b depicts a behavior opposite to β .

The variation of temperature distribution γ against y is drawn in Fig. 4(a-f). The following observations are worth noted.

Figure 4(a-f) is plotted to observe the influence of β , Br , M , ϕ , Z_1 and Z_2 on the temperature distribution. Temperature distribution decreases by increasing M and Z_1 . The temperature distribution increases by increasing values of Brinkman number Br , inclined magnetic field β and phase difference ϕ and Biot number Z_2 .

5. Conclusion

A theoretical study is made to observe the MHD flow characteristics of viscous fluid under the influence

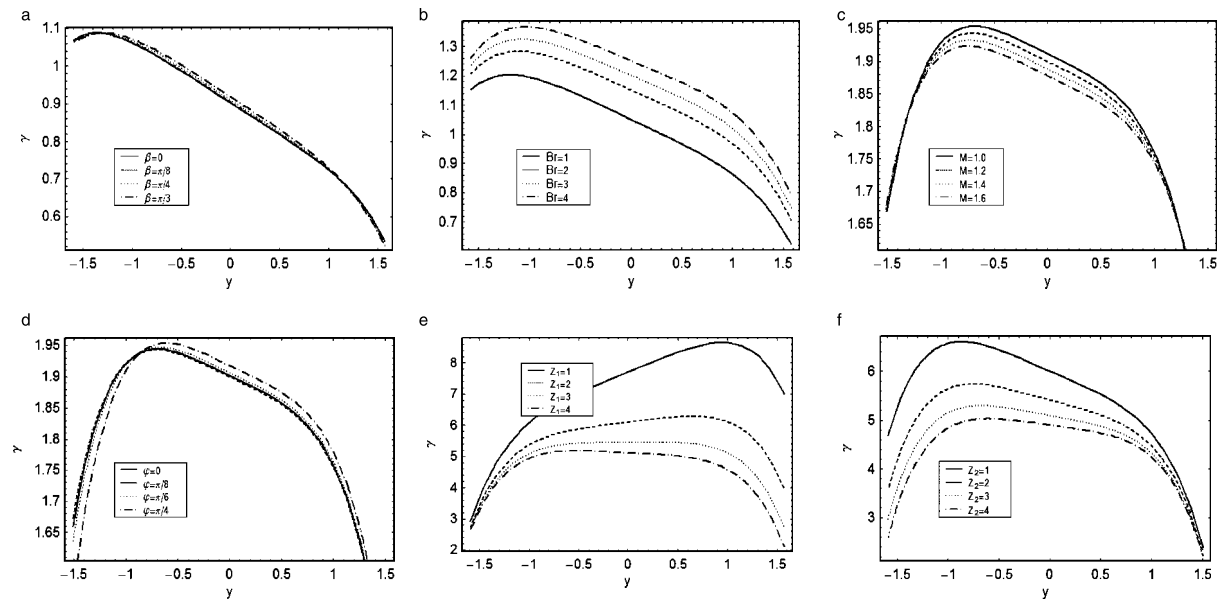


Fig. 4. a) The temperature distribution γ versus y for $a = 0.6$, $\theta = 0.3$, $\phi = \pi/8$, $b = 0.5$, $x = 0.2$, $M = 1.5$, $d = 1.1$, $Br = 1$, $Z_1 = 1$ and $Z_2 = 3$. b) The temperature distribution γ versus y $\beta = 0.05$, $a = 0.6$, $\theta = 0.3$, $\phi = \pi/8$, $b = 0.5$, $x = 0.2$, $M = 1.5$, $d = 1.1$, $Z_1 = 1$ and $Z_2 = 3$. c) The temperature distribution γ versus y $\beta = 0.05$, $a = 0.6$, $\theta = 0.3$, $\phi = \pi/8$, $b = 0.5$, $x = 0.2$, $Br = 1$, $d = 1.1$, $Z_1 = 1$ and $Z_2 = 3$. d) The temperature distribution γ versus y $\beta = 0.05$, $a = 0.6$, $\theta = 0.3$, $M = 1.5$, $b = 0.5$, $x = 0.2$, $Br = 1$, $d = 1.1$, $\phi = \pi/8$ and $Z_2 = 3$. e) The temperature distribution γ versus y $\beta = 0.05$, $a = 0.6$, $\theta = 0.3$, $M = 1.5$, $b = 0.5$, $x = 0.2$, $Br = 1$, $d = 1.1$, $\phi = \pi/8$ and $Z_1 = 1$. f) The temperature distribution γ versus y $\beta = 0.05$, $a = 0.6$, $\theta = 0.3$, $M = 1.5$, $b = 0.5$, $x = 0.2$, $Br = 1$, $d = 1.1$, $\phi = \pi/8$ and $Z_1 = 1$.

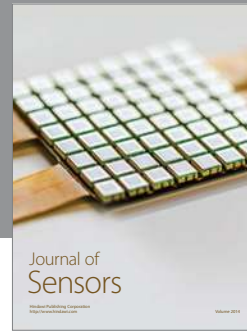
of inclined magnetic field and convective boundary conditions. The effects of different parameters on the velocity and temperature profiles are shown. An exact solution is constructed. The following observations are made.

- An increase in the values of β and M have opposite effects on the velocity u in a qualitative sense.
- The temperature profile increases by increasing Br , β , ϕ and Z_2 and while it decreases when M , Z_1 are increased.
- An increase in Brikman number Br increases the temperature profile.
- Higher values of dp/dx corresponds to smaller values of inclined magnetic field β .

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