Phase－controllable spin wave generation in iron garnet by linearly polarized light pulses<br>Yoshimine，Isao<br>Institute of Industrial Science，The University of Tokyo<br>Satoh，Takuya<br>Institute of Industrial Science，The University of Tokyo｜PRESTO，Japan Science and Technology Agency｜Faculty of Sciences，Kyushu University<br>Iida，Ryugo<br>Institute of Industrial Science，The University of Tokyo<br>Stupakiewicz，Andrzej<br>Laboratory of Magnetism，Faculty of Physics，University of Bialystok<br>他

http：／／hdl．handle．net／2324／1808891

出版情報：Journal of Applied Physics． 116 （4），pp．043907－，2014－07－24．AIP Publishing バージョン：権利関係：

## Phase-controllable spin wave generation in iron garnet by linearly polarized light pulses

Isao Yoshimine, ${ }^{1, a)}$ Takuya Satoh, ${ }^{1,2,3}$ Ryugo lida, ${ }^{1}$ Andrzej Stupakiewicz, ${ }^{4}$ Andrzej Maziewski, ${ }^{4}$ and Tsutomu Shimura ${ }^{1}$
${ }^{1)}$ Institute of Industrial Science, The University of Tokyo, Tokyo 153-8505, Japan
${ }^{2)}$ PRESTO, Japan Science and Technology Agency, Tokyo 102-0076, Japan
${ }^{3)}$ Department of Physics, Kyushu University, Fukuoka 812-8581, Japan
${ }^{4)}$ Laboratory of Magnetism, Faculty of Physics, University of Bialystok, Bialystok 15-424, Poland

A phase-controlled spin wave was nonthermally generated in bismuth-doped rareearth iron garnet by linearly polarized light pulses. We controlled the initial phase of the spin wave continuously within a range of 180 deg by changing the polarization azimuth of the excitation light. The azimuth dependences of the initial phase and amplitude of the spin wave were attributed to a combination of the inverse Cotton-Mouton effect and photoinduced magnetic anisotropy. Temporally and spatially resolved spin wave propagation was observed with a CCD camera, and the waveform was in good agreement with calculations. A nonlinear effect of the spin excitation was observed for excitation fluences higher than $100 \mathrm{~mJ} / \mathrm{cm}^{2}$.

[^0]
## I. INTRODUCTION

Transportation of spin is a major research topic in two research areas of modern physics that have been attracting considerable attention, namely, spintronics ${ }^{1}$ and magnonics. ${ }^{2}$ The spin transportation is mediated by two types of carriers: conduction electrons (spin polarized current) and localized electrons (spin wave). The propagation length of spin polarized current is limited to roughly several hundred nanometers, which is determined by the propagation length of free electrons. ${ }^{3}$ In contrast, a spin wave can also be generated in insulators, and it is known that the propagation length of a spin wave can be as large as several centimeters in an insulator with a low damping coefficient. ${ }^{4}$ Therefore, magnonics is expected to be a fundamental technology in information transport using spin waves.

In past studies, spin waves were generated by applying microwaves from a microstrip antenna, ${ }^{5,6}$ or by using spin transfer torque. ${ }^{7,8}$ Interference ${ }^{9,10}$ and phase control ${ }^{11,12}$ of spin waves generated by microwaves were realized by using a waveguide on yttrium iron garnet. This phase control was accomplished by spatial modulation of the external magnetic field ${ }^{11}$ or a change in dispersion due to the amplitude of the spin wave. ${ }^{11,12}$ However, it is necessary to attach electrodes to the sample for this type of spin wave generation, and the spatial waveform of the microwaves or spin current is limited by the shape of the electrodes.

Recently, thermal emission of spin waves using ultrashort light pulses, without the need for electrodes, was studied in $\mathrm{Ni}^{13,14}$ and permalloy ${ }^{14}$ films. Following this, spin waves were generated nonthermally in bismuth-doped rare-earth iron garnet via the inverse Faraday effect (IFE), and the propagation of spin waves was observed directly at a probe spot away from the pump spot where the spin waves were generated. ${ }^{15}$

In addition, it is expected that more-arbitrary spin wave emission will be realized by using light pulses. For example, directional control of spin wave propagation by controlling the spot shape of excitation light pulses has been reported. ${ }^{15}$ Another promising technique for controlling the spin wavefront is using a phased array, which has been applied to phononpolaritons. ${ }^{16}$ To realize a spin wave phased array, the initial phase of the spin wave must be controlled.

The light pulses used to excite spin precession via the IFE are circularly polarized, and the initial phase of the spin precession is determined by the helicity of the polarization. ${ }^{17,18}$ As a result, the initial phase of the spin waves generated via the IFE is restricted to two
phases with a difference of $\pi$ between them. On the other hand, nonthermal excitation of spin precession by linearly polarized light pulses was reported by Kalashnikova. ${ }^{19}$ This spin excitation was described as the generation of an impulsive effective field within the pump spot via the inverse Cotton-Mouton effect (ICME). Spin excitation by linearly polarized light was also reported by Hansteen ${ }^{20}$ and Atoneche; $;^{21}$ they attributed the mechanism of the excited spin precession to photoinduced magnetic anisotropy (PMA). Thus, the physics of spin excitation by linearly polarized light is still not well understood.

In this paper, we present phase-controlled spin wave emission by linearly polarized light pulses. Also, we explain the polarization azimuth dependence of the initial phase and amplitude of the spin precession based on a combination of the ICME and PMA. This paper is organized as follows. In Sec. II, we explain the material in which we generated spin waves and the experimental method of generating and observing spin waves. In Sec. III, we show that the amplitude and initial phase of spin precession excited by linearly polarized light pulses are varied continuously by changing the polarization azimuth of the light pulses. Then, we show that the polarization azimuth dependence is explained by considering both ICME and PMA. In Sec. IV, we observe propagation of a spin wave with a CCD camera and describe how the optically generated spin wave propagates. In Sec. V, we discuss nonlinearity of the spin excitation at high pump fluence.

## II. MATERIALS AND METHODS

The sample was $\mathrm{Gd}_{4 / 3} \mathrm{Yb}_{2 / 3} \mathrm{BiFe}_{5} \mathrm{O}_{12}$ (111) containing $10^{3} \mathrm{ppm} \mathrm{Pb}$ as impurities. The lateral dimensions were $6 \mathrm{~mm} \times 6 \mathrm{~mm}$, and the thickness was $d=110 \mu \mathrm{~m}$. This was a single crystal with $m 3 m$ symmetry. Saturation magnetization of the sample was $M_{\mathrm{s}}=90 \mathrm{emu} / \mathrm{cm}^{3}$, and the Curie temperature was $T_{c}=573 \mathrm{~K} .{ }^{15}$ All experiments were conducted at room temperature. We applied an in-plane external magnetic field of $H_{\text {ext }}=1 \mathrm{kOe}$. As a result, the sample was in a monodomain state. The ratio of the out-of-plane component to the inplane component of magnetization was measured to be $h=5 \times 10^{-3}$ from Faraday rotation. For the experimental details, see Ref. 22. $\{x, y, z\}$-axes are defined as a set of coordinate axes that satisfy the following conditions: the $x$-axis is parallel to the external magnetic field, and the $z$-axis is perpendicular to the sample surface. The $\{X, Y, Z\}$-axes are defined as being parallel to the $[11 \overline{2}]$, $[1 \overline{1} 0]$, and [111] crystallography axis, respectively. The $X$-axis of the
sample was tilted $\psi=-5 \mathrm{deg}$ from the $x$-axis, as shown in Fig. 1. The initial magnetization $\mathbf{M}_{0}$ is $\mathbf{M}_{0}=M_{\mathrm{s}}(\hat{\boldsymbol{x}}+h \hat{\boldsymbol{z}})$. The initial effective field $\mathbf{H}_{0}$ is the sum of the external magnetic field $\mathbf{H}_{\text {ext }}$, the uniaxial magnetic anisotropy field $\mathbf{H}_{u}$, and the demagnetizing field $\mathbf{H}_{\mathrm{d}}$, that is, $\mathbf{H}_{0}=\mathbf{H}_{\mathrm{ext}}+\mathbf{H}_{\mathrm{u}}+\mathbf{H}_{\mathrm{d}}=\left(H_{\mathrm{ext}}-H_{\mathrm{u}}-4 \pi M_{\mathrm{s}} N_{\|}\right)(\hat{\boldsymbol{x}}+h \hat{\boldsymbol{z}})=H_{0}(\hat{\boldsymbol{x}}+h \hat{\boldsymbol{z}})$. Here $H_{\mathrm{u}}=450$ Oe is the magnetic anisotropy field, and $N_{\|}=0.014$ and $N_{\perp}=0.972$ are demagnetizing factors. ${ }^{23}$ Note that $\mathbf{M}_{0}=\chi \mathbf{H}_{0}$ where $\chi=0.17$. For detailed calculation of $\mathbf{M}_{0}$ and $\mathbf{H}_{0}$, see the appendix.

Spin precession excited by linearly polarized light pulses was measured by the pumpprobe method. The sample was illuminated perpendicularly to the sample surface by the pump pulses with 1300 nm wavelength, and $\tau=150$ fs time duration. The polarization azimuth of the pump pulses was tilted by angle $\theta$ from the $x$-axis (see Fig. 1), and therefore, the electric field amplitude of the pump pulses is $\mathscr{E}=\mathscr{E}_{0}(\cos \theta \hat{\boldsymbol{x}}+\sin \theta \hat{\boldsymbol{y}})$. Light pulses with 800 nm wavelength, 150 fs time duration, and approximately 7 deg angle of incidence were used as probe pulses. The probe pulses were linearly polarized. The temporal waveform of spin precession was obtained by measuring the Faraday rotation of probe pulses, which is proportional to the out-of-plane component of the magnetization, at various delays between the pump pulses and probe pulses. We conducted two types of measurements. One is temporally resolved measurement of spin precession at the pump spot. In this experiment, pump pulses with $75 \mathrm{~mJ} / \mathrm{cm}^{2}$ fluence were focused on the sample to a spot diameter of $80 \mu \mathrm{~m}$. The definition of diameter is $2 r_{0}$ in Ref. ${ }^{15}$, which is half of the $e^{-2}$ diameter. The probe pulses had a fluence of $0.2 \mathrm{~mJ} / \mathrm{cm}^{2}$, and their polarization azimuth was tilted by 45 deg from the $x$-axis. The probe pulses were focused on the sample to a spot diameter of $30 \mu \mathrm{~m}$. Two orthogonal polarization components of the probe pulses were measured by photodetectors using a balanced detection scheme. The other measurement is spatio-temporally resolved measurement of spin wave propagation. In this experiment pump pulses with $85 \mathrm{~mJ} / \mathrm{cm}^{2}$ fluence were focused on the sample to a spot diameter of $60 \mu \mathrm{~m}$. A large area of the sample, with a diameter of 5 mm , was illuminated by probe pulses. The probe pulses had a fluence of $0.1 \mathrm{~mJ} / \mathrm{cm}^{2}$, and their polarization azimuth was along the $y$-axis. The Faraday rotation of the probe polarization was observed using a CCD camera.

## III. POLARIZATION AZIMUTH DEPENDENCE OF SPIN PRECESSION

Temporal waveforms of the Faraday rotation of the probe polarization, $\phi_{F}$, at several polarization azimuths of the pump pulses are shown in Fig. 2. These waveforms correspond to spin precession. A temporal waveform oscillating with a frequency of approximately 2.5 GHz was observed. This frequency was independent of the polarization azimuth. It was found that the initial phase of the waveform varied with the polarization azimuth of the pump pulses. This can be confirmed by the shift of the first negative peak, as indicated by arrows in the figure. To extract the initial phase, we fitted the waveforms with the function

$$
\begin{equation*}
\phi_{\mathrm{F}}(t)=A \exp (-B t) \sin (2 \pi f t+C)+D t+E \tag{1}
\end{equation*}
$$

in the range $20 \leq t \leq 400 \mathrm{ps}$. We fixed $f=2.53 \mathrm{GHz}$, and set $A, B, C, D$, and $E$ as fitting parameters. We defined $B$ independently of the polarization azimuth of the pump pulses. As a result of fitting, we obtained $B=6 \times 10^{-4} \mathrm{ps}^{-1}$. The dependences of the amplitude $A$ and initial phase $C$ on the polarization azimuth of the pump pulses $\theta$ are presented in Figs. 3(a) and (b), respectively. The initial phase was varied continuously, except at $\theta \approx 75 \mathrm{deg}$, where the amplitude was minimized, at nearly zero, and the initial phase jumped by 180 deg . In addition, the initial phase changed considerably around $\theta \approx-25 \mathrm{deg}$, where the amplitude was a local minimum.

In the following, we discuss the mechanism of photoinduced spin precession. The interaction between light and a spin system can be divided into two phenomena which have different time scales. One is impulsive generation of an effective field by light pulses, which occurs in a pulse duration that is much shorter than the period of spin precession. The other is a photoinduced change of the effective field, whose relaxation time is much longer than the period of the spin precession. These are analogous to two phenomena that generate a coherent phonon: an impulsive driving force via impulsive stimulated Raman scattering ${ }^{24}$ and a step function-like driving force via the displacive excitation of coherent phonons, ${ }^{25}$ respectively.

Here we discuss magneto-optical interactions that induce these two types of effective fields. First, we focus on ICME, which generates an impulsive effective field. ICME is one of the effects that causes spin precession described as impulsive stimulated Raman scattering. ${ }^{17,19,26}$ The Hamiltonian of ICME induced by linearly polarized light is written using modulation
of the dielectric tensor $\delta \varepsilon_{i j}{ }^{19,27,28}$ (where $i, j, k$, and $l$ denote $\{x, y, z\}$ or $\{X, Y, Z\}$ ):

$$
\begin{equation*}
\mathscr{H}_{\mathrm{ICM}}=-\operatorname{Re}\left[\frac{\delta \varepsilon_{i j}}{16 \pi} \mathscr{E}_{i} \mathscr{E}_{j}^{*} \delta_{\tau}(t)\right] . \tag{2}
\end{equation*}
$$

Here, $\delta_{\tau}(t)$ is an impulse function with width $\tau$, and $\delta \varepsilon_{i j}$ is a function of the magnetization $\mathbf{M}$ and modulation of magnetization $\mathbf{m}$, and is given by ${ }^{29,30}$ :

$$
\begin{equation*}
\delta \varepsilon_{i j}=2 g_{i j k l}(\mathbf{M})_{k}(\mathbf{m})_{l} \tag{3}
\end{equation*}
$$

Here $g$ is the fourth-rank tensor, which is symmetric over the first pair of indices and over the last pair of indices. The effective field generated by ICME is written as

$$
\begin{equation*}
\left(\mathbf{H}_{\mathrm{ICM}}\right)_{l} \delta_{\tau}(t)=-\frac{\partial \mathscr{H}_{\mathrm{ICM}}}{\partial(\mathbf{m})_{l}}=\frac{1}{8 \pi} g_{i j k l}\left(\mathbf{M}_{0}\right)_{k} \mathscr{E}_{i} \mathscr{E}_{j}^{*} \delta_{\tau}(t) \tag{4}
\end{equation*}
$$

Next we focus on PMA, whose decay to its equilibrium value is negligible. PMA energy can be written as ${ }^{20,31,32}$

$$
\begin{equation*}
W_{\mathrm{PMA}}(t)=-\frac{1}{16 \pi} a_{i j k l}(\mathbf{M})_{k}(\mathbf{M})_{l} \mathscr{C}_{i} \mathscr{E}_{j}^{*} \int_{-\infty}^{t} \delta_{\tau}\left(t^{\prime}\right) d t^{\prime} \tag{5}
\end{equation*}
$$

Therefore, the effective field $\mathbf{H}_{\text {PMA }}$ induced by PMA is expressed as

$$
\begin{align*}
\left(\mathbf{H}_{\mathrm{PMA}}\right)_{l} \int_{-\infty}^{t} \delta_{\tau}\left(t^{\prime}\right) d t^{\prime}=-\frac{\partial W_{\mathrm{PMA}}}{\partial(\mathbf{M})_{l}} \\
\quad=\frac{1}{8 \pi} a_{i j k l}\left(\mathbf{M}_{0}\right)_{k} \mathscr{E}_{i} \mathscr{E}_{j}^{*} \int_{-\infty}^{t} \delta_{\tau}\left(t^{\prime}\right) d t^{\prime} \tag{6}
\end{align*}
$$

In iron garnets, photoinduced redistribution of electrons between nonequivalent Fe ions in octahedral and tetrahedral sites ${ }^{33}$ or impurity Pb ions ${ }^{34}$ may cause a change in the magnetocrystalline anisotropy, which leads to PMA. Reduction of electrons whose polarization is parallel to the optical polarization by selective excitation is known to be a mechanism of PMA induced by linearly polarized light. ${ }^{35} a_{i j k l}$ is tensor that determines PMA, and non-zero components are determined by the symmetry of anisotropic sites in the crystal.

Impulsive generation of the effective field by ICME contributes to spin precession in the form of an instantaneous displacement of the magnetization $\mathbf{M}$. On the other hand, the generation of a step function-like effective field by PMA contributes to the spin precession as an instantaneous change of the effective field $\mathbf{H}_{\text {eff }}$. Here we assume $\mathbf{H}_{\mathrm{ICM}} \gg \mathbf{H}_{\mathrm{PMA}}$. Under the impulsive effective field $\mathbf{H}_{\mathrm{ICM}}$, the dynamics of the magnetization $\mathbf{M}$ are as follows:

$$
\begin{equation*}
\frac{d \mathbf{M}}{d t}=-\gamma\left(\mathbf{M} \times \mathbf{H}_{\mathrm{ICM}}\right) \tag{7}
\end{equation*}
$$

Here $\gamma=2.8 \mathrm{MHz} / \mathrm{Oe}$ is the gyromagnetic ratio, and $\mathbf{M}(t=\tau)$ is

$$
\begin{equation*}
\mathbf{M}(t=\tau)=\mathbf{M}_{0}-\tau \gamma\left(\mathbf{M}_{0} \times \mathbf{H}_{\mathrm{ICM}}\right) \tag{8}
\end{equation*}
$$

The effective field at $t \geq \tau, \mathbf{H}_{\text {eff }}$, is expressed as

$$
\begin{equation*}
\mathbf{H}_{\mathrm{eff}}=\mathbf{H}_{0}+\mathbf{H}_{\mathrm{PMA}} . \tag{9}
\end{equation*}
$$

The dynamics of the magnetization and effective field are illustrated in Fig. 4.
Then, we introduce vectors $\mathbf{u}_{1}, \mathbf{u}_{2}$, and $\mathbf{u}_{3}$. We define $\mathbf{u}_{1}$ as a component of $\mathbf{M}(t=\tau)$ that is perpendicular to $\mathbf{H}_{\text {eff }}$, and $\mathbf{u}_{3}$ as a component of $\mathbf{M}(t=\tau)$ that is parallel to $\mathbf{H}_{\text {eff }}$. We define $\mathbf{u}_{2}$ satisfying conditions $\left|\mathbf{u}_{1}\right|=\left|\mathbf{u}_{2}\right|, \mathbf{u}_{2} \perp \mathbf{H}_{\text {eff }}$, and $\mathbf{u}_{2} \perp \mathbf{M}(t=\tau)$. These vectors are schematically illustrated in Fig. 5. Using $\mathbf{u}_{1}, \mathbf{u}_{2}$ and $\mathbf{u}_{3}$, the magnetization $\mathbf{M}(t \geq \tau)$ precessing around $\mathbf{H}_{\text {eff }}$ is written as

$$
\begin{equation*}
\mathbf{M}(t \geq \tau)=\mathbf{u}_{1} \cos 2 \pi f t+\mathbf{u}_{2} \sin 2 \pi f t+\mathbf{u}_{3} \tag{10}
\end{equation*}
$$

Here

$$
\begin{align*}
& \mathbf{u}_{1}=\mathbf{M}(t=\tau)-\frac{\mathbf{M}(t=\tau) \cdot \mathbf{H}_{\mathrm{eff}}}{\left|\mathbf{H}_{\mathrm{eff}}\right|^{2}} \mathbf{H}_{\mathrm{eff}}  \tag{11a}\\
& \mathbf{u}_{2}=-\frac{\mathbf{M}(t=\tau) \times \mathbf{H}_{\mathrm{eff}}}{\left|\mathbf{H}_{\mathrm{eff}}\right|}  \tag{11b}\\
& \mathbf{u}_{3}=\frac{\mathbf{M}(t=\tau) \cdot \mathbf{H}_{\mathrm{eff}}}{\left|\mathbf{H}_{\mathrm{eff}}\right|^{2}} \mathbf{H}_{\mathrm{eff}} . \tag{11c}
\end{align*}
$$

We can make the approximation that $\mathbf{u}_{1}, \mathbf{u}_{2}, \mathbf{u}_{3}$ are constant vectors because the decay of $\mathbf{H}_{\text {PMA }}$ is negligible. Faraday rotation of the probe pulses, $\phi_{\mathrm{F}}$, is proportional to the $z$-component of the magnetization $(\mathbf{M})_{z}$ :

$$
\begin{equation*}
\phi_{\mathrm{F}}=F(\mathbf{M})_{z} \tag{12}
\end{equation*}
$$

Here $F=880 \mathrm{mdeg} \cdot \mathrm{cm}^{3} / \mathrm{emu}$ was obtained from static Faraday rotation. ${ }^{22}$ Comparing Eqs. (1), (10), and (12) yields

$$
\begin{align*}
& F\left(\mathbf{u}_{1}\right)_{z}=A \sin C,  \tag{13a}\\
& F\left(\mathbf{u}_{2}\right)_{z}=A \cos C . \tag{13b}
\end{align*}
$$

Here we neglect $\exp (-B t)$ in Eq. (1), which corresponds to relaxation of spin precession. Polarization dependences of $A \sin C$ and $A \cos C$ are plotted in Figs. 3(c) and (d).

Here, we derive $\mathbf{H}_{\text {ICM }}$ and $\mathbf{H}_{\text {PMA }}$ to clarify the polarization azimuth dependence of the magnetization dynamics. From Eq. (4), in the crystal with symmetry $m 3 m$, we have

$$
\begin{align*}
& \left(\mathbf{H}_{\mathrm{ICM}}\right)_{x}=-\frac{\chi \mathscr{E}_{0}^{2} H_{0}}{8 \pi} \\
& \quad \times\left[\frac{1}{2}\left(g_{1}+g_{2}\right)+\frac{1}{2}\left(g_{1}-g_{2}\right) \cos 2 \theta-h g_{3} \cos (2 \theta-3 \psi)\right]  \tag{14a}\\
& \left(\mathbf{H}_{\mathrm{ICM}}\right)_{y}=-\frac{\chi \mathscr{E}_{0}^{2} H_{0}}{8 \pi} \\
& \quad \times\left[\frac{1}{2}\left(g_{1}-g_{2}\right) \sin 2 \theta+h g_{3} \sin (2 \theta-3 \psi)\right]  \tag{14b}\\
& \left(\mathbf{H}_{\mathrm{ICM}}\right)_{z}=\frac{\chi \mathscr{E}_{0}^{2} H_{0}}{8 \pi}\left[-g_{3} \cos (2 \theta-3 \psi)+h g_{4}\right] \tag{14c}
\end{align*}
$$

Here

$$
\begin{equation*}
 \tag{15a}
\end{equation*}
$$

$\mathbf{H}_{\text {PMA }}$ can be obtained by replacing $g_{i}$ with $a_{i}$ in Eqs. (14a)-(14c), because $a_{i j k l}$ has the same non-zero components as $g_{i j k l}$.

Then we calculate the component of $A \sin C$ and $A \cos C$ that is proportional to the intensity of pump pulses $I=(n c / 8 \pi) \mathscr{E}_{0}^{2}$, neglecting higher order terms of $I$. We end up with

$$
\begin{align*}
A \sin C= & F\left(\mathbf{u}_{1}\right)_{z} \\
= & -I \frac{F \chi^{2} H_{0}}{n c}\left[\left(\tau \gamma H_{0} \frac{1}{2}\left(g_{1}-g_{2}\right)\right) \sin 2 \theta+\tau \gamma H_{0} h g_{3} \sin (2 \theta-3 \psi)\right. \\
& \left.-a_{3} \cos (2 \theta-3 \psi)+\left(\frac{h}{2}\left(a_{1}-a_{2}\right)\right) \cos 2 \theta+\left(\frac{h}{2}\left(a_{1}+a_{2}\right)+h a_{4}\right)\right], \tag{16a}
\end{align*}
$$

$$
\begin{align*}
A \cos C= & F\left(\mathbf{u}_{2}\right)_{z} \\
= & -I \frac{F \chi^{2} H_{0}}{n c}\left[\left(\frac{1}{2}\left(a_{1}-a_{2}\right)\right) \sin 2 \theta+h a_{3} \sin (2 \theta-3 \psi)\right. \\
& \left.+\tau \gamma H_{0} g_{3} \cos (2 \theta-3 \psi)+\left(\tau \gamma H_{0} \frac{h}{2}\left(g_{1}-g_{2}\right)\right) \cos 2 \theta+\tau \gamma H_{0}\left(\frac{h}{2}\left(g_{1}+g_{2}\right)-h g_{4}\right)\right] . \tag{16b}
\end{align*}
$$

Here, we neglected terms of order $h^{2}$ and postulated that $H_{0} \gg\left|\mathbf{H}_{\text {PMA }}\right|$. We fitted the polarization azimuth dependence of $A \sin C$ and $A \cos C$ using Eqs. (16a) and (16b). The results are shown in Figs. 3(c), (d) (red lines). When we take into account both ICME and PMA, we can identify parameters that determine ICME and PMA, namely, $g_{1}, g_{2}, g_{3}, a_{1}, a_{2}$, and $a_{3}$ from the fitting. On the other hand, when we take into account $\operatorname{ICME}\left(a_{i j k l}=0\right)$ or PMA $\left(g_{i j k l}=0\right)$ alone, we cannot obtain a good fit for the experimental results shown in Fig. 3. Therefore, the polarization azimuth dependence of $\left(\mathbf{u}_{1}\right)_{z}$ and $\left(\mathbf{u}_{2}\right)_{z}$ can only be described assuming both ICME and PMA, not just one of them.

From the fitting, we estimated $\left|\mathbf{H}_{\mathrm{ICM}}\right|$ and $\left|\mathbf{H}_{\mathrm{PMA}}\right|$ to be $\left|\mathbf{H}_{\mathrm{ICM}}\right| \approx 80 \mathrm{kOe}$, and $\left|\mathbf{H}_{\mathrm{PMA}}\right| \approx$ 1 Oe. The estimated value of $\left|\mathbf{H}_{\mathrm{PMA}}\right|$ is consistent with the previously reported result. ${ }^{20}$ Here we confirm the assumption $\left|\mathbf{H}_{\mathrm{ICM}}\right| \gg H_{0} \gg\left|\mathbf{H}_{\mathrm{PMA}}\right|$. Because $H_{0} \gg\left|\mathbf{H}_{\mathrm{PMA}}\right|, \mathbf{H}_{\mathrm{PMA}}$ does not affect the frequency of spin precession, which agrees with the experimental result. We also estimated the parameters $g_{1}, g_{2}, g_{3}, a_{1}, a_{2}$, and $a_{3}$ from the fitting. The parameter $g_{3}$ was three orders of magnitude smaller than $g_{1}, g_{2}$, and $g_{4}$. Therefore, considering Eqs. (14a), (14b), and (14c), the $x$-component is dominant for $\mathbf{H}_{\mathrm{ICM}}$. On the other hand, $a_{1}, a_{2}, a_{3}$, and $a_{4}$ are comparable, and thus, the $x, y$, and $z$-components are comparable for $\mathbf{H}_{\text {PMA }}$. From the estimation of $g_{1}, g_{2}, g_{3}, a_{1}, a_{2}$, and $a_{3}$, we conclude the following. When spins are excited by ICME, the spins see the crystal as being spherically symmetric. However, PMA, which occurs with the excitation of ions and the redistribution of electrons, is affected by the symmetry of the crystal.

The contributions of ICME and PMA from the values of $g$ and $a$ are separately shown in Fig. 3. We found that the contributions of ICME and PMA are comparable. The ICME and PMA components change their initial phase continuously in a 360-degree range as a function of the polarization azimuth, and they have opposite polarization azimuth dependence. The amplitude of the PMA component changes by only $25 \%$ as the polarization azimuth changes. This suggests that two types of $\mathrm{PMA}^{32}$ are observed, namely displacement
of uniaxial anisotropy and displacement of cubic anisotropy; the latter is three times larger than the former.

The resulting initial phase of spin precession is varied within a range of 180 degrees because of interference of the two effects. At $\theta \approx 75 \mathrm{deg}$, the contributions of ICME and PMA cancel each other out, and the amplitude of the spin precession becomes nearly zero. Moreover, the contribution of ICME becomes higher than the contribution of PMA at $\theta \approx 75 \mathrm{deg}$, explaining the observed jump in the initial phase of the spin precession. At $\theta \approx-25 \mathrm{deg}$, the amplitude of spin precession also becomes a local minimum because of destructive interference. On the other hand, at $\theta \approx 20 \mathrm{deg}$ and $\theta \approx-75 \mathrm{deg}$, the contributions of ICME and PMA reinforce each other, and the amplitude becomes maximum.

From Eqs. (16a) and (16b), we make two remarks. One is that the constant components with respect to $\theta$ in Figs. 3 (c) and (d) originate from the non-zero out-of-plane magnetization $h$. The other is that the polarization azimuth dependences of the amplitude and initial phase depend on the crystal orientation. This is indicated by the $\psi$-dependence of the equations. Because the absolute value of $\tau \gamma H_{0} \frac{1}{2}\left(g_{1}-g_{2}\right), \tau \gamma H_{0} g_{3}, \frac{1}{2}\left(a_{1}-a_{2}\right), a_{3}$ are all on the order of 1 mdeg and $h=0.005 \ll 1$, the components $\tau \gamma H_{0} h g_{3} \sin (2 \theta-$ $3 \psi$ ) and $\left(h / 2\left(a_{1}-a_{2}\right)\right) \cos 2 \theta$ in Eq. (16a), and the components $h a_{3} \sin (2 \theta-3 \psi)$ and $\left(\tau \gamma H_{0} h / 2\left(g_{1}-g_{2}\right)\right) \cos 2 \theta$ in (16b) are negligible. Therefore, if $\psi=30+60 n \operatorname{deg}(n$ is an integer), for example, if the external field is applied along [110] axis, the initial phase of the spin wave does not change by the polarization azimuth.

The polarization dependence of the initial phase and amplitude can be controlled by suitably designing $g_{i j k l}, a_{i j k l}$ and $\psi$. The initial phase and amplitude of the spin precession can be visualized by the polar angle and radius of each spot, respectively, on a $\left(\mathbf{u}_{1}\right)_{z}$ vs. $\left(\mathbf{u}_{2}\right)_{z}$ plot. As an example, if a $\left(\mathbf{u}_{1}\right)_{z}$ vs. $\left(\mathbf{u}_{2}\right)_{z}$ plot shows a circle centered at $(0,0)$, the initial phase only (keeping the amplitude constant) can be controlled by the polarization azimuth of the pump pulses.

## IV. PROPAGATION OF SPIN WAVES GENERATED BY LINEARLY POLARIZED LIGHT PULSES

We observed the spatio-temporal waveform using a CCD camera to examine the propagation of the spin wave generated by linearly polarized light pulses. We obtained a spatial
map of the Faraday rotation of probe pulses transmitted through the sample for various time delays. Using a CCD camera, we obtained the spatial waveform with 5 -times higher resolution and 50 -times faster speed than the scanning technique. ${ }^{15}$ The experimental result at 1.5 ns after the spin wave excitation is exemplified in Fig. 6(a), where only the oscillating component is plotted. Next, we calculated the waveform of the spin wave using the dispersion curve of the lowest mode of a backward volume magnetostatic wave (BVMSW) ${ }^{15}$. The best fit with the experimental result in the range $0.1 \leq t \leq 2 \mathrm{~ns}$ was obtained for a pump spot diameter of $60 \mu \mathrm{~m}, H_{\text {ext }}=1 \mathrm{kOe}, M_{\mathrm{s}}=1300 / 4 \pi \mathrm{emu} / \mathrm{cm}^{3}, H_{\mathrm{u}}=600$ Oe, Gilbert damping $\alpha=0.02, d=110 \mu \mathrm{~m}$, and initial phase $C=120 \mathrm{deg}$. The calculated spatial plot at $t=1.5 \mathrm{~ns}$ is shown in Fig. 6(b). The good agreement suggests that the spin wave generated by the linearly polarized light pulses propagates as a BVMSW.

Therefore, interference of the spin waves can be expressed as a linear superposition of BVMSWs. Thus, we can arrange a phased array of spin waves generated by linearly polarized light pulses and estimate the waveform of the spin wave generated by the phased array by calculating a superposition of BVMSWs, although this is out of the scope of this paper.

## V. SPIN PRECESSION GENERATED BY LIGHT PULSES WITH HIGH FLUENCE

We measured the polarization azimuth dependences of the amplitude and initial phase of spin precession at several pump fluences, as shown in Figs. 7 and 8, respectively. The frequency of the spin wave did not change. On the other hand, a component that is proportional to $\sin 4 \theta$ was observed for pump fluences higher than $100 \mathrm{~mJ} / \mathrm{cm}^{2}$ (see Fig. 7). Saturated absorption by Fe or Pb ions cannot reproduce the $\sin 4 \theta$-component. A nonlinear effect with a quadratic dependence on the pump intensity seems to show up for higher fluence. However, $I^{2}$ terms in $\left(\mathbf{u}_{1}\right)_{z}$ and $\left(\mathbf{u}_{2}\right)_{z}$, which were neglected in Eqs. (16b) and (16a), could not reproduce the experimental result. Then, we must consider mechanisms that do not occur in the linear region, for example, PMA with charge excitation via two-photon absorption.

## VI. CONCLUSION

We excited a spin wave whose amplitude and initial phase depended on the polarization azimuth of linearly polarized pump pulses. In this sample, the initial phase was varied in a 180 deg range. We characterized the polarization azimuth dependence of the spin precession based on a combination of the ICME and PMA, as shown in Eqs. (16a) and (16b). Here, the direction of the external field and the out-of-plane magnetization component play important roles.

We observed propagation of the spin wave using a CCD camera. From the spatiotemporal waveform of the spin wave, we confirmed that the spin wave generated by linearly polarized light propagates as a BVMSW. Thus, the spin precession induced by linearly polarized light pules can be used as sources of a phased array of spin waves, which enables shaping of spin waves.

We also found that a nonlinear effect affects the amplitude or initial phase of the spin wave for pump fluences higher than $100 \mathrm{~mJ} / \mathrm{cm}^{2}$.

## ACKNOWLEDGMENTS

The authors would like to thank Y. Terui and Y. Hashimoto for discussions about spin wave propagation and experimental techniques. This work was supported by the Japan Science and Technology Agency (JST) - Precursory Research for Embryonic Science and Technology (PRESTO), KAKENHI (23104706), and The Murata Science Foundation.

## Appendix: Calculation of $\mathrm{M}_{0}$ and $\mathrm{H}_{0}$

In this section, the magnetization $\mathbf{M}_{0}$ and effective field $\mathbf{H}_{0}$ before the sample is illuminated by a pump pulse are calculated. The magnetization can be calculated by minimizing the sum of the uniaxial anisotropy energy

$$
\begin{equation*}
W_{\mathrm{u}}=\frac{M_{\mathrm{s}} H_{\mathrm{u}}}{2} \sin ^{2} \xi \tag{A.1}
\end{equation*}
$$

the Zeeman energy

$$
\begin{equation*}
W_{\mathrm{ext}}=-H_{\mathrm{ext}} M_{\mathrm{s}} \sin \xi \cos (\psi-\eta), \tag{A.2}
\end{equation*}
$$

and the demagnetizing energy

$$
\begin{equation*}
W_{\mathrm{d}}=2 \pi M_{\mathrm{s}}^{2}\left(N_{\|} \sin ^{2} \xi+N_{\perp} \cos ^{2} \xi\right) \tag{A.3}
\end{equation*}
$$

Here, $\xi$ and $\eta$ are defined by the azimuth of the magnetization as

$$
\begin{equation*}
\mathbf{M}_{0}=M_{\mathrm{s}}(\sin \xi \cos \eta \hat{\boldsymbol{X}}+\sin \xi \sin \eta \hat{\boldsymbol{Y}}+\cos \xi \hat{\boldsymbol{Z}}) . \tag{A.4}
\end{equation*}
$$

The minimum of the total energy is obtained for $\eta=\psi, \xi=\arcsin \left(H_{\text {ext }} / H_{\mathrm{u}}^{*}\right)$. Here $H_{\mathrm{u}}^{*}=H_{\mathrm{u}}+4 \pi M_{\mathrm{s}}\left(N_{\|}-N_{\perp}\right)$. If $H_{\mathrm{ext}}>H_{\mathrm{u}}^{*}$, we have $\xi=\pi / 2$.

The initial effective field $\mathbf{H}_{0}$ is calculated as

$$
\begin{align*}
\left(\mathbf{H}_{0}\right)_{\|} & =-\frac{\partial\left(W_{\mathrm{u}}+W_{\mathrm{ext}}+W_{\mathrm{d}}\right)}{\partial M_{\|}} \\
& =H_{\mathrm{ext}}-H_{\mathrm{u}} \sin \xi-4 \pi M_{\mathrm{s}} N_{\|} \sin \xi  \tag{A.5a}\\
\left(\mathbf{H}_{0}\right)_{\perp} & =-\frac{\partial\left(W_{\mathrm{u}}+W_{\mathrm{ext}}+W_{\mathrm{d}}\right)}{\partial M_{\|}} \\
& =-4 \pi M_{\mathrm{s}} N_{\perp} \cos \xi \tag{A.5b}
\end{align*}
$$

For the sample we used, $\xi$ should be $\xi=\pi / 2$ when $H_{\text {ext }}=1 \mathrm{kOe}$ because $H_{\mathrm{ext}}>H_{\mathrm{u}}^{*}$. However, another experimental fact shows that $\mathbf{M}_{0}$ has an out-of-plane component which is $0.5 \%$ of the in-plane component $\left(\cos \xi=h=5 \times 10^{-3}\right)$. Then, we set the directions of $\mathbf{M}_{0}$ and $\mathbf{H}_{0}$ as parallel to the vector $(\hat{\boldsymbol{x}}+0.005 \hat{\boldsymbol{z}})$.

## REFERENCES

${ }^{1}$ S. A. Wolf, D. D. Awschalom, R. A. Buhrman, J. M. Daughton, S. von Molnár, M. L. Roukes, A. Y. Chtchelkanova, and D. M. Treger, Science 294, 1488 (2001).
${ }^{2}$ S. O. Demokritov and A. N. Slavin, Magnonics : from fundamentals to applications (Springer, Berlin, 2013).
${ }^{3}$ J. Bass and W. P. Pratt, Jr., Journal of Physics: Condensed Matter 19, 183201 (2007).
${ }^{4}$ T. Schneider, A. A. Serga, B. Leven, B. Hillebrands, R. L. Stamps, and M. P. Kostylev, Appl. Phys. Lett. 92, 022505 (2008).
${ }^{5}$ S. Tamaru, J. A. Bain, R. J. M. van de Veerdonk, T. M. Crawford, M. Covington, and M. H. Kryder, J. Appl. Phys. 91, 8034 (2002).
${ }^{6}$ A. A. Serga, A. V. Chumak, and B. Hillebrands, J. Phys. D 43, 264002 (2010).
${ }^{7}$ J. C. Slonczewski, J. Magn. Magn. Mater. 159, L1 (1996).
${ }^{8}$ L. Berger, Phys. Rev. B 54, 9353 (1996).
${ }^{9}$ S. Choi, K.-S. Lee, and S.-K. Kim, Appl. Phys. Lett. 89, 062501 (2006).
${ }^{10}$ K. Perzlmaier, G. Woltersdorf, and C. H. Back, Phys. Rev. B 77, 054425 (2008).
${ }^{11}$ U.-H. Hansen, V. E. Demidov, and S. O. Demokritov, Appl. Phys. Lett. 94, 252502 (2009).
${ }^{12}$ A. B. Ustinov, B. A. Kalinikos, and E. Lähderanta, J. Appl. Phys. 113, 113904 (2013).
${ }^{13}$ B. Lenk, G. Eilers, J. Hamrle, and M. Münzenberg, Phys. Rev. B 82, 134443 (2010).
${ }^{14}$ M. van Kampen, C. Jozsa, J. T. Kohlhepp, P. LeClair, L. Lagae, W. J. M. de Jonge, and B. Koopmans, Phys. Rev. Lett. 88, 227201 (2002).
${ }^{15}$ T. Satoh, Y. Terui, R. Moriya, B. A. Ivanov, K. Ando, E. Saitoh, T. Shimura, and K. Kuroda, Nat. Photon. 6, 662 (2012).
${ }^{16}$ T. Feurer, J. C. Vaughan, and K. A. Nelson, Science 299, 374 (2003).
${ }^{17}$ A. Kirilyuk, A. V. Kimel, and Th. Rasing, Rev. Mod. Phys. 82, 2731 (2010).
${ }^{18}$ A. V. Kimel, A. Kirilyuk, P. A. Usachev, R. V. Pisarev, A. M. Balbashov, and Th. Rasing, Nature 435, 655 (2005).
${ }^{19}$ A. M. Kalashnikova, A. V. Kimel, R. V. Pisarev, V. N. Gridnev, P. A. Usachev, A. Kirilyuk, and Th. Rasing, Phys. Rev. B 78, 104301 (2008).
${ }^{20}$ F. Hansteen, A. Kimel, A. Kirilyuk, and Th. Rasing, Phys. Rev. B 73, 014421 (2006).
${ }^{21}$ F. Atoneche, A. M. Kalashnikova, A. V. Kimel, A. Stupakiewicz, A. Maziewski, A. Kirilyuk, and Th. Rasing, Phys. Rev. B 81, 214440 (2010).
${ }^{22}$ S. Parchenko, A. Stupakiewicz, I. Yoshimine, T. Satoh, and A. Maziewski, Appl. Phys. Lett. 103, 172402 (2013).
${ }^{23}$ S. Chikazumi, Physics of ferromagnetism, 2nd ed. (Oxford University Press, 2009).
${ }^{24}$ Y.-X. Yan, E. B. Gamble, Jr., and K. A. Nelson, J. Chem. Phys. 83, 5391 (1985).
${ }^{25}$ H. J. Zeiger, J. Vidal, T. K. Cheng, E. P. Ippen, G. Dresselhaus, and M. S. Dresselhaus, Phys. Rev. B 45, 768 (1992).
${ }^{26}$ R. Iida, T. Satoh, T. Shimura, K. Kuroda, B. A. Ivanov, Y. Tokunaga, and Y. Tokura, Phys. Rev. B 84, 064402 (2011).
${ }^{27}$ V. N. Gridnev, Phys. Rev. B 77, 094426 (2008).
${ }^{28}$ P. S. Pershan, J. P. van der Ziel, and L. D. Malmstrom, Phys. Rev. 143, 574 (1966).
${ }^{29}$ V. V. Eremenko, Y. G. Litvinenko, N. K. Kharchenko, and V. M. Naumenko, Magneto-
optic effects in non-centroantisymmetrical antiferromagnetic crystals (Springer New York, 1992).
${ }^{30}$ M. G. Cottam and D. J. Lockwood, Light scattering in magnetic solids (Wiley-Interscience, 1986).
${ }^{31}$ A. Stupakiewicz, A. Maziewski, I. Davidenko, and V. Zablotskii, Phys. Rev. B 64, 064405 (2001).
${ }^{32}$ A. B. Chizhik, I. I. Davidenko, A. Maziewski, and A. Stupakiewicz, Phys. Rev. B 57, 14366 (1998).
${ }^{33}$ R. W. Teale, D. W. Temple, U. Enz, and R. F. Pearson, J. Appl. Phys. 40, 1435 (1969).
${ }^{34}$ G. B. Scott and J. L. Page, J. Appl. Phys. 48, 1342 (1977).
${ }^{35}$ E. L. Nagaev, physica status solidi (b) 145, 11 (1988).

FIG. 1. Definition of coordinate axes, polarization azimuth $\theta$, and crystallographic azimuth $\psi$. The $x$-axis is parallel to the external magnetic field.

FIG. 2. Temporal waveform of Faraday rotation of probe pulses measured at several polarization azimuths of pump pulses. Black lines show fitting curve given by Eq. (1). Arrows show first negative peak.

FIG. 4. Dynamics of magnetization and effective field at (a) $t<0$, (b) $0<t<\tau$, (c) $t=\tau$, and (d) $t>\tau$.

FIG. 5. Definition of $\mathbf{u}_{1}, \mathbf{u}_{2}$, and $\mathbf{u}_{3}$. $\mathbf{u}_{1}$ and $\mathbf{u}_{3}$ were defined to fulfill the conditions $\mathbf{u}_{1}+\mathbf{u}_{3}=$ $\mathbf{M}(t=\tau)$ and $\mathbf{u}_{3} \| \mathbf{H}_{\text {eff }}$. $\mathbf{u}_{2}$ was defined to fulfill the conditions $\left|\mathbf{u}_{1}\right|=\left|\mathbf{u}_{2}\right|$ and $\mathbf{u}_{1} \perp \mathbf{u}_{2}$.

FIG. 6. (a) Experimental spatial plot of spin wave propagation. Polarization azimuth of pump pulses was $\theta=-60$ deg. The spin wave was emitted at ( 0,0 ). (b) Calculated spatial plot using the dispersion curve of BVMSW. In both figures, the delay is $t=1.5 \mathrm{~ns}$.

FIG. 7. Polarization azimuth dependence of amplitude of spin precession at pump spot for several pump fluences.

FIG. 3. Polarization dependence of (a) amplitude $A$, (b) initial phase $C$, (c) $A \sin C$, and (d) $A \cos C$. Red solid lines are fitting curves using Eqs. (16a) and (16b). Blue broken line and green dashed line indicate the contributions of ICME and PMA, respectively.

FIG. 8. Polarization azimuth dependence of initial phase of spin precession at pump spot for several pump fluences.

## $y^{Y / /[\overline{1} 10]}$




## (a) $t<0$ <br> (b) $0<t<\tau$


(c) $t=\tau$
$\mathbf{H}_{\text {PMA }} \mathbf{M} \quad \mathbf{H}_{\mathrm{eff}}$

(d) $t>\tau$




Amplitude (mdeg)






[^0]:    ${ }^{\text {a) }}$ Electronic mail: yoshi3ne@iis.u-tokyo.ac.jp

