

Phonon surface mapping of graphite: disentangling quasi-degenerate phonon dispersions

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The two-dimensional mapping of the phonon dispersions around the K point of graphite by inelastic x-ray scattering is provided. The present work resolves the longstanding issue related to the correct assignment of transverse and longitudinal phonon branches at K . We observe an almost degeneracy of the three TO, LA and LO derived phonon branches and a strong phonon trigonal warping. Correlation effects renormalize the Kohn anomaly of the TO mode, which exhibits a trigonal warping effect opposite to that of the electronic band structure. We determined the electron-phonon coupling constant to be $166(\text{eV}/\text{Å})^2$ in excellent agreement to GW calculations. These results are fundamental for understanding angle-resolved photoemission, double-resonance Raman and transport measurements of graphene based systems.

The lattice dynamics of most “standard” materials are well known nowadays and can be routinely described by *ab-initio* methods based on density-functional perturbation theory [1]. The phonon dispersion relations of graphite and graphene have already been determined by inelastic neutron scattering [2], inelastic x-ray scattering (IXS) [3, 4], double-resonance Raman scattering [5, 6] and electron energy loss spectroscopy [7]. After the first *ab-initio* calculations [8, 9] had been corroborated by IXS [3, 4, 10], the story for graphite seemed closed [11]. However, the phonon dispersions of graphite and graphene - a single layer of graphite - have continued to present surprises in recent years: (i) two Kohn anomalies [12] at the Brillouin zone (BZ) center (Γ) and corner (K) were predicted theoretically [13, 14] and (ii) for charged graphene/graphite, the (electronic) non-adiabatic effects at Γ were predicted theoretically [15] and confirmed experimentally by Raman scattering [16, 17]. Very similar observations have been made for carbon nanotubes [18, 19, 20, 21, 22]. The precise understanding of the Kohn anomaly is highly significant for electron-phonon coupling (EPC) and thus of prime importance for the quantitative description of superconductivity in graphite intercalation compounds [23, 24], electronic transport in the high bias regime, and for the (double) resonant Raman scattering [5, 25]. The latter is now commonly used to distinguish single-layer graphene from double- and multi-layer graphene [26, 27].

Qualitatively, the Kohn anomaly of the transversal optical (TO) branch at the K point is well described by density functional theory (DFT) [14]. However, its magnitude is severely underestimated by DFT [28, 29].

Electron-electron correlation leads to an enhancement of the EPC at K . This can be quantitatively calculated [29] with the GW -approximation which also gives very good results for the electronic band-structure of graphite (see, e.g., Ref. [30]). Although the EPC at Γ can be derived from the IXS and Raman linewidth measurements [31] the experimental determination of the EPC close to the K point [29] is still missing. The experiments needed to unravel the details of the phonon dispersions are extremely challenging because three phonon branches are overlapping in a small energy window and the phonon energies have a strong dependence on doping. Thus, in order to overcome this problem there is an urgent need to map the full two-dimensional phonon dispersion relations around K point in a similar manner as done routinely for electron energy dispersions by angle-resolved photoemission spectroscopy (ARPES).

In this Letter we present a mapping of the detailed two-dimensional phonon dispersion relation around the K point of graphite single crystals measured by IXS. The phonon dispersion perpendicular to the graphene layers in graphite is practically zero for the phonon modes around K [11, 32] and thus we can use graphite to test the phonons of graphene. We prove that at K , the two branches with LA and LO character and the branch with TO character are almost triply degenerate due to the Kohn anomaly which brings down the TO branch in energy. The phonon mode assignment is carried out by explicit comparison of the measured and calculated IXS intensities in the two-dimensional map and used to disentangle overlapping phonon modes. Using the present unambiguous assignment of the phonon branches and pre-

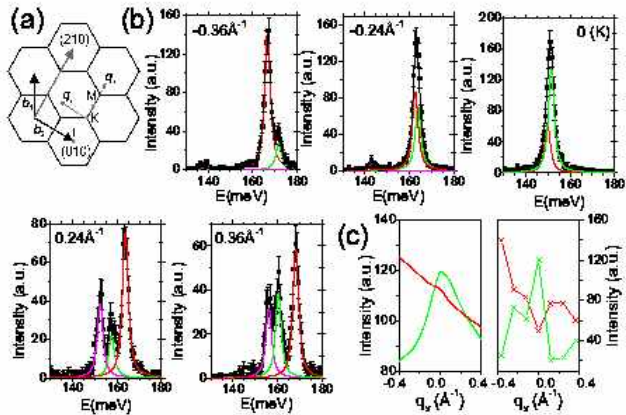


FIG. 1: (a) Scattering geometry for the IXS experiments: spectra are collected along a line starting from the (010) BZ along the (210) [i.e. ΓKM] direction. (b) IXS spectra of graphite single crystals along the ΓKM line. The three phonon modes are fit by Lorentzians. The magenta and green Lorentzians denote the LA and LO modes. The TO mode is denoted by a red Lorentzian. (c) The calculated (left panel) and measured (right panel) IXS intensities for LO (green) and TO (red) modes.

viously measured electron dispersions around K we determine the value of the EPC entirely from experiments and find quantitative agreement to GW calculations.

The experiments were performed on beamline ID28 at the ESRF, utilizing the silicon (999) setup which yields monochromatized synchrotron light of 17794 eV, providing a total energy resolution of ~ 3.3 meV [33]. The beam size at the sample position was $60 \times 30 \mu\text{m}^2$. As the spectrometer is equipped with nine analyzers, nine IXS spectra were recorded simultaneously, thus allowing an efficient coverage of the relevant portion of the phonon dispersion branches. Single crystalline graphite samples with about 1 cm diameter and $100 \mu\text{m}$ thickness were mounted on a goniometer. In Fig. 1(a) the scattering geometry and the coordinate system used throughout this work is shown. We collected IXS spectra along the line starting from the (010) reciprocal lattice point in the (210) direction. We have purposely chosen this line since calculations of the IXS intensities reveal the highest intensity for the TO mode in the (010) BZ.

The phonon frequencies are the eigenvalues of $\sqrt{\mathcal{D}_{\mathbf{q}}/M}$, where $\mathcal{D}_{\mathbf{q}}$ is the dynamical matrix at the wavevector \mathbf{q} and M is the carbon mass. The DFT dynamical matrix $\mathcal{D}_{\mathbf{q}}^{DFT}$ is computed using linear response [1], with the exchange-correlation of Ref. [34] and other computational details as in Ref. [14]. The Kohn anomaly of the TO branch near K is entirely determined [14, 29] by the contribution (to $\mathcal{D}_{\mathbf{q}}$) of the phonon self-energy between π bands $P_{\mathbf{q}}$ (defined in Eq.1 of Ref. [29]). In particular, the TO branch corresponds to the eigenvector $|p_{\mathbf{q}}\rangle$ of $P_{\mathbf{q}}$ with the eigenvalue $p_{\mathbf{q}}$ that

is largest in modulo. $p_{\mathbf{q}}$ is proportional to the square of the EPC between the π bands near the Fermi level. In Ref. [29] it was shown that DFT underestimates $|p_{\mathbf{q}}|$ and that $|p_{\mathbf{q}}|$ from the more accurate GW calculations is larger by a factor $r^{GW} = 1.61$. Here, following Ref. [29], we compute the GW dynamical matrices as

$$\mathcal{D}_{\mathbf{q}}^{GW} = \mathcal{D}_{\mathbf{q}}^{DFT} + |p_{\mathbf{q}}\rangle\langle p_{\mathbf{q}}|\{(r^{GW} - 1)p_{\mathbf{q}} + \Delta\},$$

where Δ is a constant independent of \mathbf{q} . r^{GW} determines the slope of the TO branch near K . Δ shifts rigidly the TO branch with respect to the other branches. Δ cannot be computed easily *ab-initio* (see footnote 24 of Ref. [29]) and is fitted to reproduce the present measurements. Furthermore DFT slightly overestimates (in a systematic manner) the phonon frequencies of the branches not affected by the Kohn anomaly, thus all the frequencies are scaled by -1.3 % to simplify the comparison with measurements.

Selected raw IXS spectra along the ΓKM direction are shown in Fig. 1(b). These spectra contain the contributions of three phonon modes. A lineshape analysis using Lorentzians yields the position and intensity of each mode which are assigned to the LA, LO and TO branches. Note that this characterization of phonon eigenvectors is only strictly valid for very small k away from Γ and we identify the phonon branches in the whole BZ according to their characterization close to Γ [35]. From symmetry considerations LO and LA modes are degenerate at the K point. Our results clearly show that LO/LA and TO are almost degenerate at and close to the K point. This is in striking contrast to previously determined phonon dispersions[3, 4] and can not be explained by the standard DFT phonon calculations [3]. Our mode assignment is based on a comparison of the measured and calculated IXS intensities as shown in Fig. 1(c) and further supported by a comparison to the GW calculated phonon frequencies as shown later. It is clear that the calculated and experimental IXS intensities of LO and TO show the same pattern and thus we can safely assign the TO mode as the one with higher intensity along the considered path in the (010) BZ.

From the maxima of the Lorentzians a set of ~ 100 data points is obtained in the $q_x q_y$ plane in a region of $\pm 0.6 \text{ \AA}^{-1}$ around the K point, which is further extended by the application of symmetry operations. In Fig. 2(a,b) the raw experimental data points around the K point are shown. From these data points the three-dimensional surfaces of the phonon dispersion relations are interpolated using spline functions. The interpolated phonon maps are used for further data analysis. The phonon trigonal warping effect for the LA, LO and TO modes around the K point is illustrated from the phonon equi-energy contours shown in Fig. 2(c) along with the GW calculations. Notably, the experiments and calculations are in excellent agreement to each other which further supports the mode assignment performed above. Interestingly, the phonon trigonal warping effect of the TO mode is opposite to the electronic trigonal warping

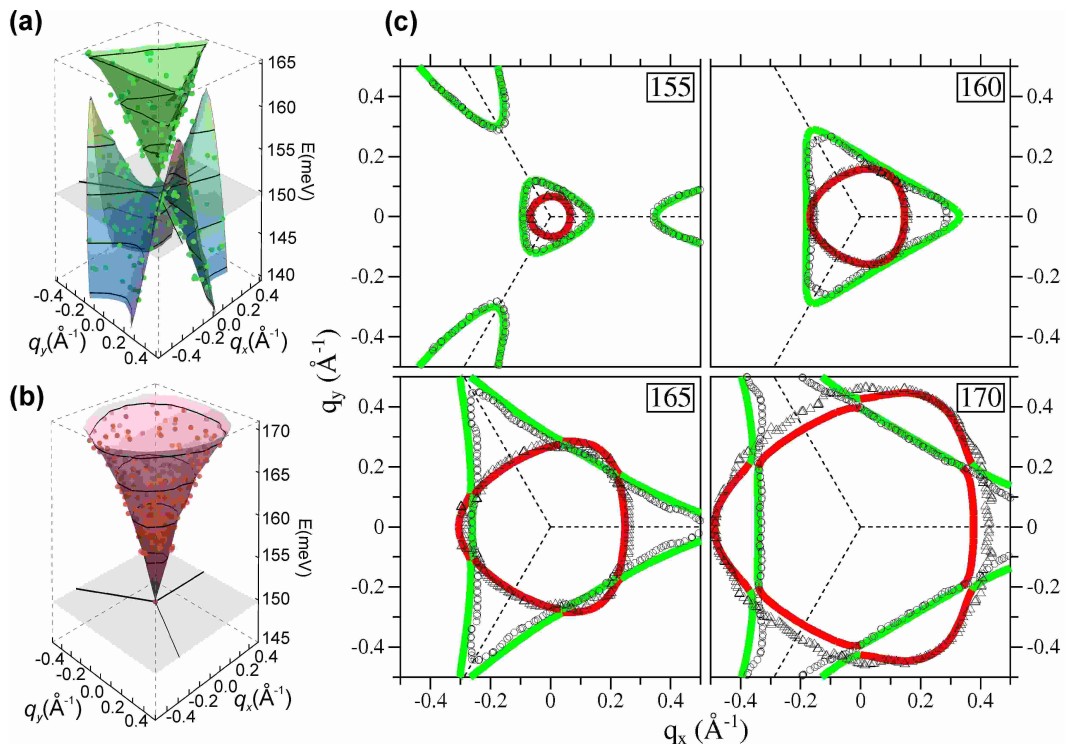


FIG. 2: The interpolated experimental two-dimensional phonon dispersion relation for (a) the longitudinal optic and acoustic phonon branches and (b) the transverse optical phonon branch that has a Kohn anomaly. Dots denote the experimental data taken from the maxima of Lorentzian fits [see Fig. 1(b)]. (c) Equi-energy contours from the interpolated phonon surfaces for the three highest phonon branches around K for energies 155 meV–170 meV. \circ and \triangle denote an interpolation to the raw experimental data in (a) and (b). Lines are GW calculations. The present color code follows the diabatic notation: branches with the same color have similar phonon patterns.

effect, i.e. the slope of the TO phonon branch is higher in KM direction, whereas the electronic bands have a higher slope in KT direction [30]. For the LA and LO modes, the phonon trigonal warping has the same angular dependence as for the electronic bands. The fact that the equi-energy contour of the TO mode is almost circular, is also in agreement with the angular dependence of the kink due to EPC in the quasiparticle dispersion measured by ARPES, where no change of the kink position, i.e. the energy of the coupling phonon [36] was observed. Furthermore, the observed contour for the TO mode can explain why the Raman linewidth of the G' peak depends weakly on the exciting laser energy. The trigonal warping of electrons and the TO phonons is opposite, canceling the effects of enlarging/shrinking of the Raman linewidths. Furthermore it is clear that the LO and TO branches cross along the high-symmetry KT direction but undergo anti-crossing along all the other directions. In a final Fig. 3 we show the phonon dispersions along the high-symmetry lines and compare it to previous DFT calculations and our GW results. It can be observed that (1) the three branches are almost touching each other at K (2) the LO and TO branches cross each other in KT direction and (3) the proper inclusion of the electron-electron correlation (through the GW ap-

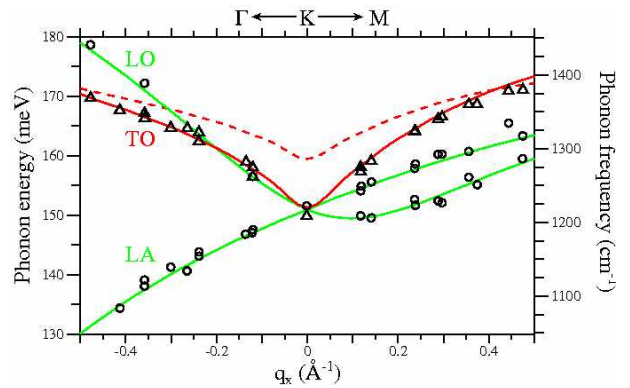


FIG. 3: Phonon dispersion along the ΓKM direction. Points are measurements extracted from the maxima of the Lorentzians from Fig. 1(b). Full lines are GW calculations. The dashed line is the TO branch from DFT calculations. The color code is the same as in Fig. 2.

proach) in the calculation of the EPC is crucial to obtain a good agreement with the experiment. Indeed GW calculations are in almost perfect agreement with measurements while DFT calculations severely underestimate the phonon slope of the TO branch and thus the EPC at K

and overestimate the phonon energy. For precise description of the experimental phonon dispersion relation, we provide simple fit formulas for phonon dispersions of the TO and LO branches. The TO phonon dispersion is given by

$$E_{TO}(q, \theta) = 2.56 \cos(3\theta)q^2 - 62.75q^2 + 73.07q + 149.8 \quad (1)$$

and the LO phonon dispersion is best fit by

$$E_{LO}(q, \theta) = -10.25q \cos^4(3\theta) - 5.32q \cos^3(3\theta) + 5.47q \cos^2(3\theta) + 26.44q^2 + 37.01q - 25.19q^2 \cos(3\theta) + 151.5. \quad (2)$$

Here $E_{TO}(q)$ and $E_{LO}(q)$ denote the phonon energies in meV of TO and LO branch, respectively, q is the phonon wavevector measured in units \AA^{-1} from K point [see Fig. 1(a)] and θ the angle away from the KM direction. From these fits we obtain the slope of the TO branch at K , $S_{TO}^K = 73.07 \text{meV}\text{\AA}$, from which we can derive an experimental value for the square of the EPC constant between π bands at K , $\langle D_K^2 \rangle_F$ [14]. Indeed, (see Eq. (10) of [14]),

$$\langle D_K^2 \rangle_F = \frac{8S_{TO}^K M \hbar \omega_{TO}^K v_f}{\sqrt{3} \hbar a_0^2}, \quad (3)$$

where $\langle D_K^2 \rangle_F$ is defined in [29], and all the parameters on the right hand side were experimentally determined in this work or previously by ARPES [30]. In particular, $\hbar \omega_{TO}^K = 149.8 \text{meV}$ is the the TO phonon energy at K , $v_f = 1.05 \times 10^6 \text{ms}^{-1}$ [30, 37] the Fermi velocity, M the carbon atom mass and $a_0 = 2.46 \text{\AA}$ the in-plane lattice constant. Using Eq.(3), we obtain $\langle D_K^2 \rangle_F = 166 (\text{eV}/\text{\AA})^2$ which is in excellent agreement to the theoretical GW value of $\langle D_K^2 \rangle_F = 164 (\text{eV}/\text{\AA})^2$ [29] and is to be compared to much lower DFT value of $\langle D_K^2 \rangle_F = 92 (\text{eV}/\text{\AA})^2$ [29].

Finally, concerning the temperature dependence of the energy ordering and the LO-TO difference at K , we performed experiments at three different temperatures (300K, 150K and 15K) and find no change in the ordering and a slight increase in the energy difference at K with decreasing temperature (2.2 meV instead of 0.7 meV).

In summary we have disentangled overlapping phonon branches and mapped the 2D phonon surfaces at the K point of graphite using a combination of IXS and *ab-initio* calculations. Excellent agreement for the phonon energies was found once many-body effects at the GW level are considered. The three highest branches around K point are almost triply degenerate, in stark contrast to previous measurements and DFT calculations [3, 4]. Furthermore the Kohn anomaly of the TO phonon branch at K was directly measured by IXS and the EPC was determined entirely from experiments. An opposite trigonal warping of the TO phonon branch as compared to the electrons and the LO phonon branch was found. This is important for understanding the angular dependence of the kink in the quasiparticle dispersion as measured by ARPES in graphite intercalation compounds and graphene and the linewidth of double-resonant Raman scattering.

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