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## Piezoresistive Cantilever Performance—Part I: Analytical Model for Sensitivity

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### Abstract

An accurate analytical model for the change in resistance of a piezoresistor is necessary for the design of silicon piezoresistive transducers. Ion implantation requires a high-temperature oxidation or annealing process to activate the dopant atoms, and this treatment results in a distorted dopant profile due to diffusion. Existing analytical models do not account for the concentration dependence of piezoresistance and are not accurate for nonuniform dopant profiles. We extend previous analytical work by introducing two nondimensional factors, namely, the efficiency and geometry factors. A practical benefit of this efficiency factor is that it separates the process parameters from the design parameters; thus, designers may address requirements for cantilever geometry and fabrication process independently. To facilitate the design process, we provide a lookup table for the efficiency factor over an extensive range of process conditions. The model was validated by comparing simulation results with the experimentally determined sensitivities of piezoresistive cantilevers. We performed 9200 TSUPREM4 simulations and fabricated 50 devices from six unique process flows; we systematically explored the design space relating process parameters and cantilever sensitivity. Our treatment focuses on piezoresistive cantilevers, but the analytical sensitivity model is extensible to other piezoresistive transducers such as membrane pressure sensors.

### Index Terms

Analytical model; force sensor; piezoresistance; piezoresistive cantilever

## I. INTRODUCTION

Piezoresistivity is a commonly used transduction mechanism for microelectromechanical systems [1] such as force sensors [2]–[7], pressure sensors [8]–[12], stress sensors [13]–[15], microphones [16], accelerometers [17], [18], temperature sensors [19], [20], and chemical sensors [21]–[23]. Piezoresistive sensors have several desirable characteristics such as straightforward fabrication, simple signal-conditioning circuitry, relatively small size, and large dynamic range. Although optical readout is a more widely used technique to measure cantilever deflection, piezoresistive cantilevers are ideal for measurements where optical access is not possible or is inconvenient [7].

Many researchers have focused on improving the resolution of piezoresistive sensors [3]–[5], [8]–[11], [14]–[16], [18], [22], [23]. However, to simplify the analysis, previous work ignores the variation in dopant profile through the device thickness and approximates the dopant atoms as being concentrated at the surface [3], [5], [6], [8], [11]. However, this assumption leads to inaccurate device sensitivity predictions, particularly for thin devices where the diffusion length during processing is not negligible.

In this paper, we present an analytical model for piezoresistive cantilevers with nonuniform doping. To address the difference between theoretical estimates and experimental results of sensitivity, we define two nondimensional numbers: an efficiency factor  $\beta^*$  and a geometry factor  $\gamma$ . The efficiency factor captures the reduction in sensitivity due to the dopant atoms being spread across the thickness, while the geometry factor addresses the reduction in sensitivity due to parasitic resistances.

The concept of an efficiency factor was first introduced by Tortonese *et al.* [2] and Harley and Kenny [4], but in this paper, we show, for the first time, how to directly relate an efficiency factor to sensitivity. Prior work assumed a constant piezoresistive coefficient throughout the device thickness; however, the piezoresistivity of silicon is a function of dopant concentration. Thus, the prior methods are only applicable to piezoresistors formed by epitaxy with negligible diffusion during processing and are not ideal for nonuniform profiles formed by ion implantation or diffusion.

We previously extended the concept of an efficiency factor to nonuniform dopant profiles [24]. In this paper, we validate the analytical model by fabricating and characterizing piezoresistive cantilevers and introduce the geometry factor which should also be considered in the design of real devices. In addition, we analyze the effect of design and process parameters on the efficiency factor and overall force sensitivity via simulation (9200 cases) with extensive experimental validation (50 devices from six unique process flows). Finally, we provide a lookup table to easily calculate the efficiency factor and sensitivity so that a process simulation tool is no longer necessary to predict the sensitivity. We present results for an ion-implanted piezoresistive cantilever, but the model is extensible to diffused piezoresistors [25] or 2-D stress distributions as found in membrane pressure sensors.

## II. METHODS

To validate the analytical sensitivity model, we designed and fabricated silicon piezoresistive cantilevers as described previously [26]. Briefly, the cantilevers were oriented in the  $\langle 110 \rangle$  direction ( $E = 169$  GPa) of a silicon-on-insulator wafer. P-type piezoresistors were formed by boron ion implantation, with doses ranging from  $5 \cdot 10^{15}$  to  $5 \cdot 10^{16}$   $\text{cm}^{-2}$ . We included designs of varying cantilever dimensions (length  $l_c$  of 1.5–6 mm, width  $w_c$  of 30–200  $\mu\text{m}$ , and thickness  $t_c$  of 7–50  $\mu\text{m}$ ) and varying piezoresistor dimensions (length  $l_p$  of 200–350  $\mu\text{m}$  and width  $w_p$  of 10–20  $\mu\text{m}$ ) in Fig. 1. A wet oxidation at 1000–1150  $^\circ\text{C}$  (15–45 min) followed by an anneal in  $\text{N}_2$  at 1000–1150  $^\circ\text{C}$  (5–32 min) electrically activates the dopant and diffuses the dopant to varying extents.

We attached the cantilevers to custom printed circuit boards (Imagineering Inc., Elk Grove Village, IL) with epoxy (Devcon, Glenview, IL) and wirebonded them with aluminum wire. The piezoresistor resistance change was transduced with a 1/4-active Wheatstone bridge and amplified with an instrumentation amplifier (Analog Devices AD8221 or Texas Instruments INA103, depending on the piezoresistor resistance) before data acquisition. Also, 1/4 of the bridge is an unstrained matched piezoresistor for temperature compensation.

We measured the spring constant, force sensitivity, and first-mode resonant frequency of each cantilever using a laser Doppler vibrometer (LDV) (Polytec OFV3001) [26]. The cantilever and printed circuit board were mounted on a piezoelectric shaker (Jodon, Ann Arbor, MI). The vibrometer laser was pointed at the tip of the cantilever to measure the velocity of the cantilever tip. We determined the resonant frequency  $f_0$  from the power spectral density of the LDV output while the shaker was driven with white noise; shaker drive signal and LDV measurement were accomplished with a vector signal analyzer (HP 89441A). We determined cantilever stiffness  $k_c$  from the resonant frequency and dimensions of cantilever

$$k_c = \frac{Ew_c t_c^3}{4l_c^3} \quad (1)$$

which can also be written as

$$k_c = 0.24\rho_c l_c w_c t_c (2\pi f_0)^2 \quad (2)$$

where  $\rho_c$  is the density of the cantilever. We calibrated the piezoresistor displacement sensitivity by shaking the cantilevers at their resonant frequency. Displacement voltage sensitivity is extracted from the tip displacement output of the vibrometer ( $S_{\text{vibro}} V_{\text{vibro}}/2\pi f_0$ ), and the voltage across the piezoresistors ( $V_{\text{piezo}}$ ) is measured from the Wheatstone bridge

$$S_{dV,\text{measured}} = \frac{2\pi f_0 V_{\text{piezo}}}{S_{\text{vibro}} V_{\text{vibro}}} \quad (3)$$

where  $S_{\text{vibro}}$  and  $V_{\text{vibro}}$  are the velocity sensitivity and velocity voltage signal of the vibrometer, respectively.

We simulated dopant profiles using TSUPREM4 (Synopsys, Mountain View, CA) (Fig. 2). To compute the efficiency factor and sensitivity of each cantilever, we used the fabrication process steps in Table I. We compared the simulation results with dopant profiles measured by spreading the resistance analysis (Solecon Laboratories, Reno, NV) of test structures (5 mm  $\times$  5 mm) fabricated during the piezoresistive cantilever process [Fig. 2(d)]. The geometry factor  $\gamma$  is calculated from finite-element analysis using COMSOL (COMSOL, Inc., Burlington, MA).

### III. ANALYTICAL MODEL FOR SENSITIVITY

#### A. Change in Resistance Due to Applied Stress

Piezoresistivity describes the change in the electrical resistance of a material due to the applied mechanical stress [27], [28]. To calculate the change in resistance due to the mechanical stress, we consider arbitrary profiles of both electrical resistance and mechanical stress, i.e., dopant concentration profile ( $p$ ) and stress distribution ( $\sigma$ ). Additionally, because resistivity  $\rho$ , carrier mobility  $\mu$ , and piezoresistivity  $\pi$  are a function of dopant concentration,  $p$ ,  $\sigma$ ,  $\rho$ ,  $\mu$ , and  $\pi$  are defined locally. Therefore, it is necessary to average the change in resistance by integrating all local variables over the three dimensions.

In this paper, we derive the analytical solution for the sensitivity of a typical device with a U-shaped piezoresistor. We make four simplifying assumptions. First, we consider resistivity ( $\rho_l$ ) only in the longitudinal direction of the piezoresistor. Current flow in a U-shaped piezoresistor can be assumed 1-D, because the piezoresistor length is much greater than its

width. Second, we assume that the doping method is uniform across the wafer so that the dopant concentration varies only across the thickness of the piezoresistor. Third, lateral diffusion is negligible compared with diffusion in the thickness direction, because the width of the piezoresistor is much larger than the junction depth. Fourth, we neglect shear piezoresistivity, because longitudinal piezoresistors are insensitive to shear stress. Assuming plane stress [28], the change in resistance is a function of the longitudinal piezoresistance coefficient ( $\pi_l$ ), transverse piezoresistance coefficient ( $\pi_t$ ), normal stress parallel to the current ( $\sigma_l$ ), and normal stress perpendicular to the current ( $\sigma_t$ )

$$\frac{\Delta\rho}{\rho} = \frac{\Delta\rho_l(x, y, z)}{\rho_l(z)} \quad (4)$$

or

$$\frac{\Delta\rho}{\rho} = \pi_l(z)\sigma_l(x, y, z) + \pi_t(z)\sigma_t(x, y, z) \quad (5)$$

where  $x$ ,  $y$ , and  $z$  are oriented parallel to the width, length, and thickness of the device, respectively (Fig. 1).

We model the piezoresistor as a composite of many thin slices connected in parallel, where the resistivity and piezoresistance coefficient of each thin slice are constant. We calculate the change in resistance of each slice, then integrate the conductance, which is the inverse of resistance, to compute the overall resistance change ( $\Delta R/R$ ) due to the applied stress. The change in resistance (see Appendix for detailed calculations) is

$$\frac{\Delta R}{R} = \frac{\pi_{l,\max} \int_{-t_c/2}^{t_c/2} q\mu p P_l \bar{\sigma}_l dz}{\int_{-t_c/2}^{t_c/2} q\mu p dz} + \frac{\pi_{t,\max} \int_{-t_c/2}^{t_c/2} q\mu p P_t \bar{\sigma}_t dz}{\int_{-t_c/2}^{t_c/2} q\mu p dz} \quad (6)$$

where  $\bar{\sigma}_l$  and  $\bar{\sigma}_t$  are the averages of longitudinal and transverse stresses in longitudinal direction, respectively ( $\int_0^{l_p} \sigma_l dy / l_p$  and  $\int_0^{l_p} \sigma_t dy / l_p$ ).  $P_l$  and  $P_t$  are the longitudinal and transverse piezoresistance factors, obtained by dividing the local piezoresistance coefficient by the maximum obtainable, i.e.,  $\pi_{l,\max}$  and  $\pi_{t,\max}$ . The piezoresistance factor  $P$  varies with temperature and dopant concentration, while  $\pi_{\max}$  varies with piezoresistor orientation. Both Kanda's theoretical model [28] based on Smith's data [27] and Harley and Kenny's empirical fit [4] based on experimental results [29]–[31] are available for the piezoresistance factor. A recent theoretical model by Richter *et al.* [32] analyzed the gap between Kanda's model and Harley's fit (Fig. 3). They achieved a good agreement between a theoretical model and experimental results if the full range of possible scattering mechanisms are considered, including acoustic phonon, nonpolar optical phonon, and ionized impurity scattering. Thus, we use the values obtained by Richter *et al.* for  $P$  and the maximum value for  $\pi_{\max}$ , i.e.,  $72 \cdot 10^{-11} \text{ Pa}^{-1}$  in the [110] direction for silicon with a p-type dopant. In addition, carrier mobility is calculated as in [33]. Equation (6) is an analytical solution of the change in resistance for a piezoresistive device due to applied stress. If we know the dopant concentration profile  $p(z)$  and stress distribution  $\sigma(x, y, z)$  of the device, then we can calculate the change in resistance and, thus, the force and displacement sensitivity.

## B. Sensitivity of a Piezoresistive Cantilever

The stress distribution is readily calculated from Euler beam theory based upon the assumptions noted earlier. An external force  $F$  applied to the tip of the cantilever induces a uniaxial stress field

$$\sigma_l = \frac{12(l_c - x)z}{w_c t_c^3} F. \quad (7)$$

The sensitivity can be expressed in terms of force or displacement and in terms of change in resistance or voltage. We indicate the sensitivity ( $S$ ) with subscripts (force  $F$ , displacement  $d$ , resistance  $\Omega$ , and voltage  $V$ ). From (6) and (7), the force sensitivity ( $(\Delta R/R)/F$ ) for an end-loaded beam is

$$S_{F\Omega} = \frac{12(l_c - 0.5l_p)\pi l_{\max} \int_{-t_c/2}^{t_c/2} q\mu p P z dz}{w_c t_c^3 \int_{-t_c/2}^{t_c/2} q\mu p dz}. \quad (8)$$

This exact solution for force sensitivity captures both dopant and stress profile effects.

## C. Geometry Factor $\gamma$

$\gamma$  is a geometry factor defined as the ratio of the resistance of the strained region in the piezoresistor to the total resistance including unstrained regions, interconnects, and contact pads [Fig. 1(c)], which act to reduce force sensitivity ( $\gamma < 1$ ). We can estimate the ratio of the resistance of the strained region to the total resistance by calculating the voltage distribution of a piezoresistor using finite-element analysis (Fig. 4).

## D. Efficiency Factor $\beta^*$

We introduce an efficiency factor  $\beta^*$  by dividing the force sensitivity for an arbitrary dopant concentration profile by the theoretical maximum force sensitivity. The theoretical maximum force sensitivity can be achieved if the dopant atoms exist only at the surface [ $z = t/2$ , Fig. 1 (e)], and the dopant concentration is small enough to maintain the maximum piezoresistance factor ( $P = 1$ ). If  $P = 1$ , then the force sensitivity becomes

$$S_{F\Omega, \max} = \frac{6(l_c - 0.5l_p)\pi l_{\max}}{w_c t_c^2}. \quad (9)$$

The efficiency factor  $\beta^*$  is defined as

$$\beta^* = \frac{S_{F\Omega}}{S_{F\Omega, \max}} = \frac{2 \int_{-t_c/2}^{t_c/2} q\mu p P z dz}{t_c \int_{-t_c/2}^{t_c/2} q\mu p dz}. \quad (10)$$

Using this efficiency factor, the force sensitivity (8) for any arbitrary dopant profile may be expressed as

$$S_{F\Omega} = \frac{6(l_c - 0.5l_p)\pi l_{\max}}{w_c t_c^2} \beta^*. \quad (11)$$

Considering a balanced 1/4-active Wheatstone bridge configuration ( $(V_{\text{out}}/V_{\text{bridge}}) \approx (\Delta R/4R)$ ), voltage force sensitivity is

$$S_{FV} = \frac{3(l_c - 0.5l_p)\pi l_{\text{max}}}{2w_c t_c^2} \gamma V_{\text{bridge}} \beta^* \quad (12)$$

where  $V_{\text{bridge}}$  is the Wheatstone bridge bias voltage. From the force sensitivity (12) and spring constant  $k_c$  (1), the displacement sensitivity is

$$S_{dV} = \frac{3Et(l_c - 0.5l_p)\pi l_{\text{max}}}{8l_c^3} \gamma V_{\text{bridge}} \beta^*. \quad (13)$$

In summary, we can calculate the force and displacement sensitivities [(12) and (13)] from the lateral cantilever dimensions ( $l_c$  and  $w_c$ ), piezoresistor length ( $l_p$ ), and  $\beta^*$ , which is a function of dopant profile and cantilever thickness ( $t_c$ ).

#### IV. EFFECT OF FABRICATION PROCESSES ON $\beta^*$

$\beta^*$  describes how the dopant profile affects the sensitivity of the device. If dopants are close to the surface and the dopant concentration is low enough to maintain a high piezoresistance factor across the resistor, then  $\beta^*$  is close to one. If the dopants are uniformly distributed through the thickness of the cantilever or the dopant concentration is very high, then  $\beta^*$  approaches zero.  $\beta^*$  is a function of only cantilever thickness and process parameters; therefore, devices from the same wafer and process have a single  $\beta^*$  independent of cantilever length and width. The practical significance of this is that we can separate the process parameters from the design parameters, making it possible to design the cantilever geometry and fabrication process separately. Additionally,  $\beta^*$  can be used for other piezoresistive devices besides cantilevers: The  $\beta^*$  of an arbitrary device is the same as the  $\beta^*$  of a piezoresistive cantilever (10) if  $\sigma$  in the device is linearly proportional to  $z$  in (6).

##### A. $\beta^*$ for Ideal Epitaxial Growth

In an ideal epitaxial piezoresistor [Fig. 1(f)] where dopant atom diffusion is negligible, the dopant concentration and the piezoresistance factor  $P$  are constant within the junction depth  $t_p$ . Thus, the efficiency factor of an ideal epitaxial cantilever is

$$\beta^* = P \left( 1 - \frac{t_p}{t_c} \right). \quad (14)$$

##### B. $\beta^*$ for Nonuniform Doping Profiles

Diffusion of dopant atoms during high-temperature processes leads to a nonuniform dopant profile. The electrically active dopant concentration profile can be simulated with TSUPREM4 [Fig. 2(a)–(c)] or experimentally measured using spreading resistance analysis [Fig. 2(d)]. In Fig. 5, we calculated  $\beta^*$  for epitaxial (A, C, and E) and ion-implanted (B, D, and F) cantilevers in various conditions such as different cantilever thickness (A and B), dopant concentration (C), implantation dose (D), epitaxial layer thickness (E), and implantation energy (F). To investigate how diffusion affects  $\beta^*$  with various process conditions,  $\beta^*$  in Fig. 5 was also calculated with various annealing conditions (temperature  $T$  and time  $t$ ) and was plotted in terms of diffusion length ( $\sqrt{Dt}$ ). The diffusion coefficient is defined as  $D = D_{i0} \exp(-E_{id}/$



$k_B T$ ), where for boron  $D_{io} = 0.037 \text{ cm}^2/\text{s}$  and  $E_{ia} = 3.46 \text{ eV}$  [34]. Each line corresponds to each annealing temperature plot with various times (15–180 min).

**1) Effect of Cantilever Thickness on  $\beta^*$** —Epitaxial piezoresistors can be approximated with (14) until the diffusion length is comparable to the cantilever thickness [Fig. 5(a)]. Similarly, ion-implanted piezoresistors have constant  $\beta^*$  values until the diffusion length becomes significant [Fig. 5(b)]. The transition point depends on cantilever thickness;  $\beta^*$  decreases in the case of thin cantilevers (5 and 7  $\mu\text{m}$ ), while  $\beta^*$  increases with diffusion length in the case of thick cantilevers (15, 25, and 50  $\mu\text{m}$ ). The trend of  $\beta^*$  with diffusion length depends upon two competing mechanisms: the depth effect and the piezoresistance factor effect. During diffusion, dopant atoms move from the top surface of the cantilever toward the neutral axis. Bending stress decreases linearly with depth; therefore,  $\beta^*$  decreases with diffusion length due to the depth effect. However, the piezoresistance factor is inversely proportional to dopant concentration; therefore, diffusion simultaneously acts to increase  $\beta^*$  by the piezoresistive factor effect. These two effects compete to determine the trend of  $\beta^*$  with diffusion length. In relatively thin cantilevers, [Fig. 5(a) and (b)], the piezoresistance factor effect is negligible, and the depth effect dominates. However, for relatively thick cantilevers [15, 25, and 50  $\mu\text{m}$ , Fig. 5(b)], the piezoresistance factor effect dominates until the junction depth is comparable to the half-thickness of the cantilever.

**2) Effect of Concentration and Dose on  $\beta^*$** —For epitaxial cantilevers of varied initial dopant concentration [Fig. 5(c)],  $\beta^*$  decreases as the dopant concentration is increased. Ion-implanted cantilevers of varied doses [Fig. 5(d)] show a similar trend;  $\beta^*$  of low-dose cantilevers is greater than that of cantilevers with a high implant dose. However,  $\beta^*$  converges for high-dose minimal- $(\sqrt{Dt})$  processes because the effects of dopant activation and solid solubility limit become substantial.  $\beta^*$  diverges with increasing diffusion length as dopant atoms are activated and diffuse away. Note that lightly doped piezoresistors have large  $\beta^*$  values, but can lead to large drift and electrical noise and may not yield optimal resolution.

**3) Effect of Initial Junction Depth on  $\beta^*$** —Junction depth is defined as the depth where the doping concentration of a piezoresistor drops to background concentration. In the case of epitaxial piezoresistors with varying initial thickness ratios ( $t_p/t_c$ ) [Fig. 5(e)],  $\beta^*$  is inversely proportional to the thickness ratio as expected. Ion-implanted cantilevers show a similar trend [Fig. 5(f)]; the formation of shallow piezoresistors by reducing implantation energy tends to improve  $\beta^*$  for a given dose. However, there is an exception to this trend in the case of low-dose low-diffusion-length piezoresistors where  $\beta^*$  is actually improved with implantation energy because of the piezoresistance factor effect.

The effect of increasing ion mass for a fixed energy is similar to that of decreasing implantation energy [Fig. 5(f)] because the initial dopant depth is reduced. Bergaud *et al.* [35] demonstrated that ultrashallow piezoresistors can be fabricated by the implantation of more massive ions such as  $\text{BF}_2$ . We calculated  $\beta^*$  for cantilevers with boron and  $\text{BF}_2$  dopant atoms in Fig. 6. The competition between the depth and piezoresistance factor effects is evident in the results.

**4) Effect of Annealing Atmosphere on  $\beta^*$** —Next, we investigated the effect of the postimplantation annealing atmosphere on  $\beta^*$  (Fig. 7). The trend of  $\beta^*$  for dry and wet oxidation is similar to the trend for inert annealing. However,  $\beta^*$  is greater for oxidizing environments because dopant segregation into the oxide acts to reduce the dopant concentration in the piezoresistor and increase  $\beta^*$  by the piezoresistance factor effect. Oxide thickness is greater for wet growth than dry growth at any  $(\sqrt{Dt})$ , and the thicker oxide leads to additional dopant segregation and oxidation-enhanced diffusion [36].

### C. Comparison With Other Analytical Models

We compare the predicted force sensitivity from the idealized model [3], [5], [6], the Tortonese model [2], [4], [22], and our model in Fig. 8. The idealized model ignores the dopant profile and assumes that all of the dopant atoms exist at the top surface. This model is useful to estimate force sensitivity, but diverges from the exact solution for cantilevers with large diffusion lengths. Tortonese *et al.* [2] later considered the dopant profile by modifying the model to include an efficiency factor  $\beta$ , which accounts for the junction-depth effect only

$$\beta = \frac{2 \int_{-t_c/2}^{t_c/2} q\mu p P z dz}{t_c \int_{-t_c/2}^{t_c/2} q\mu p P dz}. \quad (15)$$

Comparing (10) and (15), the Tortonese model ignores the piezoresistance factor effect because the piezoresistance factors in the denominator and numerator cancel. The Tortonese model uses  $P(\max(p))$ , taken as the piezoresistance factor at the maximum dopant concentration. As seen in Fig. 8, the Tortonese model underestimates force sensitivity.

### D. $\beta^*$ Lookup Table

If we separate the dependence of  $\beta^*$  from the thickness of the cantilever, then we can build a lookup table of  $\beta^*$  for various processing conditions. Changing the coordinate system from the neutral axis to the surface of the cantilever [ $z' = t_c/2 - z$ , Fig. 1(d)], we write

$$\beta^* = \frac{2 \int_0^{t_c} (\frac{t_c}{2} - z') q\mu p P dz'}{\int_0^{t_c} q\mu p dz'}. \quad (16)$$

If we assume that most dopants exist within the junction depth  $t_p$

$$\beta^* = \beta_1^* - \frac{2}{t_c} \beta_2^* \quad (17)$$

where  $\beta_1^*$  and  $\beta_2^*$  are defined as

$$\beta_1^* = \frac{\int_0^{t_p} q\mu p P dz'}{\int_0^{t_p} q\mu p dz'} \quad (18)$$

$$\beta_2^* = \frac{\int_0^{t_p} q\mu p P z' dz'}{\int_0^{t_p} q\mu p dz'}. \quad (19)$$

As defined,  $\beta_1^*$  (piezoresistance factor effect) and  $\beta_2^*$  (depth effect) depend only on processing parameters.  $\beta_1^*$  is a conductivity weighted average of the piezoresistance factor. If dopant concentration is low,  $\beta_1^*$  is high because the piezoresistance factor is high.  $\beta_2^*$  is a stress- and depth-dependent term, i.e., how close are the dopant atoms to the maximum stress at the surface. If dopant atoms are located near the surface,  $\beta_2^*$  is low, and then,  $\beta^*$  depends on  $\beta_1^*$  only. If the



dopant atoms are distributed equally across the thickness of the cantilever,  $\beta_2^* \approx 0.5t_c\beta_1^*$ , and  $\beta^*$  approaches zero. Finally, the thickness determines whether  $\beta_1^*$  or  $\beta_2^*$  is dominant (17):  $\beta^*$  depends more on  $\beta_1^*$  for thick cantilevers where the piezoresistance factor effect is more important and on  $\beta_2^*$  for thin cantilevers where the depth effect is more important.

We calculated  $\beta_1^*$  and  $\beta_2^*$  based on TSUPREM4 simulations for inert ( $N_2$ ) annealing (Fig. 9) and provided a lookup table (Table II). The oxide layer is also required for passivation; therefore, we also calculated  $\beta_1^*$  and  $\beta_2^*$  for a typical process with 1500-Å wet isolation oxide. One can estimate  $\beta^*$  using the lookup table values and (17). For example, in the case of a 10- $\mu\text{m}$ -thick cantilever with  $2 \cdot 10^{15} \text{ cm}^{-2}$  implantation dose and a 30-min  $N_2$  anneal at 1000 °C,  $\beta^*$  is 0.50 (0.53–0.13/5). To achieve a  $\beta^*$  larger than zero in (17), cantilever thickness should be larger than two times  $\beta_2^*$ ; therefore, in the case of the previous example, the cantilever thickness should be greater than 0.26  $\mu\text{m}$ .

## V. EXPERIMENTAL VALIDATION

We validated the analytical model by comparing it with numerical simulation and experimental measurements of ion-implanted piezoresistive cantilevers. Based on three different piezoresistance factors (the theoretical values of Richter *et al.* [32], Harley and Kenny's empirical model [4], and Kanda's theoretical values [28]), we calculated  $\beta^*$  from displacement sensitivity (13) and resonant frequency ( $\approx t_c \sqrt{E/\rho_s}/(2\pi l_c)$ ) equations measured by LDV

$$\beta^* = \frac{S_{dV,\text{measured}}}{\frac{3\pi}{4} \sqrt{E\rho_s} \pi l_{\text{max}} \left(1 - 0.5 \frac{l_p}{l_c}\right) \gamma f_0 V_{\text{bridge}}} \quad (20)$$

where  $\rho_s$  is the density of the cantilever and  $\gamma$  is calculated using finite-element analysis.

The predicted force sensitivity and  $\beta^*$  are in good agreement with the experimental results (Fig. 10). Fig. 10(a) shows the change in resistance based on the analytical model and experimental results when a point force is applied at the tip. The fits from Harley's and Richter's data are more accurate than Kanda's at the high dopant concentrations ( $> 5 \cdot 10^{19} \text{ cm}^{-3}$ ) applicable to our devices. Fig. 10(b)–(d) shows the force sensitivity and  $\beta^*$  as a function of diffusion length for cantilevers of varying ion implantation doses and cantilever dimensions. Most of the results are within 5% of the model; however, there are a few points where the deviation from the analytical model is up to 20%. Errors could result from the lateral spreading of dopants due to diffusion, fabrication and experimental uncertainty, or operating temperature fluctuations with resistance heating. The contribution of electrical current due to the lateral spreading of dopants is up to 6% in our case ( $w_p/t_p \sim 5$ ). The uncertainty of measured  $\beta^*$  in (20) is 7.4% from an uncertainty analysis [37] including variation in  $l_p/l_c$ ,  $\gamma$ , the Young's modulus, density, and the piezoresistance coefficient possibly from the misalignment of the cantilevers from the [110] direction as well as the undercut of the clamped boundary during backside release. Measured  $\beta^*$  values from thin cantilevers depart from the model more than thick cantilevers. We believe the cases with larger errors due to the thermal resistance of the cantilever and the decrease in piezoresistance with temperature [32].

For typical 7- $\mu\text{m}$ -thick cantilevers with 15-min wet oxidation and 10-min  $N_2$  annealing at 1000 °C,  $\beta^* = 0.50$  from TSUPREM4,  $\beta^* = 0.46$  from dopant profiles from spreading resistance analysis [Fig. 2(d)], and  $\beta^* = 0.49 \pm 0.04$  ( $N = 5$  devices and 1 wafer) from experimental sensitivity. Although TSUPREM4 predicts a greater junction depth than that measured with spreading resistance analysis,  $\beta^*$  is dominated by the high-concentration regions where the agreement between the two is excellent. In addition, we found that  $\beta^*$  for various cantilever

geometries (1686–3175  $\mu\text{m}$  long and 30–200  $\mu\text{m}$  wide) from a single wafer have only 0.04 standard deviation. This repeatability demonstrates that all devices from a single wafer (with uniform device thickness) have the same  $\beta^*$ , independent of cantilever geometry.

## VI. CONCLUSION

We have presented an improved analytical model of piezoresistive cantilever sensitivity. In addition, we investigated the effect of cantilever design and process parameters (device thickness, implant dose, implant energy, dopant atom, and annealing atmosphere) on the efficiency factor and force sensitivity. We found that there are two competing effects: the depth effect and the piezoresistance factor effect, which determine the overall efficiency factor  $\beta^*$ . Optimal conditions may be defined to maximize the efficiency factor and sensitivity when the two competing effects are balanced. We characterized numerous piezoresistive cantilevers over a range of process conditions and verified that the model agrees with simulation and experiment. By separating the wafer processing parameters from cantilever geometry, the design process is simplified, and process and geometry design are decoupled. Finally, we have also provided a lookup table for design guidance, so that other researchers can quickly and accurately predict sensitivity for piezoresistive devices.

## Acknowledgments

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## APPENDIX

### VII. CALCULATION OF TOTAL CHANGE IN RESISTANCE OF PIEZORESISTOR

Consider a thin slice of cantilever with  $t_{\text{slice}}$  thickness. The total resistance of the slice is

$$R_{\text{slice}} = 2 \int_0^{l_p} \frac{\rho(z)}{w_p t_{\text{slice}}} dy = \frac{2\rho l_p}{w_p t_{\text{slice}}}. \quad (21)$$

Similarly, the change in resistance of a slice of the piezoresistor due to piezoresistivity is

$$\Delta R_{\text{slice}} = 2 \int_0^{l_p} \frac{\Delta\rho(x, y, z)}{w_p t_{\text{slice}}} dy. \quad (22)$$

Dividing (22) by (21), we calculate the ratio of resistance change

$$\frac{\Delta R_{\text{slice}}}{R_{\text{slice}}} = \frac{1}{l_p} \int_0^{l_p} \frac{\Delta \rho}{\rho} dy = \pi_l \bar{\sigma}_l + \pi_t \bar{\sigma}_t \quad (23)$$

where  $\bar{\sigma}_l$  and  $\bar{\sigma}_t$  are the averages of longitudinal and transverse stresses in longitudinal direction, respectively ( $\int_0^{l_p} \sigma_l dy / l_p$  and  $\int_0^{l_p} \sigma_t dy / l_p$ ).

We integrate the conductance change, which is the inverse of the resistance change of slices across the thickness of the cantilever to calculate the total change in the resistance of the piezoresistor. Since the slices of the piezoresistor are connected in parallel, we calculate conductance rather than resistance. Overall, conductance is

$$G = \int_{-t_c/2}^{t_c/2} \frac{w_p}{2\rho l_p} dz = \frac{w_p}{2l_p} \int_{-t_c/2}^{t_c/2} \frac{1}{\rho} dz. \quad (24)$$

Since the change in resistance is the negative of the change in conductance ( $\Delta R/R = -\Delta G/G$ ), the change in conductance is

$$\Delta G = -\frac{\Delta R}{R^2} = -\sum_{z=-t/2}^{t/2} \frac{1}{R_{\text{slice}}} \frac{\Delta R_{\text{slice}}}{R_{\text{slice}}}. \quad (25)$$

Using (21) and (23),

$$\Delta G = -\frac{w_p}{2l_p} \int_{-t_c/2}^{t_c/2} \frac{1}{\rho} (\pi_l \bar{\sigma}_l + \pi_t \bar{\sigma}_t) dz. \quad (26)$$

Then, using (24) and (26), we can calculate the change in resistance

$$\frac{\Delta R}{R} = -\frac{\Delta G}{G} = \frac{\int_{-t_c/2}^{t_c/2} \frac{1}{\rho} (\pi_l \bar{\sigma}_l + \pi_t \bar{\sigma}_t) dz}{\int_{-t_c/2}^{t_c/2} \frac{1}{\rho} dz}. \quad (27)$$

We introduce the longitudinal piezoresistance factor  $P_l = \pi_l / \pi_{l,\max}$  and the transverse piezoresistance factor  $P_t = \pi_t / \pi_{t,\max}$ , where  $\pi_{l,\max}$  and  $\pi_{t,\max}$  are the maximum longitudinal and transverse piezoresistivities as a function of direction at 300 K, respectively. Then, the change in resistance is

$$\frac{\Delta R}{R} = \frac{\pi_{l,\max} \int_{-t_c/2}^{t_c/2} q\mu p P_l \bar{\sigma}_l dz}{\int_{-t_c/2}^{t_c/2} q\mu p dz} + \frac{\pi_{t,\max} \int_{-t_c/2}^{t_c/2} q\mu p P_t \bar{\sigma}_t dz}{\int_{-t_c/2}^{t_c/2} q\mu p dz}. \quad (28)$$

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## Biographies



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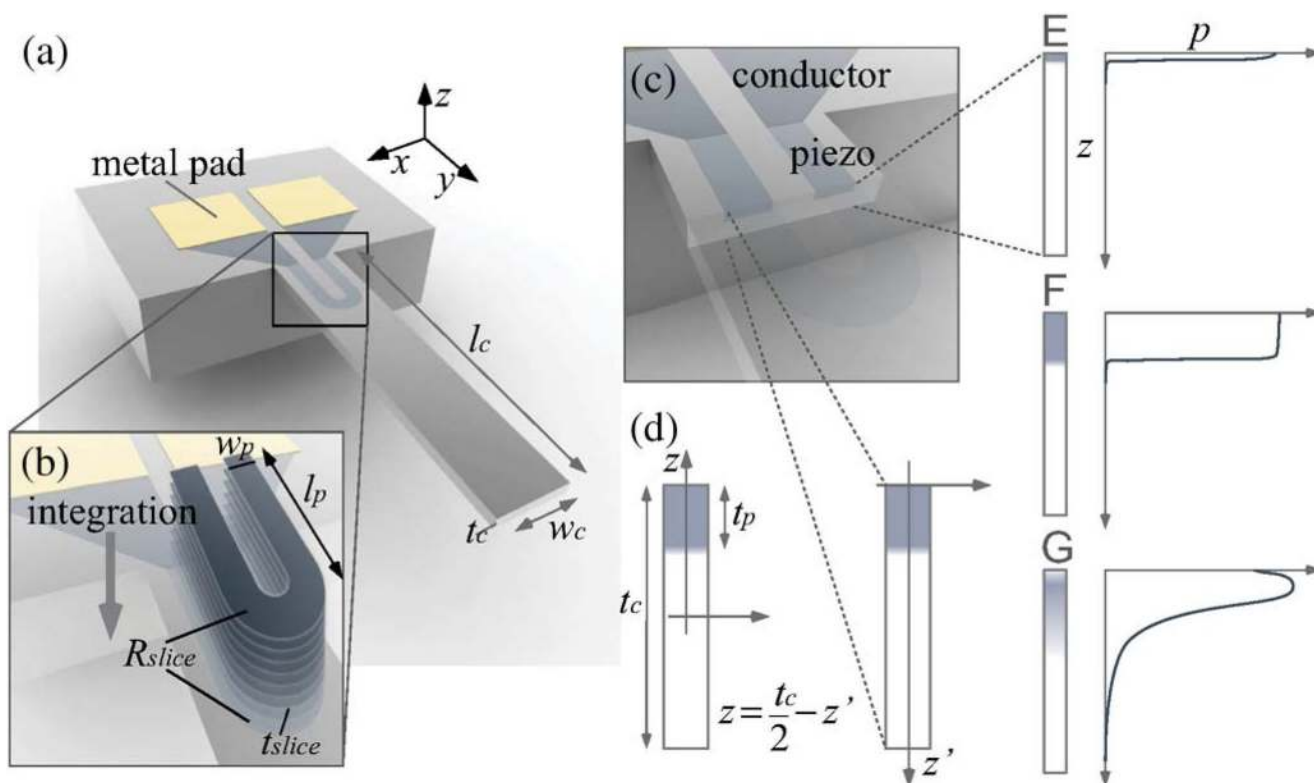


**Beth L. Pruitt** (S'99–M'02) received the B.S. degree in mechanical engineering from the Massachusetts Institute of Technology, Cambridge, in 1991, and the M.S. degree in manufacturing systems engineering and the Ph.D. degree in mechanical engineering from Stanford University, Stanford, CA, in 1992 and 2002, respectively, supported by both the Hertz Foundation Fellowship and the Stanford Future Professors of Manufacturing Fellowship.

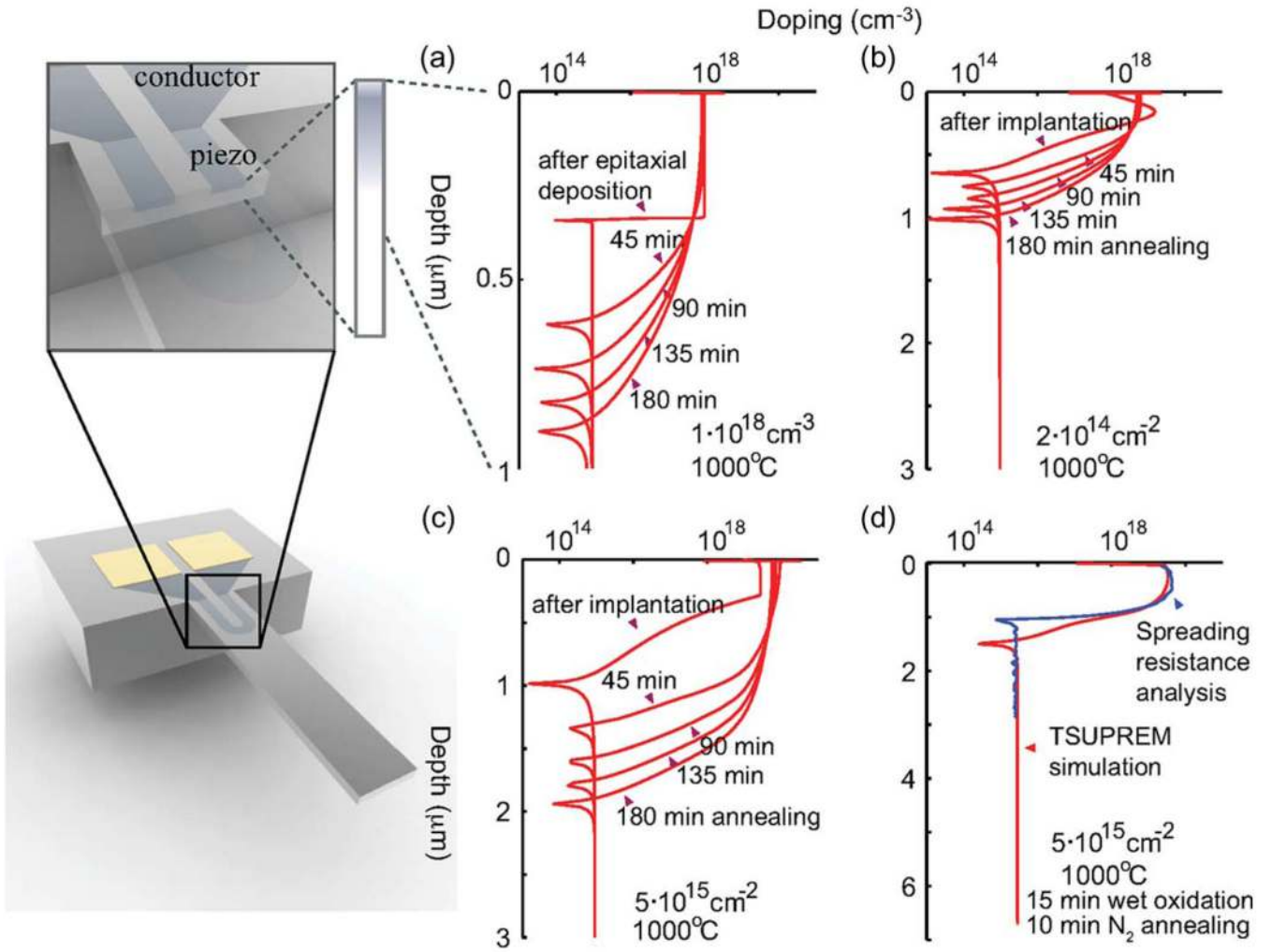
She was an Officer in the U.S. Navy with tours as an Engineering Project Manager at Naval Reactors, Washington, DC, and as an Engineering Instructor at the U.S. Naval Academy. She joined the mechanical engineering faculty at Stanford University in 2003. Her research interests include microelectromechanical systems, particularly metrologies for material characterization and biological measurements, and manufacturing and design for packaging, systems integration, and biomedical devices.

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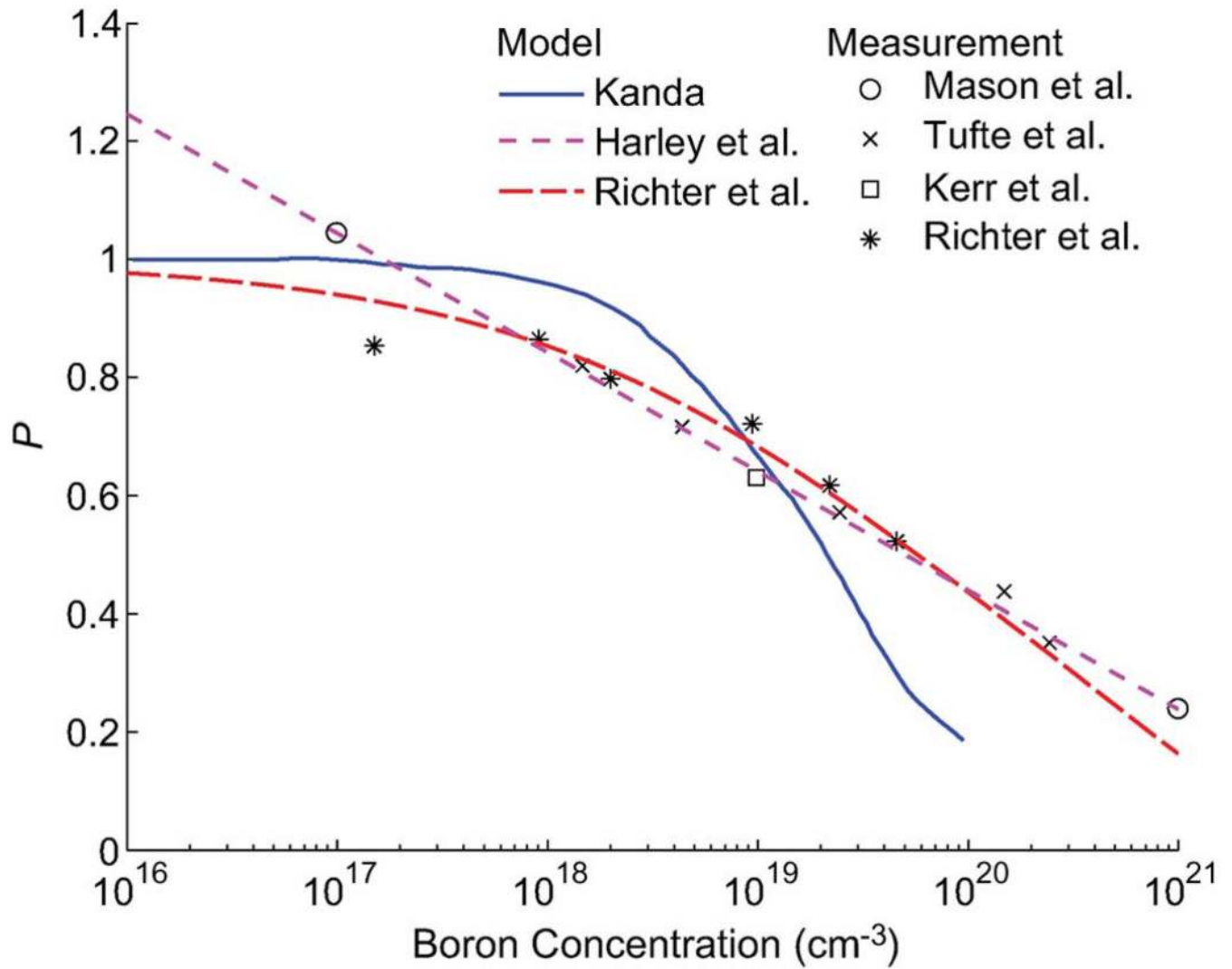




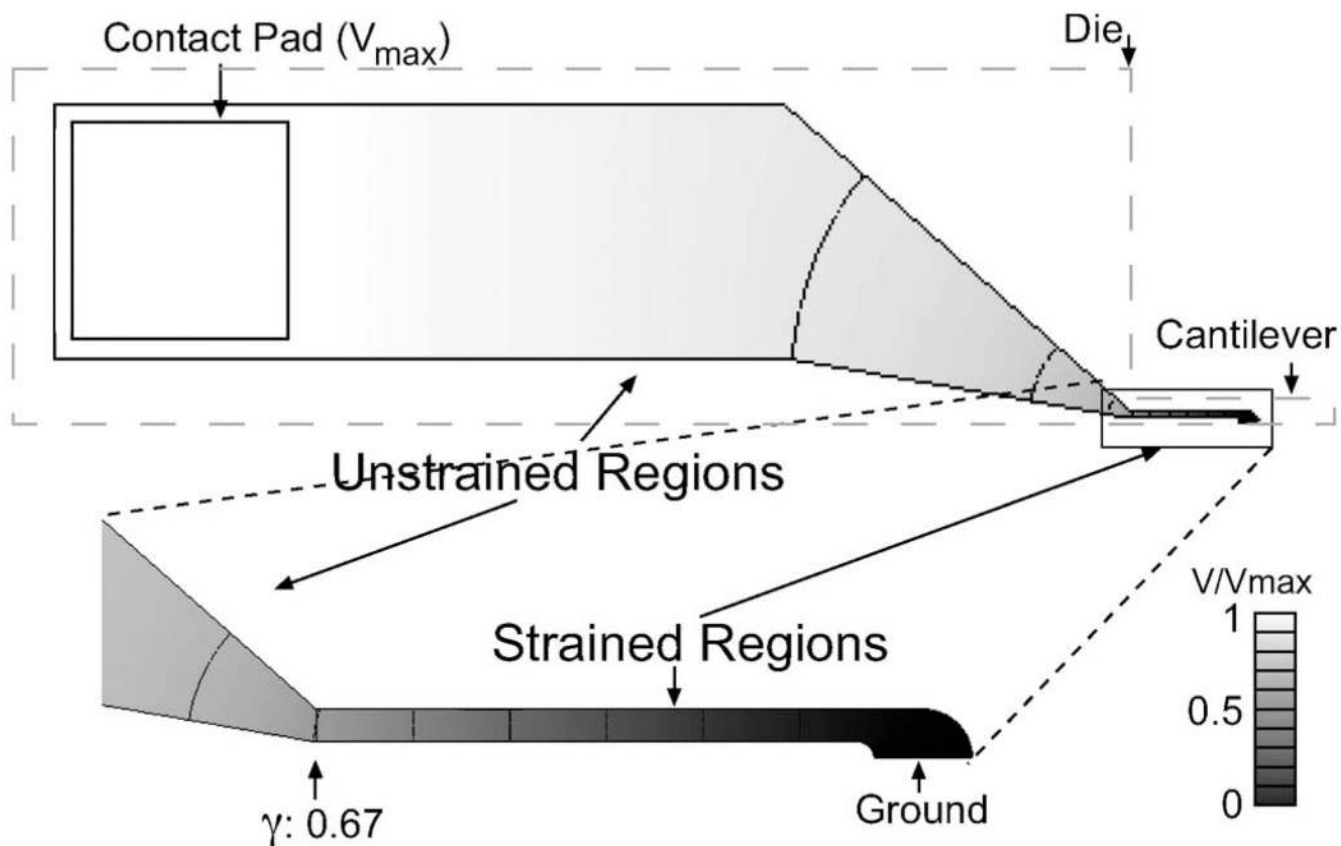
**Fig. 1.** Piezoresistive cantilever. (a) Geometry of cantilever. (b) Geometry of piezoresistor. (c) Strained region (piezoresistor) and unstrained regions (interconnects and contact pads) of the total resistance. (d) Coordinate change and dopant concentration profiles. (e) For maximum force sensitivity (all dopant atoms exist only at the surface). (f) For ideal epitaxial growth (dopant concentration is uniform within the junction depth). (g) For ion implantation, diffusion, or epitaxial growth with annealing process (dopant concentration has an approximately Gaussian distribution).



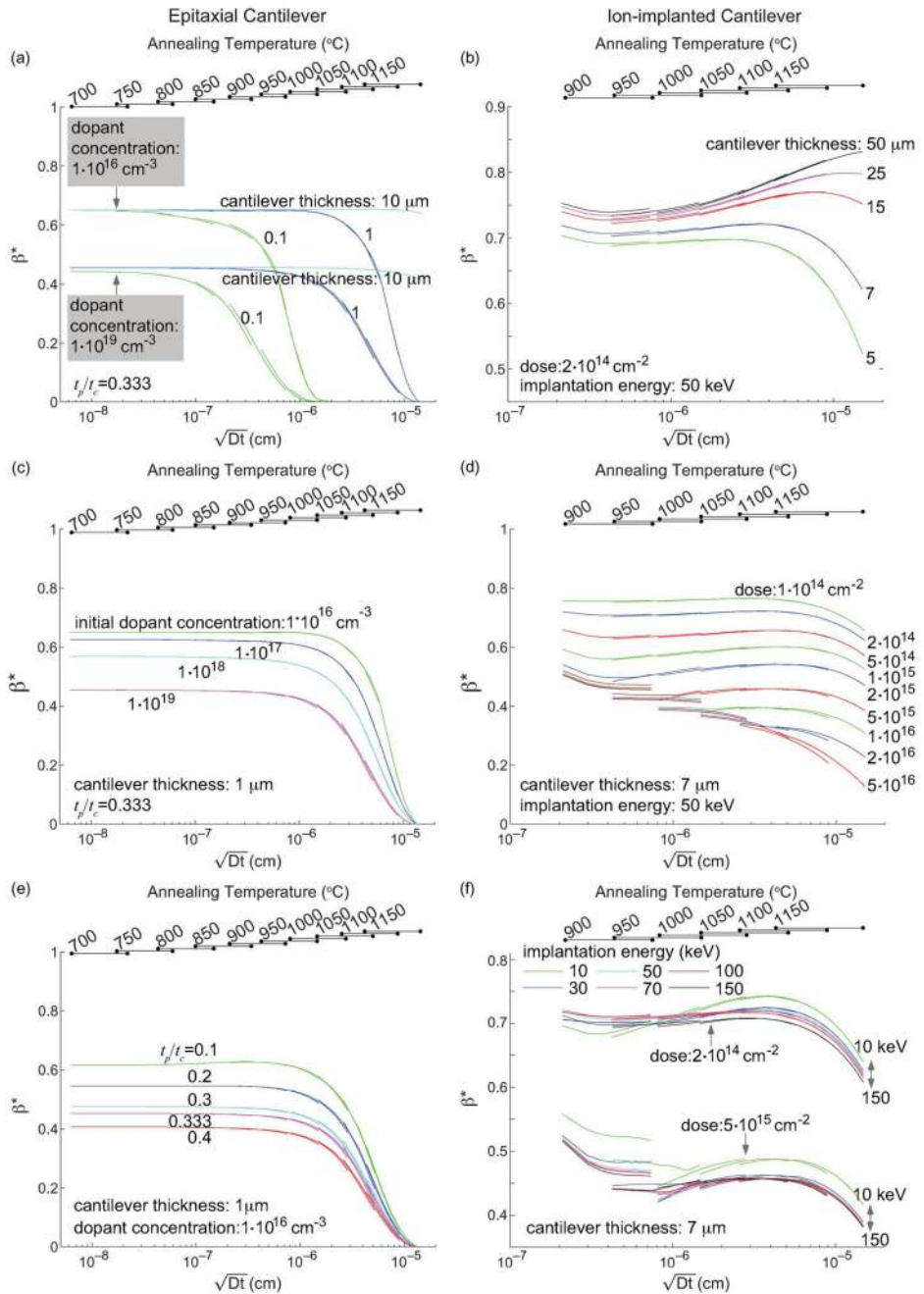
**Fig. 2.** Dopant concentration profiles for the cantilever shown are simulated using TSUPREM4. The plots compare epitaxial and ion-implanted distributions. (a) Inert N<sub>2</sub> anneal at 1000 °C for epitaxial deposition (dopant concentration: 10<sup>18</sup> cm<sup>-3</sup>). (b) For low-dose ion implantation (dopant dose: 2 · 10<sup>14</sup> cm<sup>-2</sup>). (c) For high-dose ion implantation (dopant dose: 5 · 10<sup>15</sup> cm<sup>-2</sup>). (d) Comparison of dopant profiles between TSUPREM4 result and spreading resistance analysis data.



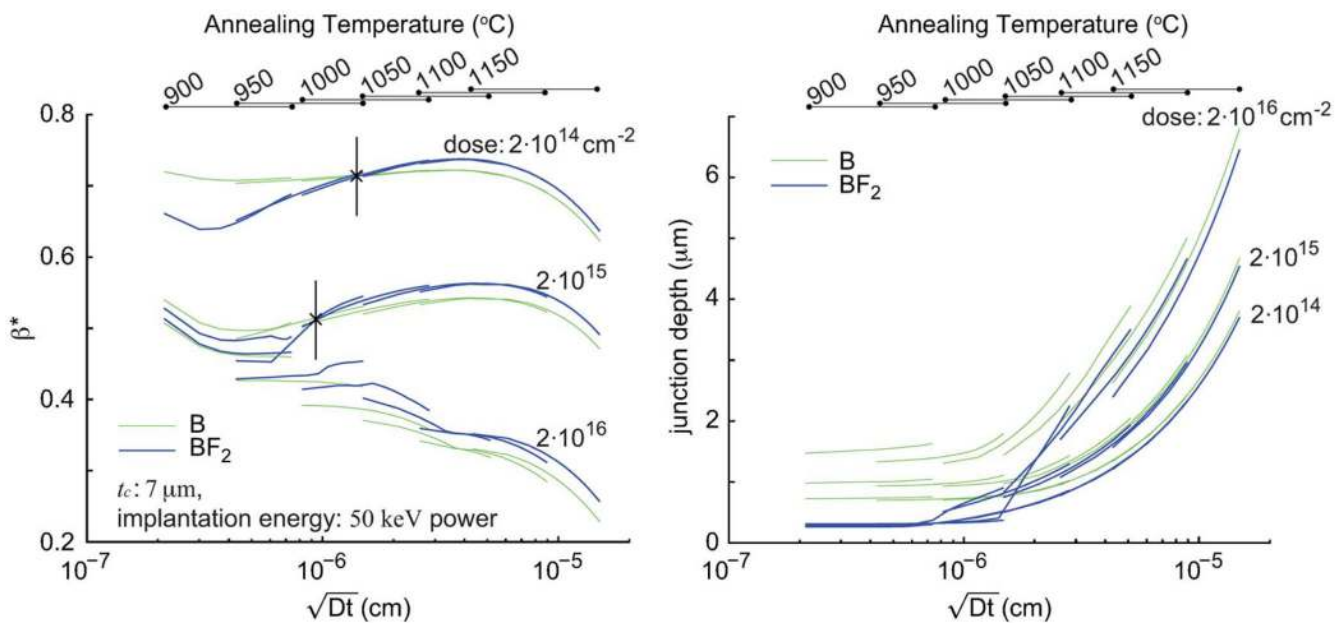
**Fig. 3.** Piezoresistance factor as a function of boron concentration. We used the model presented by Richter *et al.* [32] to calculate  $\beta^*$ . The models presented by Harley *et al.* [4] and Kanda [28] are shown for comparison and are accurate at low and high dopant concentrations, respectively.



**Fig. 4.** Normalized voltage distribution of the typical cantilever which is simulated from finite-element analysis. The geometry factor  $\gamma$  addresses the reduction in sensitivity due to parasitic resistances of unstrained regions (0.33 of total resistance in the typical cantilever). Our typical cantilever has a U-shaped piezoresistor where both strained and unstrained regions have the same sheet resistance.

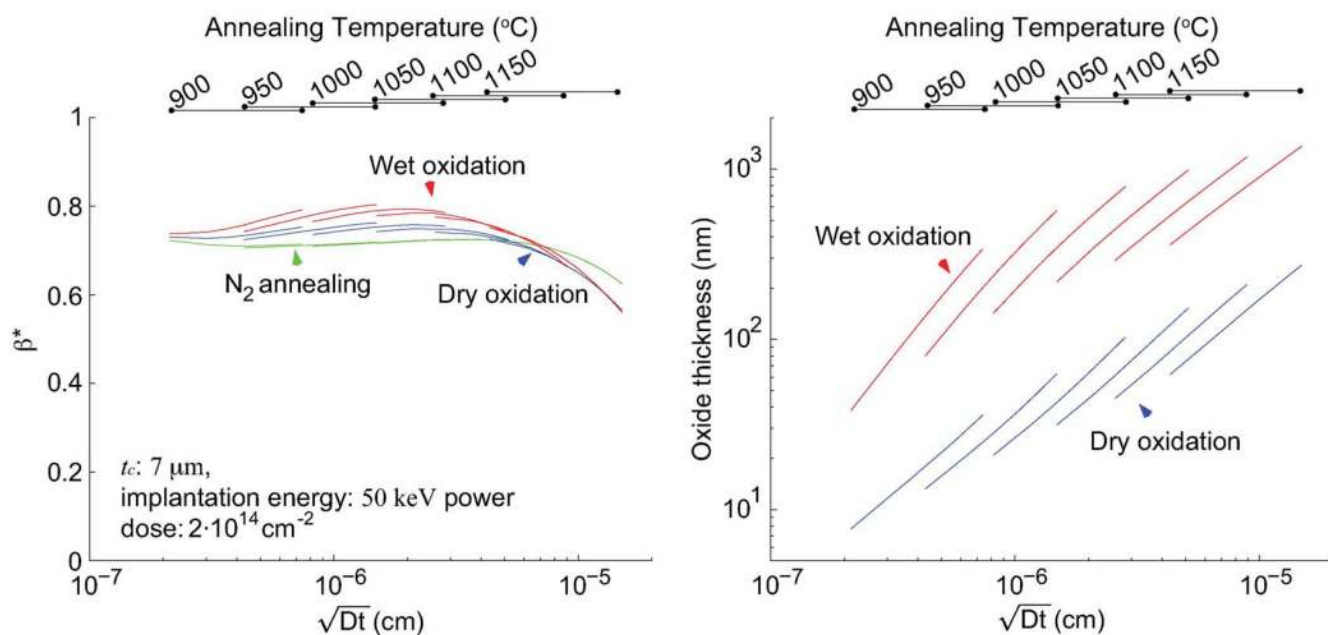


**Fig. 5.**  $\beta^*$  of epitaxial (a, c, and e) and ion-implanted (b, d, and f) cantilevers with various cantilever thicknesses (a and b), dopant concentration (c), implantation dose (d), epitaxial layer thickness (e), and implantation energy (f). Lines are discontinuous because the solid solubility limit depends upon the maximum processing temperature.



**Fig. 6.**  $\beta^*$  and junction depth of piezoresistor formed by B and  $\text{BF}_2$  ion implantation. Both low-power implantation and heavier ion implantation can yield better  $\beta^*$  and force sensitivity. However, the low dose and short diffusion lengths needed to fabricate shallow piezoresistors with  $\text{BF}_2$  require a longer annealing process to achieve better  $\beta^*$  and force sensitivity than elemental boron. The cross indicates diffusion lengths where  $\beta^*$  of piezoresistors with  $\text{BF}_2$  is the same as  $\beta^*$  of piezoresistors with B.

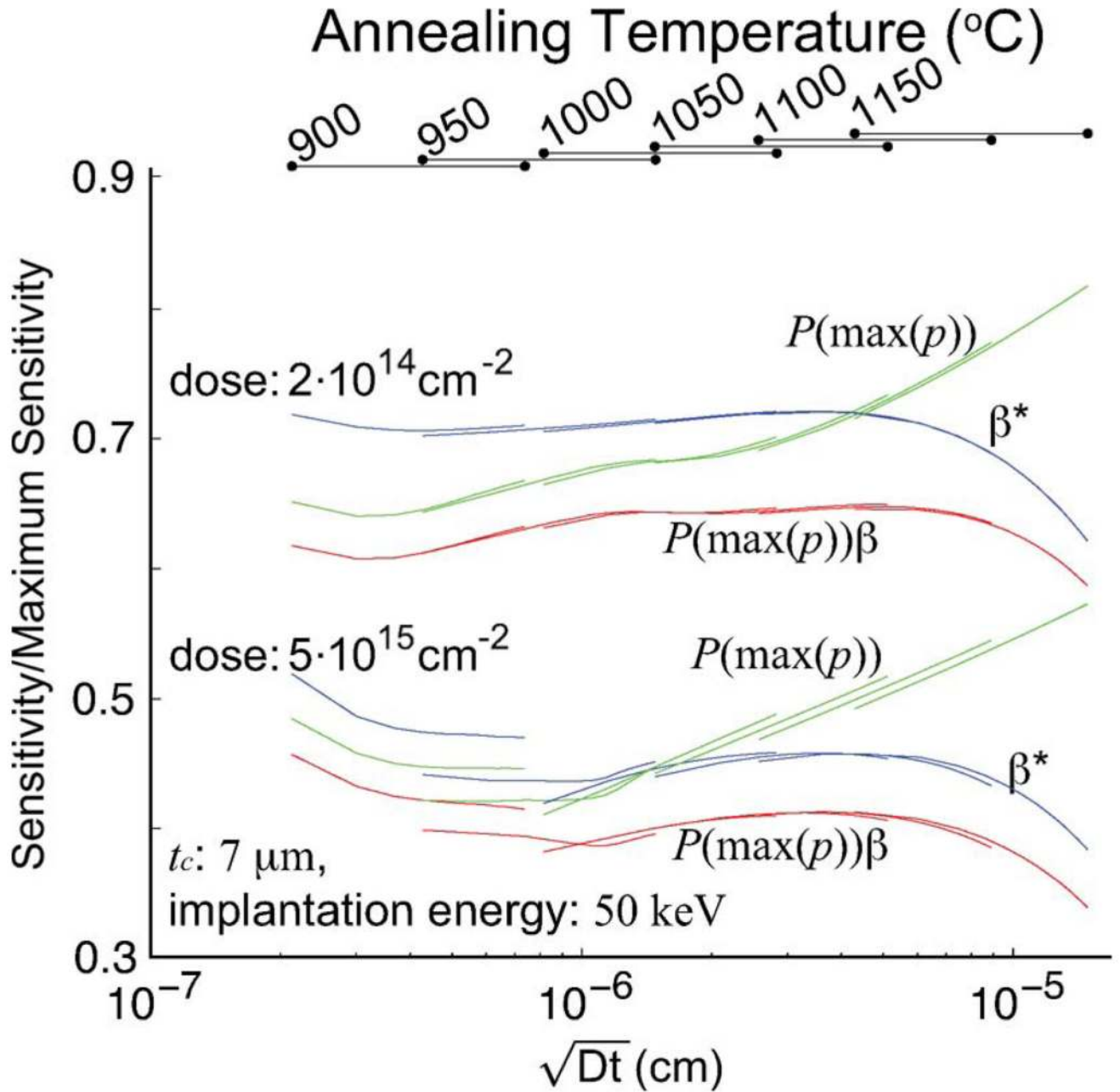




**Fig. 7.**

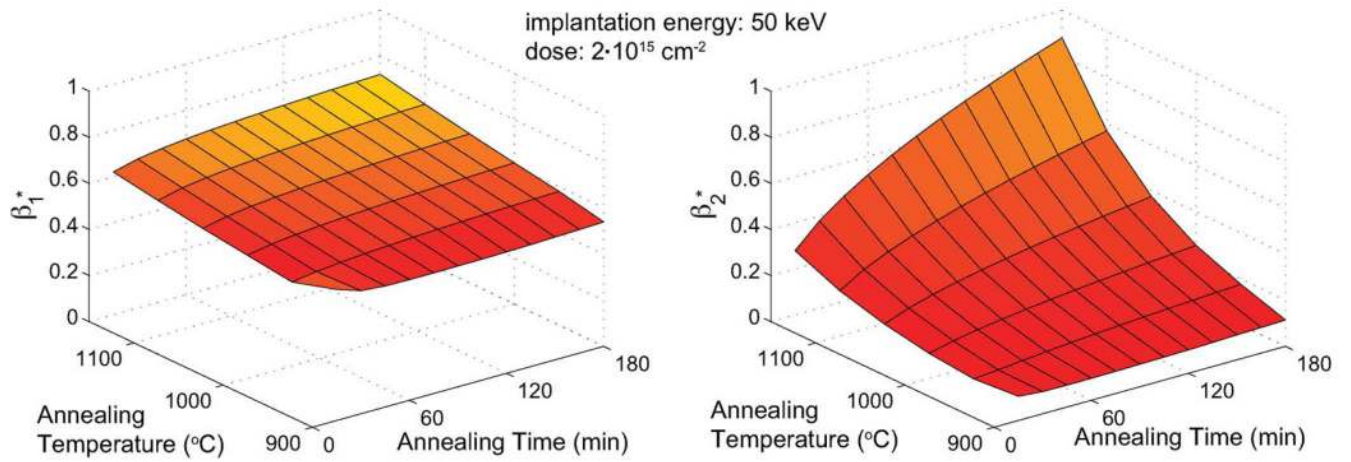
$\beta^*$  and oxide thickness of ion-implanted cantilever with different annealing methods.  $\beta^*$  is greater for oxidizing environments because dopant segregation into the oxide acts to reduce the dopant concentration in the piezoresistor and increase  $\beta^*$  by the piezoresistance factor effect. Note that  $\beta^*$  versus  $\sqrt{Dt}$  of dry and wet oxidation is discontinuous for the different annealing temperature ranges, because of dopant segregation in the oxide.





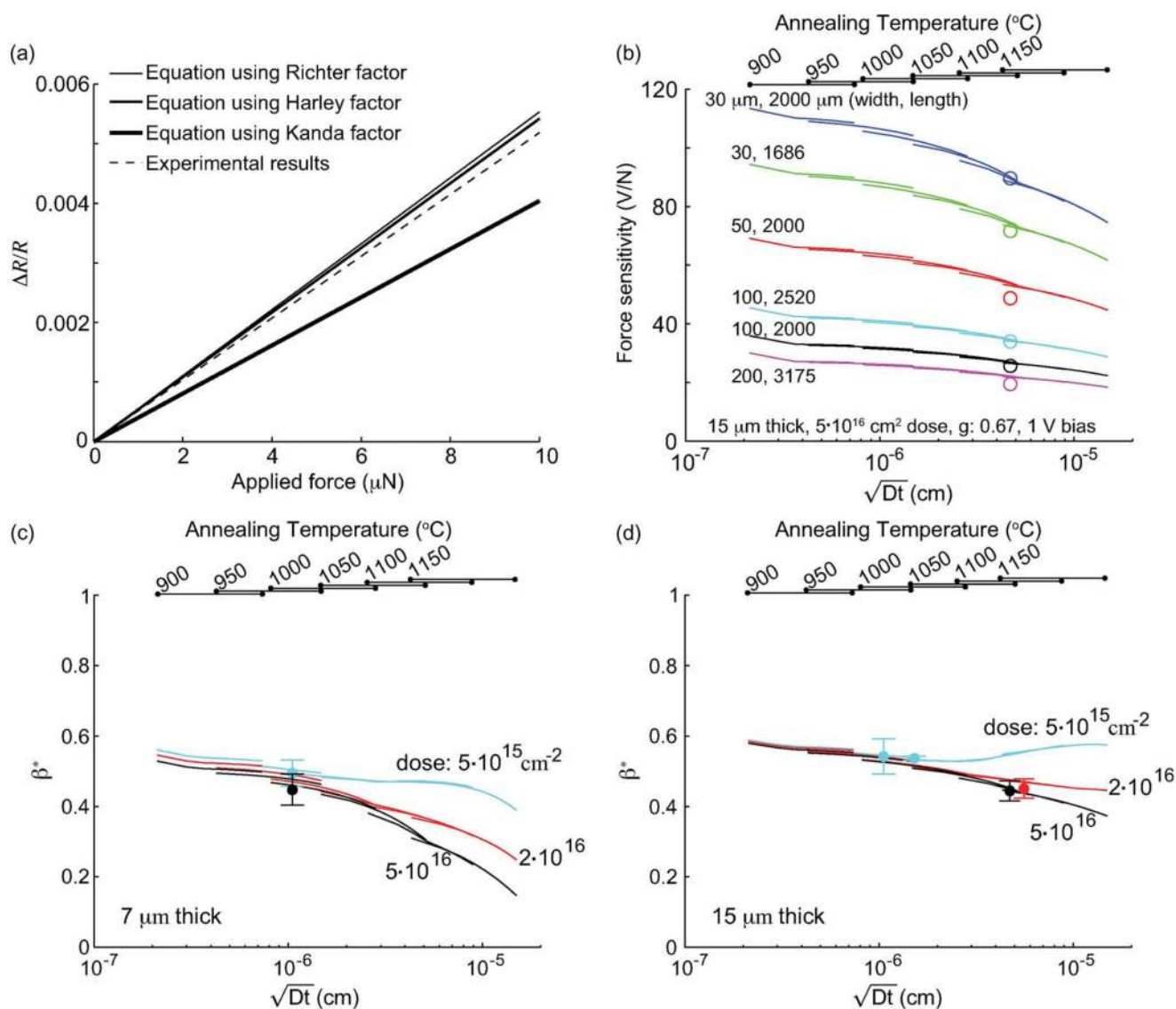
**Fig. 8.**

Comparison with other analytical models.  $P(\max(p))$ ,  $P(\max(p))\beta$ , and  $\beta^*$  indicate the simplified model [5], the Tortonese model [2], [4], and our model, respectively. The disagreement in sensitivity between the three models depends on the fabrication process and cantilever thickness.



**Fig. 9.**

$\beta_1^*$  and  $\beta_2^*$  for boron-implanted piezoresistors (50-keV energy and  $2 \cdot 10^{15} \text{ cm}^{-2}$  dose) with various inert ( $\text{N}_2$ ) annealing temperatures and times.  $\beta_1^*$  (piezoresistance factor effect) and  $\beta_2^*$  (depth effect) depend only on processing parameters.



**Fig. 10.** Validation of the analytical model. (a) Comparison of analytical models for the piezoresistance factor as a function of dopant concentration and experimental results of changes in resistance of a typical piezoresistive cantilever (2000- $\mu\text{m}$ -long 30- $\mu\text{m}$ -wide 15- $\mu\text{m}$ -thick cantilever with 350- $\mu\text{m}$ -long by 10- $\mu\text{m}$ -wide U-shaped piezoresistor having the dopant profile in Fig. 2(d)) based on piezoresistance factors of the theoretical values of Richter [32], Harley and Kenny's empirical model [4], and Kanda's theoretical values [28]. (b) Force sensitivity of piezoresistive cantilevers with various cantilever dimensions. (c and d)  $\beta^*$  of 7- and 15-  $\mu\text{m}$ -thick piezoresistive cantilever. Each point of (b) indicates a sensitivity result of one device with different cantilever dimensions, and each point of (c and d) represents measured  $\beta^*$  values of two to seven devices from different wafers fabricated with different process conditions. The (solid lines) analytical model is in good agreement with (circles) experimental results.

**TABLE I**

## Process Parameters of TSUPREM4 Simulation

Process	Parameters
Screening 250 Å oxide growth	wet O <sub>2</sub> at 850°C for 17 min
Ion implant	Boron and BF <sub>2</sub> , 10 <sup>14</sup> to 5·10 <sup>16</sup> cm <sup>-2</sup> , 10 to 150 keV energy 7 °tilt
Strip screening oxide	all
Inert N <sub>2</sub> anneal	Epitaxial: 700 to 1150°C Ion-implanted: 900 to 1150°C for 15 to 180 min (15 min step)

TABLE II

Lookup Table for  $\beta_1^*$  and  $\beta_2^*$  (in micrometers) With Boron Implantation. The First Number Given Is for a Typical Process With 1500-Å Wet Isolation Oxide With N<sub>2</sub> Annealing, While Values in Parentheses Are for Inert (N<sub>2</sub>) Annealing Alone. The Wet Isolation Oxide Was Grown at the Indicated Process Temperature for 66-, 15-, and 5-min Oxidation Time for 900 °C, 1000 °C, and 1100 °C, Respectively, and the Wafer Is Then Annealed at the Same Process Temperature for the Time Indicated in the Table.  $\beta^*$  of Piezoresistive Device Is Calculated Using (17). For Example,  $\beta^*$  of 10- $\mu$ m-Thick Device With  $2 \cdot 10^{15} \text{ cm}^{-2}$  Implantation Dose at 50 keV and a 30-min N<sub>2</sub> Anneal At 1000 °C Is  $0.53$  From  $\beta^* = \beta_1^* - \beta_2^*/0.5t_c = 0.55 - 0.13/5$

Implantation Dose (cm <sup>-2</sup> )	Implantation Energy (keV)	Annealing Temp (°C)	Annealing Time (min)																				
			15	30	45	60	75	90	105	120													
30	900	.84(.74)	.19(.09)	.84(.73)	.19(.09)	.84(.72)	.19(.09)	.84(.72)	.19(.09)	.84(.72)	.19(.09)	.84(.73)	.19(.09)	.84(.73)	.19(.09)	.84(.73)	.19(.09)	.84(.73)	.19(.09)	.84(.73)	.19(.09)		
	1000	.86(.72)	.26(.09)	.86(.74)	.26(.11)	.86(.74)	.27(.12)	.86(.75)	.27(.13)	.86(.75)	.27(.14)	.86(.75)	.27(.14)	.86(.75)	.27(.14)	.86(.76)	.28(.15)	.87(.76)	.28(.16)	.87(.77)	.29(.16)	.87(.77)	.29(.16)
	1100	.88(.77)	.43(.17)	.88(.79)	.45(.22)	.89(.80)	.47(.27)	.89(.81)	.49(.31)	.89(.82)	.51(.34)	.89(.82)	.53(.37)	.89(.83)	.55(.40)	.89(.83)	.55(.40)	.89(.83)	.55(.40)	.89(.83)	.55(.40)	.89(.83)	.57(.43)
50	900	.82(.76)	.22(.14)	.82(.75)	.22(.13)	.82(.74)	.22(.13)	.82(.75)	.22(.13)	.82(.75)	.22(.13)	.82(.75)	.22(.13)	.82(.75)	.22(.14)	.82(.75)	.22(.14)	.82(.75)	.22(.14)	.82(.75)	.22(.14)	.82(.75)	.22(.14)
	1000	.84(.74)	.28(.13)	.85(.75)	.28(.14)	.85(.76)	.29(.15)	.85(.76)	.30(.17)	.85(.77)	.30(.17)	.85(.77)	.30(.17)	.85(.77)	.30(.17)	.85(.77)	.31(.18)	.85(.77)	.31(.18)	.85(.77)	.31(.18)	.85(.77)	.31(.19)
	1100	.87(.77)	.44(.19)	.87(.79)	.47(.24)	.87(.80)	.49(.28)	.88(.81)	.51(.32)	.88(.82)	.53(.35)	.88(.82)	.55(.38)	.88(.82)	.57(.41)	.88(.83)	.59(.44)	.88(.83)	.59(.44)	.88(.83)	.59(.44)	.88(.83)	.59(.44)
100	900	.81(.78)	.29(.23)	.81(.78)	.29(.23)	.81(.78)	.29(.23)	.81(.78)	.29(.23)	.81(.78)	.29(.23)	.81(.78)	.29(.23)	.81(.78)	.29(.23)	.81(.78)	.29(.23)	.81(.78)	.29(.23)	.81(.78)	.29(.23)	.81(.78)	.29(.23)
	1000	.83(.77)	.34(.22)	.83(.77)	.34(.23)	.83(.78)	.35(.23)	.84(.78)	.35(.24)	.84(.78)	.36(.24)	.84(.79)	.36(.25)	.84(.79)	.36(.25)	.84(.79)	.36(.25)	.84(.79)	.36(.25)	.84(.79)	.36(.25)	.84(.79)	.37(.26)
	1100	.86(.79)	.49(.26)	.86(.80)	.51(.30)	.86(.81)	.53(.34)	.86(.82)	.55(.37)	.87(.82)	.57(.40)	.87(.83)	.59(.43)	.87(.83)	.61(.45)	.87(.83)	.61(.45)	.87(.83)	.61(.45)	.87(.83)	.61(.45)	.87(.83)	.62(.48)
30	900	.69(.56)	.17(.08)	.69(.53)	.17(.07)	.69(.52)	.18(.07)	.69(.52)	.18(.08)	.69(.52)	.18(.08)	.69(.52)	.18(.08)	.69(.52)	.18(.08)	.69(.52)	.18(.08)	.69(.52)	.18(.08)	.69(.52)	.18(.08)	.69(.52)	.18(.09)
	1000	.70(.53)	.25(.10)	.70(.55)	.26(.12)	.70(.57)	.27(.15)	.70(.58)	.27(.16)	.70(.58)	.28(.18)	.71(.59)	.28(.19)	.71(.60)	.29(.20)	.71(.60)	.29(.20)	.71(.60)	.29(.20)	.71(.60)	.29(.20)	.71(.60)	.29(.21)
	1100	.73(.59)	.45(.19)	.74(.62)	.48(.25)	.74(.63)	.51(.30)	.75(.64)	.53(.34)	.75(.65)	.55(.38)	.75(.66)	.57(.41)	.75(.67)	.59(.44)	.76(.67)	.59(.44)	.76(.67)	.59(.44)	.76(.67)	.59(.44)	.76(.67)	.61(.47)
50	900	.64(.57)	.18(.11)	.64(.53)	.18(.10)	.64(.52)	.18(.10)	.65(.52)	.18(.10)	.65(.52)	.18(.10)	.65(.52)	.18(.10)	.65(.52)	.18(.10)	.65(.52)	.18(.10)	.65(.52)	.18(.10)	.65(.52)	.18(.10)	.65(.52)	.18(.10)
	1000	.68(.53)	.26(.11)	.68(.55)	.27(.13)	.69(.57)	.27(.15)	.69(.57)	.28(.17)	.69(.58)	.29(.18)	.69(.59)	.29(.20)	.69(.59)	.30(.21)	.69(.60)	.30(.21)	.69(.60)	.30(.21)	.69(.60)	.30(.21)	.69(.60)	.30(.22)
	1100	.72(.59)	.44(.20)	.72(.61)	.46(.26)	.72(.63)	.49(.31)	.73(.64)	.51(.35)	.73(.65)	.53(.38)	.73(.66)	.55(.42)	.74(.66)	.57(.45)	.74(.67)	.59(.44)	.74(.67)	.59(.44)	.74(.67)	.59(.44)	.74(.67)	.59(.47)
100	900	.63(.60)	.24(.19)	.63(.57)	.24(.18)	.63(.56)	.24(.17)	.63(.56)	.24(.17)	.63(.56)	.24(.17)	.63(.56)	.24(.18)	.63(.56)	.24(.18)	.63(.56)	.24(.18)	.63(.56)	.24(.18)	.63(.56)	.24(.18)	.63(.56)	.24(.18)
	1000	.67(.57)	.31(.17)	.67(.58)	.32(.19)	.67(.59)	.33(.21)	.68(.60)	.33(.22)	.68(.60)	.33(.22)	.68(.60)	.34(.23)	.68(.60)	.34(.24)	.68(.60)	.34(.24)	.68(.60)	.34(.24)	.68(.60)	.34(.24)	.68(.60)	.35(.25)
	1100	.70(.60)	.46(.23)	.71(.62)	.49(.29)	.71(.63)	.51(.33)	.71(.64)	.54(.37)	.72(.65)	.56(.40)	.72(.66)	.58(.43)	.72(.66)	.60(.46)	.72(.67)	.60(.46)	.72(.67)	.60(.46)	.72(.67)	.60(.46)	.72(.67)	.62(.49)
900	.55(.55)	.14(.11)	.55(.52)	.14(.10)	.55(.51)	.15(.10)	.55(.51)	.15(.11)	.55(.51)	.15(.11)	.55(.51)	.15(.11)	.55(.51)	.15(.11)	.55(.51)	.15(.11)	.55(.51)	.15(.11)	.55(.51)	.15(.11)	.55(.51)	.15(.11)	

