

Planck 2015 results

VI. LFI mapmaking

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ABSTRACT

This paper describes the mapmaking procedure applied to *Planck* Low Frequency Instrument (LFI) data. The mapmaking step takes as input the calibrated timelines and pointing information. The main products are sky maps of I , Q , and U Stokes components. For the first time, we present polarization maps at LFI frequencies. The mapmaking algorithm is based on a destriping technique, which is enhanced with a noise prior. The Galactic region is masked to reduce errors arising from bandpass mismatch and high signal gradients. We apply horn-uniform radiometer weights to reduce the effects of beam-shape mismatch. The algorithm is the same as used for the 2013 release, apart from small changes in parameter settings. We validate the procedure through simulations. Special emphasis is put on the control of systematics, which is particularly important for accurate polarization analysis. We also produce low-resolution versions of the maps and corresponding noise covariance matrices. These serve as input in later analysis steps and parameter estimation. The noise covariance matrices are validated through noise Monte Carlo simulations. The residual noise in the map products is characterized through analysis of half-ring maps, noise covariance matrices, and simulations.

Key words. cosmic background radiation – methods: data analysis

1. Introduction

This paper is one of a set associated with the 2015 release of data from the *Planck*¹ mission (Planck Collaboration I 2014). It

describes the mapmaking procedure applied to time-ordered data from the *Planck* Low Frequency Instrument (LFI). Mapmaking is the next step in the LFI pipeline after calibration and dipole removal. It is followed by bandpass correction and component

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separation. A description of the complete data analysis pipeline is given in Planck Collaboration II (2016).

The mapmaking procedure applied to 2013 data was discussed in Planck Collaboration II (2014). In this work we present a thorough validation on the procedure and focus on the control of systematics (Planck Collaboration III 2016). For the first time we present polarization results. The mapmaking approach adopted for HFI is described in Planck Collaboration VIII (2016).

As its input mapmaking takes the calibrated timelines, from which the cosmological and orbital dipole signals have been removed. Also, an estimate for the Galactic straylight is subtracted from the timelines prior to mapmaking, since this is difficult to correct for at map level. Calibration and removal of stray light are described in Planck Collaboration V (2016).

In addition to data in the form of time-ordered information (TOI), required inputs are the radiometer pointing and orientation (θ, ϕ, ψ) for each sample, information on the polarization sensitivity of each radiometer, and the noise description. Output consists of sky maps of temperature and Stokes Q and U polarization, and a description of residual noise in them. Effects of beam shape are not corrected for at the mapmaking level. The LFI beams and the associated window functions are described in Planck Collaboration IV (2016).

The time-ordered data are contaminated by correlated $1/f$ noise. The aim of the mapmaking step is to remove the correlated noise as accurately as possible, while simultaneously minimizing systematic errors. Various mapmaking algorithms in the context of *Planck* are compared in Poutanen et al. (2006) and Ashdown et al. (2007a,b, 2009).

The mapmaking step is computationally challenging because of the huge amount of data. For optimal removal of noise, all of the time-ordered data for one channel must be held in computer memory at the same time. This leads to a large memory requirement (of the order of 1 TB for 70 GHz). The size of the output map is much less (of the order of 100 MB per map). Mapmaking is thus also a data compression step.

Providing a statistical description of the residual noise present in the maps, in the form of pixel-pixel noise covariance matrices, is part of the mapmaking process. Covariance matrices are used in a number of different places in the data-analysis pipeline. These matrices are impossible to employ at the native map resolution because of resource limitations. At present, the low-resolution products can only be used efficiently at HEALPix resolution $N_{\text{side}} = 16$ (corresponding to approximately 3.7° pixels) or lower. Consequently, we also produce corresponding low-resolution maps from the high-resolution maps.

This paper is organized as follows. In Sect. 2 we provide an overview of the mapmaking procedure, with emphasis on the control of systematics. Validation of the procedure with simulations is presented in Sect. 3. Production of low-resolution maps and related noise covariance matrices are discussed in Sect. 4. In Sect. 5 we give an overview of the mapmaking products and characterize the residual noise in them. A summary and conclusions are given in Sect. 6.

2. Mapmaking procedure

2.1. Madam

LFI maps were produced by the Madam mapmaking code, version number 3.7.4. The algorithm is based on the destriping technique, enhanced with a noise prior. The destriping technique as a tool for mapmaking is discussed in Maino et al. (2002),

Keihänen et al. (2004), Kurki-Suonio et al. (2009). A noise prior allows us to extend the destriping technique to very short baseline lengths, allowing more accurate noise removal. The Madam algorithm is described in Keihänen et al. (2005) and Keihänen et al. (2010). The code is the same as used for the 2013 release, but the parameter settings have been altered. The 2013 mapmaking procedure was discussed in Planck Collaboration II (2014). Here we give an overview of the method for convenience. We focus on changes made after the 2013 release, and on aspects relating to polarization.

Consider a time-ordered data stream

$$\mathbf{y} = \mathbf{s} + \mathbf{n}', \quad (1)$$

where \mathbf{s} represents the sky signal and \mathbf{n}' is noise. In the destriping technique, the correlated noise component is modelled by a sequence of offsets, here called baselines. The same offset applies for N adjacent samples in time-ordered-data. In the conventional language N is referred to as the “baseline length,” while “baseline” alone refers to the value of the offset.

The baselines are assumed to be the result of a random process. On top of the correlated noise, pure white noise with known variance is assumed. Formally we can write

$$\mathbf{n}' = \mathbf{F}\mathbf{a} + \mathbf{n}. \quad (2)$$

Vector \mathbf{a} represents the baselines and \mathbf{F} is formally a matrix that spreads the baselines into the time-ordered data. Vector \mathbf{n} represents the white noise component. The noise model ignores correlated noise at frequencies that exceed the inverse of the baseline length. The technique is suitable for $1/f$ -type noise that dies out at high frequencies. The baseline length should be chosen to be short enough to capture all frequencies below or comparable to the knee frequency of the $1/f$ spectrum.

It is important to appreciate that the baselines are expressly fitted in a subspace that has the sky-synchronous degrees of freedom projected out. This reduces the signal-to-noise ratio, but ensures that destriping does not affect the signal. In other words, the baselines are effectively used to model the noise and are not simply a filter applied to the raw timelines, which would obviously remove cosmic microwave background (CMB) structure for the short baselines that we adopt.

The signal component is modelled as

$$\mathbf{s} = \mathbf{P}\mathbf{m}, \quad (3)$$

where \mathbf{m} is a pixelized sky map, and \mathbf{P} is a pointing matrix. Map \mathbf{m} consists of three components, representing temperature and Q and U polarization. We can thus write for sample i

$$s_i = T(p_i) + Q(p_i) \cos(2\psi_i) + U(p_i) \sin(2\psi_i). \quad (4)$$

Here p_i is the pixel hit by sample i , and ψ_i is the rotation angle between the local longitude and the vector that defines the direction of polarization sensitivity of the beam.

Each sample is assigned entirely to the pixel in which the beam centre falls. Beam shape is not taken into account in this context. We are also ignoring cross-polarization, which for LFI is considered negligible (Planck Collaboration III 2016). Formally then, \mathbf{P} is a sparse matrix with three non-zero elements in each row. The factors $\cos(2\psi_i)$ and $\sin(2\psi_i)$ are included in \mathbf{P} . Limitations of the model and their impact on mapmaking are discussed in Sect. 2.3.

In the conventional destriping technique no prior information on the baselines is used. On the other hand, if the noise spectrum is known, one can construct a “noise prior”

$$\mathbf{C}_a = \langle \mathbf{a}\mathbf{a}^T \rangle. \quad (5)$$

Table 1. Frequency-specific mapmaking parameters and related information.

Channel	f_{samp} [Hz]	f_{kn} [Hz]	Baseline length		$FWHM$ [arcmin]	Resolution	
			Time [s]	samples		N_{side}	Size [arcmin]
30 GHz	32.508	0.043–0.175	0.246	8	33.0–33.2	1024	3.44
44 GHz	46.545	0.020–0.088	0.988	46	23.0–30.8	1024	3.44
70 GHz	78.769	0.006–0.059	1.000	79	12.8–13.5	1024/2048	3.44/1.72

Notes. From left: sampling frequency; knee frequency range; and chosen baseline length in seconds and as a number of samples. The three rightmost columns show the FWHM range of the main beams of the radiometers of the channel, the chosen destriping resolution as the N_{side} parameter of HEALPix, and the average size of one pixel.

The noise prior provides the extra constraint that allows us to extend the destriping technique to very short baselines. We construct the noise prior from the known noise parameters (knee frequency, white noise variance, and spectral slope), as described in Keihänen et al. (2010). It can be shown that the destriping solution gives the maximum-likelihood map in the limiting case where the baseline length approaches one sample (Keihänen et al. 2005).

With the assumptions listed above, the baseline vector \mathbf{a} can be solved from the linear system of equations

$$(\mathbf{F}^T \mathbf{C}_w^{-1} \mathbf{Z} \mathbf{F} + \mathbf{C}_a^{-1}) \hat{\mathbf{a}} = \mathbf{F}^T \mathbf{C}_w^{-1} \mathbf{Z} \mathbf{y}, \quad (6)$$

where

$$\mathbf{Z} = \mathbf{I} - \mathbf{P}(\mathbf{P}^T \mathbf{C}_w^{-1} \mathbf{P})^{-1} \mathbf{P}^T \mathbf{C}_w^{-1}. \quad (7)$$

Here \mathbf{C}_w is the white noise covariance, formally a diagonal matrix with the white noise variance on the diagonal. The final destriped map is then constructed as

$$\hat{\mathbf{m}} = (\mathbf{P}^T \mathbf{C}_w^{-1} \mathbf{P})^{-1} \mathbf{P}^T \mathbf{C}_w^{-1} (\mathbf{y} - \mathbf{F} \hat{\mathbf{a}}), \quad (8)$$

where $\hat{\mathbf{a}}$ is the baseline solution from (6). We use the hat symbol to indicate that $\hat{\mathbf{a}}$ and $\hat{\mathbf{m}}$ are estimates for the true \mathbf{a} and \mathbf{m} . The “binned map” is constructed from the timeline the same way without baseline removal:

$$\mathbf{m}_b = (\mathbf{P}^T \mathbf{C}_w^{-1} \mathbf{P})^{-1} \mathbf{P}^T \mathbf{C}_w^{-1} \mathbf{y}. \quad (9)$$

We include the same set of radiometers and the same time range in destriping phase and in map-binning phase. In this respect our approach is different from the one adopted for HFI (Planck Collaboration VIII 2016). Our approach has the benefit that single-year or single-survey maps, or maps constructed from different radiometer sets, have independent noise contributions. The price to pay is that the baseline solution in the partial maps is less accurate than in the full survey maps.

Adding a uniform offset to the time-ordered data does not have an impact on the baseline solution. This can be seen by inserting a unit vector $\mathbf{y} = \mathbf{1}$ to the right-hand side of Eq. (6). A unit vector can be expressed as $\mathbf{1} = \mathbf{P} \mathbf{m}_1$, where \mathbf{m}_1 is an (I, Q, U) map with temperature component equal to unity and with vanishing polarization. The operation $\mathbf{Z} \mathbf{P} \mathbf{m}_1$ yields zero, and consequently gives a zero baseline solution. Based on similar arguments, destriping cannot determine the absolute monopole of the temperature map, since this is indistinguishable from an offset in the timeline.

We do not impose an explicit constraint on the sequence of baselines, to avoid the degeneracy between the monopole of the maps and an offset in TOI. Instead, we make use of the fact that the conjugate gradient iteration method works for singular

systems as well, under the condition that the same eigenmodes vanish on both sides of the equation. The raw output temperature map has in general an arbitrary non-zero mean that depends on the input signal and noise in a non-trivial way. A monopole is therefore subtracted from each released temperature map in post-processing, as described in Planck Collaboration II (2016).

Similar arguments do not apply to an offset difference between radiometers of the same horn. In contrast to a common offset, a differential offset cannot be presented as a map, because it does not obey the rotation properties of the Q, U maps. A differential offset is removed by the destriping procedure, and does not leak into polarization, as long as there are enough crossing points where the same detector scans the same pixel in different orientations.

The destriping technique produces the final map through a procedure in which one first solves for the baselines, and then bins the map from the data stream from which the baselines have been removed. This two-step procedure has a benefit over direct maximum-likelihood methods, because it enables us to use techniques to make the map diverge from the maximum-likelihood solution and thus have a better control of systematics. For instance, one can apply a mask in the destriping phase while still binning the final map to cover the whole sky, in order to reduce signal error due to strong signal gradients. We discuss this in more detail in Sect. 2.3.

2.1.1. Baseline length and resolution

The baseline length is a key parameter in the Madam mapmaking algorithm. The chosen baseline length is a trade-off between computational burden and optimal noise removal. We have selected baselines that are well below the timescale given by the knee frequencies of each channel. In the case of 44 GHz and 70 GHz we have chosen to use one second long baselines. For 30 GHz, where the knee frequencies are higher, we have used shorter baselines of 0.25 s. This is different from the 2013 release, where we used one second baselines for all channels. With these choices, the baseline length is always less than a tenth of the scale given by the inverse knee frequency, the worst case being for LFI–24S, where $\text{baseline} \times f_{\text{knee}} = 0.087$. The exact baseline lengths and channel sampling frequencies are given in Table 1. The LFI knee frequencies are given in Table 2 along with other noise parameters.

Madam maps follow the HEALPix² pixelization scheme, where map resolution is defined by the parameter N_{side} . The total number of pixels in a map is $12N_{\text{side}}^2$ (Górski et al. 2005). Map resolution was chosen according to the beam width. For the majority of maps we used resolution $N_{\text{side}} = 1024$ (3.4′). At

² <http://healpix.sourceforge.net>

Table 2. Noise parameters for LFI radiometers.

Radiometer	Knee frequency f_{knee} [mHz]		Slope β		White noise σ [mK]		Weight C_w^{-1} (norm.)		Horn-uniform
	M	S	M	S	M	S	M	S	M and S
70 GHz									
LFI-18 . .	14.82	17.78	-1.060	-1.180	4.553	4.146	0.0878	0.1059	0.0973
LFI-19 . .	11.72	13.71	-1.207	-1.111	5.144	4.926	0.0688	0.0750	0.0727
LFI-20 . .	7.96	5.67	-1.198	-1.298	5.212	5.507	0.0670	0.0600	0.0642
LFI-21 . .	37.89	13.27	-1.247	-1.205	4.003	4.971	0.1136	0.0737	0.0905
LFI-22 . .	9.68	14.80	-1.424	-1.237	4.356	4.715	0.0960	0.0819	0.0895
LFI-23 . .	29.65	59.03	-1.073	-1.211	4.476	4.790	0.0909	0.0794	0.0858
44 GHz									
LFI-24 . .	26.78	88.30	-0.942	-0.908	3.159	2.734	0.1415	0.1890	0.1640
LFI-25 . .	20.07	46.37	-0.845	-0.904	2.834	2.698	0.1759	0.1940	0.1869
LFI-26 . .	64.42	68.19	-0.918	-0.758	3.295	2.887	0.1301	0.1695	0.1491
30 GHz									
LFI-27 . .	174.53	108.79	-0.927	-0.907	1.605	1.729	0.2768	0.2385	0.2583
LFI-28 . .	130.08	43.08	-0.931	-0.900	1.812	1.633	0.2172	0.2674	0.2417

Notes. Values for f_{knee} , β , and σ given here were used for the construction of the noise prior. We give also radiometer weights for pure noise weighting and for the horn-uniform weighting scheme. Horn-uniform weighting was used for actual mapmaking.

this resolution, the average pixel size corresponds to 1/10 of the beam full width at half maximum (FWHM) at 30 GHz or 1/4 at 70 GHz. A subset of 70-GHz maps was remade with resolution $N_{\text{side}} = 2048$ (1.7'). All computations were carried out in the Galactic coordinate frame. Pixel sizes are compared with beam widths in Table 2.

2.1.2. Missing data

Periods of stable pointing are regularly interrupted by manoeuvring periods, where the telescope is repointed according to the scanning strategy. These repointing periods are discarded from mapmaking. In addition there are other data sections that must be discarded, for instance due to missing data, gain saturation, or crossing of a bright object (Planck Collaboration II 2016). We accomplish this by formally setting the white noise variance C_w to infinity for the flagged samples. The procedure is different from removing the flagged data sections and appending the remaining sections end-to-end. As a result, the flagged samples do not contribute to the output map, but the correct noise correlation is preserved across the gaps.

2.1.3. Single-survey maps and handling of missing pixels

The 2015 release includes polarization maps for individual surveys (6 months of data), which do not cover the whole sky. Obviously, pixels that are not observed at all are not included in the maps. In addition there are pixels that are scanned by a single horn. The polarization analysis of those pixels requires special attention. To reliably solve for the I , Q , and U components for a pixel, the pixel has to be scanned by two horns with orthogonal polarization sensitivity, or, alternatively, twice by same horn with sufficiently different orientations of the beam. If this is not the case, we discard the pixel from the map. Even these pixels, however, can be used for destriping as we now describe.

We assess the quality of a pixel through the matrix

$$P^T C_w^{-1} P. \quad (10)$$

This is a block-diagonal matrix with 3×3 blocks along the diagonal. Each 3×3 block corresponds to one pixel, and represents the inverse of the white noise covariance within the pixel. This matrix gives an accurate diagnosis of a pixel's usefulness for polarization analysis. Pixels with insufficient polarization coverage yield a singular or poorly conditioned matrix. The inverse of the pixel matrix appears in the destriping equations, Eqs. (6) and (7). It is obvious that a singular matrix leads to a non-stable solution for the map. However, in Eq. (6) the pixel matrix appears sandwiched between two occurrences of the same pointing matrix, which lack the same eigenmodes. Matrix Z is thus finite, even if the pixel matrix is singular. This can also be seen from the fact that Z is a projection matrix, which means that all its eigenvalues are 1 or 0.

If the pixel matrix is singular, but not identically zero, we invert the non-singular eigenmodes. That way we can also utilize pixels that have been observed by a single horn. However, in the final map-binning phase we cannot use this same procedure. Instead, the badly determined pixels are excluded. We use as rejection criterion the reciprocal condition "rcond" value of the pixel matrix. For the 2015 release we chose the strict limit $\text{rcond} > 0.01$. Statistics on the sky coverage of LFI maps are provided in Sect. 5.

2.1.4. Single-horn and single-radiometer maps

In order to decompose the signal into I , Q , and U components, it is necessary to have at least three measurements from the same pixel, at different polarization angles. In a limited region around the ecliptic poles it is possible to determine the polarization signal from each individual LFI horn, since the region is scanned in different angles by the same radiometer pair, but for most of the sky we need observations from two horns (four radiometers).

We have produced temperature maps from each horn's or radiometer's data. The same formulation as above applies, but the pointing matrix P only contains the temperature column. Consequently, the matrix in Eq. (10) becomes diagonal and is trivial to invert.

In the case of horn maps, the polarization signal largely cancels out when the two radiometers are averaged, and the map gives a reliable estimate of the temperature signal. The single-radiometer maps, instead, are a mixture of temperature and polarization signals, which must be kept in mind when analysing these maps.

2.2. Noise prior

We use a prior C_a^{-1} for the noise baselines to constrain the destriping solution. Matrix C_a gives the expected correlation between noise baselines, as in Eq. (5). The details of the computation from a given input spectrum are given in Keihänen et al. (2010). The prior makes it possible to use very short baselines, and thus to model the noise accurately.

We construct the prior from the noise parameters (σ, f_{kn}, β) , which are listed in Table 2. The noise spectrum is given by

$$P(f) = \frac{\sigma^2}{f_{\text{samp}}} \left(\frac{f}{f_{\text{kn}}} \right)^\beta, \quad (11)$$

where f_{samp} is the sampling frequency (see Table 1). Below a cut-off frequency $f_{\text{min}} = 1/(3600 \text{ s})$, the spectrum is assigned a constant value $P(f_{\text{min}})$, to avoid numerical problems related to the divergence at $f = 0$.

On top of the correlated noise component there is assumed to be pure white noise with a flat spectrum

$$P_{\text{wn}}(f) = \frac{\sigma^2}{f_{\text{samp}}}. \quad (12)$$

The noise prior is based on the correlated component of Eq. (11) only, since this is the component modelled by the baselines.

We assume that the noise properties do not change significantly with time, and apply the same prior throughout the mission. We also assume that noise is uncorrelated between radiometers, and from one pointing period to another. The latter is justified by the fact that the manoeuvre periods are flagged, effectively separating pointing periods from each other (Planck Collaboration II 2016). Under these assumptions the correlation matrix C_a has a simple form and can be applied efficiently using Fourier techniques.

2.3. Handling of systematic effects

Signal variations that are not captured by the signal model (Eq. (3)) give rise to additional uncertainty in baseline determination, referred to as “signal error.” There are three main sources for signal error: signal variations within a pixel; differences in radiometer frequency response (bandpass mismatch, Leahy et al. 2010); and beam-shape mismatch. Cross-polarization in this context can be understood as part of beam mismatch.

Other sources include variable sources and gain estimation error from the preceding calibration step. All these have the effect that the same sky pixel, when observed by different radiometers or in different orientation of the beam, or just with the beam centre in slightly different position, yields different signals. Madam interprets this as additional noise and fits baselines to it.

Note that a symmetric beam component, with equal width at all radiometers that participate in the mapmaking process, does not give rise to signal error, since it does not create inconsistencies between the measurements. Instead, the beam smoothing is just interpreted as a property of the sky, and can be corrected for in a power spectrum analysis by applying an appropriate beam window function.

The same error sources also cause leakage from the temperature signal into the weaker polarization maps. The relative importance of such systematic effects, and their effect on LFI maps, is discussed in Planck Collaboration III (2016).

The effects of beam-shape mismatch and cross-polarization are not taken into account in the mapmaking step, but they are handled in the later data processing steps through application of a beam window function (Planck Collaboration IV 2016).

Ideally, optimal noise removal is achieved by destriping the data according to the maximum-likelihood solution of Eqs. (6) and (7), with C_w equal to the actual white noise covariance, and using all available data. However, this does not take the systematic effects into account, which are particularly important for accurate polarization analysis.

The two-step nature of the destriping procedure enables us to diverge from the ML solution to reduce systematics, at the cost of slightly increased residual noise. Residual noise is easier to account for, and is thus less harmful in subsequent analysis, than systematic effects. In the following sections we describe procedures we have adopted to reduce such systematic effects.

2.3.1. Destriping resolution

Signal error arising from high signal gradients, and consequent variations inside a pixel, can be reduced with an increased destriping resolution. This leads to slightly higher residual noise, since there are more unknowns to be solved for in the same amount of data.

The destriping resolution can be chosen independently from the final map resolution. In high-resolution mapmaking we have used the same resolution, $N_{\text{side}} = 1024$ (corresponding to 3.4' pixel size) or $N_{\text{side}} = 2048$ (1.7'), both for destriping and for map binning. The choice of resolution plays a more important role in the construction of low-resolution maps (Sect. 4).

2.3.2. Destriping mask

Signal error originates mostly in the Galactic plane where signal gradients as well as bandpass effects are largest. We can greatly reduce the signal error by applying a Galactic mask in the destriping phase. This is done by formally setting the white noise covariance to infinity for the samples under the mask, thus ensuring consistent treatment throughout. All samples are again included when binning the final map. Using a mask leaves fewer crossing points between scanning rings to be used for baseline determination. The residual noise is therefore expected to increase slightly.

The choice of the destriping mask is a trade-off between minimization of signal error and keeping enough data for accurate destriping. We use the same masks that were used in Planck Collaboration V (2016). The masks are illustrated in Fig. 1. The effect of masking in the destriping phase on the signal error is illustrated in Fig. 2.

2.3.3. Radiometer weighting

Individual radiometers are weighted according to C_w when data from different radiometers are combined into one map, according to Eqs. ((6)–(8)). In the maximum-likelihood solution C_w equals the white noise variance of the time-ordered data. We call this “noise weighting.”

Instead of noise weighting, we can also adopt “horn-uniform weighting,” with the purpose of reducing leakage from

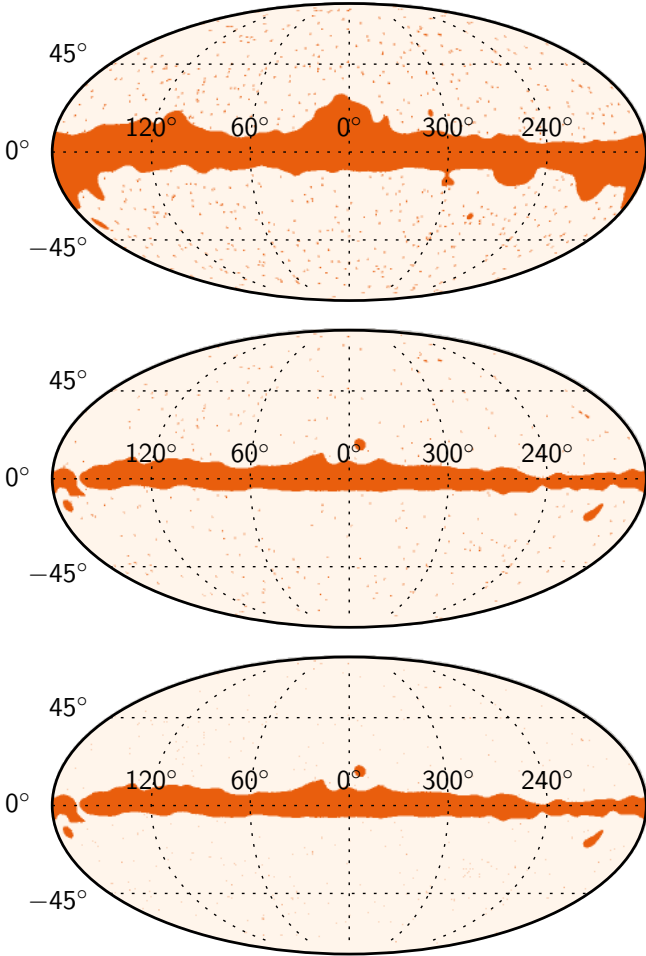


Fig. 1. Destriping masks for 30 GHz (*top*), 44 GHz (*middle*), and 70 GHz (*bottom*).

temperature to polarization. We replace the white noise covariance C_w for a radiometer by the average of the covariances of the two radiometers of a horn. The weights that go on the diagonal of C_w are constructed as

$$C_w^{-1} = \frac{2}{\sigma_M^2 + \sigma_S^2}, \quad (13)$$

where σ_M and σ_S are the white noise rms values for the two radiometers sharing a horn. The same weight is applied to both radiometers and we are neglecting variations in white noise level. C_w^{-1} can be regarded as a radiometer-specific weighting factor. The values of C_w^{-1} for both horn-uniform-weighting and pure noise weighting are given in Table 2. The numbers are based on the σ values listed in the same table. Since the same matrix C_w appears on both sides in the destriping equations, the units and overall normalization are irrelevant. The values given in the table have been normalized so that the weights of all radiometers of the frequency channel add up to 1.

At the same time we make the flags uniform, so that if a sample is flagged as unusable for one radiometer of the horn, we flag the corresponding sample for the other radiometer as well. This, together with the horn-uniform weighting, ensures that the polarization map is solved solely from the difference of the two timestreams. This has the advantage over noise weighting that

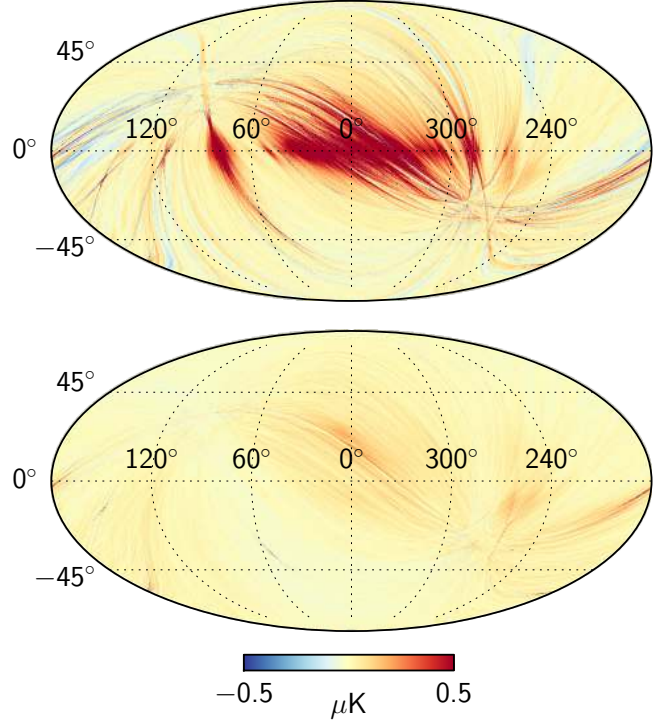


Fig. 2. Effect of the destriping mask on the 70-GHz signal error. We show the simulated signal error in temperature, without (*upper*) and with (*lower*) applying a Galactic mask. Signal error is computed as the difference between noiseless destriped and binned maps. The simulation procedure is described in Sect. 3.2.1.

any instrumental effects that are equal for both radiometers effectively cancel out. In particular this is expected to approximately apply to beam effects, since the beam shapes are similar for two radiometers sharing a horn (Planck Collaboration IV 2016). The cancellation is not perfect, however, even if the beam shapes are exactly the same, because the polarization angles of the two radiometers are not exactly orthogonal, and because the noise priors are different.

The effect of each of these procedures on signal error and on residual noise are assessed through simulations, which are described in Sect. 3

2.4. White noise covariance

When noise weighting is applied, C_w equals the actual white noise covariance, and the inverse of Eq. (10) directly gives the covariance of residual white noise in a pixel. The diagonal elements give the variance of the I , Q , U components, and the off-diagonal elements represent cross-correlations between the components.

The horn-uniform radiometer weighting complicates the picture. If C_n is the actual white noise variance in the time-ordered data, and C_w the one used for weighting, the residual white noise in the map domain is obtained as

$$C_{wn_map} = (P^T C_w^{-1} P)^{-1} P^T C_w^{-1} C_n C_w^{-1} P (P^T C_w^{-1} P)^{-1}. \quad (14)$$

We compute the white noise covariance (14) for every map produced, and provide it as auxiliary information. Obviously, this reduces to the inverse of the expression in Eq. (10) when $C_w = C_n$.

Equation (14) obtains its minimum for fixed C_n when $C_w = C_n$, and the minimum value is $(P^T C_n^{-1} P)^{-1}$. To see this, it is sufficient to notice that Eq. (14) represents the residual noise in the special case where the TOI contains only white noise with variance equal to C_n , and no destriping is applied. The variance is minimized by the maximum-likelihood solution, which in this case is $C_w = C_n$. For a general proof, see e.g., Natoli et al. (2001).

2.5. Half-ring maps

Half-ring maps are used for characterization of total residual noise. We split each pointing period in two, and use the first halves for the first half-ring map, and the second halves for the second half-ring map. Very long pointing periods are first split into sections of one hour at maximum. These are further split into two half-ring parts. We then construct maps from the two halves with the same procedure as for the full maps.

The two half-ring maps have nearly identical signal components, but independent noise contributions, apart from the lowest frequency components below the inverse of the pointing period length. We take the difference between the two maps to cancel the signal. A correction is applied to account for the small differences in the hit count distribution between the two halves. The “half-ring noise map” in a given pixel is constructed as

$$m_h = \frac{m_{h1} - m_{h2}}{w_h}, \quad (15)$$

where m_{h1} and m_{h2} are the two half-ring maps, and w_h is a weighting factor given by

$$w_h = \left[(n_{h1} + n_{h2}) \left(\frac{1}{n_{h1}} + \frac{1}{n_{h2}} \right) \right]^{1/2}. \quad (16)$$

Here n_{h1} and n_{h2} are the hit counts in the pixel under consideration. If the hit distributions are identical, this reduces to $w_h = 2$.

The half-ring noise map consists of noise with similar properties as the residual noise in the full maps, apart from the very longest time scales (over an hour) that are cancelled in the process. The noise map provides a valuable tool for the characterization of residual noise in the maps, since it is constructed from the same data as the maps themselves, and is independent of any noise model.

We expect a small error in the noise estimate based on the half-ring difference maps to come from the regions of strong temperature gradients. In these regions the signal can “leak” into the half-ring difference maps. We call this effect the “gradient leakage.” It is caused by the slightly uneven distribution of the hits within each pixel. Although in the single-survey half-ring maps these effects are visible by eye near the Galactic plane, their effect on the noise spectrum derived from the map is negligible, because they only affect a few pixels with the strongest signal gradients. In the full-mission maps the gradient leakage is further mitigated by the much larger hit count.

3. Validation of the mapmaking procedure

3.1. Simulations

We have performed a series of simulations to assess the effect of various parameter choices on map accuracy. Our goal here is not to build an error budget, but to justify the parameter choices taken in the mapmaking process. The impact of various systematic effects on the *Planck* data products is assessed in Planck Collaboration III (2016).

The simulations include noise with realistic noise parameters, and CMB+foregrounds with realistic beam shapes. In all cases we used realistic LFI radiometer pointings and flags, and constructed I , Q , U maps at HEALPix resolution $N_{\text{side}} = 1024$ (corresponding to $3.4'$).

3.1.1. Noise simulations

Madam includes an internal noise generator that we used for noise simulations. The internal generator has an advantage over external codes, because it avoids the step of writing the generated timeline on disk, thus reducing the computational cost of the simulation.

The code generates white and $1/f$ noise according to a given noise spectrum, inserts it in place of the time-ordered data, and processes it into a map in the same way as done for the actual data. The resulting map is the “residual noise map.”

The residual noise is dominated by white noise. It therefore makes sense to look at the correlated residual noise component in isolation. The residual noise map can be split into two independent components:

$$\mathbf{m}_n = \mathbf{m}_{\text{wn}} + \mathbf{m}_{\text{CRN}}. \quad (17)$$

Here \mathbf{m}_{wn} represents the binned white noise map, constructed as

$$\mathbf{m}_{\text{wn}} = (P^T C_w^{-1} P)^{-1} P^T C_w^{-1} \mathbf{y}_{\text{wn}}, \quad (18)$$

where \mathbf{y}_{wn} is the separately-generated white noise timeline. The binned white noise map does not depend on the destriping procedure, apart from the radiometer weighting.

We then find the “correlated residual noise” (CRN) map by subtracting \mathbf{m}_{wn} from the residual noise map. The CRN component includes the correlated noise residual that remains after destriping, and the error in baseline determination. It can be shown (Keihänen et al. 2010) that as long as the destriping resolution is equal to the map resolution (or exceeds it), the two components are statistically independent, i.e.,

$$\langle \mathbf{m}_{\text{wn}}^T \mathbf{m}_{\text{CRN}} \rangle = 0. \quad (19)$$

This makes the rms of the CRN map a convenient figure of merit. It shows the effects of changes in the mapmaking procedure more clearly than the full noise. The total residual noise rms is obtained as the quadrature sum of the CRN and white noise values.

In Monte Carlo simulations we generate the white noise timestream independently from the correlated $1/f$ noise timestream. This makes it possible to construct the binned white noise map and to subtract it from the total noise map to obtain the CRN map. With flight data this distinction is obviously not possible.

When generating noise we used a time-dependent noise model, where the time span of the mission was split into five sections, each of which had a different noise spectrum. At the time of constructing the simulations this was the most accurate model available. When destriping the data we used a single noise prior constructed from a constant set of noise parameters. This is equivalent to the procedure used for actual mapmaking. To reduce scatter, we generated 10 noise realizations for each combination of mapmaking parameters. The values shown are obtained as quadrature averages of the individual rms values.

3.1.2. Signal simulations

We performed signal simulations, where we generate time-ordered data starting from a sky model. We used as input the FFP7 sky model (Planck Collaboration XII 2016), which was the version available at the time of our simulations. Differences with respect to the release version FFP8 are small, and unlikely to affect the results. Each radiometer has its own input sky, integrated with the radiometer’s frequency response. We use the `convqt` and `multimod` tools of the `LevelS` package (Reinecke et al. 2006) to convolve the sky with the beam, and to scan a time-ordered data stream from the input sky according to the real radiometer pointing. We include the main and intermediate beam components, but not the far sidelobe component, since we assume that the latter is removed in the calibration process. We apply flags, and run the data through the mapmaking procedure.

The “signal error rms” is computed as the rms of the difference between destriped and binned signal maps constructed from the same data stream. It has become customary to call this quantity signal error, although its interpretation as pure error is questionable. For instance, destriping may remove some of the systematic polarization signal that arises from bandpass mismatch, but this shows up as an increased signal error. The difficulty here is that the binned map itself is subject to bandpass and beam mismatch, and there is not a unique “true” map with which we could compare the destriped maps. Signal error should rather be considered a measure of how much the destriping process modifies the signal, compared to naive binning.

Signal error rms is not a useful figure of merit when we consider the effect of radiometer weighting, because the chosen weighting scheme affects the binned map as well. To test this, we also performed another series of signal simulations where we included only unpolarized CMB in the input sky. All signal in the output polarization in these tests is thus leakage from temperature. Analysis of the output polarization maps gives information on how the chosen radiometer weighting scheme impacts the leakage.

3.2. Results

3.2.1. Baseline length and mask

In the first series of simulations we varied the baseline length and examined its effect on residual noise and signal error. The results are plotted in Figs. 3 and 4. We show the CRN and signal error rms for temperature and Q , U polarization. Because the amplitudes of residual noise and signal error are very different, we plot them in different panels. The total residual noise is a sum of the CRN component, the binned white noise component, and the signal error. Since the three components are independent, the square of total residual noise rms is obtained as a quadrature sum of the individual rms values. The rms values of the binned white noise component, again averaged over 10 noise realizations, are found in Table 3.

As expected, residual noise decreases with decreasing baseline width. The values used in actual mapmaking are indicated by circles in Figs. 3 and 4. The 0.25-s baseline length used at 30 GHz appears to be overkill, since the residual noise level changes only very little below 1 s ($0.2 \mu\text{K}$).

At 30 GHz and 70 GHz, Q and U have nearly identical noise levels. This is a consequence of the focal plane design. LFI horns are arranged in pairs that have their direction of polarization sensitivity at 45° angles to each other, so that when one horn is measuring Q , the other is measuring U , and both components

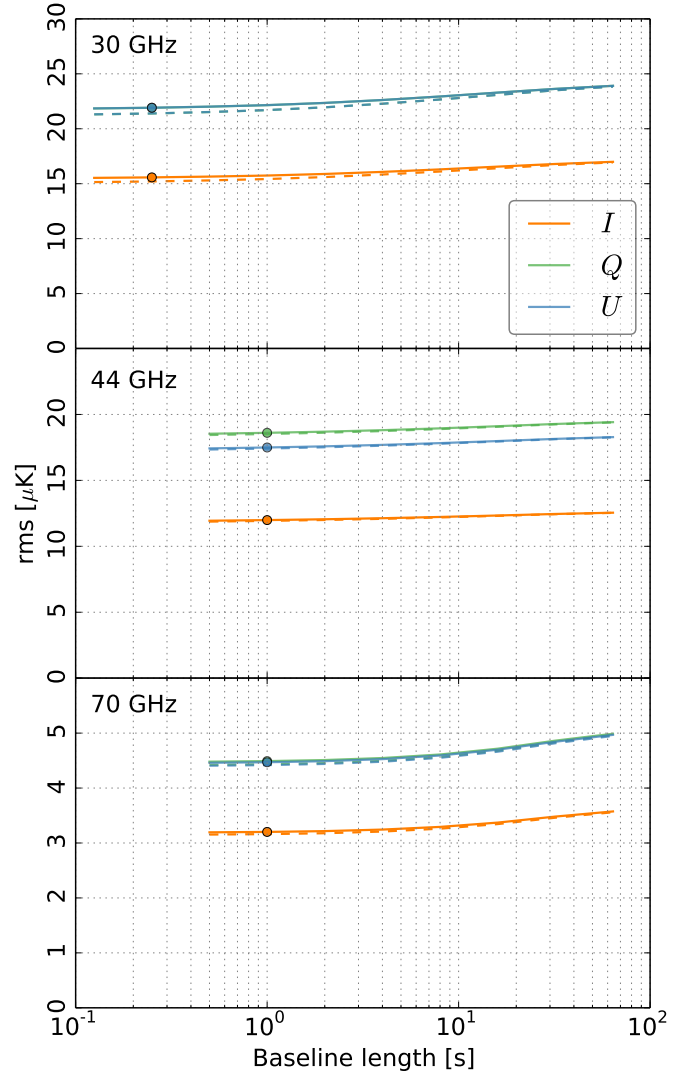


Fig. 3. Correlated residual noise (CRN) as a function of baseline length for all LFI frequencies. CRN is computed as the rms of the difference between the destriped map and the binned white noise map. We plot CRN for I (orange), Q (green), and U (blue) as a function of baseline length. Solid and dashed lines show the result with and without the destriping mask, respectively. The circles indicate the baseline value used in actual mapmaking.

are recovered with the same accuracy. An exception to this is the 44-GHz channel, where horn LFI-24 does not have a counterpart. This leads to a difference in noise levels between Q and U at 44 GHz.

The level of signal error is a result of the complicated interplay between destriping, phenomena causing signal error, and instrument design. Different phenomena dominate at different frequencies. Signal variations within a pixel and beam-shape mismatch contribute more strongly to the signal error in temperature than in polarization, because the beam patterns of two radiometers of a horn are similar, so that the effect partly cancels in polarization. The same does not apply to bandpass mismatch.

We ran the same series of simulations with and without the destriping mask. As discussed in Sect. 2.3, the mask is expected to reduce the signal error arising from high signal gradients. The masks used are depicted in Fig. 1. Figure 2 illustrates the effect of the destriping mask on signal error. We plot a map of signal error in 70-GHz temperature data, first without a destriping

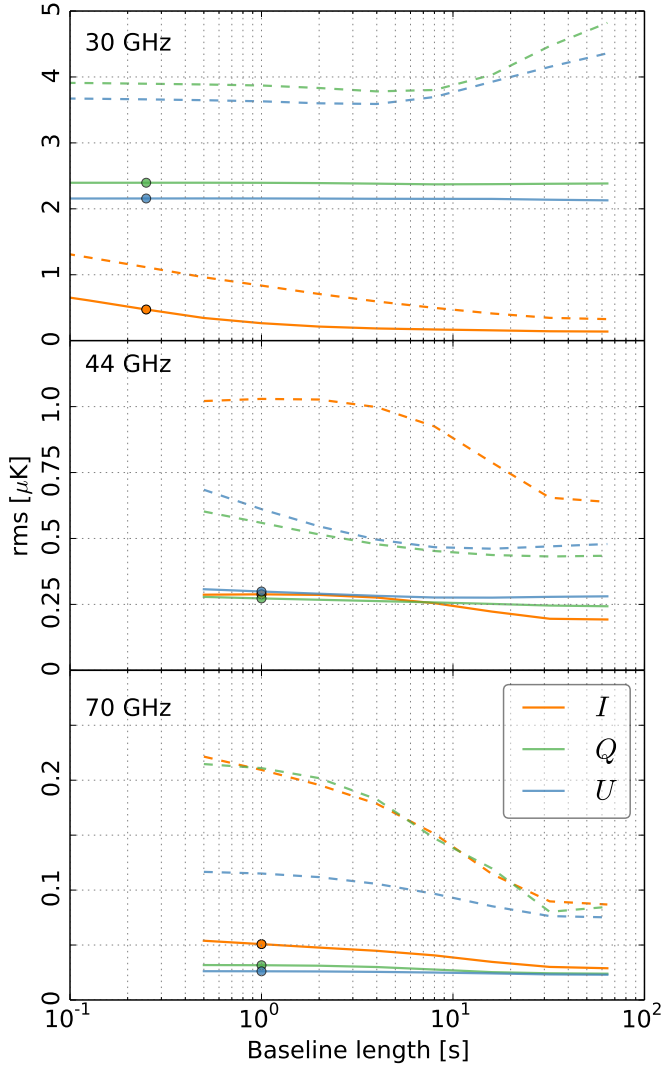


Fig. 4. Signal error as a function of baseline length for all LFI frequencies, for I (orange), Q (green), and U (blue). Signal error is computed as the rms of the difference between destriped and binned maps. Solid and dashed lines show the result with and without the destriping mask, respectively.

mask, and below it with the mask. The mask greatly reduces the error.

The mask has the effect of slightly increasing the residual noise, since there is less data to solve for the baselines; however, the effect is small, well below $1 \mu\text{K}$, as can be seen from Fig. 3. The effect is the opposite direction for signal error. The signal error increases towards shorter baselines. The overall level of the signal error is still well below that of the residual noise. The destriping mask has a dramatic effect on the signal error, decreasing it typically by a factor of 2.

We can conclude that our chosen baseline lengths are short enough for nearly optimal noise removal. At the same time the signal error is kept under control by the application of a mask.

3.2.2. Destriping resolution

In another series of simulations we varied the destriping resolution. The final maps were constructed at a fixed resolution $N_{\text{side}} = 1024$ ($3.4'$) in all cases. The baseline length was fixed to

Table 3. Impact of the detector weighting scheme on residual noise.

30 GHz	I		Q		U	
	NW	HUW	NW	HUW	NW	HUW
White	56.76	56.78	80.28	80.42	80.20	80.41
CRN	15.56	15.57	21.75	21.91	21.73	21.92
Full	58.85	58.87	83.17	83.34	83.09	83.32
44 GHz	I		Q		U	
	NW	HUW	NW	HUW	NW	HUW
White	65.42	65.81	99.88	100.44	93.80	94.37
CRN	12.52	11.99	19.36	18.61	18.28	17.49
Full	66.60	66.90	101.74	102.15	95.57	95.99
70 GHz	I		Q		U	
	NW	HUW	NW	HUW	NW	HUW
White	57.82	57.95	82.00	82.32	81.59	81.94
CRN	3.22	3.20	4.50	4.49	4.48	4.47
Full	57.91	58.04	82.12	82.44	81.71	82.06

Notes. We show the rms (in μK) of binned white noise (“white”), correlated residual noise (“CRN”), and their sum (“full”). All values are averages over 10 noise realizations. “NW” refers to noise weighting, and “HUW” to the horn-uniform weighting scheme. Noise weighting minimizes the total residual noise. In actual mapmaking we instead used horn-uniform weighting to reduce effects from beam-shape mismatch.

its nominal value, and a destriping mask was applied. The results are shown in Figs. 5 and 6.

Going to a higher resolution increases the residual noise slightly, since there are more unknowns to solve for using the same amount of data; however, the effect is again below $1 \mu\text{K}$. In signal error the effect is in the opposite direction. For the case of temperature maps, increasing the resolution reduces the signal error drastically, but the effect levels out near our chosen destriping resolution. In polarization, the effect is less dramatic.

The 30-GHz channel has the peculiar feature that the signal error is significantly higher in polarization than in temperature. It is also nearly completely insensitive to baseline length and destriping resolution. The insensitivity to baseline length suggests that the effect is coupled to a foreground component distributed over a large part of the sky. The likely explanation is leakage of synchrotron emission signal from temperature to polarization through bandpass mismatch. The steep spectrum of the synchrotron component exacerbates its sensitivity to bandpass mismatch. To verify this, we ran yet another series of simulations where we artificially turned off the bandpass mismatch by using the same input sky model for all radiometers at 30 GHz. The results are shown with dashed lines in the uppermost panel of Fig. 6. The signal error is greatly reduced, confirming that bandpass mismatch is the dominant factor in the signal error.

3.2.3. Horn-uniform weighting

The purpose of the horn-uniform weighting scheme is to reduce leakage from temperature to polarization through systematic effects that are correlated between radiometers sharing a horn. In particular this concerns leakage through beamshape mismatch.

Changing the detector weighting changes both the binned and destriped maps. Therefore CRN alone is no longer a suitable figure of merit, and we have to look at the total residual noise.

Results from noise simulations are presented in Table 3. For completeness we show also the CRN values. We compare the horn-uniform weighting scheme with weighting based on the

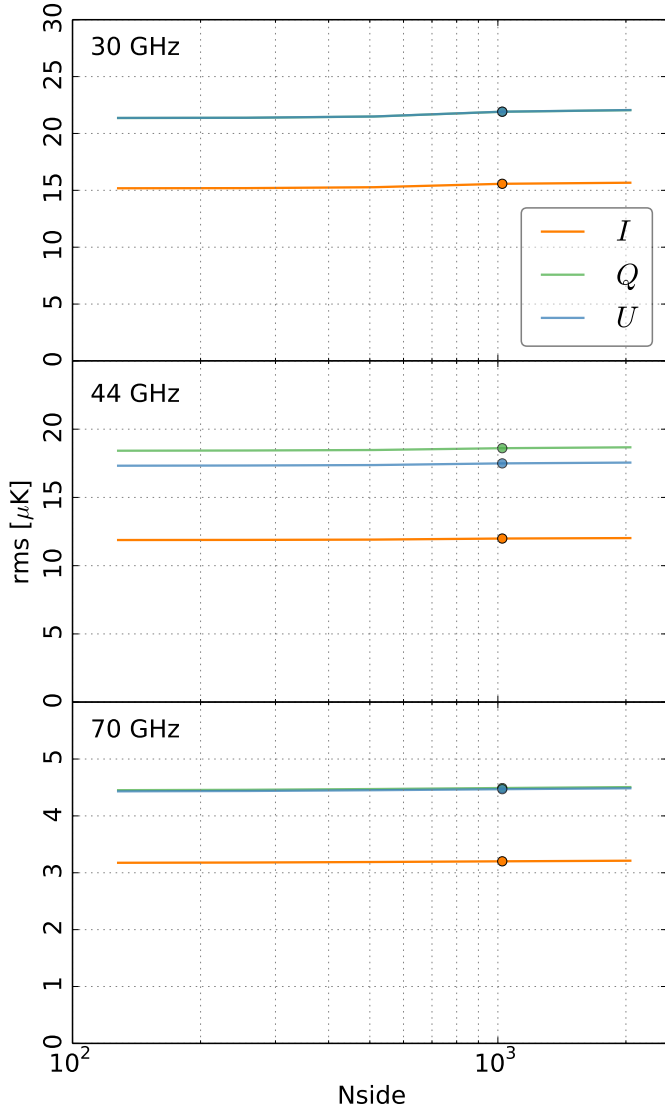


Fig. 5. Correlated residual noise (CRN) as a function of destriping resolution for all LFI frequencies. CRN is computed as the rms of the difference between the destriped map and the binned white noise map. We plot CRN for I (orange), Q (green), and U (blue) as a function of destriping resolution. The circles indicate the resolution ($N_{\text{side}} = 1024$) used in actual mapmaking.

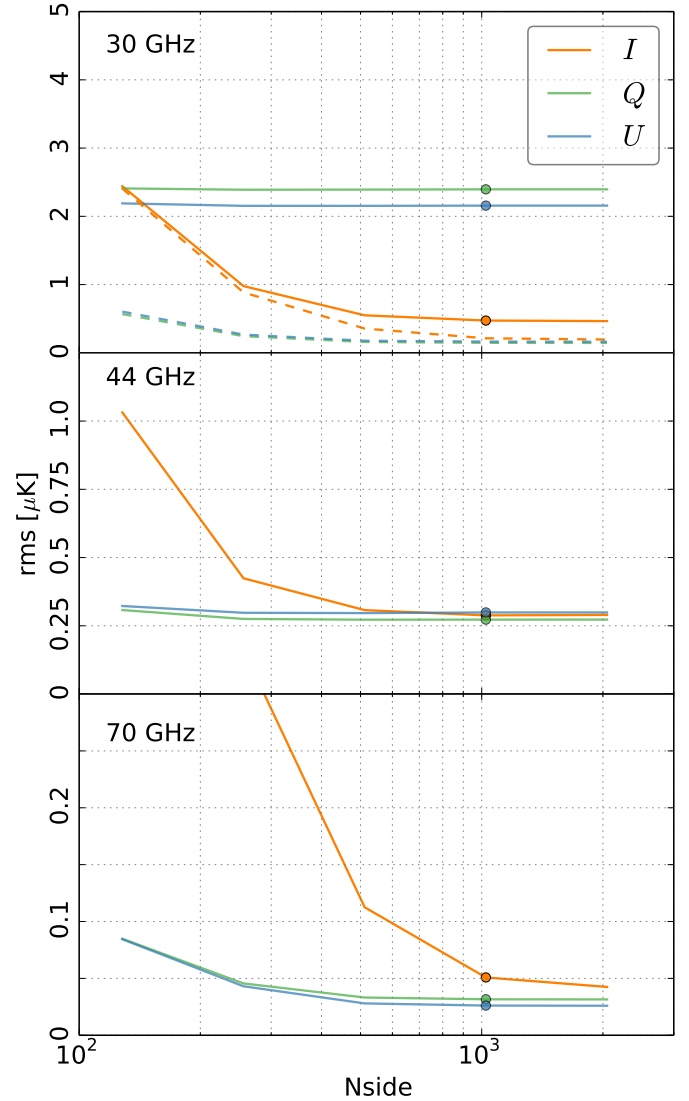


Fig. 6. Signal error as a function of destriping resolution for all LFI frequencies, for I (orange), Q (green), and U (blue). Signal error is computed as the rms of the difference between destriped and binned maps. The dashed lines in the 30-GHz case show results from a simulation without bandpass mismatch.

radiometer’s white noise level. The latter is expected to minimize the total residual noise. This is confirmed by our simulations. In all cases studied, the noise-weighting scheme yields a slightly smaller total noise residual than the horn-uniform weighting, but the differences are small. The white noise rms (see Table 2) typically vary by 10%, but this translates to a $<1\%$ effect in residual noise.

To study the effect of the radiometer weighting scheme on T -to- P leakage, we performed a series of signal simulations where we only include the CMB temperature anisotropies as inputs. The resulting Q/U maps consist purely of temperature leakage. Since foregrounds are not present, bandpass mismatch plays no role, so that beam-shape mismatch and non-idealities in pointing are the only sources of leakage. We use the rms of the Q and U polarization maps as a simple measure of error in these maps. The results are shown in Table 4.

We compare noise weighting and horn-uniform weighting in four simulations of increasing complexity. The first one is

an idealized simulation, where we have eliminated any non-idealities that could cause leakage from temperature to polarization. We use identical elliptic beams and the same pointing for both radiometers of a horn. The polarization responses (ψ_{pol} angle) are set at exactly 90° from each other, while they in reality differ from orthogonality by $\pm 0.5^\circ$ at maximum (Planck Collaboration IV 2016). With these assumptions, the horn-uniform weighting is expected to fully cancel the temperature leakage. This is confirmed by our simulation.

In the second simulation we set the polarization angles to their real values, and in the third we add to that realistic pointing, which is slightly different for the M and S radiometers. Under these circumstances, the benefit of horn-uniform weighting, as compared to noise weighting, is still dramatic. In the last simulation we keep the realistic pointing and polarization angles, and replace the elliptic beam by the realistic main beam model. In this case the difference between the two weighting schemes reduces significantly, (being about 10% at 70 GHz), but is still a factor of 2–3 at 30 GHz and 44 GHz.

Table 4. Impact of the detector weighting scheme on temperature leakage.

30 GHz	Q		U	
	NW	HUW	NW	HUW
Ideal	0.1175	6.6×10^{-15}	0.1385	6.6×10^{-15}
Non-orthogonality . . .	0.1158	0.0080	0.1377	0.0067
Realistic pointing . . .	0.1163	0.0124	0.1381	0.0119
Realistic beam	0.1671	0.0890	0.1863	0.0893
44 GHz	Q		U	
	NW	HUW	NW	HUW
Ideal	0.5073	6.5×10^{-15}	0.5817	6.3×10^{-15}
Non-orthogonality . . .	0.5239	0.0166	0.6016	0.0187
Realistic pointing . . .	0.5313	0.0663	0.6081	0.0632
Realistic beam	0.7007	0.2946	0.8189	0.3246
70 GHz	Q		U	
	NW	HUW	NW	HUW
Ideal	0.0731	4.7×10^{-15}	0.0832	4.7×10^{-15}
Non-orthogonality . . .	0.0740	0.0025	0.0841	0.0023
Realistic pointing . . .	0.0758	0.0144	0.0858	0.0144
Realistic beam	0.1900	0.1658	0.2177	0.1834

Notes. Noise weighting (NW) is compared against horn-uniform weighting (HUW). We show the rms (in μK) of the Q and U maps from a CMB simulation with unpolarized inputs. All signal in the Q , U maps is leakage from temperature through beam and pointing non-idealities. The four rows correspond to simulations with increasing complexity: idealized simulation (see main text); non-orthogonal polarization angles; realistic pointing; and realistic beam model. The case that most closely corresponds to actual mapmaking is shown in boldface.

The level of temperature leakage reflects the beam-shape mismatch at each frequency. Although the beams of a 44 GHz horn are similar in ellipticity, they have different FWHM values at the 3% level, in contrast with <1% difference at 30 GHz and 70 GHz (Planck Collaboration IV 2016). For this reason the leakage is strongest at 44 GHz.

With foregrounds present, the temperature leakage is dominated by bandpass mismatch. We do not attempt to correct for this at the mapmaking level. Bandpass mismatch is easier to model and account for at later stages of data processing than beam mismatch. Bandpass correction for *Planck* LFI is discussed in Planck Collaboration II (2016).

4. Low-resolution products

Low-resolution products are an integral part of the low- ℓ likelihood. To fully exploit the information contained in the largest structures of the CMB sky, a full statistical description of the residual noise present in the maps is required. This information is provided in the form of pixel-pixel noise covariance matrices (NCVM). However, due to resource limitations these are impossible to employ at the native map resolution. Therefore a low-resolution data set is needed for the low- ℓ analysis. This data set consist of low-resolution maps and corresponding noise covariance matrices. At present, the low-resolution data set can be efficiently used only at HEALPix resolution $N_{\text{side}} = 16$ ($220'$) (or lower). All the low-resolution products are produced at this target resolution.

We begin by reviewing how the low-resolution maps were produced for the 2015 release. Then we discuss the production of the 2015 LFI low-resolution noise covariance matrices. The

noise covariance matrix section extends the study performed for Planck Collaboration II (2014).

4.1. Low-resolution maps

A number of different approaches for producing the low-resolution maps exist. Previous work on production of low-resolution maps have been published in Keskitalo et al. (2010). An ideal method would simultaneously minimize the pixelization effects and the residual noise. Realistic methods involve a trade-off between these two goals.

We use the high-resolution maps described in Sect. 2 as input for the low-resolution map production. The chosen downgrading scheme is nearly identical to the one used in the previous 2013 release (Planck Collaboration II 2014), the only difference being the addition of regularization noise to the final products.

The signal in a given high-resolution pixel is weighted with the inverse of its noise variance when binning the signal into larger pixels, and hence the downgrading scheme is called the “noise-weighted scheme.” The weights are given by Eq. (10). The resulting map is equivalent to one that is directly binned onto the target resolution from the TOI destriped at high resolution. Specifically we apply to a high-resolution map the operation

$$\mathbf{m}_l = (\mathbf{P}_l^T \mathbf{C}_w^{-1} \mathbf{P}_l)^{-1} \mathbf{X} (\mathbf{P}_h^T \mathbf{C}_w^{-1} \mathbf{P}_h) \mathbf{m}_h \equiv \mathbf{D} \mathbf{m}_h, \quad (20)$$

where

$$\mathbf{X}_{qp} = \begin{cases} 1, & \text{if } p \text{ is a subpixel of } q, \\ 0, & \text{otherwise,} \end{cases} \quad (21)$$

is the sum of high-resolution pixels to low-resolution pixels. Here subscripts “h” and “l” refer to high and low resolution versions of the pointing matrix. The same matrix \mathbf{X} also downgrades the pointing matrix, $\mathbf{P}_l = \mathbf{P}_h \mathbf{X}^T$. After downgrading, the temperature component is smoothed with a Gaussian window function with $FWHM = 440'$, to prevent aliasing due to high-frequency power in the map.

Our implementation of the downgrading scheme first downgrades the maps to an intermediate resolution of $N_{\text{side,mid}} = 32$ ($110'$). The Stokes I part of the map is expanded into spherical harmonics, treated with the smoothing beam, and the final map is then synthesized at the target resolution. The last downgrading step for Stokes Q and U maps is performed by naive averaging of higher resolution pixels, to minimize signal distortion.

4.2. Noise covariance matrices

The statistical description of the residual noise present in a low-resolution map is given in the form of a pixel-pixel noise covariance matrix. For generalized destriping the formalism was developed in Keihänen et al. (2005) and Keskitalo et al. (2010). Using the formalism introduced in Sect. 2, the noise-noise covariance matrix \mathbf{N} is given by

$$\mathbf{N} = \left[\mathbf{P}^T (\mathbf{C}_w + \mathbf{F} \mathbf{C}_a \mathbf{F}^T)^{-1} \mathbf{P} \right]^{-1}, \quad (22)$$

which can be written in a dimensionally reduced form as

$$\mathbf{N}^{-1} = \mathbf{P}^T \mathbf{C}_w^{-1} \mathbf{P} + \mathbf{P}^T \mathbf{C}_w^{-1} \mathbf{F} (\mathbf{F}^T \mathbf{C}_w^{-1} \mathbf{F} + \mathbf{C}_a^{-1})^{-1} \mathbf{F}^T \mathbf{C}_w^{-1} \mathbf{P}. \quad (23)$$

Here P , is the pointing matrix, F spreads the noise baselines to the TOI, C_a is the noise prior, and C_w is the white noise covariance.

For the current release, we use an implementation by Madam/TOAST, a Time Ordered Astrophysics Scalable Tools (TOAST; Kisner et al., in prep.) port of Madam. The TOAST interface was chosen on the basis of added flexibility. Madam/TOAST is capable of handling arbitrarily complex noise models. It can also handle bigger chunks of data, i.e., full mission versus only single survey in the previously used implementation, leading to reduced wall-clock time in computing. Some approximations and differences exist compared to high-resolution map production, and their effects are discussed in Sect. 4.3. These are specifically the differences in baseline length and destriping resolution, as well as simplifying approximations.

The formulation in Eq. (23) describes the noise correlations of a map destriped and binned at the same resolution, according to Eqs. (6)–(8). For an exact description we should construct the matrices at HEALPix resolution $N_{\text{side}} = 1024$ ($3.4'$), and subsequently downgrade to the target resolution. However, this is computationally unfeasible. Hence we calculate the noise covariance matrices at a practical intermediate resolution, which is not necessarily the target resolution, and subsequently downgrade to the target resolution. For consistency, the noise covariance matrices must go through the same smoothing and regularization steps as are applied to the low-resolution maps.

The covariance matrix does not model the effects of using a destriping mask and horn-uniform weighting, which were introduced to reduce systematics. The impact of these approximation on the accuracy of the NCVM products is assessed through simulations in Sect. 4.3.

Applying Eq. (23) in practice requires inversion of a symmetric $3N_{\text{pix}} \times 3N_{\text{pix}}$ matrix. The inversion is performed via the eigen-decomposition of the matrix. The monopole of the I map cannot be resolved by the map-maker, and the matrix becomes singular. This ill-determined mode is left out of the analysis.

The chosen downgrading scheme leads to a highly singular covariance matrix, since after smoothing the number of pixels in the map is larger than the number of non-zero spherical harmonics, resulting in a significant number of zero eigenvalues. We regularize the products by adding a small amount of white noise to the maps, and a corresponding diagonal covariance to the matrices. The level of regularization noise is chosen to be $2\mu\text{K}$ rms for I , and $0.02\mu\text{K}$ rms for Q and U at $N_{\text{side}} = 16$ resolution.

As seen from Eq. (23), the noise covariance computation requires two inputs: the detector pointings; and the noise model derived from the flight data.

For the noise covariance matrix production we use the most representative noise models available, namely the FFP8 noise estimates (Planck Collaboration XII 2016). The noise model consists of daily $1/f$ model parameters.

The NCVM production uses the FFP8 pointing solution of TOAST as an input. It reproduces the data processing centre (DPC) pointing to sub-arcsecond accuracy, except for a few isolated time periods where the flagging in TOAST differs from the DPC one. The differences between DPC and FFP8 hits maps for all LFI frequency channels are illustrated in Fig. 7, and the statistics of hits map differences are summarized in Table 5. The differences are distributed over the celestial sphere in a random fashion, with most points appearing near the ecliptic poles where the hit count itself is largest. This type of discrepancy is negligible for the results. For survey-by-survey comparisons see Planck Collaboration XII (2016).

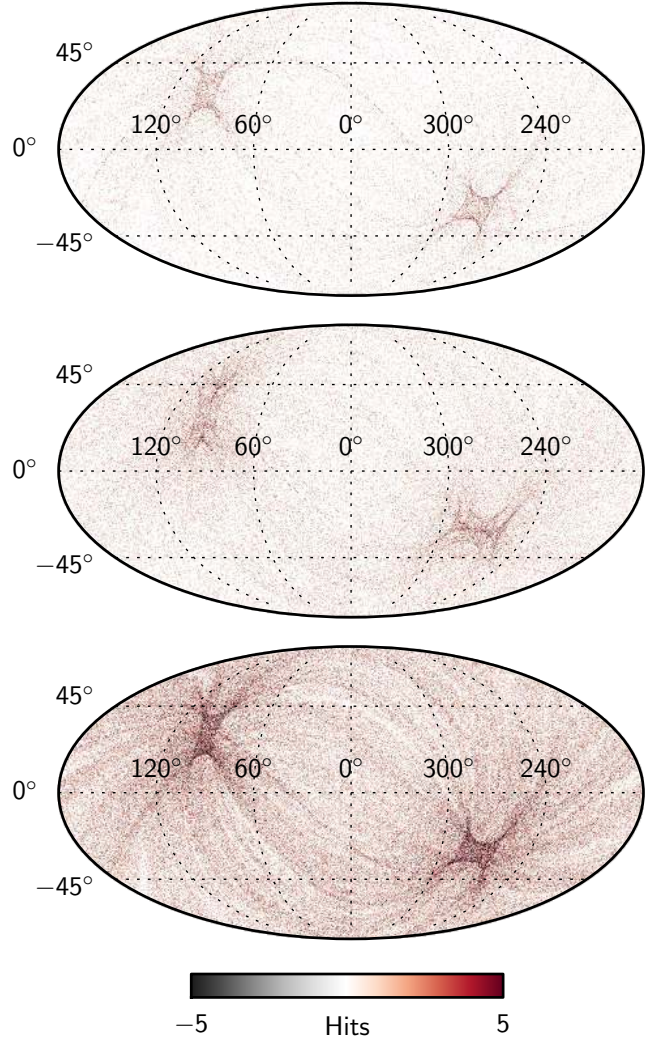


Fig. 7. Difference of DPC and FFP8 full-mission hits maps for all LFI frequency channels. The maps are shown in Galactic coordinates. *Top:* 30 GHz. *Middle:* 44 GHz. *Bottom:* 70 GHz.

For noise covariance computations the output of Madam/TOAST consists of inverse noise covariance matrices defined by Eq. (23), specifically one inverse matrix per radiometer for a given time period. For all LFI frequency channels we use 0.25-s baselines in the matrix production; the exact numbers are given in Table 5. The matrices are computed at the highest feasible resolution of $N_{\text{side}} = 64$ ($55'$). The individual inverse matrices are merged together to form the actual inverse NCVMs. These inverse matrices are then inverted using the eigen-decomposition of a matrix, and subsequently downgraded to the target resolution using the same downgrading scheme as applied for the maps. The 70-GHz full-mission noise covariance matrix computation took approximately 6 h of wall-clock time and 23 000 CPU hours.

4.3. Validation

We have performed a series of simulations to assess the effect of different parameters and approximations to the quality of the noise covariance matrices.

We performed noise MC simulations with the FFP8 pipeline (Planck Collaboration XII 2016), but by varying the mapmaking parameters. For all combinations of simulation parameters

Table 5. Frequency-specific information related to the noise covariance matrix production.

Channel	Difference hits map statistics			Hits map statistics			Baseline length	
	Min.	Max.	St. dev.	Mean	Min.	Max.	[s]	Samples
30 GHz	-18	18	0.71	1180	172	92 100	0.2461	8
44 GHz	-22	28	1.02	2530	574	134 000	0.2578	12
70 GHz	-34	44	1.88	8560	2130	266 000	0.2539	20

Notes. From left to right: the statistics of difference between DPC and FFP8 full-mission hits maps for all LFI frequency channels; the statistics of DPC full-mission hits maps; and the baseline lengths used in the noise covariance matrix production, both in seconds and as a number of samples.

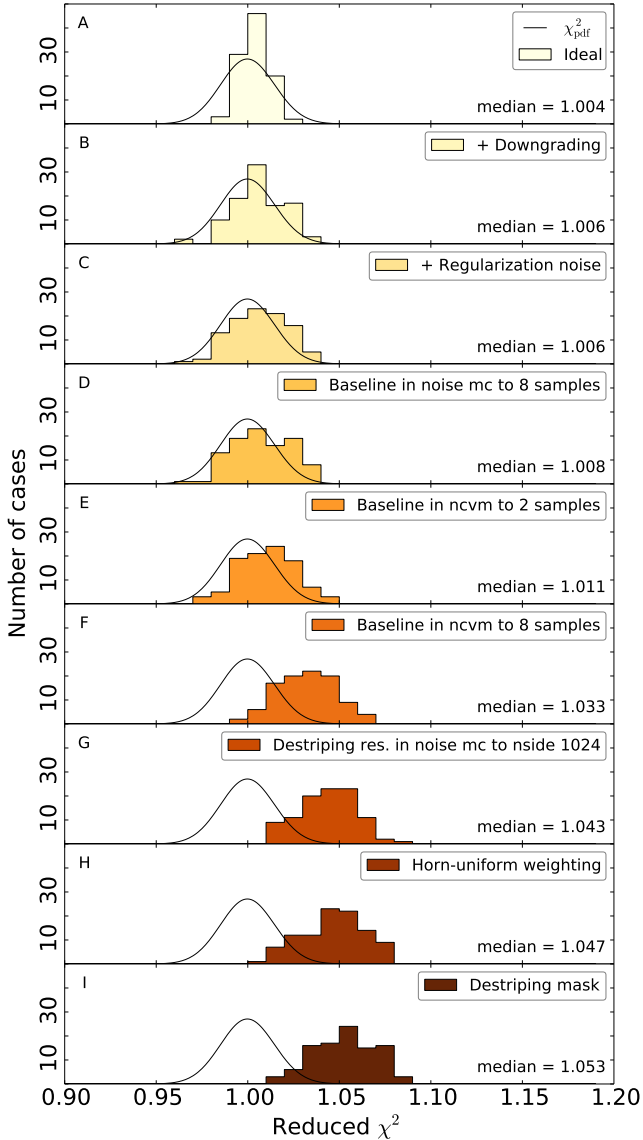


Fig. 8. Reduced χ^2 statistics for simulated full-mission 30-GHz data. The initial resolution of the noise covariance matrix is $N_{\text{side}} = 32$ ($110'$). The *uppermost panel* represents an idealized simulation, compared with the most accurate (and most expensive to produce) noise covariance matrix. The level of idealization decreases *from top to bottom*, the *lowest panel* representing a fully realistic simulation compared against a covariance matrix from production runs.

we have generated 100 realizations of noise-only maps. We altered the baseline length, the destriping resolution, the weighting scheme, or the inclusion of a destriping mask. In the noise covariance matrix production we altered the baseline length and

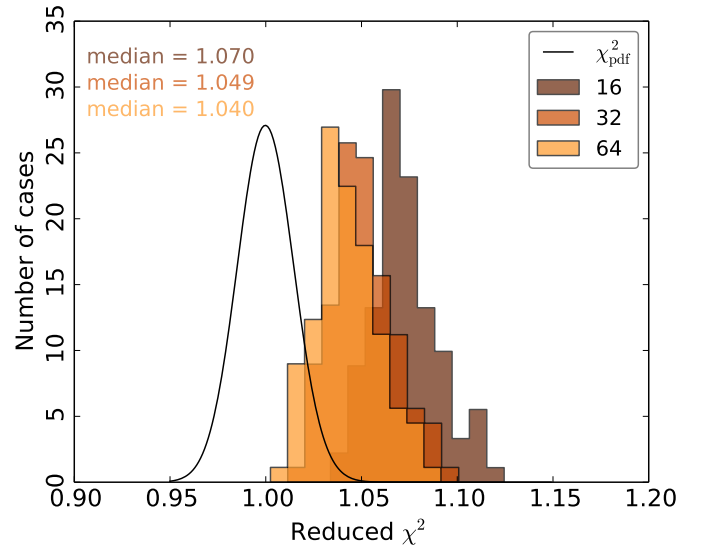


Fig. 9. Reduced χ^2 statistics for simulated full-mission 30-GHz data. The initial resolution of the noise covariance matrix is varied from $N_{\text{side}} = 16$ to 64 ($220'$ to $55'$). In all cases the covariance matrix is eventually downgraded to resolution $N_{\text{side}} = 16$ and compared against simulated maps at this resolution.

destriping resolution. We chose to perform the simulations for the 30-GHz channel, which requires the least computational resources. Figures 8 and 9 summarize the results from our simulations.

We calculate for each simulated noise map m the reduced χ^2 statistic, defined as

$$\chi^2 = \frac{m^T N^{-1} m}{N_{\text{d.o.f.}}}, \quad (24)$$

where N is the noise covariance matrix, and the number of degrees of freedom $N_{\text{d.o.f.}} = 3N_{\text{pix}}$. In the presence of ill-conditioned eigenmodes, the degrees of freedom are reduced accordingly. For unregularized, smoothed noise covariance matrices the effective number of degrees of freedom equals the number of non-zero eigenvalues. The distribution of reduced χ^2 values peaks at 1 for a noise covariance matrix that perfectly models the properties of the simulated noise maps.

In Fig. 8 the degree of idealization reduces from top to bottom. We add one effect at a time, so that the last panel represents a fully realistic simulation. We start from an idealized case (panel A), where both the noise maps and noise covariance matrices have been calculated at HEALPix resolution $N_{\text{side}} = 32$ ($110'$), with 1-sample baselines (0.03125 s). In panel B we downgrade both maps and matrix to the resolution of $N_{\text{side}} = 16$ ($220'$), and in panel C we regularize the maps and

matrices. We observe that the effects of downgrading and regularization on the χ^2 result are marginal.

The key parameter in noise covariance matrix computation is the baseline length. In earlier studies we demonstrated that shorter baseline length in the noise covariance matrix production models the residual noise better (Planck Collaboration II 2014). Given the enhanced computing resources it was possible to bring the baseline length down to one sample. Panels D–F of Fig. 8 summarize the results. In panel D we increase the baseline length in MC simulations from one sample to eight samples (0.25 s), which was the value used in actual mapmaking. Panels E–F show the effect of increasing the baseline length in matrix computation from one sample to first two samples, and then to eight samples (0.25 s). We find that reducing the baseline length in NCMV computation below 0.25 s does indeed improve the results, but at the same time the computer memory requirements increase rapidly. For the 2015 release we have used 0.25-s baselines for all LFI frequency channels, but we propose the adoption of even shorter baselines in future releases, resources permitting.

Panel G shows the effect of changing the destriping resolution in MC simulations from HEALPix $N_{\text{side}} = 32$ ($110'$) to the realistic value $N_{\text{side}} = 1024$ ($3.4'$). The noise covariance computation makes two further deviations from the high-resolution mapmaking: the horns are not uniformly weighted (panel H); no account is taken of the destriping mask (panel I). Panel I finally represents a fully realistic simulation. The effects in panels G–I are shown to be much smaller than the effects of the baseline length and the destriping resolution.

We examine the impact of resolution further in Fig. 9. As motivated in the previous section, the matrices should be calculated at the highest computationally feasible resolution. We calculated a few noise covariance matrices with varying initial resolution. Each matrix was downgraded to HEALPix resolution $N_{\text{side}} = 16$ ($220'$) and compared against a downgraded set of FFP8 noise maps (100 realizations). As expected, the highest resolution $N_{\text{side}} = 64$ ($55'$) gives the best agreement. Increasing the initial resolution beyond $N_{\text{side}} = 64$ is likely to improve results further, but the expected improvement would be very small for a huge computational effort. Increasing the initial resolution beyond $N_{\text{side}} = 64$ to $N_{\text{side}} = 128$ increases the matrix size by a factor of 16, to 2.5 TB.

5. Results

5.1. High-resolution maps

The 2015 release includes a large number of map products. A complete list is given in Planck Collaboration II (2016). Figures 10–12 show the main LFI products, which are the frequency maps for the complete 4-year data set. Shown in these figures are the temperature map, and Q and U polarization. For illustration purposes the polarization maps have been smoothed with a symmetric Gaussian beam with $FWHM = 1^\circ$.

The released maps are in Galactic coordinates. The division of the polarization signal into Q and U components is dependent on the chosen coordinate frame. The Q map represents a component where the polarization direction is aligned with the local longitude (positive Q) or with the local latitude (negative Q). The U map represents a component where the polarization direction is at a $\pm 45^\circ$ angle with respect to the longitude. The polarization maps shown here are subject to bandpass leakage (Planck Collaboration II 2016), which must be taken into account in the subsequent analysis.

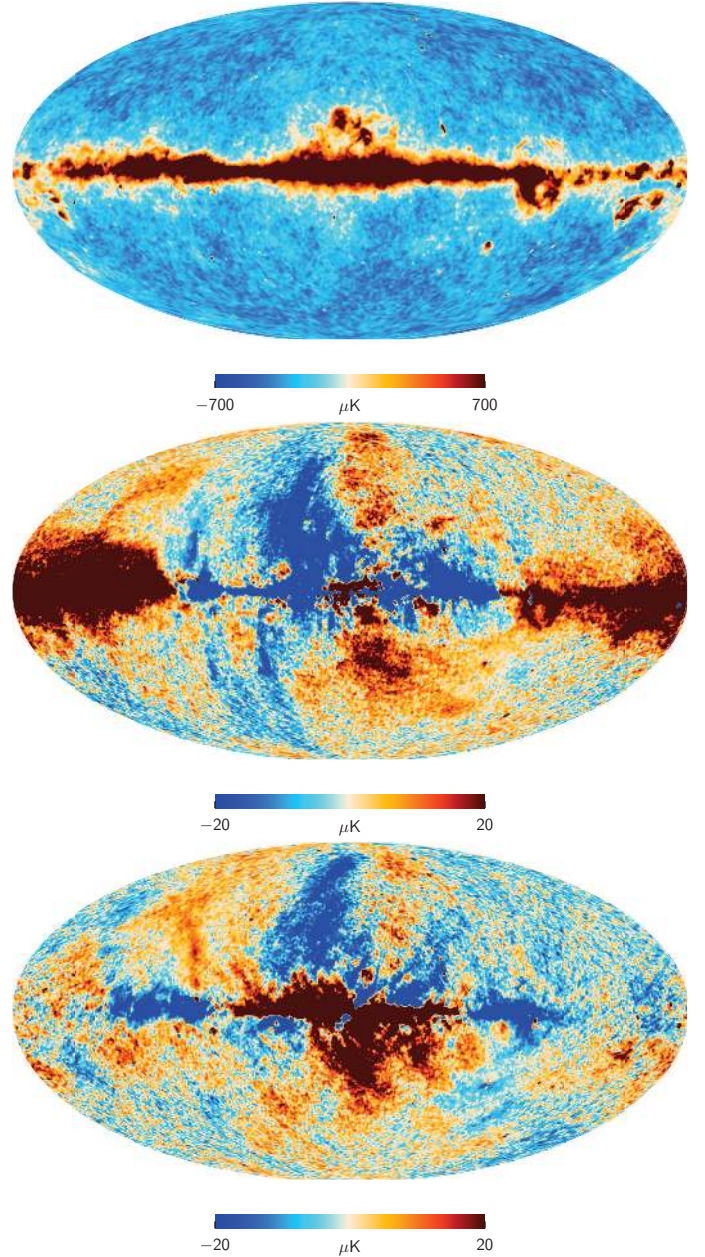


Fig. 10. LFI 30-GHz channel maps: temperature (*top*); Q polarization (*middle*); and U polarization (*bottom*). The temperature map has resolution $N_{\text{side}} = 1024$. The polarization maps have been downgraded to resolution $N_{\text{side}} = 256$ ($13.7'$) and smoothed with a $FWHM = 1^\circ$ Gaussian beam. The polarization maps are not corrected for bandpass mismatch leakage.

We do not correct for beam shape in the mapmaking process. The shape of a point source in a map directly reflects the beam shape. In particular, the power that is lost into the far sidelobes (Planck Collaboration IV 2016), is missing from the point source as well, and must be taken into account when determining source fluxes.

As auxiliary information we provide for each high-frequency map an estimate of the white noise covariance. This 3×3 matrix gives the noise correlation between Stokes components within each pixel. We also provide a corresponding pixelized hit count for each map.

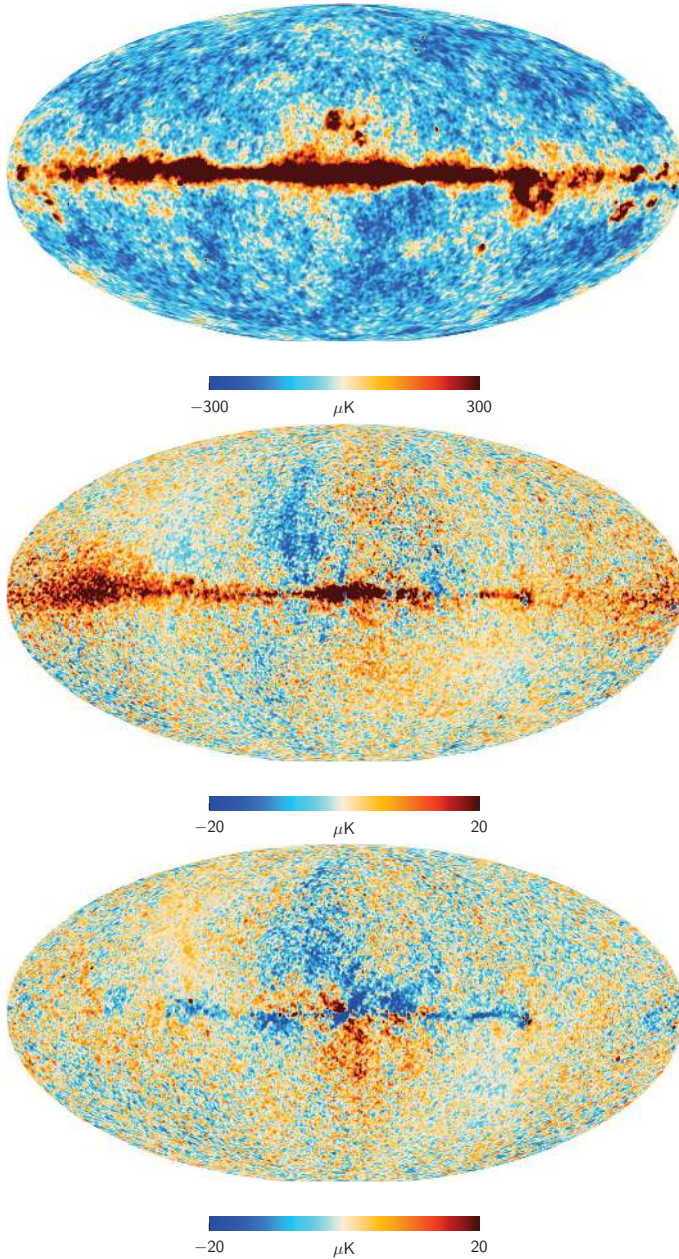


Fig. 11. LFI 44-GHz channel maps: temperature (*top*); Q polarization (*middle*); and U polarization (*bottom*). Smoothing and resolution are the same as in Fig. 10.

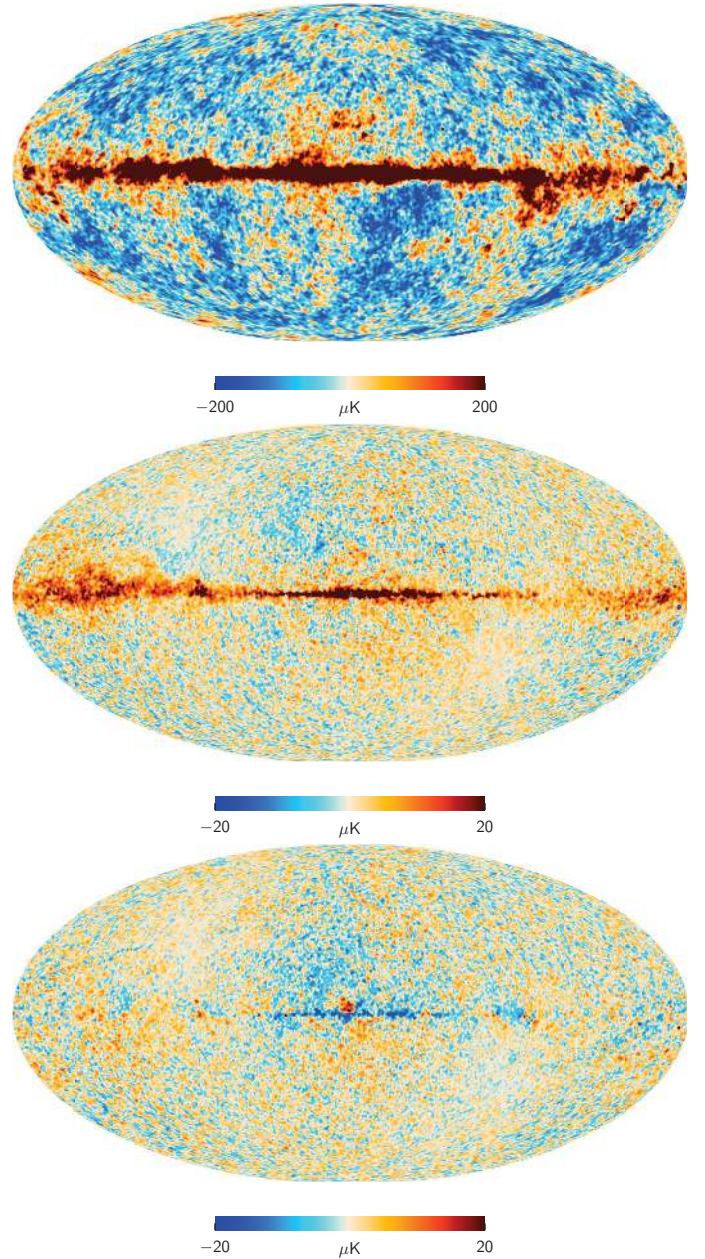


Fig. 12. LFI 70-GHz channel maps: temperature (*top*); Q polarization (*middle*); and U polarization (*bottom*). Smoothing and resolution are the same as in Fig. 10.

5.2. Sky coverage

Among other map products are single-survey maps that include data from one 6-month survey, and single-year maps that include two surveys each. These do not quite give full sky coverage. As discussed in Sect. 2.1.3, construction of (I, Q, U) Stokes components requires that a pixel is scanned by a pair of horns, with complementary polarization sensitivity. Pixels that are scanned by a single horn or radiometer, can be used for destriping, but not for the final map.

The sky coverage of the frequency maps are given in Table 6. We present three numbers for each map. In the first column (“map”) we give the sky coverage of the final map. This is the sky area that has been scanned by two radiometer pairs so that we have been able to solve the full I, Q, U triplet. The second column (“scan”) gives the sky area that is scanned by at least one

radiometer, and is thus available for the solution of the destriping equation. The focal plane is designed in such a way that in most cases a pair of horns follows the same scanning path. Each pixel is thus covered by four radiometers, and the difference between the two columns is small. An exception to this is the 44-GHz frequency channel, where horn LFI-24 does not have a counterpart. A significant part of the sky in single surveys is covered by horn LFI-24 alone. As a consequence, the sky area available for destriping is significantly higher than that available for the final map. In the third column (“destriping”) we give the sky area that remains after the Galactic mask is applied. This is the area eventually used for destriping.

Single-survey temperature maps for each full frequency are shown in Fig. 13. We indicate by different colour scales the regions used for the final map or for destriping. The combination of blue and purple regions is included in the final map. The size

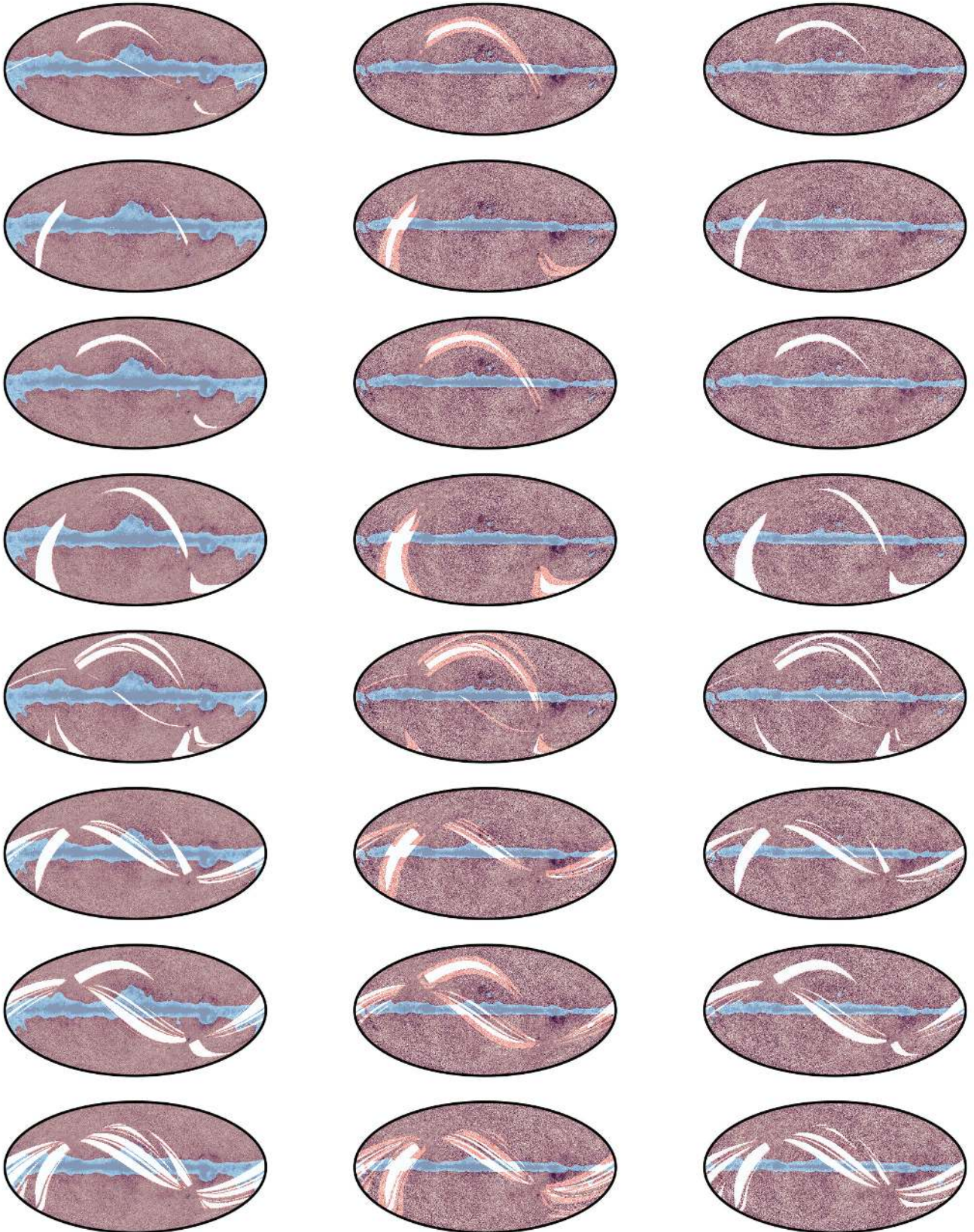


Fig. 13. Sky-coverage of single-survey temperature maps for 30, 44, and 70 GHz. *Left:* 30 GHz. *Middle:* 44 GHz. *Right:* 70 GHz. *From top to bottom,* Surveys 1 to 8. The region of the Galactic mask is shown in blue. The combination of red and purple regions is used for destripping. The small red patches, visible especially at 44 GHz, indicate pixels from which there is not enough coverage to solve the Stokes components, but which can still be used for the destripping solution. The combination on purple and blue regions is included in the final map. Unobserved regions are shown in white. The intensity of a pixel encodes Stokes I .

Table 6. Sky coverage (as a percentage) of full-mission, single-year, and single-survey frequency maps.

Survey	P_{id} range ^a	30 GHz			44 GHz			70 GHz		
		Map	Scan	Destriping	Map	Scan	Destriping	Map	Scan	Destriping
Full	3–44072	100.0	100.0	78.74	100.0	100.0	89.37	100.0	100.0	89.67
Year 1	3–10957	99.999	100.0	78.74	99.998	100.0	89.37	100.0	100.0	89.67
Year 2	10 958–21482	99.98	100.0	78.74	99.998	100.0	89.37	100.0	100.0	89.67
Year 3	21 483–32761	99.72	99.74	78.66	99.91	100.0	89.37	99.65	99.65	89.38
Year 4	32 762–44072	95.68	95.76	76.61	96.87	98.68	88.35	97.38	97.43	87.63
Survey 1	3– 5483	97.20	98.11	76.88	93.93	98.03	87.41	97.94	97.95	87.62
Survey 2	5484–10957	97.48	97.58	77.40	93.31	98.13	87.89	97.47	97.49	87.62
Survey 3	10 958–16454	97.62	97.71	76.49	93.65	98.23	87.61	97.61	97.63	87.30
Survey 4	16 455–21482	91.88	91.98	72.37	89.53	94.92	84.85	92.40	92.43	82.89
Survey 5	21 483–27404	90.89	91.02	70.27	88.43	96.70	86.08	92.44	92.50	82.33
Survey 6	27 405–32761	87.79	88.06	72.35	86.10	94.56	85.29	89.95	90.18	82.04
Survey 7	32 762–38574	85.40	85.60	68.29	83.70	92.49	82.80	88.43	88.52	79.65
Survey 8	38 575–44072	80.01	80.26	67.54	78.92	89.61	81.15	83.83	84.09	77.05

Notes. We give the pointing period (P_{id}) range for each survey combination, the sky coverage of the final map (“map”), the area that was scanned by at least one horn (“scan”) and is available for destriping, and the area that remains after applying a Galactic mask and that was used for destriping (“destriping”). Since the full-mission data set covers the full sky, the coverage of the destriping mask can be read from the intersection of the “full” (mission) row and the “destriping” column. ^(a) P_{id} is a counter for pointings of the spin axis, which had an average duration of about 45 minutes (see [Planck Collaboration I 2014](#), for the explicit definition).

of this region is given in the “map” column of Table 6. The Galactic region, shown in blue, is masked out in the destriping phase, and not used for solving the baselines. The red colour, mostly visible at 44 GHz, indicates the region that is scanned by a single horn, and is used for destriping, but is not included in the final map. The purple and red regions together correspond to the column headed “destriping” in Table 6. The region shown in white does not contain useful data.

5.3. Low-resolution products

The 2015 release includes low-resolution maps and noise covariance matrices both for the full mission and for a data selection covering surveys 1, 3, and 5–8 (Planck Collaboration II 2016) at HEALPix resolution of $N_{\text{side}} = 16$ ($220'$). They have been processed with the noise-weighted downgrading scheme, and subsequently the Stokes I component has been smoothed with a Gaussian beam of $FWHM = 440'$. Finally the products have been regularized by adding $2\mu\text{K}$ rms for I , and $0.02\mu\text{K}$ rms for Q and U of white noise at $N_{\text{side}} = 16$ resolution.

Figure 14 illustrates the full-mission low-resolution Stokes I , Q , and U maps for each *Planck* LFI frequency channel. Figure 15 illustrates a single column of the 70-GHz full-mission noise covariance matrix. The column corresponds to pixel number 1248 in the HEALPix nested pixelization scheme for $N_{\text{side}} = 16$ resolution (longitude $348^\circ 8$, latitude $12^\circ 0$). The pixel values in the plot represent correlation coefficients, since each pixel value $\langle m_p m_q \rangle$ has been normalized by $\sqrt{\langle m_p^2 \rangle \langle m_q^2 \rangle}$. In this normalization the reference pixel automatically gets unit value, and is later set to zero to bring out finer details of the noise covariance matrix. The correlations are strongest in the scanning direction.

5.4. Characterization of noise

5.4.1. Residual noise at high multipoles

Residual noise at high multipoles is dominated by non-uniform white noise, which is uncorrelated between pixels. We also

provide a description of the white noise component in the form of the white noise covariance, computed according to Eq. (14). The covariance matrix consists of a symmetric 3×3 matrix for every map pixel. The matrix gives the noise correlation between Stokes components, I , Q , and U , within each pixel. White noise gives a lower limit for the full residual noise level.

Table 7 shows the average white noise covariance per pixel in the frequency maps. We show the values of II , IQ , IU , QQ , QU , and UU noise covariance, as averages over all pixels. We also give the expected white noise level in the angular power spectrum, calculated as

$$C_{T\ell}^{\text{wn}} = \langle II \rangle \frac{4\pi}{N_{\text{pix}}} \quad (25)$$

and

$$C_{E\ell}^{\text{wn}} = C_{B\ell}^{\text{wn}} = \frac{1}{2} (\langle QQ \rangle + \langle UU \rangle) \frac{4\pi}{N_{\text{pix}}}, \quad (26)$$

where N_{pix} is the number of pixels in the map (12 582 912) and brackets indicate an average over pixels.

The 44-GHz channel shows an imbalance between Q and U components. This is due to horn LFI-24, which does not have a counterpart with complementary polarization sensitivity. The same effect can be seen in the CRN (correlated residual noise) plots in Sect. 3.

We use half-ring maps to derive an estimate for the level of correlated residual noise at high multipoles. We find that even after destriping there remains correlated residual noise at the highest multipoles, and it affects the auto-spectra at the 1% level. In Fig. 16 we plot the ratio of the estimated noise spectrum in the high-multipole regime and the white noise level reported in Table 7. We show the mean of the spectrum over multipoles $\ell = 1150$ –1800. We also show in the same figure the mean of 10 000 FFP8 noise Monte Carlo realizations, all derived from the same noise spectrum. The error bars on the MC estimates indicate the statistical 1σ variation of the realizations, not the uncertainty in the noise model.

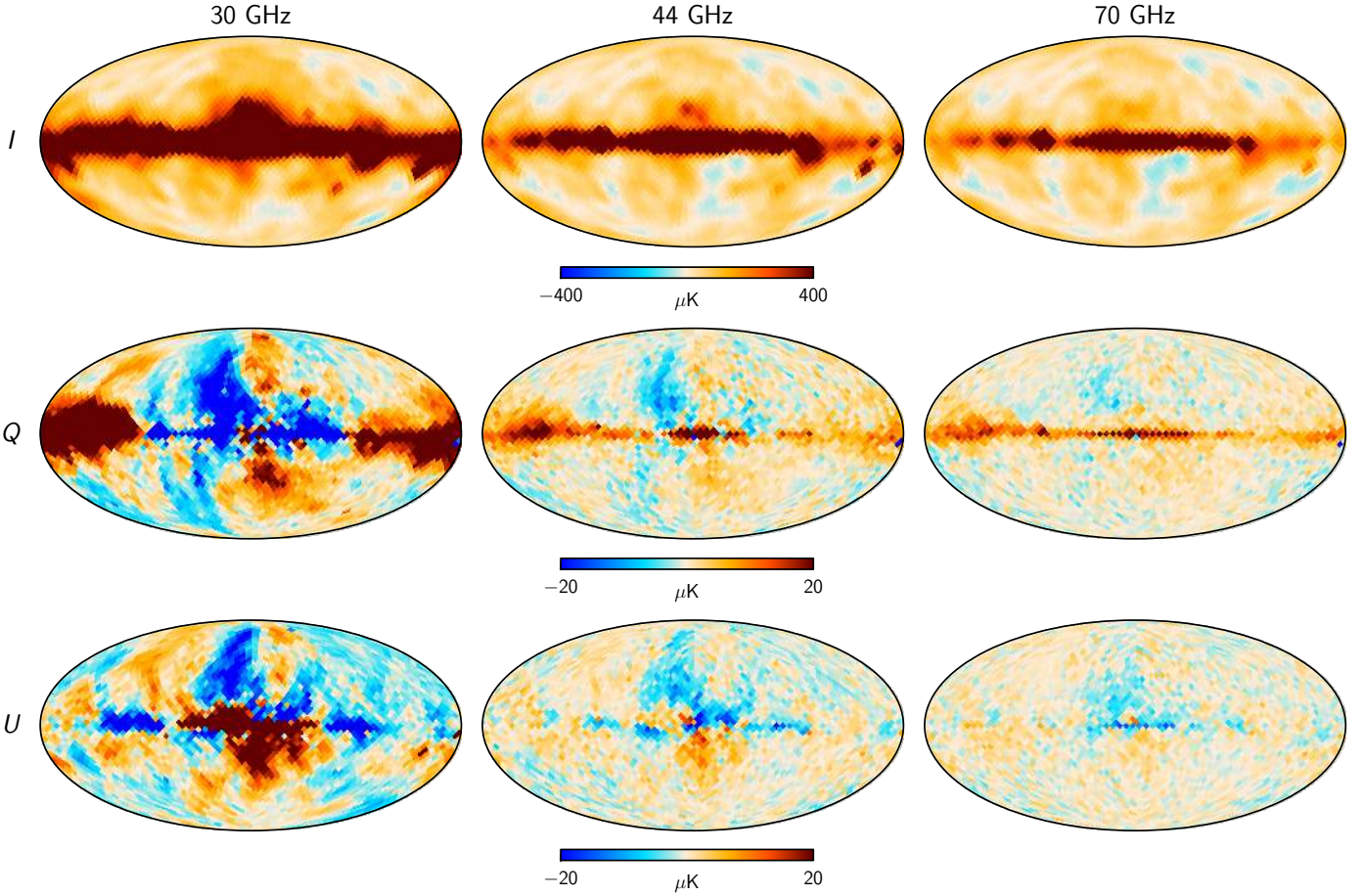


Fig. 14. LFI full-mission low-resolution maps, at $N_{\text{side}} = 16$ ($220'$). From left to right: 30 GHz; 44 GHz; and 70 GHz. From top to bottom: I (temperature), Q , and U (polarisation). Units are in μK_{CMB} . The temperature maps are smoothed with a $440'$ (FWHM) Gaussian beam.

Table 7. White noise level for frequency maps, computed from the white noise covariance matrix.

Channel	II	QQ	UU	IQ	IU	QU	C_{TT}	C_{EE}, C_{BB}
30 GHz	3224.4	6467.8	6465.1	-19.2	-71.0	-41.2	0.003220	0.006458
44 GHz	4331.0	10088.0	8906.9	-2.4	24.3	-136.9	0.004325	0.009485
70 GHz	3358.5	6775.7	6713.7	28.1	-69.0	-83.3	0.003354	0.006736

Notes. We present the average white noise covariance per pixel for Stokes components, and white noise spectrum level derived from the same numbers. All values are in μK^2 units.

5.4.2. Residual noise at low multipoles

We have three complementary methods for characterization of correlated residual noise at low multipoles: the noise covariance matrix; MC simulations; and the half-ring noise map. We now compare the noise estimates from these three methods against each other.

Figure 17 shows the reduced χ^2 statistics for full-mission noise covariance matrices. The χ^2 tests have been carried out with 10 000 FFP8 noise realizations with realistic mapmaking parameters. The vertical lines indicate the reduced χ^2 value for the half-ring noise maps. The agreement between the noise covariance matrix and the half-ring maps is best at the 70-GHz frequency channel, which is the most important for the cosmological parameter estimation.

Figures 18–20 show noise bias estimates for full-frequency maps at low multipoles. We show the six noise spectra (TT ,

EE , BB , TE , TB , EB) constructed from the NCVMs, and corresponding estimates from FFP8 noise Monte Carlo simulations. We show the average and median over 10 000 noise realizations. We plot in the same figure also the spectrum of the half-ring noise map. As this represents one realization only, it has much stronger variations than the other estimates.

6. Conclusions

In this paper we have described the mapmaking procedure used for the 2015 data release from *Planck* LFI, and characterized the noise in the map products. For the first time, we have shown polarization Q and U maps at LFI frequencies.

High-resolution maps were produced with the Madam mapmaking code. The algorithm is based on a destriping technique, which is extended to short baseline lengths with the help of a noise prior. We validated the procedure through noise and signal

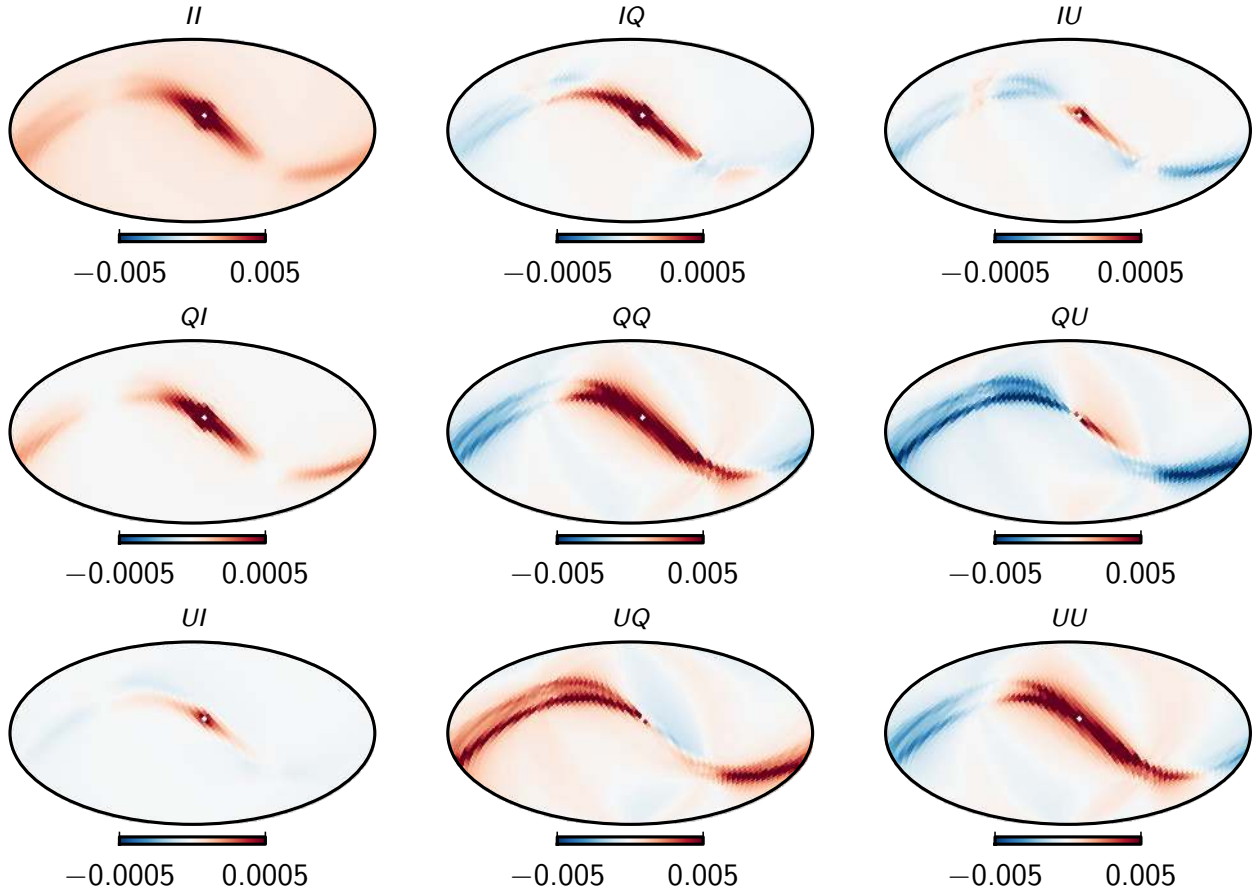


Fig. 15. A single column of the 70-GHz full-mission noise covariance matrix. The reference pixel is pixel 1248 in the HEALPIX nested pixelization scheme, centred at $(348^{\circ}8, 12^{\circ}0)$. The noise covariance matrix has been normalized to show correlation coefficients. The reference pixel is set to zero to highlight more of the finer details of the correlation structure.

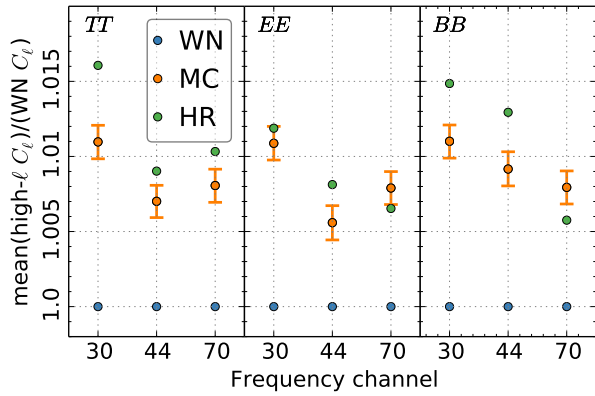


Fig. 16. Comparison of noise estimates at high multipoles, as a ratio of the full noise level and the white noise level (blue). The green dots show the estimate from half-ring maps. The orange dots show the mean of 10 000 Monte Carlo simulations. The error bars here include the statistical variation only. The values shown are mean values of the noise spectrum in the range $\ell = 1150\text{--}1800$. The absolute white noise levels in μK^2 are reported in the last two columns of Table 7.

simulations. We studied the effect of two main parameters that control the mapmaking procedure, namely the baseline length, and the destriping resolution. We showed that the values chosen for the actual pipeline are appropriate for the data set and allow

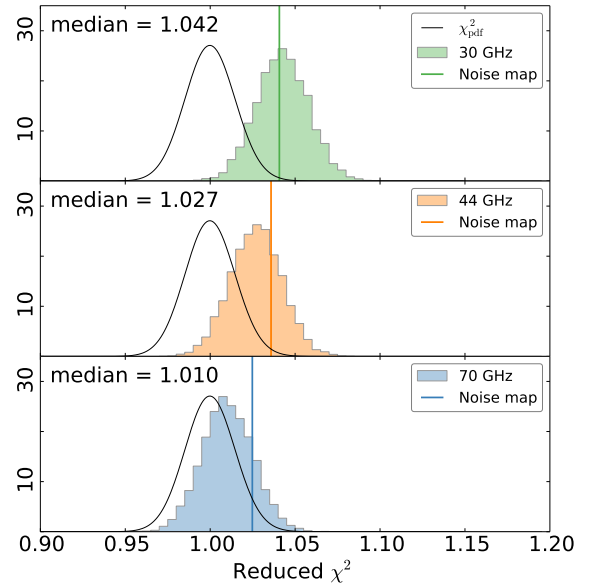


Fig. 17. Reduced χ^2 statistics for 2015 full-mission noise covariance matrices. χ^2 tests have been carried out with 10 000 FFP8 noise realizations. Vertical lines mark the reduced χ^2 value for half-ring noise maps.

for good noise removal, while keeping the signal error at a low level.

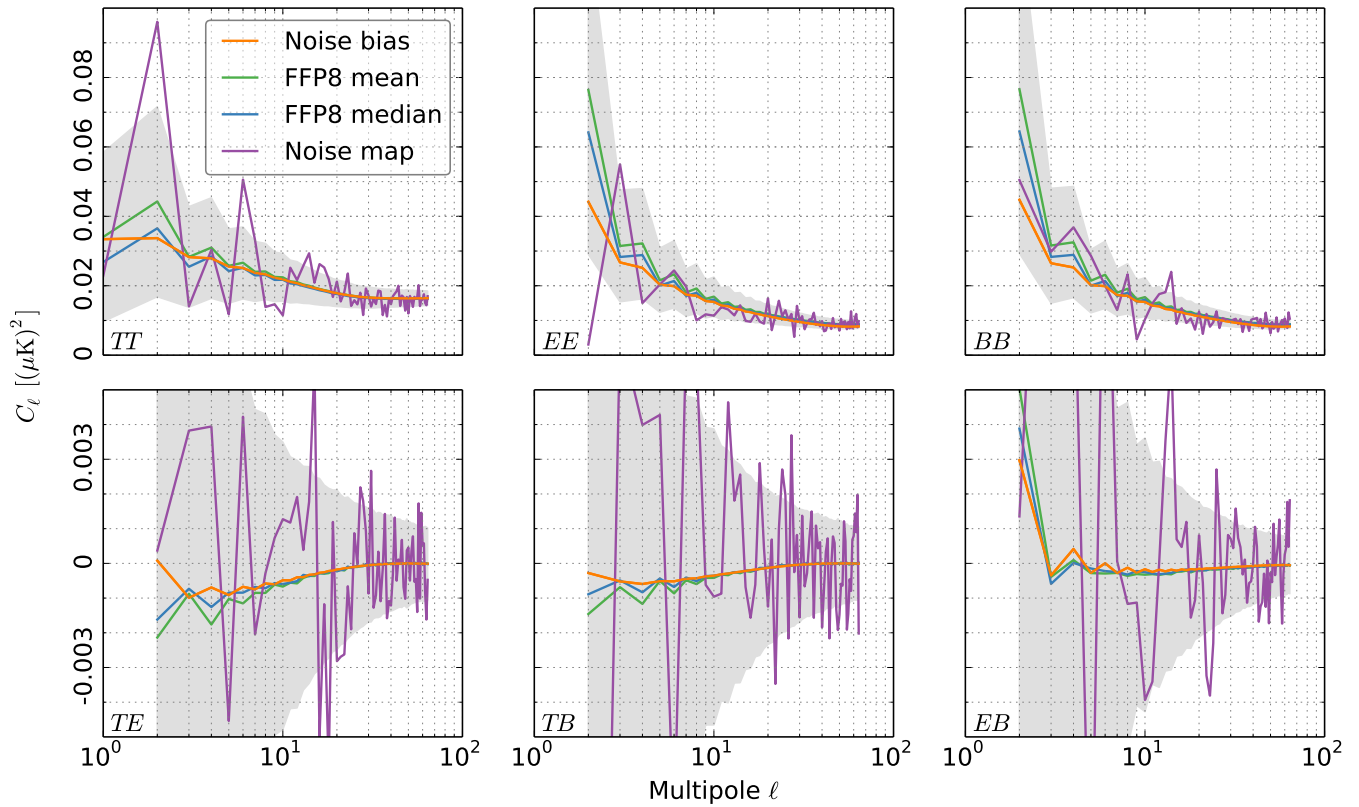


Fig. 18. Noise bias levels at 30 GHz. Noise bias from the 2015 full-mission noise covariance matrix is plotted in orange. The noise MC statistics from 10 000 FFP8 simulations are plotted in green (for the mean), blue (median) and grey ($\pm 1\sigma$ region), as well as the noise estimate of the half ring noise map in purple.

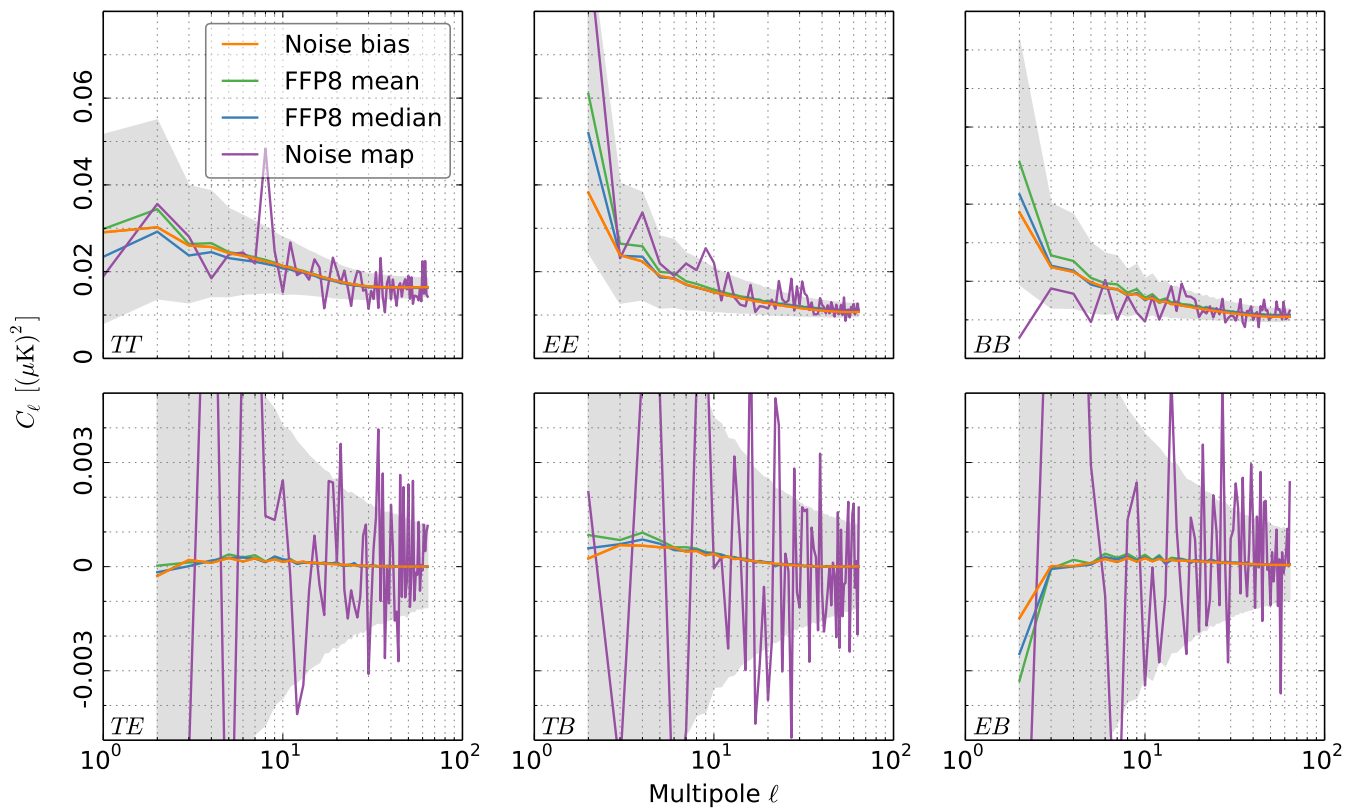


Fig. 19. Noise bias levels at 44 GHz. The line types are the same as in Fig. 17.

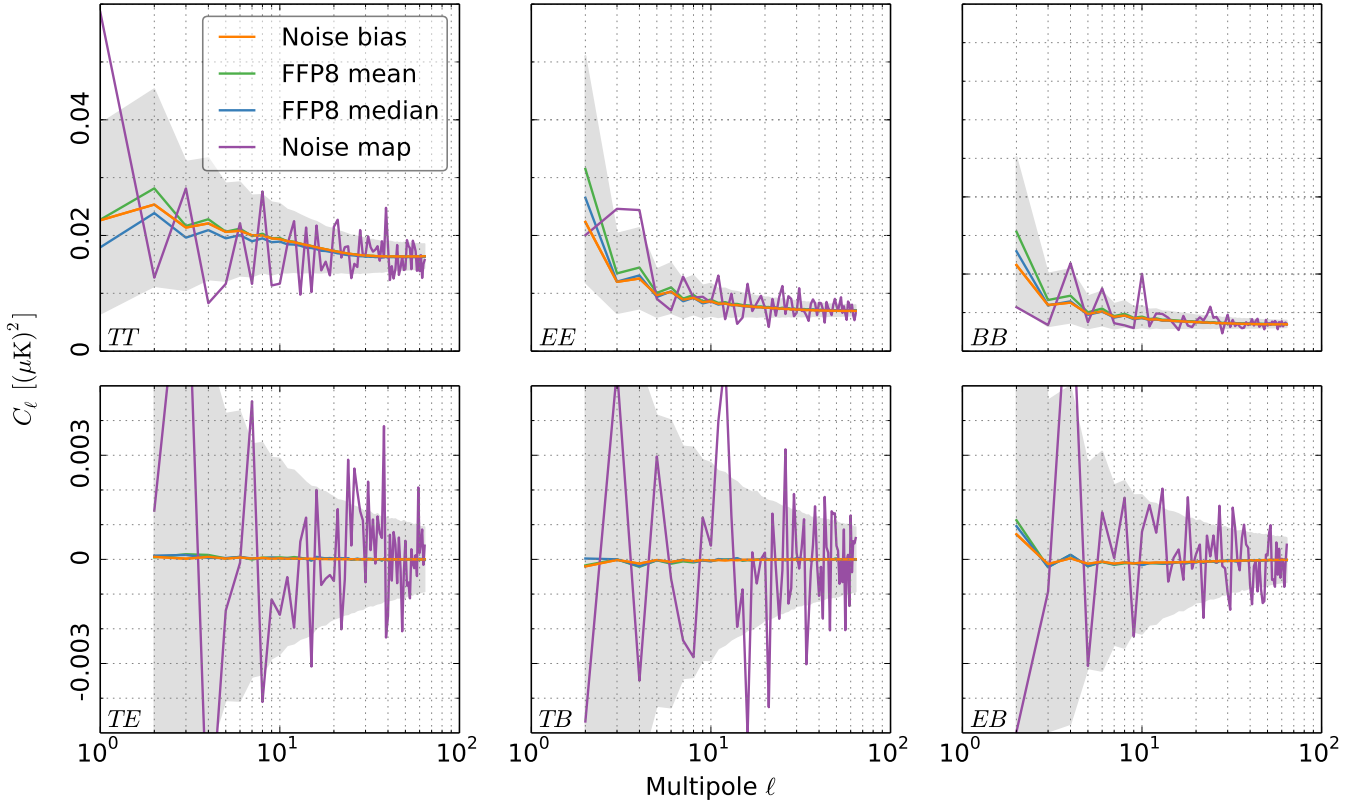


Fig. 20. Noise bias levels at 70 GHz. The line types are the same as in Fig. 17.

We have paid special attention to the reduction of unwanted systematic effects. We applied a Galactic mask to reduce the propagation of the signal error arising from bandpass mismatch and strong signal gradients. We assessed the impact of this through simulations, and showed that the signal error is indeed reduced significantly, while the cost in residual noise is low.

The horn-uniform weighting scheme was introduced to reduce leakage of temperature signal to polarization through beamshape mismatch. The effect at 30 GHz and 44 GHz was significant, but less so at 70 GHz. In all cases, however, the cost in residual noise level was small.

The polarization map products presented here are subject to bandpass mismatch leakage. The leakage correction applied is discussed in Planck Collaboration II (2016). The maps are not corrected for beam shape, or for the power to the far sidelobe part of the beam. In particular, images of point sources reflect the radiometer beam shapes. The exact beam shapes must be accounted for in the estimation of source fluxes from LFI maps.

We also described the production of low-resolution maps and noise covariance matrices. The low-resolution maps were produced by downgrading the high-resolution maps to the target HEALPix resolution of $N_{\text{side}} = 16$ ($220'$) with the noise-weighting scheme, and the I component was subsequently smoothed with a Gaussian beam. The noise covariance matrices were initially calculated at the resolution of $N_{\text{side}} = 64$ ($55'$) with Madam/TOAST software, and subsequently the same downgrading scheme was applied to them as for the maps. Finally both the low-resolution maps and matrices were regularized by adding a small amount of white noise to all products.

The matrices were validated against noise Monte Carlo simulations. The match between the matrices and the simulations was best at 70 GHz, which is the most important channel for

cosmology analysis. We performed a series of simulations to quantify the effect of each approximation involved in the noise covariance computation. The most important effects turned out to be the high destriping resolution, and the limited baseline length.

In addition to the noise covariance matrices, we characterized the residual noise in maps through noise Monte Carlo simulations and the noise maps constructed from half-ring maps. The noise estimates from the complementary methods show good agreement.

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