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Planck intermediate results. LIII. Detection of velocity dispersion from the kinetic Sunyaev-Zeldovich effect

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ABSTRACT

Using the *Planck* full-mission data, we present a detection of the temperature (and therefore velocity) dispersion due to the kinetic Sunyaev-Zeldovich (kSZ) effect from clusters of galaxies. To suppress the primary CMB and instrumental noise we derive a matched filter and then convolve it with the *Planck* foreground-cleaned “2D-ILC” maps. By using the Meta Catalogue of X-ray detected Clusters of galaxies (MCXC), we determine the normalized rms dispersion of the temperature fluctuations at the positions of clusters, finding that this shows excess variance compared with the noise expectation. We then build an unbiased statistical estimator of the signal, determining that the normalized mean temperature dispersion of 1526 clusters caused by the kSZ effect is $\langle(\Delta T/T)^2\rangle = (1.64 \pm 0.48) \times 10^{-11}$, which gives a detection at the 3.2σ level. We convert the temperature dispersion of uniform weight into a measurement of the line-of-sight velocity dispersion, by using estimates of the optical depth of each cluster (which introduces additional uncertainty into the estimate). We find that the velocity dispersion is $\langle\sigma^2\rangle = (154\,000 \pm 72\,000) (\text{km s}^{-1})^2$, which is consistent with findings from other large-scale structure studies, and provides direct evidence of statistical homogeneity on scales of $600 h^{-1}\text{Mpc}$. Our study shows the promise of using cross-correlations of the kSZ effect with large-scale structure in order to constrain the growth of structure.

Key words. Cosmology: observations – cosmic microwave background – large-scale structure of the Universe – Galaxies: clusters: general – Methods: data analysis

1. Introduction

The kinetic Sunyaev-Zeldovich (hereafter kSZ; Sunyaev & Zeldovich 1972, 1980) effect describes the temperature anisotropy of the cosmic microwave background (CMB) radiation due to inverse Compton scattering off a moving cloud of electrons. The effect can be written as

$$\frac{\Delta T}{T}(\hat{\mathbf{r}}) = -\frac{\sigma_T}{c} \int n_e(\mathbf{v} \cdot \hat{\mathbf{r}}) dl, \quad (1)$$

where σ_T is the Thomson cross-section, n_e is the electron density, $\mathbf{v} \cdot \hat{\mathbf{r}}$ is the velocity along the line-of-sight, and

dl is the path length in the radial direction. By adopting a so-called “pairwise momentum estimator,” i.e., using the weights that quantify the difference in temperature between pairs of galaxies, the effect was first detected by Hand et al. (2012) using CMB maps from the Acatama Cosmology Telescope (ACT). The detection of the kSZ effect has been further solidified using the same pairwise momentum estimator with other CMB data, including WMAP 9-year W-band data, and *Planck*’s four foreground-cleaned maps (Planck Collaboration Int. XXXVII 2016), and again more recently using a Fourier space analysis (Sugiyama et al. 2017). These measurements represent detections at

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the $2\text{--}3\sigma$ level. In addition, in [Planck Collaboration Int. XXXVII \(2016\)](#) the kSZ temperature map (δT) was estimated from *Planck* full-mission data and cross-correlated with the reconstructed linear velocity field data ($\mathbf{v} \cdot \hat{\mathbf{n}}$) from the Sloan Digital Sky Survey (SDSS-DR7) to compute the correlation function $\langle \Delta T(\mathbf{v} \cdot \hat{\mathbf{n}}) \rangle$. For this cross-correlation, $3.0\text{--}3.2\sigma$ detections were found for the foreground-cleaned *Planck* maps, and 3.8σ for the *Planck* 217-GHz map.

There has been a lot of previous work investigating how to use kSZ measurements to determine the peculiar velocity field. This idea was first proposed by [Haehnelt & Tegmark \(1996\)](#), suggesting that on small angular scales the peculiar velocities of clusters could be inferred from CMB observations. [Aghanim et al. \(2001\)](#) estimated the potential uncertainty of the kSZ measurements due to contamination by the primary CMB and thermal Sunyaev-Zeldovich (hereafter tSZ) effect. In [Holzapfel et al. \(1997\)](#), the peculiar velocities of two distant galaxy clusters, namely Abell 2163 ($z = 0.201$) and Abell 1689 ($z = 0.181$), were estimated through millimetre-wavelength observations (the SZ Infrared Experiment, SuZIE). Furthermore, [Benson et al. \(2003\)](#) estimated the bulk flow using six galaxy clusters at $z > 0.2$ from the SuZIE II experiment in three frequency bands between 150 and 350 GHz, constraining the bulk flow to be $< 1410 \text{ km s}^{-1}$ at 95% CL. In addition, [Kashlinsky & Atrio-Barandela \(2000\)](#) and [Kashlinsky et al. \(2008, 2009\)](#) estimated peculiar velocities on large scales and claimed a “dark flow” ($\gtrsim 1000 \text{ km s}^{-1}$) on Gpc scales. However, by combining galaxy cluster catalogues with *Planck* nominal mission foreground-cleaned maps, [Planck Collaboration Int. XIII \(2014\)](#) constrained the cluster velocity monopole to be $72 \pm 60 \text{ km s}^{-1}$ and the dipole (bulk flow) to be $< 254 \text{ km s}^{-1}$ (95% CL) in the CMB rest frame. This indicates that the Universe is largely homogeneous on Gpc scales, consistent with the standard Λ cold dark matter (Λ CDM) scenario with adiabatic initial conditions.¹

This work represents the third contribution of the *Planck*² Collaboration to the study of the kSZ effect. In [Planck Collaboration Int. XIII \(2014\)](#) we focused on constraining the monopole and dipole of the peculiar velocity field, which gives constraints on the large-scale inhomogeneity of the Universe. In the second paper, [Planck Collaboration Int. XXXVII \(2016\)](#), we calculated the pairwise momentum of the kSZ effect and cross-correlated this with the reconstructed peculiar velocity field ($\Delta T(\mathbf{v} \cdot \hat{\mathbf{n}})$), obtaining direct evidence of unbound gas outside the virial radii of the clusters. A follow-up paper modelled these results to reconstruct the baryon fraction and suggested that this unbound gas corresponds to *all* baryons surrounding the galaxies ([Hernández-Monteagudo et al. 2015](#)). Even though the large-scale bulk flow and monopole flow were not detected in [Planck Collaboration Int. XIII \(2014\)](#), the small-scale velocity dispersion in the nearby Universe, determined by the local gravitational potential field, might still be measurable. This is because the velocity of each

galaxy comprises two components, namely the bulk flow components, which reflect the large-scale perturbations, and a small-scale velocity dispersion component, which reflects perturbations due to the local gravitational potential (see, e.g., [Watkins et al. 2009](#); [Feldman et al. 2010](#); [Ma & Scott 2013, 2014](#)). Therefore, although the bulk flow of the galaxy clusters is constrained to be less than 254 km s^{-1} , the total velocity dispersion can still be large enough to be detected. With that motivation, in this paper we will look at a different aspect than in the previous two papers, namely focusing on 1-point statistics of *Planck* data to constrain the temperature and velocity dispersion due to the kSZ effect. This topic is relevant for large-scale structure, since the velocity dispersion that we are trying to measure can be used as a sensitive test for galaxy formation models ([Ostriker 1980](#); [Davies et al. 1983](#); [Kormendy & Bender 1996](#); [Kormendy 2001](#); [MacMillan et al. 2006](#)) and moreover, a numerical value for the small-scale dispersion often has to be assumed in studies of large-scale flows (e.g., [Ma et al. 2011](#); [Turnbull et al. 2012](#)). Providing such a statistical test through *Planck*’s full-mission foreground-cleaned maps is the main aim of the present paper.

This paper is organized as follows. In Sect. 2, we describe the *Planck* CMB data and the X-ray catalogue of detected clusters of galaxies. In Sect. 3, we discuss the filter that we develop to convolve the observational map, and the statistical methodology that we use for searching for the kSZ temperature dispersion signal. Then we present the results of our search along with relevant statistical tests. In Sect. 4, we discuss the astrophysical implications of our result, the conclusions being presented in the last section. Throughout this work, we adopt a spatially flat, Λ CDM cosmology model, with the best-fit cosmological parameters given by [Planck Collaboration XIII \(2016\)](#): $\Omega_{\text{m}} = 0.309$; $\Omega_{\Lambda} = 0.691$; $n_{\text{s}} = 0.9608$; $\sigma_8 = 0.809$; and $h = 0.68$, where the Hubble constant is $H_0 = 100h \text{ km s}^{-1} \text{ Mpc}^{-1}$.

2. Data description

2.1. *Planck* maps

2.1.1. Maps from the Planck Legacy Archive

In this work we use the publicly released *Planck* 2015 data.³ The kSZ effect gives rise to frequency-independent temperature fluctuations that are a source of secondary anisotropies. The kSZ effect should therefore be present in all CMB foreground-cleaned products. Here we investigate the four *Planck* 2015 foreground-cleaned maps, namely the *Commander*, *NILC*, *SEVEM*, and *SMICA* maps. These are the outputs of four different component-separation algorithms ([Planck Collaboration Int. XXXVII 2016](#)) and have a resolution of $\theta_{\text{FWHM}} = 5 \text{ arcmin}$. *SMICA* uses a spectral-matching approach, *SEVEM* adopts a template-fitting method to minimize the foregrounds, *NILC* is the result of an internal linear combination approach, and *Commander* uses a parametric, pixel-based Monte Carlo Markov chain technique to project out foregrounds ([Planck Collaboration XII 2014](#); [Planck Collaboration IX 2016](#); [Planck Collaboration X 2016](#)). All of these maps are produced with the intention of minimizing the foreground contribution, but there could nevertheless be some residual

¹ Although in principle one could still have an isocurvature perturbation on large scales ([Turner 1991](#); [Ma et al. 2011](#)).

² *Planck* (<http://www.esa.int/Planck>) is a project of the European Space Agency (ESA) with instruments provided by two scientific consortia funded by ESA member states and led by Principal Investigators from France and Italy, telescope reflectors provided through a collaboration between ESA and a scientific consortium led and funded by Denmark, and additional contributions from NASA (USA).

³ From the Planck Legacy Archive, <http://pla.esac.esa.int>.

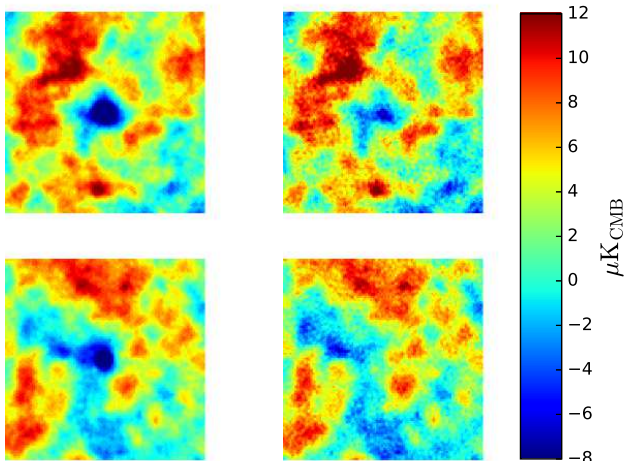


Fig. 1. *Top left:* Stack of the NILC CMB map in the directions of *Planck* SZ (PSZ) galaxy clusters. *Top right:* Stack of the 2D-ILC CMB map in the direction of PSZ galaxy clusters. This sample provides a very stringent test of the tSZ leakage, since the PSZ positions are the known places on the sky with detectable SZ signal. The stacked NILC CMB map clearly shows an excess in the centre, which is due to residual contamination from the tSZ effect, while the 2D-ILC CMB map has a signature in the centre that is consistent with the strength of other features in the stacked image. *Bottom left:* Stack of the NILC CMB map in the directions of MCXC clusters. *Bottom right:* Stack of the 2D-ILC CMB map in the direction of 1526 MCXC clusters (see Sect. 2.2 for the detail of the catalogue). For a different set of sky positions, the results are broadly consistent with those for the PSZ clusters. All these maps are $3^\circ \times 3^\circ$ in size, and use the same colour scale.

contamination from the tSZ effect, as well as other foregrounds (e.g., the Galactic kSZ effect, see [Waelkens et al. 2008](#)). We use the HEALPix package ([Górski et al. 2005](#)) to visualize and manipulate the maps.

2.1.2. The 2D-ILC map

The 2D-ILC *Planck* CMB map has the additional benefit of being constructed to remove contamination from the tSZ effect, provided that the tSZ spectral energy distribution is perfectly known across the frequency channels. The 2D-ILC CMB map has been produced by taking the *Planck* 2015 data and implementing the “constrained ILC” method developed in [Remazeilles et al. \(2011a\)](#). This component-separation approach was specifically designed to cancel out in the CMB map any residual of the tSZ effect towards galaxy clusters by using spectral filtering, as we now describe.

For a given frequency band i , the *Planck* observation map x_i can be modelled as the combination of different emission components:

$$x_i(\hat{\mathbf{r}}) = a_i s_{\text{CMB}}(\hat{\mathbf{r}}) + b_i s_{\text{tSZ}}(\hat{\mathbf{r}}) + n_i(\hat{\mathbf{r}}), \quad (2)$$

where $s_{\text{CMB}}(\hat{\mathbf{r}})$ is the CMB temperature anisotropy at pixel $\hat{\mathbf{r}}$, $s_{\text{tSZ}}(\hat{\mathbf{r}})$ is the tSZ fluctuation in the same direction, and $n_i(p)$ is a “nuisance” term including instrumental noise and

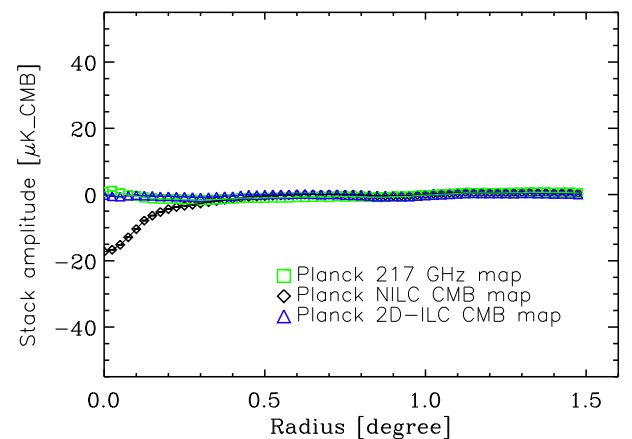
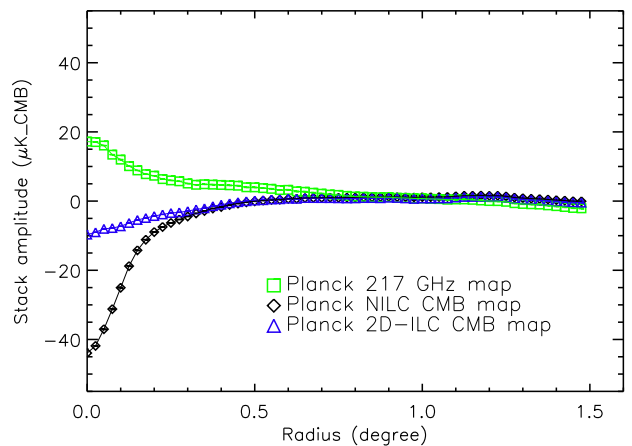


Fig. 2. Profiles for stacked patches (see Fig. 1) of the NILC CMB map (black diamonds) and the 2D-ILC CMB map (blue triangles) at the positions of PSZ clusters (*top panel*) and MCXC clusters (*bottom panel*). The profile of the stacked *Planck* 217-GHz map is also shown as a reference (green squares). The central deficit in the flux profile of the stacked NILC CMB map (black diamonds) is due to residual tSZ contamination.

Galactic foregrounds at frequency i . The CMB fluctuations scale with frequency through a known emission law parameterized by the vector \mathbf{a} , with nine components, accounting for the nine *Planck* frequency bands. The emission law of the tSZ fluctuations is also known and can be parameterized by the scaling vector \mathbf{b} in the *Planck* frequency bands. The kSZ signal is implicitly included in the CMB fluctuations, since CMB anisotropies and kSZ fluctuations share the same spectral signature.

Similar to the standard NILC method ([Basak & Delabrouille 2012, 2013](#)), the 2D-ILC approach makes a minimum-variance-weighted linear combination of the *Planck* frequency maps. Specifically $\hat{s}_{\text{CMB}}(\hat{\mathbf{r}}) = \mathbf{w}^\top \mathbf{x}(\hat{\mathbf{r}}) = \sum_{i=1}^9 w_i x_i(\hat{\mathbf{r}})$, under the condition that the scalar product of the weight vector \mathbf{w} and the CMB scaling vector \mathbf{a} is equal to unity, i.e., $\sum_{i=1}^9 w_i a_i = 1$, which guarantees the conservation of CMB anisotropies in the filtering. However, 2D-ILC ([Remazeilles et al. 2011a](#)) generalizes the standard NILC method by offering an additional constraint for the ILC weights to be orthogonal

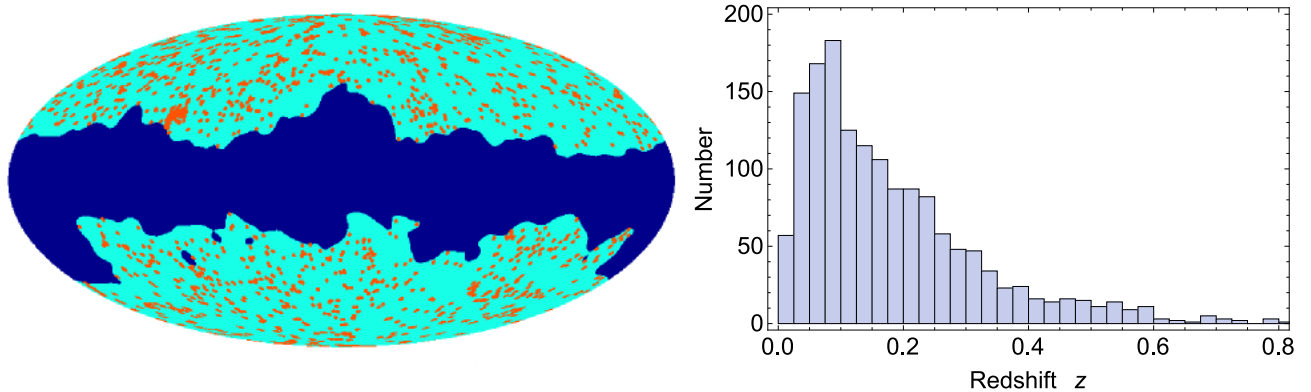


Fig. 3. *Left:* Full-sky distribution of 1526 MCXC X-ray clusters (Piffaretti et al. 2011; Planck Collaboration Int. XIII 2014) in Galactic coordinates. The dark blue area is the masked region, and the clusters are shown in orange. *Right:* Redshift histogram of 1526 X-ray clusters, with bin width $\Delta z = 0.025$.

to the tSZ emission law \mathbf{b} , while guaranteeing the conservation of the CMB component. The 2D-ILC CMB estimate is thus given by

$$\hat{s}_{\text{CMB}}(\hat{\mathbf{r}}) = \mathbf{w}^{\text{T}} \mathbf{x}(\hat{\mathbf{r}}), \quad (3)$$

such that the variance of Eq. (3) is minimized, with

$$\mathbf{w}^{\text{T}} \mathbf{a} = 1, \quad (4)$$

$$\mathbf{w}^{\text{T}} \mathbf{b} = 0. \quad (5)$$

Benefiting from the knowledge of the CMB and tSZ spectral signatures, the weights of the 2D-ILC are constructed in order to simultaneously yield unit response to the CMB emission law \mathbf{a} (Eq. 4) and zero response to the tSZ emission law \mathbf{b} (Eq. 5). The residual contamination from Galactic foregrounds and instrumental noise is controlled through the condition (Eq. 3). The exact expression for the 2D-ILC weights was derived in Remazeilles et al. (2011a) by solving the minimization problem (Eqs. 3, 4, and 5):

$$\hat{s}_{\text{CMB}}(\hat{\mathbf{r}}) = \frac{(\mathbf{b}^{\text{T}} \mathbf{C}_{\mathbf{x}}^{-1} \mathbf{b}) \mathbf{a}^{\text{T}} \mathbf{C}_{\mathbf{x}}^{-1} - (\mathbf{a}^{\text{T}} \mathbf{C}_{\mathbf{x}}^{-1} \mathbf{b}) \mathbf{b}^{\text{T}} \mathbf{C}_{\mathbf{x}}^{-1}}{(\mathbf{a}^{\text{T}} \mathbf{C}_{\mathbf{x}}^{-1} \mathbf{a}) (\mathbf{b}^{\text{T}} \mathbf{C}_{\mathbf{x}}^{-1} \mathbf{b}) - (\mathbf{a}^{\text{T}} \mathbf{C}_{\mathbf{x}}^{-1} \mathbf{b})^2} \mathbf{x}(\hat{\mathbf{r}}), \quad (6)$$

where $\mathbf{C}_{\mathbf{x}}^{ij} = \langle x_i x_j \rangle$ are the coefficients of the frequency-frequency covariance matrix of the *Planck* channel maps; in practice we compute this locally in each pixel p as

$$\mathbf{C}_{\mathbf{x}}^{ij}(p) = \sum_{p' \in \mathcal{D}(p)} x_i(p') x_j(p'). \quad (7)$$

Here the pixel domain $\mathcal{D}(p)$ (referred to as “super pixels”) around the pixel p is determined by using the following procedure: the product of frequency maps x_i and x_j is convolved with a Gaussian kernel in pixel space in order to avoid sharp edges at the boundaries of super pixels that would create spurious power (Basak & Delabrouille 2012, 2013).

Before applying the 2D-ILC filter (Eq. 6) to the *Planck* 2015 data, we first pre-process the data by performing point-source “inpainting” and wavelet decomposition, in order to optimize the foreground cleaning. In each *Planck* channel map we mask the point-sources detected at a signal-to-noise ratio (S/N) > 5 in the Second

Planck Catalogue of Compact Sources PCCS2 (Planck Collaboration XXVI 2016). The masked pixels are then filled in by interpolation with neighbouring pixels through a minimum curvature spline surface inpainting technique, as implemented in Remazeilles et al. (2015). This pre-processing of the point-source regions will guarantee reduction of the contamination from compact foregrounds in the kSZ measurement.

The inpainted *Planck* maps are then decomposed into a particular family of spherical wavelets called “needlets” (see, e.g., Narcowich et al. 2006; Guilloux et al. 2009). The needlet transform of the *Planck* maps is performed as follows. The spherical harmonic coefficients $a_{i, \ell m}$ of the *Planck* channel maps x_i are bandpass filtered in multipole space in order to isolate the different ranges of angular scales in the data. The 2D-ILC weights (Eq. 6) are then computed in pixel space from the inverse spherical harmonic transform of the bandpass-filtered $a_{i, \ell m}$ coefficients. The frequency-frequency covariance matrix in Eq. (7) is actually computed on the bandpass-filtered maps. In this way, component separation is performed for each needlet scale (i.e., range of multipoles) independently. Due to their localization properties, the needlets allow for a filtering in both pixel space and multipole space, therefore adapting the component-separation procedure to the local conditions of contamination in both spaces (see Delabrouille et al. 2009; Remazeilles et al. 2011b; Basak & Delabrouille 2012, 2013).

The upper left panel of Fig. 1 shows the result of stacking $3^\circ \times 3^\circ$ patches of the NILC *Planck* CMB map in the direction of known galaxy clusters, while the top right panel shows the result of stacking the 2D-ILC *Planck* CMB map in the direction of the same set of galaxy clusters.⁴ The *Planck* SZ sample provides a very stringent test, because these are the places on the sky where *Planck* detected a significant y signature. We see that stacking of the NILC CMB map shows a significant tSZ residual effect in the direction of galaxy clusters. Conversely, the stacking of the 2D-ILC *Planck* CMB map (right panel of Fig. 1) appears to show substantially reduced tSZ residuals, due to the 2D-ILC fil-

⁴ The *Planck* PSZ1 catalogue of galaxy clusters from the 2013 *Planck* data release has been used to determine the position of known SZ clusters.

tering. In the lower panels of Fig. 1 we show the results of the stacking procedure for the specific cluster catalogue that we will be using for the main analysis in this paper (see next section for details).

The profiles of the stacked patches are plotted in Fig. 2. The excess of power due to tSZ residuals in the NILC CMB map would clearly lead to a significant bias in any attempt to detect the kSZ signal at the positions of the galaxy clusters. As a baseline reference, the flux profile of the *Planck* 217-GHz map, stacked in the directions of these galaxy clusters, is also plotted in Fig. 2 (green squares). The tSZ signal should in principle vanish in observations at 217 GHz, since that is effectively the null frequency for the tSZ signature; in practice it is non-zero in the *Planck* 217-GHz map because of the broad spectral bandpass. In fact there is an offset of about $20 \mu\text{K}$ in the flux profile of the stacked 217-GHz map at the position of PSZ clusters. There is also still a residual offset in the 2D-ILC CMB map; however, it is smaller by a factor of about 2 than the tSZ signal in the baseline *Planck* 217-GHz map (see top panel of Fig. 2), and dramatically better than for the NILC map. This suggests that the method employed for the 2D-ILC map was successful in removing the tSZ signal.

The residual flux of the stacked 2D-ILC CMB map in the direction of galaxy clusters can be interpreted as the result of possibly imperfect assumptions in the 2D-ILC filter and the exact tSZ spectral shape across the *Planck* frequency bands. There may be several reasons behind incomplete knowledge of the tSZ spectrum: detector bandpass mismatch; calibration uncertainties; and also relativistic tSZ corrections. In addition, even if the kSZ flux is expected to vanish on average when stacking inward- and outward-moving clusters in a homogeneous universe, there is still a potential selection bias (since we use a selected subset of clusters for stacking) that may result in a non-zero average kSZ residual in the offset of the 2D-ILC map. Although it is not easy to estimate the size of all these effects, we are confident that they cannot be too large because the residual offset in the 2D-ILC map is negligible compared to the tSZ residuals in *Planck* CMB maps, and smaller by a factor of 2 with respect to the baseline *Planck* 217-GHz map.

Regarding residual Galactic foreground contamination, we checked that the angular power spectrum of the 2D-ILC CMB map on the 60% of the sky that is unmasked is consistent with the angular power spectrum of the *Planck* SMICA CMB maps. There is therefore no obvious excess of power due to Galactic emission. We also checked the amount of residual dust contamination of the kSZ signal on small angular scales in the direction of the galaxy clusters, where dusty star-forming galaxies are present (*Planck Collaboration Int. XLIII 2016*). Considering the *Planck* 857-GHz map as a dust template, we scaled it across the *Planck* frequency bands using a modified blackbody spectrum with best-fit values from *Planck Collaboration Int. XLIII (2016)*, i.e., $\beta = 1.5$ and $T = 24.2\text{K}$. This provides dust maps at each frequency band. We then applied the ILC weights that go into the 2D-ILC CMB+kSZ map (Eq. 6) to the thermal dust maps. This provides an estimate of the map of the residual dust contamination in the 2D-ILC map. We then stacked the residual dust map in the direction of the galaxy clusters from either the PSZ or the MCXC catalogue, and computed the profile of the stacked patch as in Fig. 2. We found that the residual flux from the dust

stacked in the direction of the galaxy clusters is compatible with zero.

Residual cosmic infrared background (hereafter CIB) and instrumental noise in the CMB maps will add some scatter to the measured kSZ signals in the directions of galaxy clusters, but should not lead to any bias in the stacked profile. However, any additional source of extra noise will lead to bias in the variance of the stacked profile. Since CIB and noise are not spatially localized on the sky (unlike kSZ and tSZ signals) this bias can be estimated using off-cluster positions, e.g., for the matched-filtering analysis performed in Sect. 3.2.

In order to quantify the amount of residual noise in the 2D-ILC CMB map, we apply the 2D-ILC weights (calculated from the *Planck* full-survey maps) to the first and second halves of each stable pointing period (also called “rings”). In the half-difference of the resulting “first” and “second” 2D-ILC maps, the sky emission cancels out, therefore leaving an estimate of the noise contamination in the 2D-ILC CMB maps, constructed from the full-survey data set.

The 2D-ILC CMB map shows approximately 10% more noise than the NILC CMB map; this arises from the additional constraint imposed in the 2D-ILC of cancelling out the tSZ emission. At the cost of having a slightly higher noise level, the 2D-ILC CMB map benefits from the absence of bias due to tSZ in the directions of galaxy clusters. For this reason, the 2D-ILC CMB map is particularly well suited for the extraction of the kSZ signal in the direction of galaxy clusters and we shall focus on it for the main results of this paper.

2.2. The MCXC X-ray catalogue

To trace the underlying baryon distribution, we use the Meta Catalogue of X-ray detected Clusters of galaxies (MCXC), which is an all-sky compilation of 1743 all-sky ROSAT survey-based samples (BCS, *Ebeling et al. 1998, 2000*; CIZA, *Ebeling et al. 2010*; Kocevski et al. 2007; MACS, *Ebeling et al. 2007*; NEP, *Henry et al. 2006*; NORAS, *Böhringer et al. 2000*; REFLEX, *Böhringer et al. 2004*; SCP, *Cruddace et al. 2002*) along with a few other catalogues (160SD, *Mullis et al. 2003*; 400SD, *Burenin et al. 2007*; EMSS, *Gioia & Luppino 1994*; *Henry 2004*; SHARC, *Romer et al. 2000*; *Burke et al. 2003*; WARPS, *Perlman et al. 2002*; *Horner et al. 2008*). We show stacks and profiles for this catalogue on the *Planck* map in Figs. 1 and 2. While selecting sources from this catalogue, we use the luminosity within R_{500} (the radius of the cluster within which the density is 500 times the cosmic mean density), L_{500} , and restrict the samples to have $1.5 \times 10^{33} \text{W} < L_{500} < 3.7 \times 10^{38} \text{W}$ within the band 0.1–2.4 keV (see *Piffaretti et al. 2011*). As well as L_{500} , for each cluster the catalogue gives M_{500} , the mass enclosed within R_{500} at redshift z , i.e., $M_{500} = (4\pi/3)500\rho_{\text{crit}}(z)R_{500}^3$, estimated using the empirical relation $L_{500} \propto M_{500}^{1.64}$ in *Arnaud et al. (2010)*. Further details of catalogue homogenization and calibration are described in *Piffaretti et al. (2011)* and *Planck Collaboration Int. XIII (2014)*.

For each cluster in the MCXC catalogue, the properties we use in the rest of this paper are the sky position (Galactic coordinates l, b), the redshift z , and the mass M_{500} . In Sect. 4 we will use M_{500} and z to estimate the optical depth for each cluster.

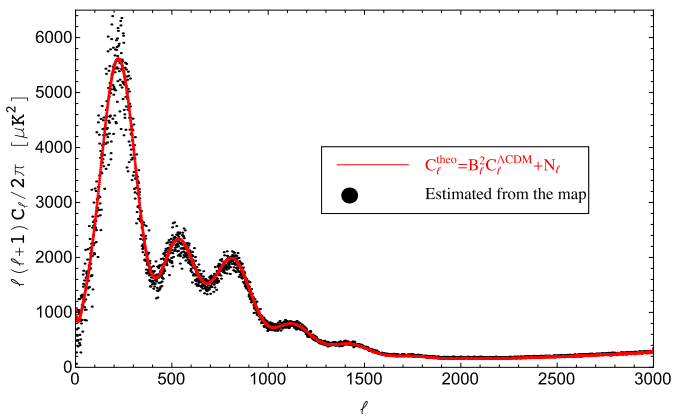


Fig. 4. Measured (black dots) and predicted (red line) power spectra from the *Planck* 2D-ILC map. The predicted spectrum is based on the best-fitting Λ CDM model convolved with the squared beam B_ℓ^2 , with the noise added. These are estimated using the pseudo- C_ℓ estimator described in Hivon et al. (2002).

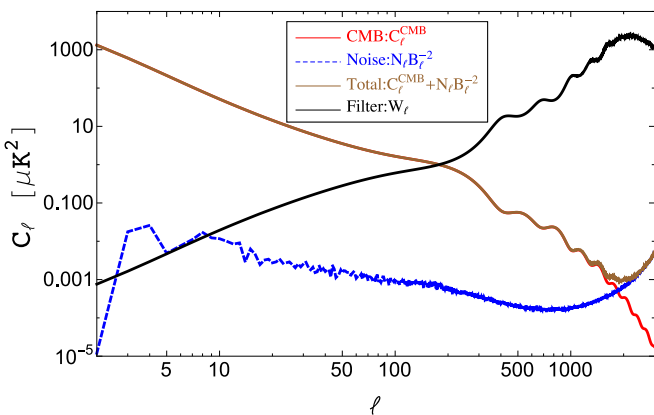


Fig. 5. Optimal matched filter (black line) for point-source detection in the *Planck* 2D-ILC map (Eq. 14). For comparison, the power spectra of the CMB signal (red line) and noise map (blue dashed line) are shown, along with their sum (brown line).

Since in the CMB map, the Galactic plane region is highly contaminated by foreground emission, we use the *Planck* Galactic and point-source mask to remove 40% of the sky area. The number of MCXC sources outside the sky mask is $N_c = 1526$ (which we use throughout the paper) and their spatial and redshift distributions are shown in Fig. 3. The full-sky distribution is presented in the left panel of Fig. 3, and one can see that the distribution of MCXC clusters is roughly uniform outside the Galactic mask. The redshift of MCXC clusters peaks at $z = 0.09$, with a long tail towards higher redshift, $z \gtrsim 0.4$.

3. Methodology and statistical tests

3.1. Matched-filter technique

The foreground-cleaned CMB maps (SEVEM, SMICA, NILC, Commander, and 2D-ILC) contain mainly the primary CMB and kSZ signals, so in order to optimally characterize the kSZ signal, we need to use a spatial filter to convolve the

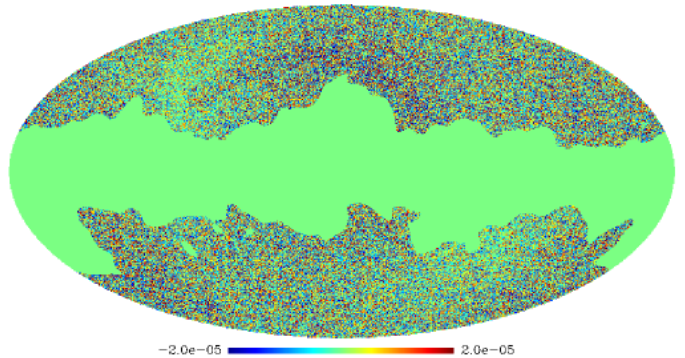


Fig. 6. Filtered (with Eq. 14) and masked 2D-ILC map in dimensionless units (i.e., $\Delta T/T$).

maps in order to downweight the CMB signal. Here we use the matched-filter technique (e.g., Tegmark & de Oliveira-Costa 1998; Ma et al. 2013), which is an easily implemented approach for suppressing the primary CMB and instrumental noise.

Most of *Planck*'s SZ-clusters are unresolved, so we treat them as point sources on the sky. In this limit, if cluster i has flux S_i at sky position \hat{r}_i , the sky temperature $\Delta T(\hat{r})$ can be written as

$$\Delta T(\hat{r}) = c \sum_j S_j \delta(\hat{r}, \hat{r}_j) + \sum_{\ell m} a_{\ell m} Y_{\ell m}(\hat{r}), \quad (8)$$

where δ is the Dirac delta function, c is the conversion factor between flux and temperature, and the spherical harmonics characterize the true CMB fluctuations. The sky signal, obtained from the *Planck* telescope is

$$\begin{aligned} \Delta T^{\text{obs}}(\hat{r}) &= c \sum_j S_j \left(\sum_{\ell} \frac{2\ell+1}{4\pi} P_{\ell}(\hat{r} \cdot \hat{r}_j) B_{\ell} \right) \\ &+ \sum_{\ell m} a_{\ell m}^{\text{noise}} Y_{\ell m}(\hat{r}), \end{aligned} \quad (9)$$

where $a_{\ell m}^{\text{noise}}$ is the true CMB signal convolved with the beam plus the detector noise, i.e., $a_{\ell m}^{\text{noise}} = B_{\ell} a_{\ell m}^{\text{CMB}} + n_{\ell m}$ (assuming that this is the only source of noise). The beam function of *Planck* foreground-cleaned maps in ℓ -space is close to a Gaussian with $\theta_{\text{FWHM}} = 5$ arcmin, i.e., $B_{\ell} = \exp(-\ell^2 \sigma_b^2/2)$, with $\sigma_b = \theta_{\text{FWHM}}/\sqrt{8 \ln 2}$. Residual foregrounds in the *Planck* CMB maps and in the 2D-ILC CMB map have been minimized in the component-separation algorithms, as demonstrated in Planck Collaboration IX (2016) for the public *Planck* CMB maps and in Planck Collaboration Int. XIII (2014) for the 2D-ILC CMB map. Figure 4 compares the angular power spectrum, C_ℓ , directly estimated from the map by using the pseudo- C_ℓ estimator (Hivon et al. 2002), and the spectrum predicted by using the best-fit Λ CDM model and noise template. One can see that the measured spectral data scatter around the predicted spectrum, and that the two spectra are quite consistent with each other.

Table 1. Statistics of the values of $(\Delta T/T) \times 10^5$ at the true 1526 cluster positions and for 1526 randomly-selected positions.

	True positions	Random positions
Mean	-0.015	-0.021
Variance	1.38	1.23
Skewness	0.37	0.09
Kurtosis	4.44	3.29

In order to maximize our sensitivity to SZ clusters, we further convolve $\Delta T^{\text{obs}}(\hat{r})$ with an optimal filter W_ℓ :

$$\Delta \tilde{T}(\hat{r}) = c \sum_j S_j \left(\sum_\ell \frac{2\ell+1}{4\pi} P_\ell(\hat{r} \cdot \hat{r}_j) B_\ell W_\ell \right) + \sum_{\ell m} a_{\ell m}^{\text{noise}} W_\ell Y_{\ell m}(\hat{r}), \quad (10)$$

where we are seeking the form of W_ℓ that will maximize cluster signal-to-noise ratio. In the direction of each cluster, the filtered signal is

$$\Delta \tilde{T}_c(\hat{r}_j) = c S_j \left[\sum_\ell \left(\frac{2\ell+1}{4\pi} \right) B_\ell W_\ell \right] \equiv (c S_j) A, \quad (11)$$

and we want to vary W_ℓ to minimize the ratio

$$\sigma^2 = \text{Var} \left(\frac{\Delta \tilde{T}_{\text{noise}}}{A} \right) = \frac{\sum_\ell \frac{2\ell+1}{4\pi} C_\ell^{\text{noise}} W_\ell^2}{\left(\sum_\ell \frac{2\ell+1}{4\pi} B_\ell W_\ell \right)^2}, \quad (12)$$

where $C_\ell^{\text{noise}} \equiv B_\ell^2 C_\ell^{\text{CMB}} + N_\ell$, and we take C_ℓ^{CMB} to be the Λ CDM model power spectrum. Since A in Eq. (11) is a constant, we minimize Eq. (12) by adding a Lagrange multiplier to the numerator (see, e.g., Ma et al. 2013), i.e., we minimize

$$\sum_\ell \frac{2\ell+1}{4\pi} C_\ell^{\text{noise}} W_\ell^2 - \lambda \left(\sum_\ell \frac{2\ell+1}{4\pi} B_\ell W_\ell \right)^2. \quad (13)$$

We then obtain

$$W_\ell = \frac{B_\ell}{B_\ell^2 C_\ell^{\text{CMB}} + N_\ell} = \frac{B_\ell}{C_\ell^{\text{noise}}}, \quad (14)$$

which we plot in Fig. 5 as a black line, along with the primary CMB C_ℓ , the noise map, and their sum. One can see that the filter function W_ℓ gives lower weight in the primary CMB domain while giving more weight in the cluster regime, $\ell \gtrsim 2000$. We then convolve the five *Planck* foreground-cleaned maps with this W_ℓ filter, noting that the noise power spectrum N_ℓ in Eq. (14) of each foreground-cleaned map is estimated by using its corresponding noise map. After we perform this step, the primary CMB features are highly suppressed (Fig. 6), and the whole sky looks essentially like a noisy map, although it still contains the kSZ information of course.

3.2. Statistical method and tests of robustness

We now proceed to estimate the kSZ temperature dispersion and perform various tests. The filtered map contains

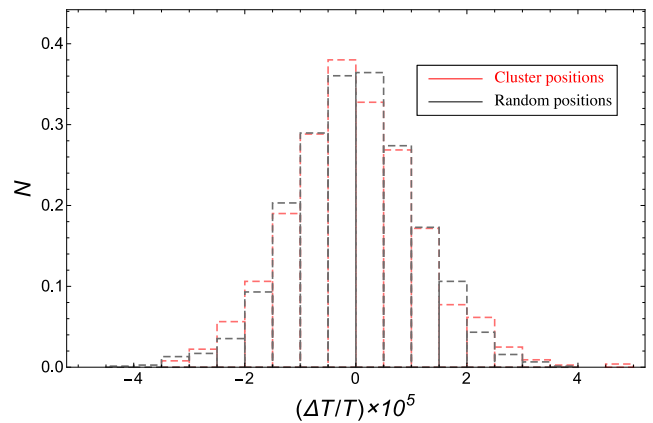


Fig. 7. The histograms of 1526 $\Delta T/T$ values of 2D-ILC map at the cluster catalogue positions (red bars), and randomly selected positions (black bars). The statistics of the true cluster positions and random positions can be found in Table 1.

Table 2. Rms values for the true sky positions of 1526 MCXC catalogue clusters (σ_{MCXC}), along with the mean (σ_{ran}) and scatter ($\sigma(\sigma_{\text{ran}})$) of the values of the rms for 5000 random catalogues, where each catalogue consists of 1526 random positions on the sky.

Map	$\sigma_{\text{MCXC}} \times 10^5$	$\sigma_{\text{ran}} \times 10^5$	$\sigma(\sigma_{\text{ran}}) \times 10^5$
2D-ILC	1.17	1.10	0.022
SMICA	1.11	0.97	0.019
NILC	1.09	0.97	0.019
SEVEM	1.12	1.00	0.020
Commander	1.09	1.03	0.020

the kSZ signal and residual noise, and from this we plot the histogram of 1526 $\Delta T/T$ values at the cluster positions (see red bars in Fig. 7). We can also randomly select the same number of pixels on the sky and plot a histogram for that. The two histograms have almost zero mean value (Table 1), but in the real cluster positions yield a larger variance than the random selections, i.e., the real cluster positions give a slightly broader distribution than for the randomly selected positions (Table 1). We also show results for the skewness and kurtosis of the two samples in Table 1, and one can see that for these statistics the real cluster positions also give larger values than for the randomly-selected positions. This suggests that there may be additional tests that could be performed to distinguish the real cluster kSZ signals; however, we leave that for future studies, and for the rest of this paper we just focus on investigating whether the slight broadening of the distribution is due to the kSZ effect.

3.2.1. Test of thermal Sunyaev-Zeldovich effect residuals

The first test we want to perform is to check whether the measured kSZ ($\Delta T/T$) value at each cluster position suffers from residuals of the tSZ effect. The mapmaking procedures of SMICA, NILC, SEVEM, and Commander minimize the variance of all non-CMB contribution to the map, but they are not designed to null the tSZ component. By contrast, the 2D-ILC map is designed to also null the tSZ contribution,

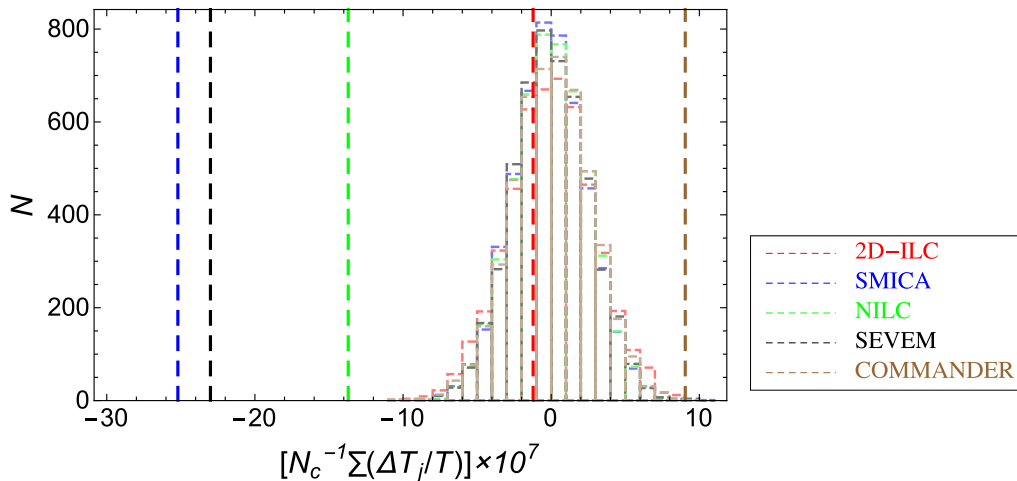


Fig. 8. Histogram of the $N_c^{-1} \sum_j (\Delta T_j / T)$ values of 5000 random catalogues on the sky (each having $N_c = 1526$), with different colours representing different *Planck* foreground-cleaned maps. The 68% width of the 2D-ILC, SMICA, NILC, SEVEM, and Commander histograms are 2.86, 2.49, 2.48, 2.53, 2.62 ($\times 10^{-7}$), respectively. The vertical lines represent the average $\Delta T / T$ values at true MCXC cluster positions for each map. One can see that only for the 2D-ILC map is this value within the 68% range of the random catalogue distribution, while others are quite far off. This indicates that, except for the 2D-ILC map, the public *Planck* maps have residual tSZ contamination at the cluster positions.

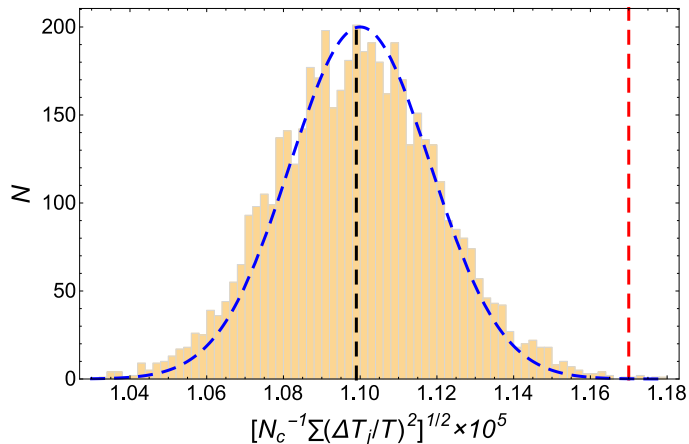


Fig. 9. Distribution of the rms for 5000 mock catalogues (yellow histogram); here each catalogue consists of N_c randomly chosen positions on the filtered 2D-ILC map. The mean and rms of the 5000 random catalogues are 1.10×10^{-5} and 2.15×10^{-7} , respectively (shown as the black dashed vertical line and the solid black arrow). For the N_c true MCXC cluster positions, the rms is 1.17×10^{-5} (red vertical dashed line).

and therefore should provide a cleaner measurement of the kSZ effect (but with a slightly higher noise level).

We first choose 5000 randomly selected catalogues from each *Planck* foreground-cleaned map, each being a collection of 1526 random positions on the sky. We then calculate the average value of $(\Delta T / T)$ for each random catalogue and plot the resulting histograms in Fig. 8. The five different colours of (overlapping) histogram represent the different *Planck* maps. One can see that they are all centred on zero, with approximately the same widths. Since the 2D-ILC map has nulled the tSZ component in the map, it does not minimize the variance of all foreground components and as a result, its width in Fig. 8 (2.86) is slightly larger than for all

other maps; in these units, the 1σ width of the histograms for SMICA, NILC, SEVEM and Commander are 2.49, 2.48, 2.53, and 2.62, respectively. This indicates that the noise level in the filtered 2D-ILC map is slightly higher than for the other four maps.

We then calculate the average value of $\Delta T / T$ at the true cluster positions for the five *Planck* foreground-cleaned maps as the vertical bars in Fig. 8. One can see that only the average value of the 2D-ILC map lies close to zero and within the 68% width of the noise histogram, while the values of all other maps are quite far from the centre of the noise distribution. This strongly suggests that at each of the true cluster positions the $(\Delta T / T)$ value contains some contribution from the tSZ effect, so that the tSZ effect contributes extra variance to the foreground-cleaned maps.

3.2.2. Test with random positions

We now want to test whether this slight broadening of the distribution is a statistically significant consequence of the kSZ effect. So for the 5000 randomly selected catalogues, we calculate the scatter of the 1526 $(\Delta T / T)$ values. We then plot (in Fig. 9) the histogram of 5000 rms values of these random catalogues, and mark the rms value of the true MCXC cluster positions for reference. One can see that the mean of the 5000 rms values of the random catalogues is 1.10×10^{-5} , and that the scatter of the 5000 rms values of the random catalogue has a width around 2.15×10^{-7} . The rms value of the 1526 true MCXC position is 1.17×10^{-5} , larger than the mean value at more than the 3σ level.

In Table 2, we list the rms value for the true sky positions of the 1526 MCXC catalogue sources (σ_{MCXC} , the mean (σ_{ran}), and standard deviation ($\sigma(\sigma_{\text{ran}})$) for 5000 random catalogues for different foreground-cleaned maps. One can see that although the absolute value of each map varies somewhat, the second column (σ_{ran}) is consistently smaller than the first column (σ_{MCXC}) by roughly $0.07\text{--}0.13 \times 10^{-5}$, which, specifically for 2D-ILC is about 3 times the scatter

Table 3. Same as Table 2 for the 2D-ILC map, but changing the assumed size of the clusters in the filtering function (Eq. 14).

	$\sigma_{\text{MCXC}} \times 10^5$	$\sigma_{\text{ran}} \times 10^5$	$\sigma(\sigma_{\text{ran}}) \times 10^5$
Point source . . .	1.17	1.10	0.022
3 arcmin	1.19	1.12	0.022
5 arcmin	1.26	1.19	0.023
7 arcmin	1.42	1.36	0.026

of the rms among catalogues ($\sigma(\sigma_{\text{ran}})$). This consistency strongly suggests that the kSZ effect contributes to the extra dispersion in the convolved $\Delta T/T$ maps at the cluster positions (since the 2D-ILC map is constructed to remove the tSZ effect). If we use the SMICA, SEVEM, NILC, and Commander maps, the detailed values will vary slightly due to the different calibration schemes of the maps, but the detection remains consistently there. The difference between σ_{MCXC} and σ_{ran} is slightly larger in the SMICA, NILC, and SEVEM maps due to residual tSZ contamination, shown as the vertical bars in Fig. 8.

This all points towards the broadening of the $\Delta T/T$ histogram being a consequence of the kSZ effect; hence we identify it as additional temperature dispersion arising from the scatter in cluster velocities detected through the kSZ effect. In Sect. 4, we will interpret this effect in terms of the line-of-sight velocity dispersion of the SZ clusters, which is an extra variance predicted in linear perturbation theory in the standard picture of structure formation (Peebles 1980).

3.2.3. Test with finite cluster size

We now want to test how much our results depend on the assumption that SZ clusters are point sources. A cluster on the sky appears to have a radius of θ_{500} , which is equal to $\theta_{500} = R_{500}/D_A$, where R_{500} is the radius from the centre of the cluster at which the density contrast is equal to 500 and D_A is the angular diameter distance to the cluster. The peak in the distribution of θ_{500} values for the MCXC clusters lies at around 3 arcmin, so we multiply the filter function (Eq. 14) with an additional ‘‘cluster beam function’’ $B_\ell^c = \exp(-\ell^2 \sigma_b^2/2)$, where $\sigma_b = \theta_{500}/\sqrt{8 \ln 2}$. We pick three different values for the cluster size, namely $\theta_{500} = 3, 5,$ and 7 arcmin, and see how our results change.

We list our findings in Table 3; one can see that the detailed values for three cases are slightly different from those of the point-source assumptions, but the changes are not dramatic. More importantly, the offsets between σ_{MCXC} and σ_{ran} stay the same for various assumptions of cluster size. Therefore the detection of the temperature dispersion due to the kSZ effect does not strongly depend on the assumption of clusters being point sources.

3.3. Statistical results

3.3.1. Statistics with the uniform weight

We now want to perform a more quantitative calculation of the significance of detection. Since the convolved map mainly consists of the kSZ signal at the cluster positions plus residual noise, we write the observed temperature fluctuation at the cluster positions as

Table 4. Statistics of the variables \hat{s}^2 due to the kSZ effect for different CMB maps.

Map	$E[s^2] \times 10^{11}$	$(V[s^2])^{1/2} \times 10^{11}$	S/N
2D-ILC	1.64	0.48	3.4
SMICA	3.53	0.37	9.4
NILC	2.75	0.38	7.3
SEVEM	3.19	0.40	8.1
Commander	1.47	0.42	3.5

Table 5. Statistics of the weighted variables \hat{s}_w^2 for different choices of weights in the 2D-ILC map. We use both linear and squared weights for each of optical depth, luminosity, mass, and $\theta_{500} = R_{500}/D_A$, where D_A is the angular diameter distance of the cluster. The third column lists the frequency $P(s_w^2 < 0)$ of finding a value of s_w^2 smaller than zero, and the fourth column lists the equivalent signal-to-noise ratio (see Appendix C).

Weight	$E[s_w^2] \times 10^{11}$	$(V[s_w^2])^{1/2} \times 10^{11}$	$P(s_w^2 < 0)$	S/N
Uniform	1.64	0.48	0.07%	3.2
τ	1.65	0.50	0.11%	3.1
τ^2	1.62	0.55	0.38%	2.7
θ_{500}	3.33	0.64	0.02%	3.5
θ_{500}^2	6.86	1.72	0.39%	2.7
L_{500}	1.34	0.91	6.94%	1.5
L_{500}^2	0.65	2.15	32.4%	0.5
M_{500}	1.91	0.65	0.43%	2.6
M_{500}^2	1.81	1.36	8.75%	1.4

tuation at the cluster positions as

$$\left(\frac{\Delta T}{T}\right) \equiv \delta = s + n, \quad (15)$$

where δ , s , and n represent the observed $\Delta T/T$ value, the kSZ signal contribution, and the residual noise, respectively, all of which are dimensionless quantities. Now we define the estimator \hat{s}^2 as

$$\hat{s}^2 = \frac{1}{N_c} \sum_i \delta_i^2 - \frac{1}{N_c} \sum_i \hat{n}_i^2, \quad (16)$$

where the summation includes all of the $N_c = 1526$ cluster positions. For the first term δ_i , we use the N_c true cluster position as the measurement of each observed $\Delta T/T$. For the second term, we randomly select N_c pixels outside the Galactic and point-source mask that are *not* cluster positions. The calculation of the first term is fixed, whereas the second term depends on the N_c random positions we choose. Each randomly selected set of N_c positions corresponds to a mock catalogue, which leads to one value of s^2 . We do this for 5000 such catalogues, where each mock catalogue has a different noise part (\hat{n}_i) in Eq. (16), but the same observed δ_i . Then we plot the histogram of s^2 values for these catalogues in the left panel of Fig. 10. One can see that the s^2 distribution is close to a Gaussian distribution with mean and error being $s^2 = (1.64 \pm 0.48) \times 10^{-11}$.

One can use a complementary method to obtain the mean and variance of \hat{s}^2 , i.e., $E[s^2]$ and $V[s^2]$. We lay out

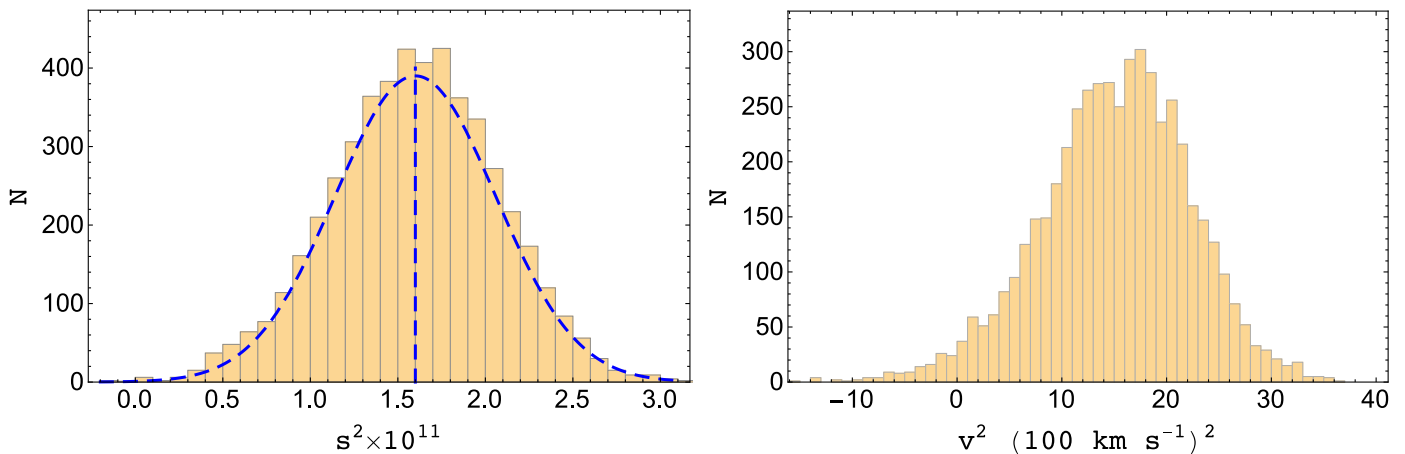


Fig. 10. *Left*– Distribution of 5000 values of s^2 with uniform weight (Eq. 16) on each position for the 2D-ILC map. *Right*– Distribution of v^2 calculated from Eq. (28), $P(v^2 < 0) = 2.48\%$. We have tested with 50000 values of s^2 and the results are consistent with 5000 values.

this calculation in Appendix A, where we directly derive these results:

$$\begin{aligned} E[s^2] &= \overline{\delta^2} - \mu_2(n); \\ V[s^2] &= \frac{1}{N_c} [\mu_4(n) - \mu_2^2(n)]. \end{aligned} \quad (17)$$

Here μ_2 and μ_4 are the second and fourth moments of the corresponding random variables.

For the moments of δ , we use the measurements at the 1526 cluster positions. For the estimate of the noise, we take all of the unmasked pixels of the convolved sky. In order to avoid selecting the real cluster positions, we remove all pixels inside a 10 arcmin aperture around each cluster. These “holes” at each cluster position constitute a negligible portion of the total unmasked pixels, and our results are not sensitive to the aperture size we choose. As a result, we have approximately 3×10^7 unmasked pixels to sample the noise. We then substitute the values into Eq. (17) to obtain the expectation values and variances.

In Table 4, we list the mean and rms value of $\widehat{s^2}$. Comparing with the 2D-ILC map, one can see that the SMICA, NILC, and SEVEM maps give larger values of $E[s^2]$ and therefore apparently higher significance levels, which we believe could be due to the fact that the residual tSZ effect in these maps contributes to the signal. However, the Commander map gives a reasonable estimate of the dispersion, since it appears to be less contaminated by tSZ residuals (see Fig. 8). As discussed in Sect. 2.1.2, the mapmaking procedure of the 2D-ILC product enables us to null the tSZ effect so that the final map should be free of tSZ, but with larger noise. This is the reason that we obtain a somewhat lower significance in Table 4 for 2D-ILC compared to some of the other maps. We will therefore mainly quote this conservative detection in the subsequent analysis.

3.3.2. Statistics with different weights

The results so far have been found using the same weights for each cluster position. We now examine the stability of the detection using weighted stacking. In Eq. (16) we defined stacking with uniform weights, which can be general-

ized to

$$\widehat{s_w^2} = \frac{\sum_i (\delta_i^2 - \widehat{n}_i^2) w_i}{\sum_i w_i}, \quad (18)$$

where w_i is the weight function. We certainly expect “larger” clusters to contribute more to the signal, but it is not obvious what cluster property will be best to use. In Table 5, we try different weighting functions w_i , with the first row being the uniform weight, which is equivalent to Eq. (16). In addition, we try as different choices of weighting function the optical depth τ and its square τ^2 ,⁵ the angular size θ_{500} and its square θ_{500}^2 , the luminosity L_{500} and its square L_{500}^2 , and the mass M_{500} and its square M_{500}^2 . Since some of these may give distributions of s_w^2 that deviate from Gaussians, we also calculate the frequencies for finding s_w^2 smaller than zero, $P(s_w^2 < 0)$. The smaller this P -value is, the more significant is the detection.

From Table 5, we see that most weighting choices are consistent with uniform weighting though with reduced significance of the detection, the exceptions being the choices of θ_{500} or θ_{500}^2 . For $w_i = \theta_{500,i}$ and $w_i = \theta_{500,i}^2$, we have P -values of 0.0002 and 0.0028, respectively, yielding (1-sided) significance levels of 3.5σ and 2.7σ . Their distributions deviate slightly from a Gaussian, with a tail toward smaller values.

The increased detection of excess variance using θ_{500} weighting stems from our choice of using a single cluster beam function for all clusters. In Sect. 3.2.3 we tested the robustness of our results to the choice of cluster beam function, finding little dependence. Nevertheless, such a test assumed all clusters had the same angular size, while in reality there is a large spread in the angular sizes of the clusters. By weighting with θ_{500} we are able to recover some of this lost signal in a quick and simple way, which we tested by comparing results for larger clusters versus smaller clusters. Despite this, it we find that the increased significance is mainly due to the increased value for $E[s_w^2]$ and not a decrease in the noise. This tension may be evidence of systematic effects in the data, which should be further investigated when better data become available.

⁵ The calculation of optical depth is shown in Sect. 4, and Eq. (27) in particular.

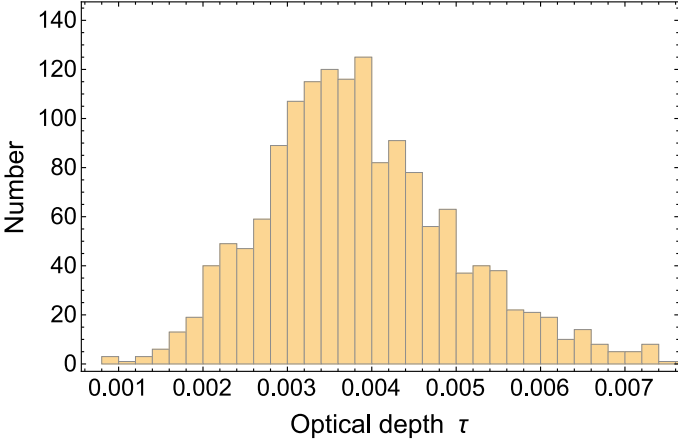


Fig. 11. Histogram of the optical depth τ derived using Eq. (27) for 1526 X-ray cluster positions.

4. Implications for the peculiar velocity field

We now want to investigate what the temperature dispersion indicates for the variance of the peculiar velocity field. As shown in Eq. (1), the dimensionless temperature fluctuation is different from the dimensionless velocity field through the line-of-sight optical depth factor τ . Since the coherence length of the velocity field is order $100 h^{-1}$ Mpc (Planck Collaboration Int. XXXVII 2016), i.e., much larger than the size of a cluster, the velocity can be taken out of the integral, giving

$$\frac{\Delta T(\hat{r})}{T} = \left(-\frac{\mathbf{v} \cdot \hat{r}}{c} \right) \tau, \quad \text{with } \tau = \sigma_T \int_0^{+\infty} n_e dl. \quad (19)$$

In order to convert the kSZ signal into a line-of-sight velocity we therefore need to obtain an estimate of τ for each cluster. In Planck Collaboration Int. XIII (2014), the values calculated are explicitly given as the optical depth per solid angle, obtained based on two scaling relations from Arnaud et al. (2005) and Arnaud et al. (2010). Here we adopt a slightly different approach, which is to determine the τ value at the central pixel of each galaxy cluster.

Many of the previous studies of the tSZ effect have used the “universal pressure profile” (UPP, Arnaud et al. 2010; Planck Collaboration Int. V 2013) and isothermal β model (Cavaliere & Fusco-Femiano 1976, 1978) to model the pressure and electron density profiles of the clusters (Grego et al. 2000; Benson et al. 2003, 2004; Hallman et al. 2007; Halverson et al. 2009; Plagge et al. 2010). Because the UPP is just a fitting function for pressure, it is difficult to separate out the electron density and the temperature unless we use the isothermal assumption. In fact, Battaglia et al. (2012) demonstrated that the UPP is not absolutely universal, and that feedback from an active galactic nucleus can change the profile in a significant way. The functional form of the β model can be derived from a parameterization of density under the assumption of isothermality of the profile (e.g., Sarazin 1986). However, since isothermality is a poor assumption for many clusters (Planck Collaboration Int. V 2013), we only consider the β model here as a fitting function. Measurements of cluster profiles from the South Pole Telescope (SPT) have found that the index $\beta = 0.86$ provides the best fit to the profiles of SZ clusters (Plagge et al. 2010), and therefore we use this value of β in the following discussion.

The electron density can be written as

$$n_e(r) = \frac{n_{e0}}{\left[1 + (r/r_c)^2 \right]^{3\beta/2}}, \quad (20)$$

where $r_c = r_{\text{vir}}/c$ is the core radius of each cluster, with c being the concentration parameter. Here we adopt the formula from Duffy et al. (2008) and Komatsu et al. (2011) to calculate the concentration parameter given the redshift and halo mass of the cluster:

$$c = \frac{5.72}{(1+z)^{0.71}} \left(\frac{M_{\text{vir}}}{10^{14} h^{-1} M_{\odot}} \right)^{-0.081}. \quad (21)$$

In the catalogue, M_{500} and redshift z are given, so one can use these two quantities to calculate the virial mass M_{vir} of the cluster. The calculation is contained in Appendix B.

The radius r_{vir} is calculated through

$$M_{\text{vir}} = \frac{4\pi}{3} [\Delta(z)\rho_c(z)] r_{\text{vir}}^3, \quad (22)$$

where $\rho_c(z)$ is the critical density of the Universe at redshift z , and $\Delta(z)$ depends on Ω_m and Ω_{Λ} as (Bryan & Norman 1998)

$$\Delta(z) = 18\pi^2 + 82[\Omega(z) - 1] - 39[\Omega(z) - 1]^2, \quad (23)$$

with $\Omega(z) = \Omega_m(1+z)^2 / [\Omega_m(1+z)^3 + \Omega_{\Lambda}]$. Thus,

$$\tau = (\sigma_T n_{e0} r_c) f_1(\beta),$$

$$f_1(\beta) = \int_{-\infty}^{+\infty} \frac{dx}{(1+x^2)^{3\beta/2}} = \frac{\sqrt{\pi} \Gamma(-\frac{1}{2} + \frac{3}{2}\beta)}{\Gamma(\frac{3}{2}\beta)}, \quad (24)$$

where Γ is the usual gamma function. To determine n_{e0} , we use $4\pi \int_0^{r_{500}} n_e(r) r^2 dr = N_e$, where

$$N_e = \left(\frac{1 + f_H}{2m_p} \right) f_{\text{gas}} M_{500}. \quad (25)$$

Here the quantity $f_H = 0.76$ is the hydrogen mass fraction, m_p is the proton mass, and $f_{\text{gas}} = (\Omega_b/\Omega_m)$ is the cosmic baryon fraction, while M_{500} is the cluster mass enclosed in the radius r_{500} . Thus,

$$n_{e0} = \frac{N_e}{4\pi r_c^3 f_2(c_{500}, \beta)},$$

$$f_2(c_{500}, \beta) = \int_0^{c_{500}} \frac{x^2 dx}{(1+x^2)^{3\beta/2}}, \quad (26)$$

where $c_{500} = r_{500}/r_c \simeq c_{\text{vir}}/2.0$ is the concentration parameter for R_{500} .

Combining Eqs. (24), (25), and (26), we have

$$\tau = \left(\frac{\sigma_T}{4\pi r_c^2} \right) \left(\frac{f_1(\beta)}{f_2(c_{500}, \beta)} \right) \left(\frac{1 + f_H}{2m_p} \right) f_{\text{gas}} M_{500}. \quad (27)$$

In Fig. 11, we plot the histogram of the optical depth values of the 1526 clusters in the sample. The mean and standard deviation are given by $\tau = (3.9 \pm 1.2) \times 10^{-3}$. Note that the uncertainty quoted here describes the scatter in the mean τ values for the whole of the sample.

We convert the temperature dispersion data listed in Table 4 to the line-of-sight velocity dispersion measurement

Table 6. Statistics of the line-of-sight velocity dispersion $v^2 \equiv (\mathbf{v} \cdot \hat{\mathbf{n}})^2$.

Map	$E[v^2]$ (100 km s ⁻¹) ²	$(V[v^2])^{1/2}$ (100 km s ⁻¹) ²	S/N
2D-ILC	15.4	7.2	2.1
SMICA	27.0	5.6	4.8
NILC	26.1	5.6	4.7
SEVEM	23.8	5.9	4.0
Commander	13.5	6.3	2.1

by using the modelled value of τ . Our procedure is as follows. For each estimate of \hat{s}^2 , we calculate its v^2 value and then we obtain an averaged value of v^2 via

$$v^2 = \frac{c^2}{N_c} \sum_{i=1}^{N_c} \frac{s_i^2}{\tau_i^2}. \quad (28)$$

We then do this for the 5000 values of \hat{s}^2 , and plot the distribution in the right panel of Fig. 10 for the 2D-ILC map. We also present results for v^2 in Table 6, where we can see that for the conservative case, i.e., the 2D-ILC map, the velocity dispersion is measured to be $v^2 = (15.4 \pm 7.2) \times (100 \text{ km s}^{-1})^2$. From the right panel of Fig. 10, we can see that the distribution is not completely Gaussian, but has a tail towards smaller v^2 . The frequency $P(v^2 < 0)$ is 2.1%, which would correspond to a detection of the dispersion of peculiar velocity from 1526 MCXC clusters at the 2.0σ level (using Appendix C).

In studies of peculiar velocity fields, the most relevant quantity is the linear line-of-sight velocity (v), or in other words $\langle v^2 \rangle^{1/2}$. We find $\langle v^2 \rangle^{1/2} = (390 \pm 270) \text{ km s}^{-1}$ (68% CL) for the 2D-ILC map. One can see that the value we find is consistent with the velocity dispersion estimated through studies of the peculiar velocity field (e.g., Riess 2000; Turnbull et al. 2012; Ma & Scott 2013; Carrick et al. 2015).

Here we need to remember that what we measured is the line-of-sight velocity dispersion, which contains both the large-scale bulk flow, and the small-scale velocity and intrinsic dispersion (see, e.g., Ma & Scott 2014). The prediction for the rms bulk flow, equation (22) of Planck Collaboration Int. XIII (2014) (or equation 4 in Ma & Pan 2014), is based on linear perturbation theory for the Λ CDM model and works only for the large-scale bulk flows. The small-scale motions and intrinsic dispersion are not fully predictable from linear perturbation theory because they depend on sub-Jeans scale structure evolution, which involves nonlinear effects. However, this small-scale velocity and intrinsic dispersion are nevertheless physical effects, which are non-negligible in general (Carrick et al. 2015). One should consider that the line-of-sight velocity dispersion that we have measured is a combination of two effects, namely large-scale bulk flows and small-scale intrinsic dispersion, where the second component is generally non-negligible.

We estimate that the histogram of separation distances between all pairs of cluster is peaked at $d \simeq 600 \text{ Mpc}$. Since the bulk flow contributes to the velocity dispersion measurement here, then we can set an upper limit on the cosmic

bulk flow on scales of $600 h^{-1} \text{ Mpc}$, $\langle v_{\text{bulk}}^2 \rangle^{1/2} < 541 \text{ km s}^{-1}$ (95% CL). Such a constraint on large-scale bulk flows indicates that the Universe is statistically homogeneous on scales of $600 h^{-1} \text{ Mpc}$. This is consistent with the limits obtained from Type-Ia supernovae (Feindt et al. 2013), the Spiral Field I -band survey (Nusser & Davis 2011; Ma & Scott 2013), ROSAT galaxy clusters (Mody & Hajian 2012), and the *Planck* peculiar velocity study (Planck Collaboration Int. XIII 2014). However, it does not allow the very large ‘‘dark flow’’ claimed in Kashlinsky et al. (2008, 2010, 2012) and Atrio-Barandela et al. (2015). In addition to ruling out such models, improved measurements of the velocity dispersion in the future have the potential to set up interesting constraints on dark energy and modified gravity (Bhattacharya & Kosowsky 2007, 2008).

5. Conclusions

The kinetic Sunyaev-Zeldovich effect gives anisotropic perturbations of the CMB sky, particularly in the direction of clusters of galaxies. Previous studies have detected the kSZ effect through the pairwise momentum estimator and temperature-velocity cross-correlation. In this paper, we have detected the kSZ effect through a measurement of the temperature dispersion and then we have interpreted this as a determination of the small-scale velocity dispersion of cosmological structure.

To do this, we first selected two sets of *Planck* foreground-cleaned maps. One set contains four *Planck* publicly available maps, namely SMICA, NILC, SEVEM, and Commander, each being produced using a different algorithm to minimize foreground emission. The second set, is the *Planck* 2D-ILC map, which nulls the tSZ component, while resulting in slightly larger residual noise in the map. We then apply a matched-filter technique to the maps, to suppress the primary CMB and instrumental noise. We specifically consider the MCXC cluster sample. Applying a Galactic and point-source mask to the maps, results in 1526 MCXC clusters remaining unmasked.

We measured the distribution of the $\Delta T/T$ values for the 1526 MCXC cluster positions, and also at 1526 randomly selected positions, to give a quantification of the noise level. We found that the 1526 true cluster positions give extra variance to the distribution, and identify this as being due to the kSZ temperature dispersion effect. We compare this signal to results from 5000 random catalogues on the sky, each composed of 1526 random positions. This extra dispersion signal is persistent in several tests that we carry out.

We then construct estimators \hat{s}^2 to quantify this effect. For the SMICA, NILC, and SEVEM maps, the significance of detection is stronger than in the 2D-ILC map, which is likely due to the fact that the residual tSZ effect in the map is correlated with the kSZ signal. However, quoting the conservative result from 2D-ILC, we obtain $\langle s^2 \rangle = (1.64 \pm 0.48) \times 10^{-11}$ (68% CL), where $\langle s^2 \rangle = N_c^{-1} \sum_j (\Delta T_j/T)^2$ ($N_c = 1526$). This gives a detection of temperature dispersion at about the 3.2σ level. This is largely consistent when we obtain results by weighting clusters with their different observed properties.

We further estimate the optical depth of each cluster, and thereby convert our temperature dispersion measurement into a velocity dispersion measurement, obtain-

ing $\langle v^2 \rangle = (15.4 \pm 7.2) \times (100 \text{ km s}^{-1})^2$ (68% CL) using a Gaussian approximation. The distribution has $P(v^2 < 0) = 2.1\%$, and the best-fit value is consistent with findings from large-scale structure studies. This constraint implies that the Universe is statistically homogeneous on scales of $600 h^{-1} \text{ Mpc}$, with the bulk flow constrained to be $\langle v_{\text{bulk}}^2 \rangle^{1/2} < 541 \text{ km s}^{-1}$ (95% CL).

The measurement that we present here shows the promise of statistical kSZ studies for constraining the growth of structure in the Universe. To improve the results in the future, one needs to have better component-separation algorithms to down-weight the residual noise contained in the kSZ map, as well as having more sensitive and higher resolution CMB maps for removing the tSZ signal. One also needs larger cluster catalogues, with the uncertainty scaling roughly as $1/\sqrt{N}$ if the residual noise is Gaussian.

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Appendix A: The statistics of s^2

Let us first define the k th moment of a distribution of a random variable x to be

$$\mu_k(x) \equiv E[x^k] = \frac{1}{N} \sum_i x_i^k. \quad (\text{A.1})$$

The $\widehat{s^2}$ estimator is defined in Eq. (16). Note that the observed δ_i^2 is always taken to be the value of kSZ on the true cluster position, so there is no randomness in δ_i^2 . We also define

$$\overline{\delta^2} \equiv \frac{1}{N_c} \sum \delta_i^2. \quad (\text{A.2})$$

Therefore, the mean value of $\widehat{s^2}$ is

$$\begin{aligned} E[s^2] &= \overline{\delta^2} - \left(\frac{1}{N_c} \sum_i E[n_i^2] \right) \\ &= \overline{\delta^2} - \mu_2(n), \end{aligned} \quad (\text{A.3})$$

while the variance of $\widehat{s^2}$ is

$$V[s^2] = E[s^4] - (E[s^2])^2. \quad (\text{A.4})$$

Therefore, we first calculate

$$\begin{aligned} s^4 &= \left[\overline{\delta^2} - \left(\frac{1}{N_c} \sum_i n_i^2 \right) \right]^2 \\ &= (\overline{\delta^2})^2 + \frac{1}{N_c^2} \sum_{ij} n_i^2 n_j^2 - \frac{2}{N_c} \overline{\delta^2} \left(\sum_i n_i^2 \right) \\ &= (\overline{\delta^2})^2 + \frac{1}{N_c} \sum_i n_i^4 + \frac{1}{N_c^2} \sum_{i,j (i \neq j)} n_i^2 n_j^2 \\ &\quad - \frac{2}{N_c} \overline{\delta^2} \left(\sum_i n_i^2 \right). \end{aligned} \quad (\text{A.5})$$

Therefore,

$$\begin{aligned} E[s^4] &= (\overline{\delta^2})^2 + \frac{1}{N_c} \mu_4(n) + \frac{N_c - 1}{N_c} (\mu_2(n))^2 \\ &\quad - 2\overline{\delta^2} \mu_2(n), \end{aligned} \quad (\text{A.6})$$

where in the above derivation we have assumed that the residual noise samples in two different pixels are uncorrelated, i.e., $\langle n_i n_j \rangle = 0$. Therefore

$$V[s^2] = \frac{1}{N_c} (\mu_4(n) - \mu_2^2(n)). \quad (\text{A.7})$$

Appendix B: Converting M_{500} to M_{vir}

For each cluster, M_{500} is defined as the mass within the radius of R_{500} , in which its average density is 500 times the critical density of the Universe,

$$M_{500} = \frac{4\pi}{3} [500\rho_c(z)] r_{500}^3, \quad (\text{B.1})$$

where

$$\rho_c(z) = 2.77454h^2 E^2(z) \times 10^{11} \text{M}_\odot / \text{Mpc}^3, \quad (\text{B.2})$$

and $E^2(z) = \Omega_m(1+z)^3 + \Omega_\Lambda$. The quantity M_{vir} is calculated via Eqs. (22) and (23), and the relationship between M_{500} and M_{vir} is (Mody & Hajian 2012)

$$\frac{M_{500}}{M_{\text{vir}}} = \frac{m(cr_{500}/r_{\text{vir}})}{m(c)}, \quad (\text{B.3})$$

where c is the concentration parameter (Eq. 21) and $m(x) = \ln(1+x) - x/(1+x)$. Given redshift z and mass M_{500} , we can thus determine r_{500} through Eq. (B.1). If we substitute M_{500} , z , and r_{500} into Eq. (B.3), this becomes an algebraic equation for M_{vir} . This is because r_{vir} can be determined from M_{vir} through Eqs. (22) and (23), and c is related to M_{vir} through Eq. (21). Therefore, we can iteratively solve for M_{vir} , given the values of M_{500} and z .

Appendix C: Converting P values into S/N ratios

Since the distribution of weighted s^2 has longer tail than Gaussian distribution, instead of calculating the ratio between mean and *rms* value of the distribution, we calculate the p-value, and list them in the third column of Table 5. We now convert them into signal-to-noise ratio. Suppose the variable x satisfies the Gaussian distribution, the normalized distribution is $L(x) = (1/\sqrt{2\pi}\sigma) \exp(-(x-\mu)^2/2\sigma^2)$. Then the cumulative probability to find $x < 0$ is

$$\epsilon = \int_{-\infty}^0 P(x) dx = \frac{1}{2} \text{Erfc} \left(\frac{\mu}{\sqrt{2}\sigma} \right), \quad (\text{C.1})$$

where

$$\text{Erfc}(x) = \frac{2}{\sqrt{\pi}} \int_x^\infty e^{-t^2} dt, \quad (\text{C.2})$$

is the complimentary error function.

Therefore the equivalent signal-to-noise ratio given the value of $P(s_w^2 < 0)$ is

$$\text{S/N} = \sqrt{2} (\text{Erfc}^{-1}(2P(s_w^2 < 0))). \quad (\text{C.3})$$

Therefore we use Eq. (C.3) to convert and obtain the fourth column of Table 5.

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