

1 **Polarization Corrected Temperatures for 10-, 19-, 37-, and 89-GHz Passive Microwave**
2 **Frequencies**

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16 **Abstract**

17 Coefficients are derived for computing polarization corrected temperature (PCT) for 10-,
18 19-, 37- and 89-GHz (and similar) frequencies, with applicability to satellites in the Global
19 Precipitation Measurement mission constellation and their predecessors. PCT for 10- and 19-GHz
20 frequencies have been non-existent or seldom used in the past; developing those is the main goal
21 of this study. For 37-GHz and 89-GHz, other formulations of PCT have already become well
22 established. We consider those frequencies here in order to test whether the large sample sizes
23 that are readily available now would point to different formulations of PCT.

24 The purpose of the PCT is to reduce effects of surface emissivity differences in a scene,
25 and draw attention to ice scattering signals related to precipitation. In particular, our intention is
26 to develop PCT formula that minimize differences between land and water surfaces, so that
27 signatures resulting from deep convection are not easily confused with water surfaces. The new
28 formulations of PCT for 10- and 19-GHz measurements hold promise for identifying and
29 investigating intense convection. Four examples are shown from relevant cases. The PCT for
30 each frequency is effective at drawing attention to the most intense convection, and removing
31 ambiguous signals that are related to underlying land or water surfaces. For 37-GHz and 89-GHz,
32 the older formulations of PCT from the literature yield generally similar values as ours, with the
33 differences mainly being a few K over oceans. An optimal formulation of PCT can depend on
34 location and season; results are presented here separated by latitude and month.

35

36

37 **1. Introduction**

38 Satellite-borne passive microwave imagers provide information on the characteristics of
39 the Earth's surface, its overlying atmosphere, and precipitation. Warm brightness temperatures
40 can result from high emissivity land surfaces or from emission by liquid cloud or rain
41 hydrometeors aloft. Low brightness temperatures can result from low emissivity surfaces such as
42 ice and water bodies, or from scattering by large precipitation ice particles. Interpretation of the
43 cause of a low brightness temperature can be ambiguous because it could result from scattering by
44 graupel or hail in a convective storm, or from a wet or water-covered surface. The interpretation
45 is especially difficult when an over-land scene includes convective storms, inland water bodies,
46 and potentially even floodwater or wet soil from recent precipitation (Fig. 1). This paper aims to
47 enable more straightforward assessment of the impacts of hydrometeors on passive microwave
48 measurements, by minimizing effects due to variability in the underlying surface.

49 An example of the ambiguity in discriminating storms from surface conditions is shown in
50 Fig. 1. Strong convective storms are depicted by radar in Fig. 1a, and some of them produce lower
51 brightness temperatures than the adjacent land scenes in Fig. 1b-d, especially in the 37-GHz
52 channel (and in higher frequencies, which are not shown here). For the lower frequencies, most
53 of the storm-associated brightness temperatures are no lower than the precipitation-free brightness
54 temperatures over the nearby Gulf of Mexico (lower right portion of each panel). Over the eastern
55 part of Texas, there are several small areas with reduced brightness temperatures that do not
56 correspond to storms in the radar image. Instead, they are associated with lakes.

57 Most current imagers have separate horizontally polarized and vertically polarized
58 channels for most frequencies, particularly for frequencies near 10-, 19-, 37-, and 89-GHz. Large
59 polarization differences in the upwelling brightness temperatures typically result from water
60 surfaces and surfaces with high soil moisture. Scattering by large ice hydrometeors typically leads
61 to much smaller polarization differences. Dry land surfaces also have smaller polarization
62 differences. A linear combination of horizontally polarized and vertically polarized brightness
63 temperatures, termed polarization corrected temperature (PCT), can remove much of the effect
64 from varying land surface characteristics (Weinman and Guetter 1977; Grody 1984; Spencer et al.
65 1989; Barrett and Kidd 1990; Todd and Bailey 1995; Kidd 1998; Toracinta et al. 2002). The PCT
66 is then useful for identifying scenes with precipitation, with less ambiguity related to the
67 underlying surface type or surface conditions. Formulae for PCT have been presented in various
68 forms in the literature, but here we follow the form:

$$69 \text{PCT}_f = (1+\Theta_f) \text{TB}_{fv} - \Theta_f \text{TB}_{fh} \quad (1)$$

70 where Θ is a coefficient that minimizes effects of surface emissivity and TB is the brightness
71 temperature at frequency f and polarization v (vertical) or h (horizontal).

72 Spatial resolution and sensitivity to typical graupel sizes both increase with increasing
73 frequency (decreasing wavelength) of the radiation. As such, much of the work involving passive
74 microwave PCT has focused on channels in the 85-91-GHz range, with some attention also given
75 to channels near 37-GHz. The Spencer et al. (1989) PCT_{85} is probably the most widely used today,
76 with the coefficient $\Theta_{85}=0.818$ derived from several days of Special Sensor Microwave Imager
77 (SSM/I; Hollinger et al. 1990) global observations of cloud-free oceanic areas. Before settling on
78 this value for Θ_{85} , Spencer et al. (1989) also discussed model calculations that imply values in the
79 range of 0.54-0.61, but those values did not work well with the observed SSM/I data. The Spencer

80 et al. (1989) formula was subsequently used in databases of mesoscale convective systems (Mohr
81 and Zipser 1996) and more general precipitation features (Nesbitt et al. 2000; Liu et al. 2008), and
82 numerous related studies.

83 Although Spencer et al. (1989) identified a constant Θ_{85} value in order to apply a uniform
84 standard for global analysis, others have emphasized that optimal choices of Θ_{85} can be a function
85 of location, season, and local conditions. Barrett and Kidd (1990) proposed $\Theta_{85}=0.64$ for
86 northwestern Europe and the United Kingdom during summer and autumn. Todd and Bailey
87 (1995) and Kidd (1998) empirically derived Θ_{85} values separately for each scene (each SSMI
88 overpass of the United Kingdom), allowing Θ_{85} to vary from day to day. Their Θ_{85} values generally
89 ranged from about 0.5-0.75. Kidd (1998) showed large daily and intra-day variations
90 superimposed on an apparent annual cycle for Θ_{85} , with lowest values in winter and highest values
91 in summer. Todd and Bailey (1995) and Kidd (1998) argued that allowing Θ_{85} to vary with local
92 conditions is important for distinguishing light rain from rain-free regions.

93 Before the first SSMI was launched with its 85-GHz frequency in 1987, 37-GHz
94 measurements were used from the Nimbus-6 Electrically Scanning Microwave Radiometer
95 (ESMR) and Scanning Multichannel Microwave Radiometer (SMMR). Weinman and Guetter
96 (1977) developed a linear transformation (they did not use the term PCT) for use with ESMR.
97 Their equation 16 uses $\Theta_{37}=1.2$ based on theory and $\Theta_{37}=1.5$ based empirically on ESMR
98 observations. Grody (1984) derived $\Theta_{37}=1.08$ and $\Theta_{19}=1.38$ for SMMR. Toracinta et al. (2002)
99 used $\Theta_{37}=1.2$ for the Tropical Rainfall Measuring Mission (TRMM; Kummerow et al. 1998)
100 precipitation feature database (Liu et al. 2008), using TRMM Microwave Imager (TMI) data. That
101 value continues to be used for Global Precipitation Measurement (GPM; Hou et al. 2014) mission
102 precipitation features. Lee et al. (2002) used $\Theta_{37}=1.18$, and that value continues to be used for the

103 popular Naval Research Laboratory – Monterey Tropical Cyclone Webpage. Jiang et al. (2018)
104 provide a nice discussion of PCT_{37} , and use it to interpret precipitation types in tropical cyclones.
105 Precipitation estimation, and more specifically the discrimination between raining and non-
106 raining areas, motivated much of the aforementioned research involving PCT_{85} . Cecil et al. (2005)
107 and Zipser et al. (2006) emphasized the use of PCT_{37} in studies of intense thunderstorms, using
108 TRMM measurements. Cecil (2009) empirically related TRMM PCT_{85} and PCT_{37} to reports of
109 large hail reaching the surface, and Cecil and Blankenship (2012) applied the PCT_{37} -hail
110 relationship to Advanced Microwave Scanning Radiometer for Earth Observing System (AMSR-
111 E) PCT_{36} (using the same Θ_{37} as in Toracinta et al. 2002) in order to estimate a global climatology
112 of hailstorm occurrence. Cecil (2009) also noted that 19-GHz measurements from TRMM are
113 more effective at giving a high-confidence indication of large hail, although relatively coarse
114 spatial resolution and the lack of a well-established PCT_{19} made it more difficult to use. Mroz et
115 al. (2017) tested an early version of the PCT_{19} that is presented here, and found it to be more
116 effective for identifying hail than any of the other GMI frequencies. We did not have a version of
117 PCT_{10} ready for inclusion in the Mroz et al. study, but even without applying the PCT, the low-
118 resolution 10-GHz measurements did show some usefulness in that study.

119 This paper is motivated by observations of reduced brightness temperatures in TRMM and
120 GPM 19-GHz and 10-GHz channels for some intense thunderstorms, besides the reduced
121 brightness temperatures that have already been well documented for the 85-89-GHz and 36-37-
122 GHz frequencies. Systematic analysis of thunderstorm-related signatures in the 19-GHz and 10-
123 GHz channels is difficult without first applying a PCT transformation to those channels. This
124 paper empirically derives values for Θ_{10} , Θ_{19} , Θ_{37} , and Θ_{89} from three years of GPM measurements,
125 and considers their spatial and seasonal variability. The main goal is to derive and evaluate useful

126 coefficients for PCT_{10} and PCT_{19} , since those have rarely been used in the past. The values for Θ_{37}
127 and Θ_{89} from the literature have proven effective over the years. We re-examine them here because
128 it has become convenient to apply our methods to vastly larger sample sizes than were used in the
129 previous studies. Our optimal coefficients (producing the smallest contrast between land and water
130 surfaces, and thus less ambiguity related to surface type) for PCT_{37} and PCT_{89} are slightly different
131 from those that have already been widely used. Our analysis shows that a broad range of
132 coefficient values can be defensible for these frequencies, when applied to global studies. As such,
133 there may be little practical benefit for many users to switch from the previous Θ_{37} and Θ_{89} values
134 to our marginally more effective values. The values derived for Θ_{10} and Θ_{19} do show promise for
135 enabling improved analysis of vigorous, deep convection.

136

137 **2. Data and Methods**

138 GPM Microwave Imager (GMI) version V05A brightness temperatures (GPM Science
139 Team, 2016) from 1 April 2014 – 31 March 2017 are used for development of PCT coefficients in
140 this study. Every other GPM orbit (odd-numbered orbits from 503-17553) and every tenth scan
141 position (of the 221 positions per GMI scan) are used, in order to speed up the required processing.
142 This amounts to using 5% of the available data during a 3-year period, while still sampling a broad
143 variety of conditions.

144 The GMI Level 2 (“GPROF”) files (Iguchi and Meneghini, 2016) are further used to
145 identify precipitation-free pixels, and to classify each pixel as land (GPROF surface types 3-5,
146 corresponding to “maximum vegetation”, “high vegetation”, and “moderate vegetation”) or ocean
147 (GPROF surface type 1). The “ocean” classification can include large water bodies, for example

148 the Great Lakes. Sea ice, arid regions, surface snow cover, rivers, coasts, and precipitation scenes
149 are excluded.

150 Each orbit is divided into 5° latitude bins. Statistics are derived separately for each of these
151 bins that has at least 10 land and 10 water pixels without precipitation. Latitude bins without
152 enough land and water pixels in a given orbit are ignored, because a comparison between land and
153 water pixels is required for building the empirical relationships. For a given latitude bin in a given
154 GPM orbit, candidate PCT values using a given Θ are computed for each pixel. The differences
155 between PCT values are then computed for every possible pairing of land and water pixels within
156 that latitude bin. If there are 10 land and 10 water pixels, for example, there would be 100 pairs
157 with land-water PCT differences. Since the GMI swath is about 900 km wide and the satellite
158 only takes a few minutes to traverse 5° , most of the land-water differences are computed within a
159 few hundred km and a few minutes of each other. Ideally, a perfect choice of Θ would yield PCT
160 differences near zero for all possible land-water pairings, and a poor choice of Θ would yield large
161 PCT differences. That ideal scenario is not realistic, because inhomogeneities in a scene besides
162 surface type would give non-zero differences. A histogram of PCT differences is computed from
163 the land-water pairings, and added to histograms computed from other orbits. This process is
164 repeated for candidate PCT values computed with Θ ranging from 0.3 to 1.79 in increments of
165 0.01. Each GMI frequency under consideration is treated separately, at its native resolution.

166 The PCT difference histograms are computed with bin size 2 K. They are accumulated
167 separately for each 5° latitude bin, for each month of the year, and for each Θ value. Even though
168 we considered only 5% of the available GMI data, before further restricting the data by surface
169 type and precipitation, most latitudes (from 55° S to 60° N) and months contain tens of millions
170 of land-water pairings for the resulting histograms. The sample size (Table 1) is relatively small

171 at far the southern latitudes because there is so little land there, and is large at the far northern
172 latitudes because of both orbital geometry and the mix of land and ocean surfaces. The seasonal
173 variation in sample size is extreme at far northern latitudes (2 million land-water pairings in
174 January, 357 million pairings in August) because surface snow and ice cover are eliminated.

175 The resulting histograms of land-water PCT differences are analyzed in Section 3 to
176 determine which Θ values most consistently yield small PCT differences. A small difference in
177 PCT between land and water pixel pairs indicates that the surface type is not strongly influencing
178 the PCT, and that we can use PCT to investigate precipitation hydrometeor signatures instead.
179 Section 3a accumulates the histograms into probability density functions across all latitudes and
180 months for a global analysis, and Section 3b examines variability by latitude and month.

181 PCT coefficients based on the results from Section 3 are applied to selected cases in Section
182 4. Those cases were observed individually by the GMI, TMI, AMSR-E, and SSMI sensors (Table
183 2). The GPM XCAL dataset (Berg et al. 2016; GPM Science Team 2016; GPM Science Team
184 2017a,b,c) is used for these, since it applies an inter-calibration among sensors, making their
185 calibrations consistent with GMI. The XCAL brightness temperatures are referred to as GPM
186 level 1C version 05A, with other satellites included as GPM constellation members. GPM level
187 1B version 05A 85-GHz data (TRMM, 2017) are also used for the TMI case, because level 1C
188 unnecessarily sets values below 50 K as missing. AMSR-E level 2A version 3 files (Ashcroft and
189 Wentz, 2013) from the National Snow and Ice Data Center (NSIDC) are also used for 89-GHz for
190 the same reason.

191

192 3. Results – Optimizing PCT Coefficients

193 a) Global analysis

194 First we consider statistics from the land-water PCT differences accumulated over all
195 months and all regions. Since a motivation for using the PCT is to eliminate the land-water
196 differences as much as possible, Fig. 2 shows what percentage of land-water pairs have PCT
197 differences below 2 K (thick lines) and below 10 K (thin lines) as a function of the choice of Θ
198 value. For convenience, we will refer to the value yielding land-water PCT differences less than
199 2 K the most often as the “best” performing Θ in a given analysis. These are not the Θ values we
200 ultimately recommend using. Defining the best Θ based on how rarely it produces large (> 10 K)
201 differences would lead to Θ values 0.03-0.04 higher. Our ultimate recommendations will consider
202 both those definitions and the regional and seasonal variability to be addressed in Section 3b.

203 Fig. 3 shows probability density functions of land-water PCT differences for the Θ values
204 that yield PCT differences less than 2 K most often, and for some other Θ values from the literature.
205 For $\Theta_{89}=0.63$, 24% of land-water pairings have PCT differences less than 2 K, another 21% have
206 differences between 2-4 K, and 16% have differences 4-6 K. Using $\Theta_{89}=0.82$ based on Spencer et
207 al. (1989) reduces those percentages to 18%, 17%, and 16%, respectively. The “best” performing
208 Θ_{37} (1.10) in this global analysis yields land-water differences in PCT_{37} that are slightly larger than
209 the differences in PCT_{89} based on using the Spencer et al. Θ_{85} . In other words, a sub-optimal choice
210 of Θ_{89} can outperform an optimal choice of Θ_{37} . Moving to still lower frequency channels, the
211 “best” performing Θ_{19} (1.36) and Θ_{10} (1.48) are progressively less effective at minimizing the land-
212 water PCT differences. This decreasing effectiveness with decreasing frequency is also seen in

213 Fig. 2. The Toracinta et al. (2002) coefficient $\Theta_{37}=1.20$ yields land-water PCT₃₇ differences less
214 than 2 K 14% of the time, and between 2-4 K another 14% of the time. This is comparable to
215 $\Theta_{19}=1.36$ yielding PCT₁₉ differences less than 2 K 15% of the time, and 2-4 K 14% of the time.
216 For $\Theta_{10}=1.48$, only 12% of land-water pairs have PCT₁₀ differences less than 2 K and 11% between
217 2-4 K. For this “best” choice of Θ_{10} from the global analysis, about half the land-water pairs have
218 PCT₁₀ differences greater than 10 K. Any choice of Θ_{10} will have many situations where it is not
219 very effective at removing the land-water contrast.

220 The probability density functions in Fig. 3 isolated the Θ values that gave the sharpest
221 peaks in the 0-2 K PCT difference bins. Fig. 4 instead depicts the performance for all Θ values,
222 in the form of two-dimensional probability density functions. The sideways V-shapes for these
223 two-dimensional probability density functions indicate that for each frequency, there is a preferred
224 range of Θ values where the land-water PCT differences tend to be small. Moving away from that
225 preferred range, Θ values that are too high or too low give larger land-water PCT differences.
226 Minimizing those land-water differences is crucial for seamlessly interpreting the precipitation
227 characteristics across a coastline, or in a scene including small water bodies. A narrow range of
228 Θ values gives acceptably small land-water PCT differences for the low-frequency channels, but
229 a broad range of Θ_{89} values gives small PCT₈₉ differences.

230

231 *b) Variability by latitude and month*

232 Figures analogous to Fig. 2-4 were generated separately for each 5° latitude bin and for
233 each month. Lower Θ values generally have better performance (i.e., less variation in PCT) in the
234 deep tropics than at higher latitudes. At mid- and high-latitudes, higher Θ values perform better

235 during the warm season and lower Θ values perform better during the cold season. The Θ values
236 that yield the highest percentage of land-water pairs with PCT differences less than 2 K are
237 compiled as functions of latitude and month in Table 3 (89-GHz), Table 4 (37-GHz), Table 5 (19-
238 GHz), and Table 6 (10-GHz).

239 Just as a range of Θ values works better for higher frequency channels than any Θ value
240 does for lower frequency channels in Fig. 2-4, a range of Θ values also works well in the tropics,
241 compared to higher latitudes. As an example, the effectiveness of each Θ value at reducing the
242 land-water contrast below 2 K (thick lines) and below 10 K (thin lines) as in Fig. 2 is reproduced
243 separately for 0° - 5° N in July (Fig. 5) and for 35° - 40° N in July (Fig. 6). The best-performing Θ
244 values are lower in the tropics than in the mid-latitudes (consistent with Tables 3-6). The PCT is
245 so much more effective at reducing the land-water contrast in the deep tropics, there is little need
246 to find the precise Θ value that gives the best scores there. One could choose whichever Θ value
247 is most acceptable for the mid-latitudes, and that Θ would also work well in the tropics.

248

249 **4. Discussion and examples**

250 Consideration of Figs. 2-4, analogous figures that are segregated by latitude and month,
251 and Tables 3-6 lead to the conclusion that while no single Θ value gives an ideal PCT formulation
252 applicable to all places and seasons, a range of Θ values can generally give credible results. Some
253 readers may wish to use PCT formulations that are most appropriate for particular regions or
254 seasons, and Tables 3-6 are suitable for selecting those Θ values. Others, including ourselves, will
255 want to apply a single Θ value for each frequency globally, all through the year. The most
256 straightforward choice would be to take the Θ values highlighted in Section 3a, but instead we

257 recommend some slight modifications to account for varying performance in different regions and
258 seasons. Our recommendations (Table 7) also round the Θ values to the nearest 0.05, since Fig.
259 2-4 and the analysis by latitude and by month suggest that precision to the nearest 0.01 is not
260 warranted.

261 The result that a high degree of precision is not warranted in selecting Θ values also
262 suggests that the same coefficients should be appropriate for use with other passive microwave
263 sensors, despite differences in footprint sizes or radiometer frequencies. Small variations in the
264 frequencies used by different radiometers can lead to brightness temperature differences of a few
265 K in rain-free regions (or several K in rain, but raining pixels are omitted from the computation of
266 PCT coefficients) (Yang et al. 2014). If the entire analysis were repeated using an 85.5 GHz (e.g.,
267 SSMI or TMI) or 91.7 GHz (e.g., SSMI/Sounder) frequency instead of the GMI's 89.0 GHz
268 frequency, there may be small changes in the details of Section 3, but likely no significant change
269 in the choice of Θ . Likewise, differences in sensors' footprint sizes should have little effect,
270 especially since the analysis is done using precipitation-free pixels.

271 For passive microwave channels in the range 85-GHz – 92-GHz (including SSMI, TMI,
272 GMI, AMSR), we recommend $\Theta_{89}=0.70$. This tends more toward the higher values that work well
273 in the mid-latitude warm seasons than the lower values that work best in the tropics, since
274 performance of PCT_{89} in the tropics is less sensitive to the precise choice of Θ_{89} . For similar
275 reasons, we recommend $\Theta_{37}=1.15$ for the 36-37-GHz channels on SSMI, TMI, GMI, and AMSR.

276 Many publications have used $\Theta_{85}=0.818$ and $\Theta_{37}=1.2$ for PCT based on Spencer et al.
277 (1989) and Toracinta et al. (2002), particularly for studies involving TRMM and GPM
278 precipitation feature databases (Nesbitt et al. 2000; Liu et al. 2008). Fig. 7-8 compare PCT values
279 computed using our recommended Θ values to those computed using the Spencer et al. (1989) and

280 Toracinta et al. (2002) values. The differences are mostly small, which was expected because the
281 Spencer et al. and Toracinta et al. versions have both proven effective over the years. Figures 2
282 and 4 show that these small changes do tend to slightly reduce the land-water contrasts when using
283 our new versions of PCT_{89} and PCT_{37} . Since the PCT formula in Equation (1) can be re-arranged
284 to include a term with Θ multiplying the polarization difference, our lower choices of Θ almost
285 always lead to slightly lower PCT values. The choice of Θ has least effect where polarization
286 differences are small (e.g., most land areas), and greatest effect where polarization differences are
287 large (e.g., water surfaces beneath optically thin airmasses). For PCT_{89} , the differences are less
288 than 1 K over most land areas and 1-4 K over most ocean locations. Exceptions over land are
289 deserts and areas of snow or ice cover, where PCT_{89} tends to be 1-3 K lower using our choice of
290 Θ_{89} . Over oceans, the largest differences (4-8 K) coincide with dry airmasses, particularly at mid-
291 and high-latitudes. For PCT_{37} , the differences over land are again less than 1 K except for deserts
292 and snowpacks, where the differences are 1-2 K. Over oceans, the differences are only 2-4 K, with
293 the higher values coinciding with drier airmasses. For both frequencies, the differences are only a
294 few tenths of a Kelvin for pixels with substantial precipitation signatures.

295 For 19-GHz channels (including SSMI, TMI, GMI, AMSR), we recommend $\Theta_{19}=1.40$.
296 This is essentially the same (after rounding) as the 1.38 value used by Grody (1984), with which
297 we were not familiar until preparing this manuscript. For channels near 10-GHz (TMI, GMI, and
298 AMSR), we recommend $\Theta_{10}=1.50$. As with the higher frequency channels, these
299 recommendations for the lower frequency channels are compromises that are intended to work
300 best in both the tropics and in mid-latitude warm seasons. For the lower frequency channels, the
301 ability to eliminate differences between land and water-covered scenes is substantially reduced
302 compared to the higher frequency channels.

303 We briefly consider cases with intense convective storms that were observed by GMI, TMI,
304 AMSR-E, and SSMI, in order to demonstrate the utility of these new PCT formulations. These
305 cases were previously identified by Cecil (2015) as having some of the most extreme 37-GHz or
306 89-GHz scattering signatures for those satellites. For each example in Fig. 9-12, the left panels
307 show vertically-polarized brightness temperatures and the right panels show PCT (using our
308 recommended coefficients, as in Table 7).

309 The storms around Texas shown in Fig. 1 are re-visited in Fig. 9, a case observed by GMI
310 on 26 May 2015. At 89-GHz (top row), the effect of the PCT is not especially noticeable for this
311 case, other than bringing the Gulf of Mexico temperatures closer to those over land. For the 37,
312 19, and 10-GHz frequencies, the PCT eliminates the sharp gradient at the coast and also eliminates
313 the signatures associated with lakes that were mentioned with Fig. 1. The individual figure panels
314 identify the minimum brightness temperature (or PCT) for each panel. Most of these minima are
315 associated with the strongest storm, west of Fort Worth. The minimum TB_{10v} (Fig. 9g) is a
316 precipitation-free Gulf of Mexico scene, but PCT_{10} (Fig. 9h) is minimized over the storm, as
317 desired.

318 A case over northern Argentina observed by TMI is shown in Fig. 10. The left panels have
319 low brightness temperatures from numerous intense thunderstorms, along with low surface
320 emissivity features such as the Parana River, Ibera Wetlands, and the Mar Chiquita salt lake. The
321 PCT in the right panels only highlight the strong storms. Zipser et al. (2006) highlighted this case
322 and mentioned its lowest PCT_{37} as 69 K. Its minimum PCT_{37} is higher (74 K) in Fig. 10d because
323 of two calibrations that were applied to TMI since that paper. The update from TRMM version 7
324 to version 8 (now known as GPM version 5, because TRMM is treated as part of the GPM
325 constellation) increased TB_{37v} and TB_{37h} by 2.8 K and 2.5 K, respectively, for the coldest pixel in

326 this case. The recalibration for consistency with GMI (known as the GPM XCAL level 1C
327 brightness temperatures) increases $T_{B_{37V}}$ by 0.69 K and decreases $T_{B_{37H}}$ by 1.56 K for the low end
328 of $T_{B_{37}}$ values, such as this. The increased $T_{B_{37V}} - T_{B_{37H}}$ polarization difference adds to the PCT_{37} .
329 The change from using Toracinta et al.'s (2002) Θ_{37} coefficient (also used by Zipser et al. 2006)
330 to ours only amounts to 0.3 K difference between the two formulations.

331 Typhoon Bolaven (2005) is shown in Fig. 11, as observed near the Philippines (east of
332 Luzon) by AMSR-E on 18 Nov 2005. The use of PCT again eliminates most of the land-water
333 contrast (with the Philippines on the far left of each panel). But the PCT also removes much of
334 the signal from rain in the lower frequency channels. Emission by liquid rain is seen as warm
335 brightness temperatures over ocean in the left panels, but only the scattering by large ice particles
336 is highlighted by the PCT in the right panels.

337 The SSMI has coarser resolution than GMI, TMI, and AMSR-E, and lacks a 10-GHz
338 channel, but the PCT highlights intense convection in SSMI's 19-, 37-, and 85-GHz frequencies.
339 The "Boundary Waters Derecho" (Price and Murphy 2002) case (Fig. 12) featured an intense storm
340 in northern Minnesota. The PCT is again effective at removing the signal associated with the lakes
341 in this region, and drawing attention to the storm.

342 The cases shown in Fig. 9-12 were selected because they were known to have extremely
343 low PCT_{37} , so they were good candidates for having substantial ice scattering signatures in the 19-
344 and 10-GHz channels. Indeed, the GMI and TMI cases had PCT_{19} reduced from near 300 K in the
345 surrounding areas to 159 K and 149 K, respectively, at the convective cores. Those two cases also
346 had noticeable scattering signatures in PCT_{10} (241 K and 265 K, respectively), despite the longer
347 wavelength and coarser resolution for this frequency (Table 2). The AMSR-E case (Typhoon
348 Bolaven, Fig. 11) had weaker signatures in the low frequency channels (235 K PCT_{19} ; 278 K

349 PCT₁₀) than the GMI and TMI cases, but it also had a weaker signature at 37-GHz (113 K). It had
350 the lowest TB_{v89} (41 K) and PCT₈₉ (41 K) of all these cases, which may result from having an
351 extraordinarily deep vertical layer of large graupel. The SSMI case from Minnesota had PCT₁₉
352 reduced to 230 K, despite SSMI's coarse resolution. Another SSMI case from the same region (28
353 June 1998) had PCT₁₉ scattered to 217 K (not shown).

354

355 **5. Conclusions**

356 Coefficients have been derived for computing PCT for 10-, 19-, 37- and 89-GHz (and
357 similar) frequencies from GMI and related radiometers. While coefficient values can be optimized
358 for particular regions and seasons using Tables 3-6, we recommend the values listed in Table 7 for
359 global applications. These result in the formulae:

$$360 \quad \text{PCT}_{10} = 2.5 \text{ TB}_{10v} - 1.5 \text{ TB}_{10h} \quad (2)$$

$$361 \quad \text{PCT}_{19} = 2.4 \text{ TB}_{19v} - 1.4 \text{ TB}_{19h} \quad (3)$$

$$362 \quad \text{PCT}_{37} = 2.15 \text{ TB}_{37v} - 1.15 \text{ TB}_{37h} \quad (4)$$

$$363 \quad \text{PCT}_{89} = 1.7 \text{ TB}_{89v} - 0.7 \text{ TB}_{89h} \quad (5)$$

364 These values were tested using four cases with intense convection observed separately by
365 the GMI, TMI, AMSR-E, and SSMI sensors. The new PCT formulations eliminated much of the
366 contrast between land and water surfaces in all four cases and for all four frequencies. The intense
367 convection is easily recognized with PCT depressions in each case, without having surface-related
368 characteristics contributing other ambiguous PCT depressions.

369 Other formulations of PCT₈₉ and PCT₃₇ have become well established. Differences
370 between our PCT₈₉ and that from Spencer et al. (1989) and between our PCT₃₇ and that from
371 Toracinta et al. (2002) were examined and tend to be small, especially for measurements involving

372 ice scattering related to precipitation. Otherwise, our PCT_{89} and PCT_{37} tend to be a few K lower
373 than the previous formulations over the oceans. The largest differences are over relatively dry
374 oceanic airmasses. Differences over land are usually less than 1 K, except for deserts and snow-
375 or ice-covered regions.

376 The key new developments from this paper are the coefficients for computing PCT_{19} and
377 PCT_{10} . We see these as tools for further investigating intense thunderstorms, using GPM and other
378 satellites with related sensors. Indeed, Mroz et al. (2017) obtained higher skill scores for hail
379 detection using a preliminary version of our PCT_{19} than the scores obtained using higher
380 frequencies or individual polarizations. PCT_{19} and PCT_{10} essentially mask the signals that come
381 from inland water bodies, or from coasts. They also have little sensitivity to most precipitation,
382 but help draw attention to the most intense convection, capable of producing large amounts of hail
383 and/or graupel that scatter the upwelling radiation in these frequencies.

384

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389 System website at <http://pps.gsfc.nasa.gov/>.

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482

483 **8. Tables**

484

485 Table 1. Sample size (in millions) of land-ocean pairings for each 5° latitude bin (bottom latitude

486 of the bin is listed in the first column) and each month.

487

Lat	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec
55	2	4	17	136	273	293	338	357	308	200	38	6
50	6	8	26	153	209	225	241	255	221	164	53	11
45	12	21	65	133	159	173	180	193	165	143	85	29
40	43	47	91	112	118	119	127	133	120	115	96	62
35	81	75	112	122	128	129	125	128	116	117	109	96
30	72	68	86	87	89	84	82	86	80	79	87	87
25	78	70	82	75	69	61	52	53	60	60	74	84
20	75	71	86	76	73	65	40	34	38	45	60	73
15	58	59	73	68	58	45	36	37	38	32	45	55
10	108	111	120	101	92	85	72	77	86	82	89	100
5	104	112	123	95	96	94	91	95	91	89	98	100
0	103	97	101	86	98	97	98	108	108	102	100	100
-5	86	80	80	72	92	91	95	103	100	95	91	88
-10	85	80	84	83	103	102	110	121	119	111	103	89
-15	89	83	90	94	120	113	121	132	130	124	108	94
-20	81	78	85	86	104	95	99	108	114	104	99	86
-25	77	75	79	79	95	84	87	92	93	82	82	77
-30	76	72	74	78	95	83	85	90	91	81	83	76
-35	90	88	83	86	97	88	89	93	97	88	95	91
-40	50	48	47	45	46	42	41	41	44	41	48	52
-45	28	27	26	26	25	22	20	20	22	23	26	28
-50	17	16	16	16	17	13	12	12	16	15	16	18
-55	6	5	6	6	6	5	3	3	5	5	5	6

488

489

490 Table 2. Footprint sizes (effective fields of view, in km) for the frequencies and instruments used
 491 in this study.

492

Sensor	GMI (Hou et al. 2014)				TMI (Kummerow et al. 1998)				AMSR-E (JAXA 2006)				SSM/I (Hollinger et al. 1990)		
Frequency (GHz)	10.65	18.7	36.5	89.0	10.7	19.35	37.0	85.5	10.65	18.7	36.5	89.0	19.35	37.0	85.5
Along-track	32	18	15	7	63	30	16	7	51	27	14	6	69	37	15
Cross-track	19	11	9	4	37	18	9	5	29	16	8	4	43	28	13

493

494 Table 3. 89-GHz PCT coefficient Θ_{89} for each latitude and month that gives the most land-ocean
 495 pixel pairs with PCT differences < 2 K.

496

Lat	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec
55	0.54	0.57	0.60	0.63	0.64	0.72	0.74	0.69	0.61	0.55	0.58	0.62
50	0.52	0.53	0.56	0.60	0.64	0.80	0.74	0.72	0.63	0.55	0.56	0.57
45	0.55	0.58	0.60	0.66	0.69	0.79	0.77	0.67	0.64	0.58	0.57	0.58
40	0.51	0.56	0.58	0.59	0.64	0.72	0.66	0.63	0.61	0.58	0.55	0.53
35	0.48	0.55	0.55	0.63	0.65	0.75	0.67	0.66	0.62	0.57	0.51	0.48
30	0.46	0.51	0.58	0.65	0.69	0.78	0.70	0.65	0.66	0.56	0.49	0.41
25	0.44	0.56	0.65	0.73	0.82	0.70	0.68	0.66	0.61	0.59	0.55	0.46
20	0.51	0.57	0.70	0.83	0.81	0.74	0.64	0.51	0.54	0.58	0.56	0.51
15	0.59	0.64	0.68	0.77	0.73	0.68	0.64	0.59	0.57	0.54	0.58	0.58
10	0.62	0.68	0.73	0.85	0.87	0.85	0.74	0.64	0.66	0.69	0.60	0.61
5	0.65	0.71	0.73	0.69	0.66	0.63	0.57	0.53	0.58	0.61	0.62	0.61
0	0.58	0.63	0.57	0.52	0.52	0.56	0.59	0.57	0.59	0.60	0.60	0.60
-5	0.59	0.62	0.56	0.52	0.56	0.61	0.61	0.64	0.64	0.63	0.61	0.61
-10	0.52	0.55	0.49	0.51	0.57	0.65	0.66	0.68	0.70	0.67	0.57	0.53
-15	0.53	0.50	0.50	0.52	0.59	0.65	0.65	0.68	0.69	0.64	0.58	0.51
-20	0.68	0.62	0.59	0.63	0.61	0.64	0.62	0.64	0.72	0.75	0.72	0.68
-25	0.81	0.77	0.70	0.67	0.66	0.61	0.60	0.63	0.73	0.81	0.78	0.82
-30	0.84	0.85	0.77	0.72	0.63	0.59	0.60	0.63	0.70	0.81	0.77	0.84
-35	0.84	0.80	0.74	0.68	0.64	0.57	0.60	0.61	0.65	0.75	0.73	0.79
-40	0.78	0.76	0.72	0.63	0.62	0.58	0.58	0.58	0.62	0.72	0.72	0.77
-45	0.71	0.66	0.62	0.58	0.55	0.49	0.52	0.54	0.55	0.66	0.62	0.67
-50	0.74	0.67	0.67	0.61	0.56	0.51	0.53	0.56	0.56	0.62	0.69	0.70
-55	0.81	0.69	0.70	0.59	0.57	0.57	0.56	0.58	0.61	0.59	0.76	0.71

497

498 Table 4. 37-GHz PCT coefficient Θ_{37} for each latitude and month that gives the most land-ocean
 499 pixel pairs with PCT differences < 2 K.

500

Lat	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec
55	0.97	0.98	1.01	1.03	1.03	1.11	1.12	1.10	1.05	0.98	0.98	1.00
50	0.96	0.97	0.99	1.03	1.07	1.17	1.13	1.13	1.08	1.02	1.00	0.98
45	0.98	1.01	1.03	1.07	1.11	1.17	1.18	1.14	1.11	1.04	1.02	1.00
40	0.97	1.01	1.01	1.03	1.09	1.15	1.12	1.12	1.09	1.05	1.01	0.99
35	0.95	1.01	1.04	1.08	1.12	1.18	1.17	1.14	1.12	1.07	1.01	0.98
30	0.96	0.99	1.07	1.11	1.14	1.20	1.17	1.14	1.13	1.08	1.01	0.98
25	0.97	1.06	1.07	1.14	1.13	1.12	1.12	1.10	1.10	1.06	1.05	0.99
20	1.02	1.09	1.13	1.20	1.14	1.14	1.11	1.05	1.06	1.06	1.05	1.04
15	1.08	1.12	1.15	1.19	1.16	1.14	1.17	1.10	1.09	1.06	1.07	1.07
10	1.25	1.27	1.35	1.42	1.32	1.28	1.24	1.17	1.16	1.16	1.17	1.23
5	1.14	1.19	1.18	1.15	1.13	1.12	1.08	1.07	1.07	1.08	1.08	1.11
0	1.07	1.10	1.08	1.05	1.04	1.06	1.06	1.06	1.07	1.07	1.06	1.06
-5	1.08	1.10	1.07	1.05	1.07	1.09	1.09	1.10	1.11	1.09	1.10	1.07
-10	1.08	1.09	1.06	1.06	1.09	1.12	1.12	1.16	1.15	1.14	1.09	1.08
-15	1.08	1.08	1.06	1.05	1.09	1.11	1.12	1.14	1.15	1.13	1.10	1.07
-20	1.16	1.15	1.12	1.12	1.11	1.14	1.13	1.17	1.23	1.30	1.26	1.18
-25	1.25	1.24	1.21	1.17	1.17	1.17	1.16	1.21	1.25	1.35	1.30	1.30
-30	1.27	1.23	1.21	1.19	1.16	1.13	1.12	1.16	1.21	1.28	1.23	1.30
-35	1.31	1.22	1.23	1.19	1.14	1.08	1.09	1.13	1.15	1.20	1.21	1.27
-40	1.22	1.18	1.18	1.11	1.10	1.04	1.04	1.06	1.07	1.15	1.17	1.21
-45	1.20	1.19	1.14	1.08	1.08	1.01	1.01	1.04	1.04	1.12	1.14	1.18
-50	1.30	1.22	1.21	1.09	1.09	1.04	1.05	1.08	1.08	1.14	1.22	1.22
-55	1.27	1.17	1.17	1.08	1.05	1.04	1.04	1.05	1.07	1.08	1.17	1.17

501

502 Table 5. 19-GHz PCT coefficient Θ_{19} for each latitude and month that gives the most land-ocean
 503 pixel pairs with PCT differences < 2 K.

504

Lat	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec
55	1.29	1.30	1.32	1.33	1.34	1.43	1.42	1.40	1.34	1.28	1.29	1.29
50	1.28	1.29	1.34	1.37	1.39	1.49	1.44	1.42	1.38	1.33	1.32	1.29
45	1.28	1.35	1.40	1.43	1.44	1.48	1.49	1.44	1.41	1.37	1.35	1.31
40	1.29	1.34	1.34	1.36	1.40	1.45	1.43	1.40	1.38	1.35	1.32	1.29
35	1.28	1.34	1.36	1.40	1.43	1.48	1.48	1.43	1.40	1.37	1.31	1.28
30	1.23	1.28	1.36	1.41	1.42	1.47	1.42	1.38	1.38	1.33	1.26	1.25
25	1.24	1.29	1.33	1.39	1.39	1.38	1.37	1.35	1.34	1.31	1.30	1.26
20	1.29	1.37	1.37	1.42	1.39	1.38	1.35	1.29	1.31	1.31	1.30	1.31
15	1.32	1.38	1.42	1.41	1.38	1.37	1.38	1.33	1.33	1.30	1.31	1.31
10	1.62	1.69	1.74	1.79	1.57	1.52	1.48	1.42	1.41	1.39	1.39	1.39
5	1.37	1.43	1.41	1.38	1.37	1.36	1.33	1.31	1.32	1.32	1.33	1.35
0	1.32	1.34	1.32	1.30	1.29	1.31	1.30	1.31	1.32	1.31	1.31	1.31
-5	1.33	1.35	1.32	1.30	1.32	1.33	1.33	1.34	1.35	1.34	1.34	1.32
-10	1.32	1.33	1.31	1.30	1.33	1.35	1.36	1.39	1.39	1.37	1.34	1.32
-15	1.33	1.33	1.31	1.30	1.33	1.35	1.37	1.40	1.41	1.39	1.35	1.32
-20	1.42	1.39	1.38	1.37	1.35	1.41	1.43	1.46	1.59	1.63	1.58	1.46
-25	1.53	1.48	1.48	1.44	1.46	1.49	1.51	1.56	1.59	1.70	1.68	1.59
-30	1.49	1.47	1.44	1.42	1.40	1.40	1.43	1.42	1.47	1.59	1.48	1.51
-35	1.57	1.47	1.49	1.46	1.42	1.39	1.41	1.43	1.44	1.51	1.49	1.58
-40	1.48	1.44	1.44	1.39	1.40	1.34	1.35	1.38	1.38	1.45	1.47	1.49
-45	1.67	1.66	1.59	1.38	1.49	1.39	1.39	1.45	1.41	1.49	1.56	1.68
-50	1.79	1.75	1.72	1.55	1.53	1.49	1.51	1.53	1.53	1.61	1.73	1.75
-55	1.66	1.59	1.57	1.47	1.43	1.43	1.44	1.45	1.43	1.48	1.55	1.59

505

506 Table 6. 10-GHz PCT coefficient Θ_{10} for each latitude and month that gives the most land-ocean
 507 pixel pairs with PCT differences < 2 K.

508

Lat	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec
55	1.47	1.50	1.53	1.53	1.53	1.61	1.58	1.55	1.49	1.45	1.47	1.48
50	1.47	1.50	1.55	1.54	1.54	1.65	1.58	1.55	1.52	1.49	1.48	1.47
45	1.44	1.49	1.73	1.79	1.58	1.63	1.63	1.57	1.55	1.53	1.49	1.47
40	1.48	1.54	1.56	1.57	1.58	1.62	1.58	1.53	1.52	1.51	1.49	1.48
35	1.45	1.53	1.57	1.60	1.61	1.63	1.62	1.51	1.50	1.52	1.46	1.46
30	1.36	1.40	1.50	1.55	1.55	1.57	1.52	1.48	1.48	1.44	1.38	1.37
25	1.36	1.41	1.46	1.49	1.50	1.50	1.47	1.45	1.44	1.42	1.38	1.37
20	1.40	1.47	1.47	1.51	1.50	1.47	1.45	1.40	1.42	1.42	1.42	1.43
15	1.42	1.47	1.50	1.49	1.48	1.47	1.46	1.43	1.43	1.41	1.41	1.42
10	1.79	1.79	1.79	1.78	1.68	1.64	1.58	1.53	1.51	1.48	1.48	1.79
5	1.46	1.50	1.49	1.46	1.46	1.45	1.43	1.42	1.43	1.42	1.43	1.43
0	1.42	1.44	1.43	1.42	1.41	1.42	1.40	1.41	1.42	1.42	1.42	1.41
-5	1.43	1.45	1.42	1.41	1.42	1.43	1.43	1.44	1.45	1.44	1.45	1.43
-10	1.43	1.44	1.42	1.40	1.43	1.45	1.45	1.49	1.49	1.47	1.44	1.43
-15	1.44	1.44	1.42	1.41	1.43	1.45	1.50	1.51	1.52	1.49	1.46	1.43
-20	1.54	1.50	1.49	1.47	1.45	1.57	1.59	1.66	1.75	1.79	1.79	1.61
-25	1.64	1.57	1.61	1.55	1.67	1.71	1.73	1.78	1.79	1.79	1.79	1.79
-30	1.59	1.56	1.54	1.53	1.51	1.51	1.58	1.56	1.60	1.73	1.61	1.62
-35	1.69	1.58	1.62	1.58	1.58	1.55	1.57	1.59	1.61	1.71	1.66	1.72
-40	1.62	1.57	1.55	1.52	1.55	1.50	1.52	1.59	1.54	1.59	1.61	1.61
-45	1.56	1.53	1.53	1.79	1.79	1.76	1.77	1.79	1.79	1.79	1.53	1.53
-50	1.62	1.56	1.59	1.79	1.79	1.79	1.79	1.79	1.79	1.79	1.58	1.59
-55	1.79	1.79	1.79	1.79	1.79	1.77	1.79	1.78	1.76	1.79	1.79	1.79

509

510 Table 7. PCT coefficients Θ from this study, and from the literature.
 511

source	85-89 GHz	36-37 GHz	19 GHz	10 GHz
This study	0.70 (GMI)	1.15 (GMI)	1.40 (GMI)	1.50 (GMI)
Spencer et al. 1989	0.818 (SSMI) 0.54-0.61 (model)			
Toracinta et al. 2002		1.20 (TMI)		
Weinman and Guetter 1977		1.50 (ESMR) 1.20 (model)		
Grody (1984)		1.08 (SMMR)	1.38 (SMMR)	
Barrett and Kidd (1990)	0.64 (SSMI)			
Todd and Bailey (1995); Kidd (1998)	0.5-0.75 (SSMI)			
Lee et al. (2002)		1.18		

512
 513

514 **9. List of Figures**

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555

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558 minimum brightness temperature (or PCT) in the domain is printed.

559

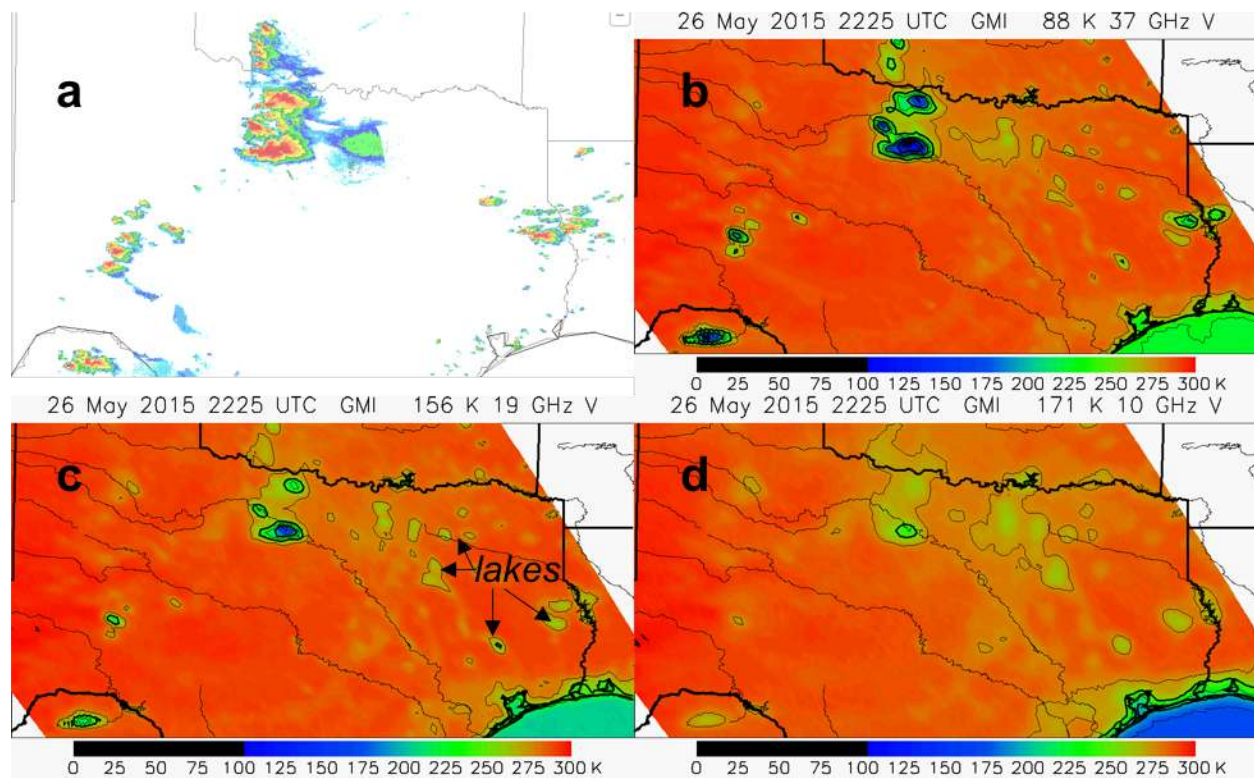


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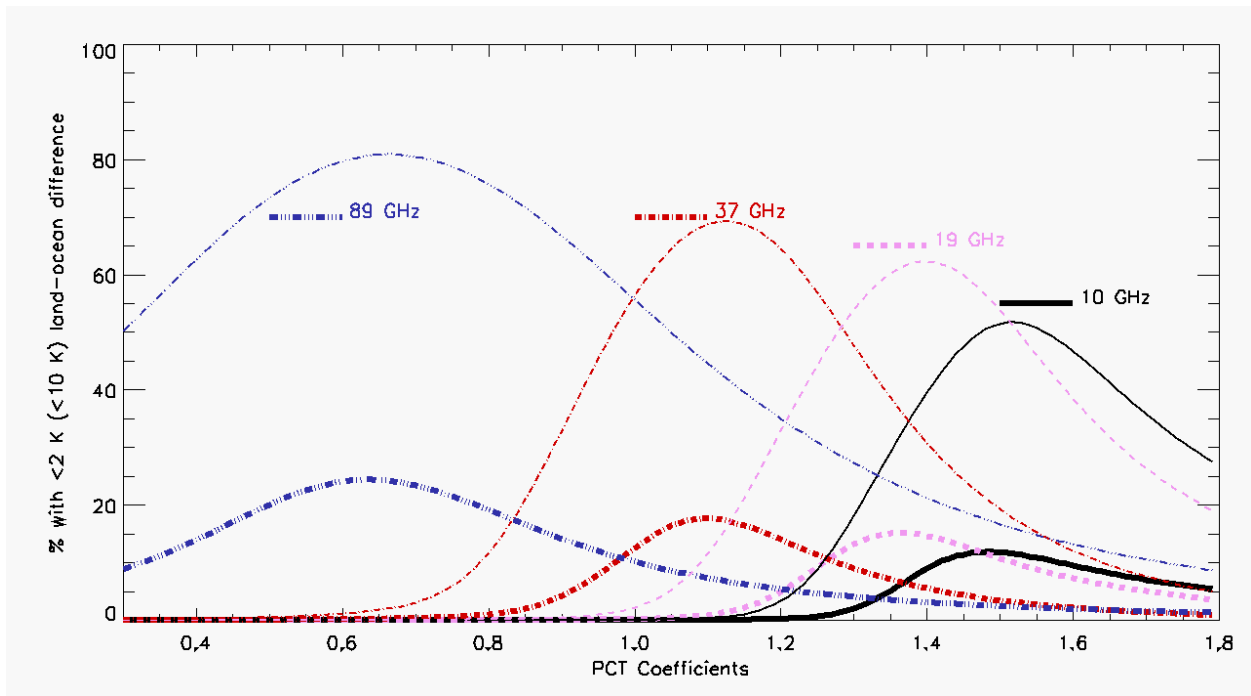


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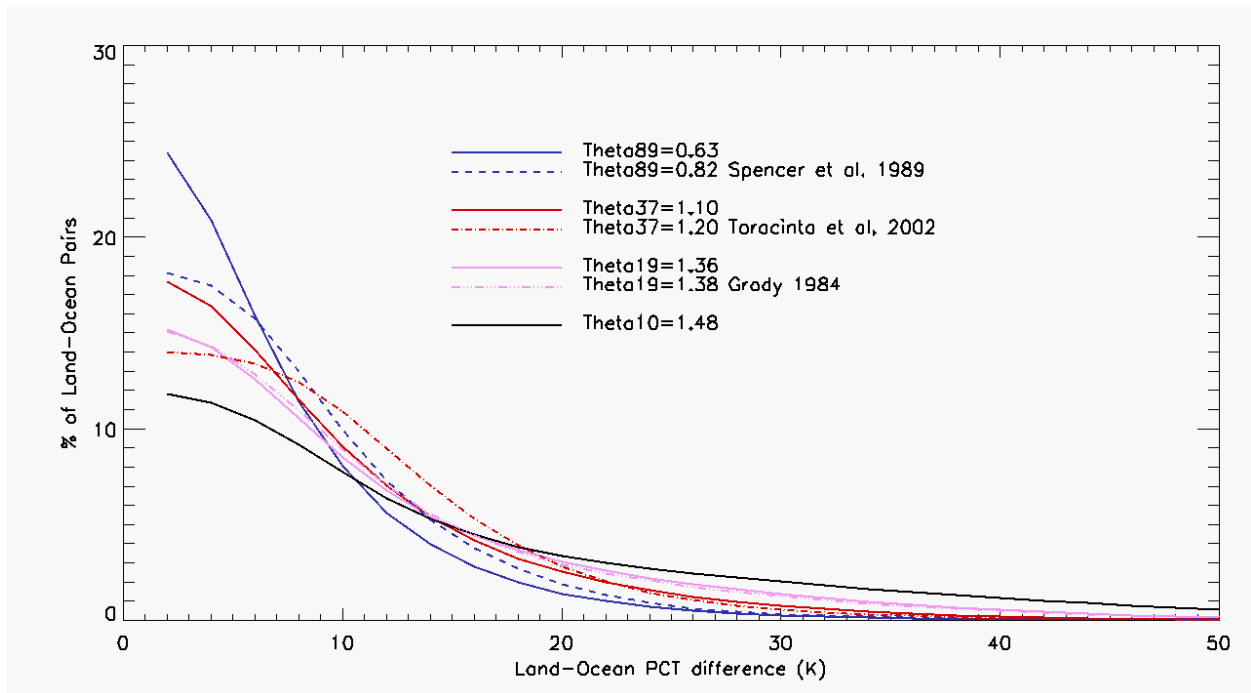


Figure 3. Probability density functions of the land-ocean PCT difference (bin size = 2 K) for selected PCT coefficients Θ .

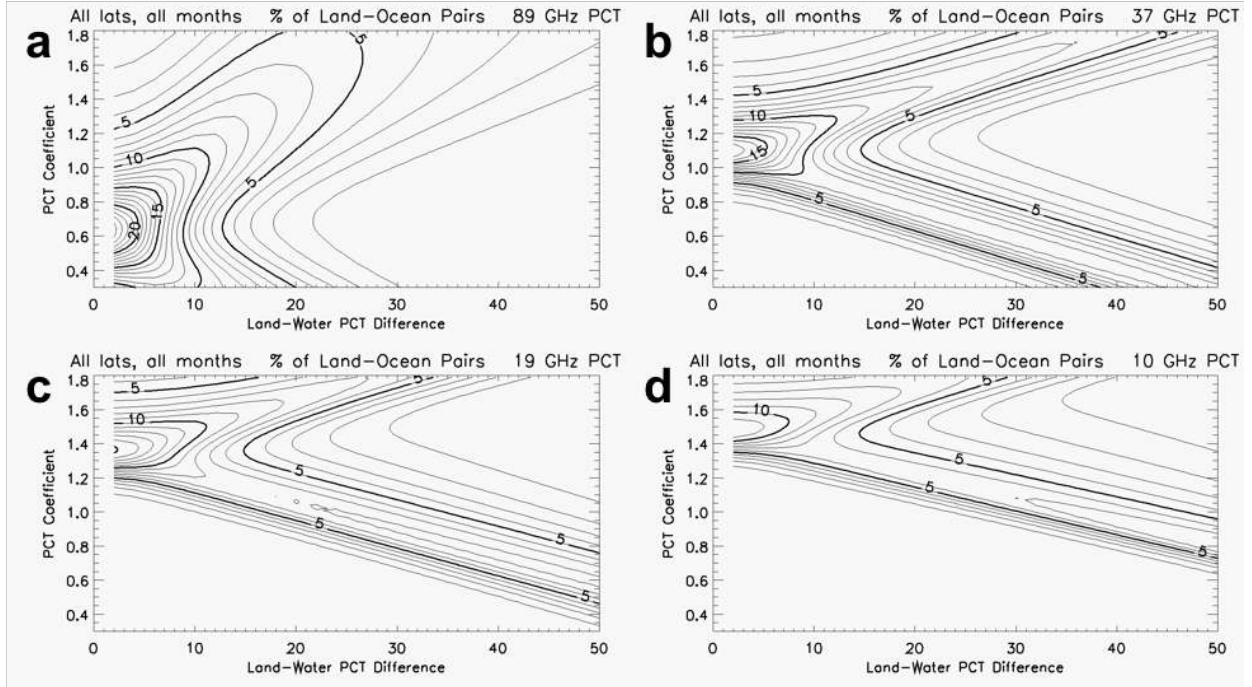


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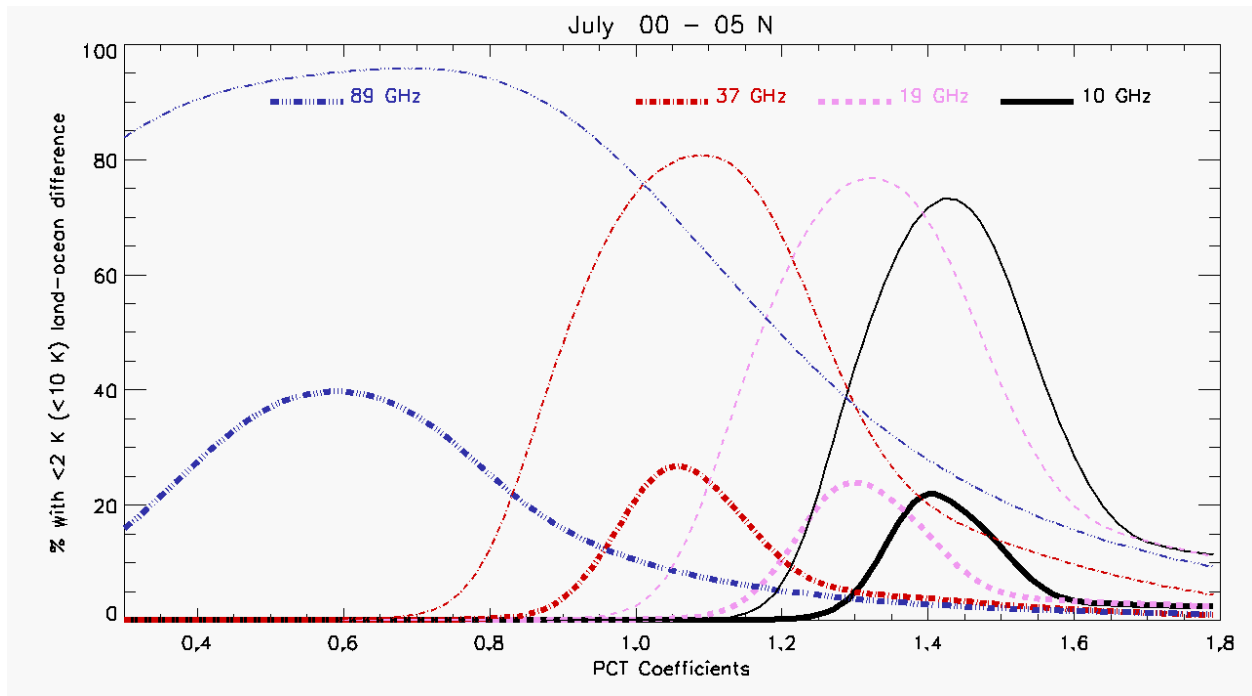


Figure 5. Percentage of land-ocean PCT differences less than 2 K (thick lines) and less than 10 K (thin lines), as a function of Θ value, for the $0^\circ - 5^\circ$ N latitude bin in July.

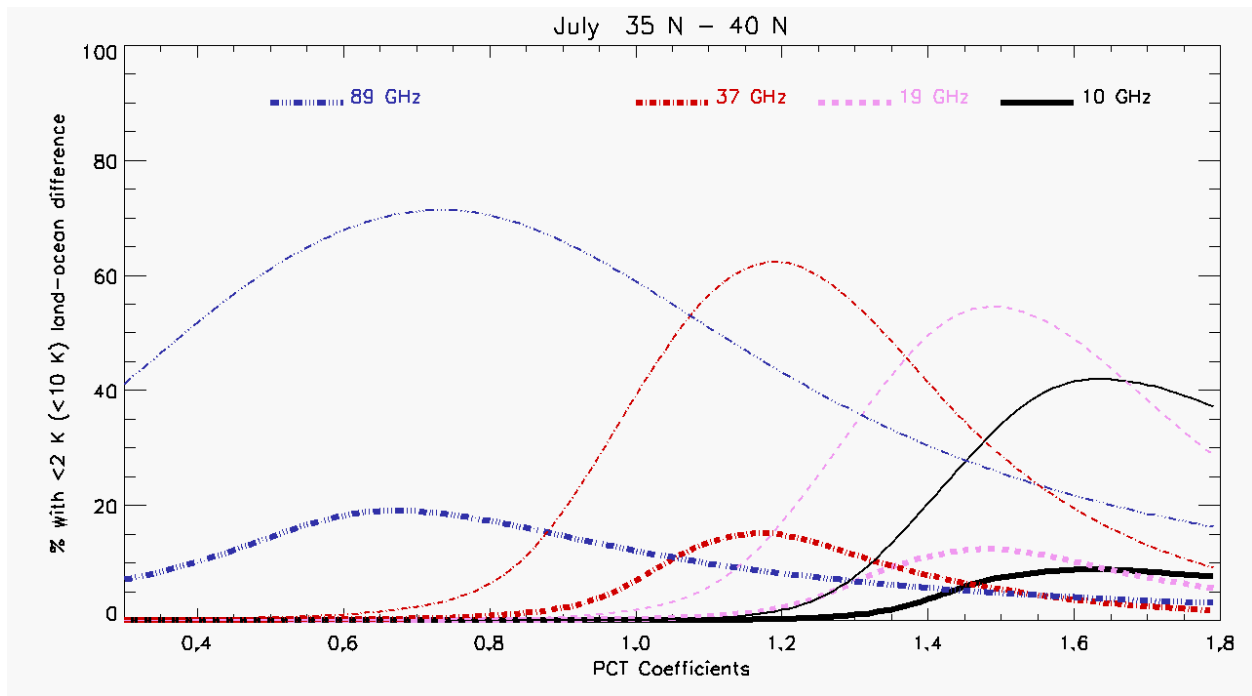


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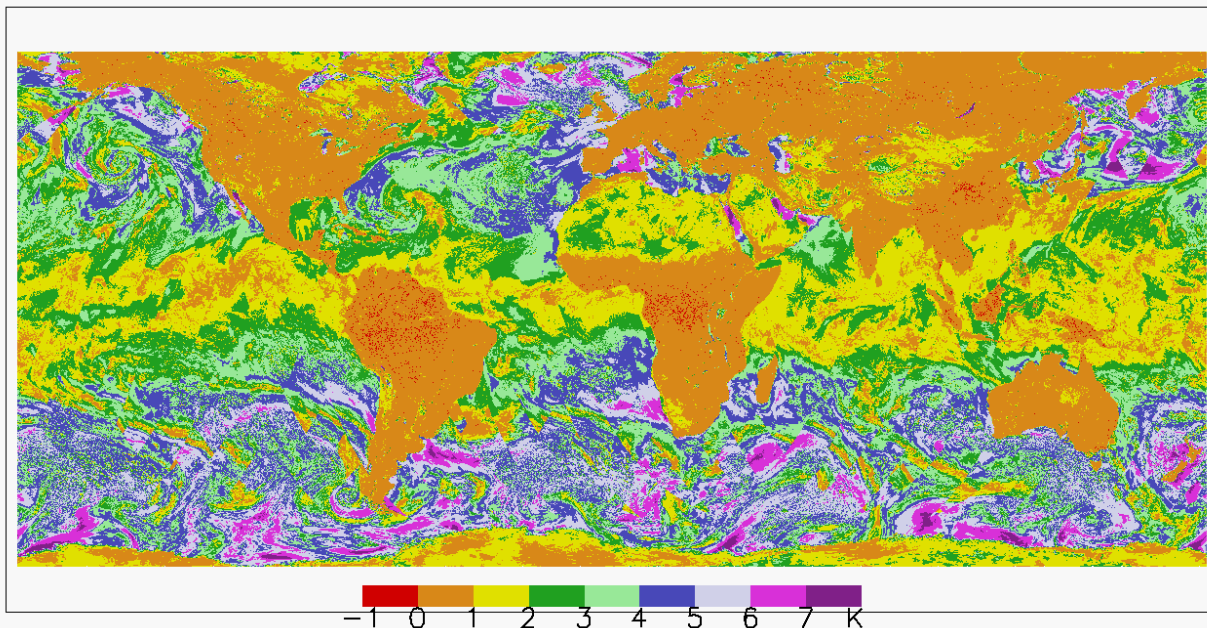


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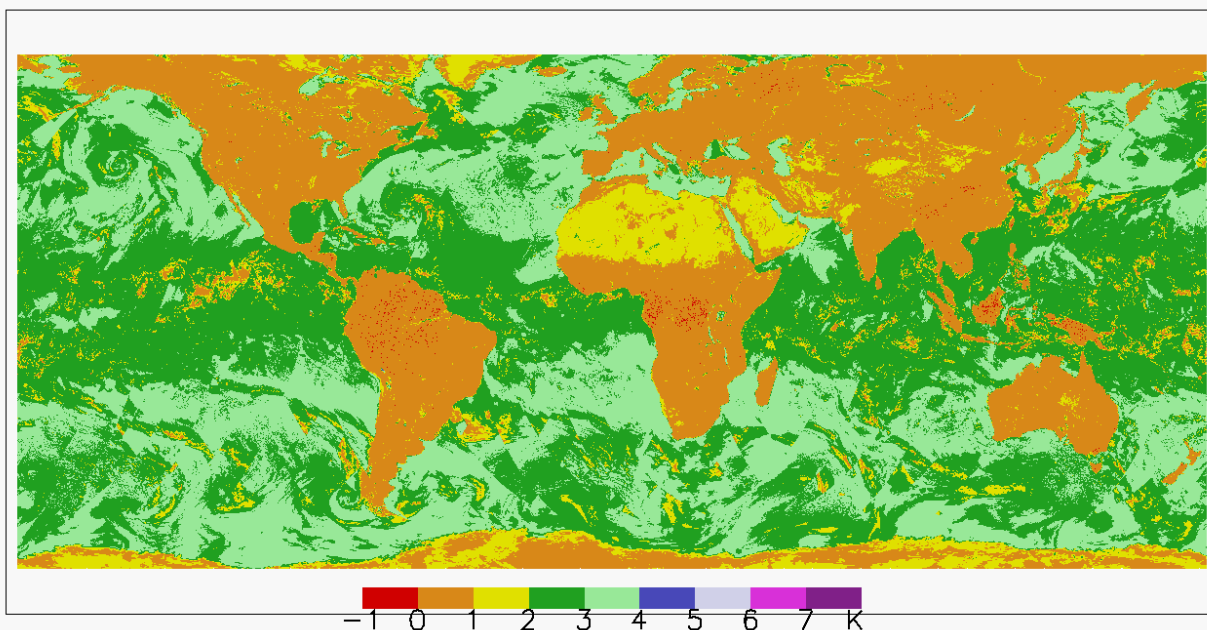


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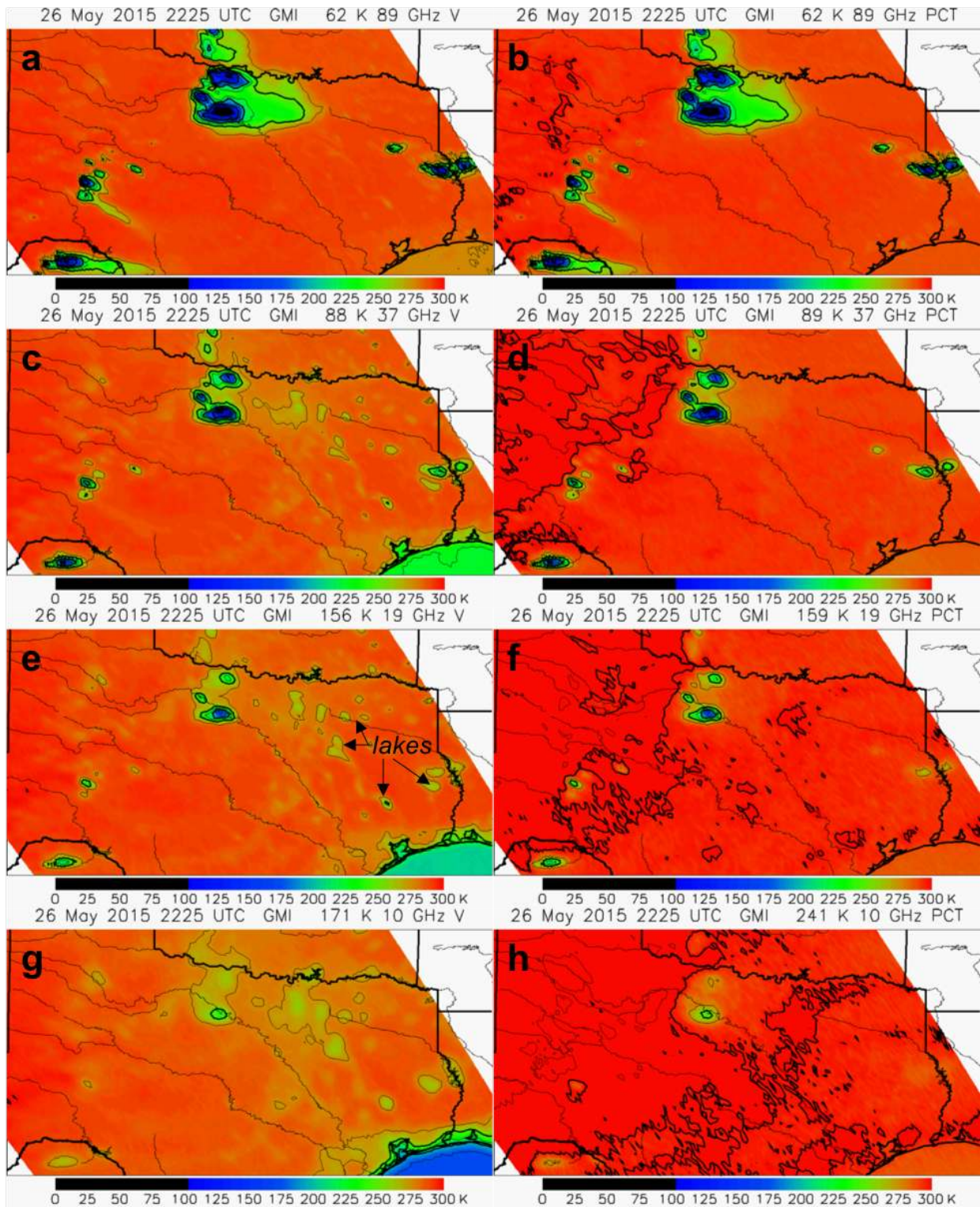


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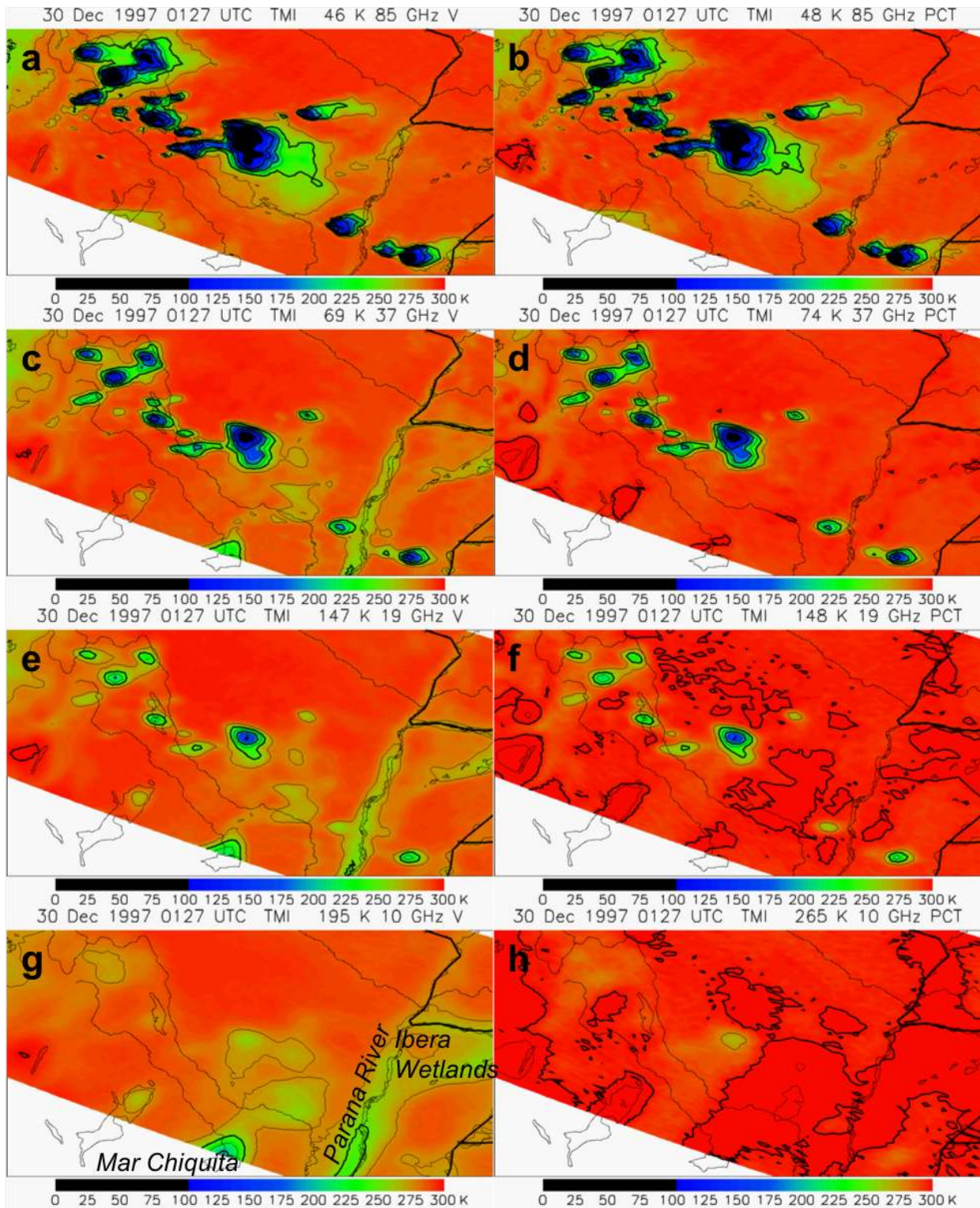


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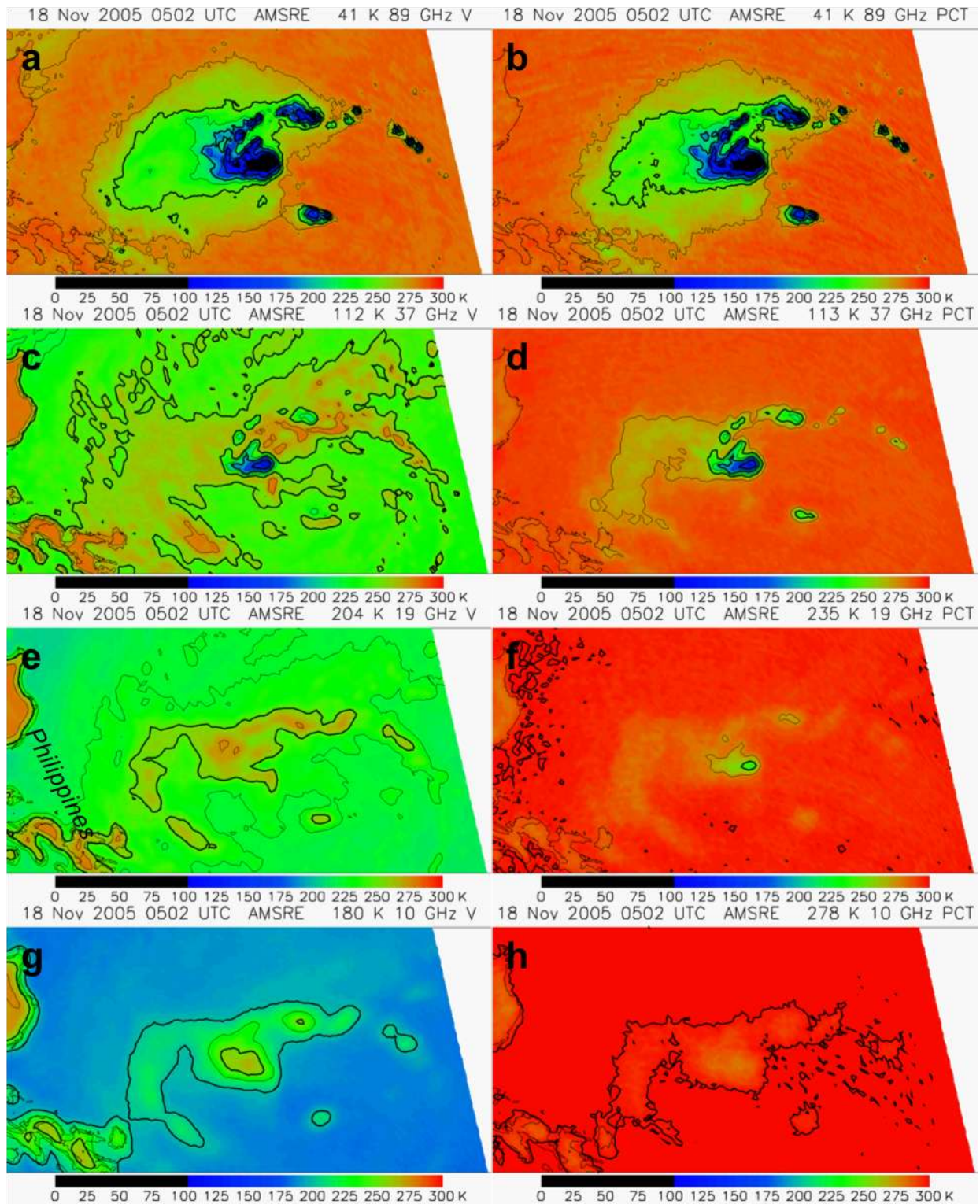


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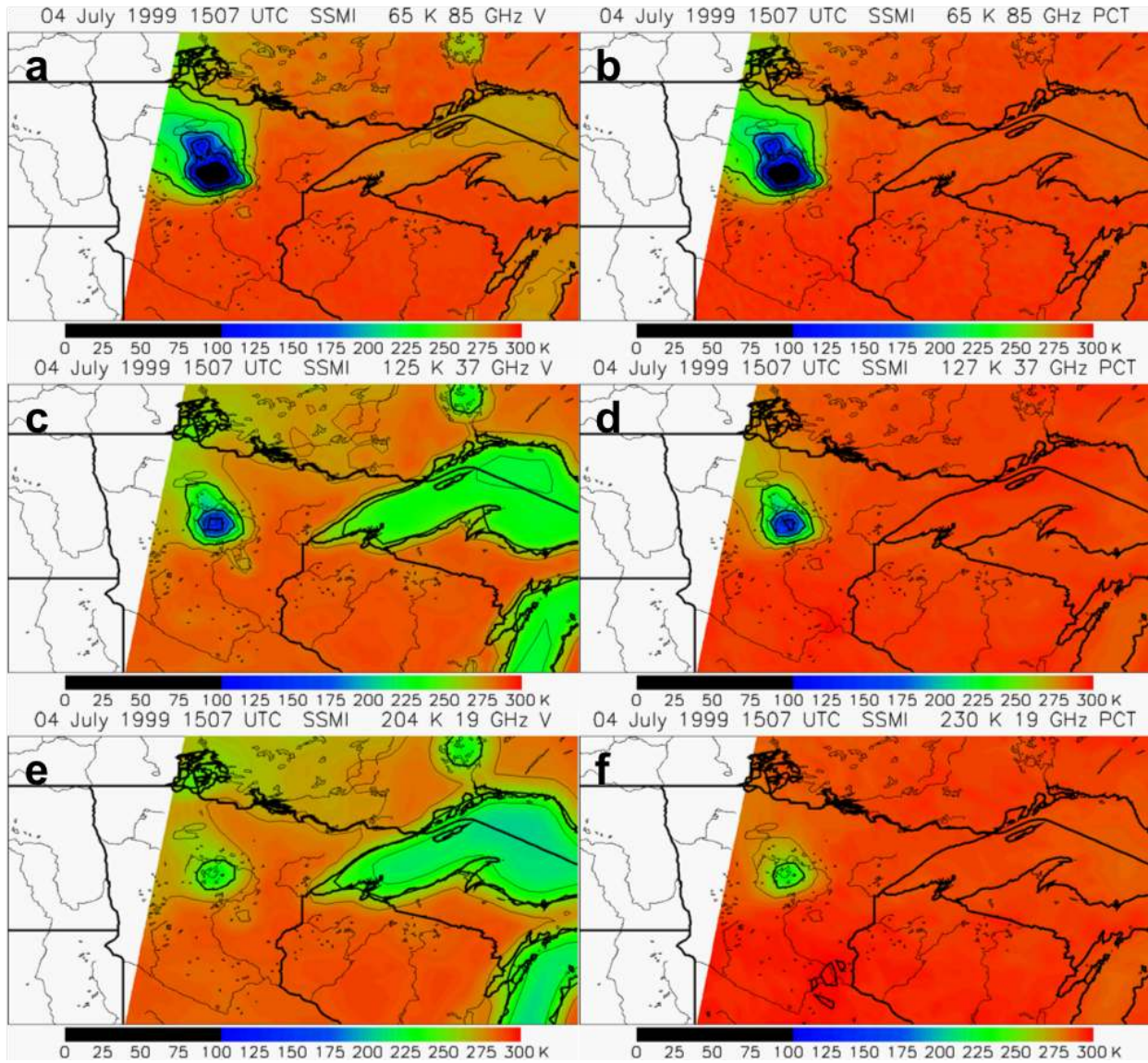


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