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Possible itinerant excitations and quantum spin state transitions in the effective spin-1/2 triangular-lattice antiferromagnet Na₂BaCo(PO₄)₂

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The most fascinating feature of certain two-dimensional (2D) gapless quantum spin liquid (QSL) is that their spinon excitations behave like the fermionic carriers of a paramagnetic metal. The spinon Fermi surface is then expected to produce a linear increase of the thermal conductivity with temperature that should manifest via a residual value (κ_0/T) in the zero-temperature limit. However, this linear in *T* behavior has been reported for very few QSL candidates. Here, we studied the ultralow-temperature thermal conductivity of an effective spin-1/2 triangular QSL candidate Na₂BaCo(PO₄)₂, which has an antiferromagnetic order at very low temperature ($T_N \sim 148$ mK), and observed a finite κ_0/T extrapolated from the data above T_N . Moreover, while approaching zero temperature, it exhibits series of quantum spin state transitions with applied field along the *c* axis. These observations indicate that Na₂BaCo (PO₄)₂ possibly behaves as a gapless QSL with itinerant spin excitations above T_N and its strong quantum spin fluctuations persist below T_N .

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he two-dimensional (2D) triangular lattice antiferromagnet (TAF) with spin-1/2 is one of the simplest geometrically frustrated systems with strong quantum spin fluctuations, which recently has caught attention due to its exotic quantum magnetism. One celebrated example is the 2D gapless quantum spin liquid (QSL)¹⁻⁴ that can host non-abelian quasiparticle⁵ and fractional excitations^{6,7} known as spinons^{8,9}, which allows quantum mechanical encryption and transportation of information with potential for creating a qubit that is protected against environmental influences¹⁰. Three experimental hallmarks have been widely accepted as evidence for spinon, including (i) a broad continuous magnetic intensity in the inelastic neutron scattering (INS) spectrum^{6,11,12}; (ii) a large magnetic specific heat with power law ($C \sim T^{\alpha}$) temperature dependence^{13–15}, and (iii) a nonzero residual thermal conductivity κ_0/T in the zero-temperature limit¹⁶⁻¹⁹. While most of the suggested 2D gapless QSLs exhibit the first two hallmarks, they do not exhibit the third one. In reality, so far only the organic EtMe₃Sb[Pd(dmit)₂]₂ reported by Yamashita et al.^{18,19} and the inorganic 1T-TaS₂ reported by Murayama et al.²⁰ exhibit a non-zero κ_0/T term, both of which are spin-1/2 TAFs. However, some other groups also reported a zero κ_0/T term in these two materials, raising a controversy^{21–23}. For another QSL candidate pyrochlore Tb₂Ti₂O₇, a saturated value of κ/T at 0.3 K was reported which resembles that of a dirty metal²⁴. For other oxides, such as YbMgGaO₄²⁵, another TAF with effective spin-1/2 Yb3+ ions, and Ca10Cr7O28 with bilayer kagome lattice²⁶, the reported κ_0/T term tends to be zero upon approaching zero temperature. This behavior could be closely related to the chemical disorder in both cases. For instance, YbMgGaO₄ has Mg²⁺/Ga³⁺ site mixture²⁷ and Ca₁₀Cr₇O₂₈ has disorder among the two different Cr³⁺ positions^{28,29}.

Another example of exotic magnetism in spin-1/2 TAFs is the quantum spin state transition. The theoretical studies have proposed that in a spin-1/2 TAF, the quantum spin fluctuations (QSFs) stabilize a novel up up down (UUD) phase while approaching zero temperature with the applied field parallel to either easy plane or easy axis^{30,31}. This UUD phase exhibits itself as a magnetization plateau within a certain magnetic field regime and with one-third of the saturation moment. Experimentally, it is very rare to observe such a UUD phase in TAFs while approaching zero temperature. One example is Ba₃CoSb₂O₉, another TAF with effective spin-1/2 Co²⁺ ions, which orders around 3.5 K and exhibits a UUD phase at ultralow temperatures^{32–34}. More recently, the UUD phase also has been proposed for $AYbCh_2$ (A = Na and Cs, Ch = O, S, Se), one TAF family with effective spin-1/2 Yb³⁺ ions³⁵⁻³⁸. Further detailed experimental and theoretical studies on Ba3CoSb2O9 revealed more complex quantum spin state transitions (QSSTs)³⁹⁻⁴⁵. Specifically, with increasing field along the *ab* plane, its 120° spin structure at zero field is followed by a canted 120° spin structure, the UUD phase, a coplanar phase (the V phase), and another coplanar phase (the V' phase) before entering the fully polarized state. While for B // c, the 120° spin structure will be followed by an umbrella spin structure and a V phase.

While searching for new spin-1/2 TAFs without chemical disorder to explore the novel physics of QSL and QSSTs, the new Co-based triangular lattice antiferromagnet Na₂BaCo(PO₄)₂⁴⁶ caught our attention. This system has a trigonal crystal structure with lattice parameter a = 5.3185 Å and c = 7.0081 Å. The magnetic CoO₆ octahedra form a triangular network in the *ab* plane, separated by a layer of nonmagnetic BaO₁₂ polyhedra. Meanwhile, the Na⁺ ions fill the gaps in the CoO₆ layers (Fig. 1a, b). Overall, no site mixture among the ions has been observed. Due to its Kramers ion nature, the Co²⁺ ions can be treated as effective spin-1/2 at low temperatures. The magnetic susceptibility, INS spectrum, and specific heat data show no magnetic

ordering down to 50 mK but with large magnetic specific heat and localized low-energy spin fluctuations. Then, as discussed above, to confirm whether this system is a truly gapless QSL or not, it is crucial to look for the possible existence of itinerant spinons. Moreover, until now, no magnetic phase diagram has been reported for this new TAF and its possibility for QSSTs is awaiting exploration.

Results

Magnetic susceptibility. By following the recipe in ref. ⁴⁶, we grew single crystals of Na₂BaCo(PO₄)₂. Figure 1c shows the inverse of the DC magnetic susceptibility $(1/\chi)$ with applied field B // ab. A change of slope is observed around 50 K. The effective moment is estimated to be 5.37 $\mu_{\rm B}$ for 150 < T < 300 K and 4.0 $\mu_{\rm B}$ for 2 < T < 20 K by using the linear Curie–Weiss fittings. This decrease of effective moment indicates a crossover of spin state for Co^{2+} ions from S = 3/2 at high temperatures to an effective spin-1/2 at low temperatures. For Co²⁺⁺ ions in an octahedral environment, as for Na2BaCo(PO4)2, the crystal field and spinorbital coupling can lead to a Kramers doublet with the effective spin-1/2 as the ground state. For other triangular lattice antiferromagnets with octahedral Co sites, such as Ba₃CoSb₂O₉³² and $ACoB_3$ (A = Cs, Rb; B = Cl, Br)⁴⁷, the ground state also has effective spin-1/2. Therefore, the $\theta_{\rm CW} = -2.5$ K from the lowtemperatures fitting represents its intrinsic antiferromagnetic exchange energy. According to the mean field theory, θ_{CW} is given as $(-zJS(S+1))/3k_B$, where J is the exchange interaction of the Heisenberg Hamiltonian $J\Sigma_{(i,j)}S_iS_j$, and z is the number of nearest neighbors. For the effective S = 1/2 triangular lattice with z = 6, we obtained $J/k_{\rm B} = -2/3\theta_{\rm CW} = 1.7$ K.

Thermal conductivity. Figure 2a shows the zero-field thermal conductivity of Na₂BaCo(PO₄)₂ in the temperature range of 70 mK to 30 K. At higher temperature, it behaves like a usual insulating crystal. The peak at 12 K with a large value of 90 WK⁻¹ m⁻¹ can be understood as the so-called phonon peak. It is notable that such a large phonon peak indicates high quality of the single crystal sample. Also shown are the thermal conductivity in 14 T field, either along the *c* or the *a* axis, which can increase the κ at most temperatures up to 7 K.

Figure 2b–d show the ultralow-temperature thermal conductivity at 0 T and 14 T fields. Several features are noteworthy. First, all these data are well fitted by $\kappa/T = \kappa_0/T + bT^2$ with *b* as a constant in a very broad temperature range (from several tens to 500 mK or more, particularly up to 700 mK for zero field), while the fitting parameters κ_0/T and *b* are clearly different for them. Second, in zero field the fitting gives $\kappa_0/T = 0.0062 \text{ WK}^{-2} \text{ m}^{-1}$, that is, the presence of a residual value in κ/T while extending to zero temperature is clearly resolved. Third, the fitting curves in Fig. 2 yield intercepts of $0 \pm 0.0005 \text{ WK}^{-2} \text{ m}^{-1}$ for data with 14 T l/c and 14 T l/a. The error is at least one order of magnitude smaller than the zero-field κ_0/T value, which indicates zero κ_0/T for the 14 T data.

Specific heat. As shown in the inset to Fig. 2b, the zero-field $\kappa(T)$ data also shows a very weak anomaly around 100 mK. To learn the nature of this anomaly, the specific heat (C_p) was measured at very low temperatures down to 50 mK, as shown in Fig. 3. At zero field, the C_p exhibits a broad peak around 630 mK followed by a small and sharp peak at 148 mK. This sharp peak should represent an antiferromagnetic ordering, which is likely related to the anomaly observed from the zero field $\kappa(T)$. With increasing field along the *c* axis, this peak's position shifts to ~310 mK for B = 0.5 and 1 T; meanwhile, its intensity abruptly increases for B = 0.5 and 1 T and then this peak disappears for B = 1.5 T, as shown in Fig. 3a. By



Fig. 1 Structure and magnetic susceptibility of Na₂BaCo(PO₄)₂. a The crystallographic structure. **b** The triangular lattice of Co²⁺ ions in the *ab* plane. **c** The inverse of the DC susceptibility measured with 0.1T magnetic field along the *ab* plane. The solid lines are the Curie-Weiss fittings to high-temperature or low-temperature data.



Fig. 2 Ultralow-temperature thermal conductivity of Na₂BaCo(PO₄)₂. a The zero-field thermal conductivity of Na₂BaCo(PO₄)₂ in temperature range of 70 mK - 30 K. The heat current is along the *a* axis. The peak at 12 K is the so-called phonon peak. Also shown are the thermal conductivity in 14 T magnetic field along the *c* or the *a* axis. In most of this temperature region, high magnetic field enhances the thermal conductivity. **b** Data in zero field plotted in κ/T vs T^2 . The solid line is a linear fit of the data at T < 700 mK. A nonzero residual thermal conductivity $\kappa_0/T = 0.0062$ WK⁻² m⁻¹ is resolved. The inset shows a magnified view of the lowest-temperature data. There is a very weak anomaly at T < 100 mK. **c**, **d** Thermal conductivity in 14 T magnetic field plotted as κ/T vs T^2 . The solid lines are a linear fits for data at T < 550 mK (for B / / c) and at T < 500 mK (for B / / a). There is no residual term ($\kappa_0/T = 0$).

assuming that the lattice contribution can be described by $C_{\rm ph} = \beta T^3 + \beta_5 T^5 + \beta_7 T^7$ with $\beta = 8.83 \times 10^{-4}$ JK⁻⁴mol⁻¹, $\beta_5 = -3.32 \times 10^{-7}$ JK⁻⁶ mol⁻¹, and $\beta_7 = 6.67 \times 10^{-11}$ JK⁻⁸ mol⁻¹ (see Supplementary Fig. 1), the change of magnetic entropy below 4 K, $\Delta S_{\rm mag}$, was calculated by integrating $(C_{\rm p}-C_{\rm ph})/T$ (Fig. 3b). The obtained values are 5.1 and 5.4 JK⁻¹ mol⁻¹ for B = 0 and 1 T, respectively, which are approaching the value of Rln2. This is another strong evidence that Na₂BaCo(PO₄)₂ can be treated as an effective spin-1/2 system. At zero field, the recovered entropy below 200 mK (where the peak starts) is 1.6 JK⁻¹mol⁻¹. This is only 28% of Rln2, which indicates the strong spin fluctuations above $T_{\rm N}$. A small upturn of

the specific heat is observed at the lowest temperatures, which could be attributed to a contribution from the nuclear entropy. Figure 3c shows the specific heat data for B // a. Similar to the results for B // c, the low magnetic fields along the a axis can also change the position of the peak at 148 mK but with weaker field dependence.

Residual thermal conductivity. It is abnormal for Na₂BaCo (PO₄)₂ to exhibit a non-zero κ_0/T term extrapolated from the data above T_N . One possible scenario is that it behaves as a QSL above T_N with gapless magnetic excitations, which give rise to power-law temperature dependences of the low temperature physical



Fig. 3 Ultralow-temperature specific heat of Na₂BaCo(PO₄)₂. a, **c** The zero-field data and those in different magnetic fields along the *c* axis or the *a* axis. The temperature range is 50 mK to 4 K. **b**, **d** The magnetic entropy for B // c and B // a, obtained by integrating the magnetic specific heat.

properties. Indeed, the reported INS spectrum⁴⁶ and specific heat data reported here support the presence of strong spin fluctuations above T_N . While the 2D QSL is stable at zero temperature in the strict sense, it is also known that QSL behavior, such as spinon excitations can survive at a finite temperature regime if the temperature scale is smaller than the exchange interaction, J. To our knowledge, a couple of quantum magnets exhibit quantum spin disordered states including QSL in a temperature range $T_{\rm N}\,{<}$ T < J due to the combination of strong geometrical frustration with enhanced quantum spin fluctuations for spin-1/2, as present in Na₂BaCo(PO₄)₂ with $T_N = 148$ mK and $J \sim 1.7$ K. One good example is the Volborthite, $Cu_3V_2O_7(OH)_2\cdot 2H_2O$, with a 2D distorted kagome lattice of Cu^{2+} (S = 1/2) ions, which antiferromagnetically orders at $T_N \sim 1$ K with exchange constant $J \sim$ 60 K^{48,49}. A finite linear *T*-dependent contribution of specific heat extrapolated to $T = 0 \text{ K}^{48}$ and a negative thermal Hall conductivity observed above T_N^{49} both strongly support the presence of a QSL state with gapless spin excitations above T_N for Volborthite. While no clear non-zero κ_0/T term was observed for Volborthite due to its relatively high ordering temperature, the estimated mean free path of the spin excitations from the 8K magnetic thermal conductivity is about 80 times its inter-spin distance, which indicates its spin excitations are highly mobile⁴⁹. The related theoretical work also proposes the existence of spinon Fermi surface in Volborthite above $T_N^{50,51}$. Another relevant example is pyrochlore $Yb_2Ti_2O_7$ with effective spin-1/2 Yb^{3+} ions, which ferromagnetically orders at $T_{\rm C} \sim 0.2$ K⁵². For Yb₂Ti₂O₇, the XY and off diagonal components of the interactions, $J_{\perp} \sim 0.58$ K and $J_{z\pm} \sim 1.7$ K, respectively, produce quantum spin fluctuations^{53,54}. Its reported specific data suggests strong

quantum fluctuations above $T_{\rm C}^{55,56}$. Its observed diffuse scattering and pinch point structure of the INS spectrum and related model calculation further suggest the presence of a quantum spin ice state above $T_{\rm C}^{57}$. Lately, the unusual behavior of the magnetothermal conductivity⁵⁸ and thermal Hall conductivity⁵⁹ suggests the emergence of highly itinerant quantum magnetic monopoles in this quantum spin ice state.

By following ref. ¹⁸'s method, we estimate the mean free path (l_s) and life time of the spin excitation (τ_s) of the quasiparticles responsible for the excitations in Na₂BaCo(PO₄)₂ by calculating $\frac{k_0}{T} = \frac{\pi \kappa_B^2}{9h} \frac{l_s}{ad} = \frac{\pi}{9} \left(\frac{\kappa_B}{h}\right)^2 \frac{l}{d} \tau_s.$ Here, $a \ (\sim 5.32 \text{ Å})$ and $d \ (\sim 7.01 \text{ Å})$ are nearest-neighbor and interlayer spin distance, respectively. From the observed $\kappa_0/T = 0.0062$ WK⁻² m⁻¹, the l_s is obtained as 36.6 Å, indicating that the excitations are mobile to a distance seven times as long as the inter-spin distance without being scattered. Third, in high magnetic field of 14 T, although the κ is much larger than the zero-field data, the fitting gives a negligibly small value of, or vanishing κ_0/T . This is reasonable since 14 T is strong enough to polarize all spins and completely suppress the spinon excitations of the QSL state. Thus, the 14 T data should be a result of pure phonon heat transport. From the specific heat data (see Supplementary Fig. 1), it is found that the phonon specific heat can be approximated as $C_{\rm ph} = \beta T^3$ at very low temperatures with the coefficient $\beta = 8.83 \times 10^{-4} \, \text{JK}^{-4} \, \text{mol}^{-1}$. The phonon velocity can be calculated from the β value as $v_{\rm ph} = 2430 \, {\rm m s}^{-1}$. The phonon thermal conductivity in the ballistic scattering limit is $\kappa_{\rm ph} = (1/3)C_{\rm ph}v_{\rm ph}l_{\rm ph}$, where the phonon mean free path is determined by the averaged sample width of $l_{\rm ph} = 2\sqrt{A/\pi} = 0.32 \, {\rm mm}$ for this sample. Thus, the phonon

thermal conductivity at low temperature is expected as $\kappa_{\rm ph} = 2.21 \times T^3 \, {\rm WK^{-1}} \, {\rm m^{-1}}$. Note that this estimation is different from the 14 T data by only a factor of 2, which is acceptable. If one assumes that the 14 T data is purely due to the phonon term, much smaller signal in zero field indicates that the phonon ballistic scattering limit is not achieved, although κ/T nicely follows $\kappa_0/T + bT^2$. Therefore, in zero field the phonons are always suffering some scattering effect besides the boundary. Apparently, at very low temperatures only the magnetic excitations can take the role of phonon scattering.

Another possible scenario is that this non-zero κ_0/T term is related to other abnormal quasiparticles besides spinon, which means the high-T (> T_N) phase may not be ascribed to the QSL. Either way, future studies are desirable to learn the exact origin for this interesting residual thermal conductivity in Na₂BaCo (PO₄)₂.

Field dependence of thermal conductivity and AC susceptibility. The dramatic change of the C_p peak with B // c suggests the possibility of spin state transitions. For further investigation, more detailed κ and AC susceptibility in magnetic fields were measured. For B // c, the $\kappa(B)$ curve at 92 mK exhibits four minima at B_{c1} , B_{c2} , B_{c3} , and B_{c4} (Fig. 4a). With increasing temperatures, $\kappa(B)$ only exhibits two minima at 151 mK and no minimum at T > 300 mK. The $\kappa(T)$ measured at 0.5 and 1.0 T (Fig. 4b) clearly shows a slope change around 310 mK, which is consistent with the C_p peaks' position measured at the same fields. The AC susceptibility, χ' , measured at 22 mK (Fig. 4c) shows three peaks at B_{c1} , B_{c2} , and B_{c3} . The values of these three critical fields are consistent with the B_{c1} , B_{c2} , and B_{c3} observed from $\kappa(B)$. With increasing temperatures, the B_{c1} peak shifts to higher fields and the B_{c2} and B_{c3} peaks shifts to lower fields. At T > 280 mK, the peaks almost disappear. Since the measured χ' shows no frequency dependence (not shown here), it could be approximately treated as the derivative of the DC magnetization M(B). We calculated M(B) by integrating χ' . The obtained M(B)at 22 mK (Fig. 4d) clearly shows a plateau regime between B_{c1} and B_{c2} and a slope change at B_{c3} followed by saturation around 2.5 T. Although we cannot infer the absolute value of M(B) here, it is obvious that the magnetization of the plateau (around 0.29, here we scaled the M value to the 3 T value) is around 1/3 of the saturation value (around 0.84 after we subtract the Van Vleck paramagnetic background, which is the upper dashed line in Fig. 4d).

For comparison, the above measurements were also performed for B // a. The $\kappa(B)$ curve (Fig. 5a) at 92 mK shows two minima at B_{a1} and B_{a2} , while the $\kappa(T)$ (Fig. 5b) measured at different fields shows no obvious slope change. The χ' (Fig. 5c) measured at 25 mK shows a broad peak around B_{a1} and a sharp peak around B_{a2} . With increasing temperature, B_{a1} and B_{a2} shift to higher and



Fig. 4 Thermal conductivity and AC susceptibility of Na₂BaCo(PO₄)₂ for *B* **//** *c***. a Magnetic-field dependence of thermal conductivity at different temperatures. For clarifying, the 151 mK, 252 mK and 380 mK curves are shifted upward by 0.5, 1.0 and 1.5, respectively. At 92 mK, there are four minima indicated by arrows. With increasing temperature, the minima become weaker and disappear above 380 mK. b** Temperature dependence of κ in different fields. At low fields of 0.5 and 1.7, there is a clear slope change of $\kappa(T)$ curves around 310 mK, which has good correspondence to the specific-heat anomaly. **c** AC magnetic susceptibility at different temperatures. There are three peaks in the low-temperature curves. **d** Magnetization curves obtained by integrating the AC susceptibility data and renormalized with the 3 T value. The lower dashed line indicates a -1/3 plateau and the upper dashed line indicates the Van Vleck paramagnetic background.



Fig. 5 Thermal conductivity and AC susceptibility of Na₂BaCo(PO₄)₂ for *B* **//** *a***. a Magnetic-field dependence of thermal conductivity at different temperatures. For clarifying, the 151 mK, 252 mK and 380 mK curves are shifted upward by 0.5, 1.0 and 1.5, respectively. At very low temperatures, there are two minima on the \kappa(***B***) curves which disappear above 252 mK. b** Temperature dependence of κ in different fields. No clear anomaly is observed. **c** AC magnetic susceptibility at different temperatures. There are two peaks in the low-temperature curves. **d** Magnetization curves obtained by integrating the AC susceptibility data and renormalized with the 3 T value. The dashed line indicates the Van Vleck paramagnetic background.

lower fields, respectively, and both disappear at T > 290 mK. The calculated M(B) at 25 mK shows a slope change around the $1/3M_s$ position. These results are clearly different from those for B // c.

Phase diagram. Based on the critical fields and ordering temperatures presented above, the magnetic phase diagrams for B // cand *B* // *a* are constructed in Fig. 6. For *B* // *a*, since both the $\kappa(B)$ and χ' data consistently show two critical fields and B_{a2} is very close to the field where the magnetization becomes flat (or saturated), it is natural for us to assign B_{a2} as the saturation field and B_{a1} as a critical field for a spin state transition. On the other hand, for B // c, the $\kappa(B)$ exhibits four critical fields while the χ' shows three. Here we assign the B_{c4} as the saturation field for two reasons: (i) if we assign B_{c3} as the saturation field, it will be difficult to understand why there is still a possible spin state transition at $B_{c4} > B_{c3}$ after all spins have been polarized; (ii) a close look of the calculated M(B) curve shows that B_{c3} represents a slope change before the magnetization becomes flat, which most likely represents a spin state transition. One possible situation is that since this B_{c3} peak of χ' data is so close to the saturation field position, it may smear out the expected χ' peak at B_{c4} . Accordingly, besides the paramagnetic phase at high temperatures and fully polarized phase at high fields, with increasing field, there are four phases for B // c (Fig. 6a) and two phases for B // a (Fig. 6b).

Now we compare the phase diagrams of Na₂BaCo(PO₄)₂ to those of Ba₃CoSb₂O₉ listed in the introduction. For *B* //*c* we are confident that the phase II is the UUD phase based on the $1/3M_s$

plateau observed at 22 mK. Since the 120° spin structure is a prerequired phase for the appearance of UUD phase, we ascribe the phase I as the canted 120° spin structure. Whether the phase III and IV are the V and V' phase or the phase I and II for B // a are the umbrella and V phases or not cannot be said at this stage. Further studies such as neutron diffraction are needed to address this question.

We emphasize that in Na₂BaCo(PO₄)₂, the UUD phase only survives for *B* // *c*, which strongly suggests its easy axis anisotropy as the theory predicted³¹. Ba₃CoSb₂O₉ and AYbCh₂ are both TAFs with easy plane anisotropy. To our knowledge, Na₂BaCo (PO₄)₂ is a very rare example of spin-1/2 TAF with single crystalline form to exhibit series of QSSTs along the easy axis. Another two examples for spin-1/2 TAFs with easy axis anisotropy to show UUD phase are Ba₃CoNb₂O₉^{60,61} and Ba₂La₂CoTe₂O₁₂⁶², but both of them are polycrystalline form.

Discussion

In summary, we clearly observed a nonzero residual thermal conductivity, κ_0/T , extrapolated from the data above T_N (~148 mK) in an effective spin-1/2 triangular antiferromagnet Na₂BaCo (PO₄)₂. This abnormal feature indicates that Na₂BaCo(PO₄)₂ possibly behaves as a gapless QSL with itinerant spin excitations above T_N . Moreover, its strong quantum spin fluctuations persist below T_N and help to stabilize a series of spin state transitions while approaching zero temperature. With applied field along the *c* axis, this includes the UUD phase with a 1/3 M_s magnetization



Fig. 6 Phase diagram of Na₂BaCo(PO₄)₂. The magnetic phase diagrams of Na₂BaCo(PO₄)₂ for *B* // *c* (**a**) and *B* // *a* (**b**). The data points are obtained from the AC susceptibility (AC), specific heat (*C*_p) and temperature or field dependence of thermal conductivity (κ (*T*) and κ (*B*)) measurements. The dashed lines are phase boundaries. For *B* // *c*, there are four phases (I, II, III, and IV) in the low-temperature and low-field for *B* // *a*. The dashed lines are a guide to the eye.

plateau. This makes $Na_2BaCo(PO_4)_2$ a unique TAF with easy axis anisotropy to exhibit a UUD phase.

Methods

Sample preparation and characterization. The single crystals were grown by flux method as reported in ref. ⁴⁶. One adjustment made is that Platinum crucibles instead of alumina crucibles were used in our growth. The powder X-ray diffraction measurement on the ground single crystals confirmed its lattice structure is the same as reported in ref. ⁴⁶. Laue back diffraction confirmed the flat surface of the as grown crystals is the *ab* plane. DC magnetic susceptibility was measured with a Quantum Design superconducting quantum interference device (SQUID) magnetometer. The applied field B = 0.1 T is parallel to the *ab* plane. Specific heat was measured with a Quantum Design Physical Property Measurements System (PPMS), equipped with a dilution refrigerator insert.

AC susceptibility measurements. The AC susceptibility measurements were conducted with a voltage controlled current source (Stanford Research, CSS80) and lock-in amplifier (Stanford Research, SR830). The phase of the lock-in amplifier is set to measure the first harmonic signal. Single crystal samples of Na₂BaCo(PO₄)₂ were prepared to allow the AC and DC magnetic fields to be perpendicular and parallel to the *c* axis separately in the measurements. The rms amplitude of the ac excitation field is set to be 0.6 Oe with the frequency fixed to be 220 Hz. The measurements were performed at SCM1 of the National High Magnetic Field Laboratory, Tallahassee, by using a dilution refrigerator. The data was obtained by the zero field cooling process and we increased the magnetic field during the ramping process.

Thermal conductivity measurements. Thermal conductivity was measured by using a "one heater, two thermometers" technique in a ³He/⁴He dilution refrigerator and in a ³He refrigerator, equipped with a 14 T superconducting magnet^{63–73}. The sample was cut precisely along the crystallographic axes with dimensions of $3.0 \times 0.63 \times 0.14$ mm³, where the longest and the shortest dimensions are along the *a* and the *c* axes, respectively. The heat currents were applied along the *a* axis while the magnetic fields were applied along either the *a* or *c* axis. Since the AC susceptibility clearly showed no hysteresis with sweeping field, we did not perform all the specific heat and thermal conductivity measurements with the zero-field cooling process. However, we carefully checked the first $\kappa(B)$ measurement at 92 mK for both *B* // *c* and *B* // *a*. The sample was zero-field cooled to 92 mK and the κ was measured with increasing field to 14 T and then decreasing field to 0 T. No hysteresis was observed in $\kappa(B)$.

For low-temperature thermal conductivity measurements, calibrating the magnetoresistance effect of resistor thermometers is a basic requirement. The thermometers (RuO₂) used at 300 mK to 30 K in the ³He refrigerator are precalibrated by using a capacitance sensor (Lakeshore Cryotronics) as the reference^{65,67-69}; the thermometers (RuO₂) used at 50 mK to 1 K in the dilution refrigerator are pre-calibrated by using a RuO2 reference sensor (Lakeshore Cryotronics) mounted at the mixture chamber (the superconducting magnet was equipped with a cancellation coil at the height of mixture chamber)7 The resolution of the κ measurements is typically better than 3% (better at higher temperature). The sample size was determined by using microscopy and has uncertainty of <5%. Therefore, the total error bar of is κ always < 8%. The uncertainty of κ_0/T caused by the fitting is ~2%. The κ_0/T value of Na₂BaCo(PO₄)₂ is ~30 times smaller than that of $EtMe_3Sb[Pd(dmit)_2]_2$ and ~10 times smaller than that of 1T-TaS_2^{18-20} . One may ask whether this value is too small to be resolved by the κ measurement at ultralow temperatures. We would like to mention that this residual thermal conductivity is actually comparable to those in high- T_c cuprate superconductors (HTSC). For HTSC, the κ_0/T is contributed by the nodal quasiparticles from the *d*-wave superconducting state and has been experimentally observed by us in many materials, including La_{2-x}Sr_xCuO₄, YBaCu₃O₁₂ Bi₂Sr₂₋ $_{x}La_{x}CuO_{6+\delta}$, and Bi₂Sr₂CaCu₂O_{8+ δ}⁶⁴⁻⁶⁷. In these materials, it is well resolved that the κ_0/T varies from 0.0015 to 0.06 WK⁻²m⁻¹ and shows systematic changes with the carrier concentration. Similar experimental results have also been reported by other groups for both the cuprate and the iron-based superconductors⁷⁴ Therefore, a κ_0/T value of 0.0062 WK⁻²m⁻¹ is big enough to be correctly detected by a high-level measurement.

Demagnetization effect. Here we list the used samples' dimensions and weights for various measurements. AC susceptibility: for B // a, $1.44 \times 1.15 \times 4.80 \text{ mm}^3$, 33.2 mg; for B // c, $1.30 \times 1.30 \times 5.20 \text{ mm}^3$, 36.7 mg. For both cases, the field is along the longest dimension. Specific heat: for B // a, $1.96 \times 0.45 \times 0.38 \text{ mm}^3$, 1.40 mg; for B // c, $1.87 \times 1.16 \times 0.18 \text{ mm}^3$, 1.63 mg. For both cases, the field is along the shortest dimension. Thermal conductivity: $3.0 \times 0.63 \times 0.14 \text{ mm}^3$, 1.11 mg. For B // a, the field is along the longest dimension, for B // c, the field is along the shortest dimension. The estimated upper limit of the modification of B by the demagnetization effects for AC susceptibility is <1% for both directions, for s precific heat is <4% for B // a, and <8% for B // c, such kind of small modification was neglected.

Data availability

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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Author contributions

N.L., W.J.C., and X.F.S. performed thermal conductivity measurements and analyzed the data with help from X.Z. and H.D.Z. X.Y.Y. performed the specific heat measurements. Q.H., Q.C., E.S.C., and H.D.Z. made the samples and performed the low-temperature AC susceptibility measurements. X.F.S. and H.D.Z. wrote the paper with input from all other co-authors.

Competing interests

The authors declare no competing interests.

Additional information

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