

1 Predicting Discharge and Erosion for the Abay (Blue Nile) with a Simple Model

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## ABSTRACT

Models accurately representing the underlying hydrological processes and sediment dynamics in the Nile Basin are necessary for optimum use of water resources. Previous research in the Abay (Blue Nile) has indicated that direct runoff is generated either from saturated areas at the lower portions of the hill slopes or from areas of exposed bedrock. Thus, models that are based on infiltration excess processes are not appropriate. Furthermore, many of these same models are developed for temperate climates and might not be suitable for monsoonal climates with distinct dry periods in the Nile basin. The objective of this study is to develop a simple hydrology and erosion models using saturation excess runoff principles and interflow processes appropriate for a monsoonal climate and a mountainous landscape. We developed a hydrology model using a water balance approach by dividing the landscape into variable saturated areas, exposed rock and hillslopes. Water balance models have been shown to simulate river flows well at five day or longer intervals when the main runoff mechanism is saturation excess. The hydrology model was developed and coupled with an erosion model using available precipitation and potential evaporation data and a minimum of calibration parameters. This model was applied to the Blue Nile. The model predicts direct runoff from saturated areas and impermeable areas (such as bedrock outcrops) and subsurface flow from the remainder of the hillslopes. The ratio of direct runoff to total flow is used to predict the sediment concentration by assuming that only the direct runoff is responsible for the sediment load in the stream. There is reasonable agreement between the model predictions and the ten-day observed discharge and sediment concentration at the gauging station on Blue Nile upstream of Rosaries Dam at the Ethiopia-Sudan border

**Key words:** Model, Erosion, Sedimentation, Rainfall-runoff, monsoonal climate

## INTRODUCTION

47

48 The Abay (Blue Nile) River in Ethiopia contributes significant flow and sediment to the Nile River. Thus,  
49 a better understanding of the hydrological processes, erosive losses, and sedimentation mechanisms in the  
50 various watersheds in the headwaters of the Nile River is of considerable importance. There is a need to  
51 improve and augment current resource management and development activities in areas with heavy  
52 degradation and low productivity, particularly in Ethiopia, where it is generally believed that only five  
53 percent of surface water is utilized (Weiß and Schaldach,2008). There is a particular need to develop  
54 further existing hydropower and irrigation potential of the Abay (Blue Nile) for socio-economic  
55 development in Ethiopia, while maintaining sustainable operation of water infrastructure systems  
56 downstream in Sudan and Egypt. Sustainable operation is dependent in large part on preventing silting up  
57 of reservoirs. This paper focuses on characterizing the rainfall-runoff-sediment relationships for the  
58 Ethiopian portion of the Blue Nile River. The majority of the sedimentation of rivers in the basin occurs  
59 during the early period of the rainy season and peaks of sediment are consistently measured before peaks  
60 of discharge for a given rainy season. Typical erosion models based on stream power would predict the  
61 greatest concentration to occur when the velocity and discharges are at their maximum (e.g., SWAT,  
62 AnnAGNPS, GWLF). Thus, innovative models are called for to predict erosion and sedimentation that  
63 are consistent with the hydrology of the region. Once developed, these models can be used for managing  
64 and or mitigating the sedimentation of newly constructed reservoirs.

65 A review by Awulachew et al. (2009) shows that the number of models simulating the discharge from  
66 watersheds in the Blue Nile and other river basins in Ethiopia and Africa has increased exponentially in  
67 recent years. Most of these models were originally developed for applications in temperate regions. They  
68 range from relatively simple engineering approaches such as the Rational Method (Desta 2003), to more  
69 complex models such as SWAT (Setegn et al. 2008) the Precipitation Runoff Modeling System (PRMS)  
70 (Legesse et al. 2003), Water Erosion Prediction Project (WEPP) (Zeleeke 2000), the Agricultural Non-  
71 Point Source model (AGNPS) (Haregeweyn and Yohannes 2003; Mohammed et al. 2004), and water

72 balance approaches (Ayenew and Gebreegziabher 2006; Kim and Kaluarachchi 2008). Implementation of  
73 these models yielded mixed results. For example, AGNPS was tested in the highlands of Ethiopia on the  
74 Augucho Catchment but could not reproduce observed runoff patterns. PRMS was similarly tested by  
75 Legesse et al. (2003) for South Central Ethiopia, and needed extensive calibration to predict the monthly  
76 runoff. It should not have been surprising that the above mentioned models are not performing well  
77 because they are based on the SCS curve number approach, of which the parameter values are obtained  
78 statistically from plot data in the USA with a temperate climate. The watershed behavior in a temperate  
79 climate than in a monsoonal climate where during the dry period the soil dries out completely, something  
80 that does not happen in the USA. Statistical methods are only valid for conditions that they are tested for.

81 Many simple water balance type approaches have been attempted for the Nile Basin. Both Mishra et al  
82 (2006) and Conway (1997) developed useful results with grid-based water balance models for the Blue  
83 Nile Basin using monthly discharge data from the El Deim Station in Sudan, located close to the  
84 Ethiopian border. They were studying the spatial variability of flow parameters and the sensitivity of  
85 runoff to changes in climate. Using a water balance model Kebede et al. (2006) concentrated on Lake  
86 Tana and developed a water balance utilizing relatively long durations (>30 years) of data for  
87 precipitation, evaporation, inflows of major tributaries and outflows to the Blue Nile. The simple water  
88 balance models often perform better especially over monthly time steps than their more complicated  
89 counterparts that have many more calibration parameters, but are not without problems either because  
90 different parameter sets are required for different basin sizes in the Blue Nile Basin as shown by Kim and  
91 Kaluarachchi (2008). One of the weaknesses of Kebebe et al. (2006) was that they did not differentiate  
92 between the hills and valleys in their simplified model.

93 To model the hydrology realistically the conceptual framework for the model should be correct.  
94 According to Liu et al. (2008), saturation excess runoff from saturated areas dominates the runoff process  
95 in several watersheds in the Ethiopian highlands. Subsequent field visits showed that runoff was produced  
96 from exposed hardpan and bedrock as well. Runoff from these almost impermeable areas can be modeled

97 with either saturation excess models with a very small amount of retention before runoff occurs or  
98 infiltration excess models with a minimal infiltration capacity. Water balance models are consistent with  
99 the above-mentioned type of runoff processes, since the runoff can be related to the available watershed  
100 storage capacity and the amount of precipitation but not generally to the precipitation intensity. Moreover,  
101 [as described above](#) models developed and intended for use in temperate regions where rainfall is  
102 generally well distributed throughout the year do not perform well in regions with monsoonal rainfall  
103 distributions (Liu et al., 2008). Therefore, water balance models, that track soil moisture levels and the  
104 degree of saturation, often perform better than more complicated models in Ethiopian type landscapes  
105 (Johnson and Curtis, 1994; Conway, 1997; Kebede et al., 2006; Liu et al., 2008).

106 Despite the copious literature on runoff and hydrology in the Nile Basin, there are very few erosion  
107 models published in the refereed literature for Ethiopia. Haregeweyn and Yohannes (2003) applied  
108 AGNPS model Augucho catchment and predicted the sediment loads for this small watershed with some  
109 success. The Universal Soil Loss Equation (USLE) was calibrated for Ethiopian conditions by Haile et al.  
110 (2006). Tamene and Vlek employed the USLE together with sediment deposition routine. Other  
111 approaches use expert judgment in the erosion predictions (Feoli et al. 2002; Sonneveld, 2003; Nyssen et  
112 al. 2007). Some publications use erosion assessments as part of an economic evaluation of soil and water  
113 conservation practices (Hengsdijk et al, 2005; Okumu et al 2004; Shiferaw and Holden 2000) however  
114 this practice is not without controversy, as the erosion estimates are, at best, a subject to dispute (Nyssen  
115 et al. 2006). Models predicting soil loss for large watersheds do not exist in the refereed literature (Hurni  
116 et al. 2005), thus there is a need to develop and test erosion models for larger scales. These erosion  
117 models necessarily need to be based on the proper hydrology. Only then, can the drastic land use changes  
118 that have occurred during the last 30 years in Ethiopia (as documented by Zeleke, 2000 and Zeleke and  
119 Hurni, 2001) be modeled and analyzed successfully.

120 Since saturation excess runoff is the dominate runoff production mechanism from the low laying areas  
121 and rock outcrops in the Ethiopian highlands and most models are based on infiltration excess runoff

122 mechanisms, these models do not always perform well. Thus, a more realistic model needs to be  
123 developed. Consequently, the objective of this study is to develop a physically based runoff and sediment  
124 loss model (using mainly existing data sources as input data with a minimum of calibration parameters)  
125 that is based on the saturation excess runoff process and is valid for monsoonal climates. We expect by  
126 using the correct conceptual hydrological model, scaling issues will be minimized.

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## MODEL DEVELOPMENT

129 In this section, we develop simple water balance type hydrology and erosion model. The hydrology model  
130 assumes that overland flow is generated from saturated areas in the relatively flatter areas in the landscape  
131 and areas where bedrock is exposed. The remainder of the landscape mainly is assumed to have  
132 sufficiently high conductivity so that rainfall infiltrates and is lost subsequently as evaporation, interflow  
133 or base flow. The erosion model predicts sediment concentrations based on the assumption that interflow and  
134 base flow are sediment free and that the sediment is carried by overland flow. The model, therefore,  
135 directly uses the input from the hydrology model for the calculations of the sediment concentrations.

136 A similar water balance type rainfall-runoff model was developed and tested by Collick et al. (2008) to  
137 predict the stream flow for four relatively small watersheds (< 500 ha) in the Blue Nile Basin. The authors  
138 reported reasonable predictions on a daily or weekly time step using nearly identical parameters for  
139 watersheds hundreds of kilometers apart. In this paper, some minor modifications were made with respect  
140 to interflow generation for predicting the discharge of the entire Blue Nile. For clarity, we will present the  
141 complete watershed water balance model and add a simple erosion model. Model parameters to predict  
142 the discharge were initially set to that of Collick et al. (2008). Model parameters for discharge were then  
143 refined and sediment parameters calibrated with the discharge and sediment concentration measured at  
144 the Ethiopia-Sudan border gauge station for 1993-1994 water year and then validated with data available  
145 for 2003 and 2004 rainy season.

146 **Predicting direct runoff, interflow and base flow**

147 The watershed is divided into two sections, the hillslopes, and the relatively flatter areas that become  
148 saturated during the rainfall season (Figure 1). The hillslopes are divided in two regions that have either  
149 restricted infiltration and storage or have high percolation rates (McHugh, 2006) and most of the water is  
150 transported subsurface as interflow (e.g. over a restrictive layer) or base flow (percolated from the soil  
151 profile to deeper soil and rock layers). The flatter areas that drain the surrounding hillslopes become  
152 runoff source areas when saturated (Figure 1). These areas can usually be recognized during the rainfall  
153 season as wet areas under permanent grass cover located near a stream. Evapotranspiration is extracted  
154 from a root zone. On the high infiltration hill slope areas excess water in the root zone is percolated  
155 through the subsoil. On the exposed hardpan or bedrock and in the saturated contributing areas, all excess  
156 water becomes surface runoff.

157 The amount of water stored in the topmost layer (root zone) of the soil,  $S$  (mm), for hillslopes and the  
158 runoff source areas were estimated separately with a water balance equation of the form:

159 
$$S = S_{t-\Delta t} + (P - AET - R - Perc)\Delta t \quad (1)$$

160 where  $P$  is precipitation, ( $\text{mm d}^{-1}$ );  $AET$  is the actual evapotranspiration, ( $\text{mm d}^{-1}$ ),  $S_{t-\Delta t}$ , previous time step  
161 storage, (mm),  $R$  saturation excess runoff ( $\text{mm d}^{-1}$ ),  $Perc$  is percolation to the subsoil ( $\text{mm d}^{-1}$ ) and  $\Delta t$  is  
162 the time step.

163 During wet periods when the rainfall exceeds potential evapotranspiration,  $PET$  (i.e.,  $P > PET$ ), the actual  
164 evaporation,  $AET$ , is equal to the potential evaporation,  $PET$ . Conversely, when evaporation exceeds  
165 rainfall (i.e.,  $P < PET$ ), the Thornthwaite and Mather (1955) procedure is used to calculate actual  
166 evapotranspiration,  $AET$  (Steenhuis and van der Molen, 1986). In this method  $AET$  decreases linearly with  
167 moisture content, e.g.:

168 
$$AET = PET \left( \frac{S_t}{S_{max}} \right) \quad (2)$$

169

170 Where  $S_t$  (mm) is the available water storage in the root zone per unit area and  $S_{max}$  (mm) is the maximum  
 171 available soil storage capacity and is defined as the difference between the amount of water stored in the  
 172 top soil layer at wilting point and the maximum moisture content, equal to either the field capacity for the  
 173 hill slope soils or saturation (e.g., soil porosity) in runoff contributing areas.  $S_{max}$  varies according to soil  
 174 characteristics (e.g., porosity, bulk density) and soil layer depth. Based Eq. 2 the surface soil layer  
 175 moisture storage can be written as:

$$S_t = S_{t-\Delta t} \left[ \exp \left( \frac{(P - PET)\Delta t}{S_{max}} \right) \right] \quad \text{when } P < PET \quad (3)$$

176  
177

178 In this simplified model, direct runoff occurs only from the runoff contributing area when the soil  
 179 moisture balance indicates that the soil is saturated. Recharge and interflow originate from the remaining  
 180 hill slopes. It is assumed that the surface runoff from these areas is minimal. This will underestimate the  
 181 runoff during major rainfall events but since our interest in weekly to monthly intervals was not  
 182 considered a major limitation.

183 In the overland flow contributing areas when rainfall exceeds evapotranspiration and fully saturates the  
 184 soil, any moisture above saturation becomes runoff, and the runoff,  $R$ , can be determined by adding the  
 185 change in soil moisture from the previous time step to the difference between precipitation and actual  
 186 evapotranspiration, e.g.,

187 
$$R = S_{t-\Delta t} + (P - AET)\Delta t \quad (4a)$$

188 
$$S_t = S_{max} \quad (4b)$$



189 For high infiltration areas on hillslopes the water flows either as interflow or baseflow to the stream.  
 190 Rainfall in excess of field capacity becomes recharge and is routed to two reservoirs that produce

191  
 192 baseflow or interflow. We assumed that the baseflow reservoir is filled first and when full, the interflow  
 193 reservoir starts filling. The baseflow reservoir acts as a linear reservoir and its outflow,  $BF$ , and storage,  
 194  $BS_t$ , are calculated when the storage is less than the maximum storage,  $BS_{max}$  as:

$$195 \quad BS_t = BS_{t-\Delta t} + (Perc - BF_{t-\Delta t})\Delta t \quad (5a)$$

$$196 \quad BF_t = \frac{BS_t [1 - \exp(-\alpha\Delta t)]}{\Delta t} \quad (5b)$$

197 where  $\alpha$  is the half life of the aquifer or the time it takes for half of the volume of the aquifer to flow out  
 198 without the aquifer being recharged.

199 When the maximum storage,  $BS_{max}$ , is reached then:

$$200 \quad BS_t = BS_{max} \quad (6a)$$

$$201 \quad BF_t = \frac{BS_{max} [1 - \exp(-\alpha\Delta t)]}{\Delta t} \quad (6b)$$

202 Interflow originates from the hillslopes and with the slope of the landscape as the major driving force of  
 203 the water. Under these circumstances, the flow decreases linearly (i.e., a zero order reservoir) after a  
 204 recharge event. The total interflow,  $IF_t$  at time  $t$  can be obtained by superimposing the fluxes for the  
 205 individual events (details are given in the Appendix):

$$206 \quad IF_t = \sum_{\tau=0,1,2}^{\tau^*} 2Perc_{t-\tau}^* \left( \frac{1}{\tau^*} - \frac{\tau}{\tau^{*2}} \right), \quad \tau \leq \tau^* \quad (7)$$

208 where  $\tau^*$  is the duration of the period after the rainstorm until the interflow ceases,  $IF_t$  is the interflow at a  
 209 time  $t$ ,  $Perc_{t-\tau}^*$  is the percolation on  $t-\tau$  days.

210 **Predicting sediment concentration**

211 The Blue Nile runs through a deep gorge partly over bedrock before it reaches the Sudan border. This  
212 means that the sediment concentration depends on the amount of suspended sediment delivered by  
213 contributing reaches to the main stem of the Nile. Assuming that subsurface flow does not cause erosion  
214 then all sediment is contributed by the direct surface runoff (Mul et al., 2008). Therefore, it is reasonable  
215 to assume that the sediment concentration in the Nile is determined by direct runoff from the contributing  
216 areas. Initially, at the beginning of the rainy season, the contributing areas expand and once the watershed  
217 is sufficiently saturated the contributing areas do not expand further and the hillslopes begin contributing  
218 interflow. Thus, once the watershed is saturated (i.e., the hillslopes are contributing water to the stream);  
219 the sediment concentration in the water is a function of the surface runoff and interflow components. In  
220 other words, the subsurface flow dilutes the concentration of sediment delivered by the direct runoff  
221 delivered to the stream. The sediment concentration in the river,  $C^*$ , occurs just before the hillslopes  
222 begin contributing interflow. The discharge is  $R^*$  at that time.

223 Based on the conceptual model above for the period that the hillslopes are contributing interflow the  
224 sediment concentration,  $C$ , in the river water is the ratio of the direct runoff and total runoff multiplied by  
225  $C^*$ , viz:

226 
$$C = C^* \frac{R}{R + IF + BS} \quad (8)$$

227

228 where  $R$ , runoff,  $IF$ , interflow, and  $BS$ , baseflow are predicted by the water balance model, above.

229 For the period when the subsurface flow is negligible at the onset of the rainy season, the soil erodibility  
230 is the greatest because the soil is dry and loose. At the same time from the beginning of the rainfall season  
231 the contributing area increases and initially the discharge is less for any given amount of rainfall than it

232 would be later in the season. Although we do not know the exact mechanisms, it is reasonable to assume  
233 that the concentration is equal to the ratio of predicted runoff to direct runoff,  $R^*$  viz:

234

$$C = C^* \frac{R}{R^*} \quad (9)$$

235

236 Thus, the concentration  $C^*$  and  $R^*$  are calibration parameters, and are set equal to the ten day averaged  
237 sediment concentration and the discharge during the period just before interflow starts as simulated by the  
238 model.

239 **APPLICATION: THE ABAY (BLUE NILE)**

240 The Blue Nile Basin at the border with Sudan covers an area of approximately 180,000 km<sup>2</sup>. The river  
241 and its tributaries drain a large proportion of the central, western and southwestern highlands of Ethiopia.  
242 The basin is characterized by a highly rugged topography and considerable variation of altitude ranging  
243 from about 500 m at Sudan border to over 4,250 m above mean sea level (msl) in the Ethiopian highlands.  
244 Together with the Dinder and Rahad that join the Blue Nile in Sudan, Ethiopia provides 62% of the flow  
245 reaching Aswan (World Bank 2006).

246 Rainfall varies significantly with altitude and is considerably greater in the Ethiopian highlands than on  
247 the Plains of Sudan. Rainfall ranges from less than 1,000 mm/yr near the border of Sudan to between  
248 1,400 and 1,800 mm over parts of the upper basin, in particular, some areas south of Lake Tana. Rainfall  
249 exceeds 2,000 mm in parts of the Didessa and Beles catchments.

250 Both the temporal and spatial distribution of rainfall is governed, , by the movement of air masses  
251 associated with the Inter-Tropical Convergence Zone (ITCZ). During the winter dry season (known in  
252 Ethiopia as Bega) the region is affected by a dry northeast continental air-mass. From March to May  
253 (Belg) the ITCZ brings rain particularly to the southern and southwestern parts of the Basin. In May, there  
254 is a short intermission before the main wet season (known locally as Kremt). Around June, the southwest

255 airstream extends over the entire Ethiopian highlands and produces the main rainy season. The summer  
256 months account for a large proportion of mean annual rainfall, roughly 70% occurs between June and  
257 September and this proportion generally increases with latitude, ranging from 60 to 80%

258 **Available discharge and sediment data:** There is relatively little sediment concentration data available  
259 for the Blue Nile. One data set of continuous sediment concentrations is given by Ahmed (2003) and  
260 consists of ten day averaged sediment concentrations at the gauge station upstream of Rosaries Dam north  
261 of the Ethiopia-Sudan border for the period June-October 1993. The 10-day discharge values at this  
262 station and the averaged precipitation over the entire Blue Nile basin in Ethiopia are also available for the  
263 period of May 1<sup>st</sup> 1993 to April 30<sup>th</sup> 1994. In addition, discharge and sediment concentration were  
264 obtained for July, August, September, and October for 2003 and 2004. A long record of rainfall in  
265 Ethiopia was available from 1995 to 2006 for 15 stations in the Nile basin. We use the 1993 data for  
266 calibration and the 2003 and 2004 data for validation.

267 **Calibration:** To use the water balance in 1993-1994 water year for calibration we need to start the  
268 simulations before the rainfall period begins (and the sediment data were available), thus, we choose to  
269 start in January 1993 (Figure 2a).

270 Parameters needed to simulate discharge include *PET*, which varies little between years and it was set at 5  
271 mm d<sup>-1</sup> during the dry season and 3.3 mm d<sup>-1</sup> during the rainy season. The maximum storages,  $S_{max}$ , for  
272 the contributing area and hillslopes were based initially on the values from Collick et al. (2008) for three  
273 SRCP watersheds. Note that for the relatively flat contributing areas and bedrock areas this maximum  
274 storage term represents the amount of water that is required to fill up a dry soils before it is saturated and  
275 overland flow will occur. For the hillslopes,  $S_{max}$  is the moisture required to bring a dry soil up to field  
276 capacity after which any extra water will percolate downward. Although the Collick et al. (2008) values  
277 gave a reasonable fit, we decided to vary them slightly to improve the agreement between observed and  
278 predicted values as the correct distribution between subsurface flow and overland flow directly

279 determines the predicted sediment concentrations. Collick et al. (2008) assumed that 40% of the  
280 landscape had a  $S_{max}$  value of 100 mm. This represents the contributing area in their model. For the Blue  
281 Nile basin, we found a slightly better fit by reducing the contributing area to 30%. We divided the  
282 contributing area in two parts (Table 1a): 20% of the area (consisting of the exposed hardpan or bed rock  
283 areas) needed little rain to generate direct runoff (i.e.,  $S_{max} = 10\text{mm}$ ) and 10% (the saturated bottom lands)  
284 needed 250 mm of effective precipitation after the dry season before generating runoff (i.e.,  $S_{max} =$   
285 250mm). Note that the weighted average  $S_{max}$  for the runoff contributing area in the Blue Nile Basin in  
286 Ethiopia compares well with the  $S_{max}$  value of 100 mm storage for two of the three SRCP watersheds  
287 (Collick et al., 2008).

288 Scale is important when simulating the hydrological dynamics of the hillslopes in the Blue Nile as  
289 compared to the SRCP watersheds located in the upper reaches of the basin (Collick et al., 2008; Hurni et  
290 al., 2004). We used a  $S_{max}$  value of 500 mm for the hillslopes where the water infiltrates (Table 1a). In two  
291 of three SRCP watersheds, approximately 20% of the moisture was lost to deep percolation. To simulate  
292 deep percolation, Collick et al. (2008) assumed that the  $S_{max}$  was essentially infinite (4000 mm). If we  
293 ignore this reservoir, because the deep percolation over the whole Blue Nile in Ethiopia is negligible, we  
294 find that the  $S_{max} = 500$  mm for the high infiltration area of the Nile basin (Table 1a) compares well with  
295 the values used in Collick et al. (2008).

296 Scale impacts the interflow and baseflow predictions in the conveyance zone more than the storage values  
297 in the uppermost soil layer. A more complicated approach was needed to represent adequately the  
298 complex landscape by using both a linear ground water reservoir and a zero order hillslope reservoir.  
299 Fitted parameters are given in Table 1b. The  $\tau^*$  value of 140 days indicates that the hillslopes contribute  
300 interflow up to 140 days after the storm occurs. To model sediment concentration (Eqs. 8 and 9), the only  
301 calibration parameters is the observed concentration,  $C^*$ , before interflow occurs and the flux,  $R^*$ , at that  
302 time. We have set this concentration at 5000 mg/l (Table 1b). The discharge at that time is equivalent to  
303 1.4 mm/day over the whole basin. The remaining parameter values are all obtained from the water

304 balance model presented in Figures 2a and 3. Observed and predicted sediment concentrations are shown  
305 in Figure 4a. The simulated discharge and sediment concentration fit the observed values well as  
306 indicated by the regression coefficient  $R^2$  and Nash-Sutcliffe model efficiency coefficient close to one in  
307 Table 2.

308

### 309 **Simulation results**

310 The calibrated parameters in Tables 1a and 1b were used to predict the discharge and sediment  
311 concentrations of the Blue Nile for the years 2003 and 2004 at the station upstream of Rosaries dam. The  
312 predicted and observed stream discharges are depicted in Figures 2b and 2c. The observed sediment  
313 concentrations are compared with the predicted concentrations in Figures 4b and 4c. The fit between  
314 observed and predicted discharge and sediment concentrations are shown in Table 2. Despite both the  
315 different rainfall pattern (total annual precipitation in 1993, 1425 mm; in 2003, 1215 mm; in 2004, 1275  
316 mm) and the simplicity of the model, the discharge and sediment concentrations are reasonably well  
317 simulated. In all cases the *F-test* was significant indicating that the observed and predicted values were  
318 not significantly different (Table 2). In 2003 the  $R^2$  of the discharge regression was somewhat low  
319 although the visual inspection of the regression in Figure 2a shows the fit to be acceptable. The low  $R^2$   
320 was caused by missing the trend in discharge predictions at the end of June and beginning of July. The  
321 range in data for 2003 was smaller than for 1993 since we had only the data for the rainy season and not  
322 for the dry season. Although the goodness of fit in Table 2 was reasonable for 2004, the discharge was  
323 under predicted in August and the first half of September. One of the problems in accurate modeling of  
324 the discharge is that the precipitation measurements do not exist in the large area of the northwestern Blue  
325 Nile. Figures 1 and 3 show that the flow at the end of the dry season is extremely small indicating that  
326 there is little carryover of water from one year to the next.

327 It is surprising that the sediment concentrations are predicted with reasonable accuracy (Table 2) and  
328 particularly that the sediment concentration from the calibration period (1993) performs well despite the  
329 significantly higher sediment concentration observed in 2003 and 2004.. It is reassuring that the model  
330 captures the high sediment concentration on the rising limb and the lower concentration on the falling  
331 limb, verifying that the majority of the flow in the river is base flow that is sediment free (Mul et al.,  
332 2008). It is interesting that this simple sediment model can predict the sediment concentrations well using  
333 fluxes predicted by the water balance model. We cannot predict the sediment concentration at the end of  
334 July when the concentration suddenly drops.

## 335 **DISCUSSION AND CONCLUSIONS**

336 The hydrological model presented here is based on generating direct runoff on saturated areas, and is  
337 reasonably robust. In the beginning of the rainy season almost all flow in the river is direct runoff  
338 generated from the 20% of the area that has the smallest storage and likely originates from the bare rock  
339 or low storage areas where there is little infiltration or storage of rainfall. As the rainy season progresses  
340 (cumulative rainfall increases), the rest of the landscape wets up and direct runoff is generated from the  
341 remaining 10% of the contributing area followed by base and interflow from the hill slopes around early  
342 July (Figure 3). Note that this corresponds to the time that the sediment concentration in the river is  
343 decreasing from the maximum (Figure 4).

344 The annual volumes of discharge can be found as areas under the discharge curve in Figure 2. The  
345 volumes of predicted and observed discharge in 1993-1994 water year (Figure 2a) and 2003 (Figure 2b)  
346 are equal. Since there is no carryover storage of flows from year to year the predicted discharge is equal  
347 to the annual precipitation minus the annual evapotranspiration. Thus, the water balance of the Blue Nile  
348 balances within a hydrologic year. In 2004 (Figure 2c) although we obtained only a partial record (just  
349 like in 2003), it seems that we could not close the water balance as well but that might be partially caused  
350 by the uncertainty in precipitation.

351 Figure 2 shows that the discharge is only 20-30% of the precipitation in June, July, and August, during  
352 the period when the majority of rainfall occurs. Our water balance approach is able to explain this  
353 observed runoff coefficient (i.e., discharge/precipitation) by distributing the effective rainfall (rainfall  
354 minus evapotranspiration) over the contributing and saturated areas that generate direct runoff. For our  
355 simulations the area that contributes runoff is 30% of the total basin area at the time that the soil is  
356 saturated. Thirty percent of the area does not contribute 30% of the rainfall as streamflow since runoff has  
357 to be adjusted for the evaporation that occurs during the period. A portion of the discharge in August (as  
358 shown in Figure 3) when the runoff coefficient is the greatest, originates from interflow and base flow  
359 generated from the 70 % of the basin area where the rainfall infiltrates.

360 It is also interesting to note how minimal the scale effects are for the basin. Using similar parameters to  
361 Collick et al. (2008) (predicting discharge from small watersheds <500 ha) we were able to model the  
362 flow from the Blue Nile basin in Ethiopia with equal efficiency. The Basin as a whole and the small  
363 watersheds have nearly the same portions of contributing areas and hillslope areas with similar amounts  
364 of water needed before overland flow or interflow starts after the onset of the rains. However, the  
365 interflow component did show some scale effects. The interflow period last longer for the Blue Nile  
366 watershed than for small watersheds. This should have been expected since in the small catchments up to  
367 20% of interflow was not recorded at the gage, and likely ended up as a regional flow , which would be  
368 measured at larger gauges. We are unable to study at scale effects of the sediment since the sediment  
369 concentrations were not analyzed in the small watersheds.

370 Despite the reasonable fit of the predicted and observed concentrations, processes governing the erosion  
371 and sedimentation dynamics are not fully understood in the Blue Nile, thus the sediment predictions in  
372 this paper should be considered tentative until more testing is done. It is interesting to note the decrease in  
373 observed stream sediment concentrations before the peak discharge occurs, and that the model captures  
374 the phenomenon is important, but other, more complicated process may play a role. For instance, it could  
375 be the result of relating the sediment concentration to the time when the watershed becomes covered by



376 vegetation or when the watershed is fully wetted up and erodibility of all soils are decreasing. Based on  
377 watershed outflow concentrations, we cannot discriminate between these mechanisms since both signals  
378 appear at the same time because when interflow occurs the watershed is wet and vegetation begins to  
379 develop. However, the interflow explanation seems to be reasonable since during the rainy season high  
380 sediment concentrations are observed in the basin and relatively sediment free water is observed after the  
381 surface runoff has ended. Currently there are very few sediment models available and although the model  
382 described here can capture the trends, more research is needed to elucidate erosion processes, particularly  
383 gully erosion within the watershed (Daba et al., 2003; Billi and Dramis, 2003).

384

#### 385 Acknowledgement

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387 carried under the auspices of the International Water Management Institute (IWMI) managed project,  
388 PN19 'Upstream-Downstream in the Blue Nile

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390

391 **APPENDIX A**

392 **DERIVATION OF INTERFLOW DISCHARGE FOR ZERO ORDER RESERVOIRS**

393 The flux from a reservoir in general can be expressed as a function of the flux from the aquifer (Brutsaert  
394 and Nieber, 1977)

395 
$$\frac{dQ}{dt} = -aQ^b \quad (A1)$$

396 where  $a$  is a constant. Hillslopes can be modeled as zero order reservoir  $b=0$  (Steenhuis et al., 1999;  
397 Stagnitti et al., 2004) and regular groundwater outflow as a first order reservoir  $b=1$

398 The flux equation is derived for a zero order reservoir as a function of the reservoir storage  $S$  the flux  
399 from the reservoir decreases linearly for a single storm, i.e.:

400 
$$\frac{dQ_t}{dt} = -a_0 \quad (A2)$$

401 Without loss of generality we can replace the time  $t$  with  $\tau$  in Eq. A1 defined as the time after the storm  
402 has occurred. In addition, we have designated the flow  $Q_t$  is from the particular storm occurring at time  $t$ .  
403 Integrating with respect to  $t$  subject to the boundary condition that at time  $\tau^*$  after the rain event the flux  
404 is zero (i.e.,  $Q=0$  at  $\tau=\tau^*$ ). Integrating Eq. A2 with the boundary condition specified and  $\tau$  as the time  
405 variable:

406 
$$Q_t = a_0(\tau^* - \tau) \quad (A3)$$

407 Integrating again from  $\tau=0$  to  $\tau = \tau^*$  we find the storage in the  
408 aquifer: 
$$\int_0^{\tau^*} Q_t d\tau = SI_t = \frac{1}{2} a_0 \tau^{*2} \quad (A4)$$

409

410 Where  $Perc^*_t$  is the amount of water added to the reservoir at time  $t$ . In order to conserve mass it is  
411 obvious from Eq. A3 that:

412

$$a_o = \frac{2Perc_t^*}{\tau^{*2}} \quad (A5)$$

413

414 Combining Eqs. A5 and A3 results in the zero order flow equation for the discharge of the aquifer for a  
415 storm occurring at time  $t$ :

416

$$Q_t = 2Perc_t^* \left( \frac{1}{\tau^*} - \frac{\tau}{\tau^{*2}} \right) \quad (A6)$$

417

418 The total flux is equal for a daily time step

419

$$BI_t = \sum_{\tau=0}^{\tau^*} 2Perc_{t-\tau}^* \left( \frac{1}{\tau^*} - \frac{\tau}{\tau^{*2}} \right) \quad (A7)$$

420

421

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## List of Tables and Figures

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Figure 3: Subsurface and direct runoff components of the hydrograph shown in Figure 2a.

Figure 4: Predicted and observed sediment concentration in the Abay (Blue Nile) at the Ethiopian Sudan border upstream of the Rosaries Dam. a) 1993 calibrated; b) 2003 validation; c) 2004 validation.

Table 1: Input parameters for the model. 1a: Model input values for surface flow components: The watershed is divided up in areas with different characteristics: exposed bedrock and saturated areas that contribute surface runoff or hillsides that produce recharge when the soil is above field capacity. Maximum storage of water is the amount of water needed from wilting point to become either saturated or to reach field capacity. 1b: Model input values for the baseflow and interflow parameters. SBmax is the maximum storage of the linear base flow reservoir;  $\alpha$  is the time it takes in days to reduce the volume of the baseflow reservoir by a factor 2 under no recharge conditions,  $t^*$  is the duration of the period after a single rainstorm until interflow ceases,  $C^*$  and  $R^*$  are the calibrated sediment concentration and discharge rate respectively just before interflow becomes significant.

539 Table 2: Statistical analysis of simulated and observed 10 day averaged discharge and sediment  
540 concentrations in the Blue Nile at the Ethiopia-Sudan border. Both the linear regression R-square  
541 and the Nash-Sutcliffe efficiency are calculated. The slope and the intercept of the linear  
542 regression are shown.

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546 Table 1a: Model input values for surface flow components: The watershed is divided up in areas  
 547 with different characteristics: exposed bedrock and saturated areas that contribute surface runoff  
 548 or hillsides that produce recharge when the soil is above field capacity. Maximum storage of  
 549 water is the amount of water needed from wilting point to become either saturated or to reach  
 550 field capacity.  
 551

<i>Description of area</i>	<i>Maximum of Water storage, mm</i>	<i>Portion occupying in watershed</i>
contributing area rock outcrops	10	0.2
contributing area saturated bottoms	250	0.1
recharge area Hillside	500	0.7

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556 Table 1b: Model input values for the baseflow and interflow parameters.  $SB_{max}$  is the maximum  
 557 storage of the linear base flow reservoir;  $\alpha$  is the time it takes in days to reduce the volume of the  
 558 baseflow reservoir by a factor 2 under no recharge conditions,  $t^*$  is the duration of the period  
 559 after a single rainstorm until interflow ceases,  $C^*$  and  $R^*$  are the calibrated sediment  
 560 concentration and discharge rate respectively just before interflow becomes significant.  
 561

<i>Parameter description</i>	<i>Value</i>	<i>Units</i>
Maximum storage capacity of linear reservoir, $SB_{max}$	20	mm
Half life, $\alpha$	35	days
Interflow duration after rainfall. $t^*$	140	days
Calibrated sediment concentration, $C^*$	500	mg/l
Calibrated amount of runoff $R^*$	1.4	mm/day

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584 Table 2: Statistical analysis of simulated and observed 10 day averaged discharge and sediment  
 585 concentrations in the Blue Nile at the Ethiopian Sudanese border. Both the linear regression R-  
 586 square and the Nash-Sutcliffe efficiency are calculated. The slope and the intercept of the linear  
 587 regression are shown.

588

	<b>1993-1994</b>		<b>2003</b>		<b>2004</b>	
	<b>Flow</b>	<b>Sediment</b>	<b>Flow</b>	<b>Sediment</b>	<b>Flow</b>	<b>Sediment</b>
<b>Slope</b>	0.99	0.84	0.87	0.88	1.19	0.95
<b>Intercept</b>	0.58	-19.72	1.20	-183.62	0.67	776.04
<b>p-value (F-test)*</b>	<0.001	<0.001	0.017	0.001	<0.001	0.002
<b>R<sup>2†</sup></b>	0.98	0.81	0.45	0.74	0.80	0.74
<b>NSE‡</b>	0.98	0.75	0.42	0.60	0.73	0.69

589 \*Test of significance for regression of observed and predicted response.

590 †Simple R-square of regression

591 ‡Nash –Sutcliffe efficiency defined as:  $1 - \left( \frac{\sum(\text{Observed} - \text{Predicted})^2}{\sum(\text{Observed} - \text{Observed Mean})^2} \right)$

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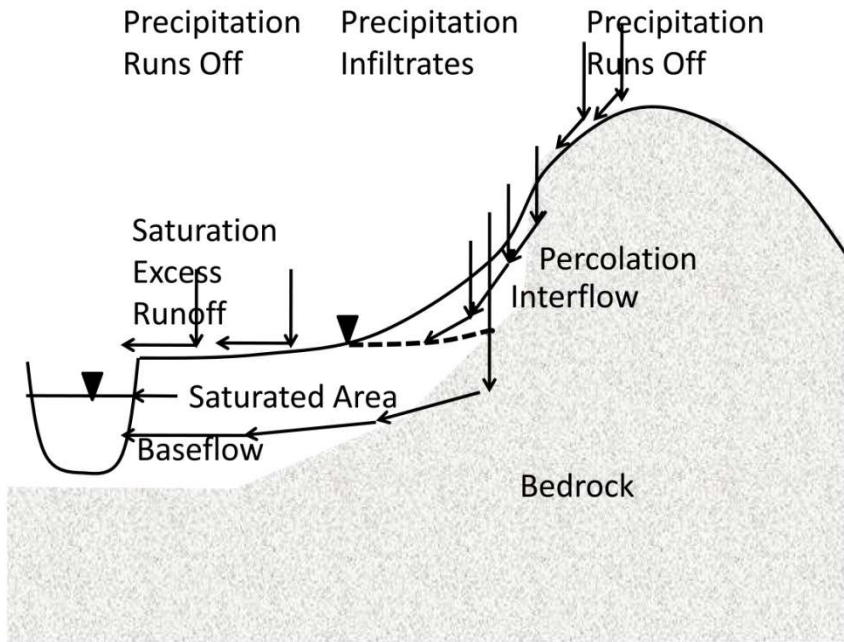


Figure 1: Simplified Hillslope

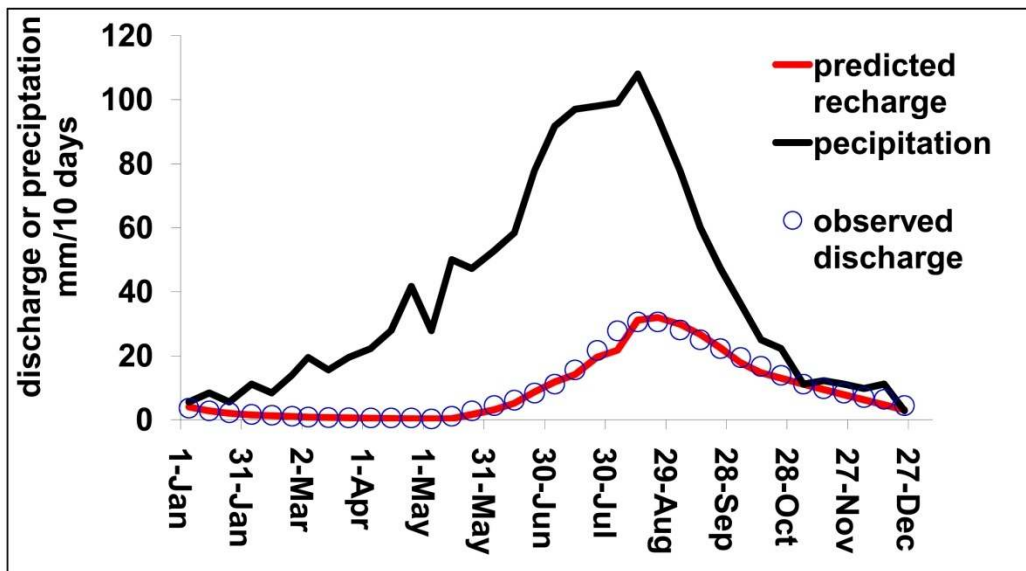


Figure 2a

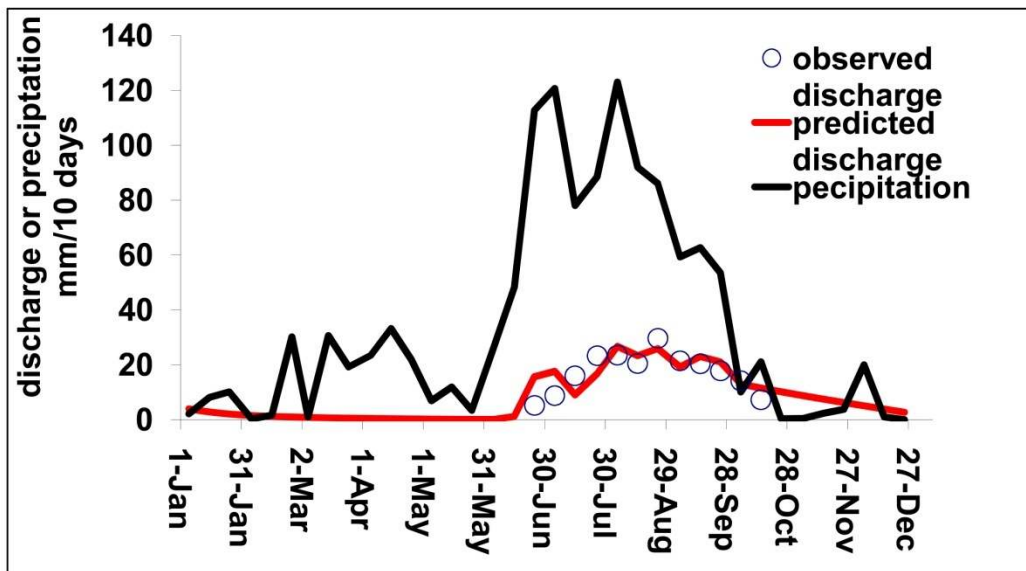


Figure 2b

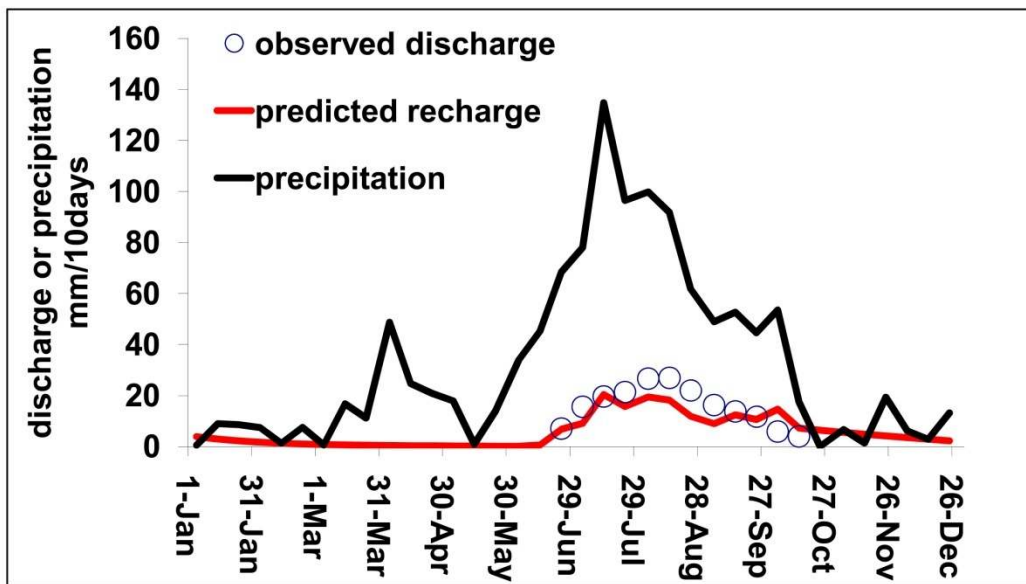


Figure 2c



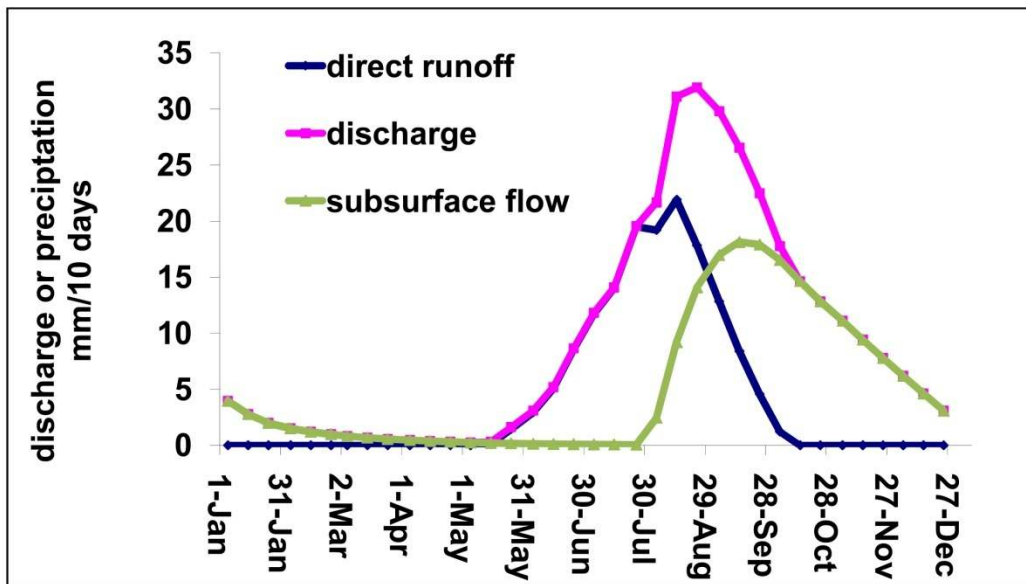


Figure 3

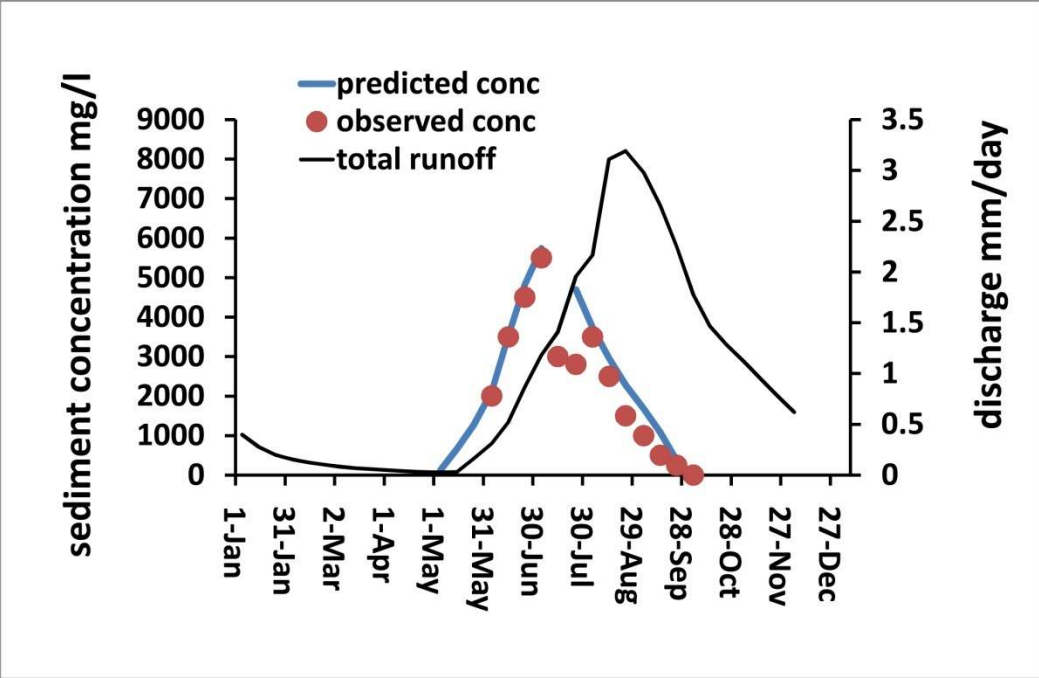


Figure 4a

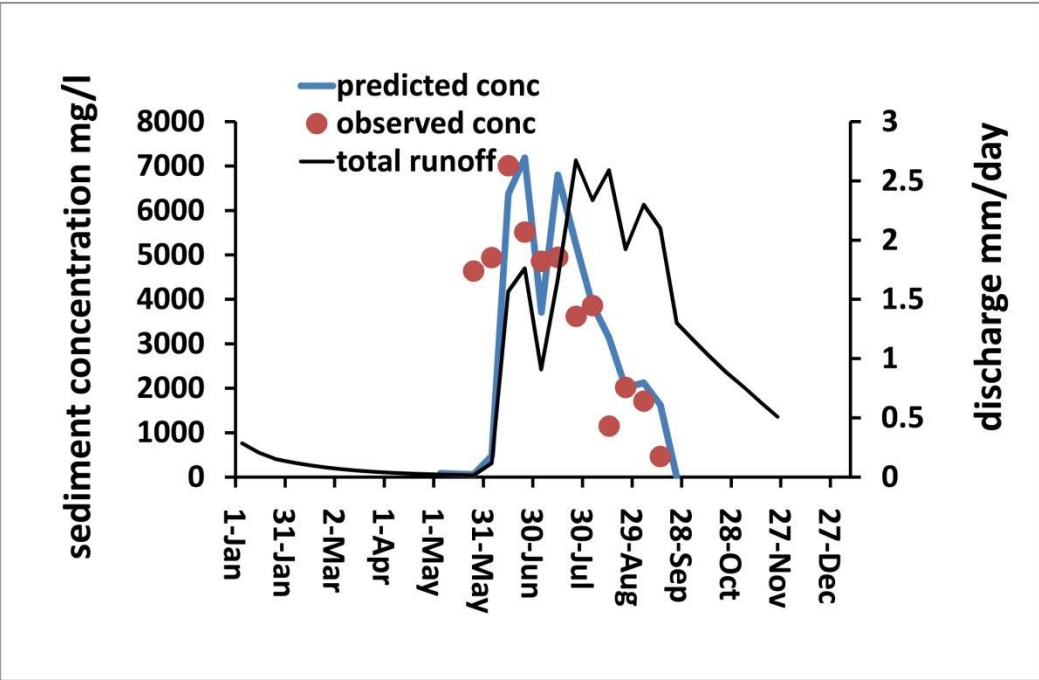


Figure 4b

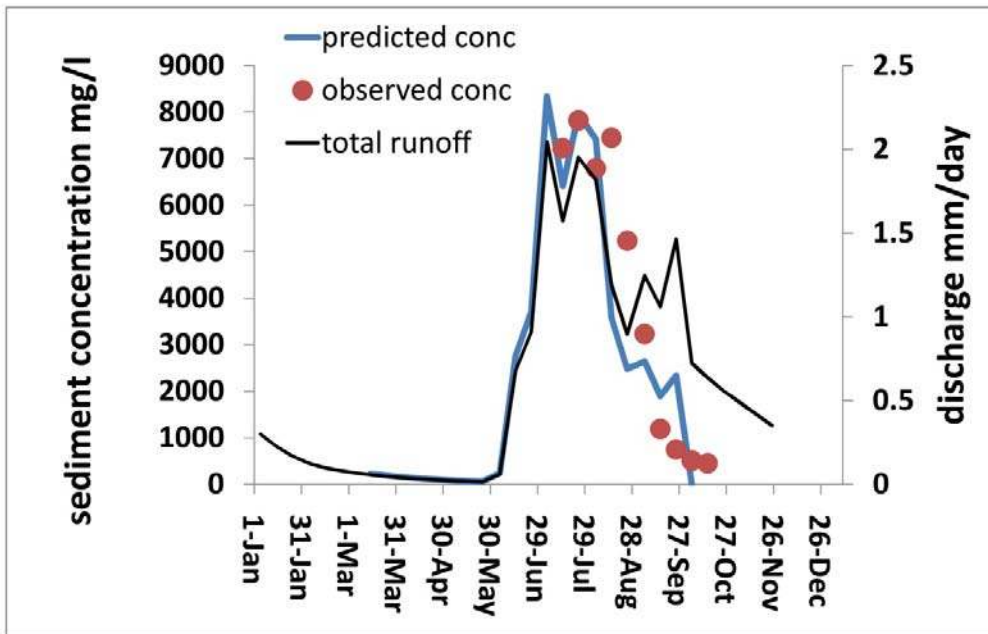


Figure 4c