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38 **Predicting the peak resistance of a spudcan penetrating**
39 **sand overlying clay**
40

41 **Abstract**

42 Accurately predicting the peak penetration resistance, q_{peak} , during spudcan installation into sand
43 overlying clay is crucial to an offshore mobile jack-up industry still suffering regular punch-through
44 failures. This paper describes a series of spudcan penetration tests performed on medium loose sand
45 overlying clay and compares the response to existing centrifuge data from tests performed on dense
46 sand overlying clay. Together this data demonstrates that punch-through is a potential problem for
47 both dense and loose sand overlying clay soil stratigraphies. Using this experimental database the
48 failure stress dependent model of Lee et al. (2009) has been modified to account for the embedment
49 depth and the depth of occurrence of q_{peak} is shown to be a function of the sand thickness, H_s . The
50 model has then been recalibrated, taking these findings into account, for a larger range of material
51 properties and ratios of sand thickness to spudcan diameter (H_s/D). Finally, the performance of the
52 modified and recalibrated model is verified by comparing its predictions to those calculated using the
53 current recommended practice given in the ISO (2012) 'guidelines'. The comparisons show that the
54 modified model yields more accurate predictions of q_{peak} over the range of H_s/D of practical interest,
55 which when used in practice will potentially mitigate the risk of unexpected punch-through on sand
56 overlying clay stratigraphies.

57 **CE Database subject headings:**

58 Centrifuge models; load bearing capacity; sand; clays; footings; offshore structures

59 **Keywords:**

60 Centrifuge modelling; spudcan; sand; clay; punch-through; offshore engineering

61 **Introduction**

62 Modern jack-up structures typically consist of a triangular platform with three legs that are jacked
63 through the deck into the seabed. A jack-up is then installed by filling water ballast tanks on the
64 platform, which pushes the legs and large inverted conical spudcan footings attached at the ends into
65 the seabed soil. This preloading procedure continues until the spudcans have been effectively proof
66 tested, at which time the ballast water is dumped and the platform is jacked up above the water
67 surface for operation. When jack-up platforms are installed on seabed sediments consisting of a sand
68 layer overlying soft clay, there is the potential for punch-through failure, where the spudcan footing
69 pushes the stronger layer into the softer layer. This can cause vertical displacement of one or more
70 legs of the platform in a rapid and uncontrolled manner, which as a consequence can lead to buckling
71 of the legs or in extreme cases even toppling of the platform. The cost of these incidents is estimated
72 at between US\$10-30 million and they are continuing to be problematic (Hossain and Safinus, 2012).
73 Therefore, accurately predicting the peak penetration resistance and thus the potential for punch-
74 through failure is an important issue for jack-up platform operators both for operational safety and
75 field development economics.

76 Craig and Chua (1990) performed a series of centrifuge tests investigating the potential for punch-
77 through of foundations on sand overlying clay. They observed that a peak penetration resistance was
78 attained relatively rapidly, which was followed by reducing penetration resistance that caused rapid
79 leg penetration. Cutting of the samples along the central cross section after spudcan extraction
80 exposed a slightly downwards-tapering plug of sand with depth approximately equal to the sand layer
81 height. In contrast, an inverted truncated cone sand plug was visualized by Teh et al. (2008) using the
82 particle image velocimetry technique (White et al. 2003) in a centrifuge and the failure mechanism of
83 spudcan foundations on sand overlying clay was discussed. Teh et al. (2010) proposed that the bearing
84 resistance–depth profile of a punch-through event can be determined by three characteristic bearing
85 resistances and corresponding depths. Based on an extensive series of flat footing and spudcan
86 penetration tests on dense sand overlying clay and the observations of Teh et al. (2008), Lee et al.

87 (2009) proposed a failure stress dependent model to calculate the peak penetration resistance, q_{peak} .
88 However, the model was calibrated solely using experimental data for dense sand overlying clay and
89 for limited geometries of spudcan foundations. Its performance, therefore, requires further validation.
90 Of greatest concern is whether re-calibration is needed for looser sands overlying clay soil conditions.

91 The aims of this paper are to:

- 92 1. Model experimentally the penetration resistance of a spudcan of generalized geometry
93 penetrating medium loose sand overlying clay in the centrifuge, and assess the potential for
94 punch-through failure.
- 95 2. Extend the stress dependent model for predicting peak penetration resistance of Lee (2009) to
96 (i) both loose and dense sands and (ii) to account for the embedment depth of the peak
97 penetration resistance.
- 98 3. Recalibrate the modified model based on the experimental results.
- 99 4. Investigate the ability of the modified model to predict peak penetration resistance during
100 spudcan foundation installation on sands overlying clay.
- 101 5. Assess the performance of the modified model by comparison with current recommended
102 practices using centrifuge data reported in the literature.

103 **Experimental Setup**

104 Physical modelling of spudcan penetration on medium loose sand overlying clay was conducted using
105 the drum centrifuge at the University of Western Australia (UWA), a detailed description of which
106 was reported by Stewart et al. (1998). Spudcan foundations in practice are typically circular with
107 diameters of 10 to 20 m. In this investigation a generalised geometry spudcan as illustrated in Fig. 1,
108 was used and referred to as the UWA spudcan. The spigot angle of 76° and main conical angle of 13°
109 were kept constant for different model spudcan diameters to ensure any geometric impacts remained
110 consistent between tests. Table 1 contains a summary of the prototype spudcan geometries tested in

111 this investigation. This UWA spudcan was identical to the model spudcan in dense sand overlying
112 clay by Lee (2009).

113 Commercially available super fine silica sand and kaolin clay were adopted in all the centrifuge tests
114 to form the sand and clay layers respectively. Both materials have been well characterized and used
115 extensively in the geotechnical centrifuges at UWA. The key properties of the sand and clay are
116 summarized in Cheong (2002) and Stewart (1992) respectively.

117 The kaolin clay was mixed into slurry with a water content of 120%. It was then placed in the drum
118 channel using the actuator at an acceleration of 20 g until the channel was full, before being normally
119 consolidated at an acceleration of 300 g. After consolidation, the normally consolidated clay was
120 scraped back leaving a non-zero shear strength at the sample surface and the desired target clay
121 thickness of 150 mm. A fabric membrane was then placed on top of the clay, and sand was pluviated
122 into the channel under an acceleration of 20 g using a specially-designed sand placement tool.
123 Medium loose sand was formed by pluviating the fine particles through a layer of water kept on top of
124 the sample. The underlying clay was then lightly over-consolidated at an acceleration of 300 g. The
125 sand and fabric membrane were then removed before the sand was laid again following the same
126 procedure but without the fabric membrane. The fabric membrane was used to facilitate removal of
127 the surcharging sand layer, which was disturbed during normal consolidation of the underlying clay
128 layer, allowing relaying of a new undisturbed sand layer for testing. A target sand thickness was
129 achieved by scraping the sand surface down to the desired height by means of a scraping plate
130 attached to the actuator. All tests were conducted at 200 g and the over-consolidation ratio, *OCR*, for
131 underlying clay was at least 1.5.

132 **Testing Procedure**

133 A total of 15 spudcan penetration tests were performed on medium loose sand overlying clay with
134 sand thickness H_s of 16, 25 and 30 mm. Five tests were conducted at each height, as detailed in Table
135 1. The ratio of H_s/D was then between 0.16 and 1.0, which covers the range of practical interest as no

136 punch-through failures have been reported for $H_s/D > 1$. The first five tests were performed with a
137 sand thickness of 30 mm. Following these tests the sand was further scraped back, to 25 mm and then
138 to 16 mm (the bottom clay was re-consolidated under 200 g overnight after each scraping process),
139 allowing tests to be performed at three sand thicknesses. At each stage the sand was removed over the
140 entire drum channel, but the tests were conducted in different and untouched sites.

141 The relative density, I_D , of the sand layer was determined by extracting four samples from equidistant
142 radial locations in the channel using 60 mm diameter sampling tubes after surcharging and before the
143 tests (at 1 g). The samples were collected from the bed carefully ensuring minimal disturbance, and
144 yielded an average relative density of 43%, with a standard deviation of 7%, indicating relatively
145 uniform medium loose sand. The submerged unit weight of the sand, γ'_s was measured to be 10.0
146 kN/m³. The submerged unit weight of the clay, γ'_c , was measured directly on 20 mm diameter samples
147 extracted by a tube sampler, which was 7.1 kN/m³ on average.

148 The spudcans were loaded using displacement control at a constant penetration rate. The penetration
149 rates were determined such that drained behavior in sand and undrained behavior in clay was attained.
150 The following normalized penetration rate, V , was widely adopted to describe the drainage condition
151 (Finnie and Randolph, 1994)

$$152 \quad V = \frac{vD}{c_v} \quad (1)$$

153 where v is the penetration velocity of foundation, D is the foundation diameter and c_v is the
154 consolidation coefficient. For undrained conditions in clay there is a transition range of $30 < V < 300$
155 over which partial drainage are minimized (Finnie and Randolph, 1994). The dimensionless velocity
156 V was maintained as 120 in the clay ($c_v = 2$ m²/year, Stewart (1992)) for all tests by varying the
157 penetration velocity accordingly. Thus, the penetration velocities, v , for $D = 30$ mm and 100 mm were
158 0.254 mm/s and 0.076 mm/s respectively. The silica sand has been estimated to have a c_v of at least
159 60,000 m²/year (Lee, 2009) and therefore, V was less than 0.01 in the sand layer for the penetration
160 rates and spudcan sizes used. This ensured fully drained behaviour in the sand layer.

161 To obtain the undrained shear strength profile of clay layer, T-bar penetrometer tests were performed
162 on the clay layer in isolation following careful removal of the upper sand layer after all of the spudcan
163 penetration tests had been completed. This was intended to eliminate the influence of entrapped sand
164 beneath the penetrometer and avoid potential damage to the penetrometer that may have occurred if it
165 was penetrated through the sand layer. An intermediate roughness T-bar factor of 10.5 was assumed.
166 Given that the *OCR* increased as the sand was scraped away at intervals during the test schedule to
167 allow for thinner sand thickness, the shear strength profile of clay measured with the sand removed
168 was calculated using the following relationship to account for the impact of changes in *OCR* to the
169 shear strength (Koutsoftas and Ladd, 1985)

$$170 \quad \frac{s_u}{\sigma'_v} = aOCR^b \quad (2)$$

171 where s_u is the undrained shear strength, σ'_v is the vertical effective stress, and a and b are fitting
172 parameters. Two example T-bar tests from different locations within the drum channel are presented
173 in Fig. 2 indicating excellent sample uniformity. The *OCR* profiles for each of the three layer heights
174 were calculated using the measured effective unit weights of the sand and clay layers, prototype
175 dimensions and the consolidation g -level. The best fit of Eq. 2 to the T-bar penetrometer profiles for
176 all three sand layer heights tested was found with values for a and b of 0.16 and 0.74, respectively.
177 Thus, the sand-clay interface shear strengths and shear strength gradients for the underlying clay
178 layers tested were estimated using linear best fits to the non-linear profiles estimated using Eq. (2) and
179 are summarized in Table 1. In the following, all experimental results are reported with prototype
180 dimensions.

181 **Results and Discussion**

182 ***Penetration Resistance Profiles***

183 The nominal penetration resistance, q_{nom} , profiles (penetration force normalized by the maximum
184 bearing area of spudcan) for 15 medium loose sand overlying clay centrifuge tests are shown in Fig. 3.

185 They are grouped for different sand thickness. The displacement measurements are zeroed upon full
186 embedment of the spigot (i.e. spudcan embedded until a depth measured from the tip of the spigot
187 equal to $t_1 + t_2$ given in Table 1) as illustrated in Fig. 1. In general, both potential for punch-through
188 and rapid leg run (see Fig. 3) are observed in these nominal penetration resistance profiles, indicating
189 potential risk for spudcan installation on this type of soil stratigraphy. Punch-through and rapid leg
190 run might occur when there is a rapid vertical spudcan displacement. For the case of 'punch-through'
191 this is the result of an obvious reduction in the penetration resistance profile, while for rapid leg run
192 the rapid displacement may stem from a period of nearly constant q_{peak} in the penetration resistance
193 profile. Generally, punch-through is more likely to occur for larger H_s/D ratios and rapid leg run is
194 prone for lower ratios of H_s/D . Rapid leg run is potentially just as dangerous as punch-through since
195 the uncontrolled displacements shown here are as large as $0.3D - 0.7D$.

196 Fig. 4 presents selected typical nominal penetration resistance profiles for two pairs of spudcan
197 penetration tests on dense and medium loose sand overlying clay (noting that the $I_D = 92\%$ cases
198 presented are the data of Lee (2009)). These profiles have been chosen since Fig. 4(a) and (c) and Fig.
199 4(b) and (d) exhibit identical D , very similar H_s , and consequently very close values of H_s/D .
200 Comparison of these penetration resistance profiles provides insight into the impact of various
201 parameters on the peak penetration resistance and the potential of hazardous failure.

202 The comparisons of Fig. 4(a) and (b) and Fig. 4(c) and (d) demonstrate the impact of H_s/D on the
203 nominal penetration resistance profiles. For both dense and loose sands q_{peak} reduces with H_s/D . For
204 dense sand with $H_s/D = 0.78$, the q_{peak} is 620 kPa, while it is 430 kPa for $H_s/D = 0.44$. The reduction
205 of q_{peak} for medium loose sand is not so obvious, but still has a value of 15% for $H_s/D = 0.43$
206 compared with $H_s/D = 0.75$. This is because during the mobilization of q_{peak} , for high H_s/D , the
207 influence zone is mainly confined to the sand layer, which would contribute to a large q_{peak} . For the
208 dense sand tests in Fig. 4(a) and (b), the reduction of H_s/D decreases the magnitude of the peak
209 penetration resistance q_{peak} and also the potential length of the uncontrolled vertical displacement. For
210 the medium loose sand tests in Fig. 4(c) and (d), the impact of reducing H_s/D is to change the

211 potential of failure from punch-through to rapid leg run. This is further confirmed by the other
212 medium loose sand tests presented in Fig. 3.

213 Comparison of Fig. 4(a) and (c) and Fig. 4(b) and (d) highlights the impact of I_D on the failure mode.
214 For high H_s/D , in Fig. 4(a) and (c), reducing the I_D changes the penetration resistance from a peaked
215 and sudden failure, with significant rapid post-peak resistance reduction, to a more progressive failure
216 with attenuated post-peak resistance reduction. For low H_s/D , in Fig. 4(b) and (d), the same trend is
217 evident except that the medium loose sand failure potential becomes a rapid leg run rather than punch-
218 through.

219 This indicates that punch-through or rapid leg run failure is a potential problem for sand overlying
220 clay stratigraphies involving sand from medium loose to dense states, since even in Fig. 4(d), which
221 exhibits the smallest q_{peak} , the potential for uncontrolled rapid leg run was observed. As a result, the
222 failure stress dependent model proposed by Lee et al. (2009) for dense sand overlying clay is
223 developed in this paper to accurately predict q_{peak} for problems involving sand from medium loose to
224 dense states.

225 ***Peak Penetration Resistance***

226 Fig. 5 presents the peak penetration resistance, q_{peak} , versus the widest cross-sectional area for each of
227 the spudcans tested. The data are grouped in accordance with the thickness and relative density of the
228 sand layer. Fig. 5 illustrates that the general variations of the peak penetration resistances with the
229 widest cross-sectional areas may be fitted with power law equations. Specific equations are not given
230 for these fits since they are only intended to demonstrate trends in the results.

231 The bearing capacities of the spudcan for modern jack-ups are reported to be in the range of 200 to
232 600 kPa (Osborne et al. 2008). The experimentally measured peak penetration resistances shown in
233 Fig. 5 are within this range, which suggests that the current centrifuge model tests were appropriately
234 scaled to calibrate the proposed failure stress dependent model.

235 ***Depth of Peak Penetration Resistance***

236 In addition to the peak penetration resistance q_{peak} , the depth at which the peak penetration resistance
237 occurs must be predicted, since both are necessary for providing a full penetration resistance profile
238 for spudcan penetration on sand overlying clay. Based on centrifuge tests on dense sand overlying
239 clay conducted at UWA and at the National University of Singapore (NUS), Teh et al. (2010)
240 proposed that the effective sand thickness, H_{eff} , at mobilisation of q_{peak} was equal to $0.88H_s$. The depth
241 of penetration required to mobilise the peak penetration resistance, d_{peak} ($d_{peak} = H_s - H_{eff}$), is therefore
242 $0.12H_s$. Fig. 6 is a summary of the correlation between H_{eff}/D and H_s/D for all the centrifuge tests
243 listed in Table 1 and 2, except the beam centrifuge test of Lee (2009) of which the penetration
244 resistance profiles were not available. The relationship proposed by Teh et al. (2010) is consistent for
245 both UWA and NUS geometries of spudcan and the soil properties reported in Table 1 and 2. Thus the
246 depth of peak penetration resistance relative to the lowest elevation of the spudcan widest cross-
247 sectional area may be expressed with confidence as:

$$248 \quad d_{peak} = 0.12H_s \quad (3)$$

249 **Failure Stress Dependent Prediction Model**

250 ***Performance of Original Failure Stress Dependent Model***

251 As shown in Fig. 7, Lee et al. (2009) proposed an analytical model, which assumes that the peak
252 penetration resistance occurs when a sand frustrum with dispersion angle (the angle between assumed
253 slip surface and vertical plane) equal to the angle of dilation, ψ , is pushed into the underlying clay.
254 Hence, q_{peak} is the sum of the frictional resistance in the sand, the bearing capacity of the underlying
255 clay and the weight of the sand frustrum. The operative friction and dilation angles are related to q_{peak}
256 using a modified form of Bolton's (1986) empirical relationships:

$$257 \quad I_R = I_D (Q - \ln(p')) - 1 \quad 0 < I_R < 4 \quad (4)$$

$$258 \quad \phi' - \phi_{cv} = mI_R \quad (5)$$

259
$$0.8\psi = \phi' - \phi_{cv} \quad (6)$$

260 where I_R is a dilatancy indicator in degree, Q is the natural logarithm of the grain crushing strength
261 expressed in kPa, p' is the mean effective stress, ϕ' is the operative friction angle, ϕ_{cv} is the critical
262 state friction angle and m is a constant. Lee (2009) used 25 centrifuge model tests on dense sand
263 overlying clay and accompanying small-strain finite element simulations to back-analyze a best fit
264 value for m of 2.65. The authors also performed similar simulations of the medium loose sand
265 overlying clay tests presented in this paper with good comparability with the experimental
266 measurements, providing confidence that a value for m of 2.65 was appropriate irrespective of the
267 relative density of the sand layer.

268 In Lee's analytical model, a distribution factor, D_F , is defined to relate the local stress along the
269 failure surface to the average vertical stress, or more specifically the ratio of the vertical effective
270 stress at the slip surface to the mean vertical effective stress. The distribution factor depends on the
271 ratio H_s/D of flat or spudcan foundations and bilinear equations were proposed to depict the above
272 relationship.

273 For current tests for medium loose sand layers, optimized D_F values were derived by varying D_F until
274 the q_{peak} predicted by the original model of Lee et al. (2009) was equal to the measured. The optimised
275 D_F values are plotted against H_s/D in Fig. 8(a) alongside the calculated resistance divided by the
276 experimental resistance ($q_{peak, calculated}/q_{peak, measured}$) in Fig. 8(b). The bilinear variations of D_F with H_s/D
277 suggested by Lee et al. (2009) are plotted in Fig. 8 as well. Some skew of the regression line is
278 evident in Fig. 8(b), particularly with smaller H_s/D , which means the original model underestimates
279 the peak penetration resistance for smaller H_s/D . This is further verified by Fig. 8(a) as the bilinear
280 D_F equations do not capture the trend well, especially for cases when $H_s/D < 0.3$. This is not
281 unexpected since the above failure mechanism and bilinear D_F equations in its original state was
282 calibrated solely using experimental data for spudcans in a single height ($H_s = 6.2$ m) of dense sand
283 ($I_D = 92\%$) overlying clay. The original mechanism was validated, and not calibrated, using data from

284 only three tests performed on loose sand overlying clay reported in the literature. In addition, the
285 embedment depth achieved during mobilization of q_{peak} , is not accounted for.

286 ***Modification of the Failure Stress Dependent Model***

287 To account for the embedment depth at failure the original mechanism was modified, as shown in Fig.
288 9. In this modified failure mechanism, the peak penetration resistance is derived following the same
289 procedure as Lee (2009), but the embedment depth attained during mobilization of q_{peak} is taken into
290 account. The D_F values are optimized and a new power relationship with H_s/D is proposed based on
291 the modified failure mechanism. In brief, the problem is treated mathematically as a series of
292 infinitesimally thin horizontal discs, which allows the following differential equation to be formulated

$$293 \quad \frac{\partial \overline{\sigma'_z}}{\partial z} + \frac{E \tan \psi}{(D/2 + z \tan \psi)} \overline{\sigma'_z} - \gamma'_s = 0 \quad (7)$$

294 where $\overline{\sigma'_z}$ is the average vertical stress in each horizontal disc at depth z . The parameter E is adopted
295 to simplify the algebra and taken as

$$296 \quad E = 2 \left[1 + D_F \left(\frac{\tan \phi^*}{\tan \psi} - 1 \right) \right] \quad (8)$$

297 where ϕ^* is a reduced friction angle caused by non-associated flow which can be expressed as
298 (Drescher and Detournay, 1993)

$$299 \quad \tan \phi^* = \frac{\sin \phi' \cos \psi}{1 - \sin \phi' \sin \psi} \quad (9)$$

300 By assuming that D_F is constant with depth, Eq. (7) can be integrated to give

$$301 \quad \left(\frac{D}{2} + z \tan \psi \right)^E \cdot \overline{\sigma'_z} = \frac{\gamma'_s \left(\frac{D}{2} + z \tan \psi \right)^{E+1}}{\tan \psi (E+1)} + C \quad (10)$$

302 where C is a constant which can be determined through the following critical condition. Referring to
 303 the conceptual model in Fig. 9, when the depth z is equal to the effective sand thickness, H_{eff} , the
 304 mean vertical effective stress is equal to the bearing capacity of the underlying clay layer, thus C can
 305 be expressed as

$$306 \quad C = \left(\frac{D}{2} + H_{eff} \tan \psi \right)^E \cdot \left[(N_{c0} s_{u0} + q_0 + \gamma'_s H_{eff} + \gamma'_s d_{peak}) - \frac{\gamma'_s \left(\frac{D}{2} + H_{eff} \tan \psi \right)}{\tan \psi (E + 1)} \right] \quad (11)$$

307 where N_{c0} is the bearing capacity factor of clay at foundation base, which is obtained using the
 308 relationship proposed by Houlsby and Martin (2003) for circular foundations with shear strength
 309 increasing linearly with depth; s_{u0} is the undrained shear strength of the clay at the sand-clay interface
 310 and q_0 is the effective overburden pressure at the depth of the foundation.

311 By substituting Eq. (11) into Eq. (10), the mean vertical effective stress can be expressed as:

$$312 \quad \overline{\sigma'_z} = \frac{\gamma'_s \left(\frac{D}{2} + z \tan \psi \right)}{\tan \psi (E + 1)} + \frac{\left(\frac{D}{2} + H_{eff} \tan \psi \right)^E}{\left(\frac{D}{2} + z \tan \psi \right)^E} \cdot \left[(N_{c0} s_{u0} + q_0 + \gamma'_s H_{eff} + \gamma'_s d_{peak}) - \frac{\gamma'_s \left(\frac{D}{2} + H_{eff} \tan \psi \right)}{\tan \psi (E + 1)} \right] \quad (12)$$

313 According to Fig. 9, the spudcan penetration depth z is measured from the depth where the peak
 314 penetration resistance occurs and the peak penetration resistance can be obtained by setting z equal to
 315 zero. As discussed above, $H_{eff} = 0.88H_s$ for both tests involving dense and loose sand layers, by
 316 substituting $\overline{\sigma'_z}$ with q_{peak} and input the values for d_{peak} and H_{eff} in Eq. (12), the peak penetration
 317 resistance is thus expressed in terms of H_s :

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$$\begin{aligned}
 318 \quad q_{peak} = & (N_{c0}s_{u0} + q_0 + 0.12\gamma'_s H_s) \left(1 + \frac{1.76H_s}{D} \tan \psi \right)^E \\
 & + \frac{\gamma'_s D}{2 \tan \psi (E+1)} \left[1 - \left(1 - \frac{1.76H_s}{D} E \tan \psi \right) \left(1 + \frac{1.76H_s}{D} \tan \psi \right)^E \right]
 \end{aligned} \quad (13)$$

319 for cases where $\phi' > \phi_{cv}$. Similarly, for cases where $\phi' = \phi_{cv}$, the peak penetration resistance can be
 320 calculated as:

$$321 \quad q_{peak} = (N_{c0}s_{u0} + q_0 + 0.12\gamma'_s H_s) e^{E_0} + 0.88\gamma'_s H_s \left[e^{E_0} \left(1 - \frac{1}{E_0} \right) + \frac{1}{E_0} \right] \quad (14)$$

322 where E_0 is equal to

$$323 \quad E_0 = 3.52D_F \sin \phi_{cv} \frac{H_s}{D} \quad (15)$$

324 In Eq. (4), the mean effective stress p' is substituted with q_{peak} in Eq. (13) and through an iterative
 325 procedure using Eqs. (4) to (6) and (13) in a spreadsheet analysis (for example in MS Excel), this
 326 approach allows the operative friction angle and dilatancy (and thus dispersion angle of the sand
 327 frustum) to be related to the stress level at failure rather than the initial state. This method is
 328 advantageous as it avoids the use of design charts and sensitivity analysis can be conducted with ease.

329 Based on the modified failure stress dependent model and with the benefit of the additional
 330 experimental data presented, the distribution factor was recalibrated and optimized in terms of a wide
 331 range of spudcan geometries and of soil conditions incorporating both loose and dense sand overlying
 332 clay. The optimised D_F for the additional fifteen centrifuge tests for medium loose sand and tests for
 333 the dense sand by Lee (2009) are presented in Fig. 10(a). It is observed that the relationship between
 334 D_F and H_s/D is non-linear and better fitted with the power law.

$$335 \quad D_F = 0.642 \left(\frac{H_s}{D} \right)^{-0.576} \quad as \quad 0.16 \leq \frac{H_s}{D} \leq 1.0 \quad (16)$$

336 Using the original model and linear relationships proposed by Lee et al. (2009) the coefficient of
337 determination, R^2 , is 0.77 for experimental data in Fig. 10, whilst $R^2 = 0.94$ using the modified model
338 and the power relationship in Eq. (16). For low H_s/D , the embedded volume of the spudcan during
339 mobilisation of q_{peak} is a far larger proportion of the volume of the inverted truncated cone in the
340 modified failure mechanism than that for high H_s/D . This embedded volume causes increasing lateral
341 stress, and then the larger values of D_F . The embedded volume of the spudcan can also be expressed
342 in terms of H_s/D using a similar power relationship. Although it is not possible to link D_F directly to
343 the embedded volume of the spudcan at q_{peak} , (given that the increase in mean stress at the failure
344 surface of the proposed failure mechanism is highly unlikely to be directly proportional to the volume
345 of sand displaced during spudcan embedment) the similar power relationship would suggest that the
346 non-linear relationship proposed in Eq. (16) to describe D_F for spudcans is logical.

347 Similar to Fig. 8(b), the scattered markers in Fig. 10(b) shows the predictions for both loose and dense
348 sand tests based on the modified mechanism and power relationship of D_F . There is reduced skew for
349 the whole range of H_s/D of practical interest. This is because the embedment depth during the
350 mobilization of peak penetration resistance is accounted for in the modified failure mechanism and
351 the new D_F relationship is calibrated for a larger range of spudcan diameters and soil properties. More
352 tests are needed to investigate the suitability of the D_F relationship for different spudcan shapes
353 (conical angles).

354 ***Performance of the Modified Model in Predicting q_{peak}***

355 To further validate the performance of the modified and recalibrated model, three series of additional
356 centrifuge test data for the penetration of spudcans into sand overlying normally or lightly over-
357 consolidated clay have been compared. These additional tests comprise of seven tests by Teh (2007)
358 in the NUS centrifuge, three tests by Teh (2007) in the UWA beam centrifuge and five tests by Lee
359 (2009) in the UWA beam centrifuge. Table 1 and 2 contain a summary of the relevant geometric and
360 material parameters of these tests, as well as the experimental results. All the data used in this
361 validation were derived from tests with siliceous sand; consequently Q in Eq. (4) was assumed as 10

362 (Bolton, 1986). The critical state friction angle was taken as 31° for the sand used in the UWA tests
363 (White et al. 2008) and 32° for the Toyoura sand used in the NUS tests (Jamiolkowski et al. 2003).

364 The performance of the modified model is compared to the primary (based on the load spread
365 method) and alternative (based upon the punching shear method) recommendations of ISO (2012).
366 For each method, the measured and calculated peak penetration resistance predictions are presented
367 with $q_{peak, calculated}$ against $q_{peak, measured}$ and $q_{peak, calculated}/q_{peak, measured}$ against H_s/D , as shown in Fig. 11. A
368 linear regression line is used in the $q_{peak, calculated}/q_{peak, measured}$ figure to identify any apparent trend in
369 performance of the calculation with respect to H_s/D . Table 3 provides a summary of key performance
370 indicators such as mean, maximum, minimum, standard deviation and skew, where $\theta = \arctan(s)$ and s
371 is the slope of the regression line.

372 For both the ISO (2012) primary and alternative recommendations conservative predictions of q_{peak}
373 are obtained, with the majority of the predicted peak penetration resistances less than 60% of the
374 measured peak penetration resistances. The reason is that both methods ignore the properties of the
375 sand: the load spread factor is not related to the sand properties in the primary recommendation, and
376 the frictional resistance through the sand is expressed in terms of the normalized shear strength of the
377 underlying clay layer in the alternative recommendation. The alternative recommendation made by
378 ISO (2012) based on the punching shear mechanism actually performs better than the primary
379 recommendation based on the load-spread method. Referring back to Fig. 4 demonstrates the
380 implication of this conservative prediction of q_{peak} . For both medium loose and dense sands, such
381 conservatism would lead to gross under-estimation of the potential impact of both punch-through and
382 rapid leg run as the depth over which the event may occur would also be underestimated. The skew
383 angles presented in Fig. 11 and Table 3 demonstrate that the methods from ISO (2012)
384 recommendations exhibit significant bias in performance, with worsening predictions for larger H_s/D
385 for the load spread method. This is because at higher H_s/D ratios the thicker sand thickness leads to
386 the capacity of resistance generated by the sand being a larger proportion of q_{peak} . Hence, by ignoring

387 the contribution of the sand layer in the load spread method the predictions worsen with increasing
388 H_s/D .

389 In contrast to the ISO (2012) recommendations, the modified failure stress dependent model with the
390 recalibrated D_F provides an average of all the predictions of $q_{peak, calculated}/q_{peak, measured}$ of 1.01 and a
391 standard deviation of 0.11. All predictions, apart from test NUS_F5 from Teh (2007), are within \pm
392 20% of the measured values. The significantly less skew with respect to H_s/D for the predictions
393 indicates that the modified failure stress dependent model is capable of accounting for changes in
394 stratigraphy far more effectively than the ISO methods. This is because the failure stress is highly
395 dependent upon sand thickness and foundation size as demonstrated in Fig. 5, and the operative
396 friction angle and angle of inclination of the inverted truncated cone mechanism is related to the
397 failure stress in the modified failure stress dependent model. By adopting the modified failure stress
398 dependent model to improve the accuracy of the estimation of q_{peak} , the uncertainty and risk associated
399 with spudcan installation in sand overlying clay stratigraphies may be reduced.

400 **Conclusions**

401 Fifteen centrifuge tests have been conducted within a drum centrifuge to investigate spudcan
402 foundation behavior on medium loose sand overlying clay, representing the first comprehensive
403 investigation of punch-through or rapid leg-run potential for medium loose sand overlying clay. The
404 tests covered different prototype sand thicknesses in the range of 3.2 to 6 m and spudcan diameters in
405 the range of 6 to 20 m, corresponding to H_s/D ratios of 0.16 to 1. This covers the range of practical
406 interest for punch-through failure of jack-up platforms. This new data was combined with the data for
407 spudcan penetrating dense sand overlying clay from Lee (2009) to allow recalibration of the modified
408 failure stress dependent model. Interpretation of this data has led to the following conclusions:

- 409 1. The potential for catastrophic punch-through and rapid leg run of spudcans, already
410 demonstrated for dense sand overlying clay, is also a potential problem for medium loose
411 sand overlying clay sites.

- 412 2. The depth of occurrence of q_{peak} has been further confirmed experimentally to be a function of
413 H_s for the range of H_s/D of practical interest. Coupling the depth of occurrence with accurate
414 prediction of q_{peak} provides the first step in predicting the risk of punch-through failure for
415 sand overlying clay sites.
- 416 3. The failure stress dependent model of Lee et al. (2009) for predicting q_{peak} on sand overlying
417 clay has been modified to account for mobilization induced embedment. This modified
418 mechanism has been used to derive an equation to describe q_{peak} in terms of the undisturbed
419 sand thickness.
- 420 4. A new relationship has been proposed for D_F , which is used to relate the stress at the failure
421 surface to the average vertical stress in the modified failure stress dependent model. This
422 provides improved prediction of q_{peak} over a larger range of sand thickness to spudcan
423 diameter ratios H_s/D as well as sand relative densities. At this juncture the new relationship
424 has been calibrated and validated only for spudcan shapes similar to that tested here.
- 425 5. The modified failure stress dependent model, which is based on a kinematically admissible
426 failure mechanism and accounts for the embedment depth caused by mobilization of q_{peak} , was
427 shown to be capable of accurately predicting the peak penetration resistance q_{peak} for both
428 loose and dense sand overlying clay.
- 429 6. The performance of the modified failure stress dependent model has been compared with the
430 current recommended practice of the ISO (2012) primary and alternative recommendations,
431 and it was demonstrated that the modified model provides more accurate prediction of q_{peak}
432 with less bias with relation to H_s/D for a wide range of dense and loose sand over clay sites.

433 In summary, when used to back-calculate centrifuge data, the use of the ISO (2012) q_{peak} prediction
434 methods significantly underestimates the potential for punch-through during spudcan penetration on
435 sand overlying clay. The modified failure stress dependent model improves the q_{peak} predictions and
436 its adoption for field conditions offshore has the potential to better predict the potential for punch-

437 through or rapid leg run events during spudcan installation on sand overlying clay. This would
438 significantly reduce the risk associated with operating jack-up platforms in offshore locations with
439 sand overlying clay soil stratigraphy.

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