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RESEARCH ARTICLE

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Key Points:

- Particle travel times over bedforms are exponentially distributed as proposed for planar beds
- Streamwise and lateral hop distances over bedforms are not Weibull distributed as proposed for planar beds
- Bedforms increase the variance in streamwise and lateral hop distances and increase diffusive-like transport

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Probability Distributions of Particle Hop Distance and Travel Time Over Equilibrium Mobile Bedforms

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The joint probability distribution of streamwise particle hop distance, lateral particle hop distance, and travel time constrains the relationships between topographic change and sediment transport at the granular scale. Previous studies have investigated the ensemble characteristics of particle motions over plane bed topography; however, it is unclear whether reported distributions remain valid when bedforms are present. Here, we present measurements of particle motion over bedform topography obtained in a laboratory flume and compare these to particle motions over plane bed topography with otherwise similar conditions. We find substantial differences in particle motion in the presence of bedforms that are relevant to macroscopic models of sediment transport. Most notably, bedforms increase the standard deviation of streamwise and lateral hop distances relative to the mean streamwise hop distance. This implies that bedforms increase the streamwise and lateral diffusion lengths and, equivalently, increase diffusive-like fluxes.

1. Introduction

The joint probability distribution of particle hop distance and travel time encapsulates the relationship between granular sediment motion and topographic change (Ancey, 2010; Furbish et al., 2012; Nakagawa & Tsujimoto, 1976; Pelosi & Parker, 2014; Tsujimoto, 1978). Considerable attention has been devoted to the problem of discerning the forms of the associated marginal distributions and predicting their parameters or moments under steady, uniform macroscopic flow conditions (Abbott & Francis, 1977; Fathel et al., 2015; Furbish, Fathel, & Schmeeckle 2016; Hosseini Sadabadi et al., 2019; Lajeunesse et al., 2010; Liu et al., 2019). This objective represents an important step toward the development of models for large-scale fluvial morphodynamics that are consistent with the physics of grain-scale sediment transport.

Likely forms for the marginal probability distributions of particle hop distances and travel times can be obtained from simple assumptions about particle motion through statistical-mechanical arguments (Furbish, Fathel, & Schmeeckle, 2016; Furbish & Schmeeckle, 2013). These authors suggest that travel times are exponentially distributed, while streamwise and absolute lateral hop distances follow a Weibull distribution with shape parameter $0.5 \le k < 1$, neglecting the small fraction of particles that move in the upstream direction. Previous experimental measurements of particle motion confirm these predictions for uniform flow conditions over a flat streambed (Campagnol et al., 2015; Fathel et al., 2015, Furbish, Fathel, & Schmeeckle 2016; Lajeunesse et al., 2010; Liu et al., 2019; Wu et al., 2020). This still leaves a gap in understanding for the wide range of conditions under which the coupled motion of fluid and sediment amplifies small perturbations in bed elevation leading to the development of ripples and dunes (García, 2008; Southard & Boguchwal, 1990; Van den Berg & Van Gelder, 1993). We therefore seek to determine the forms of these distributions in the presence of equilibrium mobile bedforms.

The processes governing growth, coarsening, and subsequent dynamical behavior of bedforms involve a continual feedback between topography, flow, and sediment transport (Best, 1992; Charru et al., 2013; Coleman et al., 2006; Coleman & Nikora, 2011; Costello, 1974; McLean, 1990; Mclean et al., 1994; Southard & Dingler, 1971; Venditti et al., 2005a, 2006). A rich literature related to flow over bedforms reveals persistent zones of flow acceleration, expansion, and separation, which modulate the bed stress and transport fields (Best, 2005, 2009; Kwoll et al., 2017; Maddux, McLean, & Nelson, 2003; Maddux, Nelson, & McLean,

©2020. American Geophysical Union. All Rights Reserved. 2003; Mclean et al., 1994; Muste et al., 2016, Naqshband et al., 2017). Only recently have researchers begun to examine the effects of this interaction on particle kinematics through particle tracking and acoustic techniques. Experimental results indicate that instantaneous quantities like particle activity and velocity vary systematically in relation to topographic position while retaining probability distributions similar to those observed under plane bed conditions (Leary & Schmeeckle, 2017; Terwisscha van Scheltinga et al., 2019; Tsubaki et al., 2018; Wilson & Hay, 2016). What remains unclear is how bedforms influence Lagrangian integral quantities like particle hop distance and travel time, particularly insofar as they relate to the ensemble average flux and its advective and diffusive components (Ancey et al., 2015; Furbish et al., 2012).

The purpose of this paper is to clarify how bedforms influence time-integrated particle behavior by comparing observations of particle motion over bedforms and plane bed topography. We consider intermediate-timescale hops, defined as periods of continuous motion separated by periods of rest (*sensu* Ballio et al., 2018; Nikora et al., 2001). Here, we present the results of experiments designed to reveal differences in the probability distributions of particle hop distance and travel time over equilibrium mobile bedforms compared with plane bed topography. We focus on properties that are relevant to macroscopic transport to determine whether existing theory developed for plane bed topography provides a suitable description of particle motion when bedforms are present on the bed.

2. Theory

The topography of a granular bed evolves through the processes of particle entrainment and disentrainment. Each entrainment or disentrainment event produces a small change in bed elevation, which, averaged over time, results in macroscopic topographic change. This notion underlies the entrainment form of Exner equation (Furbish et al., 2012; Nakagawa & Tsujimoto, 1976; Parker et al., 2000; Tsujimoto, 1978), expressing the time rate of change of bed elevation η (L) at time *t*, streamwise position *x*, and cross-stream position *y* in terms of the difference between the volumetric particle entrainment rate *E* (L T⁻¹) and disentrainment rate *D* (L T⁻¹) per unit bed area:

$$c_b \frac{\partial \eta}{\partial t}(t, x, y) = -E(t, x, y) + D(t, x, y).$$
 (1)

Here, $c_b(-)$ is the concentration of particles in the bed.

Paired entrainment and disentrainment events are explicitly linked through the motion of individual particles, defining a spatiotemporal displacement vector with components of streamwise hop distance L_x (L), lateral hop distance L_y (L), and travel time T_p (T). Because these quantities are defined in terms of particle exchanges with the bed, they also form the basis for the relationship between sediment transport and topographic change. This statement can be demonstrated by invoking a master equation to rewrite D(tx,y) as

$$D(t, x, y) = \int_{-\infty}^{\infty} \int_{0}^{\infty} E(t - T_p, x - L_x, y - L_y) f_{T_p, L_x, L_y}(T_p, L_x, L_y; t - T_p, x - L_x, y - L_y) dT_p dL_x dL_y,$$
(2)

where $f_{T_p,L_x,L_y}(T_p, L_x, L_y; t, x, y)$ is the joint probability distribution of streamwise hop distance, lateral hop distance, and travel time of particles entrained at (t,x,y). Equation 2 (Furbish et al., 2012) is fundamentally nonlocal in that it integrates conditions over space and time; however, it can be approximated in terms of local variables as a Fokker-Planck equation (Furbish et al., 2012, 2017), given by

$$c_{b}\frac{\partial\eta}{\partial t}(t,x,y) = -\frac{\partial}{\partial x}E\overline{L_{x}} - \frac{\partial}{\partial y}E\overline{L_{y}} - \frac{\partial}{\partial t}E\overline{T_{p}} + \frac{1}{2\partial x^{2}}E\overline{L_{x}}^{2} + \frac{1}{2\partial y^{2}}E\overline{L_{y}}^{2} + \frac{1}{2\partial x\partial y}E\overline{L_{x}}\overline{L_{y}}$$
(3)

where overbars denote ensemble averages. This approximation is valid as long as the marginal probability distributions of hop distance and travel time have finite first and second moments and as long as the spatiotemporal scales of particle motion are small relative to the scales of change in flow conditions (Furbish et al., 2012). The one-dimensional fluxes q_x (L²T⁻¹) and q_y (L²T⁻¹) are obtained from (3) by assuming conditions are approximately steady in time and uniform in one spatial dimension. These assumptions

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are appropriate for many practical problems (Furbish et al., 2012; Furbish, Schmeeckle, et al., 2016). Noting that the variance is equal to the mean squared hop distance minus the squared mean, (i.e., $\sigma_{L_x}^2 = \overline{L_x^2} - \overline{L_x^2}^2$), the one dimensional fluxes are given by

$$q_{x}(t, x, y) = E\overline{L_{x}} - \frac{1}{2\partial x}E\overline{L_{x}}^{-2} - \frac{1}{2\partial x}E\sigma_{L_{x}}^{2}$$
(4)

and

$$q_{y}(t, x, y) = E\overline{L_{y}} - \frac{1}{2\partial y}E\overline{L_{y}}^{2} - \frac{1}{2\partial x}E\sigma_{L_{y}}^{2}.$$
(5)

As noted by Furbish et al. (2017), these terms do not map directly onto conventional advective and diffusive components of the flux containing the mean particle velocity and diffusivity. Instead, the first two terms comprise an advective-like flux consisting of a local term that is equal to the total flux under uniform transport conditions and a nonlocal term that accounts for spatial variability in particle entrainment rate and mean hop distance. The third term is like a diffusive flux in that it is driven by the variance in particle hop distance. This interpretation differs from previous studies, reflecting the decomposition of the raw variance (i.e., $\overline{I_x^2}$) into terms containing the squared mean and variance. Under this interpretation, the squared coefficient of variation (the ratio of the standard deviation to the mean) of particle hop distances is like an inverse Peclet number in that it scales the relative propensity for diffusion-like and advection-like transport. Similarly, the ratio of the variance to the mean is like a diffusion length in that it scales the diffusive-like flux. This idea is fully discussed in section 4.4.

The objective of this paper is to reveal the manner in which bedforms influence the marginal probability distribution of particle travel time $f_{T_p}(T_p)$, streamwise hop distance $f_{L_x}(L_x)$, and lateral hop distance $f_{L_y}(L_y)$. This work is primarily motivated by macroscopic morphodynamic modeling problems (e.g., Abramian et al., 2019) for which the most important features of these distributions are the statistical moments contained in Equations 3–5. We consider multiple indicators of distribution fit; however, we place special emphasis on those which pertain to the estimation of these moments. Results are interpreted in the context of probability distribution models proposed by Fathel et al. (2015), which are consistent with various mechanical constraints (Furbish, Fathel, & Schmeeckle, 2016) as well as with empirical constraints imposed by an extensive data set of particle motion over plane bed topography (Roseberry et al., 2012). These distributions exist on the domain from 0 to infinity and thus ignore hops in the upstream direction. They also have thin tails and fixed coefficients of variation, implying that the propensity for diffusion-like transport varies in proportion to the advective component of flux across a wide range of conditions as discussed in more detail below. We aim to determine the extent to which the constraints that derive from the forms of these distributions provide a realistic foundation for modeling macroscopic sediment transport phenomena when bedforms are present.

3. Experiments

3.1. Overview

In order to compare the ensemble statistics of particle motions that are characteristic of plane bed and bedform topography, we conducted two flume experiments differentiated primarily by the presence or absence of equilibrium bedforms. For each experiment we recorded videos of fluorescent tracer particles that were used to construct empirical distributions of particle hop distance and travel time. In considering fixed distributions of these quantities, we appeal to the idea of an ensemble of nominally identical systems first described by Gibbs (1902) and elaborated recently with respect to bedload transport by Furbish et al. (2012). We designed our experiments so that the distributions measured over a finite temporal and spatial domain may be assumed to be equivalent to the instantaneous ensemble distribution at any position and time. This assumption is reasonable as long as the macroscopic average conditions are steady and uniform over the domain of data collection.

Theory and analyses presented here assume a steady, uniform probability distribution of particle hop distance and travel time that is independent of x, y, and t. Although previous studies find that particle motion depends on location relative to bedform features (Leary & Schmeeckle, 2017; Terwisscha van Scheltinga et al., 2019; Tsubaki et al., 2018; Wilson & Hay, 2016), we emphasize that the existence of bedforms does



not preclude the possibility of considering a stationary distribution averaged over all possible configurations of bedform topography. Bedforms are viewed as stochastic fluctuations in bed elevation, and there is a timescale over which a single location on the bed experiences a representative sample of all possible configurations of topography characteristic of the macroscopic flow conditions (e.g., the bedform field timescale as envisioned by Furbish et al., 2012). In this context, the term "macroscopic" implies averaging over scales much larger than an individual bedform.

In order to ensure that measured distributions reflect ensemble probability distributions characteristic of macroscopic flow conditions, measured particle motions would ideally contain a sample that is representative of all possible microconfigurations of flow and topography. In practice, this means that particle hops should be measured over spatiotemporal scales that are much larger than those of significant autocorrelation in flow velocity and bed elevation. Due to practical limitations, this was not possible for the bedform condition: Particle motions were recorded over a small region of the bed with streamwise and cross-stream dimensions comparable to the bedform length scale, which we assume is similar to the autocorrelation length scale of topography (Nikora et al., 1997; Nordin, 1971). Nonetheless, we posit that these data are sufficient to reveal important features of particle motion over two 10-s intervals. All tracer particle motions in the measurement window were included in our analysis such that the empirical distributions approximately reflect the relative entrainment rates in stoss and lee regions of one bedform. For additional discussion of issues related to the finite sampling window, see section 4.5.

3.2. Description of Experiments

Experiments were conducted in a 7.2-m-long × 0.29-m-wide flume capable of recirculating both sediment and water. Bedforms were allowed to develop under constant flow conditions over a period of 48 hr, at which point particle motions were recorded using a downward-looking camera. Plane bed conditions were then achieved by manually grading the bed using a plastic paddle, and particle motions were recorded again. Flume boundary conditions remained constant throughout this procedure: Water discharge was 18 L/s, the flume slope was 0.001, and flow depth at the outlet was set to approximately H = 0.16 m. The mean flow velocity was U = 0.39 m/s, and the Froude number was $Fr = U/\sqrt{gH} = 0.31$.

The bed material consisted of natural sediment collected in an aeolian dune field near the Seminoe Reservoir in Wyoming. Fine sediment was removed prior to these experiments by continuously siphoning turbid water in the outlet reservoir and replacing it with clear water. The resulting bed material had a median diameter of 330 µm and median settling velocity $\omega_s = 4.4$ cm/s. The Base-2 logarithmic standard deviation was 0.69 (68% of the bed material was within a multiplicative factor of $2^{0.69} = 1.61$ of the mean). This is typical of hydraulically sorted natural sediment in fluvial systems but is a significant departure from the single-grain size experiments reported in previous studies. The implications of this difference are discussed in section 4.2.

Particle motions were measured using videos of fluorescent tracer particles. To this end, a small fraction of the bed material was removed from the flume and coated with a thin layer of fluorescent paint. Although we cannot rule out the possibility that the paint caused small differences in particle properties, we expect that such effects are small and do not influence the primary findings of this study. Approximately 30 cm³ (including pore space) of tracer particles were added back into the flume and allowed to mix with the unpainted bed material over a period of several weeks of continuous run time under a range of flow conditions. The thickness of sediment within the flume was approximately 8 cm such that the total volume of sediment in the flume including pore space was approximately 170,000 cm³ and tracer particles composed an estimated 0.017% of the bed material. For comparison, the tracer particle percentage estimated by comparing the tracer particle flux and the bedform bedload flux (discussed below) is 0.019%. Particles were illuminated with black lights (GE Black Light Blue bulbs, peak wavelength = 368 nm) through the side windows of the flume test reach (Figures 1a and 1b), which increased the contrast of tracer particles against the bed and facilitated consistent tracking (Naqshband et al., 2017). We assume that this procedure provides an unbiased sample of complete particle hops representing the full distribution of particle sizes.

Acoustic measurements of the near-bed flow velocity profile were collected over equilibrium bedforms to compute the bed stress condition (Bagherimiyab & Lemmin, 2013; Le Bouteiller & Venditti, 2015). The



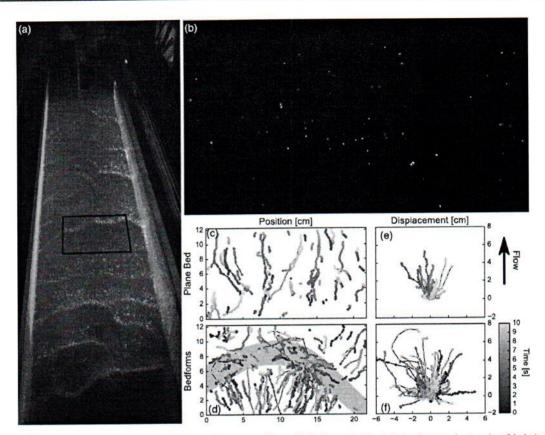


Figure 1. Experimental setup and tracked particle motions. (a) Oblique view of flume with bedforms. Black box indicates the approximate region of the bed where videos of fluorescent tracer particles were recorded. (b) Still image from video of fluorescent tracer particles during the bedform condition. Flow is from bottom to top. (c) Tracked particle motions over plane bed and (d) bedform topography. Gray region in (d) indicates the position of a bedform lee face. Note that the particle transport direction exhibits conditional dependence on topographic configuration in the vicinity of the particle that is discussed in more detail in section 4.1. (e) Visualization of particle displacements over plane bed and (f) bedform topography. Topographic effects manifest as qualitative differences in between (e) and (f).

sidewall-corrected shear velocity was $u_* = 2.4$ cm/s. This produced bedload dominated bedforms with a suspension number (the ratio of shear velocity to sediment settling velocity) of 0.54. For comparison, the unit bedload flux estimated from bedform migration using the bedform bedload equation of Simons et al. (1965) was $q_b = 4.1 \times 10^{-7} \text{ m}^2/\text{s}$. Applying the Wong and Parker (2006) bedload equation and solving for stress suggests that the effective shear velocity (i.e., skin friction) driving sediment transport was $u_{ssk} = 1.8$ cm/s. This is consistent with the notion that pressure differences across a bedform reduce the bedload transport rate associated with a specified average bed stress.

Although fluid velocities were not measured directly for the plane bed condition, we may estimate of the shear velocity by comparing the relative magnitudes of the tracer particle flux (discussed below) using the Wong and Parker (2006) bedload equation. The tracer particle flux for the plane bed experiment was 2.1 particles per second per meter width. The bedload flux is estimated to be 1.9×10^{-7} m²/s leading to an estimated shear velocity of $u_* = 1.7$ cm/s and a suspension number of 0.38. We emphasize that this estimate requires substantial assumptions and is reported here as a rough approximation to contextualize our experiments. However, the specific values of the shear velocity are not central to any of the theoretical developments or interpretations presented below.

Characteristic scales of bedform topography were computed from one-dimensional scans obtained using an ultrasonic profiler mounted to a moving cart. Equilibrium bedforms had a characteristic height $H_c = 1.5$ cm, a characteristic length $L_c = 16$ cm, and a characteristic migration velocity $V_c = 0.50$ cm/min. Bedform height was determined using $H_c = 2\sqrt{2}\sigma_\eta$ where σ_η is the standard deviation of bed elevation (McElroy, 2009). L_c was determined from the spectral centroid of the bed profile, and V_c was determined from the maximum of the cross-correlation function of successive scans (Van der Mark & Blom, 2007). The characteristic evolution timescale of bed elevation η computed as $T_\eta = \eta/(\partial_\eta/\partial_t)$, was approximately 8 min, such that topography is effectively fixed within the 10-s data collection intervals.

Videos of particle motion were recorded using a submerged downward-looking camera mounted near the centerline of the flume with the lens approximately 15 cm from the bed. Videos were collected at a resolution of 1920 by 1,080 pixels and at a frame rate of 30 frames per second. This window covered a streamwise distance of 12.2 cm and a cross-stream distance of 21.7 cm. Two 10-s intervals from each video were used for this analysis. Image registration and rectification were performed using OpenCV in Python (Bradski, 2000) Particles were digitized manually using TrackMate (Tinevez et al., 2017), an open-source particle tracking package for ImageJ (Rueden et al., 2017; Schindelin et al., 2012). All particles that moved during each interval were tracked for their entire visible path, including rest times (Figure 1).

The position of the particle centroid was tracked to within roughly one pixel such that the total uncertainty in each estimate of particle hop distance is roughly 0.022 cm (or one pixel at the start and beginning of each hop). Note that this is comparable to the median particle diameter. The uncertainty in each particle hop distance is approximately 6.25% of the mean hop distance in the plane bed experiment and 9.5% of the mean hop distance in the bedform experiment. This error may be positive or negative such that it is unlikely to bias estimates of the mean hop distance. In principle, this type of uncertainty could result in a positive bias in estimates of the variance by adding normally distributed noise; however, the magnitude of this effect is small and equivalent for both experiments. As a result, it is ignored in the analysis presented below.

The timing of the end and beginning of particle motions can be constrained to within one frame (0.033 s). Assuming perfect detection of particle motion, the measured hop duration will always be greater than or equal to the true hop duration because motion will always be registered as starting the frame before motion begins and ending the frame after motion ends. This effect will introduces a positive bias to empirical estimates of the mean travel time if the particle is assumed to be moving for the full duration over which motion is observed. Correcting for this bias is not trivial and depends on assumptions about the underlying distribution of particle travel times; however, we note that the effect on the computed moments is small, biasing the estimate of the mean travel time by approximately one frame time and introducing essentially no bias to the stimate of the variance. A moderate bias correction does not influence the primary findings of this paper and is not performed here.

3.3. Definition of a Particle Hop

The concept of a complete particle "hop" follows from the notion that particles may occupy one of two mutually exclusive states: motion and rest (Hosseini Sadabadi et al., 2019). This distinction is critical to the interpretation of particle-kinematic statements of sediment mass conservation, namely, the divergence and entrainment forms of the Exner equation. However, differentiating between active and stationary particles is not straightforward: Grains on the bed surface may wiggle in place without moving appreciably and may accumulate significant displacements over long timescales due to granular creep (Houssais et al., 2015). In fact, granular transport occurs via numerous phases (Houssais & Jerolmack, 2017); the binary view of mobility is merely a convenience adopted to delineate highly disparate scales of particle velocity and flux for the purposes of mathematical abstraction.

This reasoning suggests that particles on or below the bed surface are not truly stationary in the sense that they have detectable mean velocities averaged over long timescales. Consequently, empirical studies of particle motion which attempt to differentiate between mobile and immobile grains do so according to criteria that, despite their intuitive appeal, lack clear physical justification (Hosseini Sadabadi et al., 2019). For example, particles are often treated as mobile when their velocity exceeds a threshold value that is either explicitly stated or set implicitly by the resolution of the technique used to digitize particle motions. Such criteria retain the important property of mass conservation as long as the mobile and immobile states encompass all grains and are mutually exclusive, and mobile particles are not counted toward the elevation of the bed. Moreover, velocity criteria are valid in scenarios where sediment transport and morphodynamics are dominated by bedload transport rather than granular creep.

Other criteria that are equally valid from a theoretical perspective may lead to different results as to whether certain particles are mobile or immobile, ultimately producing differences in measured distributions of particle hop distance and travel time (Hosseini Sadabadi et al., 2019). We recognize this issue but do not attempt to solve it here. Instead, we use an approach that is similar to previous studies (Liu et al., 2019) and acknowledge where our results might be sensitive to this choice. Velocity criteria are an objective, reproducible solution to this problem. Different velocity thresholds may produce different distributions of particle hop distance and travel time but will lead to essentially the same estimate of the macroscopic flux as long as the velocity threshold is sufficiently small.

The exact value of the velocity threshold used here was chosen following the approach of Liu et al. (2019). Specifically, we examined particle motions under a range of velocity thresholds and found that values ranging from 0.2 to 0.5 cm/s reliably discriminated between visually identified mobile and immobile states. The exact value of the threshold within this range affects the absolute magnitude of empirical moments but has almost no effect on the primary findings of this paper, which concern their relative magnitudes and the shape of the distribution functions. Reported results were obtained using a velocity threshold of 0.3 cm/s. This value is significantly lower than the threshold velocities adopted by Liu et al. (2019) and Lajeunesse et al. (2010), perhaps because the lower frame rate (30 frames per second in the present study compared with 90 frames per second) allows more precise estimates of frame-averaged velocity. This number corresponds to a one-frame displacement of 0.01 cm over one thirtieth of a second, which is roughly one pixel or one third of the median grain diameter. Particles with frame-averaged velocities greater than or equal to the threshold velocity are considered mobile, and all other particles are considered immobile. A complete hop is defined as an uninterrupted period in the mobile state that begins and ends with transitions to and from the immobile state. Insofar as previous plane bed studies necessarily employ some variant of this approach, it is sufficient to eveal the extent to which particle motions over bedforms conform to existing theory.

4. Results and Discussion

The experimental procedure described in the previous section yielded measurements of 360 complete particle hops for the plane bed condition and 1,170 hops for the bedform condition. These data are visualized in Figure 1, which shows all tracked particle motions, and Figure 2, which shows the pairwise relationships between variables. Descriptive statistics are reported in Table 1.

Tracked particle paths reveal significant qualitative differences between the plane bed and bedform experiments. Notably, particle behavior clearly depends on position relative to bedform features in a manner that is reminiscent of the backward facing step experiments of Leary and Schmeeckle (2017) and the particle velocity fields reported by Tsubaki et al. (2018) and Terwisscha van Scheltinga et al. (2019). Particle transport direction is highly variable in the region of flow separation immediately downstream of the bedform crest. On the stoss side, particle transport direction is more regular and the mean local transport direction is approximately perpendicular to the nearest crest (Figures 1c and 1d). These behaviors produce significant qualitative differences in the characteristics of particle displacement as shown in Figures 1e, 1f, and 2.

Empirical moments are reported in Table 1. Although the mean particle travel time and mean streamwise hop distance are slightly larger in the plane bed experiment, we find that the distribution of particle hop distances over bedforms has much larger variance in the cross-stream and streamwise directions. This difference reflects the increased variability in hop distances evident in Figure 2. The sample size in both experiments was sufficiently large such that conventional measures of statistical uncertainty indicate that moments are estimated with high precision. For example, the 95% asymptotic confidence interval for the estimate of the mean travel time in the bedform experiment ranges from 0.12 to 0.14 s. More sophisticated estimates of statistical uncertainty produce similar results. However, these statistical measures only quantify uncertainty associated with measurement error and finite sample size and cannot quantify uncertainty associated with the finite measurement window (section 4.5). We believe that this effect is the primary source of for other parameters are not reported here.

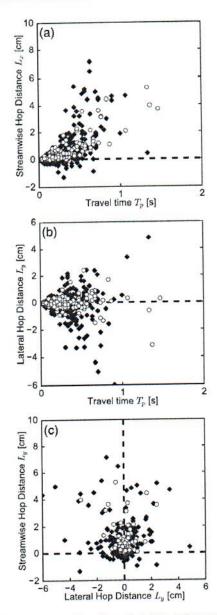


Figure 2. Pairwise comparison of measured particle hop distances and travel times. Dashed lines indicate particle hop distances of 0. Bedform data are shown in black diamonds, and plane bed data are shown in white circles. Panels (a) and (b) illustrate a conditional dependence of streamwise and lateral particle hop distance on travel time that is used by Fathel et al. (2015) to derive the Weibull distribution for particle hop distances. Panel (c) encompasses the primary qualitative differences between the plane bed and bedform experiments; particle motions over bedforms exhibit a wider spread in both the streamwise and cross-stream directions, and upstream hops appear to occur more frequently and have larger magnitudes over bedforms than over planar topography.



| and the second second second second second | Plane bed | Bedforms |
|--|--|--|
| Mean travel time T_p | 0.18 s 0.042 s^2 | 0.13 s 0.023 s ² |
| Variance $\sigma_{T_p}^2$ | 1.13 | 1.13 |
| Coefficient of variation σ_{T_p} / T_p Mean streamwise hop distance I_x | 0.32 cm 0.43 cm ² | 0.21 cm 0.47 cm ² |
| Variance $\sigma_{l_x}^2$ Coefficient of variation σ_{L_x}/L_x | 2.04 | 3.25 2.22 cm |
| Streamwise diffusion length ℓ_{D_s} Inverse Peclet number $P \not\subset^1$ | 1.34 cm 4.2 | 10.6 |
| Mean lateral hop distance I_{γ} Variance σ_{L}^{2} | -2.2×10^{-3} cm 0.11 cm ² | -2.8×10^{-2} cm 0.27 cm ² |
| CV of absolute values $\sigma_{ L_r }/ L_y $ | 2.20 | 2.70 |
| Coefficient of lateral transport σ_{I_2}/L_x | 1.03 | 2.49 |
| Lateral diffusion length $\ell_{D_{\gamma}}$ Inverse Peclet number Pe_{γ}^{-1} | 0.34 cm 1.07 | 1.29 cm 6.17 |

4.1. Physical Mechanism for Observed Differences in Particle Behavior

Previous studies of particle motion find that particle velocities are conditionally dependent on the local topographic configuration due to the coupling of topography, flow, and sediment transport (Terwisscha van Scheltinga et al., 2019; Tsubaki et al., 2018). Topographically induced correlations in flow velocity exist over spatial scales that are comparable to the bedform length; in contrast, we find that the average hop distance is much smaller than a bedform length. As a result, individual particle hops do not converge on the ensemble statistics of motion (Fathel et al., 2016; Furbish et al., 2017), instead reflecting topographically induced deviations from the mean flow field.

As an example, consider a particle that is entrained on a stoss slope that is oriented obliquely relative to the mean flow direction. This topographic configuration usually results in flow being redirected laterally (Best, 2005; Venditti et al., 2005b), causing a corresponding lateral component of sediment movement (Tsubaki et al., 2018; Terwisscha van Scheltinga et al., 2019) that is possibly amplified by gravitational effects (Parker et al., 2003). Because particle motions are short relative to the spatial scales of topography, this particle is likely to spend the entire interval from entrainment to disentrainment on this oblique slope. A large lateral hop distance would be highly improbable over plane bed topography under similar mean flow conditions, but would be typical for particles entrained in this location.

We suggest that observed differences in probability distributions of particle hop distance and travel time are the result of this effect. Over plane bed topography, turbulent fluctuations in flow velocity and collisions between particles are the primary sources of variability (Fathel et al., 2015; Hosseini Sadabadi et al., 2019; Nikora et al., 2001, 2002; Seizilles et al., 2014). We infer that localized fluctuations in flow velocity driven by bedform topography cause variability in particle behavior that is superimposed on variability driven by turbulence and particle collisions. Tsubaki et al. (2018) and Terwisscha van Scheltinga et al. (2019) report similar behaviors, which manifest as deviations from the mean particle velocity field characterized by crest-normal transport on the stoss sides of bedforms (Fryberger & Dean, 1979; Werner & Kocurek, 1997), and highly variable transport over lee faces and troughs (Figures 1c and 1d). This causes a marked qualitative difference in particle behavior that is apparent in Figures 1e, 1f, and 2 as enhanced variability in transport the entrainment forms of the flux and Exner equations.

4.2. Effect of Naturally Sorted Sediment

Our analysis assumes that the marginal distributions of particle hop distance and travel time have thin tails such that the mean and the variance are well defined. Although previous studies suggest that this is true for monodisperse sediment undergoing low bedload transport (Fathel et al., 2015; Furbish, Fathel, & Schmeeckle 2016; Liu et al., 2019), heavy-tailed distributions of hop distance and travel time are possible if a range of grain sizes are present and the mean hop distance varies with grain size (Ganti et al., 2010). Our experiments involved naturally sorted sediment, which is valuable insofar as we seek to understand

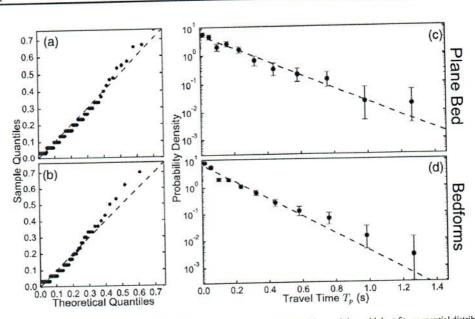


Figure 3. Quantile-quantile (a, b) and density plots (c, d) comparing measured distributions of particle travel time with best fit exponential distributions (dashed lines). Densities were computed using logarithmically spaced bins. Error bars represent the 95% Bayesian credible interval for a binomial proportion obtained using Jeffrey's prior (Brown et al., 2001). Deviations from theory are similar in both experiments and do not cause a substantial difference in the coefficient of variation in travel times. We interpret observed deviations as measurement error rather than as genuine features of the data set.

natural transport systems. However, it is important to consider the extent to which theory developed for uniform sediment may be applicable to the present research.

As a starting point, we consider the distribution of streamwise hop distance as a margin of the joint distribution of particle hop distance and grain size, $f_{L_x,D}(L_x, D)$:

$$f_{L_x}(L_x) = \int_0^\infty f_{L_x|D}(L_x|D) f_D(D) dD.$$
 (6)

Ganti et al. (2010) clarify how this integration may lead to a heavy-tailed distribution of hop distance. Specifically, if $f_{L_X|D}(L_X|D)$ is exponential with mean varying in proportion (or inverse proportion) to grain size and $f_L(D)$ is a Gamma distribution with shape parameter α , then $f_{L_X}(L_X)$ is a generalized Pareto distribution. This argument also holds for particle travel times. In this scenario, the mean only converges if $\alpha > 1$ and the variance only converges if $\alpha > 2$. We note that the coefficient of variation of a Gamma distribution is equal to $1/\sqrt{\alpha}$. Thus, the weight of the tails depends on the degree of sorting of the bed material, where well-sorted sediments are less likely to have heavy-tailed distributions of hop distance and travel time. The best fit Gamma distribution for the bed material used in these experiments has a shape parameter $\alpha = 4.83$ such the mean and variance are well defined. On this basis, we suggest that it is reasonable to expect that the distributions of hop distance and travel time are thin tailed.

Even if the distributions have thin tails, variability in grain size implies that the marginal probability distributions of hop distance and travel time depend on (a) the functional form of the grain-size specific distribution of hop distance and travel time (e.g., $f_{L_{X}|D}(L_{X}|D)$, (b) the relationship between the grain size and the parameters of this conditional distribution, and (c) the relative entrainment rates of different grain sizes (which may differ from the grain size distribution of the bed material due to selective entrainment and vertical sorting). Each of these effects may be present in our data; however, we focus on the collective outcome and have not attempted to evaluate their importance individually.

4.3. Comparison of Theoretical and Empirical Distributions

4.3.1. Travel Times

Previous studies suggest that the marginal probability distribution of bedload particle travel times is exponential (Fathel et al., 2015; Furbish, Fathel, & Schmeeckle, 2016); that is,

$$f_{T_p}(T_p) = \frac{1}{\tau} e^{-T_p/\tau},$$
(7)

where τ is a characteristic travel time. This implies a fixed temporal disentrainment rate for moving particles (Furbish, Fathel, Schmeeckle, 2016; Tucker & Bradley, 2010). In other words, the probability that a particle in motion at time t is deposited over the next small time interval dt does not depend on how long the particle has been in motion at t in the absence of other information about the flow and topographic configuration. Previous studies have suggested that this distribution is not strictly exponential (due to the presence of truncated tails) but may be treated as such for most practical purposes (Fathel et al., 2015).

Quantile-quantile (Q-Q) plots (Figures 3a and 3b) and histograms (Figures 3c and 3d) reveal that the exponential distribution provides a reasonable fit to plane bed and bedform particle travel times (Figure 3). The coefficient of variation (the ratio of the standard deviation to the mean) of an exponentially distributed random variable is 1, which is an important diagnostic test of distribution fit. Measured coefficients of variation are 1.13 for both experiments (Table 1). Based on these observations, we suggest that (a) our data confirm the findings of previous authors with regard to the exponential distribution of particle travel times over plane bed topography and (b) the presence of equilibrium mobile bedforms does not substantially influence the functional form of this distribution. We also find no evidence that the distribution of travel times is heavy-tailed despite variability in bed material grain size typical of natural fluvial systems.

4.3.2. Streamwise Hop Distances

Theoretical distributions proposed by Fathel et al. (2015) to describe streamwise hop distances follow from exponentially distributed travel times combined with the assumption that particles with longer travel times have the opportunity to attain higher velocities (Roseberry et al., 2012). This suggests that a conditional dependence of particle hop distance on travel time (evident in Figures 2a and 2b) that can be approximated by $L_x = a_x T_p^{b_x} + \epsilon_x$ (Fathel et al., 2015), where a_x is a characteristic acceleration, ϵ_x is a residual deviation term, and b_x is a scaling parameter that may be connected to suspension conditions. For bedload-dominated transport, particle travel times are short relative to the timescale required to accelerate particles to the mean near-bed fluid velocity and particle hops are dominated by the unsteady acceleration and deceleration phases of motion (Campagnol et al., 2015). As a result, previous studies which report bedload-dominated transport over plane bed topography (e.g., Fathel et al., 2015) find that $L_x/T_p \sim T_p$ and leading to $b_x = 2$. It has been suggested that this dependence disappears at higher suspension conditions (Ancey & Heyman, 2014; Campagnol et al., 2015; Heyman et al., 2016; Wu et al., 2020); however, we restrict our attention to bedload-dominated transport similar to previous plane bed studies. Ignoring the residual deviation and assuming exponentially distributed travel times leads to the expectation that hop distances follow Weibull distributions (Fathel et al., 2015). Thus, the marginal distribution of streamwise hop distances is given by

$$f_{L_x}(L_x) = \frac{k_x}{\lambda_x} \left(\frac{x}{\lambda_x}\right)^{k_x - 1} e^{-(x/\lambda)^{k_x}}$$
(8)

where $k_x = 1/b_x$ and $\lambda_x = a_x \tau^{b_x}$. If $k_x = 1/2$, then the mean and variance in particle hop distance can be expressed in terms of model parameters as $\overline{L_x} = 2a_x\tau^2$ and $\sigma_{L_x}^2 = 20a_x^2\tau^4$.

In considering whether this distribution is suitable for hop distances over bedforms, we focus primarily on the considerations relevant to macroscopic morphodynamic modeling outlined in section 2. Specifically, we ask whether estimates of distribution parameters a_x and τ can lead to accurate predictions of the mean hop distance $\overline{L_{\alpha}}$ and the variance $\sigma_{L_{\alpha}}^2$. This question is of central importance if the eventual goal is to construct macroscopic morphodynamic models that are consistent with the physics of grain-scale sediment transport. The proposed Weibull distribution with shape parameter k = 1/2 prescribes a fixed coefficient of variation $\sqrt{5} \approx 2.23$. This implies that the variance $\sigma_{I_a}^2$ can be estimated from a measurement of the mean. If k is



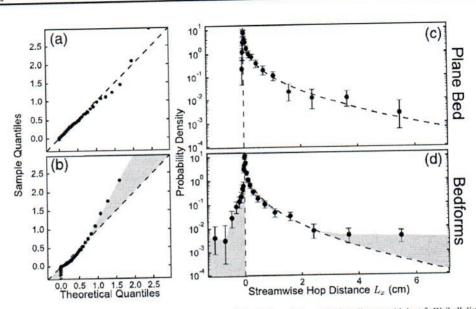


Figure 4. Quantile-quantile (a, b) and density plots (c, d) comparing measured distributions of streamwise hop distance with best fit Weibull distributions with shape parameter k = 1/2 (dashed lines). Densities were computed using logarithmically spaced bins. Error bars represent the 95% Bayesian credible interval for a binomial proportion obtained using Jeffrey's prior (Brown et al., 2001). Red regions in panels (b) and (d) highlight systematic deviations from plane bed theory.

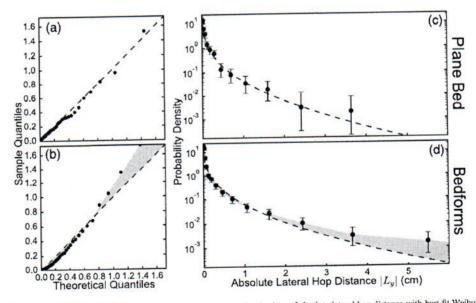


Figure 5. Quantile-quantile (a, b) and density plots (c, d) comparing measured distributions of absolute lateral hop distance with best fit Weibull distributions with shape parameter k = 1/2 (dashed lines). Densities were computed using logarithmically spaced bins. Error bars represent the 95% Bayesian credible interval for a binomial proportion obtained using Jeffrey's prior (Brown et al., 2001). Red regions in panels (b) and (d) highlight systematic deviations from plane bed theory.

allowed to vary between 1/2 and 1, the coefficient of variation must be between 1 and $\sqrt{5}$. The coefficient of variation therefore is an important indicator of distribution fit; if it is significantly larger than $\sqrt{5}$ or smaller than 1, no single estimate of model parameters appropriately characterizes the advective and diffusive components of the flux simultaneously.

Measured streamwise hop distances in the plane bed experiment have a coefficient of variation of 2.05 compared with 2.23 predicted from theory. Ignoring upstream hops does not significantly affect the estimate of the mean because only 5% of hops occur in the upstream direction and the average upstream hop distance is very small relative to the average downstream hop distance (0.1 mm compared with 3.5 mm). As with travel times, we find no evidence that the distribution of particle hop distance is heavy tailed for the moderately sorted sand used in this experiment. We suggest that the distribution of streamwise bedload hop distances over plane bed topography in hydraulically sorted, natural sediments can be sufficiently approximated using a Weibull distribution with shape parameter k = 1/2 in the context of macroscopic transport problems.

In contrast, the distribution of streamwise hop distances over bedforms exhibits significant deviations from theory. Qualitative comparison of the histogram and a best fit theoretical distribution (Figure 4d) reveals systematic differences in probability density across the full range of observed hop distances that results in a concave-up relationship between empirical and theoretical quantiles (Figure 4b). A much larger fraction of hops occur in the upstream direction (15%), and these possess an average upstream displacement that are a significant fraction of the average downstream displacement (0.8 mm compared with 2.8 mm). We conclude that the presence of bedforms leads to an important difference in empirical moments: The coefficient of variation in measured streamwise hop distances is 3.25, meaning that the standard deviation does not vary with the mean as expected. Instead, observed spatiotemporal correlations between particle behavior and topography lead to an increased variance relative to the mean (Figures 1d and 1f) that violates constraints imposed by plane bed theory.

4.3.3. Lateral Hop Distances

The streamwise and lateral coordinates are defined such that lateral hop distances have a mean of 0 and are symmetrically distributed under steady, uniform transport conditions considered here. Like with streamwise hop distances, Roseberry et al. (2012) and Fathel et al. (2015) find that the absolute lateral displacement is correlated with travel time leading to $|L_y| = a_y T_p^{b_y} + \epsilon_y$, where $h_y \approx 2$. The distribution of absolute lateral hop distances can therefore be approximated using a Weibull distribution with shape parameter k = 1/2 and scale parameter $\lambda = a_y \tau^2$. For particle motions over plane bed topography, quantile-quantile (Figure 5a) and histogram plots (Figure 5c) reveal that absolute lateral hop distances over plane bed topography are well approximated by the best fit Weibull distribution with fixed shape parameter k = 1/2.

Once again, we consider whether the proposed Weibull distribution can accurately quantify the first and second moments of measured lateral hop distances. This distribution implies that the mean absolute lateral hop distance is given by $\overline{|L_y|} = 2a_y \tau^2$, the variance is given by $\sigma_{|L_y|}^2 = 20a_y^2 \tau^4$, and the coefficient of variation is $\sqrt{5}$. Because the distribution of signed lateral hop distances is symmetric with mean equal to 0, the variance is equal to the raw variance of absolute lateral hop distances; that is, $\sigma_{L_y}^2 = \overline{|L_y|^2} = \overline{|L_y|^2} + \sigma_{|L_y|}^2$. The first and second moments that are relevant to macroscopic transport problems can be expressed in terms of distribution parameters as $\overline{L_y} = 0$ and $\sigma_{L_y}^2 = 24a_y^2 \tau^4$.

The empirical coefficient of variation for absolute lateral hop distances is 2.20, compared with 2.23 predicted from theory. For particle motions over bedform topography, the coefficient of variation in absolute lateral hop distances is 2.7, while the histogram plot (Figure 5d) reveals systematic deviations from predicted bin frequencies resulting in a concave-up relationship between theoretical and measured quantiles (Figure 5b). Again, this may indicate a heavy-tailed distribution of absolute lateral hop distances. If the distribution is not heavy tailed, then bedforms cause a significant increase in the variance of the signed lateral hop distances (0.27 cm² compared with 0.11 cm²), both by altering the shape of the distribution of absolute lateral hop distances and by increasing the average absolute lateral hop distance. This result primarily reflects an increase in the variability in transport direction as characterized by the coefficient of lateral transport (Table 1).



4.4. Bedload Diffusion

We have found that bedforms increase the variance of the ensemble probability distributions of streamwise and absolute lateral hop distances. Here, we consider the significance of this observation in the context of macroscopic transport equations under the assumption that these moments are in fact finite and well represented by our data. As noted previously, the Fokker-Planck approximation of the one-dimensional entrainment flux consists of three terms: a local advective term that represents the mean hop distance, a nonlocal advective term that squared the squared mean, and a diffusive term that represents the variance. These three terms are not guaranteed to map directly onto the typical advective and diffusive terms contained in the activity form of the flux (Furbish et al., 2012, 2017); thus, we refer to the sum of the first two terms as the advective-like flux and the third term as a diffusive-like flux.

Nonlocal advective-like and diffusive-like transport terms are 0 under steady, uniform transport conditions (Furbish et al., 2012). In order to compare the advective and diffusive behavior associated with a fixed distribution of particle hop distances, we consider a simple disequilibrium scenario in which the sediment flux varies due to a constant spatial gradient in the particle entrainment rate, $\partial E/\partial x = \beta$. In this case, the total flux is steady, varying only as a function of *x* and is given by

$$q_x(x) = E(x)\overline{L_x} - \frac{1}{2}\beta\overline{L_x}^2 - \frac{1}{2}\beta\sigma_{L_x}^2.$$
(9)

and the flux gradient is given by

$$\frac{\partial}{\partial x}q_x(x) = \beta \overline{L_x}$$
(10)

The diffusive flux is related to gradients in the advective flux by a diffusion length ℓ_{D_x} (Seizilles et al., 2014) as

$$q_{x_{\text{diffusive}}} = -\ell_{D_{x}} \frac{\partial}{\partial x} q_{x}(x).$$
(11)

For the simple disequilibrium conditions considered here, this diffusion length reduces to $\ell_{D_x} = \sigma_{L_x}^2 / \overline{L_x}$.

If hop distances are assumed to follow a Weibull distribution with shape parameter k = 1/2, the diffusion length is given by $\ell_{D_k} = 5\overline{L_w}$. The ratio of diffusion length to hop length $\ell_{D_k}/\overline{L_x}$ is like an inverse Peclet number in that it scales the relative propensity for diffusion-like and advection-like transport in the presence of gradients in particle entrainment rate. We recognize that the entrainment rate and the probability distributions of particle hop distance vary together in response to changes in boundary conditions; however, this mathematical abstraction is useful in that it enables a direct characterization of the effects of bedform development on particle diffusion.

For the plane bed experiment reported here, we find that measured distributions of particle hop distance lead to $\ell_{D_x} = 4.2L_x^-$. Thus, the Weibull distribution proposed by previous authors appropriately predicts the measured relationship between streamwise diffusion and streamwise advection for naturally sorted sediments transported over planar topography. In contrast, we find for the bedform condition that $\ell_{D_x} = 10.6L_x^-$, deviating significantly from theory.

Following similar arguments presented above but assuming a constant lateral gradient in particle entrainment rate $\partial E/\partial y$, it is straightforward to show that the lateral diffusive flux is related to the lateral gradient in the streamwise advective flux by a diffusion length $\ell_{D_y} = \sigma_{L_y}^2/\overline{L_x}$. Though we lack a clear basis for predicting the lateral diffusion length as we have done for the streamwise diffusion length above, we assume as a starting point that the lateral Peclet number is fixed over plane bed topography (as theory predicts for the streamwise Peclet number). For measured particle hop distances over plane bed topography, we find that $\ell_{D_y} = 1.07\overline{L_x}$. In contrast, particle motions in the bedform experiment have a lateral diffusion length of $\ell_{D_y} = 6.17\overline{L_x}$.

An important assumption in this analysis is that the distribution of particle hop distance is independent of the entrainment rate. Correlations between these variables cannot be evaluated using data reported here and may serve to enhance or diminish macroscopic diffusion. Nevertheless, bedform development appears to increase the propensity for streamwise and lateral diffusive transport quantified by an inverse Peclet number that is equal to the squared coefficient of variation (for streamwise diffusion) or the squared coefficient of lateral transport (for lateral diffusion). This difference cannot be explained by an increase in shear stress alone, which would likely cause an increase in the mean streamwise hop distance (Lajeunesse et al., 2010). Instead, bedform development results in a decrease of the mean streamwise hop distance with a concurrent increase of the variance of streamwise and lateral hop distances in our experiments. The notion that this difference is primarily caused by the development of bedform topography is entirely consistent with previously observed differences in particle behavior described by Wilson and Hay (2016), Leary and Schmeeckle (2017), Tsubaki et al. (2018), and Terwisscha van Scheltinga et al. (2019).

4.5. Experimental Censorship

We have interpreted these data as representative of the ensemble distribution of particle hop distances and travel times characteristic of macroscopic flow conditions. In principle, this requires an unbiased sample of particle motions representing all possible microconfigurations of flow, topography, and sediment transport. However, practical considerations limited the spatiotemporal extent over which it was possible to measure particle motions. This has two effects which could potentially influence our results.

The first effect is related to the fact that particles with longer hop distances and travel times are more likely to begin or end their motions outside of the measurement window. This effect causes a systematic reduction in the sample mean and variance relative to the true mean and variance because hops are censored at a rate that is proportional to their duration and length. In order to evaluate the importance of this effect, we performed the correction proposed by Ballio et al. (2019). This correction resulted in almost no change in estimates of the mean or variance in either of our experiments. Although this correction cannot account for all forms of censorship (e.g., truncation of the distribution), we are confident that our results are not substantially influenced by this effect.

The second effect concerns the fact that our sampling window is not large enough to capture a representative sample of particle motions originating from all possible microconfigurations of flow and topography characteristic of the macroscopic transport conditions. The importance of this effect cannot be evaluated directly from available data. Nevertheless, we argue that our data are sufficient to provide unequivocal support for the primary claims made in this paper. Observed differences in particle behavior are consistent with previous studies of particle motion over bedforms (e.g., Leary & Schmeeckle, 2017; Tsubaki et al., 2018; Wilson & Hay, 2016) and qualitative differences illustrated in Figure 1. Additionally, the mean lateral hop distance in the bedform experiment is approximately 0 (-0.028 cm) despite clear spatial correlations in lateral hop distance within the measurement window (Figure 1). Assuming the true mean lateral hop distance is 0, we tentatively interpret this as an indicator that the spatiotemporal extent of our measurement window is sufficiently large such that the measured statistics have begun to converge on the true ensemble statistics. By way of analogy, consider the problem of estimating the mean and variance of bed elevation in a stable bedform field. Measurements from a single bedform will provide reasonable first-order estimates of these quantities despite the fact that there is variability between bedforms (Nikora et al., 1997; Robert & Richards, 1988).

We argue that the primary findings of this paper concerning the forms of the distributions of particle hop distance and travel time over bedforms are robust to possible censorship effects. Increases in streamwise and lateral diffusivity are consistent with observations of particle motion reported by previous authors cannot be explained by censorship or sampling biases.

4.6. Limitations and Future Work

Our theoretical and experimental approach has several important limitations that must be addressed in order to extend the utility of our results to a wide range of macroscopic morphodynamic modeling problems. Here, we outline these limitations and provides suggestions for future studies focused on particle motions over bedforms.

The first limitation discussed in section 3.3 is that measured distributions of particle hop distance and travel time depend on the criterion used for differentiating between mobile and immobile particles. Bed elevation

is also defined with respect to the positions of particles in the immobile phase such that different criteria potentially lead to different descriptions of topography. We report results obtained using a mobility criterion that is consistent with previous work but ultimately subjective. Different criteria are valid as long as they obey mass conservation (i.e., mobile and immobile states encompass all particles and are mutually exclusive) and therefore provide alternative but compatible descriptions of sediment transport and morphodynamics. Recognizing this, the next step is to investigate how different choices of mobility criteria influence measured statistics of topography and particle motion. The morphodynamic interpretation of varying thresholds is similar to the scale-dependent active layer concept (Church & Haschenburger, 2017) and could potentially lead to valuable insights regarding interactions between fluctuations in bed elevation at the grain, bedform, bar, and channel scale (e.g., Nikora et al., 1997).

Another important issue is that the theoretical framework presented here is only valid for quasi-steady, uniform transport. In principle, this condition is satisfied if we consider macroscopic transport averaged over bedform-scale fluctuations (i.e., averaged over the bedform field timescale as envisioned by Furbish et al., 2012); however, an important caveat is that Equations 4 and 5 assume that the entrainment rate and hop distance are independent. This assumption is valid for planar topography because the entrainment rate is effectively uniform, but bedforms potentially introduce correlations between the entrainment rate and hop distance that can influence the macroscopic transport rate.

To clarify this point, consider that the entrainment rate may fluctuate under macroscopically steady, uniform boundary conditions when bedforms are present. In this case, the instantaneous entrainment rate may be viewed as a probabilistic quantity and the ensemble average flux (over all possible topographic configurations) is given by $q_x = \overline{EL_x}$. This becomes $q_x = EL_x$ if *E* is constant, or $q_x = \overline{E} L_x$ if *E* and L_x are independent. If they are not independent, the flux may be expressed in terms of a mean and deviatoric component as

$$q_x = \vec{E} L_x + \vec{E} L_x \tag{12}$$

where E' = E - E and $L'_x = L_x - L_x$. The second term in this expression is a covariance and can be rewritten as $\overline{E'L'_x} = \rho_{EL_x} \sigma_E \sigma_{L_x}$, where ρ_{El_x} is the correlation coefficient for the entrainment rate and hop distance, σ_E is the standard deviation of the entrainment rate, and σ_{L_x} is the standard deviation of the hop distance. The diffusive contribution to the flux under disequilibrium conditions may similarly be expanded in terms of mean and deviatoric components. This clarifies how correlations can influence the macroscopic transport rate and leads to several unanswered questions. First, are the entrainment rate and hop distance correlated over equilibrium mobile bedforms? Second, how does the correlation coefficient change under different conditions? Third, how do entrainment rate and hop distance vary within a statistically homogeneous bedform field as a function of local topography?

Because our experimental approach was aimed at quantifying the probability distribution of particle hop distance and travel time averaged over all possible topographic configurations, our results are limited in their capacity to elucidate the interaction between particle motion and bedform evolution at the granular scale. Nevertheless, our results clearly indicate that particle motions vary systematically in relation to topography. Future studies investigating this relationship may clarify (a) how morphodynamic feedbacks lead to a stable condition where the motion of individual particles perpetuates an statistically steady, uniform topographic configuration, and (b) how bedforms influence the advective and diffusive components of the flux under different flow conditions.

5. Conclusions

This paper presents results of an experimental study comparing the probability distributions that describe the spatiotemporal scales of particle motion linking particle entrainment and disentrainment events. Measured distributions of particle travel time, T_p , streamwise hop distance, L_{∞} and lateral hop distance, L_y , are compared with previously proposed theoretical distributions describing particle motions over plane bed topography. We confirm that particle motions over plane bed topography in natural sediments conform to existing theory. Travel times follow an exponential distribution while streamwise and absolute lateral hop distances follow a Weibull distribution with shape parameter k = 1/2.



In contrast, we find that particle hop distances over bedforms possess an increased standard deviation in both the streamwise and lateral directions relative to the mean streamwise hop distance. We argue that this effect is consistent with observations of particle motion over bedforms reported by previous authors; quantities like particle activity and velocity vary systematically in relation to topographic position. Topographically induced deviations from mean-particle behavior coupled with local flow velocity result in an additional source of variability that is superimposed on turbulent flow and particle collision effects. At the macroscopic scale, this means that the relative magnitudes of advective and diffusive-like transport implied by plane bed distributions cannot be assumed when bedforms are present. Instead, bedforms increase the propensity for streamwise and lateral diffusion-like transport.

Data Availability Statement

Data and code are available through Figshare (Ashley et al., 2019).

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