

Probing dark energy with baryonic oscillations and future radio surveys of neutral hydrogen

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ABSTRACT

Current surveys may be on the verge of measuring the baryonic oscillations in the galaxy power spectrum, which are clearly seen imprinted on the cosmic microwave background. It has recently been proposed that these oscillations allow a ‘standard ruler’ method of probing the equation of state of dark energy. In this paper we present a new calculation of the number of galaxies future radio telescopes will detect in surveys of the sky in neutral hydrogen (H I). We estimate the likely statistical errors if the standard ruler method were to be applied to such surveys. We emphasize uncertainties in our calculations, and pinpoint the most important features of future H I surveys if they are to provide new constraints on dark energy via baryonic oscillations. Designs of future radio telescopes are required to have a large bandwidth (characterized by β , the ratio of the instantaneous bandwidth to the bandwidth required by survey) and to have the widest instantaneous (1.4 GHz) field of view (FOV) possible. Given the expected sensitivity of a future Square Kilometre Array (SKA), given that half of its collecting area will be concentrated in a core of diameter ~ 5 km, and given a reasonable survey duration ($T_0 \sim 1$ yr), we show that there will be negligible shot noise on a power spectrum derived from H I galaxies out to redshift $z \simeq 1.5$. To access the largest cosmic volume possible by surveying all the sky available, we argue that β , T_0 and FOV must obey the relation $\beta \text{ FOV } T_0 \gtrsim 10 \text{ deg}^2 \text{ yr}$. A ~ 1 -yr SKA survey would then contain $\gtrsim 10^9 (f_{\text{sky}}/0.5)$ H I galaxies and provide constraints on the dark energy parameter w of order $\Delta w \simeq 0.01 (f_{\text{sky}}/0.5)^{-0.5}$, where f_{sky} is the fraction of the whole sky observed.

Key words: supernovae: general – cosmological parameters – large-scale structure of Universe – radio lines: general.

1 INTRODUCTION

We are now widely believed to have entered an era of precision cosmology (e.g. Percival et al. 2001; Spergel et al. 2003). It is therefore important that all new surveys, and all new equipment designed to make these surveys, are able to make precision measurements. These measurements should not only improve on the current constraints on the cosmological parameters but also begin to seriously constrain the equation of state of dark energy and its evolution with cosmic epoch. These constraints will eventually distinguish between a cosmological constant and other models for dark energy, such as quintessence (e.g. Carroll, Press & Turner 1992; Caldwell, Dave & Steinhardt 1998).

Recently, much effort has been expended to establish the best way of determining the properties of dark energy. Several methods have been proposed: the use of Type Ia supernovae to probe the luminosity distance (e.g. Weller & Albrecht 2002); the use of cluster number counts (Haiman, Mohr & Holder 2001) or counts of galaxies (New-

man & Davis 2000); weak gravitational lensing (Cooray & Huterer 1999); the Alcock–Paczynski test (Ballinger, Peacock & Heavens 1996); and the cosmic microwave background (CMB; e.g. Douspis et al. 2003). In this paper we examine one method in particular, the ‘standard ruler’ method based on baryonic oscillations (Eisenstein 2002), as several authors (Blake & Glazebrook 2003; Hu & Haiman 2003; Seo & Eisenstein 2003) have argued that it suffers from a set of systematic errors that are much less serious than those of the other methods.

We investigate here the role in dark energy studies of future radio surveys of neutral hydrogen (H I). Such surveys are likely to reach full fruition with the proposed next-generation radio synthesis array, the Square Kilometre Array (SKA; Carilli & Rawlings 2004).

In Section 2 we describe how we would be able to detect H I at high redshifts with future radio surveys. There are no direct observations of H I in emission in the high-redshift Universe as the current radio telescopes used to search for H I in emission are only sensitive enough to reach redshifts of around 0.2 (Zwaan, van Dokkum & Verheijen 2001). Nevertheless, we have evidence of large amounts of high-redshift H I through the damped-Ly α objects seen in absorption in quasar optical spectra (Storrie-Lombardi & Wolfe 2000;

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Peroux et al. 2001). In Section 3 we use this information to constrain possible evolutions of the H I mass function and to produce a new calculation of the number density of H I galaxies to be detected by future radio telescopes which improve on previous estimates (Briggs 1999; van der Hulst 1999). We compare our ‘best-guess’ evolutionary model with other observational constraints in Section 4; fitting formulae are given in Appendix A.

Having an estimate of what future radio surveys will be able to see in the 21-cm line of H I in emission, we can see what cosmological tests we can perform on such data and decide on their pros and cons. We focus here on probing dark energy with the baryonic oscillations method but other cosmological experiments are possible (see Blake et al. 2004; Rawlings et al. 2004). In Section 5 we show that, given the likely capabilities of future radio telescopes, the optimal survey would be an ‘all-hemisphere survey’ of all the sky area available. We then compute what comoving cosmological volume and numbers of sources are likely to be available in such surveys and we estimate the accuracy that the baryonic oscillations ‘standard ruler’ method (e.g. Blake & Glazebrook 2003; Hu & Haiman 2003; Seo & Eisenstein 2003) can give us in measuring the equation of state of dark energy; this is typically described by the parameter $w = p/\rho$ (Turner & White 1997), where p is the pressure and ρc^2 is the energy density of the dark energy component.

In Section 6 we discuss the uncertainties of our approach and discuss how they might influence the results of the standard ruler method used. We also discuss how the results would change if different assumptions are made for key features of the future radio surveys as well as some potential problems in using this method with future radio survey data.

For this paper we adopt the following cosmological values: $\Omega_M = 0.3$, $\Omega_\Lambda = 0.7$ and $h_{70} = 1$. We use the matter power spectrum given in Bardeen et al. (1986) with a normalization given by the *Wilkinson Microwave Anisotropy Probe* results (Spergel et al. 2003) which corresponds to $\sigma_8 \simeq 0.84$. For a given type of matter x we define Ω_x as being the ratio of the density of x to the critical density of the Universe today. When we refer to volumes, lengths, etc., we consider comoving cosmological values unless specified otherwise.

Unless stated otherwise, if we mention the field of view (FOV) of a radio telescope/array, we are referring to the instantaneous FOV this instrument possesses, and can image, at 1.4 GHz. It is vital to remember that for many radio telescopes the FOV that can be imaged becomes larger at lower frequencies.

2 PROSPECTS FOR FUTURE RADIO SURVEY OF H I

2.1 Sensitivity of radio receivers

The ratio of the signal to the noise power in a single-polarization radio receiver is

$$\frac{(1/2)A_{\text{eff}}S\Delta\nu}{kT_{\text{sys}}\Delta\nu} = \frac{A_{\text{eff}}S}{2kT_{\text{sys}}}, \quad (1)$$

where A_{eff} is the effective collective area of the telescope (incorporating all inefficiencies), S is the flux density, $\Delta\nu$ is the bandwidth and T_{sys} is the system temperature (incorporating all contributions).

In this paper we scale all limiting sensitivities to that expected for the SKA. The SKA science requirements (Jones 2004) demand $A_{\text{eff}}/T_{\text{sys}} = 2 \times 10^4 \text{ m}^2 \text{ K}^{-1}$ over the frequency range 0.5–5 GHz. As the discussions in this paper will be limited to H I at redshifts

$z \lesssim 2$ (i.e. frequencies in the range 0.5–1.4 GHz), this means that we can write the ‘radiometry equation’ for the SKA in a very simple form:

$$S_{\text{lim}} = \frac{2kT_{\text{sys}}}{A_{\text{eff}}\sqrt{2\Delta\nu t}} \simeq \frac{100 \text{ nJy}}{\sqrt{\Delta\nu t}}. \quad (2)$$

Here, S_{lim} is the rms sensitivity for dual-polarization observations with the SKA and the $\sqrt{2\Delta\nu t}$ term allows for the increase in sensitivity by averaging independent measurements of the signal-to-noise ratio.

2.2 Mass detection limit of H I

Neutral hydrogen (H I) will be found in emission with future radio surveys via the 21-cm line radiation due to the difference in energy in hyperfine atomic structure (e.g. Field 1958). From atomic physics we know that the emissivity is

$$\epsilon_\nu = \frac{1}{4\pi} h\nu_{12} A_{12} \frac{N_2}{N_H} N_H \varphi(\nu), \quad (3)$$

where ν_{12} and A_{12} are the rest-frame frequency and Einstein A coefficient for this transition, respectively, $\varphi(\nu)$ is the line profile of the 21-cm line, which is considered here as a delta function, and N_H and N_2 are the total number of hydrogen atoms, and number of atoms in the upper (level 2), respectively.

We can write $N_2/N_H = (N_2/N_1)/(N_1/N_H)$. The first ratio is given by $N_2/N_1 = (g_2/g_1) \exp(-h\nu_{12}/T_S)$, where N_1 is the number of atoms in level 1 and $g_1 = 1$ and $g_2 = 3$ are the statistical weights for these levels. T_S is the so-called spin temperature and is an effective temperature resulting from the coupling of the CMB temperature T_{CMB} and the kinetic temperature T_K of the gas. In the case of the CMB radiation alone, the spin temperature will equal the CMB temperature. If we have any collisional excitation or scattering by Ly α photons, the spin temperature will couple to the kinetic temperature as well as the CMB temperature and will therefore be a weighted average of both (Rohlfs & Wilson 1999). In cases we are considering here (dense clouds) we have both the kinetic temperature and the CMB temperature much larger than $h\nu_{12} = 0.06 \text{ K}$ and, given that $g_2/g_1 = 3$, we have $N_2/N_1 \simeq 3$.

Observations show that T_S can be as large as 300 K in low-redshift galaxies (Chengalur & Kanekar 2000) and that, in damped-Ly α objects at higher redshifts, limits on H I absorption lines imply larger values of T_S of the order of 1000 K or more (Kanekar & Chengalur 2003). If we are dealing with H I in emission, we will obtain the same signal whatever T_S ; however, the fact that the spin temperature is higher at higher redshifts is telling us that we are probably probing a different type of interstellar medium. At high redshift we are typically probing a warm neutral intergalactic medium that is present in larger fraction in smaller less dense dark matter haloes (Young & Knezek 1989). We can safely say that in all cases of our interest $N_2/N_H \simeq 3/4$.

If we consider a cloud of hydrogen, the monochromatic luminosity we would obtain from this 21-cm line emission will be

$$L_\nu = \int_V \int_\Omega \epsilon_\nu dV d\Omega = \frac{3}{4} h\nu A_{12} \frac{M_{\text{H I}}}{m_H} \varphi(\nu). \quad (4)$$

So, given the expression for the monochromatic flux density $S_\nu = L_{\nu(1+z)}/[4\pi D_L^2(z)]$ (Peacock 1999; equation 3.87), where $D_L(z)$ is the luminosity distance to the galaxy, we can integrate equation (4) over frequency to obtain

$$\int S_\nu d\nu = \frac{1}{4\pi} \frac{3}{4} h A_{12} \frac{M_{\text{H I}}}{m_H} \frac{1+z}{D_L^2(z)} \int \nu \varphi(\nu) d\nu. \quad (5)$$

Therefore, we obtain the expression for the mass corresponding to the flux seen in our observations

$$M_{\text{H I}}(z) = \frac{16\pi}{3} \frac{m_{\text{H}}}{A_{12}hc} \frac{D_L^2(z)}{1+z} \int S_\nu dV, \quad (6)$$

where the integral is now over V , the line-of-sight width corresponding to the projected circular velocity of the galaxy. In more useful units

$$\frac{M_{\text{H I}}(z)}{M_\odot} = \frac{0.235}{1+z} \frac{D_L^2(z)}{\text{Mpc}^2} \frac{S_\nu}{\nu \text{Jy}} \frac{V}{\text{km s}^{-1}}, \quad (7)$$

noting that the factor of $(1+z)$ arises as $S_\nu V$ needs to be multiplied by $v_{12}/(1+z)$ to produce an integrated line flux.

We have neglected H I self-absorption effects, which means that the H I mass may be a slight underestimate, but this is likely to be a problem only when the discs of the largest galaxies seen close to edge on (Rao, Turnshek & Briggs 1995).

2.3 Sensitivity limits of future radio surveys

The H I Parkes All-Sky Survey (HIPASS; Ryan-Weber et al. 2002) used channels of velocity width $\Delta V = 13 \text{ km s}^{-1}$ and was capable of detecting typical galaxies out to $z \simeq 0.02$. It is important that the ΔV chosen for an H I survey is not larger than the velocity width of the object being observed, because this would result in both the loss of signal-to-noise ratio and the danger of mistaking signal for interference. The HIPASS does not show any evidence that many sources have low-velocity width and the very lowest velocities found are around 30 km s^{-1} . These widths might change systematically with redshift. Zwaan et al. (2001) have detected an example of an H I-rich cloud at $z = 0.18$ with a velocity profile of width $V = 60 \text{ km s}^{-1}$. We take $\Delta V = 30 \text{ km s}^{-1}$ but caution that even finer velocity bins may prove necessary to avoid losing signal-to-noise ratio on the narrowest-line objects, particularly if linewidth correlates negatively with redshift. The current ‘Strawman design’ for the SKA (Jones 2004) suggests that channels of width $\Delta V \simeq 30 \text{ km s}^{-1}$ will be available. We assume throughout that H I lines are detected and measured using optimal smoothing techniques.

In the standard picture of galaxy formation (e.g. Rees & Ostriker 1977; White & Rees 1978), we expect dark matter haloes to form potential wells, with gas falling into these potential wells becoming shock heated to the virial temperature. Cooling can then occur if the free-fall time-scale is longer than the cooling time-scale. Dekel & Silk (1986) have shown that the objects that can cool have circular velocities between 10 and 200 km s^{-1} . Further to this, it is argued that objects with circular velocity between 10 and 30 km s^{-1} are likely to be totally dark as their potential wells are so shallow that the cold gas will disappear by evaporation due to photoionization (Dekel 2004). These theoretical arguments lead us to perform our calculations with an assumed $\Delta V = 30 \text{ km s}^{-1}$, which means that only objects with the lowest circular velocities and with nearly face-on rotating discs will have H I line profiles with $V \lesssim \Delta V$.

In every $\Delta V = 30 \text{ km s}^{-1}$ channel there will be a rms noise that will be dependent on frequency ν , estimated for the SKA to be $\sim 2 \mu\text{Jy}$ at $\nu = 1.4 \text{ GHz}$ (H I at $z = 0$) to $\sim 4 \mu\text{Jy}$ at $\nu = 470 \text{ MHz}$ (H I at $z \simeq 2$) for a 4-h pointed observation. We denote this noise by σ_{4h} .

We assume that the average hydrogen-rich galaxy has a rectangular line-of-sight velocity spread $V_0 = 300 \text{ km s}^{-1}$ (which corresponds to a circular velocity of around 200 km s^{-1}) at $z = 0$ and we also assume a ‘Tully–Fisher-like’ relationship $V^4 \propto M_{\text{DM}}^2/R_0^2$ (Peacock 1999, p. 622) that would hold at higher redshift, where M_{DM} is the dark matter mass of the galaxy and R_0 is the galaxy

radius. The evolution we choose for M_{DM} and R_0 with redshift is explained in Section 3.2, and this will impose a corresponding scaling of V with z ; this choice will in fact force the linewidth to correlate negatively with redshift [as $V(z) = V_0(1+z)^{-1/2}$] although the physical lower limit of 30 km s^{-1} proposed by Dekel (2004) should mean that this cannot decrease without limit for haloes containing H I. Then, the limiting H I mass that a radio survey will be able to detect at redshift z is

$$M_{\text{H I}}(z) = \frac{16\pi}{3} \frac{m_{\text{H}}}{A_{12}hc} \frac{D_L^2(z)}{1+z} f^{-1} \frac{V(z)}{\sqrt{V(z)/\Delta V}} S_N \sigma_{4h} \sqrt{\frac{4}{t}}. \quad (8)$$

Here, S_N is the signal-to-noise level we choose to yield a robust detection, t is the integration time in h for a given FOV and f is the fraction of the sensitivity relative to the SKA; by definition $f = 1$ for the SKA, and current radio telescopes have $f \lesssim 0.01$.

2.4 Survey geometry

Currently, the ‘Strawman design’ for the SKA (Jones 2004) has a FOV of at least 1 deg^2 . For most realizations of an SKA, the FOV will be much larger at frequencies smaller than 1.4 GHz , which will correspond to H I at redshifts larger than $z \simeq 0$. In fact, the FOV, in units of deg^2 , will typically, because it is controlled by the diffraction limit of a dish) grow as $(1+z)^2$ if we are probing H I at increasing redshift. In Section 5 we consider future telescopes where the FOV for H I galaxies may vary with a different power of the frequency/redshift.

So, let us consider for illustrative purposes that we have a square beam and that we would like to cover a square sky patch of 64 deg^2 with an integration time of 8 h per deg^2 . If we simply point the telescope 64 times at each square that we will name A1, A2, . . . H7, H8, then we will have covered the sky smoothly at $z = 0$, but the data at $z = 0.5$ will have parts of the sky that will have a higher sensitivity than others. This would be an undesired feature in the data for the purposes of making a uniform survey of H I.

In order to deal with this, we consider the following. Instead of pointing the telescope at each of A1, A2, . . . , we take data n times in between A1 and A2 with $1/n$ th of the total time we would have spent on each of A1 and A2. We can then take the data that we receive from each small pointing and add it to the data available from other pointings. We end up with a survey with increasing sensitivity for increasing redshifts because a source at higher redshift will be accessible to a larger fraction of the pointings and will therefore have a longer effective integration time for higher-redshift objects. In fact, the effective integration time for such a ‘tiled’ survey will increase smoothly as $(1+z)^2$ for a given integration time at $z = 0$. Ideally we would like to have a very smooth survey, but in practice it may not be possible to obtain maps with very large n because of limited computing capabilities. The wiggles on the power spectrum are at intervals of $\sim 0.05 \text{ Mpc}^{-1}$ so the survey needs to have a smooth window function even on scales corresponding to $k \sim 0.01 \text{ Mpc}^{-1}$. If this is not the case, the wiggles will be smoothed out by correlated errors on the power spectrum estimation (see Blake & Glazebrook 2003). Thus, for the purposes of this experiment we would like to have a smooth sky map on sizes of $\gtrsim 600 \text{ Mpc}$. The choice of $n \gtrsim 10$ would ensure that smoothness is achieved on scales of the same size as the wiggles at the redshifts ($z \sim 1$) of interest. We also would not have excessive data storage requirements as the integration time would be of the order of minutes similar to those used in current radio surveys. More complicated survey schemes will be needed with interferometric arrays to ensure optimal ultraviolet coverage.

So, for a given time of survey per deg^2 the limiting mass that the SKA will be able to see is

$$M_{\text{HI}}(z) = \frac{16\pi}{3} \frac{m_{\text{H}}}{A_{12}hc} \frac{D_L^2(z)}{(1+z)^{1+p}} f^{-1} \sqrt{V(z)\Delta V} S_{\text{N}}\sigma_{4\text{h}} \sqrt{\frac{4}{t}}, \quad (9)$$

where we have assumed that all redshifts are accessible by a single pointing and where p is defined by the FOV changing with frequency ν as ν^{-2p} (i.e. for a ν^{-2} dependence we have $p = 1$).

As we are covering a certain patch of the sky, the centre of this patch will have the sensitivity given by equation (9), but the corners of the survey will have lower sensitivities as the beam will not have covered those areas as often as those in the centre. This will be the case for most of the survey area if we are looking at a small patch of the sky, but if we are performing a large survey, then this area with smaller sensitivity will be a small fraction of the total area of the survey, and can be neglected. We show in Section 5 that the optimal survey for this experiment is an all-sky survey, so this effect should therefore be negligible.

The assumption that the FOV changes with redshift will make a big difference to the total cosmic volume being surveyed in a given length of time, and this assumption is relaxed in Section 5 where we consider different values of p .

2.5 Source count

We consider the local mass function of H I (Zwaan et al. 2003) $dn/d\log_{10}M_{\text{HI}}$ in units of Mpc^{-3} . The number of sources viewed assuming that this mass function is constant in z will be

$$\frac{dN}{dz} = \int_{M_{\text{HI}}(z)}^{\infty} \frac{dn}{d\log_{10}M_{\text{HI}}} \frac{dV}{dz} d\log_{10}M_{\text{HI}}, \quad (10)$$

where $M_{\text{HI}}(z)$ is the limiting mass that can be detected; this quantity is plotted in Fig. 1 in which the gain in sensitivity at high redshifts from a ‘tiled’ survey is made clear.

However, this assumes that the H I mass function is constant throughout all redshifts, which is clearly very unlikely to be correct as neutral hydrogen is constantly being used in star formation,

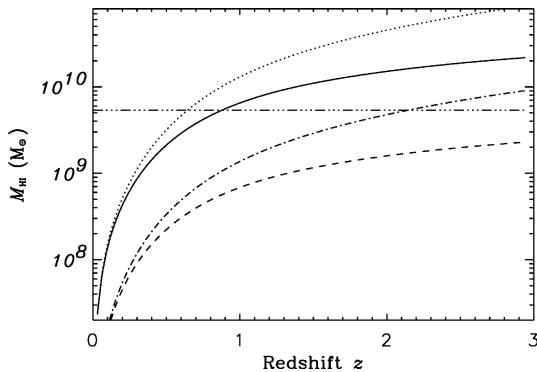


Figure 1. Limiting H I mass M_{HI} for surveys with an SKA-like instrument for a signal-to-noise (S_{N}) ratio of 10 in a 4-h integration time (solid and dotted lines) and a 360-h integration time (dot-dashed and dashed lines); the mass is in units of M_{\odot} . The dotted and dot-dashed lines assume pointed observations and the solid and dashed lines assume tiled surveys as discussed in Section 2.4. The horizontal line corresponds to the break of the H I mass function M_{HI}^* at low redshifts from Zwaan et al. (2003). We can see how an SKA 360-h integration time can take us very deep in z , but a simple 4-h SKA integration time is enough to detect an M_{HI}^* galaxy (assuming no evolution in the break of the H I mass function) out to redshift $z \sim 1$. This is for an array that has an effective FOV scaling with frequency ν as ν^{-2} (see Sections 2.2 and 2.3).

ionized in processes such as supernovae explosions as well as being created in processes such as cooling flows (e.g. White & Frenk 1991). We therefore have to try and see how this H I mass function evolves with redshift to have a clearer idea of what number density will be accessible by surveys with next-generation radio telescopes. This is the purpose of Section 3 where we assume that the H I observed traces collapsed dark matter haloes.

2.6 Source visibility for an interferometer

In the previous sections we have assumed that a source in the sky has a flux that will be detected perfectly by the radio telescope. This is not the case if the survey is carried out with an interferometer. Because the output of the correlator observing an extended radio source on certain baselines does not recover the total flux density, we only recover the ‘correlated flux density’, which is the modulus of the complex visibility of each baseline.

Here we estimate the signal that we lose if we perform such surveys with an interferometer. We assume that our average galaxy has a physical radius $R_0 = 15$ kpc at redshift 0. We assume that the dark matter mass of a typical galaxy halo changes as $M_{\text{DM}}^*(z)$ according to the hierarchical growth of haloes (Press & Schechter 1974) and that the characteristic density ρ of a halo changes as $\rho \propto (1+z)^3$; that is, the density of the collapsed galaxy changes in the same way as the background density of dark matter. In the standard picture of disc formation (e.g. Peebles 1969; Fall & Efstathiou 1980) we expect the disc of a galaxy to be a factor of λ smaller than the radius of the dark matter halo, where λ is the spin parameter and can be taken as a constant (Efstathiou & Jones 1979). Now given that $M_{\text{DM}}(z) \simeq \rho(z) R^3(z)/R_0^3$ we can approximate the proper radius of an average galaxy as

$$R(z) \simeq R_0 \left[\frac{M_{\text{DM}}^*(z)}{M_{\text{DM}}^*(0)} \right]^{1/3} \frac{1}{1+z}, \quad (11)$$

where our choice of $M_{\text{DM}}^*(z) \propto (1+z)^{-3}$ is explained in Section 3.2. This will impose an evolution of the characteristic sizes of discs with redshift that is proportional to $(1+z)^{-2}$; this is in rough agreement with observations of disc sizes from the *Hubble Deep Field* (e.g. Poli et al. 1999; Giallongo et al. 2000). Other prescriptions for the evolution of the disc sizes could have been used (e.g. Ferguson 2003) but this would not have made a large difference to our calculations. We use a characteristic size scale for an H I disc in a galaxy at the break of the H I mass function at redshift $z = 0$ of $R_0 = 15$ kpc (Salpeter & Hoffman 1996).

We assume that the galaxy has a surface brightness that corresponds to a two-dimensional Gaussian profile with angular spread equal to $R(z)/D_{\text{A}}(z)$ in radians, where $D_{\text{A}}(z)$ is the angular diameter distance to the galaxy. The Fourier transform of this Gaussian will be the complex visibility of each baseline. The spread of this Fourier transform is

$$D_{\text{baseline}} \sim \frac{c}{\nu_{12}} (1+z) D_{\text{A}}(z) \frac{1}{\pi R(z)}, \quad (12)$$

so each antenna, when correlated with other antennas, will only be sensitive to a fraction of the total flux of the source, depending on the baseline.

Obviously we need to assume a certain configuration for the antennas. We adopt a composite array (see Jones 2004) in which the interferometer will be configured with 20 per cent of the collecting area inside a diameter of ~ 1 km, 50 per cent of the collecting area within a diameter of ~ 5 km, 75 per cent of the collecting area within a diameter of ~ 150 km and the final

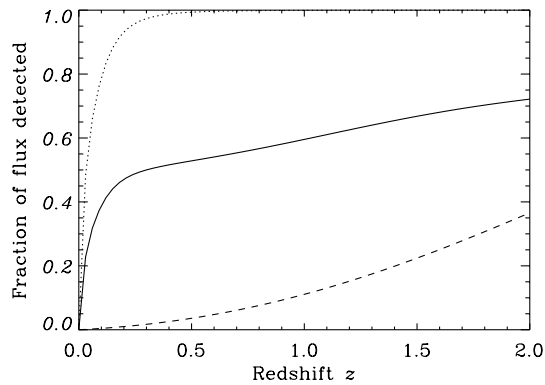


Figure 2. The fraction of flux detected from an extended model galaxy by an SKA-like interferometer as a function of redshift for different array distributions. The dashed line assumes a scale-free array, the dotted line assumes an array with just a core, and the solid line assumes the composite array as described in Section 2.6.

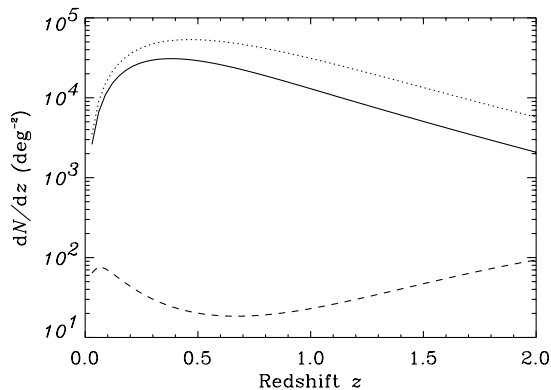


Figure 3. Differential number density dN/dz of sources per deg^2 if we assume a fixed SKA-like sensitivity, a 4-h integration time, a 10σ detection limit and no evolution of the H I mass function (although galaxy radii are assumed to change with redshift in the way described by equation 11). Three choices of antenna distributions are considered: (i) a simple scale-free array with resolution 0.1 arcsec at 1.4 GHz (Conway 1998) (dashed line); (ii) a core only (dotted line); (iii) the composite array described in Section 2.6 (solid line). Performing H I surveys with an array having a large fraction of the collecting area in short baselines is vital as many sources are resolved out by the longer baselines.

25 per cent spread over a diameter of 3000 km in a scale-free configuration (Conway 1998).

We illustrate how much the configuration affects the fraction of the flux detected by plotting the number of sources seen with different configurations (Figs 2 and 3). The fraction of flux detected from sources improves rapidly as the source moves to larger redshift and has smaller angular size, and is therefore visible to a greater fraction of the interferometer baselines. As seen in Fig. 3 it is vital that a large fraction of the collecting area is in short baselines so that we do not ‘resolve out’ extended sources and miss most of the H I galaxies in a survey.

2.7 Survey completeness limit

If we perform a survey and take data out to redshift $z \sim 1.5$ we would need to cover frequencies from 1.4 GHz down to 560 MHz; with channels of width 30 km s^{-1} , we would have data in roughly 10 000 channels. A survey over half of the sky at a resolution corresponding to $\simeq 1$ arcsec would have about $20\,000 \text{ deg}^2$, so we therefore would

have around 10^{11} pixels in the sky. Our survey would therefore have around 10^{15} pixels in three dimensions. We would therefore require a 8σ catalogue in order not to have any spurious sources if the noise was perfectly Gaussian.

Nevertheless, we expect to find sources of noise that will not be so well behaved. We therefore adopt a signal-to-noise level of 10σ for our calculations. In this way, we can be reasonably confident that our catalogue will be largely free of spurious sources.

We note that the HIPASS Bright Galaxy Catalogue (BGC; Ryan-Weber et al. 2002) is a 9σ catalogue, and the number of pixels, in three dimensions, in their survey is only $\sim 10^8$, given that they perform a survey out to $13\,000 \text{ km s}^{-1}$, have a resolution of around 13 km s^{-1} and survey half the sky with a resolution of the order of 15 arcmin. We therefore conclude that depending on the sources of systematic errors, it might be necessary in a real survey to have a much higher detection level if we want the catalogue to be free of spurious sources (possibly higher than 10σ). We stress that such a change would not affect our results significantly.

3 POSSIBLE EVOLUTION OF THE H I MASS FUNCTION

3.1 Information from damped- $\text{Ly}\alpha$ systems

The number density of H I sources we will be able to detect will be a direct function of the evolution of the mass function of neutral hydrogen. If we are able to construct a reasonable model that would predict this mass function at high redshift, we would be able to have a good estimate of the number of sources that will be detected.

If we perform an H I survey out to cosmological redshifts, we will be sensitive mainly to objects near the break of the mass function. In the following sections we use scaling relations according to the properties of such galaxies (i.e. we assume that the population at all redshifts have such properties). We estimate the H I mass function at high redshifts but we are not too concerned if the low-mass objects are not correctly described.

In order to calculate the H I mass function at higher redshifts, we use damped- $\text{Ly}\alpha$ results as a probe. The current sensitivity of radio telescopes limits the detection of H I in emission to only $z \simeq 0.2$ (Zwaan et al. 2001), so we can only probe high- z objects in absorption. The damped- $\text{Ly}\alpha$ systems give us a distribution of the number density of objects as a function of the column density as well as the total $\Omega_{\text{HI}}(z)$ at each redshift. One might think that by looking at the distribution of column densities at high redshift we could find the distribution in mass at high z . There is indeed a correlation between high column density and high mass but the scatter is extremely large (Ryan-Weber et al. 2002) because small clouds with not much H I can have lines of sight passing through their dense cores giving a high column density and H I-rich galaxies can have lines of sight passing through their low-column-density regions. We cannot obtain directly a mass function from the distributions in column density, but we argue that the highest column densities are mainly in collapsed structures (see Section 4), and they account for most of the mass of neutral hydrogen (Proulx et al. 2001). The total density of neutral gas at high redshift is the vital information that damped- $\text{Ly}\alpha$ systems give us, and this of course directly constrains the H I-mass-weighted area under the H I mass function.

3.2 Possible evolution of the H I mass function

We assume that the mass function of H I can be described as a Schechter function at higher redshifts and that all the hydrogen

seen in damped-Ly α systems is in collapsed haloes at high redshift (see Section 4). It is not known whether this assumption is valid at higher redshifts, but we are confident that this is a reasonable approximation at least up to the redshifts in which we are interested. We therefore have three parameters to determine at every redshift: the normalization θ^* , the faint-end slope α and the break of the mass function M_{HI}^* .

All our calculations use the redshift-zero H I mass function measured by the HIPASS team (Zwaan et al. 2003). In their paper they parametrize the H I mass function by a Schechter function

$$\frac{dn}{d(M_{\text{HI}}/M_{\text{HI}}^*)} = \theta^* \left(\frac{M_{\text{HI}}}{M_{\text{HI}}^*} \right)^\alpha \exp \left(-\frac{M_{\text{HI}}}{M_{\text{HI}}^*} \right), \quad (13)$$

where $\alpha = -1.3$, $M_{\text{HI}}^* = 10^{9.48} M_\odot$ and $\theta^* = 0.025 \text{ Mpc}^{-3}$ (Zwaan et al. 2003). We assume that the faint-end slope will not play a big role in determining the number of sources to be seen. We keep this value constant and equal to the value ($\alpha = -1.3$) seen at $z = 0$.

The value of the normalization is set according to the amount of gas found at redshift z following the results from damped-Ly α observations (Proulx et al. 2001); we assume that the neutral gas in these damped-Ly α clouds is in collapsed objects. The integral of the H I mass times the H I mass function equals the total density of neutral gas and is given by damped-Ly α results (see equation 14). Nevertheless, recent results show that if we could select quasars in the radio we might infer a higher amount of H I because there might be an obscuration selection effect in finding neutral gas via damped systems selected in the optical (Ellison et al. 2001). We therefore multiply the Proulx et al. (2001) results by a small factor (namely 1.5; Ellison et al. 2001) to account for this potential selection effect. We then fit a function to force the normalization of our H I mass function to account for the amount of gas that must be present at that redshift; this is done by forcing the integral under the H I mass function (weighted by M_{HI}) to equal that measured by the damped-Ly α results. We point out here that we have ignored the weak constraints on Ω_{HI} from Rao & Turnshek (2000) who predicted a larger amount of neutral gas at $z < 1.65$ on the basis of objects selected via Mg II absorption and followed up with the *Hubble Space Telescope* (HST) to obtain damped-Ly α measurements. Their constraints are uncertain because of small number statistics, but also because there are numerous systematic effects that may not yet have been completely understood (Rao & Turnshek 2000). From Proulx et al. (2001) we have

$$\Omega_{\text{HI}}(z) = \frac{1}{\rho_c} \int_{-\infty}^{\infty} M_{\text{HI}} \frac{dn}{d \log_{10} M_{\text{HI}}} (z) d \log_{10} M_{\text{HI}}, \quad (14)$$

which leads to

$$\Omega_{\text{HI}}(z) = \theta^*(z) \Gamma(2 + \alpha) M_{\text{HI}}^*(z) / \rho_c, \quad (15)$$

where Γ is the gamma function and ρ_c is the critical density of the Universe; we have used the Schechter function as the form of the H I mass function.

The only thing left to choose is how the break of this mass function will evolve in cosmic time. This is not well constrained by current data and can make a significant difference to our results. If we adopt the standard hierarchical formation scenario, where smaller objects merge to produce bigger objects, one would naively expect that this break would shift to lower masses at higher redshifts. Nevertheless, the problem is not so simple. There are many other processes that may lead to the opposite result. For example, if star formation is more efficient in hydrogen-rich objects, then they will tend to form

stars at a higher rate than their lower-mass counterparts. In this case, if star formation is the main process, the break could shift towards higher H I masses at higher redshifts.

A complete theory of galaxy formation would be able to give us the answer to this problem. We do not however possess such a theory. We therefore will make three extreme choices for the change in the break. In model A, we consider a break that remains constant throughout all redshifts. In model B, we consider the case where $M_{\text{HI}} \propto M_{\text{DM}}$; in this choice we are assuming that the H I follows a hierarchical formation in the same way as dark matter clusters. In this model B, we use the fact that the Press–Schechter mass function (Press & Schechter 1974) is roughly self-similar in $\nu = \delta_c / [\sigma(M) D(z)]$ (Jenkins et al. 2001) where $\sigma^2(M)$ is the variance of the density field (at $z = 0$) smoothed over a cosmic volume corresponding to mass M , $D(z)$ is the linear growth factor and $\delta_c \simeq 1.67$ is the linear theory threshold for collapse (Lokas & Hoffman 2001). If we consider a change such that $\sigma(M) D(z)$ remains constant, we can see how a characteristic mass of dark matter changes with redshift. In fact, $\sigma(M) \simeq M^{-(n+3)/6}$ where n is the slope of the power spectrum at the scales of interest. We choose $n \simeq -1$ because this is appropriate for galaxy scales (Peacock 1999, p. 499). We can roughly say that $M_{\text{DM}} \propto D^3(z) \simeq (1+z)^{-3}$ in this model. With this choice, the scaling of the average radius of a disc with redshift according to equation (11) would be roughly $R(z) \simeq R_0 (1+z)^{-2}$, a scaling of galaxy sizes with redshift that is often simply assumed (e.g. Silk & Bouwens 1999).

The assumption that $M_{\text{HI}} \propto M_{\text{DM}}$ is not the most physically reasonable assumption we could make. In fact, model B is an extreme case, the function of which is only to provide a limit to our predictions. The main reason for this is that this model neglects the effects of star formation over a range of cosmic epochs. However, we also know that this assumption must break down in high-mass haloes (e.g. rich clusters) where the ratio of M_{HI} to M_{DM} is much lower than in galaxies (Battye, Davis & Weller 2004). This is due, at least in part, to the long-established fact that the mass-to-light ratio is larger in the most massive haloes due to long cooling time-scales, but it may also reflect a reduction in neutral content once galaxies become subhaloes of a larger dark matter halo (e.g. Zwaan et al. 2001). In extrapolating correctly to high redshift, we would need to account for times when these subhaloes were distinct haloes; this would make the location of the break of the H I mass function move to lower masses less rapidly than model B.

In model C, we consider the case where $M_{\text{baryons}} \propto M_{\text{DM}}$. Once more, this neglects the subhalo problem but it does attempt to take account of the star formation. We assume that outflows will reduce the fraction of baryons in a galaxy but accretion will bring the fraction back close to the nucleosynthesis value or some relatively fixed value of it (Silk 2003); a steady state between these two processes would bring the ratio of baryons to dark matter to a constant value. In this case we can say that

$$M_{\text{HI}} \propto \frac{\Omega_{\text{HI}}(z)}{\Omega_{\text{stars}}(z) + \Omega_{\text{HI}}(z) + \Omega_{\text{H}_2}(z)} M_{\text{DM}},$$

where $\Omega_{\text{stars}}(z)$ is given by

$$\Omega_{\text{stars}}(z) = \frac{1}{\rho_c} \int_z^\infty \frac{\dot{\rho}_{\text{stars}}(z)}{H(z)(1+z)} dz, \quad (16)$$

and where the star formation rate (SFR) $\dot{\rho}_{\text{stars}}(z)$ as a function of cosmic time is taken from Choudhury & Padmanabhan (2002) and corrected to the cosmology we use here [$H(z)$ is the Hubble Constant at redshift z]. The choice of Ω_{H_2} is more complex. From Young &

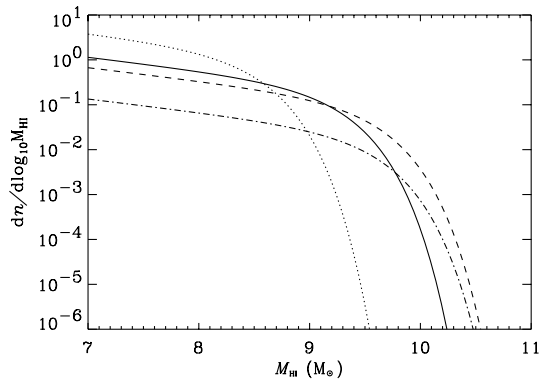


Figure 4. The H I mass function plotted at redshift $z = 2$ for models A (dashed line), B (dotted line) and C (solid line). We also plot the Schechter function fit to the measured H I mass function at $z = 0$ (dot-dashed line). Measurements of the total density of H I in the high- z Universe from observations of damped-Ly α systems (Section 3.1) fix the area, in an H I mass-weighted sense, under the curves for models A, B and C, but the existing observational data are insufficient to establish the evolution of the location of the break in the H I mass function.

Knezeck (1989) we know that the ratio of molecular hydrogen (H_2) to neutral hydrogen (H I) is a function of the galaxy type varying by a factor of ~ 20 depending on type. However, Young & Knezeck argued that the largest ratios ($M_{H_2}/M_{H I} \sim 4$) are found in the most massive galaxies with deepest potential wells that correspond to dense stellar cores with low spin temperatures. Less massive galaxies have a smaller proportion of molecular hydrogen ($M_{H_2}/M_{H I} \sim 0.2$) and have less dense cores with high spin temperature. We cannot implement this in a completely consistent way in our model C, so we decide to choose a ratio so that $\Omega_{H I}(z) = \Omega_{H_2}(z)$, which is consistent with the local baryon budget (Fukugita, Hogan & Peebles 1998). We also neglect the ionized fraction of gas in a galaxy, i.e. ($\Omega_{H II} \simeq 0$), which is a reasonable assumption for collapsed galaxy-sized haloes (Fukugita et al. 1998). In model C the break of the H I mass function will still shift toward smaller H I masses at higher redshifts, but more slowly than model B as it takes into account the fact that galaxies at higher redshifts have more gas and less stars. In Fig. 4 we plot the H I mass function at redshift $z = 2$ for models A, B, C and no-evolution.

3.3 Limits on the number count

We plot in Fig. 5 the differential number density dN/dz of objects seen, per deg^2 , by a future SKA-like telescope for our models A, B and C; we also plot the number density with an H I mass function that does not evolve with redshift. We can see that the evidence from damped-Ly α systems for more H I in collapsed objects (Section 3.1) predicts a larger number density of H I-emitting objects.

We also see that considering a different break in the H I mass function makes some difference to the amount of objects seen. Even though we tried to choose very different possible alternatives, we see that there is not a huge difference in the total number of H I sources. There are two reasons for this. First, if we consider a change in the position of the break of the H I mass function and still consider that the total H I mass is the same at a given redshift, the model with a lower break will have many more low-mass objects to account for the same mass at that redshift. If we have a survey that has enough sensitivity to reach those masses, we will see those objects. Secondly, the change in the break becomes significant only

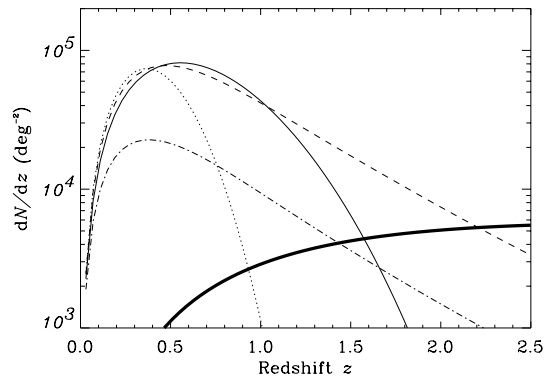


Figure 5. The differential number density (dN/dz) per deg^2 of objects in an SKA-like survey with a signal-to-noise detection level of 10, and an integration time of 4 h in a tiled survey for our three evolution models – models A (dashed), B (dotted) and C (solid) – plus a no-evolution model (dot-dashed). The integral under these curves represents the total number of H I emitting objects per deg^2 , which are 8.0×10^4 , 6.5×10^4 , 2.0×10^4 and 3.5×10^4 , for models A, B, C and the no-evolution model, respectively. We note that we assume more neutral gas at higher redshifts in the three evolution models, so the number of H I sources in these models increases; depending on the choice of break in the H I mass function, the models probe out to different redshifts. The thick line defines the number density of objects needed at high redshift in order for us to be cosmic variance limited when reconstructing the galaxy power spectrum (see Section 5.2).

at higher redshifts and these redshifts are probed at longer integration times. We can therefore say that for low integration times the total number of H I sources is uncertain to a factor of only ~ 2 (see Fig. 5).

Although different breaks in the H I mass function give roughly the same amount of sources, they yield surveys probing significantly different volumes in space. We define the depth of our survey (z_{max}) carefully in Section 5.2, but we can already see (Fig. 5) that, for a 4-h integration time, model A probes redshifts as high as 2.1, whereas model B only probes redshifts as high as 1.0. Model C, chosen to have a break between the breaks for models A and B, probes out to redshift 1.5.

Our preferred model in the next sections is model C. In Section 6 we quantify how much longer or shorter a survey will take if the H I mass function is closer to models A or B (or if we have an evolution that mimics the no-evolution scenario) instead of model C in order to obtain the same cosmological constraints on w .

4 OTHER CONSTRAINTS ON THE EVOLUTION OF THE H I MASS FUNCTION

In Section 3 we tried to see how the H I mass function could change with redshift. We stress here that we are only concerned whether the objects near the break of this mass function are well described, as they are the ones that will dominate future surveys at the redshifts of interest. We have assumed that an average galaxy at $z = 0$ has a radius of ~ 15 kpc and a circular velocity of 200 km s^{-1} . We have also assumed scaling relations that describe their behaviour at higher redshift. We have assumed no scatter on these relations.

To obtain an expression for the normalization of the mass function we have assumed in Section 3.2 that damped-Ly α systems are collapsed objects with radii of the same size as galaxies at the redshifts they are observed. If we assume that the path-length through the

absorber is roughly $l \simeq N_{\text{HI}}/n_{\text{HI}}$ where N_{HI} is the column density and n_{HI} is the H I number density and f_c is the ratio of the density in baryons in a collapsed halo to the universal density of baryons (e.g. from nucleosynthesis), we have $l/\text{kpc} = 109 (N_{\text{HI}}/10^{23} \text{ m}^{-2}) (f_c/180)^{-1} (1+z)^{-3}$ (Peacock 1999, p. 365). This means that the most extreme damped systems ($N_{\text{HI}} \sim 10^{24} \text{ m}^{-2}$) are consistent with having the dimensions of galactic discs; at $z = 1$, the damped systems would have radii of around 1–10 kpc. This is not the case for much lower column density systems. Nevertheless, the total mass obtained by integrating the damped-Ly α systems over column density is mainly due to high column density objects (Proulx et al. 2001), i.e. those that are most likely to be collapsed and to have the sizes of galactic discs.

When a blind H I survey is made in the local Universe, it is reported that essentially all of the galaxies found have optical counterparts (Ryan-Weber et al. 2002). If a large fraction of the gas were in non-collapsed objects at higher redshifts, then this would reduce significantly the number of detections by a future survey. There have been searches at low redshifts for large clouds of gas with high mass and very low column density (Minchin et al. 2003). These searches have found no large clouds with low column density, and have also found that all collapsed galaxies detected in H I have an average column density $N_{\text{HI}} \sim 10^{23}$ to 10^{25} m^{-2} . In Ryan-Weber et al. (2002), a sample of 34 galaxies from this HIPASS was observed at higher spatial resolution so that the column density could be computed at each point of each galaxy. The resulting column density distribution is similar to those in the damped-Ly α results (Proulx et al. 2001), allowing for an increase in normalization for the reasons outlined in Section 3; however, in this case we know that the galaxies in the HIPASS are in collapsed objects. This is strong evidence that the H I found in blind surveys traces the dark matter potential wells in a similar way to the baryons, and this suggests that the H I found at high redshift is likely to be in collapsed objects such as young galaxies.

In our model C we have assumed that the mass in baryons in a galaxy follows the dark matter mass. Observationally, there is compelling evidence that this is the case if we look at the Tully–Fisher relation in spirals. McGaugh et al. (2000) have shown that the Tully–Fisher relation obtained using only the stellar component of spiral galaxies has a break at around 90 km s^{-1} ; however, this break disappears if, instead of considering just the stellar population, they use the total baryonic mass of the galaxy composed of gas plus stars. They obtain a very good fit for both ends of their data, i.e. for low and high circular velocities. This baryonic Tully–Fisher relation has the following implication: the mass of gas plus stars is directly proportional to the mass in dark matter, and any other dark component is unlikely to be important as it would introduce too much scatter.

If we look at the blue luminosity function of galaxies at redshift $z = 1$, we can use scaling relations in order to estimate whether it is consistent with model C. We crudely assume that the blue luminosity density is proportional to the SFR at each epoch. Therefore, the ratio of the breaks of the H I mass function and the blue luminosity function should be in proportion to the ratio of Ω_{HI} to the SFR. Given that we have an estimate of the SFR and the density of neutral hydrogen at $z = 1$ (Section 3.2), we can infer the position of the break of the $z = 1$ H I mass function by knowing the position of the break of the $z = 1$ luminosity function of blue galaxies; this has been taken from COMBO-17 (Chris Wolf, private communication based on the data from Wolf et al. 2003). We plot and compare this model with our models A, B and C. We can see from Fig. 6 that models A and C are clearly preferred by this comparison. In fact, at redshift

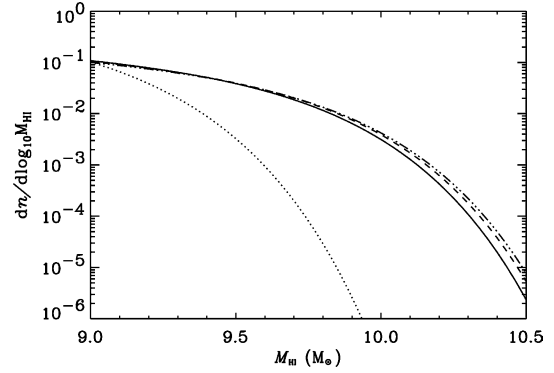


Figure 6. The H I mass function plotted at redshift $z = 1$ for models A (dashed line), B (dotted line) and C (solid line). We compare these models with the H I mass function that is inferred from the optical luminosity function of blue galaxies as described in Section 4 (triple-dot-dashed line). The curves for model A, model C and the model inferred from the blue luminosity function are very similar and almost indistinguishable from each other. This indicates that the H I mass function is likely to be closer to models A or C than to model B.

$z = 1$ our models A and C give essentially the same prediction for the H I mass function as can be inferred from the similar dN/dz for these two models over the redshift range $0 \lesssim z \lesssim 1$.

In our model we assume that the average dark matter halo in a galaxy at the break of the H I mass function is smaller at higher redshifts according to hierarchical processes; however, on the other hand, these galaxies have fewer stars and are more gaseous. So, if we take galaxies at $z \simeq 2$, their average luminosity will be roughly proportional to the stars in that galaxy, which will be approximately $\{\Omega_{\text{stars}}(z)/[\Omega_{\text{stars}}(z) + 2\Omega_{\text{HI}}(z)]\} L^*$. Thus, at $z = 2$, these galaxies would be, assuming no scatter, 50 times fainter optically than L^* (i.e. objects at the break of the optical Schechter luminosity function). Deep near-infrared imaging with the *HST* typically fails to detect stellar counterparts to damped-Ly α objects (Warren et al. 2001) to limits that are consistent with our rough calculation based on model C.

It is also well known that it is very hard to find known damped-Ly α systems in H I absorption in the radio. This is also in agreement with model C as, at high redshifts, this predicts smaller gas-rich clouds with shallower gravitational potentials and consisting mainly of a warm neutral medium that has a high spin temperature (Kanekar & Chegalur 2003). Because of the high spin temperature it will be hard to find these objects in absorption in the radio until we have instruments with the sensitivity of the SKA.

Finally, there have been searches for H α lines associated with star formation in damped-Ly α systems, but typically no line flux is found. This can impose (assuming a negligible dust obscuration) a maximum SFR which would correspond to $11.4\text{--}36.7 M_{\odot} \text{ yr}^{-1}$ for the studied objects (Bunker et al. 1999). Because our break for the H I mass function moves towards the left for our preferred model C, the SFR in high- z objects would be lower than in galaxies at the break of the low- z H I mass function. We therefore would not expect any line flux to be detected in such searches, as the SFR is likely to be too low to produce a robust detection; thus, these results are also in agreement with model C. Nevertheless, if we do have a star formation $\sim 10 M_{\odot} \text{ yr}^{-1}$, we would have an associated continuum emission in the radio of $\sim 1 \mu\text{Jy}$ at redshift $z = 2$ (Condon 1992), and we will trivially be able to detect this level of emission with SKA-like instruments (equation 2). In fact, the continuum emission is only a factor of 15 fainter than the corresponding line emission.

Good bandpass calibration will therefore be essential for the line detection of star-forming galaxies, particularly those that may, because of inevitable scatter, have a continuum flux of the same order of magnitude as the 21-cm line emission.

We have to stress here that model C is basically taking the known population of H I-emitting objects at $z = 0$ and trying to see what they would look like at higher redshift. It is likely though that there will be another population of H I-emitting objects which would be the subunits of large elliptical galaxies today. These subunits would probably have been H I-rich in the high- z Universe, before they merged to form a large elliptical galaxy and before they became part of large dark matter haloes, such as groups and clusters. Nevertheless, we think that these objects would still be rare at redshifts around $z \simeq 1.5$. First, given the colour information on elliptical galaxies found in observations (Bower, Lucey & Ellis 1992), it is argued that most of the stars in giant elliptical galaxies must have been formed at redshifts higher than 1.5 to explain their consistently red colours. Secondly, a population of extremely red objects is now well established at $z \simeq 1.5$ (e.g. Daddi, Cimatti & Rensini 2000), which look to be progenitors of nearby ellipticals, and which appear to be red because of the old stellar populations, as was first demonstrated for $z \simeq 1.5$ radio galaxies (Dunlop et al. 1996). Thirdly, if such a population exists it is likely that they would appear as large spiral galaxies at $z \simeq 1.5$; however, observationally (Wolfe et al. 1985) only one such example has been detected as a damped-Ly α system at $z \simeq 2$. Most damped-Ly α objects are consistent with being smaller galaxies with a warm neutral medium (e.g. Kanekar & Chegalur 2003), which would be the precursors of the spiral population today. We neglect the elliptical population but caution that it may start to contribute significantly to the H I population at redshift $z \sim 2$ (Section 6).

We have emphasized here how the break of the H I mass function is likely to change with redshift, but this change is not directly constrained by current data. However, we have discussed various observational constraints in this section which are in good agreement with our model C. If the break of the H I mass function were to remain at very high masses at higher redshifts, then we would expect brighter galaxies and stronger star formation lines associated with most damped-Ly α objects. On the other hand, if the H I break shifts towards very low masses at higher redshifts, it is hard to find consistency with the blue luminosity function at $z = 1$ (Fig. 6). Finally, we note that our model C is in good agreement out to $z \sim 1.5$ with the predictions of semi-analytical models; see Rawlings et al. (2004) for a comparison with models from Cole et al. (1994) and Benson et al. (2003).

5 PROBING DARK ENERGY VIA BARYONIC OSCILLATIONS

It has been proposed in the literature by several authors (e.g. Blake & Glazebrook 2003; Hu & Haiman 2003; Seo & Eisenstein 2003) that measuring the baryonic oscillations in the galaxy power spectrum allows a clean method of probing properties of dark energy, which could be performed provided enough cosmic volume and enough tracers of this volume (e.g. galaxies) are available.

There are two sources of error in such a power spectrum measurement. The first of these is sample or cosmic variance, which is linked to the fact that the number of independent spatial modes that we can measure in a given cosmic volume is finite. This error is inversely proportional to the square root of the cosmic volume covered by a survey (see equation 17). In the case of an H I survey with

an SKA-like telescope, this will be determined by the area of the sky we will be able to survey and the integration time we will spend in each deg², which will in turn constrain the maximum redshift at which we will be able to detect H I sources (see Section 5.2 and Fig. 5). The other source of error is shot noise due to the imperfect sampling of the fluctuations due to the finite number of tracers in the volume. The total fractional error in the power spectrum, assuming the optimized weighting scheme of Feldman, Kaiser & Peacock (1994), is

$$\left(\frac{\sigma_P}{P}\right)^2 = 2 \frac{1}{4\pi k^2 \Delta k} \frac{(2\pi)^3}{V_{\text{survey}}} \left(\frac{1+nP}{nP}\right)^2, \quad (17)$$

where P is the value of the power spectrum at wavelength k and n is the number of sources per volume in our sample.¹

We would like to minimize the error we obtain from a $P(k)$ measurement. This would involve designing a survey that would have maximum volume, provided that there are enough sources so that the shot noise is negligible compared to the error due to cosmic variance. In order to have a negligible shot noise, we would need $nP \gg 1$ (equation 17) but this would involve obtaining an enormous amount of sources per volume. As is argued in detail by Seo & Eisenstein (2003), there is no great gain in going from $nP \sim 3$ to $nP \rightarrow \infty$, so we assume that our errors will become large compared to cosmic variance only when $nP < 3$.

Having $nP \sim 3$ means that $N/V \sim 3/P$ so we have errors in the shot noise that will be small if $dN/dz > (3/P)(dV/dz)$. Here, dN/dz is the differential number density of sources that we obtain from our model, and dV/dz is the usual comoving volume element. Given that at redshifts of interest ($z \sim 1.5$) the ‘wiggles’ in the power spectrum will have been erased by non-linear clustering for $k \gtrsim 0.25 \text{ Mpc}^{-1}$ (see Blake & Glazebrook 2003), we take $P(0.14 \text{ Mpc}^{-1})$ for our calculations, i.e. the position of the first wiggles in the power spectrum. We have assumed that H I galaxies have a bias that increases slowly as a function of redshift roughly as $g(z)$, from a bias of ~ 1 at low redshift. The close association at low redshifts between galaxies selected by their H I content and the normal ‘late-type’ galaxy population (e.g. Minchin et al. 2003) and the unit bias of this population with respect to the dark matter (Peacock et al. 2001; Verde et al. 2002) suggest that this assumption is reasonable. We then assume that the systematic rise in the bias cancels with the drop in the normalization of $P(k)$. We estimate that measurements will be statistically useful until the differential number density drops below $dN/dz \sim 5000$ galaxies per deg² (see Fig. 5). This defines the maximum redshift we can probe with a given integration time.

5.1 Optimal survey strategy

The error on the dark energy parameter w will not depend only on the cosmic volume probed and the shot noise of the experiment. It depends also on the number of wiggles probed (which is a function of the redshifts surveyed given that non-linearities can dilute and erase these wiggles), represented by $n_w(z)$ and on the strength of the test, which can be represented as the distortion of the wiggle length as a function of redshift (see fig. 5 of Blake & Glazebrook 2003). Note from the $1/k^2$ dependence of equation (17) that high- k wiggles are easier to measure provided that they have not been diluted or even erased by non-linearities.

¹ We adopt the Fourier transform convention in which nP has no units.

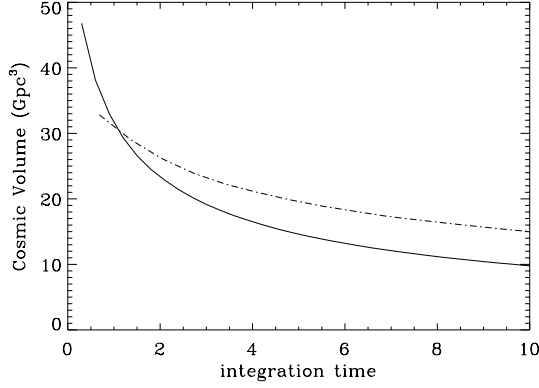


Figure 7. The solid line shows the cosmic volume surveyed in 1 yr for a 1-deg² FOV SKA-like instrument at 10 σ detection level and with a FOV scaling with frequency ν as ν^{-2} ; this is plotted as a function of integration time per pointing. Note that we may choose to have a short integration time and cover a large fraction of the sky or have a deeper survey over a smaller area. Note also that, assuming a dedicated telescope and negligible overheads, if we choose an integration time as low as ~ 0.3 h we can cover half of the sky in ~ 1 yr. It is clear that the optimal survey in terms of volume access is the shallower survey over all the sky available. The dot-dashed line is the volume weighted by the number of wiggles in the linear part of the power spectrum for the same survey. We stress that it has no physical value but that it reflects the fact that the volume at higher redshift is more useful for dark energy parameter constraints. We can see that even with the fudge factor that takes account of this, an all-hemisphere survey is still the best option for an SKA-like instrument.

First, we calculate the best shape for a survey so that we obtain the biggest volume in the smallest time. Would it be a shallow survey that would cover the whole sky or a deep survey that would cover only a fraction of the sky? In order to determine this, we compute the volume surveyed by multiplying the area covered in the sky by the effective volume covered by the data. From Tegmark (1997) we obtain

$$V_{\text{survey}} = \frac{T_0}{t_1} \frac{\text{FOV}}{20\,000 \text{ deg}^2} \int_V \left(\frac{nP}{1+nP} \right)^2 dV, \quad (18)$$

where T_0 is the total time of the survey, and t_0 is the integration time spent per pointing, $t_1 = t_0/\beta$, where $\beta = \min(1, BW_{\text{SKA}}/BW_{\text{survey}})$. Here, BW_{SKA} denotes the bandwidth allowed given a particular realization of an SKA-like instrument and BW_{survey} represents the frequency range corresponding to H I redshifted throughout the range of redshifts of the survey. In most SKA realizations β is expected to be below one, but should not be an order of magnitude below one.

We choose a survey time of one year and a FOV of 1 deg², and then set the optimum integration time that will maximize V . As we can see from Fig. 7 we obtain the largest volumes when we perform a shallow survey across all the available sky.

Nevertheless, the survey with the largest volume is not necessarily the best survey to probe dark energy. A survey at high redshift may have more wiggles and therefore provide a better constraint than a survey with a large volume at low redshift. In order to illustrate this, we plot in Fig. 7 a volume weighted by $n_w(z)$. We stress here that this is only a toy model to illustrate that even though the test may be more efficient at high redshifts, the sensitivities and FOV of the SKA are such that a survey with the largest area is likely still to be the optimal survey. We expect to produce a more rigorous calculation of these effects.

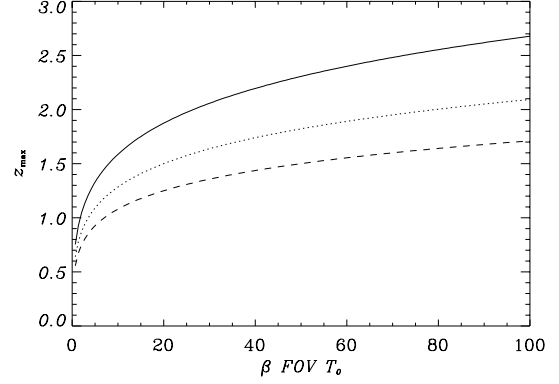


Figure 8. Maximum redshift z_{max} probed by a survey as a function of telescope specifications and duration T_0 of an SKA survey in units of yr. We assume that half the sky is observable so the integration time we choose trades off linearly with the FOV. A larger FOV will allow us to spend longer in a patch of the sky and therefore to probe to deeper redshifts. The solid line is for a telescope with a FOV scaling with frequency ν as ν^{-2} , the dashed line is for surveys with telescopes with a constant FOV and the dotted line is for surveys with telescopes with a FOV scaling as ν^{-1} . The three curves have SKA-like sensitivity.

If we look at fig. 5 of Blake & Glazebrook (2003) we can see that the baryonic oscillations test is considerably weaker below a redshift of 0.5. On the other hand, we can see that even with this volume-weighted function in Fig. 7 the largest volume-weighted volume we obtain is for integration times that have the largest area available in the sky. All of these surveys probe redshifts larger than 0.5, in fact as we can see from Fig. 8 these surveys probe volumes at least as high as $z \sim 0.7$ – 0.8 . A survey that is designed to probe dark energy with baryonic oscillations must have a considerable volume at redshifts larger than 0.5.

We therefore conclude that the optimal way of probing large-scale structure with future radio surveys with a sensitivity comparable to that of an SKA will be to produce surveys that probe all the area available on the sky. We caution that this might not be the case if the telescope sensitivity is significantly lower.

5.2 Surveys attainable by future radio telescopes

The factor $nP/(1+nP)$ in equation (18) will be very close to 1 for most redshifts where we have data and will fall sharply to 0 where the H I starts to become too faint to be detected. Here we consider $nP/(1+nP)$ as a step-down function that becomes zero at z_{max} . We define this maximum redshift z_{max} as the redshift where we become shot-noise limited (i.e. $nP \sim 3$), which corresponds to $dN/dz \sim 5000 \text{ deg}^2$. We therefore have

$$V_{\text{survey}} \simeq \frac{T_0}{t_0} \frac{\beta \text{FOV}}{20\,000 \text{ deg}^2} \int_0^{z_{\text{max}}(t_0)} \frac{dV}{dz} dz, \quad (19)$$

so the value of z_{max} will determine the maximum depth to which we will be able to reproduce a galaxy power spectrum reliably.

In Fig. 8 we plot the maximum redshift of a given survey with an SKA-like instrument as a function of how the FOV scales with z . There are four features of the future radio telescope that are vital in order for this survey to be optimal. The first feature is the sensitivity of the instrument. As we can see from Fig. 8, with an SKA-like telescope our gain in z_{max} starts dropping quickly as we start probing

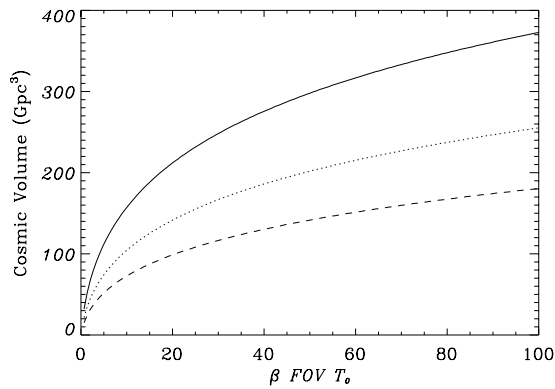


Figure 9. Cosmic volume probed by a survey with a future radio telescope as a function of telescope specifications and length of survey at a 10σ level of detection. The solid line is for telescopes with a FOV scaling with frequency ν as ν^{-2} , the dashed line is for surveys with telescopes with a constant FOV and the dotted line is for surveys with telescopes with a FOV scaling as ν^{-1} . The three curves have SKA-like sensitivity.

redshifts ~ 1.5 . We conclude that if redshifts of the order of 1.5 have to be reached in order to probe dark energy optimally with this survey, then a full SKA-like sensitivity is needed. As we see in Section 5.3, this is indeed the case and the full SKA will be needed to properly probe dark energy.

The second and third features are the FOV and β , the useful bandwidth of the telescope, which are essentially degenerate. We can clearly see in Fig. 9 that although SKA-like sensitivity is vital to obtain a large cosmic volume, the factor β FOV plays an equally important role. The fourth and final feature is the way the FOV scales with frequency. We can see in Figs 8 and 9 the effect of this choice, and we show the huge advantage that is gained if the SKA design can have FOV scaling with frequency as ν^{-2} .

The choice of these four features will indicate the depth of an eventual survey. For example, a telescope with $f = 1$, β FOV = 1 deg^2 and a FOV scaling as ν^{-2} can survey 40 Gpc^3 in 1 yr. In 10 yr, the same telescope will be able to survey 150 Gpc^3 by probing deeper in redshift. This same 150 Gpc^3 could be completed in just 1 yr if β FOV = 10 deg^2 .

We note here that the angular resolution required by the baryonic oscillations method is much less than the angular resolution expected of future radio interferometers such as the SKA. The results from Fig. 9 are independent of the resolution of the instrument because the baryonic ‘wiggles’ probe very large angular scales, and confusion will not be a serious issue given the accurate redshifts available for objects in a low-resolution H I survey. This method can therefore be used whether the instrument being used is an SKA-like array or the core of such an array.

5.3 Constraints on dark energy

Now, given that we can have a realistic idea of what type of survey future radio telescopes may produce, we can relate these surveys to an estimated error on the measurement of w . There are likely to be other efforts in measuring the equation of state of dark energy using the baryonic oscillations method. As argued in Blake & Glazebrook (2003), an optical survey would, in 1 yr, be able to measure w to $\Delta w \simeq 0.1$, provided a spectrograph that can take data on 3000 galaxies at a time is available on an 8-m optical telescope.

In 1 yr, a dedicated 8-m telescope with such an instrument could cover a cosmic volume of $\sim 6 \text{ Gpc}^3$ (a volume six times greater than that covered by the Sloan Digital Sky Survey). This Kilo-Aperture Optical Spectrograph (KAOS) project has been proposed (Barden 2003; Glazebrook 2003) and may produce results in the next decade.

As we can see from equation (17), the error on the power spectrum scales as the $V_{\text{survey}}^{-1/2}$, and this error would relate to the error on the size scale of the wiggles, which would in turn directly relate to an error on the parameter w . We therefore expect the error on w to improve as $V_{\text{survey}}^{1/2}$ as we cover more volume. At the likely rate of data collection, after a decade of results, the KAOS project is likely to produce a constraint roughly a factor of $\sim f_{\text{sky}}^{0.5} = \sqrt{10}$ better and therefore constrain w down to $\Delta w \simeq 0.03$, surveying a volume² of around 60 Gpc^3 .

The volume surveyed in a 1-yr survey with a dedicated radio telescope with $f = 1$ and β FOV $\simeq 1 \text{ deg}^2$ and a FOV scaling as ν^{-2} is around 40 Gpc^3 . Given that it is unlikely that an array such as the future SKA will be dedicated to a single project, we conclude that if β FOV $\sim 1 \text{ deg}^2$ for the SKA we would only be able, on the time-scale of years, to obtain constraints of around $\Delta w \simeq 0.03$ (see Fig. 9), comparable to those from KAOS.

We therefore argue that a future radio telescope with a small ($\sim 1 \text{ deg}^2$) FOV could constrain w well, but similar constraints will already be available by the time this telescope is operational. However, a data set with $z_{\text{max}} \sim 1.5$ in a hemisphere, which is achievable in 1 yr provided β FOV $\gtrsim 10$ (see Fig. 8), would obtain constraints of $\Delta w \simeq 0.01$ ($f_{\text{sky}}/0.5$)^{-0.5} given the extra volume available. We would be able to improve considerably on these constraints in following years of survey by probing deeper in redshift and accruing more volume (see Fig. 9). If we parametrize the equation of state in the form $w = w_0 + w_1 z$, we would have $\Delta w_0 \simeq 0.035$ and $\Delta w_1 \simeq 0.1$ (Blake et al. 2004). Such a data set would be ideal to probe the properties of dark energy and its evolution with redshift.

We conclude that for an SKA-like telescope, studies of dark energy demand that the optimal telescope has a FOV scaling with frequency ν as ν^{-2} , and β FOV $\gtrsim 10 \text{ deg}^2$.

6 UNCERTAINTIES AND POSSIBLE PROBLEMS WITH FUTURE H I SURVEYS

In the previous sections we have assumed certain generic features of future radio surveys, and we have also assumed a certain evolution for the mass function of H I. With these two ingredients, we have derived a number density of sources that would be accessible to us if we perform a survey of H I with a future radio telescope. In this section, we relax some of the key assumptions, one by one, and see how this would affect studies of dark energy based on baryonic oscillations. We present the duration of the survey needed in order to constrain the equation of state of dark energy to the same accuracy. Some of the results of this section are summarized in Table 1.

If we relax the assumptions we have made regarding the evolution of the H I mass function, we could assume that the evolution would be better described by models A or B rather than model C. In Fig. 10 we plot the number density of H I sources for an integration time of 2 h for model A and an integration time of of 32 h for model B.

² Note that optical surveys with KAOS cover sky area to similar volume depths at a similar rate to an SKA with FOV = 1 deg^2 , but can never be fully dedicated to such a survey because of daylight and bright phases of moonlight.

Table 1. As mentioned in Section 5.3, with an all-hemisphere survey covering redshifts 0–1.5 we would be able to measure w to $\Delta w \simeq 0.01$; this table illustrates how much longer/shorter it would take if we had chosen a different telescope design (rather than a FOV scaling as ν^{-2}) or a different model (rather than model C) for the H I mass function. For example, a telescope with twice the FOV would do the survey \sim two times faster, or if the real H I mass function were closer to model A, the survey would take \sim eight times longer.

Changes	Change in time required to complete survey
FOV	$\propto 1/\text{FOV}$
FOV $\propto \nu^{-1}$	$\times \sim 2$
FOV $\propto \nu^0$	$\times \sim 4$
Bandwidth	$\propto 1/\beta$
Model A	$\times \sim 8$
Model B	$\propto \sim 2$
No evolution	$\times \sim 1$

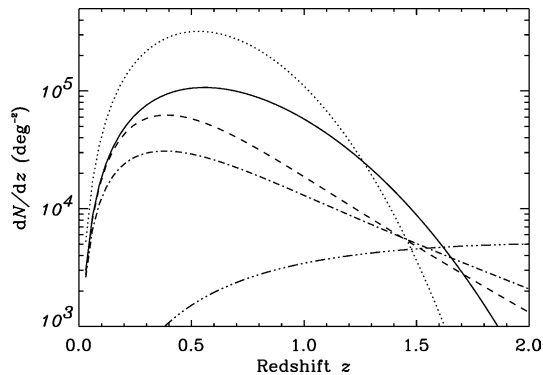


Figure 10. The differential number density dN/dz per deg^2 of objects in an SKA survey with a signal-to-noise detection level of 10. Different integration times were chosen for our three evolution models – models A (2-h; dashed), B (32-h; dotted) and C (4-h; solid) – and for a no-evolution model (6-h; dot-dashed), probing out to same redshift $z_{\text{max}} \sim 1.5$. The triple-dot-dashed line defines the number density of objects needed at high redshift for us to be cosmic variance limited when reconstructing the galaxy power spectrum (see Section 5).

We have chosen these integration times so that the number density of objects is enough to probe the Universe out to the same redshift ($z_{\text{max}} \sim 1.5$; see Section 5.2) as for model C with tiled surveys with 4-h integrations. We conclude that if we have made an error in choosing the evolution of the H I mass function, the time-scale of our survey would have to be multiplied by a factor of between ~ 8 and ~ 0.5 in order for us to obtain similar constraints. As discussed in Section 4, models A and B are not preferred by observations, but they are not yet completely ruled out; it is plausible that a survey would take between half of the time estimated and \sim eight times longer.

As we can see clearly from Section 5, the gain which accrues from an increase in FOV is linear in time. A survey with a telescope with twice the FOV will be able to produce similar results in half of the time. The same is applicable to an increase in the effective bandwidth β of the correlator. A telescope with β halved will take twice as long

to produce a given survey. However, most of the volume surveyed is at high redshift, and given that the frequency range at low redshifts (0–0.5) is relatively large, it may be desirable to neglect the low-redshift range of the survey in order to produce a high-redshift survey with a higher value of β .

The relationship between the scaling of the FOV with frequency and the performance of the survey is more complicated to assess as it changes depending on the β FOV of the telescope. However, on average, if a telescope is built with a FOV scaling with frequency as ν^{-1} , it would be able to probe the same volume around two times slower than a telescope whose FOV scales as ν^{-2} (see Fig. 9). If a telescope has a constant FOV, it will be \sim four times slower than a telescope with a FOV scaling as ν^{-2} (see Fig. 9).

The way in which H I galaxies trace the dark matter fluctuations, the bias, is another important uncertainty in our calculations. There are ways in which bias might make the baryonic oscillations method more powerful than we have suggested. First, following Blake & Glazebrook (2003) a high bias population requires a lower number density of sources to avoid shot-noise limitation. Secondly, as discussed in Section 3.2, our method of estimating the H I mass function at high redshift effectively ignores the most massive (i.e. elliptical) galaxies because they have low H I content in the low-redshift Universe. The most massive systems at some (as yet unknown) high redshift are likely to have significant H I content and they are likely to be highly biased tracers of the dark matter mass, as is seen for the most massive galaxies at low redshift (Norberg et al. 2001) and for high-redshift quasars (Croom et al. 2002).

Another unknown in this analysis is the biasing model for the power spectrum. It is not known whether a halo model (e.g. see Seljak 2000; Peacock & Smith 2000) could induce a bias that could possibly dilute some of the wiggles. Blake & Glazebrook (2003) argue that at large scales, where the first few baryonic wiggles are found, the power spectrum should have a constant bias as only extremely rare fluctuations will be going non-linear.

7 CONCLUDING REMARKS

The most important features for the design of future radio telescopes have to be identified if they are to be used to probe dark energy in new and interesting ways. The instantaneous 1.4-GHz FOV of the telescope must be at least an order of magnitude larger than the $\sim 1 \text{ deg}^2$ FOV achievable now by optical multi-object spectrographs, so that a ‘whole hemisphere’ can be surveyed on a reasonable (i.e. ~ 1 yr) time-scale. H I surveys with the SKA would then in ~ 1 yr contain $\sim 10^9$ galaxies with redshifts in the range $0 \lesssim z \lesssim 1.5$. The sensitivity of the telescope must eventually equal that proposed for the SKA, because this is the only way of detecting H I galaxies out to $z \sim 1.5$, and therefore obtaining constraints on the dark energy parameter w of the order $\Delta w \sim 0.01$. An SKA with a FOV $\sim 1 \text{ deg}^2$ would be a very inefficient telescope for dark energy studies. The instantaneous bandwidth of the telescope must cover the frequency range corresponding to H I in the redshift range $0.5 \lesssim z \lesssim 1.5$ in as few settings as possible; that is, β , the ratio of the SKA bandwidth to the survey bandwidth, must be close to unity, because otherwise it trades off linearly with the FOV. The baseline distribution of the SKA must have a large fraction (at least 50 per cent) of the collecting area within a ~ 5 -km diameter core.

The most efficient way of making an SKA survey aimed at constraining the properties of dark energy will be to first make a survey of all the sky available, and only then probe deeper in redshift. We have shown that, provided β FOV $\gtrsim 10 \text{ deg}^2$, H I surveys with a full

SKA would, after ~ 1 yr, contain $\sim 10^9 (f_{\text{sky}}/0.5)$ galaxies with redshifts in the redshift range $0 \lesssim z \lesssim 1.5$, and hence provide constraints on the dark energy parameter w of order $\Delta w \simeq 0.01 (f_{\text{sky}}/0.5)^{-0.5}$, where f_{sky} is the fraction of the whole sky.

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REFERENCES

- Ballinger W. E., Peacock J. A., Heavens A. F., 1996, *MNRAS*, 282, 877
- Bardeen J., Bond J., Kaiser N., Szalay A., 1986, *ApJ*, 304, 15B
- Barden S., 2003, in Brown M., Dey A., eds, *ASP Conf. Ser. Vol. 280, Next Generation Wide-Field Multi-Object Spectroscopy*. Astron. Soc. Pac., San Francisco, p. 89
- Battye R. A., Davis R. D., Weller J., 2004, *MNRAS*, 355, 1339
- Benson A. J., Bower R. G., Frenk C. S., Lacey C. G., Baugh C. M., Cole S., 2003, *ApJ*, 599, 38
- Blake C., Glazebrook K., 2003, *ApJ*, 594, 665
- Blake C., Abdalla F. B., Bridle S., Rawlings S., 2004, *New Astron. Rev.*, in press (astro-ph/0409278)
- Bower R. G., Lucey J. R., Ellis R., 1992, *MNRAS*, 254, 589
- Briggs F., 1999, in van Haarlem M. P., ed., *Perspectives on Radio Astronomy: Science with Large Antenna arrays*. ASTRON, Dwingeloo, p. 74
- Bunker A., Warren S. J., Clements D. L., Willinger G. M., Hewett P. C., 1999, *MNRAS*, 309, 875
- Caldwell R. R., Dave R., Steinhart P., 1998, *Phys. Rev. Lett.*, 80, 1582
- Carilli C., Rawlings S., 2004, *New Astron. Rev.*, in press (astro-ph/0409274)
- Carroll S., Press W. H., Turner E. L., 1992, *ARA&A*, 30, 499
- Chegalur J. N., Kanekar N., 2000, *MNRAS*, 318, 303
- Choudhury T., Padmanabhan T., 2002, *ApJ*, 574, 59
- Cole S., Aragon-Salamanca A., Frenk C. S., Navarro J. F., Zepf S. E., 1994, *MNRAS*, 271, 781
- Condon J. J., 1992, *ARA&A*, 30, 575
- Conway J. E., 1998, *MMA*, Memo 216
- Cooray A. R., Huterer D., 1999, *ApJ*, 513, 95
- Croom S. M., Boyle B. J., Loaring N. S., Miller L., Outram P. J., Shanks T., Smith R. J., 2002, *MNRAS*, 335, 459
- Daddi E., Cimatti A., Rensini A., 2000, *A&A*, 362, L45
- Dekel A., 2004, in Bender R., Renzini A., eds, *Venice Workshop on Multi-wavelength Mapping of Galaxy Formation and Evolution*, in press (astro-ph/0401503)
- Dekel A., Silk J., 1986, *ApJ*, 303, 39
- Douspis M., Riazuelo A., Zolnierowski Y., Blanchard A., 2003, *A&A*, 405, 409
- Dunlop J., Peacock J. A., Spinrad H., Dey A., Jimenez R., Stern D., Windhorst R., 1996, *Nat*, 381, 581
- Efstathiou G., Jones B. J. T., 1979, *MNRAS*, 186, 133
- Eisenstein D. J., 2002, in Brown M., Dey A., eds, *ASP Conf. Ser. Vol. 280, Large-scale Structure and Future Surveys in Next Generation Wide-field Multi-object Spectroscopy*. Astron. Soc. Pac., San Francisco, p. 35
- Ellison S. L., Yan L., Hook I. M., Pettini M., Wall J. V., Shaver P., 2001, *A&A*, 379, 393
- Fall S. M., Efstathiou G., 1980, *MNRAS*, 193, 189
- Feldman H. A., Kaiser N., Peacock J. A., 1994, *ApJ*, 426, 23
- Ferguson H. C. et al., 2003, *AAS*, 202, 1704
- Field G. B., 1958, *Proc. IRE*, 46, 240
- Fukugita M., Hogan C. J., Peebles P., 1998, *ApJ*, 503, 518
- Giallongo E., Menci N., Poli F., D'Odorico S., Fontana A., 2000, *ApJ*, 530, L73
- Glazebrook K., 2003, in Brown M., Dey A., eds, *ASP Conf. Ser. Vol. 280, Next Generation Wide-field Multi-object Spectroscopy*. Astron. Soc. Pac., San Francisco, p. 101
- Haiman Z., Mohr J. J., Holder G. P., 2001, *ApJ*, 553, 545
- Hu W., Haiman Z., 2003, *Phys. Rev. D*, 68, 063004
- Jenkins A., Frenk C. S., White S. D. M., Colberg J. M., Cole S., Evrard A. D., Couchman H. M. D., Yoshida M., 2001, *MNRAS*, 321, 372
- Jones D. L., 2004, *SKA*, Memo 45
- Kanekar N., Chegalur J. N., 2003, *A&A*, 399, 857
- Lokas E., Hoffman Y., 2001, in Spooner N. J. C., Kudryavtsev V., eds, *Proc. 3rd International Workshop on the Identification of Dark Matter*. World Scientific, Singapore, p. 121
- McGaugh S. S., Schombert J. M., Bothun G. D., de Blok W. J. G., 2000, *ApJ*, 533, L99
- Minchin et al., 2003, *MNRAS*, 346, 787
- Newman J. A., Davis M., 2000, *ApJ*, 534, L11
- Norberg P. et al., 2001, *MNRAS*, 328, 64
- Peacock J. A., 1999, *Cosmological Physics*. Cambridge Univ. Press, Cambridge
- Peacock J. A., Smith R. E., 2000, *MNRAS*, 318, 1144
- Peacock J. A. et al., 2001, *Nat*, 410, 169
- Peebles P. J. E., 1969 *ApJ*, 155, 393
- Percival W. J. et al., 2001, *MNRAS*, 327, 1297
- Peroux C., Irwin M., McMahon R. G., Storrie-Lombardi L. J., 2001, *Astrophys. Space Sci. Suppl.*, 277, 551
- Poli F., Giallongo E., Menci N., D'Odorico S., Fontana A., 1999, *ApJ*, 527, 662
- Press W., Schechter P., 1974, *ApJ*, 187, 425
- Rao S. M., Turnshek D. A., 2000, *ApJS*, 130, 1
- Rao S. M., Turnshek D. A., Briggs F. H., 1995, *ApJ*, 449, 488
- Rawlings S., Abdalla F. B., Bridle S., Blake C. A., Baugh C. M., Greenhill L. H., van der Hulst J. M., 2004, *New Astron. Rev.*, in press (astro-ph/0409479)
- Rees M., Ostriker J., 1977, *MNRAS*, 179, 541
- Rohlfs K., Wilson T. L., 1999, *Tools of Radio Astronomy*. Springer-Verlag, Berlin
- Ryan-Weber E. et al., 2002, *AJ*, 124, 1954
- Salpeter E., Hoffman G., 1996, *ApJ*, 465, 595
- Seljak U., 2000, *MNRAS*, 318, 203
- Seo H., Eisenstein D. J., 2003, *ApJ*, 598, 720
- Silk J., 2003, *MNRAS*, 343, 249
- Silk J., Bouwens R., 1999, *Ap&SS*, 265, 379
- Spergel D. et al., 2003, *ApJS*, 148, 175
- Storrie-Lombardi L., Wolfe A., 2000, *ApJ*, 543, 552
- Tegmark M., 1997, *Phys. Rev. Lett.*, 79, 3806
- Turner M. S., White M., 1997, *Phys. Rev. D*, 56, 4439
- van der Hulst T., 1999, in van Haarlem M. P., ed., *Perspectives on Radio Astronomy: Science with Large Antenna arrays*. ASTRON, Dwingeloo, p. 229
- Verde L. et al., 2002, *MNRAS*, 335, 432
- Warren S. J., Moller P., Fall S. M., Jacobsen P., 2001, *MNRAS*, 326, 759
- Weller J., Albrecht A., 2002, *Phys. Rev. D*, 65, 3512
- White S. D. M., Frenk C., 1991, *ApJ*, 379, 52
- White S. D. M., Rees M., 1978, *MNRAS*, 183, 341
- Wolf C., Meisenheimer K., Rix H. W., Borch A., Dye S., Kleinheinrich M., 2003, *A&A*, 401, 73
- Wolfe A. S., Briggs F. H., Turnshek D. A., Davis M. M., Smith H. E., Cohen R. D., 1985, *ApJ*, 294, L67
- Young J. S., Knezeck P., 1989, *ApJ*, 347, L55
- Zwaan M. A., van Dokkum P. G., Verheijen M. A. W., 2001, *Sci*, 293, 1800
- Zwaan M. A. et al., 2003, *AJ*, 125, 2842

APPENDIX A: FITTING FORMULAE

We present here (Table A1) some fitting formulae for the differential number density of objects expected in an SKA survey given the range of integration times shown in Table A1. Fitting formulae and numerical results are plotted in Fig. A1.

We have used the following fitting formula:

$$\frac{dN}{dz} = A z \exp \left[-\frac{(z - z_c)^2}{2\Delta z^2} \right]. \quad (\text{A1})$$

Table A1. Fitting functions (dotted lines) for the differential number density of galaxies for a signal-to-noise detection of 10, a FOV scaling as ν^{-2} and for SKA-like sensitivity. We have chosen model C to make our predictions (solid lines) and fitted for several integration times (see Table A1).

Integration time	A	z_c	Δz
1 h	1.58×10^5	0.170	0.351
4 h	2.52×10^5	0.211	0.461
36 h	4.95×10^5	0.283	0.701
360 h	9.33×10^5	0.386	1.045

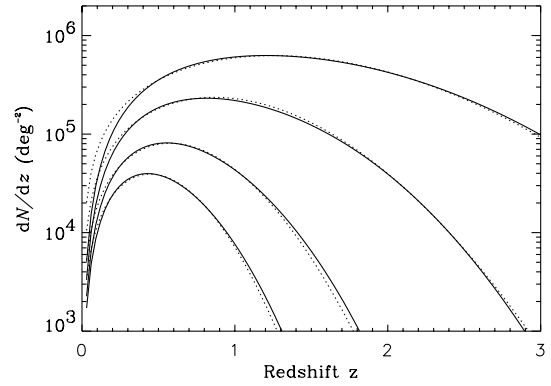


Figure A1. The comparison between our fitting formulae and the expected number density of sources from model C. For all the plots we have assumed SKA-like sensitivity, a FOV scaling with frequency ν as ν^{-2} , and a signal-to-noise detection limit of 10. The fittings are valid for the regions shown and become less accurate for redshifts larger than 3.0.

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