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Probing the upper band gap of atomic rhenium disulfide layers

Krishna P. Dhakal¹, Hyunmin Kim⁶, Seonwoo Lee¹, Youngjae Kim³, JaeDong Lee³ and Jong-Hyun Ahn⁶

Abstract

Here, we investigate the ultrafast carrier dynamics and electronic states of exfoliated ReS_2 films using time-resolved second harmonic generation (TSHG) microscopy and density functional theory (DFT) calculations. The second harmonic generation (SHG) of layers with various thicknesses is probed using a 1.19-eV beam. Up to ~13 nm, a gradual increment is observed, followed by a decrease caused by bulk interferometric light absorption. The addition of a pump pulse tuned to the exciton band gap (1.57 eV) creates a decay-to-rise TSHG profile as a function of the probe delay. The power and thickness dependencies indicate that the electron–hole recombination is mediated by defects and surfaces. The two photon absorptions of 2.38 eV in the excited state that are induced by pumping from 1.57 to 1.72 eV are restricted because these transitions highly correlate with the forbidden *d*–*d* intrasubshell orbital transitions. However, the combined usage of a frequency-doubled pump (2.38 eV) with wavelength-variant SHG probes (2.60–2.82 eV) allows us to vividly monitor the variations in TSHG profiles from decay-to-rise to rise-to-decay, which imply the existence of an additional electron absorption state (*s*-orbital) at an approximate distance of 5.05 eV from the highest occupied molecular orbital states. This observation was critically examined by considering the allowance of each electronic transition and a small upper band gap (~0.5 eV) using modified DFT calculations.

Introduction

Rhenium disulfide (ReS₂) is a group-VII transition metal dichalcogenide (TMD) material that exhibits considerable potential for photovoltaic applications due to its remarkable optoelectronic properties^{1–9} such as a direct band gap and a large work function^{8,9}. ReS₂ is characterized as containing a rich optical and electronic structural diversity due to the stable distorted triclinic 1T crystalline phase owing to the in-plane anisotropic excitons and phonons^{2–7} compared with the isotropic 2H crystal of group-VI TMDs, such as MoS₂ and WSe₂^{10–19}. Thus, increased attention has been devoted to investigating the resolution of the peculiar electronic and optical

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The second harmonic generation (SHG) of atomically thin group-VI TMDs has been extensively studied because of the high second order susceptibility (χ^2) and crystalline structural selectivity. Recently, confocal SHG microscopy was used to identify the relative orientations of the underlying layers in multilayer TMD crystals^{12,17},

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properties of the atomic layers of ReS₂; the density of the electronic valence band states was directly measured using the angle-resolved photoemission spectroscopy (ARPES) technique²⁰, whereas the formation of birefringent excitons was identified using polarization fluorescence microscopy⁴. Additionally, the excitonic lifetime and diffusion coefficient were investigated using the pump–probe optical transient absorption technique²¹, which also explained the blueshift in absorption in the presence of a highly intense pump fluence induced by the optical Stark effect²². Even today, a deeper understanding of the static and dynamic features of the optoelectronic properties of ReS₂ systems is required to develop practical device applications.

which were not completely understood in the case of ReS₂ due to the poor SHG conversion efficiency associated with the complex crystalline symmetry. In principle, the 1L ReS₂ crystal (C_i point group) does not exhibit a noncentrosymmetric structure³, in which the asymmetric inversion center is only associated with A_{u} , whereas the A_{g} harmonic oscillation modes are symmetric. Thus, the polarization-dependent SHG signals of ReS₂ crystals are not caused by the dependency of $A_{\rm u}$ on the increment in the layer number but rather by the stacking alignmentinduced broken inversion center, which is similar to that observed in 3R-like MoS₂ crystals^{12,17}. Furthermore, the aforementioned SHG "probe" could be utilized to create a time-resolved SHG (TSHG) spectroscopic condition characterized by the synchronized illumination of the pump pulse beam, which features the ultrafast carrier dynamics of atomically thin MoS₂ even without an SHG contrast (i.e., for even-number MoS₂ layers)^{18,23}. In TSHG spectroscopy, the probing action of SHG is analogous to single-photon transient absorption, which is observed at the energy of the SHG of the probe photon^{22,23}. More specifically, Jang et al.¹⁸ employed TSHG microspectroscopy to visualize the structure-dependent electron and phonon behavior with a spatial resolution of ~300 nm. In the excited state, absorption occurred at ~4.20 eV (by combining the 1.82 eV pump and the 2.38 eV SHG probe) from the valence band of MoS₂; this was not observed for WSe₂ above 4.03 eV (by combining the 1.65 eV pump and the 2.38 eV SHG probe). Additionally, Lindenberg and coauthors²³ reported that an electronic transition to a distance of 6.02 eV from the ground state (by combining the 3.61 eV pump and the 2.41 eV SHG probe) of the monolayered MoS₂ is allowed using TSHG spectroscopy. The electronic transition is not allowed at 7.76 eV (by combining the 4.66 eV pump and the 3.10 eV SHG probe). Given the aforementioned results and background, the time- and pump/probe energy-dependent SHG of various ReS₂ systems should be investigated in more detail.

In this study, we investigated the ultrafast intraconduction band transitions of ReS2 crystals using pump-probe TSHG microscopy and density functional theory (DFT) calculations. First, it was shown that the layer thickness-dependent SHG by 1.19-eV optical pulses quantitatively increases as a function of the layer number up to a thickness of ~ 13 nm and then gradually decreases, exhibiting a weak signal for the bulk counterpart. The polarization tendency of ReS2 also differed from that of the renowned molybdenum- and tungsten-based dichalcogenides, in which the SHG emission alters with odd or even layer numbers, rather resembling that of MoTe₂. The addition of an excitonic wavelength (1.57 eV) pump caused a time-dependent decay-to-rise trend of the transient SHG signal originating from the ground state depletion (GSD) due to the lack of a permitted excited electron state at ~2.38 eV in the lowest unoccupied molecular orbital (LUMO) of the conduction band. A highly limited stimulated emission effect is expected due to the difference between the energy of the probe photon (1.19 eV) and that of the excitonic resonance (1.57 eV). The pump fluence dependence of the inverse lifetimes of excitons confirmed that the ultrafast carrier relaxation of ReS₂ is highly affected by the crystalline defects. Further, the carrier lifetime change as a function of the number of layers matches that of the surface defect-quantized model well, indicating that the defect that is highly localized on the surface plays a major role in the recombination of the electron and hole in the ReS₂ substrate. Direct optical pumping at a high energy (2.38 eV) demonstrated a transition of the TSHG profiles from decay-to-rise (2.60 eV) to rise-to-decay (2.82 eV), indicating possible absorption at the gamma point of the Brillion zone in the excited state at a distance of ~5.05 eV from the highest occupied molecular orbital (HOMO) of the valence band.

Results

The schematic depicted in Fig. 1a illustrates the microscopic setup to conduct the SHG study of the ReS₂ crystal. More details about the TSHG optical microscopy setup were reported previously (refer to the Section 1, Supporting Information)¹⁸. A dual-mode Er-doped fiber laser system (Spectra-Physics, Insight Deepsee Dual) was used as a laser pumping oscillator (80 MHz) for a confocal galvanometric scanning (Olympus, Fluoview 1000) microscope (Olympus, IX 83) to create the SHG images of the exfoliated ReS2 flakes. One dichroic mirror (DMSP1000R, Thorlabs) was used to spatially overlap the wavelength-variable (120 fs, 680-1300 nm) and 220 fs, 1040 nm pulse beams; the other mirror (RDM690, Olympus) was used to extract the SHG signal from the incident photons. The oil immersion lens (UPlanFLN, Olympus) in our microscopic system allowed us to enhance the signal-to-noise ratio (1.35 NA) and simplified the heat dissipation from the sample. We mechanically exfoliated the ReS₂ crystals (2D material) that were tethered on 300-nm silicon dioxide (SiO₂)-coated silicon substrates. Figure 1b depicts SHG images representative of the mono-, bi-, and trilayer along with bulk systems and the experimental and simulated intensity profiles as a function of the sample thickness with ~10 mW illumination at the sample. The optical micrographs corresponding to the SHG images are depicted in the inset of the lower intensity profile. The exact layer thickness of the respective crystal was confirmed using optical contrast, photoluminescence (PL) spectroscopy, Raman spectroscopy, and atomic force microscopy (Figure S1 in Section 2, Supporting Information). A weak SH signal from the monolayer was observed at the substrate interface, while the SH signals from the bilayer and the other thicker layer





direction (double-sided arrow)

were strongly enhanced in contrast to the 2H MoS₂, as illustrated in the mapping images of the SH (Fig. 1b and Figure S2, Supporting Information). In principle, the SHG output is maximized if the input laser and the output SHG signal in a system with noncentrosymmetry have identical polarization parallel to the crystalline surface. We rotated the sample by fixing the analyzer and polarizer in a direction parallel to the linearly polarized light and further determined the maximum SHG contrast. The plot in the lower part of Fig. 1b displays the maximum SHG intensity produced by the various layers of ReS₂ crystals. Note that the monolayer of ReS2 itself is not a perfectly noncentrosymmetric material like other well-known TMD monolayers, such as 1L MoS₂. In principle, the 1L ReS₂ crystal belongs to the C_i point group, which does not exhibit a noncentrosymmetric structure³. However, in the presence of a substrate interface, a broken inversion symmetric center could still exist in the centrosymmetric atomic layers²⁴, allowing for a weak SHG response of 1L ReS₂. The SHG intensity increases with the layer number in systems with more than one layer, maximizes at a layer thickness of ~13 nm, and then decreases.

The SHG intensity in the *N*th layer of an AAA-type 3R MoS_2 system increases quadratically as a function of the layer number (Figure S3, Supporting Information)^{12,17}. However, various factors can modulate the quadratic dependence model ($\sim N^2$), such as the constructive interference by the neighboring dielectric layers, reabsorption of SHG photons by the adjacent crystals, and net variation in the SH dipole moment, which is a function of the stacking sequence with increasing sample thickness (Figure S3 and S4 in Section 3, Supporting Information). Considering all these parameters, the observed layer-dependent SHG tendency of a low-symmetry crystal, such

as ReS₂, can be modeled as

$$I(2\omega) = N^{n} |\chi_{S}^{2}|^{2} |F|^{2} f(\phi), \qquad (1)$$

where $|F|^2$ is the electric field enhancement induced by the SiO₂ layer and $f(\phi)$ is the phase function dependent on the angle between the input laser polarization and the initial crystallographic orientation. Here, the power factor (*n*) of *N* was maintained at 0.6.

To characterize the anisotropic SHG behavior of the ReS₂ crystals, we measured the polarization dependency of the SHG signal. Figure 1c depicts the optical images of the 1L and 8–9L samples, which were used to monitor the polarization dependence; the SHG intensities were plotted (Fig. 1d, e) as a function of the sample rotation angle, where the analyzer and polarization of the beam (1.19 eV) were adjusted parallel to each other. More details of the anisotropic SHG are provided in Section 4 of the Supporting Information, Figure S5–S7. The anisotropic SHG responses of the 1L ReS₂ crystal represent a butterfly-like pattern in the corresponding polar plots (Fig. 1d). However, the polarization dependence of the 8-9L samples exhibited a more tweaked two-lobe circular pattern. The SHG patterns for the ReS₂ crystal were consistent with that of the nonlinear optical properties of the C_s point group, which was analogous to the 1T' phase MoTe₂ crystal²⁵. Additionally, a few TEM studies revealed the appearance of in-plane diamond-like Re in the ReS₂ 1T' phase 1,2,26,27 . In this geometry, the incident electric field (I_{ω}) generates a second harmonic signal $(I_{2\omega})$ along the parallel and crossed polarization directions. Therefore, by considering the components (α and β) of the secondorder susceptibility tensor, the intensity of the SHG signals of the point group (C_s) can be expressed as $I(2\omega) \propto |\alpha \cos^3\theta + \beta \cos\theta \sin^2\theta|^2$. The values of each component of the susceptibility tensors obtained by fitting were $\alpha = 0.5$ and $\beta = 2.25$ for 1L and $\alpha = 0.85$ and $\beta =$ 1.90 for 8L-9L samples. We assume that deviations may be caused by the substrate-induced strain effect or some other possible structural imperfection.

The bilayer sample was initially analyzed by TSHG microspectroscopy because it is the simplest form of the theoretically available SHG, even under strain-free conditions. Figure 2a is a schematic energy diagram of the bilayer ReS₂, which depicts the allowed energy transitions induced by the pump and probe beams. The time delay (τ) of the probe beam is schematically illustrated; further, instantaneous two-photon absorption with a high-energy band gap (C exciton or nesting band) is known to be resonated^{10,16,28}. The time-dependent TSHG profiles for three different pump pulses (1.45, 1.57, and 1.75 eV with an ~0.6 mJ/cm² fluence) are displayed in Fig. 2b. The position of the zero probe delay (time zero) condition was determined based on the maximum sum frequency

generation at 2.76 eV by the overlap of the pump and probe beams. A high signal-to-noise (S/N > 50) decay-torise-type TSHG profile was observed, which was caused by the loss in the probing SHG signal when the pump beam was tuned to the A excitonic position of 1.57 eV (Figure S8, Supporting Information). The sharp decay near the zero probe delay time was attributed to the electronic effect (bound charge depletion and band gap shrinkage)^{23,29–31}. The cross-correlation of the pump and probe beams was illustrated using a Gaussian profile with a full width at half maximum of 120 fs for comparison. Based on the literature³¹, the decay dynamics of 2D material systems can be modeled using a traditional biexponential fitting or an Auger-related energy-transferring mechanism either through exciton-exciton annihilation (Rate $\propto N_e^2$) or through three-body interaction (Rate $\propto N_e^{-3}$). Given a certain period of time (<40 ps), the exciton-mediated Auger recombination model is sufficient to explain most of the time-resolved SHG spectra. Figure 2c depicts an optical image of the 2L ReS₂ flake; the corresponding TSHG experiment was performed in the absence (second image) and presence (third image) of a pump beam (the dotted circle position i in Fig. 2b). The TSHG signal (ΔI) and its phase information can be simply defined as the difference between the SHG signals obtained with and without the pump beams and can be given as follows¹⁸. See the Supporting Information for the detailed derivation, Section 4b.

$$\Delta I^{2\omega} = \left| I_{pump+probe}^{2\omega} - I_{probe}^{2\omega} \right|$$

= $\beta \chi_{ReS_2}^2 \chi_{ReS_2}^3 . |I^{\omega}|^2 . E_p + \gamma . |\chi_{ReS_2}^3|^2 . I^p . |I^{\omega}|^2$
 $\propto (k \cos \theta + r \cos^2 \theta) * I(2\omega)$ (2)

The polar plots of SHG in the absence of a pump beam and $\Delta I(2\omega)$ of the bilayer sample are illustrated in Fig. 2d, e. The images corresponding to various rotation angles are provided in the Supporting Information (Figure S6). The lattice constants (α and β) for the probe-only case (Fig. 2d) were determined to be 0.5 and 2.42, respectively. We can clearly observe the formation of a butterfly pattern due to the gradual dipping in the middle of the lobes, which was similar to that in the case of the monolayer. The polarization-dependent TSHG (ΔI) was achieved by subtracting the probe-only SHG from the SHG of the deepest valley position, leading to the appearance of two new fitting parameters (r and k) associated with the crosscorrelating electromagnetic field¹⁸. The four parameters $(\alpha, \beta, r, \text{ and } k)$ used to fit the TSHG were 0.35, 4.3, 0.7, and 0.01, respectively, even though the final term was quite negligible, which caused the elimination of the $\chi^{(2)}$ term in the signal. The intensity decrease was most drastic at ~45° from the b axis, resulting in the formation of four-fold



symmetry petals due to the dominance of the β term in Eq. (2). This $\chi^{(3)}$ -dominant event is analogous to the case of the four-fold polarization dependence of MoS₂ TSHG spectroscopy when the polarization of the beam was rotated²³. No clear evidence proving the presence of structural disordering by monitoring the polarization dependence of further probe delay conditions was noted.

The carrier dynamics of the bulk region was investigated using a 13L sample with a pump fluence of 0.6, 1.3, 3, and 8 mJ/cm². The results are summarized in Fig. 3a. A clear decay-to-rise trend near the zero probe delay, followed by a gradual recovery of the SHG response, was obtained for each fluence. The maximum power level employed to perform our study was set below the Mott transition fluence condition $(\sim 10 \text{ mJ/cm}^2)^{23,32}$. The fluences applied in our experiment were high enough to produce photoexcited electrons in the range of $10^{12}-10^{13}$ cm⁻²²¹. The SHG images captured at the zero probe delay position for each of the pump powers are presented on the top right of Fig. 3a (refer to Figure S8 for detailed pump fluence-dependent TSHG images, Supporting Information), confirming the damage-free conditions of the ReS₂ crystals exposed to the aforementioned power levels. Further, as the power level increased, the dip near time zero further increased; a large number of carriers excited to the conduction band gradually affected the structural modulation because the injecting pump fluence was close to the level of one photon absorption per unit cell (~10 mJ/cm²)^{23,29-32}. Prior results illustrated that intense femtosecond laser pulses can agitate the second-



order susceptibility of bulk inorganic semiconductors, such as GaAs and InSb, at a different time scale^{29,30}. Additionally, the evolution of a highly populated state with a higher laser fluence (8 mJ cm^{-2}) is likely to cause a long recovery time (>0.5 ns)²³.

A zoomed-in view of the TSHG profile in the inset demonstrates that all the electronic decay dynamics roughly occurred within ~0.5 ps, while the slight initial rise observed in the 8 mJ/cm² excitation is likely related to the pseudoexcited state absorption caused by the temporally populated electrons (~10¹³/cm²) in the conduction band. Additionally, the carrier lifetime is inversely proportional to the input pump energy, as illustrated in the bottom right of Fig. 3a. This result is in agreement with the defect-assisted Auger recombination model $(dn/dt = -R_c \times n \times p)$, where *n* and *p* are the electron and hole densities, respectively; R_c is the recombination constant) when the electron and hole densities are identical^{33,34}. Further, the direct band transition and the subsequent radiative electron-hole recombination are restricted to the bulk system; thus, the generated heat is more likely to be consumed in the form of phonons or Auger recombinations¹⁸. However, the phonon-assisted carrier recombination is effectively activated when the lattice temperature is highly elevated. Therefore, the Auger recombination process will play a predominate role in relaxing the excited electrons that must have originated from the effect of the weak electron coupling of the

interlayers of the ReS₂ crystals in comparison with that of the multilayer MoS₂ crystals. In addition, the Auger recombination process is known to be an important mechanism to capture not only free but also bound electrons. Sun et al.³⁵ suggested a simple kinetic model $(dn_x/dt = -R \times n_x^2)$ to explain the dynamics of the exciton-exciton annihilation in monolayered MoS₂, where the solution could be represented as $n_r^{-1} \propto \text{flu}$ ence⁻¹ $\propto R \times t$. Here, the exciton density (n_x) is inversely proportional to the carrier lifetime (1/t) for a certain level of photoexcitation. The parameter R represents the recombination rate constant ($\sim 0.7 \text{ cm}^2/\text{s}$), which is approximately one order of magnitude larger than that of the MoS₂ monolayers (Figure S9 in Section 5, Supporting Information). The defect states of the bulk ReS₂ systems were also investigated using laser power-dependent PL emission ($\lambda_{ex} = 520$ nm), which confirmed the presence of defect state emission and the band edge exciton, and the anomalous broadening of the PL spectra obtained at a high excitation power indicated the influence of the defect states (Supporting Information, Figure S7 and S10)³⁶.

Subsequently, the variation in TSHG spectra from 2- to 16-layer samples was studied (Fig. 3b). Optical and TSHG images representative of the different delay positions are illustrated on the top of Fig. 3c (see also Figure S11, Supporting Information). Sharp decays before time zero were noted again, within a period of $\sim 2 \text{ ps}$ (I), regardless of the sample thickness in the case of an identical (~1 mJ cm^{-2}) pump fluence. In this short temporal range, the SHG recovery could be significantly influenced by electron-electron scattering, defect ionization, and/or the thermalization of the photoexcited carrier by optical phonon emission^{21,33,34}. For all sample thicknesses, an inflection in the TSHG spectra (change in the rapid-toslow recovery trend) was observed between 2 and 5 ps of probe delay (II). The region labeled "III" exhibited a gradual damping of the electron recovery process as a function of the increasing layer thickness, indicating the prominent feature of a slow three-body Auger recombination process within the bulk system. We fitted the observed transient features of the TSHG curves with the second exponential terms after the inflecting points (red solid lines). The fitted lifetimes and layer thicknesses are summarized at the bottom right: 2L, 68 ps; 3L, 88 ps; 5L, 106 ps; 9L, 113 ps; 13L, 124 ps; and 16L, 135 ps (refer to Figure S12 for details about the biexponential fitting, Supporting Information). The observed time scales demonstrate an interesting relation with the layer number, similar to that observed for the MoS₂ layers, indicating that the carrier lifetime variation is caused by the combination of the surface and bulk Auger-related recombination. To balance the surface and bulk contributions, we additionally assumed a model based on the probability density of electrons, similar to that in the MoS_2 case^{33,34} (details are provided in Section 6 of the Supporting Information). The values calculated for *T* matched the experimentally observed lifetimes, as depicted at the bottom of Fig. 3c, which indicated that the lifetime of the carrier was strongly controlled by the defect states of the ReS₂ crystal, as previously reported for MoS₂, except for a slight appearance of the long three-body Auger recombination process (1 ns level in MoS₂).

In the following section, we discuss the mechanisms of the electronic transitions observed in the TSHG spectra of the bilayer ReS₂ crystals. As discussed above, the usage of a pump energy under excitonic resonance conditions (1.57 eV) and a probe energy (1.19 eV) targeted to 2.38 eVcaused the formation of a decay-to-rise TSHG profile. This tendency is opposite to that observed in the case of an MoS₂ crystal measured under corresponding excitonic resonance conditions (near 1.8 eV)¹⁸. To understand the different electronic transitions, in addition to the aforementioned ones, we employed a new wavelength-fixed pump (2.38 eV) associated with tunable probe beams (1.3-1.41 eV). The extracted TSHG spectra were normalized and organized to better understand Fig. 4a; the corresponding optical and SHG images are illustrated at the top. A modulation in the probe energy clearly affirmed the distinct change in the trend from decay-to-rise (1.30–1.34 eV) to rise-to-decay (1.37–1.41 eV). Those changes are not simply due to the probe energy dependent anisotropic TSHG as we confirmed by measuring the angle-dependent TSHG for the two different (1.3 and 1.41 eV) probe condition (refer to Figure S13, Supporting Information). A similar change in the rise-to-decay profile to a decay-to-rise profile was observed in the TSHG spectrum of the monolayer MoS₂, which seems to be related to the existence of an energy state that allowed for excited state absorption (ESA) at 6.02 eV from the HOMO state; the states vanished at 7.76 eV^{23} . However, the recovery time (stage II) of the rise-to-decay profile was approximately doubled compared with that of the decayto-rise profile reported in the literature, which is in contrast to the trend observed in our study. The competition between GSD and ESA may be slightly biased towards GSD with 1.30 eV (at 4.98 eV), which allows for bleaching of the ground state with a limited efficiency. Additionally, the gradual appearance of the rise-to-decay trend in the early stage of the TSHG profile with a 1.34-eV probe (at 5.04 eV) implied that the competition between GSD and ESA is time-dependent, where the initiated GSD switched to ESA for 1 ps, followed by a sudden return. Further, to specify the ground state absorption of the probe pulses within the electronic bands of the ReS₂ crystal, we measured the reflection spectra of 2L ReS₂, as depicted in Fig. 4b. The spectra reveal that the pump beam at 2.38 eV can be strongly absorbed, whereas the linear absorptions of the probe beams are negligible, irrespective of the



allowance of their absorption induced by the two-photon action in the 2ω region. Based on the experimental absorption data and postulates regarding the behavior of the SHG probe reported in the literature, we suggest two schemes that can distinguish between the decay-to-rise and rise-to-decay profiles in Fig. 4c. We assume that the pump beam used up ground state electrons assigned for generating SHG by 1.30 and 1.34 eV probe beams, leading to the decay-to-rise profile. Further, an additional ESA is allowed in the cases that exhibited the probing of 1.37 and 1.41 eV due to the presence of a certain transition-permitted energy state. Note that the ESA corresponds to an "increment" in SHG due to the additional signal of the probe beams induced by ESA in addition to the intrinsic SHG without the pump source.

Along with the GSD domination in the TSHG profile when combining the 1.57-eV pump with the 1.19-eV probe, the alternating appearances of ESA and GSD with a probe beam difference of only a few tenths of meV should be verified. The allowance of an electronic transition could be directly determined using the angular momentum conservation rule ($\Delta L = \pm 1$). However, unlike populated homogeneous molecules with fixed eigenstates, the highly degenerate electron structures of 2D materials prevent the precise elucidation of the selectivity of their electron transitions. Therefore, we initially performed DFT calculations, implemented using the Vienna ab initio simulation package (VASP) code, to determine the availability of quantum states for each pump and probe absorption. The band structures theoretically calculated for 2L ReS₂ are depicted in Fig. 5a (refer to the Supporting Information for calculation details). The results exhibit that the minimum direct band gap is \sim 1.40 eV at the Γ point, which matches the electronically measured and theoretically calculated values reported in the literature^{8,9}. In fact, this value is somewhat lower than the excitonic resonance (1.57 eV) optically measured for the 2L ReS_2 crystal and can be adjusted by a compressive strain of ~2%, reaching 1.53 eV, an ~2.5% difference from 1.57 eV with the upper band structure intact. Notably, the calculation predicts that there is an additional small-size band gap (~0.5 eV) above the band gap at the Γ point (4.55-5.05 eV from the HOMO). Given the 1.57-eV pump, the interband transition of electrons was seemingly dominated by the p-d transitions. The ESA behavior was not experimentally permitted, although many degenerate electron states existed above the bottom edge of the conduction band by as much as 2.38 eV (i.e., 3.95 eV



above the ground state), as summarized in Fig. 5a. To explain this phenomenon, we categorized the degenerate conduction band states according to the subshell orbital types (Fig. 5b, c), among which most comprised Re d and s and S p orbitals. Note that the populated electrons at the bottom edge of the conduction band excited by a pump energy of 1.57 eV have a limited probability of being probed by SHG because the involved electronic transition is triggered by instantaneous two-photon absorption via the d-d transition path, which is forbidden based on the selection rule ($\Delta L = 0$). More specifically, the dominance of the *d* orbital (\sim 70%) at the bottom edge position is retained (~65%) at the electronic transition level of the second probe absorption (3.95 eV from the ground state), which further limits the appearance of ESA. Additionally, a 1-eV gap at the Γ position is another factor that restricts the fast electronic transition without the assistance of the optical phonon. Once the electrons are excited in the case of a 2.38-eV pump, the two-photon absorption by the 1.41-eV probe photon will successfully occur based on ΔL = 1 in the transition from d (L = 2) to the hybrid orbital of Re *s* and S p (5.10 eV from the HOMO band) because the

hybrid orbital is characterized by the antibonding of Re *s* and S p and the L = 1 channel dominates the angular momentum expansion due to its antisymmetry.

$$\left|\phi_{s}^{Re}\phi_{p}^{S}\right\rangle^{*} = C_{L=1}|L=1\rangle + C_{L=3}|L=3\rangle + \dots \dots \dots (3)$$

A schematic based on the aforementioned calculation is shown (Fig. 5d) to better understand the hybridization of the Re *s* and S *p* orbitals and the related electronic density of the states that comprised the Re *s* and S *p* and Re *d* orbitals. However, the same two-photon action is unlikely to occur when using the 1.30-eV probe because the position located at a distance of 4.98 eV from the HOMO band is located in the upper band gap. Note that the Re *s* orbitals at ~5.10 eV are highly populated compared with the Mo *s* orbital density in the case of the MoS₂ system based on our calculation, where the direct band gap is located at K (data not shown).

Discussion

We demonstrated the possible existence of a 0.5-eV band gap at a distance of 4 eV from the ground state of the

bilayer ReS₂ crystal using time-resolved TSHG microscopy. We initially investigated the lower part of the gap using a 1.19-eV probe (2.38 eV SHG) and wavelengthvariable pump photons from 1.41 to 1.72 eV. Here, the probe-only thickness-dependent SHG gradually plateaued in the ~13-nm layer and was closely modeled using the dipole summation and self-interferometric absorption mechanisms; the polarization dependence of the SHG varied in a layer-by-layer manner, following the model designed for the distorted 1T crystal. Each layer exhibited maximized GSD behavior in the presence of the 1.57-eV pump beam (corresponding to the nondegenerate direct band gap), with excitonic lifetimes that were typically modeled as Auger-assisted surface-dominant electron-hole recombination. Time-dependent rise-todecay behavior (i.e., the ESA condition) was not observed because the two-photon transition (2.38 eV) that followed band gap pumping (1.57 eV) corresponded to the forbidden intraconduction band d-d transition. Finally, the usage of a frequency-doubled pump (2.38 eV) and various probe energies (1.37-1.41 eV) enabled us to perform analysis at a distance up to 5.2 eV from the ground state, thereby revealing a new allowed ESA at ~5.05 eV. The modified VASP-type DFT calculations revealed that this transition is strongly related to the "allowed d-s transition" and further confirmed the existence of another gap with a size of ~0.5 eV. Our microscopic visualization based on the thickness-dependent modeling of the SHG, spatiotemporal assessment of carrier dynamics, and confirmation of the existence of a higher energy band gap of ReS2 crystalline systems ascertained the benefit of TSHG microscopy for understanding the fundamental physical properties required to design new optoelectronic devices based on TMD and van der Waals-related heterostructures.

Materials and methods

Sample preparation and optical characterization

Single crystals of ReS_2 with various layer thicknesses were exfoliated on a Si/SiO₂ substrate from a commercially available natural crystal (2D semiconductor company). These crystals were directly used to study the Raman, PL, absorption, and nonlinear optical properties at room temperature. Details of the instrumentation for the optical properties and correlated electronic band structure are provided in Supporting Information Section 1.

Theoretical calculation

We employed the first-principles electronic structure calculation performed on the VASP code with the Perdew–Burke–Ernzerhof (PBE) generalized gradient approximation (GGA) exchange correlation functional^{37–39} and a Monkhorst–Pack⁴⁰ grid of a $9 \times 9 \times 1$ k-points

mesh. An energy cutoff of 500 eV was adopted. The freestanding bilayer $1T' \text{ ReS}_2$ was calculated with Dudarev's DFT + U⁴¹ correction of 5 eV for the *p* orbitals of S atoms.

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Author contributions

H.K., J.L., and J.-H.A. planned and supervised the project. K.P.D. prepared all the samples. K.P.D. and H.K. conducted all experiments. S.L. and Y.K. performed the theoretical calculations. K.P.D., J.-H.A., H.K., and J.L. analyzed the data and wrote the manuscript.

Conflict of interest

The authors declare that they have no conflict of interest.

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