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PROGRAM DESIGN WITH ABSTRACT DATA TYPES

Lawrence Flon

Carnegie-Mellon University

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Program Design With Abstract Data Types

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Abstract data types modularization specification

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Summary

Acknowledgement

Introduction

This paper explores the use of abstract data types as a modularization and structuring technique in the design of programs, particularly large: programs including compliers and operating systems. The emphasis is on design. The particular language in which the program will be coded should be of relatively little importance in the design process. We are interested in a technique for constructing specifications which can be converted at another time (and possibly by others) into an implementation. Programming languages which provide data type facilities to varying degrees have been in existence since about 1967 when SIMULA-67 [1] appeared. Since then, there has been an ever increasing number of such languages, notably ALGOL-68 [7], PASCAL [8], and EL1 [6]. There are more advanced languages currently under development or proposed, including ALPHARD [9], CLU [3], and PASQUAL[5]. A useful bibliography of papers concerned with data types and programming languages may be found in [5].

Abstraction refers to the mental process which, when confronted with a set of objects, can distinguish some objects from others on the basis of what they have in common. What is "abstracted out" is a unifying theme, called the type of those objects. To pick a conventional example, the set { 7, 1.35, -6, 'A', 0.3E6 } contains three types of entities: integers, reals, and characters. These are types which just about every programming language provides. More abstractly, the set contains only two types: numbers and characters. Even more abstractly, it contains only one type - constant. When we prefix "data type" with "abstract" we mean an arbitrarily complex type which characterizes a certain kind of behavior.

The concept of using abstractions in programs to control complexity is certainly

not a new one. For very small programs it is sufficient to use a straightforward control flow through the program statements. Slightly larger to medium sized programs require the use of procedures to group individual statements in a logical manner, while a main program directs the flow of centrol among the various top-level procedures. When dealing with large programs it becomes necessary to group the individual procedures into modules. The process by which this should be done is not yet universally understood. This paper expresses the view that the use of data types as a modularization principle is the right approach.

We will begin by discussing what it means to define a new data type and will describe some basic data structuring mechanisms. Numerous examples are given to familiarize the reader with the notation, building up to the final example involving the classion of a directory system.

1) Type Definitions

A type definition has two basic attributes:

- 1) functional specification: the behavior of a particular class of objects as seen by users of that class.
- 2) algorithmic specification: the means by which that behavior is accomplished.

The distinction between functional and algorithmic specification is most important. First, it allows programmers to construct implementations in parallel with one another without any more information in common than their mutual interfaces. Second, it ensures that a change in data structure or algorithm is localized as long as

the functional specifications remain unchanged. A type definition is really a module in the sense of the information boundaries discussed by Parnas [4]. It provides a clear design procedure for the modularization of a large program or system, where one has been previously lacking.

Language defined types such as integer, roal, and boolean are called scalar types. The term scalar is intended to signify that values of such a type are considered to be indivisible. The scalar type integer characterizes single values taken from the range {-n,...,n}, in conjunction with a set of operations which may be applied to integers, such as addition, subtraction, multiplication, etc. As far as a user of type integer is concerned, he should not know about, and more importantly not rely on, the way in which integers are represented or the particular algorithms which implement integer arithmetic on his computer. Adhering to this principle makes program portability possible, since different machines may use different algorithms. We generalize these notions to abstract data types and say that a type definition consists of:

- 1) a representation for objects of the type, known only to the definition itself (algorithmic specification).
- 2) a set of operations which manipulate this representation, the names and calling sequences of which are known to users of the type (functional specification), but the algorithms of which are known only to the definition itself (algorithmic specification).

The binding of operations to particular types is vital to the description of behavior. It is not enough to present a picture of a control block as the description of a "process" in an operating system. What is necessary is an explanation of exactly

what can be done to a process, and specifically <u>not</u> how it is done. In fact control block formats should not be disseminated at all; rather only a description of valid operations which can be used on that data structure should be provided to users. One of the most important things gained from this is the "sanctity" of a data structure. Every data structure may be viewed as having an invariant relation which it is characterized by (e.g. the mathematical notions of "list" and "tree"). It is easier to verify the invariance of this relation if the relavant changes to the structure are made by a small number of "privileged" procedures. If you parcel out a data structure address and the right to modify arbitrary fields in arbitrary ways, it is possible (likely, in a brand new program) to find inconsistencies in the structure due to program bugs anywhere in the entire system. If all the information that is distributed is operation names, the scope of possible sources of error is greatly reduced to the implementation of those very operations.

The next sections present a set of tools useful for the description of data abstractions, and introduce some relatively intuitive syntax.

2) Enumeration Types

Often in the course of writing a program in a standard language, a programmer will find the need to express values of scalar types which are not provided by the language. For example, one might find an inventory program which, in order to identify the color of an object, uses integers to represent red=1, yellow=2, etc. When designing this program, it is not relevant to define the mapping between colors and integers, since this is merely an implementation detail. A mechanism is needed for defining a new type by exhibiting the set of constants which comprise its values. A

type so defined is called an enumeration type, the concept having been taken from PASCAL. An example of the definition of enumeration types might be:

type color = {red,yellow,blue,green} end;

type weekday = {monday,tuesday,wednesday,thursday,friday} end;

In order to declare variables as instances of particular types, we will use syntax of the form:

declare payday,dayoff:weekday, shade:color;

The declaration states that payday and dayoff are variables which may only possess values appropriate to type weekday, and that shade can only possess a value appropriate to type color. These variables behave as do more common scalar variables with respect to their appropriate constants. For example,

payday ← wednesday;

would be valid, but

payday ← red;

would be meaningless. Operations are defined for enumeration types as for example,

type color = {red,yellow,blue,green}

op complement(c:color):color =

case c of

begin red:

green;

yellow: blue;

green: red;

blue: yellow

and

end;

The operations provided by a type are declared inside the scope of the definition in order to exhibit modularity. The brackets type and end delimit the definition. To use one of these operations in a program description, it is necessary to prefix the operation name with the type name in order to permit several types to have operations with the same name (and for readability). The complement operation takes a single parameter of type color and returns a value of the same type. For example, if the statements

shade←green; shade←color.complement(shade);

were executed, shade would obtain the value red. Even though in most languages an implementation of these types will require the use of Integers, nevertheless the irrelevance of the mapping may be preserved by declaring macros (or variables) for use in place of the integer constants.

3) Composite Types

Given the ability to define new scalar types, we must now be able to build upon those definitions to define more interesting types.

Consider as an example the definition of the type complex. We wish to represent numbers in the complex plane and provide arithmetic operations on them.

We need to specify to use:s that the operations

add(w,z:complex) complex
mul(w,z:complex):complex
create(a,b:real):complex

will be available. Add will take two complex values and produce the complex sum. Mul will behave analogously. Create will form a new cumplex value equal to a+bl. In terms of algorithmic specification, we can represent a complex value by its real and Imaginary parts. Consider the following definition:

type complex = declars r,i:real;

op add(w,z:complex):complex =
 begin
 declare sum:complex;

sum.r←w.r+z.r; sum.i←w.i+z.i; return sum end;

```
op mul(w,z:complex):complex =
begin
declare prod:complex;

prod.r←w.r*z.r-w.i*z.i;
prod.i←w.r*z.i+w.i*z.r;
return prod
end;

op create(a,b:real):complex =
begin
declare c:complex;

c.r←a; c.i←b
return c
end
end;
```

The body of the definition contains some variable declarations (r and i) and some operation definitions (add, mul, and create). When a variable of type complex is declared, e.g.

declare x:complex;

or dynamically allocated, e.g.

complex.create(1,2)

the variables inside the definition of complex are allocated, just as when an integer variable is declared the bit string by which it is represented is allocated. From outside the definition it appears that x is an atomic entity to be used with the operations provided, e.g.

complex.add(x,y).

From inside the type definition, as within, say, the microcode which implements integer arithmetic, the structure of x is visible. In this case the structure consists of the variables r and i. To access a particular structure, it is necessary to specify which structure by prefixing the variables with the name of a complex variable. For example, the use of w.r in the body of the add operation refers to the r part of the complex object w which was passed in as a parameter. The use of sumi refers to the I part of the locally declared complex object sum. An implementation of this type in a language with dynamic storage allocation will be straightforward, i.e. it will be possible to return a pointer to a newly allocated structure representing the result of an operation. In other languages it may be necessary to write the operations as subroutines, passing the destination variable as an output parameter. In FORTRAN, storage allocation could be simulated by declaring an array of pairs, each index into the array representing a single complex value. The informal language in which these examples are presented assumes that functions can return values of arbitrary types.

An example of the use of type complex might be:

declare x:complex;

x←complex.add(complex.create(1,-2), complex.create(2,3));

which would result in x acquiring the value 3+i.

Note that we were not <u>forced</u> to represent complex values in terms of their real and imaginary parts. We are free to re-design the type definition as long as we conform to the stated specifications of the operations. For example, we might decide to use polar coordinates to represent a complex value, if that made the operations more efficient. Although the create operation is still specified to produce the value

a+bi from parameters a and b, there is nothing to prevent it from internally converting to any other representation, and there is certainly nothing to prevent us from writing a different create operation which expects arguments with a new significance. e.g.

type complex =
declare r,theta:real;

op create(a,b:real):complex =
begin
declare c::complex;

c.r ← sqrt(a + a + b + b);
c.theta ← arcsin(b/c.r);

return c end

end:

In addition to the allocation of the structure variables, when a variable of type complex (or any type) is declared, the create operation is implicitly invoked. This is important in order to allow the data structure invariant relation (if there is one) to be established. Although in this simple example this is unnecessary, it will become necessary later on.

4) Data Structuring

A comprehensive presentation of data structuring methods in relation to types may be found in [2]. We will discuss briefly some structuring mechanisms in order to have some syntactic base upon which to build.

4.1) Arrays

In the past, an array has generally been thought of as a table indexed by Integers, as is the case with a matrix. A matrix, however, is a type, having certain operations such as multiplication and inversion defined for it. An array is only a structuring mechanism and might as well be generalized to a more powerful mapping than is possible with just integer domains. Think of the array as a mapping from any finite scalar type to any type at all. For example,

declare A:array[color] of integer;

declares a vector which is indexed by objects of type color and whose Individual elements are integers. We could use such an array to represent the frequencles of the various colors of light, e.g. A[red] = 6485.

A two dimensional array can be modeled as a vector of vectors, e.g.

declare A:array [1:10] of array[1:5] of real;

so that A[i] denotes a row (or column, depending upon the Interpretation).

4.2) Records

Another means of grouping values is the record structure. The local data of any type declaration can be thought of as a record. The variable of the local data denote the fields of the record. These fields are accessed as previously noted, by prefixing the field name by the name of the complete object. While arrays are used to

group values of the same type records are used to group values of potentially differing type. Often records are used to structure data in a hierarchical manner, as in PL/I or COBOL. For this facility we will use the notation

declare r:record
$$(f_1:t_1,f_2:t_2,...,f_n:t_n);$$

to declare a variable r which has n subfields $(r.f_1,r.f_2,...,r.f_n)$ of types $(t_1,t_2,...,t_n)$ respectively. The t_i can be arbitrary, including other records. For example,

declare person:record (name:string, age:integer, salary:record (regular:real, overtime:real));

The subfields of this variable are person.name, person.age, person.salary.regular, and person.salary.overtime. It is possible to declare a table as an array of records, e.g.

doclare T:array[1:100] of record (height, weight:integer);

in which case the fields would be accessed as T[i].height and T[i].weight. In general, however, if a record is to be used in any non-trivial way, it should be embedded in a type declaration, e.g.

declare T:array[1:100] of medicalrec;

where medicalrec defines the fields of the record as local data and provides operations on that data. Since it is not unlikely that the structure of medicalrec will change at

some point during system development, in this way we anticipate modifications by restricting their scope.

4.3) References

A reference value is a pointer to an object, with the restriction that reference variables can only reference objects of a single type. Typeless pointer variables are the cause of many program bugs since they are free to point to arbitrary addresses. References are much safer to use and make programs less devious in their logic. The reference concept is important with regard to the use of a dynamic storage allocation mechanism. We postulate the operations new and free for every data type, but make them available for use only inside of a type definition. This is because of the need for initialization of the data structure invariant relation discussed in section 1. From outside of a type definition, the create operation must be used.

If c is a reference to complex, i.e.

deciare c:ref complex;

then, inside of type complex, the statement

c←new complex;

causes the dynamic allocation of a complex object, and assigns a reference to that new object to c. The statement

free c;

results in the storage referenced by c being released. All that we can do with the value of c is to assign it to other ref complex variables or pass it as a procedure argument, since as yet we have not defined any operations for reference types. In particular, we will not allow statements such as

c+c+2;

which are likely to introduce errors. More importantly, these statements violate the notion of type, since if the address contained in c is incremented by 2 it probably no longer is the address of a complex variable. We will define an operator for references called dereferencing, which converts a reference into the object it references. If c contains a valid reference, then c1 is of type complex. For example, c1 is the r field of the complex object referenced by c. It is not legal to write c.r, since c is not of type complex. This imposes more structure on the program specifications and prevents many possible bugs. Our examples assume that 1 applies to the reference immediately to its left. We will use the reference value null to indicate that no object is currently being referenced.

5) A Small Abstraction

With the tools just presented, we can begin to describe some simple abstract objects. Suppose we would like to model the concept of a "bag" full of data, in the sense that once a datum is inserted in the bag, it can only be removed by trial and error, since "reaching your hand" into the bag is done blindly. Assume that the bag is to hold integers.

We need to provide certain key operations, namely:

empty(b:bag):boolean put(b:bag,i:i:iteger) take(b:bag):integer

and we would like to guarantee to the external world that a "taken" element is chosen at random. There are several ways to specify this type. One way is to use a vector to represent the state of the bag, although we have to place an upper limit on the size of the bag. Consider:

type bag =

declare A.array[1:100] of integer,
top:integer;

op create:bag begin declare b:ref bag;

> b←new bag; b1.top←0; return b1 end;

So far we have specified that a bag will consist of a vector of length 100 (A), and an integer (top) which we will use to indicate the current size. We have specified the create operation, since here it is necessary to perform initialization. The invariant relation of a hag is "the bag contains (top) elements" so we must set top to zero whenever a bag is created. If we had allowed the new operation to be used outside of the type definition, top could remain unitialized.

We can specify the empty and put operations easily:

```
op empty(b:bag):boolean = return (b.top=0);

op put(b:bag,integer) =
    if b.top=100 then error comment overflow;
    else
        begin
        b.top+b.top+1;
        b.A[top]+i
        end;
```

Assuming a uniform random number generator, take can be specified as:

```
op take(b:bag):integer =
if b.top=0 then error comment underflow;
else
begin
declare k,i:integer;

k+randint(1,b.top);
i+b.A[k];
b.A[k];
b.A[k]+b.A[top]
b.ton+b.top-1;
return i
end
end of type bag;
```

If we desire to remove the restriction on the size of a bag, we can store the bag contents in a list. To define a list of integers, we need to define each node in the list and the rules for connecting them. We will first specify type node, so that we can use its general purpose operations to manage a list:

type node =

declare val:integer,
next:ref node;

op create(i:integer):node =
begin
declare n:ref node;

n←new node;
n1.val←i;
n1.next←null;
return n1
end;

op destroy(n:node) = free n;

The operation called follow causes node1 to point at node2:

op follow(node1,node2:node) = node1.next←node2;

Operation successor returns the current next value of nodel:

op successor(node1:node):node = return node1.next1;

and operation value returns the current integer value of node1:

op value(node1:node):integer = return node1.val
end of type node;

A useful type of list for the purpose of defining type bag is a circular list, so that a random choice from a bag is accomplished by "spinning" the list before deletion.

A circular list of integers defined using type node could be:

```
type clist =

declare current:ref node,
size:integer;

op create:clist =
begin
declare c:ref clist;

c←new clist;
c↑.current←null;
c↑.size←0;
return c↑
end;
```

The insert operation maintains the proper circularity:

```
op insert(i:integer,c:clist) =
     begin
     declare t,n:ref node;
     c.size+c.size+l;
     n←node.create(i);
     if c.size=0 then
           begin
           c.current←n;
           node.follow(c.current1,c.current1)
      else
           begin
           t←node.successor(c.current1);
           node.follow(c.current1,n1);
           node.follow(n1,t1)
           end
      end;
```

The circular list spin operation can be defined as:

and the remove operation (which deletes the element after current) as;

```
op remove(c:clist):integer =
     begin
     declare
               t:ref node,
                k:integer;
                              comment underflow;
     if c.size=0 then error
     else if c.size=1 then
          begin
           k←node.value(c.current1);
           node.destroy(c.current1);
           c.current-null;
           return k
           end
     eise
           begin
           t←node.successor(c.current1);
           node.fcflow(c.current1,node.successor(11));
           k←node.value(t1);
           node.destroy(11);
           return k
           end
     end:
```

One more useful operation will tell us if the list is empty:

```
op empty(c:clist):boolean = return (c.size=0)
end of type clist;
```

Now type bag can be simply defined as:

```
type bag =
    declare c:clist;

comment the create operation for a clist performs the
        necessary initialization for a bag;

op empty(b:bag):boolean) = return clist.empty(b.c);

op put(b:bag,i:integer) = clist.insert(i,b.c);

op take(b:bag):integer =
        begin
        clist.spin(b.c);
        return clist.remove(b.c)
        end

end of type bag;
```

Note that we have completely re-designed the algorithmic specification of type bag, but left the functional specifications unchanged. Any user of type bag would not have had his programs affected (except for the size restriction having been removed). Note also that the intermediate types node and clist can be re-used in the specification of other list structures or more abstract types such as bag without the need for duplication of code or effort. In addition, the three types make up three modules suitable for independent programmer work assignments.

6) Parameterization

As we mentioned in the introduction, abstraction involves the noticing of similarities. This requires that things which may be potentially dissimilar among a group of objects have a wide range of freedom of variation. The use of parameters to procedures is necessary to convey the notion of abstract operation. The "square" operation gains its usefulness because it will square any number. When types are given parameters, they acquire much wider applicability in a similar way.

A parameterized type is called a *type constructor*, since the types resulting from different parameter values may be widely differing. Consider the definition of type string in terms of the primitive type character:

A type constructor may be thought of as a macro. When its actual parameters are specified, it completely defines a new type. In the declaration of r in string.concat, the parameter to its type is given as (s.len+t.len). A vector of this length (A) is allocated, along with a word (len) containing this value. If not for the ability to parameterize a type definition, we would have to define a new type string for every possible string length!

Even more important is the ability to use type names as parameters to type definitions. In our previous example, we made the unfortunate (and irrelevant) committeent that the objects contained in a bag must be integers. If, however, we had written the definition of bag as:

type bag =
 declare c:clist(integer);

etc.

end:

we would be using a much more general notion of list. In fact, there is no reason to restrict a bag to only integers:

type bag(t:type) = declare c:clist(t);

etc.

end;

with t replacing all occurrences of integer. Type clist would be defined in the same way as before, except that the type of the variable called current would be determined from a parameter, as would the type of the variable called val in type node.

It would not be hard to implement the notions of bag and clist in a language with dynamic allocation and pointer facilities. In other languages it might be necessary to re-implement them for every different parameter value (e.g. using arrays), but at least the <u>specifications</u> do not have to be re-done.

In general, parameterization gives us the ability to precisely describe such concepts as stack, queue, tree, etc., without tying clown the types of values which are not important to the <u>structure</u> of the data.

7) A Larger Design Example

A data type having many applications in systems programming is the <u>hash table</u>. For this discussion, we characterize a hash table by the type of object used to Index the table, by the type of object stored in the table, and by the number of buckets provided:

type hashtable(buckets:integer,index,result:type) =

Each bucket contains a list of elements with the same hash value. Each element is an (index,result) value pair. Assuming a type pair which we can use to group two values of arbitrary type:

and assuming a definition for type list similar to LISP:

end;

```
type list(t:type) =
    declare p:ref pair(t,list(t));
    op head(I:list(t)):t = return pair.leftval(I.p1);
                comment LISP car;
    op tail(I:list(t)):list(t) = return pair.rightval(I.p1);
                comment LISP cdr;
    op cons(tv:t,lv:list(t)):list(t) =
          begin
          declare q:ref list(t);
          q←list.create;
          q.p←pair.create(tv,lv);
          return q1
          end;
    op create:list(t) =
          begin
          declare I:ref list(t);
          I←new list:
          I1.p←nuli;
          return IT
          end;
    op empty(I:list):boolean = return (I.p=null)
    end;
```

we can specify the structure of a hashtable as:

declare A:array[1:buckets] of list(pair(index,result));

In order to find a result value given an index value, the appropriate array element must be found using a hash function. Then the list must be searched for the index value. Since the hash table module knows nothing about the representation of values of type index, it is up to index itself to provide that hash function. For example,

in the case of indexing by strings, we would expect to find the operation string, hash defined. We can then define the hashtable find operation as:

op find(h:hashtable,i:index):result =
 return search(i,h.A[1+(index.hash(i) mod upperbound(h.A))]);

where search is a procedure (local to type hashtable only) to scan the list:

procedure search(i:index,l:list(pair(index,result))):result =
 begin
 declare p:list(pair(index,result));

p←l;
while not list.empty(p) do
 if pair.leftval(list.head(p))=i then
 return pair.rightval(list.head(p))
 else p←list.tail(p);

return result.undefined end;

Note that if the search procedure does not find the index on the list, it returns the undefined value of type result - a convenient way to indicate an error to the caller. This of course assumes an operation called "undefined" for type result.

It now remains to be able to insert values into the hash table. The Insert function must search the appropriate list and only add to the list if the value is not already there:

```
op insert(h:hashtable,i:index,r:result):boolean =
begin
declare n:integer;

n←1+(index.hash(i) mod upperbound(h.A));

if search(i,h.A[n])=result.undefined then
begin
A[n]←list.cons(pair.create(i,r),A[n]);
return true
end
else return false
end;
```

Finally, the creation of a new hashtable requires some initialization:

```
op create:hashtable =
begin
declare h:ref hashtable(buckets,index,result);

h←new hashtable;
for i from 1 to upperbound(h1.A) do
h1.A[i]←null;

return h1-
end
end of type hashtable;
```

8) A Directory System

To illustrate the power of systems design using data types, we have chosen as our final example a hypothetical directory system as might be found in an operating system.

The directory system to be designed will be a hierarchical one, in which a node name consists of a path through the directory structure to the appropriate descriptor.

For example, the name A.B.C refers to directory A, subdirectory B, descriptor C. There should be no a priori bound on the number of directories, nor on the depth of the hierarchy. We will not restrict the definition to that of <u>file</u> directory, since the notion of file is not relevant to the structure. The purpose of the directory is to associate an object of type descriptor (maybe filedescriptor) with one of type path. The operations provided for directories should include <u>lookup</u> and <u>insertion</u> functions. If we think of a path name as a list of strings, we can define type path as:

```
type path =
    declare l:list(string);

op first(p:path):string = return list.head(p.l);

op rest(p:path):path = return list.tail(p.l);

op empty(p:path):boolean = return list.empty(p.l);

op terminal(p:path):boolean = return path.empty(path.rest(p))
end;
```

The directory itself will contain objects which will either be descriptors or subdirectories. We will call this type directory for directory entry. The structure of a directory, then, will be a hashtable (as previously described) which is indexed by a string and which contains directory objects:

type directory(descriptor:type) =
 declare H:hashtable(100,string,direntry(descriptor));

The hashtable will have 100 buckets, but we could have left that as a parameter to directory.

In order to look up a path in a directory, we must first find the directry corresponding to the path header (via hashtable.find) and then look up the rest of the path through the directry:

```
op lookup(p:path,d:directory:descriptor) =
    begin
    declare t:ref direntry;

t-hashtable.find(d.H,path.first(p));

if t1=direntry.undefined then
    return descriptor.undefined
else return direntry.lookup(path.rest(p),t1)
end;
```

Insertion in a directory may require the creation of a directory and its insertion in the hashtable, or simply insertion in an existing directory:

```
op insert(p:path,d:directory,r:descriptor):boolean =
begin
declare t:ref direntr/;

t←hashtable.find(d.H,path.first(p));

if t↑=direntry.undefined then
begin
t←direntry.create(p,r);
return hashtable.insert(d.H,path.first(p),r)
end
else return direntry.insert(path.rest(p),t↑,r)
end;
```

Finally, the creation of a directory is accomplished by:

op create:directory(descriptor) =
 (nev/ directory(descriptor))?

end of type directory;

Having finished the definition of type directory, we must now tackie the definition of type directory. A directory has a name (part of a path) and either indicates a descriptor or a sub-directory:

type direntry(descriptor:type) =

deciare name:string,
node:boolean,
value:ref descriptor,
subdir:ref directory(descriptor);

To look up a path in a direntry which is a node requires checking that the path terminates at that point. If the direntry refers to a sub-directory, then the directory.lookup operation is recursively applied:

op lookup(p:path,d:direntry):descriptor =
 if d.node then
 if path.empty(p) then return d.value1
 else return descriptor.undefined
 else return descriptor.lookup(p,d.subdir1);

To insert a descriptor in an existing direntry, we must do the insertion in the sub-directory (if there is one):

op insert(p:path,d:direntry,r:descriptor):boolean =
 if d.node or path.empty(p) then return false
 eise return directory.insert(p,d.subdir1,r);

Creation of a new direntry (as required by the directory.insert operation) is straightforward when the path is a terminal. When it is not, creation of the direntry requires creation of a sub-directory:

```
op create(p:path,r:descriptor):direntry(descriptor) =
     begin
     declare d:ref direntry(descriptor);
     d-new direntry:
     if path.terminal(p) then
          bezin
           d1.name←path.first(p);
           d1.node←true:
           d1.subdir←null;
           d1.value←r
           end
     else
           begin
           dî.name←path.first(p);
           d1.node ←false;
           d1.value←null;
           d1.subdir-directory(descriptor).create;
           directory.insert(path.rest(p),d1.subdir1,r)
           end;
      return dî
end:
```

In the end we have a precise description of the concept of directory. This directory system may be used in conjunction with a file system (note that there is a difference between a file system and the directory structure it uses, as we have just shown). It may also be used to store objects in a protection system, or for any of a number of other applications. Each of the types directory, direntry, hashtable, etc. may be viewed as a module suitable for a programmer work assignment.

Summary

There is much confusion in the programming community today over such concepts as modularity, structured programming, specifications, etc. What we have presented here is a technique for employing all of these tools in unified form - i.e. data types. We have, of course, omitted discussion of many topics associated with data types, but have done so on the grounds that we are concerned with design and specification, and not coding. The freedom to use a specification language without constraints of particular syntax is very important.

The use of data types as a modularization principle views a module as being responsible for the maintenance of some invariance. The explicit advantage of this is that system verification may be done selectively by module. An implication of this is that most changes to the system will be restricted to a small number of modules, if not a single one.

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REFERENCES

- Dahl, O. J. et al, "Simula 67 Common Base Language," Norwegian Computing Center, Oslo (May 1968).
- 2 Hoare, C. A. R., "Notes on Data Structuring," in **Structured Programming**, Academic Press, London (1972).
- 3 Liskov, B. and Zilles, S., "Programming With Abstract Data Types," SIGPLAN Notices (April 1974) 50-59.
- 4 Parnas, D. L., "On the Criteria to be Used in Decomposing Systems into Modules," CACM 15,12 (Dec. 1972) 1053-1058.
- 5 Tennent, R. D., "PASQUAL: A Proposed Generalization of PASCAL," Department of Computing and Information Science, Queens University, Kingston, Ont. (Feb. 1975).
- 6 Wegbreit, B., "The Treatment of Data Types in EL1," CACM 17,5 (May 1974) 251-264.
- 7 van Wijngaarden, A. (ed.), "Report on the Algorithmic Language ALGOL 68," Numerische Mathematik 14, 79-218 (1969).
- 8 Wirth, N., "The Programming Language PASCAL (Revised Report)," Berichte der Fachgruppe Computer-Wissenschaften, Eidgenossische Technische Hochschule, Zurich (1972).
- 9 Wulf, W. A., "ALPHARD: Towards a Language to Support Structured Programs," Department of Computer Science, Carnegie-Mellon University, Pittsburgh, Pa. (April 1974).