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**Published on:** 16 May 2019 - bioRxiv (Cold Spring Harbor Laboratory)

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1 Propagation of cortical activity via open-loop intrathalamic architectures: a computational analysis

2  
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22 Keywords: Thalamus; thalamic reticular nucleus; intrathalamic signaling; cortical signaling; open-loop;  
23 propagation; computational model

24 **Abstract:**

25 Propagation of signals across the cerebral cortex is a core component of many cognitive processes and is  
26 generally thought to be mediated by direct intracortical connectivity. The thalamus, by contrast, is  
27 considered to be devoid of internal connections and organized as a collection of parallel inputs to the  
28 cortex. Here, we provide evidence that “open-loop” intrathalamic connections involving the thalamic  
29 reticular nucleus (TRN) can support propagation of oscillatory activity across the cortex. Recent studies  
30 support the existence of open-loop thalamo-reticulo-thalamic (TC-TRN-TC) synaptic motifs in addition  
31 to traditional closed-loop architectures. We hypothesized that open-loop structural modules, when  
32 connected in series, might underlie thalamic and, therefore cortical, signal propagation. Using a  
33 supercomputing platform to simulate thousands of permutations of a thalamo-reticular-cortical network  
34 and allowing select synapses to vary both by class and individually, we evaluated the relative capacities  
35 of closed- and open-loop TC-TRN-TC synaptic configurations to support both propagation and  
36 oscillation. We observed that 1) signal propagation was best supported in networks possessing strong  
37 open-loop TC-TRN-TC connectivity; 2) intrareticular synapses were neither primary substrates of  
38 propagation nor oscillation; and 3) heterogeneous synaptic networks supported more robust propagation  
39 of oscillation than their homogeneous counterparts. These findings suggest that open-loop heterogeneous  
40 intrathalamic architectures complement direct intracortical connectivity to facilitate cortical signal  
41 propagation.

42

43 **Significance Statement:**

44 Interactions between the dorsal thalamus and thalamic reticular nucleus (TRN) are speculated to  
45 contribute to phenomena such as arousal, attention, sleep, and seizures. Despite the importance of the  
46 TRN, the synaptic microarchitectures forming the basis for dorsal thalamus-TRN interactions are not fully  
47 understood. The computational neural model we present incorporates “open-loop” thalamo-reticular-  
48 thalamic (TC-TRN-TC) synaptic motifs, which have been experimentally observed. We elucidate how  
49 open-loop motifs possess the capacity to shape the propagative properties of signals intrinsic to the  
50 thalamus and evaluate the wave dynamics they support relative to closed-loop TC-TRN-TC pathways and  
51 intrareticular synaptic connections. Our model also generates predictions regarding how different spatial  
52 distributions of reticulothalamic and intrareticular synapses affect these signaling properties.

53 **Introduction:**

54 Propagation of activity across the cerebral cortex is thought to underlie multiple cognitive processes, as  
55 well as pathological processes such as epilepsy and migraine (1-4). Cortical regions are highly  
56 interconnected via direct axonal projections as well as via polysynaptic pathways involving the basal  
57 ganglia and thalamus (5, 6). Cortical signal propagation is generally thought to be mediated via direct  
58 cortical connections (7, 8), but recent evidence suggests that the thalamus serves as a control point to  
59 modify cortical activity during cognitive processes such as attentional shifting (9). An advantage of a  
60 thalamic mode of signal propagation is the efficiency by which modulatory influences may control  
61 thalamic, and therefore cortical, propagation. The thalamus, however, is generally thought to have limited  
62 internal connectivity and therefore limited capacity to serve as a substrate for signal propagation.

63  
64 A major intermediary allowing for communication between thalamocortical neurons, the thalamic  
65 reticular nucleus (TRN), is a sheet of GABAergic neurons that partially envelops the dorsal thalamus  
66 (10). It has been speculated to participate in phenomena ranging from selective attention (11-13) to sleep  
67 and arousal (12-15) and fear responses (16), and may play a role in generating absence seizures (17-21),  
68 symptoms of neurodevelopmental disorders (22, 23), and schizophrenia (24). The TRN projects  
69 exclusively to TC neurons, while receiving reciprocal, glutamatergic thalamoreticular (TC-TRN)  
70 connections (25).

71  
72 The structural microarchitecture of bidirectional pathways connecting the dorsal thalamus and TRN has  
73 been the subject of ongoing debate. It was originally assumed that thalamo-reticulo-thalamic (TC-TRN-  
74 TC) pathways were reciprocal, forming “closed loops” of recurrent inhibition delivered to TC neurons  
75 (Fig. 1A, left) (10, 15, 26-28). While closed disynaptic loops have indeed been confirmed, they were only  
76 identified in a minority of examined TC-TRN pairs (10, 29-33). Another connectional scheme between  
77 the dorsal thalamus and TRN is the so-called “open-loop” TC-TRN-TC pathway, wherein a TC neuron is  
78 not reciprocally inhibited by the TRN neuron it excites (Fig. 1A, right). Open-loop configurations have  
79 been inferred from recordings in rodent thalamic slice preparations (34-38) and confirmed in anatomical  
80 studies (32, 39, 40). Furthermore, open-loop pathway variants in the form of X-TRN-TC are also known  
81 to exist, with X representing indirect sources of modulation to the sensory thalamus via the TRN, such as  
82 monoaminergic and cholinergic brainstem nuclei, nuclei of the basal forebrain, amygdala, and prefrontal  
83 cortex (9, 41-45).

84  
85 We previously observed through a computational model that the open-loop TC-TRN-TC pathway, rather  
86 than uniformly depressing thalamic (and consequently cortical) activity, paradoxically enhanced  
87 thalamocortical output over a range of TC and TRN input frequencies (46). This finding demonstrated the  
88 capacity of an open-loop system to function as a tunable filter of thalamocortical transmission, subject to  
89 the temporal dynamics of input to the TRN, whether from other, non-reciprocally connected TC neurons  
90 or extrinsic sources. In both our previous model and earlier models built on closed-loop TC-TRN-TC  
91 synaptic motifs, the post-inhibitory rebound exhibited by TC neurons, as mediated by T-type  $Ca^{2+}$   
92 channels and driven by inhibition from the TRN, served as a catalyst of signal propagation within the  
93 networks (9, 46-55).

94  
95 Based on previous studies of open-loop TC-TRN-TC synaptic organization, we hypothesized that these  
96 synaptic modules might underlie intrathalamic and therefore intracortical signal propagation.  
97 Accordingly, we sought here to evaluate the efficacy of open-loop pathways relative to other potential  
98 synaptic configurations in mediating signal transmission across the thalamus and cortex. To this end, we  
99 constructed a model network based on that of (46) by connecting in series three thalamo-reticulo-layer-4-  
100 cortical (TC-TRN-L4) pathways, potentially featuring both closed- and/or open-loop TC-TRN-TC motifs,  
101 with the latter constituting one mode of connectivity between parallel TC-TRN-L4 pathways.  
102 Intracellular synapses represented the other structural connections between pathways, based on the  
103 identification of both GABAergic (56-62) and electrical synapses (61-65) between TRN neurons. Thus,

104 we included three different polysynaptic configurations between vertical pathways in our network (Fig.  
105 1B, from left to right): 1) those with a chemical intrareticular synapse; 2) those with an electrical  
106 intrareticular synapse; and 3) open-loop TC-TRN-TC pathways. To analyze how each variety of inter-  
107 pathway connection contributed to network dynamics, permutations of the baseline network were  
108 generated by varying three properties associated with each of the inter-pathway synaptic motifs. We  
109 quantified network dynamics as a function of variable TC-TRN-TC and intrareticular synaptic  
110 architectures by defining and measuring two properties inherent to stimulus-evoked responses in each  
111 network variant: propagation and oscillation, with the latter included in light of the fact that many  
112 characterized thalamic waveforms both oscillate and propagate through the thalamus and cortex (25).

113

### 114 **Network architecture and simulations:**

115 We constructed a neuronal network comprising three interconnected thalamo-reticulo-cortical pathways  
116 (Fig. 1C). Thalamic, reticular, and cortical cell layers were aligned topographically, such that TC<sub>A</sub>  
117 projected to both TRN<sub>A</sub> and L4<sub>A</sub> (10, 25, 52, 66, 67).

118

119 In the case of homogeneously varied synaptic network permutations, the synaptic parameters associated  
120 with three inter-pathway motifs varied as a class, with all external, TC-TRN, and TC-L4 synaptic  
121 conductances held constant: 1) GABAergic intrareticular (TRN-TRN<sub>GABA</sub>) synapses ranged in  
122 conductance between 0 and 450 nS; 2) electrical intrareticular (TRN-TRN<sub>Elec</sub>) synapses ranged in  
123 coupling coefficient between 0 and 0.36; and 3) a TC-TRN-TC “openness” coefficient, defined as the  
124 weight distribution of lateral (open-loop, comprising 2 synapses of the form TRN<sub>i</sub>→TC<sub>i+1</sub>) vs. recurrent  
125 (closed-loop, comprising 3 synapses of the form TRN<sub>i</sub>→TC<sub>i</sub>) reticulothalamic connectivity, varied  
126 between 0 (completely closed-loop) and 1.0 (completely open-loop) and with a baseline TRN-TC  
127 conductance of 80 nS.

128

129 For the heterogeneously varied synaptic network variants, all TRN-TRN and TRN-TC synapses were  
130 allowed to vary independently. Domains for each of the synaptic variables were selected to include the  
131 range of conductance or coupling strengths reported in physiological measurements and/or used in similar  
132 neural models (19, 49, 52, 54, 63, 64, 67).

133

134 Ongoing afferent synaptic input was delivered to every TC neuron in the model as Poisson-modulated  
135 spike trains centered at 40 Hz. An additional 200-Hz pulse train was applied to neuron TC<sub>A</sub> between  
136  $t=0.400$  and  $t=1.500$  s during every network simulation run. This high-frequency stimulus was modeled  
137 on those used to elicit spindle-like waves in a ferret thalamoreticular slice preparation (18, 68). A given  
138 network’s output was compiled by assembling spike histograms (10-ms bins) averaging 1,000 simulations  
139 for every L4 neuron (Fig. 1D). Network properties were quantified in the most downstream element of the  
140 cortical output layer, L4<sub>C</sub>. Propagation across a network was quantified as the amplitude of the initial  
141 stimulus-evoked response in the detrended L4<sub>C</sub> histogram. The degree of oscillation supported by each  
142 network permutation was defined as the amplitude of the first off-center peak in the normalized  
143 autocorrelogram of post-stimulation activity (Fig. 1D). Both propagation and oscillation scores are  
144 reported as normalized to the maximum scores tabulated for each property. Given the high prevalence of  
145 propagating oscillatory waves in the cerebral cortex [reviewed in (69)], we furthermore defined a  
146 composite “optimization” (*Op*) metric to measure the capacity of networks to simultaneously support and  
147 balance between propagation (*Pr*) and oscillation (*Os*):

$$148 \quad Op = \sqrt{Pr^2 + Os^2} - |Pr - Os| \quad (1)$$

149

### 150 **Results:**

#### 151 *Homogeneously varied synaptic models*

152 Stimulus-evoked responses propagated linearly across the length of homogeneous synaptic networks,  
153 occurring at average fixed intervals of  $93.31 \pm 0.35$  ms (mean  $\pm$  standard error of the mean; range, 60-110

154 ms) between adjacent TC-TRN-L4 pathways, across all model permutations and with a mean velocity of  
155 0.54 mm/s, assuming a 50  $\mu\text{m}$  separation between adjacent neurons in each network layer. All 770  
156 homogeneous network variants were ranked according to their cortical propagation scores (Fig. 2A, top).  
157 Linear regression analysis ( $R^2=0.793$ , root-mean-square-error or RMSE=0.047,  $p<0.0001$ ) demonstrated a  
158 strong positive correlation between the TC-TRN-TC openness coefficient and propagation score  
159 (normalized regression coefficient or NRC=1.000). By contrast, chemical and electrical TRN-TRN  
160 synaptic connectivity tended to modestly diminish propagation (NRC=-0.173 and NRC=-0.136,  
161 respectively; Table S1). Further, other excitatory connectivity, such as cortico-cortical or corticothalamic  
162 connectivity, often postulated as being important for cortical signal propagation (5, 7, 8), was not  
163 necessary. Thus, the homogeneously varied synaptic network permutations that best accommodated  
164 signal propagation were generally ones with weak or absent synapses between TRN neurons and strong  
165 open-loop TC-TRN-TC connections. For example, Network a, which epitomizes this architecture,  
166 exhibited robust signal propagation in response to a fixed stimulus delivered to TC<sub>A</sub>; a representative  
167 simulation of this network is shown in Fig. 2B, left, and its position in Fig. 2C is labeled. Stimulus-  
168 evoked activity in this network tended to propagate efficiently from L4<sub>A</sub> to L4<sub>C</sub>: near-synchronous  
169 propagation cascades were elicited in both the TRN and L4 layers of the model, having been stimulated  
170 by propagating activity in upstream TC neurons. Smooth, linear propagation of action potentials across  
171 the network depended on the synchronous induction of inhibitory postsynaptic potentials (IPSPs) and the  
172 ensuing post-inhibitory rebound spikes in TC neurons, which occurred reliably and at fixed intervals in  
173 Network a.

174  
175 A 2<sup>o</sup> multiple regression model of propagation as a function of all three synaptic class variables  
176 ( $R^2=0.842$ , RMSE=0.041,  $p<0.0001$ ; Table S1) revealed modestly negative interaction term between  
177 TRN-TRN<sub>Elec</sub> synapses and TC-TRN-TC openness (NRC=-0.365), indicating that in networks where both  
178 electrical synapses were strong and TC-TRN-TC openness high, the extent of supported propagation  
179 diminished nonlinearly; a smaller negative interaction between TRN-TRN<sub>GABA</sub> synapses and TC-TRN-TC  
180 openness was also observed (NRC=-0.152). Together, these terms suggested that propagation was more  
181 significantly affected by connections in the TRN layer as a function of increasing open-loop TC-TRN-TC  
182 architecture. This relationship is evident in Fig. 2C, as propagation scores conspicuously decreased in  
183 network variants with an openness coefficient of 1.0 as either chemical or electrical synapses increase in  
184 weight.

185  
186 Oscillatory responses recurred in L4<sub>C</sub> neurons at a mean frequency of  $9.07 \pm 0.2$  Hz (range, 7.14-12.50  
187 Hz) across all homogeneous model permutations. Propagation and oscillation scores across all 770  
188 homogeneous networks were strongly anticorrelated (Pearson's  $r=-0.671$ ,  $p<0.0001$ ). Accordingly,  
189 oscillation was best accommodated in network permutations exhibiting strongly closed-loop connectivity  
190 (Fig. 2A, bottom), however the capacity to support oscillation was neither markedly linear nor  
191 monotonically decreasing as a function of increasing openness coefficient (Fig. 2D). Rather, a one-way  
192 analysis of variance (ANOVA) with Tukey's tests revealed that, on average, oscillation scores peaked and  
193 remained statistically indistinguishable from one another across the subset of network permutations with  
194 openness coefficients between 0 and 0.4, with scores then decreasing in a roughly linear fashion with  
195 increasing TC-TRN-TC openness [ $F(10,759)=137.8$ ,  $p<0.0001$ ]. These data suggest that networks with  
196 mixed open- and closed-loop connectivity (which is likely close to physiological reality) can support the  
197 coexistence of oscillation and propagation (see *Heterogeneously varied synaptic models*, below).

198  
199 The predominant mechanism by which oscillation arose in L4<sub>C</sub> was through post-inhibitory rebound in  
200 TC<sub>C</sub>, as engendered by the strong recurrent inhibition found in network permutations exhibiting primarily  
201 closed-loop TC-TRN-TC connectivity. This mode of oscillation was exemplified by Network b, a  
202 strongly closed-loop network variant. In the simulation shown of this network (Fig. 2B, right), oscillatory  
203 activity was enabled by a single epoch of signal propagation. Notably, neither the presence of strong

204 GABAergic nor electrical intrareticular synapses in Network b exerted much effect on its ability to  
205 support oscillation, as predicted by the regression models.

206  
207 *Heterogeneously varied synaptic models*

208 Recent studies have highlighted heterogeneity in TRN neuronal connectivity, synaptic physiology and  
209 chemical identities (70-72). We therefore examined the impact of allowing all synaptic connections  
210 involving the TRN to be independently varied. We constructed circuit-level schematics of linear  
211 regression models for propagation (Fig. 3A, top) and oscillation (Fig. 3A, bottom) as functions of the 14  
212 synaptic variables in heterogeneous networks.

213  
214 Propagation in heterogeneously varied synaptic networks increased chiefly as a function of increasing the  
215 strength of the more downstream of the two laterally inhibitory TRN-TC synapses,  $TRN_B \rightarrow TC_C$ : the  
216 corresponding term in a linear regression model of propagation ( $R^2=0.742$ ,  $RMSE=0.069$ ,  $p<0.0001$ ;  
217 Table S2) possessed an NRC of 1.000 (Fig. 3A, top). Propagation scores also scaled to a lesser extent  
218 with the more upstream laterally inhibitory reticulothalamic synapse,  $TRN_A \rightarrow TC_B$  (NRC=0.608). The  
219 two inhibitory intrareticular synapses originating at the rightmost end of the model network,  
220  $TRN_C \rightarrow TRN_A$  and  $TRN_C \rightarrow TRN_B$ , both exerted a small negative effect on propagation (NRC=-0.087 and  
221 NRC=-0.084, respectively). Additionally, two TRN- $TRN_{Elec}$  synapses,  $TRN_A=TRN_B$  and  $TRN_A=TRN_C$   
222 (where the "=" denotes an electrical synapses), marginally decremented propagation in heterogeneous  
223 networks, with NRCs of -0.051 and -0.072, respectively. These findings at an individual synaptic level  
224 comported with the observation that strong TRN-TRN interactions, whether chemical or electrical, tended  
225 to impede signal propagation in homogeneous network variants.

226  
227 A 2° regression model ( $R^2=0.857$ ,  $RMSE=0.051$ ,  $p<0.0001$ ; Table S2) disclosed a large, propagation-  
228 enhancing interaction between the two laterally inhibitory synapses (NRC=0.753), underscoring the same  
229 dependence of propagation on strong open-loop TC-TRN-TC connectivity as seen in homogeneously  
230 synaptic networks, but additionally demonstrating that propagation scores increased nonlinearly as a  
231 function of simultaneously increasing the weights of  $TRN_A \rightarrow TC_B$  and  $TRN_B \rightarrow TC_C$ . Interactions between  
232 TRN-TRN synapses of either variety and TRN-TC synapses tended diminish propagation, as did those  
233 between recurrent and lateral inhibitory TRN-TC synapses. Taken together, the linear and 2° regression  
234 models indicated that heterogeneous network permutations with strong laterally inhibitory TRN-TC  
235 synapses tended to best support propagation. Consistent response propagation across the length of the  
236 network was epitomized by Network a', in which  $TRN_A \rightarrow TC_B$  and  $TRN_B \rightarrow TC_C$  were both relatively  
237 strong and those synapses impeding propagation relatively weak (Fig. 3B, left).

238  
239 *Comparisons between homogeneously and heterogeneously varied synaptic architectures*

240 In contrast to the homogeneous models, there was a very small negative correlation between the  
241 propagation and oscillation scores of these networks ( $r=-0.0296$ ,  $p=0.0008$ ), suggesting that propagation  
242 and oscillation more easily coexist in heterogeneous than homogeneous models. This supposition was  
243 confirmed through a 2° regression analysis ( $R^2=0.388$ ,  $RMSE=0.118$ ,  $p<0.0001$ ), which suggested that  
244 interactions between recurrently and laterally inhibitory TRN-TC synapses (NRCs ranging between 0.345  
245 and 0.669) facilitated the propagation of oscillation, a mechanism typified by Network b' (Fig. 3B, right).  
246 Two intrareticular synapses,  $TRN_A-TRN_C$  and  $TRN_A=TRN_C$ , tended to contribute modestly to oscillation  
247 (NRCs of 0.115 and 0.117, respectively, in the linear regression model,  $R^2=0.253$ ,  $RMSE=0.131$ ,  
248  $p<0.0001$ ; Fig. 3A, bottom), while, in their individual capacities,  $TRN_A \rightarrow TC_B$  and  $TRN_B \rightarrow TC_C$   
249 diminished oscillation (NRCs of -1.000 and -0.892, respectively).

250  
251 We analyzed the relative capacities of homogeneously and heterogeneously varied synaptic networks to  
252 support propagation, oscillation, and optimization by comparing the 20 highest scores achieved by  
253 homogeneous and heterogeneous network permutations with respect to each performance metric. No  
254 significant differences in mean propagation scores between top-performing homogeneous and

255 heterogeneous networks were disclosed [unpaired  $t$ -test,  $t(38)=0.46$ ,  $p=0.647$ ; Fig. 4]. We attributed this  
256 lack of differences to the fact that network permutations in which the synapses  $TRN_A \rightarrow TC_B$  and  
257  $TRN_B \rightarrow TC_C$  were both maximally weighted would be equally capable of supporting robust signal  
258 propagation, regardless of whether these synapses were varied homogeneously or heterogeneously. By  
259 contrast, top-scoring heterogeneous network variants better supported both oscillation [ $t(38)=13.88$ ,  
260  $p<0.0001$ ] and optimization [ $t(38)=18.04$ ,  $p<0.0001$ ] than their homogeneous counterparts. Because  
261 networks supporting the propagation of oscillatory activity would, by definition, score high with respect  
262 to optimization, these results not only confirmed that heterogeneous networks were more likely than  
263 homogenous networks to accommodate this oscillatory mechanism, but furthermore that propagation of  
264 oscillation across the thalamocortical network was associated with higher oscillation scores than post-  
265 inhibitory-driven oscillation in  $TC_C$ , the predominant form of oscillation observed in homogeneous  
266 networks.

### 267 **Discussion:**

269 The simulations presented here suggest that open-loop TC-TRN-TC synaptic motifs (Fig. 1B, right) could  
270 function as a substrate for signal propagation across cortical networks without the need for direct cortico-  
271 cortical, intra-reticular or corticothalamic connectivity. Post-inhibitory rebound mediated by T-type  
272 calcium channels served as a substrate for both propagation and oscillation in the simulated networks.  
273 TRN-TRN connections, either chemical or electrical (Fig. 1B, left and middle), diminished horizontal  
274 propagation by disrupting the precise timing relationships required to propagate a signal across the  
275 network. Models with heterogeneously varied TRN synapses outperformed those whose synapses varied  
276 as a class with respect to the propagation of oscillatory activity, consistent with the emerging literature  
277 documenting cellular and synaptic heterogeneity in the TRN (70-72). These data suggest that widespread  
278 propagating cortical activity, under both pathological and physiological conditions, may be mediated, at  
279 least in part, by intrathalamic connections. The model makes strong predictions that can be tested  
280 physiologically. Finally, the approach used here, which employed supercomputing applications to search  
281 through a very large parameter space, serves as model for future computational models with large  
282 parameter spaces.

284 Like most of the thalamic (19, 47-50) and thalamocortical models (52, 53, 55) that inspired our model, we  
285 utilized single-compartment, Hodgkin-Huxley neurons. While these model cells contribute to the  
286 computational parsimony and practicality of network models, particularly where the analysis of network  
287 dynamics is prioritized, they neglect the intrinsic cable properties of real neurons and, relatedly, the  
288 spatially disparate nature of synaptic integration and heterogeneous expression of intrinsic and synaptic  
289 conductances (73, 74). Such considerations are particularly relevant here relative to dendritic distributions  
290 of T- and H-currents in TC neurons (52, 54, 75, 76) and TRN neurons (54, 77-79). Although  
291 multicompartment neuronal models incorporating such details could conceivably alter the network  
292 dynamics being studied, they were not necessary to simulate the propagation of oscillatory waves seen  
293 physiologically (18, 19, 48-50).

295 Additionally, the present model omitted explicit corticothalamic and corticoreticular synapses, both of  
296 which have been identified and physiologically characterized to varying degrees (80-86), though the  
297 former were effectively amalgamated with both feedforward sensory and modulatory projections to the  
298 thalamus in the form of the Poisson-modulated external input we delivered to individual TC neurons.  
299 Both forms of feedback have been implicated in the spread of spindle waves and in the maintenance of  
300 their synchronization over large distance scales (on the order of the length of the mammalian forebrain)  
301 and are furthermore known to drive spindle wave formation and propagation *in vivo* by polysynaptically  
302 recruiting TC neurons via TRN-mediated post-inhibitory rebound (80, 83, 86-91). It should be noted,  
303 however, that short-range coherence of spindle waves, which can be elicited in isolated thalamic slice  
304 preparations (18, 68), is preserved following decortication, both *in vivo* and *in silico* (52, 83, 88). By  
305 extension, it is reasonable to assume that the dynamics of the spindle-like waveforms generated in our



306 small-scale, broadly feedforward model, in which the cortex served solely as an output layer, would not  
307 be qualitatively altered by corticothalamic or corticoreticular feedback.

308

309 *Comparison to related computational models and physiological data*

310 Although the production of spindle waves was not an explicit objective of our study, some of the wave  
311 dynamics arising in our networks were nevertheless consistent with those inherent to spindle or spindle-  
312 like waves. Despite possessing higher degrees of TC→TRN and TRN→TC synaptic divergence and  
313 lacking the exclusively open-loop TC-TRN-TC architecture characterizing a subset of our network  
314 variants, other isolated thalamic models allowing for longitudinal wave propagation similarly  
315 accommodated this propagation along the lattice of interconnected TC and TRN neurons by way of  
316 laterally inhibitory TRN-TC synapses (19, 48, 50, 92); at short ranges, this mechanism of signal  
317 propagation also prevailed in larger-scale thalamo-reticulo-cortical models, while corticothalamic  
318 projections acted to propagate activity to more distal sites [(52); see (93), for a schematic illustrating  
319 short- and long-range thalamocortical wave propagation]. Comparably, recurrently inhibitory TRN-TC  
320 synapses have been documented to play a vital role in the generation of oscillatory behavior in the  
321 thalamus (17, 93). The temporal parameters of propagating and oscillation signals in our model also  
322 matched some of those previously reported: the mean signal propagation velocity and oscillation  
323 frequency measured across homogeneous networks fell within the ranges of spindle wave propagation  
324 velocities and intraspindle spike frequencies reported in both physiological and computational spindle  
325 wave studies (19, 48, 68, 94, 95).

326

327 Several key structural elements of our set of network models and the range of phenomena they produced  
328 distinguish them from previous thalamic and thalamocortical models. One particularly notable point of  
329 departure relative to similar network models was the extent to which thalamoreticular, reticulothalamic,  
330 and thalamocortical synapses diverged. Although all three classes of synapses are known to diverge  
331 significantly and have been observed to target neuronal somata hundreds of microns from their origins  
332 (25, 32, 58, 96-100), the TC-TRN, TRN-TC, and TC-L4 synapses in our model were constrained to  
333 remain strictly local and minimally divergent (or non-divergent, in the case of TC-TRN and TC-L4  
334 synapses). With respect to the first two classes of synapses, this constraint was imposed to probe the  
335 impact the disynaptic TC-TRN-TC open-loop motifs characterizing a subset of network permutations,  
336 which constituted one of the foci of our study, and analyze the signal propagation they may support. This  
337 neuroanatomical scheme contrasted with previous computational models featuring parallel,  
338 interconnected thalamoreticular pathways, in which both TC and TRN synapsed bidirectionally with  
339 several neighboring TRN and TC cells, respectively, within a radius of several hundred microns (e.g., 19,  
340 48-50, 52-54, 67, 101). It is highly likely that if more divergent synaptic connections were used in the  
341 current model, even greater propagation would have been observed.

342

343 *The functional implications open-loop thalamo-reticulo-thalamic synaptic motifs*

344 The spread of activity from one cortical region to another is a foundational concept at the core of our  
345 understanding of sensory processing, higher order-cognitive functions such as attention and language,  
346 sleep-related oscillatory phenomena, and pathological findings such as propagation of ictal discharges and  
347 migraine. Despite the importance of communication between cortical regions, its underlying substrates  
348 are not well understood. It has long been speculated that the TRN could serve as a control point for large-  
349 scale cortical signal processing given its central location, the high degree of convergence of projections  
350 involved in attention, arousal and emotion onto the TRN and the TRN's particularly strong control over  
351 TC firing properties (11-13, 102-104). Although the anatomical bases of open-loop TC-TRN-TC motifs  
352 have been partially characterized, their functional significance in the brain lingers as a subject of  
353 continued speculation. Here we show that open-loop TC-TRN-TC architectures can support at least short-  
354 range cortical signal propagation. Within the thalamus, these configurations have thus far been observed  
355 both within and across individual thalamic nuclei and are thought to serve as pathways for intra- and  
356 cross-modal modulation, respectively (32, 34-40); as has been previously surmised, these synaptic

357 pathways could also plausibly lend themselves to sensory enhancement, multisensory integration, and  
358 attentional mechanisms (10, 35, 46, 105). At a minimum, and as inferred from physiological studies,  
359 open-loop pathways should be fully capable of supporting signaling propagation from one thalamic relay  
360 neuron to another through a limited number of intervening synapses (with a disynaptic pathway serving as  
361 the shortest such configuration). Moreover, interference with thalamoreticular transmission should cause  
362 a breakdown in some forms of cortical signal propagation. Recent work has established that stimulation of  
363 the TRN *in vivo* can induce propagating rhythmic activity across the cortex (106-108). These data suggest  
364 that abnormal cortical signal propagation seen in seizures, migraines or hallucinations may be disrupted  
365 by targeted therapeutics applied to the TRN. Both forthcoming physiological investigation and future  
366 modeling studies will be able to evaluate these predictions and help provide a full accounting of the role  
367 of the various modes of connectivity between cortical regions.

## 369 **Methods:**

### 370 *Intrinsic neuronal models*

371 Our network model was directly based on an earlier incarnation published by our research group (46).  
372 Single-compartment TC, TRN, and L4 model neurons obeyed Hodgkin-Huxley kinetics, with membrane  
373 potentials  $V$  varying according to the first-order differential equation

$$374 \quad C \frac{dV}{dt} = -g_L(V - E_L) - \sum_i g_i(V)(V - E_i) \quad (2)$$

375 where  $C$  is the membrane capacitance,  $g_L$  and  $E_L$  are the leakage conductance and reversal potential,  
376 respectively, and  $g_i(V)$  and  $E_i$  are the dynamic conductance and reversal potential, respectively, of the  $i$ th  
377 voltage-gated, ligand-gated (chemical synaptic), or electrical synaptic conductance (for electrical synaptic  
378 conductances, the effective reversal potential is equal to the presynaptic membrane potential; see  
379 Equation 3a). All three varieties of model neurons expressed both the standard transient sodium ( $I_{Na}$ ) and  
380 delayed-rectifier potassium ( $I_K$ ) currents, as reported by (46). TC and TRN neurons additionally included  
381 a T-type calcium conductance (T-current;  $I_T$ ) and hyperpolarization-activated cation current (H-current;  
382  $I_H$ ), following the TC model of (109). Both TRN and L4 cells expressed a slow, non-inactivating  
383 potassium conductance ( $I_M$ ), following the modeling of (110), which accounts for the spike-frequency  
384 adaptation previously reported in physiological recordings from these neurons (46, 111). A list of intrinsic  
385 model cell parameters, including current conductances, reversal potentials, selected gating kinetics, and  
386 membrane capacitance, can be found in Table S3.

### 387 *Synaptic models*

388 The kinetics of chemical synapses in our model network conformed to the synaptic depression model of  
389 (112), following our previous computational network model (46). This model presupposes a finite  
390 quantity of “resources,” akin to synaptic vesicles, capable of being released by the presynaptic neuron;  
391 these resources can exist in an active, inactive, or recovered state. A parameter  $U_{SE}$  characterizes the  
392 fraction of recovered resources that can be converted to an active state (i.e., for release by the presynaptic  
393 neuron) following action potential induction in the presynaptic axon terminal(s). Following resource  
394 activation, synapses inactivate according to the time constant  $\tau_{inact}$ ; resources become available again for  
395 activation after a recovery period described by the time constant  $\tau_{recov}$ . These parameters, along with the  
396 neurotransmitters, postsynaptic conductances, and reversal potentials characterizing all of the chemical  
397 synapses in our model, are given in Table S4.

399 Glutamatergic thalamoreticular and thalamocortical (TC-L4) and baseline GABAergic reticulothalamic  
400 synaptic parameters matched those of our earlier model (46), with the latter synapses allowed to vary in  
401 conductance. TRN-TC signaling was mediated exclusively through GABA<sub>A</sub> receptors, mirroring other  
402 thalamic and thalamocortical models in which the slower TRN-TC GABA<sub>B</sub> conductance was omitted (51,  
403 54, 55). Both GABAergic (TRN-TRN<sub>GABA</sub>) and electrical synapses (TRN-TRN<sub>elec</sub>) were included  
404 between TRN neurons; as with TRN-TC synapses, both varieties of TRN-TRN synapses were allowed to  
405

406 vary in strength. Although evidence has been presented challenging the existence of GABAergic  
407 intracellular synapses in certain mammalian species and age groups (10, 63, 113-115), our model  
408 avoided making assumptions regarding their presence, strength, or spatial distribution by allowing the  
409 associated synaptic conductances to vary over a range of physiological values, including zero, and in  
410 distribution. The reversal potential, conductance, and kinetics of the external synapses projecting to the  
411 TC neurons were directly based on retinogeniculate synapses (116), although the generic nature of the  
412 external inputs in our model allows them to represent not only immediately upstream sensory input but  
413 also brainstem modulation (e.g., serotonergic, adrenergic) known to act on thalamic nuclei (117).

414  
415 Electrical synapses between TRN neurons were based on the Cx36-dependent intracellular gap junctions  
416 first identified by (58). For TRN neurons, the sum of electrical synaptic currents ( $I_{Elec}$ ) entering any  
417 postsynaptic neuron  $j$  from presynaptic neurons  $i$  was included in the rightmost term from Equation 1 and  
418 calculated as

$$419 \quad I_{Elec(j)} = \sum_i g_{ij} (V_j - V_i) \quad (3a)$$

420 where  $g_{ij}$  was itself calculated as

$$421 \quad g_{ij} = D(x) \frac{g_{gap}}{1/CC - 1} \quad (3b)$$

422 where  $CC$  was the electrical coupling coefficient between TRN neurons  $i$  and  $j$ ,  $g_{gap}$  is the gap junction  
423 conductance (set at 5 nS), and  $D(x)$  was a scaling factor that depended on the physical distance between  
424 the coupled TRN neurons (54, 73, 118). TRN-TRN<sub>Elec</sub> synapses were symmetrical (non-rectifying), such  
425 that  $G_{ij}=G_{ji}$ .

426  
427 We extrapolated the attenuation of intracellular synaptic strength as a function of intracellular distance  
428 based on mappings of intrinsic connections within the TRN along a horizontal (anteroposterior) plane  
429 assembled by (61). Assuming 1) an intracellular distance of 50  $\mu\text{m}$  between adjacent TRN neurons, 2) a  
430 distance  $x$  (in multiples of 50  $\mu\text{m}$ ) between non-adjacent neurons, and 3) a Gaussian falloff in synaptic  
431 strength (119), the baseline (adjacent-neuron) conductances of TRN-TRN<sub>GABA</sub> and TRN-TRN<sub>Elec</sub>  
432 synapses were scaled for non-adjacent synapses using the function

$$433 \quad D(x) = e^{-\frac{x^2}{2\lambda^2}} \quad (4)$$

434 where  $\lambda_{GABA}=531 \mu\text{m}$  and  $\lambda_{Elec}=130 \mu\text{m}$ .

435  
436 Given the small spatial scale of our model, synaptic delays associated with finite axonal conductance  
437 times within the TRN and between the TRN and dorsal thalamus were disregarded, mirroring the  
438 simplification incorporated into previous thalamic and thalamocortical models simulating synaptic  
439 interactions on the order of 100 microns (48, 54). Although small ( $\sim 1$  ms) thalamocortical delays were  
440 inserted into the network model of (54), these were likewise omitted on the basis of the cortex functioning  
441 solely as an output layer in our model.

#### 442 443 *Computations and statistics*

444 Our model was coded, simulated, and analyzed in MATLAB R2018b (MathWorks), utilizing both a Dell  
445 Inspiron 3847 and Hewlett-Packard Z840 running Windows 10 and nodes on the Illinois Campus Cluster  
446 (National Center for Supercomputing Applications, University of Illinois at Urbana-Champaign).  
447 Simulations employed 0.1-ms time steps, with temporal integration based on the hybrid analytic-numeral  
448 integration method of (120), which optimizes between accurate solutions to Hodgkin-Huxley and synaptic  
449 models and computational efficiency. All simulations commenced with a 200-ms equilibration period,  
450 during which no external stimulation was delivered to TC neurons; this allowed all network elements to  
451 attain steady-state conditions. Statistical analysis was performed in both MATLAB and R (121), with the  
452 *glmnet* package (122) utilized within the latter platform to perform regression analyses. Multiple linear  
453 regression was employed to establish rudimentary relationships between synaptic classes (homogeneously  
454 synaptic networks) or individual synapses (heterogeneously synaptic networks) and each of the two

455 studied network properties, even in instances where these relationships deviated from linearity. 2°  
456 regression models with interaction terms elucidated how synaptic interactions and nonlinearities affected  
457 these network properties. Regressions were optimized using elastic net regularization, with the specific  
458 regularization hyperparameter  $\alpha$  selected to minimize each regression model's root-mean-square error. To  
459 convey the relative influence of different synaptic classes or individual synapses on dynamic network  
460 properties, all regression coefficients are reported here as normalized to the coefficient with the largest  
461 absolute value; the effects corresponding to NRCs with absolute values of less than 0.05 were disregarded  
462 as negligibly influential on network dynamics. Both unpaired Student *t*-tests and one-way ANOVA  
463 models were used to compare the mean property scores between different sets of networks, with Tukey's  
464 honestly significant difference tests used to ascertain pairwise difference between groups in the latter.  
465 Kolmogorov-Smirnov and Levene's tests were employed to confirm normality and homogeneity of  
466 variance, respectively, when utilizing parametric mean-comparison tests; data were log-transformed as  
467 needed to conform to these prerequisites.

#### 468 **Acknowledgments:**

470 This work made use of the Illinois Campus Cluster, a computing resource that is operated by the Illinois  
471 Campus Cluster Program (ICCP) in conjunction with the National Center for Supercomputing  
472 Applications (NCSA) and which is supported by funds from the University of Illinois at Urbana-  
473 Champaign. We additionally thank Profs. Thomas Anastasio, Ruoqing Zhu, and Rama Ratnam, Drs. Kush  
474 Paul and Baher Ibrahim, and Mr. Weddie Jackson for their valuable analytical, statistical, and technical  
475 insights.

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866 **Figure Legends:**

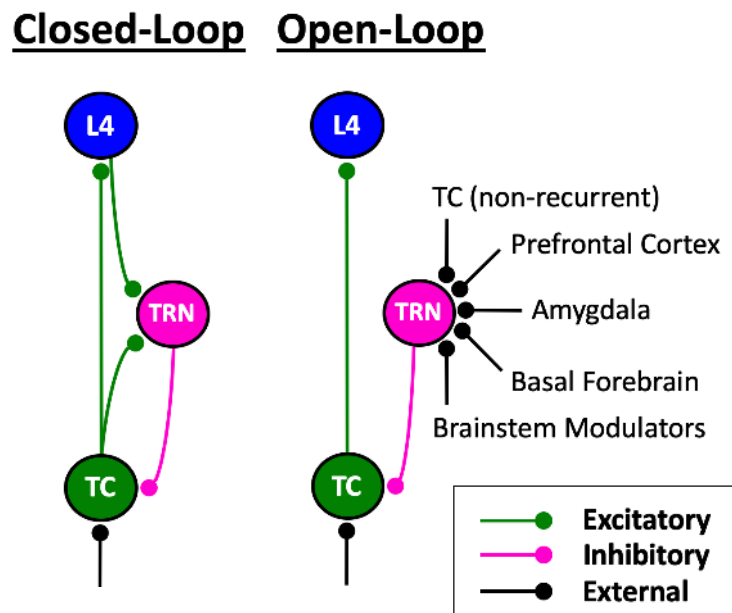
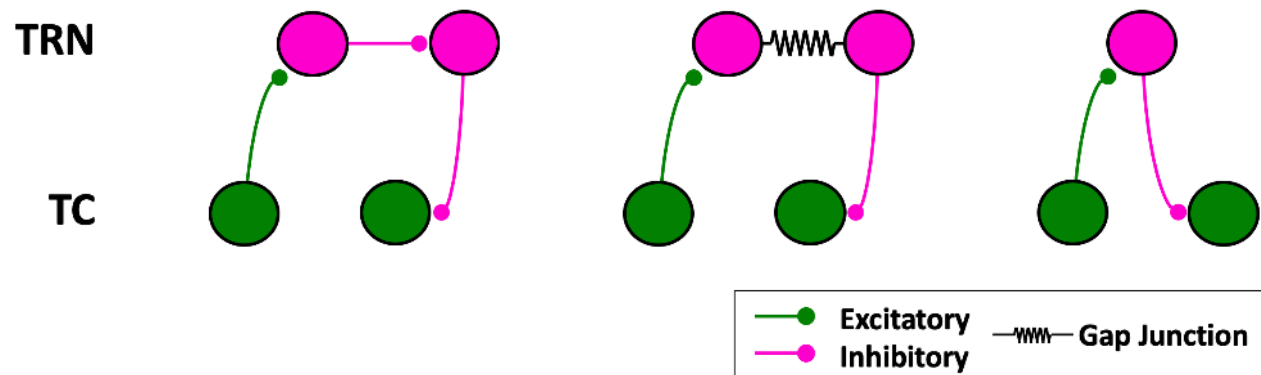
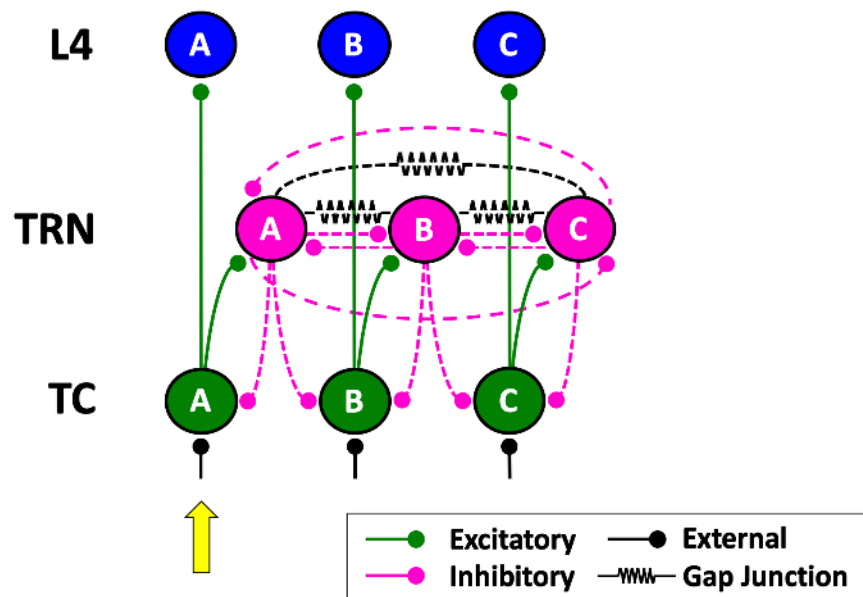
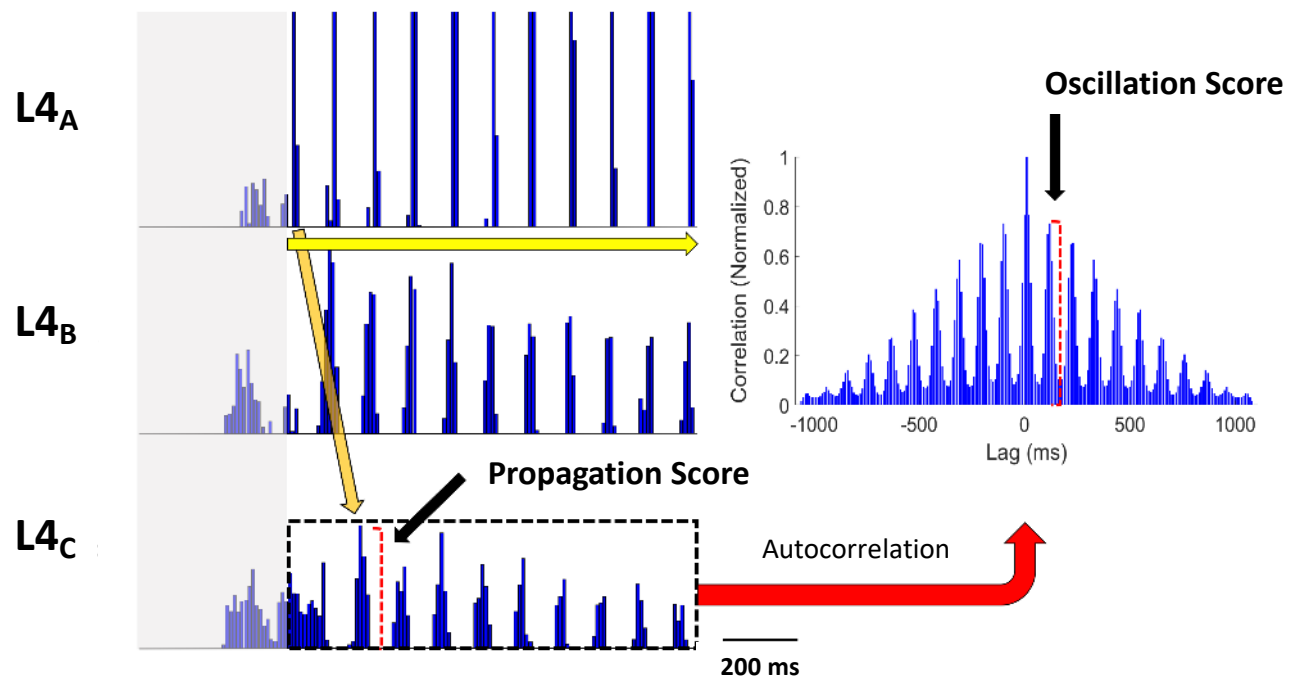
867 **Figure 1.** Pathways and properties of thalamocortical signaling. **A:** Closed- vs. open-loop thalamo-  
868 reticulo-thalamic configurations. **B:** Three possible pathways through which a signal might propagate  
869 from one thalamocortical (TC) neuron to another via the thalamic reticular nucleus (TRN). **C:** Baseline  
870 thalamo-reticulo-cortical model network. Broken-line synapses were allowed to vary either as a class  
871 (homogeneously) or independently of one another (heterogeneously). **D:** Sample L4 spike histograms  
872 (detrended) in a network permutation responding to a fixed, sustained stimulus delivered to TC<sub>A</sub> (yellow  
873 arrow). The propagation score assigned to any network permutation was quantified as the amplitude of  
874 the initial stimulus-evoked response in the detrended L4<sub>C</sub> histogram; response propagation across the L4  
875 subnetwork (orange arrow) was consistently linear, and thus the initial response in L4<sub>C</sub> was observed at a  
876 fixed interval relative to the onset of stimulation. Oscillation intrinsic to any network variant was  
877 quantified as the amplitude of the first off-center peak in the normalized autocorrelogram (right) of post-  
878 stimulation activity in the detrended L4<sub>C</sub> histogram (within broken black box). The initial 400 ms of  
879 activity preceding the fixed stimulus (in grey) is shown here for each histogram but was not included in  
880 the calculations of either propagation or oscillation. Note that the bin heights in the L4<sub>A</sub> histogram shown  
881 here were truncated in order to maintain identical vertical scaling across all three L4 histograms.  
882

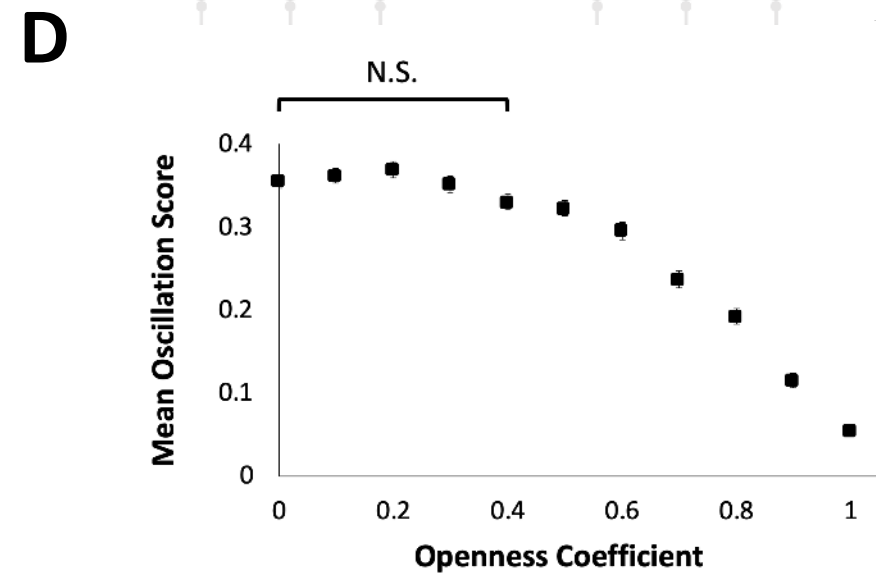
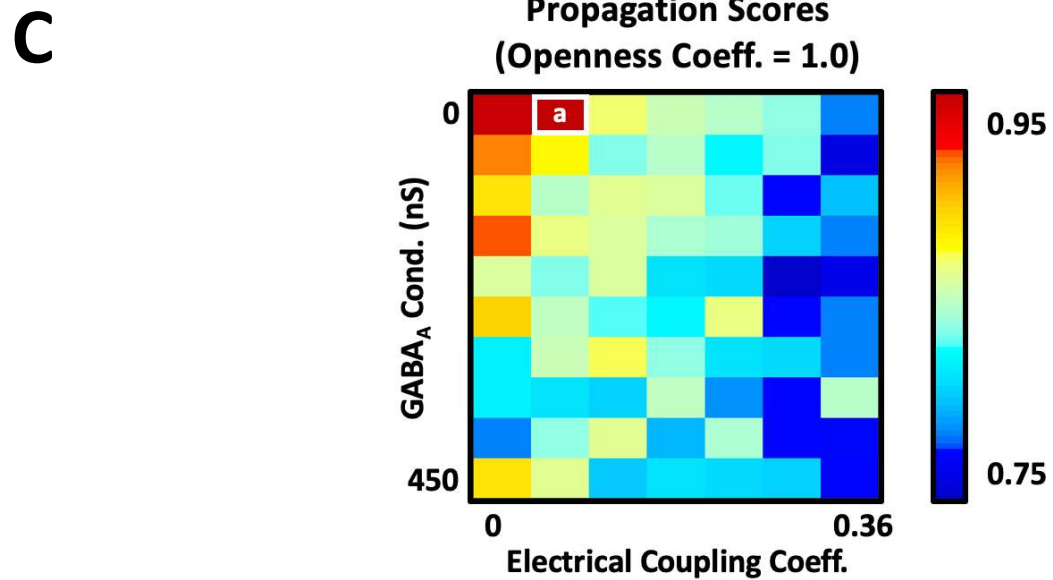
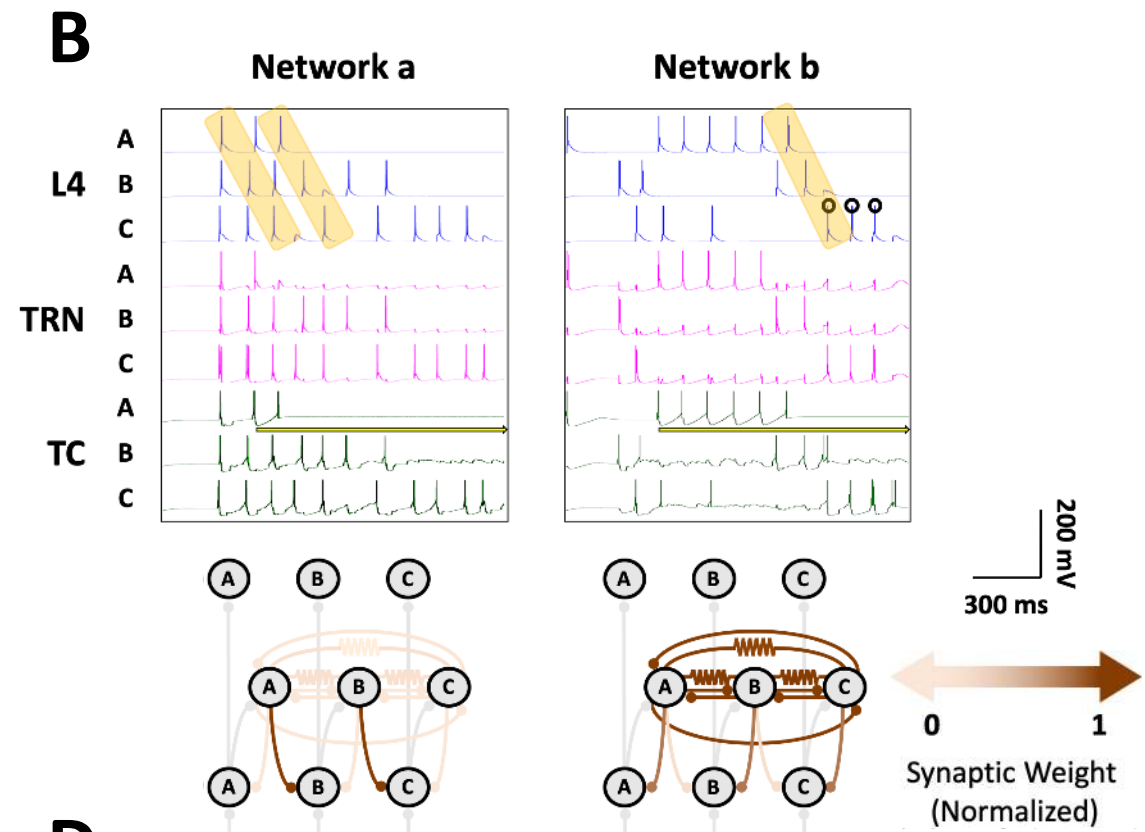
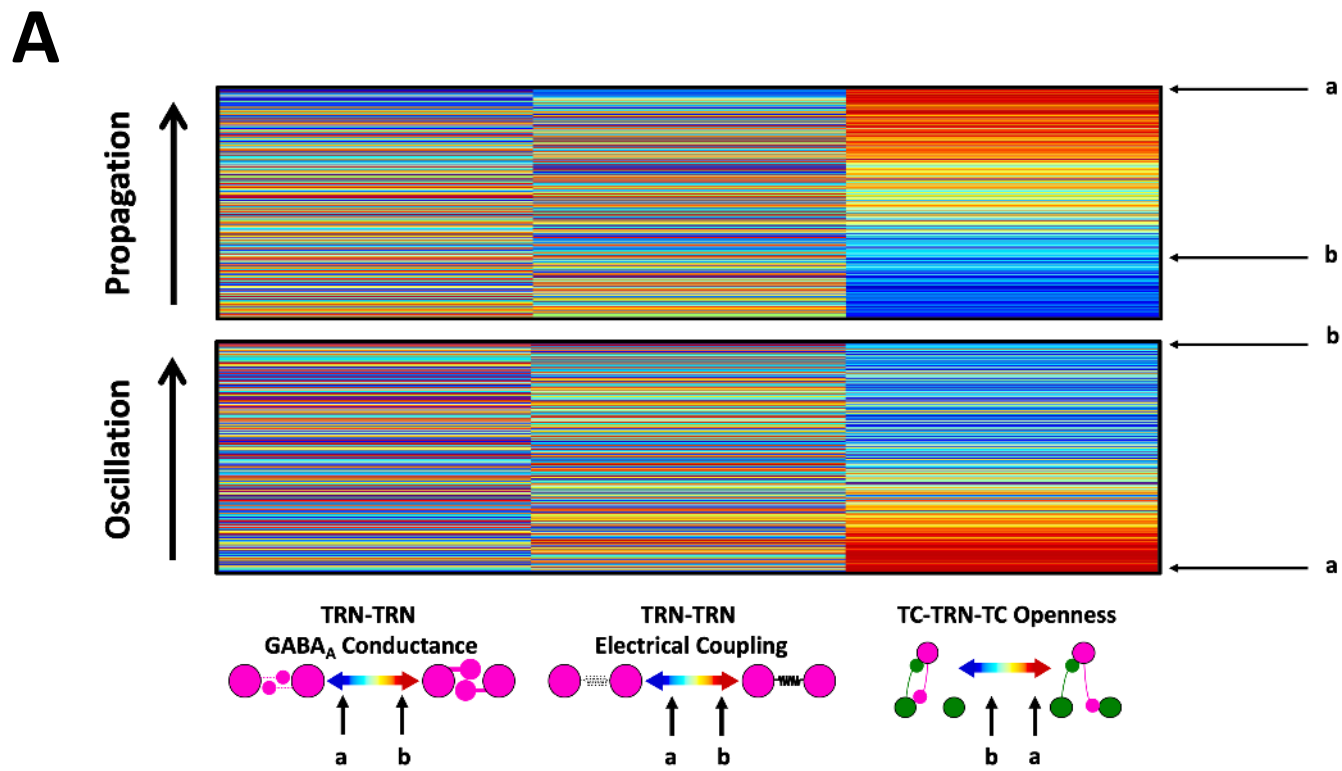
883 **Figure 2.** Propagation and oscillation in homogeneously varied synaptic networks (N=770). **A:** Ordinal  
884 heat maps ranking homogeneously varied synaptic network permutations according to the extent of  
885 supported signal propagation and oscillation. The network property ranks and synaptic makeups of two  
886 selected networks, Networks a and b, are indicated. **B:** Representative simulations and circuit diagrams  
887 depicting the normalized synaptic makeups for the two selected networks. The yellow arrow indicates  
888 when the fixed stimulus was delivered to TC<sub>A</sub> in each simulation. Orange highlighting indicates epochs of  
889 linear propagation, while circles are placed above spikes occurring during periods of oscillatory activity.  
890 **C:** A heat map displaying propagation scores in TRN-TRN synaptic parameter space for the 70 fully  
891 open-loop networks (openness coefficient=1.0), with Network a highlighted. **D:** Mean oscillation scores  
892 for networks varied nonlinearly as a function of their openness coefficients, with networks possessing  
893 openness coefficients of 0 and 0.4 supporting oscillation to equal extents (one-way ANOVA with Tukey  
894 post-hoc tests,  $F(10,759)=137.8, p<0.0001$ ). Error bars indicate standard errors of the mean; N.S.=not  
895 significant.  
896

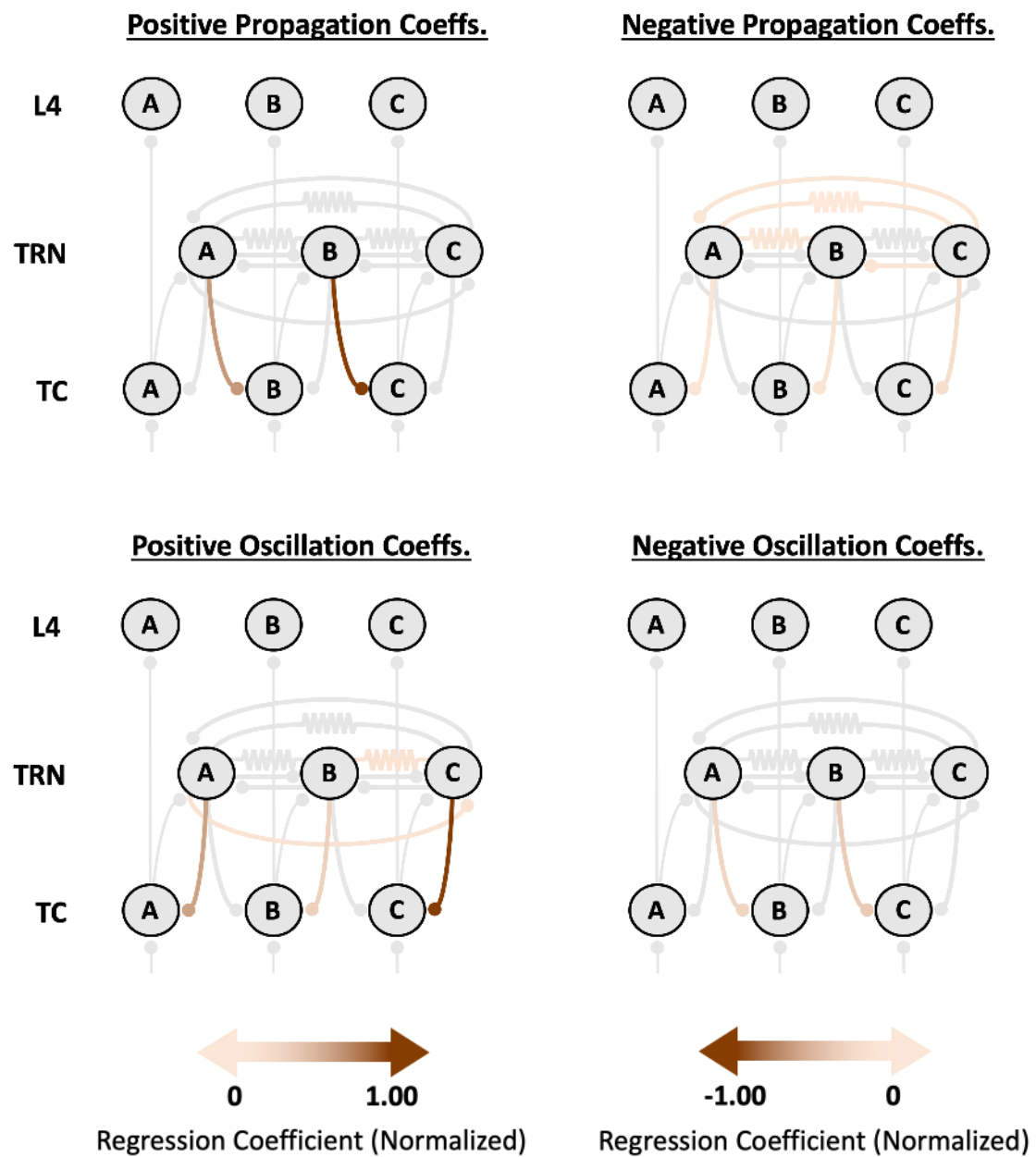
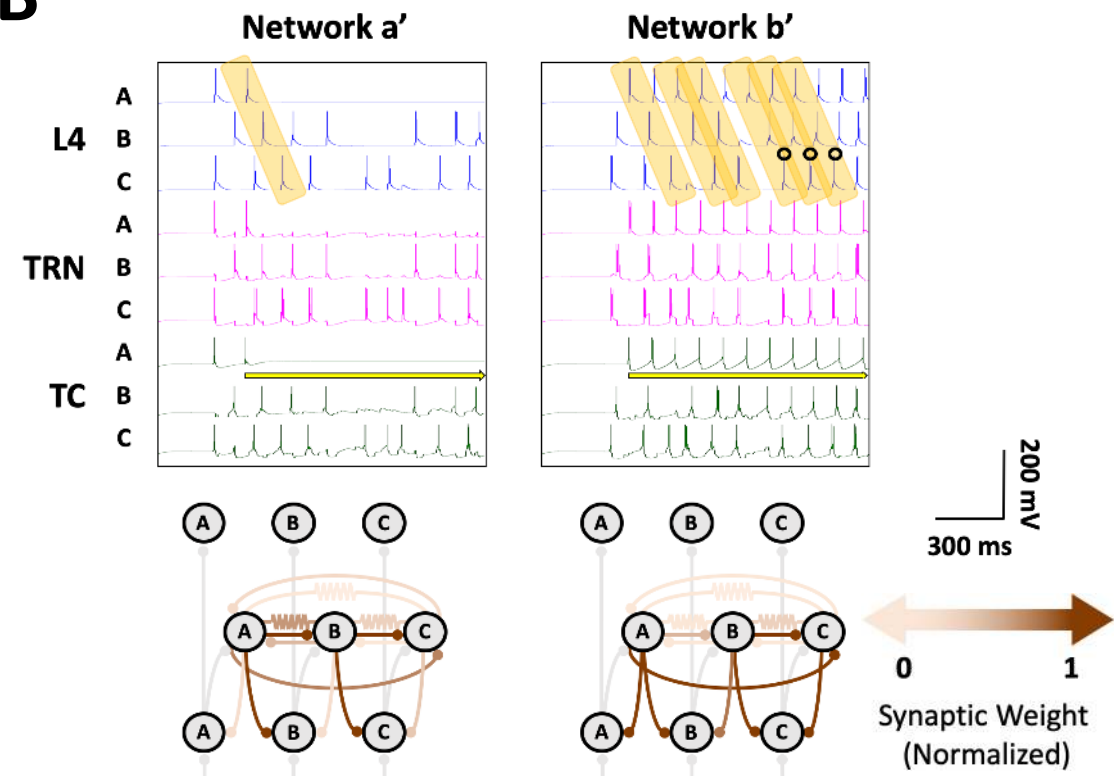
897 **Figure 3.** Propagation and oscillation in heterogeneously varied synaptic networks (N=12,681). **A:**  
898 Network regression models illustrating how propagation (top) and oscillation (bottom) varied as a  
899 function of individual synaptic weights across simulated heterogeneously synaptic network permutations.  
900 Gray synapses are either non-variable or associated with normalized regression coefficients with absolute  
901 values under 0.05. Synapses with positive and negative coefficients in the regression models are depicted  
902 separately in the left- and right-sided circuit diagrams, respectively. **B:** Representative simulations for two  
903 selected heterogeneous networks, whose normalized synaptic weights are depicted in the circuit diagrams.  
904 Networks a' and b' respectively illustrate propagation and propagation of oscillation from Column A to  
905 Column C.  
906

907 **Figure 4.** Propagation, as measured in those network permutations scoring highest with respect to the  
908 property, was equally supported in networks where synaptic weights varied independently of one another  
909 (heterogeneously; red) as in networks where synaptic strength varied homogeneously (blue) by class

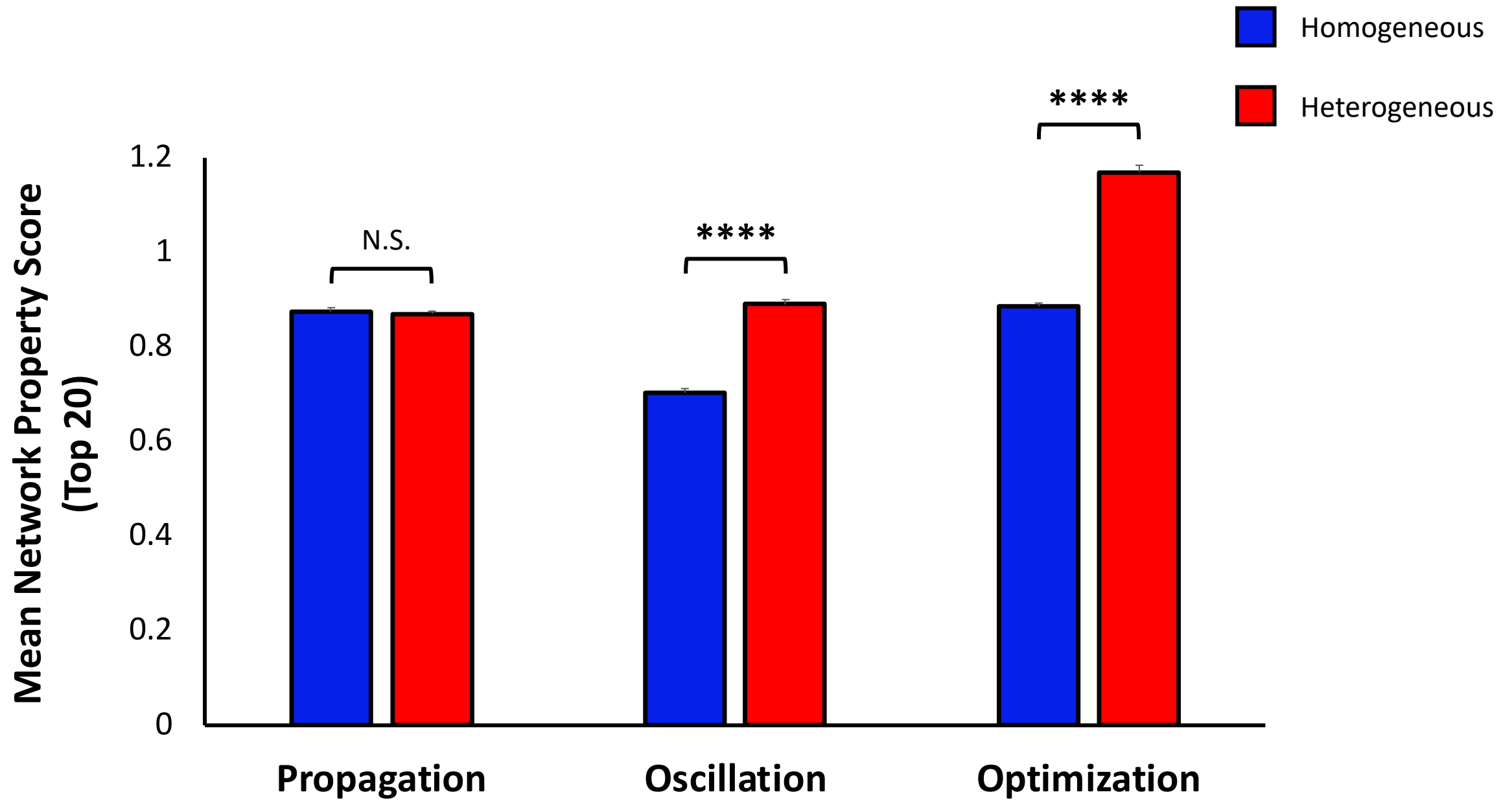
910 [unpaired  $t$ -test,  $t(38)=0.46$ ,  $p=0.647$ ]. By contrast, oscillation and optimization scores were significantly  
911 higher in top-performing heterogeneous networks than their homogeneous counterparts [oscillation:  
912  $t(38)=13.88$ ,  $p<0.0001$ ; optimization:  $t(38)=18.04$ ,  $p<0.0001$ ]. Each bar corresponds to a mean of the top  
913 20 network propagation or oscillation scores within each synaptic architecture group; error bars indicate  
914 standard errors of the mean. \*\*\*\*= $p<0.0001$ ; N.S.=not significant.

**A****B****C****D**



**A****B**





**Table S1. Normalized linear and second-order regression coefficients for propagation and oscillation in homogeneously varied synaptic networks.**

Normalized Regression Coefficients (NRCs)				
Synaptic Variable	Propagation Linear	Propagation 2°	Oscillation Linear	Oscillation 2°
TRN-TRN <sub>GABA</sub>	-0.173	-0.670	-	0.060
TRN-TRN <sub>Elec</sub>	-0.136	-0.347	-	-
TRN-TC	1.000	1.000	-1.000	-0.052
(TRN-TRN <sub>GABA</sub> ) <sup>2</sup>	-	0.332	-	-
(TRN-TRN <sub>Elec</sub> ) <sup>2</sup>	-	0.164	-	-
(TRN-TC) <sup>2</sup>	-	0.594	-	-1.000
TRN-TRN <sub>GABA</sub> x TRN-TRN <sub>Elec</sub>	-	0.262	-	-
TRN-TRN <sub>GABA</sub> x TRN-TC	-	-0.152	-	-
TRN-TRN <sub>Elec</sub> x TRN-TC	-	-0.365	-	-

• The regressions include 1°, 2°, and interaction terms corresponding to TRN-TRN<sub>GABA</sub>, TRN-TRN<sub>Elec</sub>, and open-loop TC-TRN-TC synapses/pathways. Terms associated with regression coefficients of absolute values < 0.05 are omitted. Positive and negative terms are highlighted in red and blue, respectively. Linear regression for propagation,  $R^2=0.793$ , RMSE=0.047,  $p<0.0001$ ; second-order regression for propagation,  $R^2=0.842$ , RMSE=0.041,  $p<0.0001$ ; linear regression for oscillation,  $R^2=0.526$ , RMSE=0.145,  $p<0.0001$ ; second-order regression for oscillation,  $R^2=0.630$ , RMSE=0.128,  $p<0.0001$ .

**Table S2. Normalized linear and second-order regression coefficients for propagation and oscillation in heterogeneously varied synaptic networks.**

Normalized Regression Coefficients (NRCs)				
Synaptic Variable	Propagation Linear	Propagation 2°	Oscillation Linear	Oscillation 2°
TRN <sub>A</sub> -TRN <sub>C</sub>	-	-	0.115	-
TRN <sub>C</sub> -TRN <sub>A</sub>	-0.088			
TRN <sub>C</sub> -TRN <sub>B</sub>	-0.084	-0.073	-	-
TRN <sub>A</sub> =TRN <sub>B</sub>	-0.051	-0.091	-	-
TRN <sub>A</sub> =TRN <sub>C</sub>	-0.072	-	-	-
TRN <sub>B</sub> =TRN <sub>C</sub>	-	-0.113	0.117	-
TRN <sub>A</sub> -TC <sub>A</sub>	-0.075	-	0.621	0.077
TRN <sub>A</sub> -TC <sub>B</sub>	0.608	0.571	-0.289	-1.000
TRN <sub>B</sub> -TC <sub>B</sub>	-0.128	-0.196	0.333	0.417
TRN <sub>B</sub> -TC <sub>C</sub>	1.000	1.000	-0.379	-0.892
TRN <sub>C</sub> -TC <sub>C</sub>	-0.207	-0.239	1.000	0.107
(TRN <sub>C</sub> -TRN <sub>B</sub> ) <sup>2</sup>	-	0.079	-	-
(TRN <sub>A</sub> -TC <sub>B</sub> ) <sup>2</sup>	-	-0.245	-	0.189
(TRN <sub>B</sub> -TC <sub>B</sub> ) <sup>2</sup>	-	0.174	-	-0.093
(TRN <sub>B</sub> -TC <sub>C</sub> ) <sup>2</sup>	-	-0.472	-	0.278
(TRN <sub>C</sub> -TC <sub>C</sub> ) <sup>2</sup>	-	0.187	-	-0.146

Normalized Regression Coefficients (NRCs), continued		
Synaptic Variable	Propagation 2°	Oscillation 2°
TRN <sub>A</sub> -TRN <sub>B</sub> x TRN <sub>A</sub> -TC <sub>B</sub>	0.070	-
TRN <sub>A</sub> -TRN <sub>C</sub> x TRN <sub>C</sub> -TC <sub>C</sub>	-	0.215
TRN <sub>B</sub> -TRN <sub>A</sub> x TRN <sub>A</sub> =TRN <sub>B</sub>	-	0.111
TRN <sub>B</sub> -TRN <sub>A</sub> x TRN <sub>A</sub> -TC <sub>A</sub>	-	-0.186
TRN <sub>C</sub> -TRN <sub>A</sub> x TRN <sub>A</sub> -TC <sub>A</sub>	-	-0.172
TRN <sub>C</sub> -TRN <sub>A</sub> x TRN <sub>A</sub> -TC <sub>B</sub>	-0.119	-
TRN <sub>C</sub> -TRN <sub>A</sub> x TRN <sub>B</sub> -TC <sub>C</sub>	-0.096	-
TRN <sub>C</sub> -TRN <sub>B</sub> x TRN <sub>B</sub> -TC <sub>C</sub>	-0.153	-
TRN <sub>A</sub> =TRN <sub>B</sub> x TRN <sub>B</sub> -TC <sub>C</sub>	-	-0.129
TRN <sub>A</sub> =TRN <sub>C</sub> x TRN <sub>A</sub> -TC <sub>A</sub>	-	-0.114
TRN <sub>A</sub> =TRN <sub>C</sub> x TRN <sub>C</sub> -TC <sub>C</sub>	-0.079	-
TRN <sub>A</sub> -TC <sub>A</sub> x TRN <sub>A</sub> -TC <sub>B</sub>	-	0.634
TRN <sub>A</sub> -TC <sub>A</sub> x TRN <sub>B</sub> -TC <sub>C</sub>	-	0.449
TRN <sub>A</sub> -TC <sub>B</sub> x TRN <sub>B</sub> -TC <sub>B</sub>	-0.166	0.361
TRN <sub>A</sub> -TC <sub>B</sub> x TRN <sub>B</sub> -TC <sub>C</sub>	0.753	-0.274
TRN <sub>A</sub> -TC <sub>B</sub> x TRN <sub>C</sub> -TC <sub>C</sub>	-0.106	0.669
TRN <sub>B</sub> -TC <sub>B</sub> x TRN <sub>B</sub> -TC <sub>C</sub>	-	0.345
TRN <sub>B</sub> -TC <sub>B</sub> x TRN <sub>C</sub> -TC <sub>C</sub>	-	-0.192
TRN <sub>B</sub> -TC <sub>C</sub> x TRN <sub>C</sub> -TC <sub>C</sub>	-0.124	0.399

• The regressions include 1°, 2°, and interaction terms corresponding to the 14 variable synapses in the networks. Equal signs denote gap junctions. Linear regression for propagation,  $R^2=0.742$ ,  $RMSE=0.069$ ,  $p<0.0001$ ; second-order regression for propagation,  $R^2=0.857$ ,

RMSE=0.051,  $p < 0.0001$ ; linear regression for oscillation,  $R^2=0.253$ , RMSE=0.131,  $p < 0.0001$ ; second-order regression for oscillation,  $R^2=0.388$ , RMSE=0.118,  $p < 0.0001$ .

**Table S3. Intrinsic model cellular parameters.**

Model Cellular Parameters			
Parameter	TC cell	TRN cell	L4 cell
Leak conductance, $g_L$ (nS)	3.263	3.7928	4.8128
Leak reversal potential, $E_L$ (mV)	-60.03	-57	-60.2354
Transient sodium conductance, $g_{Na}$ (nS)	1,500	3,000	3,000
Sodium equilibrium potential, $E_{Na}$ (mV)	50		
Delayed-rectifier potassium conductance, $g_K$ (nS)	520	400	140
M-type potassium conductance, $g_M$ (nS)	-	3.5	1.5
M-type potassium time constant, $\tau_M$ (ms)	-	200	180
Potassium equilibrium potential, $E_K$ (mV)	-100		-90
T-type calcium conductance, $g_T$ (nS)	45	21	-
Calcium equilibrium potential, $E_T$ (mV)	120		
H-current conductance, $g_H$ (nS)	0.608	0.0192	-
H-current reversal potential, $E_H$ (mV)	-33		-
Membrane capacitance, $C_m$ (pF)	100.4	75.0	109.3865

**Table S4. Model synaptic parameters.**

Model Synaptic Parameters						
Synapse	Neurotransmitter	Conductance (nS)	$\tau_{\text{recov}}$ (ms)	$\tau_{\text{inact}}$ (ms)	Reversal Potential (mV)	$U_{SE}$
External synapse to TC cell	(Glutamate)	32	125	2.64	0	0.76
TC-to-TRN cell synapse (TC-TRN)	Glutamate	150	500	2.64	0	0.76
TC-to-L4 cell synapse (TC-L4)	Glutamate	50	160	11.52	0	0.8113
TRN-to-TC cell synapse (TRN-TC)	GABA <sub>A</sub>	Variable (0-80)	167.29	16.62	-80	0.62
Chemical TRN-to-TRN cell synapse (TRN-TRN <sub>GABA</sub> )	GABA <sub>A</sub>	Variable (0-450)	225	15	-75	0.62