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Quadrupole transitions of the $1 \leftarrow 0$ band of N_2 observed in a high resolution atmospheric spectrum

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Résumé. — Un spectre d'absorption à haute résolution de l'atmosphère terrestre enregistré à Kitt Peak à l'aide d'un spectromètre par transformation de Fourier a permis d'observer les transitions quadrupolaires S7 à S16 de la bande 1 \leftarrow 0 de N₂. L'analyse des largeurs équivalentes et des profondeurs centrales de ces raies conduit, d'une part à la détermination de la dérivée du moment quadrupolaire $(\partial Q/\partial r)_e = (0.94 \pm 0.05) ea_0$ et d'autre part, à une estimation du coefficient d'élargissement par l'air $\gamma_{N_2-air}^0 = 0.06 \pm 0.02$ cm⁻¹ atm.⁻¹ à 296 K. En outre l'identification des raies telluriques observées entre 2 391,5 et 2 467 cm⁻¹ est donnée.

Abstract. — Using a high resolution atmospheric absorption spectrum recorded at Kitt Peak with the solar Fourier transform spectrometer, it has been possible to observe the quadrupole transitions S7 to S16 of the $1 \leftarrow 0$ band of N₂. The analysis of the equivalent widths and of the central depths of these lines has enabled us to determine the derivative of the quadrupole moment $(\partial Q/\partial r)_e = (0.94 \pm 0.05) ea_0$ and to estimate the broadening coefficient by air $\gamma_{N_2-air}^0 = 0.06 \pm 0.02$ cm⁻¹ atm.⁻¹ at 296 K. Finally the assignment of telluric lines between 2 391.5 and 2 467 cm⁻¹ is also given.

1. Introduction. — Fourier transform spectroscopy is able to produce spectra of very high resolution as well as very high signal to noise ratio. These qualities are very useful in atmospheric physics since it is now possible to detect very weak absorptions due to the most intense lines of trace gases or due to the weakest lines of more abundant constituents. The atmospheric spectrum between 2 391.5 and 2 467 cm⁻¹ studied in this work has been recorded with the solar Fourier transform spectrometer of Kitt Peak National Observatory (2 078 m) with a resolution of 0.009 cm^{-1} using the sun as a source. This spectral region which lies just above the end of the very strong $CO_2 v_3$ band (see Fig. 1) is influenced by the CO_2 continuum and to a lesser extent by the N_2 continuum but is relatively free of any strong lines. These conditions are favourable to search for the quadrupole lines of the $1 \leftarrow 0$

band of N_2 the intensity of which is expected to be very small.

2. Analysis. — The spectrum was recorded around 11.00 AM (local time) on October 25, 1979 at an average secant of 1.475. The ground pressure was 798 mbars and the ground temperature 23 °C. A portion of the spectrum is shown in figure 1. Using the AFGL line parameter compilation [1] the CO₂, N₂O and CH₄ telluric lines were first identified but some strong enough lines were left unassigned. Among them, some lines much broader than the telluric ones (see Fig. 2) were tentatively attributed to the sun. Some others were without any doubt of telluric origin because their profile was the result of the superposition of a wide tropospheric contribution and of a narrow stratospheric one. Using the

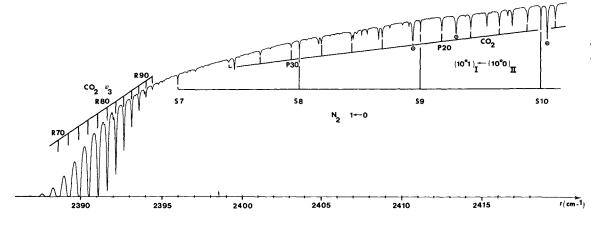


Fig. 1. — Portion of the atmospheric spectrum between 2 387 and 2 420 cm⁻¹. The lines S7 to S10 of the $1 \leftarrow 0$ quadrupole band of N₂ are easily seen superimposed on the CO₂ and N₂ continua. Some CO₂ and solar lines also appear.

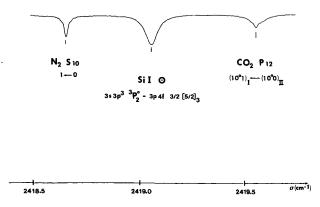


Fig. 2. — Detailed portion of the atmospheric spectrum showing the S10 quadrupole line of the $1 \leftarrow 0$ band of N₂ together with a Si I solar line and a CO₂ telluric line. Observe the very different line profiles : The solar line is very broad; when comparing the N₂ and CO₂ lines, the stratospheric part of the N₂ line is more prominent because the lower state energy of the CO₂ transition is much higher (hot band).

results obtained by Bendtsen [2] on the Raman spectrum of N₂ it has been possible to assign these lines to the quadrupole transitions S7 to S16 of the $1 \leftarrow 0$ band of the nitrogen molecule (¹). We have gathered in table I the list of the lines observed in the spectrum with their position, assignment and central depth.

3. **Results.** — It is important to deduce from our atmospheric spectrum quantitative results on the intensity of the N₂ lines because it seems difficult to obtain in the laboratory an optical density $P \times l$ comparable to what can be reached using the atmosphere as the absorbing medium

$$(P \times l \simeq 5 \times 10^5 \text{ atm. cm})$$
 .

Thus, we have performed a quantitative analysis based on a simplified atmospheric model (constant temperature gradient of 6 K/km in the troposphere, constant temperature of 209 K above 15 km in the stratosphere) to reproduce the observed equivalent widths W and central depths H of the N₂ lines. From these quantities (see columns 5 and 6 of table II) we have deduced the intensities $k_{\sigma}^{\rm N}$ (in cm⁻¹/molecule cm⁻¹) at 296 K of 7 lines of the quadrupole 1 \leftarrow 0 band and we have estimated an average broadening coefficient $\gamma_{\rm N_2-air}^{\rm 0} = 0.06 \pm 0.02$ cm⁻¹ atm.⁻¹ at 296 K. This calculation is based on the equations :

$$\tau(\sigma') = \int_0^\infty k_\sigma^{N}(T) N(z) \Phi(T, P, \sigma') dz$$
$$W = \int_{\substack{\text{on the} \\ \text{line}}} [1 - \exp(-\tau(\sigma'))] d\sigma'$$
$$H = \int_{\substack{\text{on the} \\ \text{line}}} f(\sigma - \sigma') [1 - \exp(-\tau(\sigma'))] d\sigma$$

where

- N(z) is the number density at altitude z (in molecule cm⁻³); - $\Phi(T, P, \sigma')$ is the normalized line profile :

$$\Phi(T, P, \sigma') \,\mathrm{d}\sigma' = 1 \,;$$

- $f(\sigma - \sigma')$ is the normalized instrumental profile : $\int f(\sigma - \sigma') d\sigma' = 1.$

The line profile Φ is a Voigt profile involving the Doppler half-width $\gamma_D(T)$ and the Lorentz half-width $\gamma_L(T, P) = \gamma^0(T_0) \frac{P}{P_0} \left(\frac{T_0}{T}\right)^{1/2}$.

The intensity of a quadrupole line v', $J' \leftarrow v$, J [3] is given by :

$$k_{\sigma}^{N}(T) = \frac{8 \pi^{5}}{15 hc} \sigma^{3} e^{-E''/kT} g_{J} \frac{(2 J + 1)}{Z(T)} \times |\langle J 0 20 | J' 0 \rangle|^{2} |\langle v | Q | v' \rangle|^{2}$$

^{(&}lt;sup>1</sup>) The S6 line is barely visible between the very strongly absorbing R68 and R70 ν_3 lines of CO₂.

Table I. — Atmospheric spectrum between 2 392 and 2 465 cm⁻¹.

The meaning of the different columns is: σ : Wavenumber (in cm⁻¹) of the line. For solar lines, because of the Doppler shift, the actual wavenumber is $\sigma \times 1.000\ 001\ 941\ 5$. P: Percentage of absorption at the centre of the line. The notation b in this column means that the corresponding line is blended in a stronger one; in this case the neighbouring lines are joined by a brace.

Assignment : For telluric CO₂ or N₂O lines, except when explicitly stated, the vibrational assignment is : for CO₂ $(10^{0}1)_{I} - (10^{0}0)_{II}$: for N₂O $(12^{0}0) - (00^{0}0)$ or $(13^{1}0) - (01^{1}0)$ when the c, d notation appears.

Telluric CH₄ lines belong to the P branch of the 2 v_4 band. \odot means a solar line,) or) means that the line lies respectively downward or upward of the quoted position of the blend.

| σ | Р | Assignment | σ | Р | Ass | ignment | σ | P | Assignment |
|------------------------|-----------------------|--|------------------------|----------------------|------------------|-----------------------------------|------------------------|---------------------------------|--|
| (cm ⁻¹) | (%) | | (cm ⁻¹) | (%) | | - | (cm ⁻¹) | (%) | Ū |
| 2391.6520 | 94 | $CO_2 \nu_3 R 80$ | 2431.6772 | 1.2 | CO 2 | R 2 | 2449.8000 | (b | N ₂ O P9c |
| 2392.0050 2392.1740 | 4.8 75 | CO ₂ V ₃ R 82 | 2431.7680 2431.9780 | 2.3 0.8 | CH₄ N₂O | P 29 c | 2449.8412 2450.1072 | 2.7 45 | N ₂ O P9d+CH ₄ N ₂ O P14 |
| 2392.6740 | 51 | $CO_2 \nu_3 R 82$ $CO_2 \nu_3 R 84$ | 2432.524 | 19 0 ? | | P 34 + CH ₄ | 2450.2112 | (⁴ _b | CO_2 R 30 |
| 2393.1480 | 30 | CO ₂ V ₃ R 86 | 2432.8980 | 0.8 | N ₂ O | Р 28 с | 2450.4484 | 1.3 | - |
| 2393.5976 | 18 3.4 | $CO_2 \nu_3 R 88$ | 2433.1760 2433.3840 | 4.3 /13 | CO2 N2O | R 4 P 33 | 2450.6604 | 1.0 | N ₂ O P 8 c |
| 2393.9208 2394.0196 | 8.3 | CO ₂ V ₃ R 90 | 2433.3840 | (¹³ b | N20 | P 28 d | 2450.8480 2450.9680 | 47 | CH ₄ N ₂ O P 13 |
| 2394.4176 | 4.1 | CO ₂ V ₃ R 92 | 2433.5876 | 8.8 | N ₂ | S 12 | 2451.0732 | 6.3 | CH4 |
| 2395.9652 | 8.3 | N ₂ S 7 | 2433.8120 2434.2840 | 0.9 | N20 N20 | Р 27 с Р 32 | 2451.3400 2451.5192 | 2.3 | CO ₂ R 32 N ₂ O P 7 c |
| 2397.0472 2399.0644 | 1.9 2.6 | CO ₂ P 36 CO ₂ P 34 | 2434.2840 | 16 5.4 | | F 52 R 6 | 2451.5192 | 1.3 1.3 | N ₂ O P7c N ₂ O P7d |
| 2399.4228 | 8.7 | 0 | 2434.75 | 0.8 | N ₂ O | Р 26 с | 2451.8268 | 44 | N ₂ O P 12 |
| 2401.0532 | 3.0 | CO ₂ P 32 | 2435.1804 | 17 | N ₂ O | P 31 | 2452.2816 | 8.0 | CH4 |
| 2403.0200 2403.5656 | 3.6 12 | CO ₂ P 30 N ₂ S 8 | 2435.6360 2435.8420 | 1.0 | N ₂ O | Р 25 с | 2452.3800 2452.4376 | (b 2.3 | N ₂ O P6c,d CO ₂ R34 |
| 2404.7640 | /Ъ | СН4 | 2436.0760 | 24 | N20 | $P 30 + CO_2 R 8)$ | 2452.6840 | 43 | N ₂ O P 11 |
| 2404.7896 | 4.5 | CH4 | 2436.5412 | 1.1 | N ₂ O | Р 24 с | 2452.8456 | 7.0 | CH4 |
| 2404.9600 2406.8756 | 4.5 | CO ₂ P 28 CO ₂ P 26 | 2436.9676 2437.4484 | 22. /b | N20 N20 | Р 29 Р 23 с | 2453.2280 2453.3540 | 1.3 | N ₂ O P 5 c,d |
| 2406.9720 | 3.0 | CH4 | 2437.5128 | (7.0 | CO2 | R 10 | 2453.5388 | 42 | N ₂ O P 10 + CO ₂ R 36 |
| 2407.1720 | 1.3 | | 2437.8588 | 28 | N_2O | P 28 + X | 2454.0760 | 1.1 | N ₂ O P 4 c,d |
| 2407.4880 | 3.4 | CH4 | 2438.3464 2438.7460 | 1.1 26 | N 20 N 20 | P 22 c P 27 | 2454.3924 | 39 | N ₂ O P 9 |
| 2407.8428 2408.5480 | 3.4 7.9 | СН 4 СН 4 | 2438.9040 | 6.6 | CO 2 | R 12 | 2454.9212 2455.2440 | 0.8 37 | N ₂ O P 3 c,d N ₂ O P 8 |
| 2408.7648 | 6.6 | CO ₂ P 24 | 2439.1372 | 0.9 | | | 2455.5364 | 0.8 | N20 1 0 |
| 2409.2272 | 2.2 | ⊙Si I | 2439.2444 | 1.1 | N ₂ O | P 21 c | 2455.7004 | 2.1 | N ₂ S 15 |
| 2410.0140 2410.4160 | 1.4 | © 51 1 CH4 | 2439.6320 2440.1408 | 28 1.1 | N20 N20 | Р 26 Р 20 с | 2456.0944 2456.3684 | 34 1.6 | N ₂ O P 7 |
| 2410.6320 | (b) | CO ₂ P 22 | 2440.2680 | 6.9 | CO ₂ | R 14 | 2456.5550 | 2.4 | |
| 2410.6560 | \II | ⊙Si I+CH4) | 2440.4216 | 0.7 | N ₂ O | P 20 d | 2456.9428 | 31 | N ₂ O P 6 |
| 2411.1280 | 6.7 | N ₂ S 9 | 2440.5160 2440.9976 | 30 4.6 | N ₂ O | P 25 S 13 | 2457.0740 | 8.9 | \odot Si I N ₂ O (13 ¹ 0)-(01 ¹ 0) Q |
| 2412.4660 2413.3610 | 7.9 10 | CO ₂ P 20 © Si I | 2440.9970 | (^{4.0} | N2 N20 | P 19 c | 2457.4488 2457.7888 | 1.3 29 | $N_{2}O (13 O) = (01 O) Q$ $N_{2}O P 5 + O Si I$ |
| 2414.2776 | 8.3 | CO ₂ P 18 | 2441.2840 | (b | N_2O | P 19 d | 2458.6344 | 22 | N ₂ O P 4 |
| 2415.2824 | 7.2 | ⊙ ? | 2441.3972 | 133 | N ₂ O | P 24 | 2458.7940 | 1.6 | |
| 2416.0628 2416.5760 | 8.3 3.3 | CO ₂ P 16 © ? | 2441.4868 2441.5992 | 6.8 /11 | CH4 CH4 | + CO ₂ R 16 | 2459.4776 2459.5744 | 18 8.4 | N2O P3 CH4 |
| 2416.8600 | 9.0 | õ? | 2441.6464 | (ъ | CH 4 | 507 <u>1</u> 1 10 | 2459.7740 | 8.3 | CH4 |
| 2417.8212 | 8.1 | CO ₂ P 14 | 2441.9216 | 1.1 | N ₂ O | P 18 c | 2460.1360 | 13 | ⊙ ? |
| 2418.6520 | 13 | N₂ S 10 @SiI | 2442.1460 2442.2772 | 1.1 34 | N20 N20 | P 18 d P 23 | 2460.3192 2461.1588 | 11 5.8 | N ₂ O P 2 N ₂ O P 1 |
| 2419.0576 2419.5524 | 18 7.8 | CO ₂ P 12 | 2442.8100 | 1.1 | N ₂ 0 | P 17 c | 2462.8332 | 5.3 | N ₂ O R O |
| 2421.2572 | 7.0 | CO ₂ P 10 | 2442.9152 | 8.8 | CO ₂ | R 18 | 2462.9936 | 3.6 | N ₂ S 16 |
| 2421.4640 | 1.4 | N ₂ O P 46 | 2443.0048 | 1.1 37 | N ₂ O | P 17 d P 22 | 2463.2360 | (¹⁵ [⊚] ?+ | N ₂ O R 6 c |
| 2422.3996 2422.7372 | 1.5 | N ₂ O P 45 | 2443.1552 2443.6920 | 1.0 | N20 N20 | P 16 c | 2463.2848 2463.6680 | 11 | N ₂ O R 6 d N ₂ O R 1 |
| 2422.9356 | 5.6 | CO2 P8 | 2443.8664 | 1.0 | N20 | P 16 d | 2463.8472 | 11 | 0? |
| 2423.2560 | 2.5 | CH4 | 2444.0308 | 38 | N20 | P 21 | 2464.1172 | 1.6 | N ₂ O R 7 d |
| 2423.3132 2424.2560 | 5.1 2.1 | X? + CH ₄ + N ₂ O P 44 ⁾ N ₂ O P 43 | 2444.1976 2444.5724 | 5.3 1.0 | CO2 N2O | R 20 Р 15 с | 2464.5004 2464.6848 | 17 0.7 | N2O R 2 CH4 |
| 2424.2360 | 4.5 | CO ₂ P 6 | 2444.7240 | 1.0 | N20 | P 15 d | 2464.8632 | 1.2 | N ₂ O R 8 c |
| 2424.8780 | 3.6 | ⊙ Si I | 2444.9040 | 40 | N_2O | P 20 | 2464.9496 | 1.6 | N_2O R 8 d + CH ₄ |
| 2425.1800 | 3.2 | N ₂ O P 42 N ₂ O P 41 | 2445.4536 2445.7760 | 8.0 42 | CO2 N2O | R 22+N ₂ 0P14 c P19 | 2465.3320 2465.6744 | 22 | N ₂ O R 3 N ₂ O R 9 c |
| 2426.1028 2426.1392 | (^в 7.1 | N ₂ O P 41 N ₂ S 11 | 2445.9724 | 9.5 | οs | | 2465.7164 | (b 3.5 | CH4 |
| 2426.2080 | 1.2 | CO ₂ P 4 | 2446.3252 | 1.4 | N_2O | P 13 c | 2465.7768 | ∖ь | N ₂ O R 9 d |
| 2427.0212 | 4.3 | N ₂ O P 40 | 2446.4340 2446.6460 | 1.4 44 | N20 N20 | P 13 d P 18 + $CO_2R 24^3$ | 2466.1608 | 28 1.0 | N ₂ O R 4 N ₂ O R 10 c |
| 2427.3180 2427.8052 | 1.1 | CO ₂ P 2 | 2447.1988 | 1.4 | N20 | P 12 c | 2466.6092 | 11 | © ? + R 10 d + CH |
| 2427.9380 | 5.1 | N ₂ O P 39 | 2447.2880 | 1.4 | N ₂ O | P 12 d | 2466.9884 | 34 | N ₂ O R 5 |
| 2428,8200 | $\binom{13}{3}$ | CH4 | 2447.5140 | 43 | N ₂ 0 | P 17 R 26 | | | |
| 2428.8480 2429.1568 | \ь 5.9 | N ₂ O P 38 CH ₄ | 2447.8876 2448.0688 | 4.8 1.4 | CO2 N2O | P 11 c | | | |
| 2429.1508 | 5.7 | CH4 | 2448.1404 | 1.4 | N20 | Plld | | | |
| 2429.7640 | 7.6 | N ₂ O P 37 | 2448.3800 | 46 | N20 | P 16+N ₂ S 14 | | | |
| 2429.9360 | 1.2 | N ₂ O P 36 | 2448.9348 2448.9960 | 1.4 | N20 N20 | P 10 c + CH | | | |
| 2430.6720 2431.0680 | 8.5 9.2 | N ₂ O P 36 CH ₄ | 2449.0856 | 9.1 | | i 1+CO ₂ R 28 | | | |
| 2431.5796 | 13 | N ₂ O P 35 + CH ₄ | 2449.2444 | 45 | N_2O | P 15 | | | |
| | | | | | | | | | |

| Assign- ment | $\sigma_{obs.}$ (cm ⁻¹) | $\sigma_{calc.}$ $(cm^{-1})^{(a)}$ | E'' (cm ⁻¹) (^{<i>a</i>}) | W (10 ⁻³ cm ⁻¹) | P (%) | $k_{\sigma}^{\mu}(\text{obs.})$ $k_{\sigma}^{\nu}(\text{calc.})$ (°) ($10^{-28} \text{ cm}^{-1}/\text{molecule}^{-2}$ at 296 K) | | $\left(\frac{\partial Q}{\partial r}\right)_{e}/ea_{0}(b)$ |
|-----------------|-------------------------------------|------------------------------------|--|--|----------|--|------|--|
| — | | | | — | | | — | _ |
| S7 | 2 395.965 2 | .969 1 | 111.398 | 3.43 | 8.3 | 1.78 | 1.57 | 1.00 |
| S8 | 2 403.565 6 | .568 5 | 143.219 | 5.58 | 11.7 | 2.97 | 3.04 | 0.93 |
| S9 | 2 411.128 0 | .130 5 | 179.015 | 2.23 | 6.7 | 1.22 | 1.42 | 0.87 |
| S10 | 2 418.652 0 | .654 8 | 218.783 | 4.84 | 12.6 | 2.76 | 2.60 | 0.97 |
| S11 | 2 426.139 2 | .141 1 | 262.523 | | | | 1.15 | |
| S12 | 2 433.587 6 | .589 3 | 310.233 | 3.24 | 8.8 | 2.03 | 1.99 | 0.95 |
| S13 | 2 440.9 976 | .998 9 | 361.912 | | | | 0.84 | |
| S14 | (^b) | 2 448.369 8 | 417.557 | | | | 1.38 | |
| S15 | 2 455.700 4 | .701 6 | 477.166 | 0.682 | 2.1 | 0.49 | 0.56 | 0.88 |
| S16 | 2 462.993 6 | .994 1 | 540.738 | 1.30 | 3.6 | 0.98 | 0.88 | 1.00 |
| | | | | | | | | 0.94 ± 0.05 |

Table II. — N_2 quadrupole vibration-rotation lines (1-0 band).

(a) Calculated from J. Bendtsen [2].

(^b) See text.

where

Z(T) is the total partition function (for N₂ Z(296) = 465).

 g_J is the nuclear spin statistical weight (3 or 6 for J odd or even).

• N < 1 >

 $\langle j_1 m_1 j_2 m_2 | jm \rangle$ is a Clebsch-Gordan coefficient and we have :

$$|\langle J 0 20 | J' 0 \rangle|^{2} = \begin{cases} \frac{3 J(J-1)}{2(2 J-1) (2 J+1)} & \text{for O lines } (J' = J-2) \\ \frac{J(J+1)}{(2 J-1) (2 J+3)} & \text{for Q lines } (J' = J) \\ \frac{3(J+1) (J+2)}{2(2 J+1) (2 J+3)} & \text{for S lines } (J' = J+2) \end{cases}$$

If one writes

$$Q = Q_{e} + \left(\frac{\partial Q}{\partial r}\right)_{e} \Delta r + \cdots$$

one has to first order

$$\langle v | Q | v + 1 \rangle = \left(\frac{\partial Q}{\partial r}\right)_{\rm e} r_{\rm e} \left(\frac{B_{\rm e}}{\omega_{\rm e}}\right)^{1/2} \sqrt{v+1}.$$

Using the following spectroscopic data [4] :

$$r_{\rm e} = 1.097\ 685\ {\rm \AA}\ , \ \ B_{\rm e} = 1.998\ 24\ {\rm cm}^{-1}\ ,$$

 $\omega_{\rm e} = 2\ 358.57\ {\rm cm}^{-1}$

for each line, we have determined from the observed intensity $k_{\sigma}^{N}(obs.)$ a value of $(\partial Q/\partial r)_{e}/ea_{0}$ which is given in the last column of table II. The average value with its statistical errors is :

$$\left(\frac{\partial Q}{\partial r}\right)_{\rm e} = (0.94 \pm 0.05) \ ea_0$$

which is in good agreement with the values $0.95 ea_0$ [5] and $0.97 ea_0$ [6] deduced from collision-induced fundamental transitions. Finally using our value of $(\partial Q/\partial r)_e$ we have computed the intensities $k_{\sigma}^{N}(\text{calc.})$ quoted in table II. In addition to its atmospheric interest, this work shows that, when measuring the continuum in the laboratory, it is necessary to take into account the contribution of the quadrupole lines which have not been observed in such experiments because of a higher pressure and a lower resolution.

Note. — After this manuscript was ready, we have been aware of a paper by Goldman *et al.* [A. Goldman, J. Reid and L. S. Rothman, *Geophys. Res. Lett.* **8** (1981) 77] reporting the observation of O₂ quadrupole lines in the 1 600 cm⁻¹ region and mentioning the existence of N₂ quadrupole lines in the 2 400 cm⁻¹ region.

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