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Quantum phase transition from triangular to stripe charge order in NbSe₂

Anjan Soumyanarayanan^{a,b,1}, Michael M. Yee^a, Yang He^a, Jasper van Wezel^{c,d,2}, Dirk J. Rahn^e, Kai Rossnagel^e, E. W. Hudson^f, Michael R. Norman^c, and Jennifer E. Hoffman^{a,1}

^aDepartment of Physics, Harvard University, Cambridge, MA 02138; ^bDepartment of Physics, Massachusetts Institute of Technology, Cambridge, MA 02139; ^cMaterials Science Division, Argonne National Laboratory, Argonne, IL 60439; ^dH. H. Wills Physics Laboratory, University of Bristol, Bristol BS8 1TL, United Kingdom; ^eInstitute of Experimental and Applied Physics, University of Kiel, 24098 Kiel, Germany; and ^fDepartment of Physics, Pennsylvania State University, State College, PA 16802

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The competition between proximate electronic phases produces a complex phenomenology in strongly correlated systems. In particular, fluctuations associated with periodic charge or spin modulations, known as density waves, may lead to exotic superconductivity in several correlated materials. However, density waves have been difficult to isolate in the presence of chemical disorder, and the suspected causal link between competing density wave orders and high-temperature superconductivity is not understood. Here we used scanning tunneling microscopy to image a previously unknown unidirectional (stripe) charge-density wave (CDW) smoothly interfacing with the familiar tridirectional (triangular) CDW on the surface of the stoichiometric superconductor NbSe₂. Our low-temperature measurements rule out thermal fluctuations and point to local strain as the tuning parameter for this quantum phase transition. We use this quantum interface to resolve two longstanding debates about the anomalous spectroscopic gap and the role of Fermi surface nesting in the CDW phase of NbSe₂. Our results highlight the importance of local strain in governing phase transitions and competing phenomena, and suggest a promising direction of inquiry for resolving similarly longstanding debates in cuprate superconductors and other strongly correlated materials.

competing order | scanning tunneling spectroscopy | transition metal dichalcogenides

Whereas a classical phase transition separates two states of matter at different temperatures, two ordered ground states of a material at zero temperature are separated by a quantum critical point (QCP). The competition between proximate ordered phases near the QCP can dramatically influence a large region of the phase diagram (1). Whereas the fluctuations from competing quantum states lead to exotic physics even at higher temperatures, low-temperature studies of these states may lead to a better understanding of the root of the competition. Density waves—charge- or spin-ordered states of collective origin driven by instabilities of the Fermi surface (FS)—exist in close proximity to superconductivity (SC) in several classes of correlated materials (2–4), and various proposals emerged recently to study their interplay in the presence of strong inhomogeneity in these systems (5). In this light, it is surprising that charge-density waves (CDWs) are not fully understood, even in the weakly correlated and stoichiometric transition metal dichalcogenides (TMDCs). Whereas a classic CDW arises from strong FS nesting, resulting in a sharply peaked susceptibility and a Kohn anomaly at the CDW wavevector, the quasi-2D TMDCs are known to deviate from this picture (6, 7).

NbSe₂ is a layered TMDC that has generated much recent interest (8–10) as a model system for understanding the interplay of the CDW and SC phases with onset at $T_{\text{CDW}} \sim 33$ K and $T_{\text{SC}} \sim 7$ K respectively (11, 12). Despite extensive study (9, 13–16), several key facts about its familiar tridirectional (3Q) CDW remain unresolved, including the role of FS nesting in determining its wavevector \vec{q}_{3Q} and the magnitude of the spectral gap and its

role in the energetics of the transition. First, angle-resolved photoemission (ARPES) studies have been unable to uniquely identify \vec{q}_{3Q} -nested FS regions in NbSe₂ (9, 13, 16–20). Meanwhile, recent studies indicate a broadly peaked susceptibility and a soft phonon over a range of wavevectors around \vec{q}_{3Q} (6, 15, 16), suggesting instead that the q -dependence of the electron-phonon coupling might play an important role in driving the transition. Second, kinks in tunneling spectra at ± 35 mV ($\pm \varepsilon_K$), historically identified as gap edges, correspond to an anomalously large energy scale for the corresponding T_{CDW} ($2\varepsilon_K/3.5k_B T_{\text{CDW}} \sim 7.05$) (21), whereas recent ARPES studies indicate a much smaller gap, ~ 3 –5 mV (13, 16).

Our discovery, by low-temperature scanning tunneling microscopy (STM), of a unidirectional (1Q) CDW with distinct wavelength and tunneling spectra from the 3Q CDW, in conjunction with band structure calculations, allows us to resolve both longstanding questions of the wavevector and the gap. First, the distinct wavelengths demonstrate that FS nesting plays a negligible role in setting their magnitude. Second, the distinct tunneling spectra of the 1Q CDW region help us disentangle the 3Q CDW spectra to expose a particle-hole asymmetric gap, riding on top of a strong inelastic background.

Results

Fig. 1A shows a topographic image of a locally commensurate ($3a_0$) CDW on 2H-NbSe₂. Its microscopic 3Q nature is confirmed by the existence of a secondary CDW peak in the Fourier transform (FT) in Fig. 1B, in contrast to bulk measurements (10). Phase slips result in an overall periodicity of $\lambda_{3Q} \simeq 3.05 a_0$, corresponding to $\vec{q}_{3Q} \simeq 0.328 \vec{Q}_0$, where \vec{Q}_0 is the Bragg vector (10, 11, 22). Our primary experimental discovery is shown in Fig. 2A, where regions of unidirectional (1Q) CDW with unique wavevector \vec{q}_{1Q} along a single 3Q direction form an atomically smooth interface with the 3Q CDW. The absence of atomic lattice discontinuities rules out the possibility of an NbSe₂ polytype interface (23). Although other TMDCs are known to exhibit a thermally induced triclinic CDW state that varies with doping near T_{CDW} (22, 24), no such anisotropy has been reported in 2H-NbSe₂. Moreover, our observations are at temperatures $T \ll T_{\text{CDW}}$, where thermal fluctuations are

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¹To whom correspondence may be addressed. E-mail: anjan@physics.harvard.edu or jhoffman@physics.harvard.edu.

²Present address: H.H. Wills Physics Laboratory, University of Bristol, Bristol BS8 1TL, United Kingdom.

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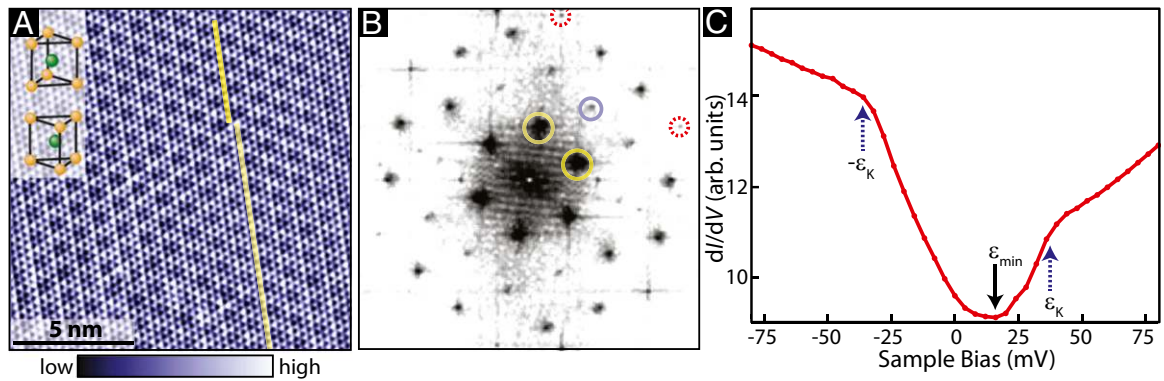


Fig. 1. STM of the 3Q CDW. (A) Atomic resolution topograph showing the $\sim 3 a_0$ periodic CDW. Yellow lines are overlaid on a one-atom shift of the CDW maximum (phase slip). (Inset) Crystal structure of $2H\text{-NbSe}_2$, with layers of Nb (green) atoms sandwiched between layers of Se (orange) atoms. (B) FT of a larger (~ 45 nm) topograph, displaying a 3Q CDW. Primary CDW wavevectors, \vec{q}_1 and \vec{q}_2 (yellow circles); a secondary CDW wavevector, $\vec{q}_1 + \vec{q}_2$ (blue circle); and Bragg vectors (dashed red circles) are indicated. (C) Average dI/dV spectrum acquired from the area in A, showing kinks at $\sim \pm 35$ mV ($\pm \varepsilon_K$), the minimum ε_{\min} offset from ε_F ($V_{\text{bias}} = 0$) by ~ 17 mV, and marked asymmetry about ε_F . Setpoint parameters: sample bias, $V_{\text{sample}} = -50$ mV (A), -60 mV (B) and -80 mV (C); junction resistance, $R_j = 2.5$ G Ω (A), 0.1 G Ω (B), and 0.4 G Ω (C); and root mean square (RMS) lock-in excitation, $V_{\text{rms}} = 3.5$ mV (C).

insignificant, implying that the 1Q CDW is a distinct quantum phase.

The 1Q CDW regions take the form of elevated topographic ribbons, exemplified in Fig. 2 B and C, suggesting a strain-induced phase (SI Text II). The observation of Y-junctions between ribbons with differently oriented \vec{q}_{1Q} rules out extrinsic uniaxial strain and suggests instead locally varying strain, perhaps because of underlying defects causing nanoscale buckling of the top few atomic layers. From a survey of several ribbons, we place upper bounds of 3% on the vertical strain and 0.06% on the lateral strain (SI Text II).

Fig. 3 A and B show the dominant Fourier peak for the 1Q modulation, $\vec{q}_{1Q} \simeq (2/7)\vec{Q}_0$, corresponding to a wavelength, $\lambda_{1Q} \simeq 3.5 a_0$. No similar periodicity or rich harmonic structure has been reported thus far in any TMDC system (12). We develop a phenomenological understanding of the 1Q harmonic structure following McMillan's Landau theory (22, 25). Rather than a uniform $3.5 a_0$ charge modulation, the system could lower its energy by locking the charge modulation to the lattice with $3 a_0$ periodicity. This would require compensation by a one-atom phase slip every two oscillations, corresponding to a $2\pi/3$ discommensuration, as shown in Fig. 3C (22). The resulting har-

monic structure shown in Fig. 3D reproduces all observed peak positions. Moreover, the rich harmonic content we observe is another indication of the strong coupling of the electronic modulation to the lattice. An even better agreement with relative peak heights might be obtained by considering spatial variations in the order parameter amplitude (22).

The stark contrast between our observation of two CDW wavevectors \vec{q}_{1Q} and \vec{q}_{3Q} of the same orientation but with 13% difference in magnitude, and the recent X-ray measurements reported by Feng et al. (10), provides strong evidence against FS nesting at one particular wavevector as a driving force for either CDW. Although our 13% wavevector difference arose from moderate anisotropic strain (up to 0.06% in-plane), Feng et al. applied hydrostatic pressure sufficient to induce in-plane lattice distortions up to 1.6%, yet observed no measurable deviation of the CDW wavevector from q_{3Q} (10). The observed insensitivity of q_{3Q} to hydrostatic pressure would clearly indicate that the FS does not qualitatively change in the presence of even relatively large lattice distortions, and thus would rule out a change in the FS as the source of our observed 13% wavevector difference. Furthermore, consistent with our experiment and with previous calculations (6, 15, 16), we find no sharp peak in the susceptibility

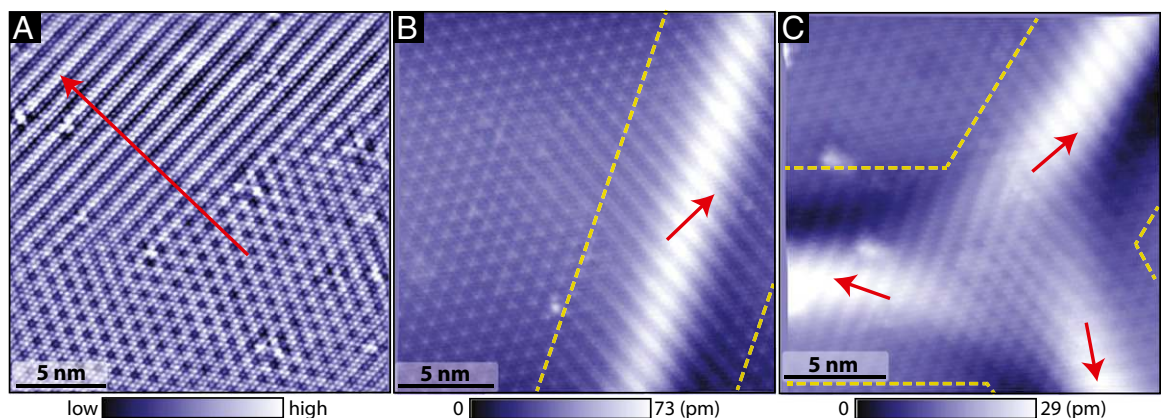


Fig. 2. The 1Q–3Q interface. (A) Topograph showing an atomically smooth interface between the 3Q (Bottom) and 1Q (Top) CDWs. (B) Topograph showing formation of 1Q CDW along a “ribbon.” Ribbons are typically 10–20 nm in width and elevated by 20–40 pm. Dashed yellow lines indicate the approximate extent of the ribbon; the red arrow points along the 1Q CDW direction (\vec{q}_{1Q}). (C) Topograph showing a Y-junction among three such 1Q ribbons, each with a different 1Q CDW direction. The topograph in A has been leveled by removing a polynomial background to show the CDW interface clearly. Setpoint parameters: $V_{\text{sample}} = -50$ mV, $R_j = 1$ G Ω (A and C), and 5 G Ω (B).

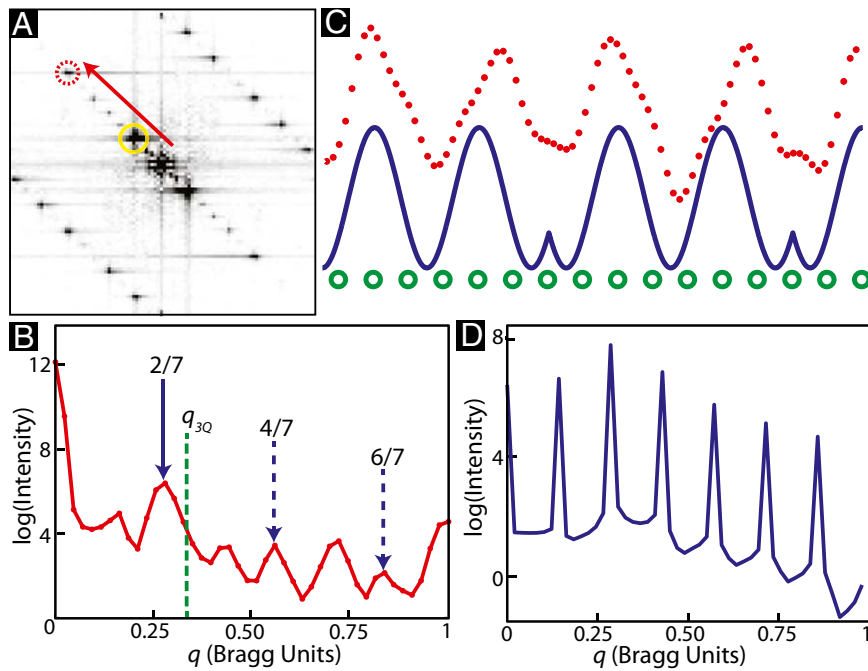


Fig. 3. The 1Q CDW. (A) FT of the out-of-feedback current at +50 mV over a 1Q region (upper left quadrant of Fig. 2A). The dominant CDW wavevector (yellow circle) and Bragg vector (dashed red circle) are indicated. (B) Linecut of the FT intensity parallel to the red line in A from the center to the Bragg peak, in units of the Bragg vector Q_0 . The dominant peak, $q_{1Q} \approx (2/7)Q_0$ (solid blue arrow), and its harmonics (dashed blue arrows) are identified and are distinct from the $3Q$ wavevector q_{3Q} (dashed green line). The remaining peaks are Bragg reflections of these three peaks. Setpoint parameters: $V_{\text{sample}} = -50$ mV and $R_j = 0.2$ G Ω . (C) Phenomenological model of the observed 1Q CDW wavelength, $\lambda_{1Q} \approx 3.5 a_0$ (details in text). The atomic periodicity is indicated by green circles, and the phase of the CDW order parameter from the model is shown in blue (22). A topographic linecut (red dots) is extracted from Fig. 2A along the red arrow (\vec{q}_{1Q}), filtered to remove atomic corrugations and overlaid for comparison. (D) Simulated FT intensity from the cartoon CDW modulation in C, for comparison with experimental peak positions in B.

(Fig. 4) computed from our modeled band structure (SI Text III). Therefore, our observations and calculations both indicate that the FS can play only a minor role in determining CDW wavevectors in NbSe₂. This highlights the key role the q -dependence of alternative mechanisms, such as electron–phonon coupling, may play in driving the transition, and particularly the manner in which these mechanisms may be influenced by local strain.

The two CDW regions display quite different tunneling spectra, as shown in Fig. 5 A and B. We use a fit to the NbSe₂ band

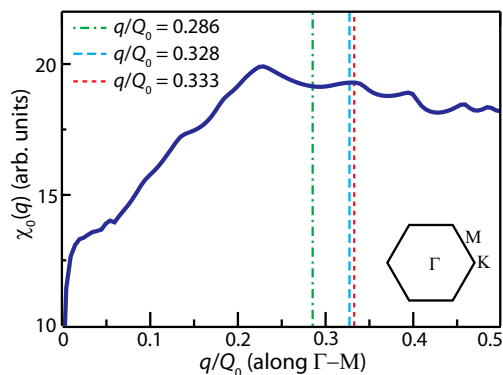


Fig. 4. Susceptibility. The noninteracting susceptibility $\chi_0(q, \omega=0)$ calculated from a fit to the NbSe₂ band structure (SI Text III) along the Γ -M direction of the reciprocal lattice, displaying a broad maximum over a range of wavevectors: $\vec{q} \sim (0.25 - 0.4)Q_0$ (6, 15, 16). The CDW wavevectors q_{1Q} , q_{3Q} , and $Q_0/3$ are overlaid for comparison. (Inset) Brillouin zone (BZ) of the hexagonal NbSe₂ lattice.

structure (SI Text III) and impose a CDW wavevector \vec{q} , gap $\tilde{\Delta}$, and broadening parameter $\tilde{\Gamma}$ to calculate the density of states (DOS) in Fig. 5C (SI Text IV). For the $3Q$ CDW state, the measured dI/dV spectrum, proportional to the DOS, is reproduced best using $\vec{q} = (0.333 \pm 0.004)Q_0$ (the observed local CDW periodicity), $\tilde{\Delta} = (12 \pm 2)$ mV (which previously was not apparent from direct observations by spectroscopic techniques), and $\tilde{\Gamma} = 5$ mV. The calculations capture the overall shape, width, and center ε_{min} of the gap structure within 30 mV of ε_F (SI Text IV). The fact that ε_{min} is offset from ε_F should be unsurprising for a quasi-2D system (26), but had not been understood or observed in NbSe₂ until now because of the limitations of spectroscopic techniques, which are sensitive to filled states only (13).

We disentangle the CDW gap from other effects in the $3Q$ spectra through a comparison with the $1Q$ spectra in Fig. 5B. These V-shaped $1Q$ spectra resemble the linear tunneling conductance background historically attributed to the inelastic coupling of tunneling electrons to a flat bosonic spectrum (27). That this background is much stronger in the $1Q$ region, obscuring band structure effects, likely is a strain-induced phenomenon, which may be related to the buckling and associated decoupling of the topmost layers in the $1Q$ region. Meanwhile, present in both $1Q$ and $3Q$ spectra (thus, unlikely to be associated with these different CDWs), yet absent in calculations (thus, unlikely to be a band structure effect), are the ± 35 mV kinks, previously and mistakenly identified as the CDW gap (21). We universally observe the kinks even well above T_{CDW} , which further demonstrates their lack of bearing on the CDW phase (SI Text IV). ARPES studies observe a prominent band structure kink at a similar energy in the Se Γ -pocket (16, 19), attributed to coupling to an optical phonon (14). Therefore, we conclude that this self-energy effect is responsible for the ε_K -kinks in the tunneling spectra as well. The discrepancy between the data

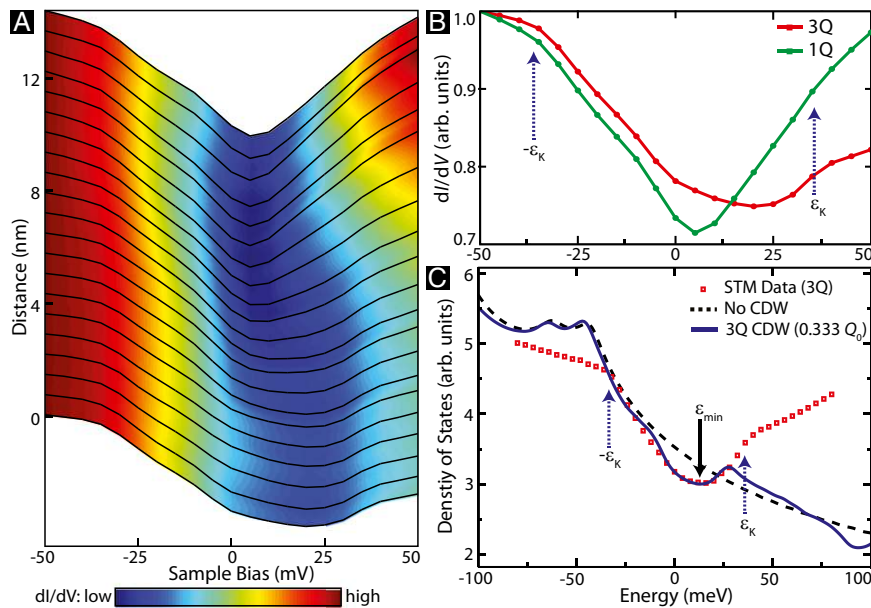


Fig. 5. Spectroscopy across the 1Q–3Q interface. (A) Linecut of dI/dV spectra across the 1Q–3Q interface taken along the red arrow in Fig. 2A. (B) Representative spectra in the 3Q (red) and 1Q (green) regions of Fig. 2A are overlaid for comparison. The 1Q spectra have a minimum close to ϵ_F , a deep V-shape with reduced asymmetry, and kinks at $\pm\epsilon_K$. The spectra are normalized at -50 mV. Setpoint parameters: $V_{\text{sample}} = -50$ mV, $R_I = 0.2$ G Ω , and $V_{\text{rms}} = 3.5$ mV. (C) Calculated DOS for NbSe₂ in the “normal” state (black) and in the presence of a 3Q CDW (blue) using $\tilde{q} = 0.333Q_0$, $\tilde{\Delta} = 12$ mV, compared with the 3Q STM spectrum (red) (details in *SI Text IV*). The calculations reproduce the observed asymmetry, offset ϵ_{min} , and shape of the gap structure.

and band structure calculations above ~ 30 mV in Fig. 5C thus may be attributed to the inelastic tunneling background and self-energy effects.

Discussion

We therefore resolve a longstanding debate about the anomalous CDW gap magnitude reported by STM measurements (21), and caution that not all ϵ_F -symmetric kinks in tunneling spectra are associated with order (e.g., density wave or superconducting gaps). On the contrary, we emphasize that the true CDW signature in NbSe₂ is offset from ϵ_F , which has confused an active research community for two decades, and has been disentangled now only by a combination of spatially resolved filled- and empty-state spectroscopy of a proximate (1Q) phase and band structure calculations (26). This emphasizes the need for full experimental exploration of proximate phases in other pertinent materials, combined with quantitative modeling. We further suggest that controlled local strain, through epitaxy or intentional defects, may be a useful tuning parameter to access the necessary proximate phases for comparison.

Beyond providing unique insight into the nature of the 3Q CDW in NbSe₂, our work motivates the utility of the 1Q–3Q interface in NbSe₂ as a platform to explore competing quantum phases in the weakly correlated limit, as a step toward understanding them in strongly correlated systems. In the Landau picture of CDWs (25), a quantum phase transition between 3Q and 1Q states may arise by tuning the coefficient of the interaction term among the three inequivalent CDW propagation directions (although in our case, the magnitude of q differs between the two states). In NbSe₂, even at low temperatures $T \ll T_{\text{CDW}}$, where the amplitude of the order parameter is already large, moderate strain is seen to have a strong influence, indicating that the system is intrinsically close to the QCP separating these states. We note that a related phase transition between the observed 1Q CDW phase and a “hidden” 2Q phase has been suggested, but not directly visualized, in the rare-earth tritellurides (28, 29).

Our discovery provides a unique perspective on the role of density wave order in complex systems. First, our resolution of

two longstanding debates about NbSe₂ puts this much-studied material on firmer footing as a well-understood model system for CDW studies and competing ground states in superconductors. We have disentangled the true CDW gap, and clarified that FS nesting plays a minor role in determining the CDW wavevectors in this material, thereby highlighting the role of other mechanisms in driving the transition. Second, our revelation of a particle-hole asymmetric CDW gap emphasizes the limitations of filled-state-only probes, e.g., ARPES, for investigating phases other than SC—which is unambiguously particle-hole symmetric. Full spectral probes such as STM, in combination with quantitative calculations, are necessary to understand the competition between SC and particle-hole asymmetric phases. Third, our observation of the local effect of even moderate strain in driving a quantum phase transition calls for a reinvestigation of possible phase inhomogeneity in other strongly correlated systems, in which larger strain may occur (30, 31).

In the cuprate superconductors, an analogous phase boundary between unidirectional (1Q) charge “stripes” and bidirectional (2Q) “checkerboard” has been predicted (32, 33). The introduction of quenched disorder results in discommensurations in the 2Q phase and disordered orientational order in the 1Q phase, making them hard to distinguish—especially in the cuprate superconductors, thought to be in proximity to the 1Q–2Q phase boundary (32, 33). Recent STM studies of the $\sim 4a_0$ charge order in the cuprate Bi₂Sr₂Ca_{n-1}Cu_nO_{2n+4+x} (BSCCO) have had conflicting interpretations, with interpretations suggesting of fluctuating 2Q and 1Q order (34, 35). However, the influence of strain, from the supermodulation lattice buckling or from randomly distributed dopants, is seldom accounted for. Previous studies have shown that both these strain phenomena correlate with nanoscale electronic inhomogeneity (30, 36). A possible explanation is local stabilization of the 1Q state, producing 1Q–2Q and 1Q–1Q interfaces with spectral differences, analogous to Figs. 2 and 5A and B. Although the presence of strong disorder [up to 12% strain variations on a nanometer length scale (30)] complicates the interpretations in BSCCO, we stress the importance of isolating and modeling strain effects for better

understanding and control of the phase transitions in cuprates. Finally, the microscopic visualization of the role of strain in stabilizing new order suggests a controlled route toward engineering novel quantum phases and interfaces and studying symmetry breaking in strongly correlated materials. In this regard, we suggest a connection to the emerging importance of strain as a route to high- T_c superconductivity in novel iron-based materials (37, 38).

Materials and Methods

STM Experiments. Measurements were performed using a home-built STM at temperatures between 2 K and 10 K. Magnetic fields of up to 6 T were used to suppress the superconducting state as needed. Single crystals of 2H-NbSe₂ were cleaved in situ in cryogenic ultrahigh vacuum and inserted into the STM. A mechanically cut Pt-Ir tip, cleaned by field emission and characterized on gold, was used for the measurements. Spectroscopy data were acquired using a lock-in technique at 1.115 kHz. The topographic and spectroscopic signatures of the 1Q ribbons have been verified with several tips.

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Band Structure and DOS Calculations. The band structure of 2H-NbSe₂ close to E_F consists of two Nb-4d-derived bands and one Se-4p “pancake”-shaped hole pocket (6). The Nb-4d bands are modeled using a tight-binding fit to the observed ARPES band structure (16), and the Se-4p pocket is approximated by a simple quadratic form to fit first principles calculations (6) (details in *SI Text III*). Using all three bands, the DOS in the presence of a CDW is calculated by imposing a constant coupling between electronic states connected by any one of the three q -vectors. The strength of the coupling Δ is taken as a free parameter in the reproduction of the experimentally observed DOS, and the size of \tilde{q} is allowed to vary slightly around the observed value of 0.328 Q_0 (details in *SI Text IV*).

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Supporting Information

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SI Text

Sample Characterization. NbSe₂ is a layered transition metal dichalcogenide whose 2H polytype has a hexagonal structure and D_{6h}^4 space group symmetry. The unit cell (Fig. S1A) consists of two sandwiches of Se–Nb–Se. The crystal typically cleaves between the neighboring Se layers, coupled by weak van der Waals forces.

Single crystals of 2H-NbSe₂ were grown by chemical vapor transport using iodine as the transport agent. A transport characterization of the sample batch used in this work is shown in Fig. S1B. The superconducting transition is observed at $T_{SC} \sim 7$ K. The residual resistivity ratio, defined as the ratio of resistances $R(295\text{K})/R(7.5\text{K})$, is ~ 16 .

1Q Ribbons: Height and Orientation. The 1Q charge-density wave (CDW) typically appears in regions that persist in one direction with apparent 20–40 pm topographic elevation, forming a 10–20-nm wide ribbon structure (Fig. S2 A–C). We note that the topographic elevation $z_{STM}(\vec{r}, V_0, I_0)$ as measured by maintaining a constant current I_0 with bias setpoint V_0 at lateral tip position $\vec{r} \equiv (x, y)$ may be given by:

$$z_{STM}(\vec{r}, V_0, I_0) \simeq z_T(\vec{r}) + \frac{1}{\kappa(\vec{r})} \ln \left(\frac{I_0}{\int_0^{V_0} dV eD(\vec{r}, eV)} \right). \quad [\text{S1}]$$

Here $z_T(\vec{r})$ is the true topographic corrugation of the sample, $\kappa(\vec{r})$ is a measure of the local tunnel barrier height, and $D(\vec{r}, eV)$ is the local density of states (LDOS) of the sample at energy eV . Because of the logarithmic sensitivity of $z_{STM}(\vec{r}, V_0, I_0)$ to the integral of the LDOS from the Fermi energy, ε_F (corresponding to $V = 0$) up to the bias setpoint eV_0 , scanning tunneling microscopy (STM) topographs may contain electronic artifacts masquerading as geometric effects. Therefore, we present two pieces of evidence for the true geometric elevation of these ribbons.

First, a tabulation of the relative orientation θ_{R,Q_0} of the ribbon to the nearest Bragg vector of the underlying hexagonal lattice for the various ribbons imaged in the study shows a seemingly random spread from -30° to 30° —the full range of available angles (Fig. S2 D and E). Furthermore, these ribbon structures may intersect to form X- as well as Y-junctions (Fig. S2 A and B), and the angle between intersecting ribbons varies from 40° to 60° . The fact that ribbon orientation does not respect lattice symmetry strongly suggests a true geometric rather than electronic origin of their apparent height. We contrast this observation with enhanced STM topographic corrugation associated with predominantly electronic features in a wide range of other materials, which respect the symmetry of the hexagonal (1, 2) or square (3) lattice.

Second, the measured height of these ribbons in STM topographs exhibits $<5\%$ dependence on bias setpoint within 400 mV below the Fermi energy (Fig. S3 A–C). We note that this energy range over which the measured height of the ribbons is invariant is much larger than the spectral range of CDW variation (~ 50 mV). We further note the contrast between the bias-independent ribbons and single-atom impurity resonances, whose measured “height” varies by 50–70% between Fig. S3A and S3B. Therefore, we conclude that the measured height (20–40 pm) and width (10–20 nm) of these ribbons has a predominantly geometric origin.

Having established the topographic origin of these ribbons (Figs. S2 and S3), we suggest that these ribbons likely are a topographic rippling of the top few layers. These ribbons may arise

during the cleaving process as the result of underlying growth defects that may intercalate between Se–Nb–Se sandwich layers. We note that similar topographic ribbon deformations were observed recently in another layered chalcogenide (Bi₂Te₃) (4).

We estimate the in-plane and out-of-plane lattice strain associated with the topographic ribbon features. Using the maximum topographic elevation of an observed ribbon (40 pm), we can put an upper limit on the out-of-plane distortion by assuming that a minimum of two sandwich layers are elevated (any fewer and the defects causing the elevation likely would be visible in our topographs). The out-of-plane distortion therefore is $\leq 3\%$ (40 pm/12.54 Å) of the unit cell spacing. To measure the in-plane distortion, we first use the Lawler-Fujita algorithm (5), which can determine the lateral location of atoms with precision $\sim 2\%$ of the lattice spacing (6, 7). With this algorithm, we do not observe any change in the lattice constant across the ribbon, which places a direct experimental upper limit on the in-plane distortion of $\sim 2\%$.

However, we can estimate the actual in-plane distortion indirectly from the measured out-of-plane distortion by modeling the ribbon as a half-period of a sinusoid with height h (40 pm) and width W (10 nm) (Fig. S3D). The total lateral deformation due to such a ribbon is $\delta W \sim 45$ pm, corresponding to $\sim 0.06\%$ of the lattice spacing. As this is well below the resolution of the Lawler-Fujita algorithm, it is not surprising that the in-plane distortion is not detectable in STM topographs. From the upper bounds of 3% on the vertical strain and 0.06% on the lateral strain, we note that the magnitude of the strain field leading to the formation of these ribbons is moderate compared with some other correlated materials (8, 9). We also note that although the magnitude of lattice distortion of these ribbons may seem small in the context of the observed quantum phase inhomogeneity, a comparison with other known materials suggests that strain of this magnitude may be sufficient to drive a transition to the unidirectional CDW phase (10).

Previously, we discussed the ribbon orientation with respect to the lattice (θ_{R,Q_0}); we now consider the ribbon orientation with respect to the 1Q CDW wavevector ($\theta_{R,q_{1Q}}$), also detailed in Fig. S2 D and E. In a simple picture of the strained ribbon structure, we would expect the ribbon-induced strain to couple strongly to the 1Q CDW orientation either parallel or perpendicular to the ribbon; thus, we would expect to observe values of $\theta_{R,q_{1Q}}$ either between 0° and 30° or between 60° and 90° . However, we often find $\theta_{R,q_{1Q}}$ to be in the 30 – 60° range as well. Insufficient statistics prevent us from inferring a clear connection between ribbon orientation and \vec{q}_{1Q} orientation, but the wide distribution of relative angles suggests the complexity of the interaction.

Band Structure Calculations. The band structure of 2H-NbSe₂ close to ε_F consists of two Nb-4d-derived bands and one Se-4p “pancake”-shaped hole pocket (11, 12). Close to ε_F , the Se-4p pancake-shaped hole pocket that surrounds the Γ -point can be modeled by a simple quadratic form:

$$E = A \cdot \frac{a_0^2}{4\pi^2} (k_x^2 + k_y^2) + B. \quad [\text{S2}]$$

With the values of $A = -5.4$ eV and $B = -0.65$ eV, this model accurately reproduces the dispersion obtained in first principles local density approximation (LDA) calculations by Johannes et al. (11), as shown in Fig. S4A. To model the Nb-4d bands, we use a tight-binding fit to the band structure observed in angle-resolved photoemission (ARPES) experiments, as reported by Rahn et al.

(13). We find that a small ($\sim +16$ meV) offset in the chemical potential relative to the parameters used by Rahn et al. was needed to reproduce the observed DOS from STM measurements. This offset is within the accuracy of the tight-binding fitting scheme (13). The band energies of the tight-binding description are given by (13)

$$E = t_0 + t_1 [2 \cos \xi \cos \eta + \cos 2\xi] + t_2 [2 \cos 3\xi \cos \eta + \cos 2\eta] + t_3 [2 \cos 2\xi \cos 2\eta + \cos 4\xi] + t_4 [\cos \xi \cos 3\eta + \cos 5\xi \cos \eta + \cos 4\xi \cos 2\eta] + t_5 [2 \cos 3\xi \cos 3\eta + \cos 6\xi], \quad [S3]$$

where $\xi = \frac{1}{2}k_x a$ and $\eta = \frac{1}{2}\sqrt{3}k_y a$ and k_y is along $\Gamma - M$. The values of the tight-binding parameters (including the offset) used in this work are presented in Table S1.

Density of States Calculations. To calculate the DOS in the presence of a $3Q$ CDW, we impose a coupling between states connected by any one of the three \tilde{q} -vectors, given by

$$\mathcal{H}_{\text{CDW}} = \tilde{\Delta} \sum_{\tilde{k}} \left(c_{\tilde{k}+\tilde{q}}^\dagger c_{\tilde{k}} + \text{h.c.} \right). \quad [S4]$$

The strength $\tilde{\Delta}$ of the coupling is taken as a free parameter in the reproduction of the experimentally observed DOS, with a broadening parameter fixed at $\Gamma = 5$ meV. Adjusting the size of \tilde{q} slightly around the observed value of $q_{3Q} = 0.328 Q_0$, we find the best match with STM spectra using $\tilde{q} = 0.333 Q_0$ (corresponding to the locally commensurate CDW periodicity), $\tilde{\Delta} = 12$ meV. With these parameter values, the gap structure in the calculated DOS closely approaches the overall shape, width, and center of the gap structure seen in the measured data within ± 30 meV of the Fermi energy ϵ_F , as shown in Fig. 5C.

To demonstrate the accuracy of this fit, we show the effects of varying the wavevector \tilde{q} by $1 - 2\%$ (Fig. S5 A and B), and the gap value $\tilde{\Delta}$ by $10 - 20\%$ (Fig. S5 C and D). Using these fit parameter variations, we estimate the errors for \tilde{q} and $\tilde{\Delta}$ to be $0.004 Q_0$ and 2 meV, respectively. The value of $\tilde{\Delta}$, however, may be an overestimate, leading to a systematic error of the same order as the fit uncertainty, because the described procedure does not take into account the particle-hole symmetric

inelastic background in the experimental DOS. Accurate modeling of the inelastic background would require detailed temperature-dependent spectroscopic data, which is beyond the scope of this work.

Crucially, we note that the particle-hole asymmetry in the CDW gap, with its minimum centered above ϵ_F , cannot be removed by the subtraction of a particle-hole symmetric background. Likewise, the striking deviation of our fitted gap parameter ($\tilde{\Delta} = 12$ meV) from previous results [four times larger than the 3 meV value detailed by Borisenko et al. (14) and three times smaller than the 35 meV value detailed by Hess et al. (15)] far exceeds fit or systematic uncertainties.

To experimentally verify the lack of bearing of the 35 mV kinks on the CDW phase, we performed spectroscopy up to 45 K, and universally observed the presence of these kinks in the STM spectra well above T_{CDW} (~ 33 K). A comparison of the typical spectrum acquired at 40 K with that acquired at 2 K is shown in Fig. S6. We note that the data acquired at 40 K are thermally smeared by $\mathcal{O}(3k_B T)$, i.e., ~ 10 mV, resulting in a broadening of the kinks. Despite this, the kinks remain distinguishable and are present throughout all spatial regions studied in this work.

For completeness, we show in Fig. S7A the calculated DOS in the presence of a $1Q$ CDW at the experimentally observed wavevector, $q_{1Q} = 0.286 Q_0$, using $\tilde{\Delta} = 12$ meV. The lack of correspondence between this calculation (green curve in Fig. S7A) and the measured dI/dV spectrum (green curve in Fig. 5B) may be attributed to the increased intensity of the inelastic background in the buckled region of the $1Q$ ribbons. This background is evident in the V -shape of the dI/dV spectrum in Fig. 5B, centered close to ϵ_F , as explained theoretically (16) and observed experimentally across a wide variety of materials (16–23).

We also compare our results with a calculation of the DOS based on a tight-binding fit to the full 3D LDA band structure reported by Johannes et al. (11). The DOS obtained using this 3D LDA fit is compared with the results based on the 2D fit in Fig. S7B. We find that the STM data are best reproduced using the band structure observed by ARPES, and that there is a noticeable difference between the depths of the gaps in the 2D ARPES-based and those of the 3D LDA-based band structure fits (despite independent parameter optimization), which is indicative of some difference between the surface and bulk dispersions (11).

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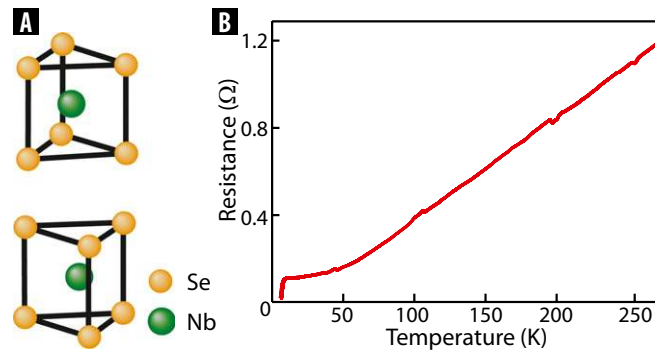


Fig. S1. Sample characterization. (A) The layered hexagonal crystal structure of 2H-NbSe₂, with alternating sandwiches of Se-Nb-Se. (B) Temperature dependence of the resistance for the sample batch used for this study, showing a superconducting transition at ~7 K.

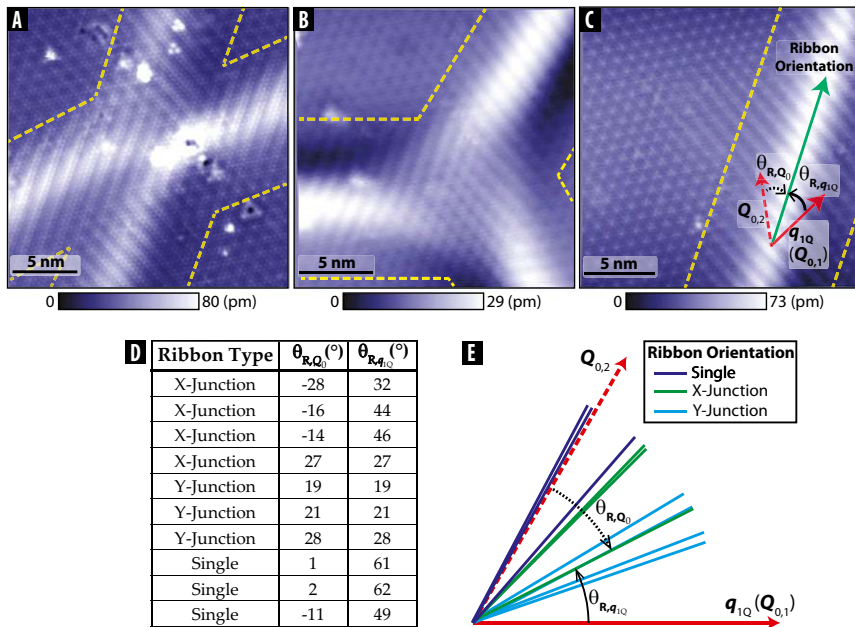


Fig. S2. 1Q ribbons: orientation. (A and B) STM topographs showing ribbons of unidirectional (1Q) CDW, intersecting to form an X-junction (A) and a Y-junction (B), with CDW wavevector \vec{q}_{1Q} varying between the arms. Dashed yellow lines indicate the approximate extent of the ribbons. Setpoint parameters: $V_{\text{sample}} = -50$ mV for both; $R_j = 5$ GΩ(A), 1 GΩ(B). (C) STM topograph of a 1Q-3Q interface (top arm of X-junction, also shown in Fig. 2B), demonstrating the definitions of the relative orientations θ_{R,Q_0} between the ribbon (green arrow) and the nearest Bragg vector (dashed red arrow), and $\theta_{R,q_{1Q}}$ between the ribbon and 1Q wavevector \vec{q}_{1Q} (solid red arrow). (D) Table detailing the values of θ_{R,Q_0} and $\theta_{R,q_{1Q}}$ observed in the various 1Q ribbons studied in this work, with the first entry corresponding to C. (E) Illustration of the spread of values in D. The dark blue (single), green (X-junction), and cyan (Y-junction) lines describe the orientation of the various ribbons with respect to the 1Q wavevector \vec{q}_{1Q} along the $Q_{0,1}$ Bragg vector (solid red arrow) and another Bragg vector $Q_{0,2}$ (dashed red arrow).

Table S1. Tight-binding parameters for the two Nb bands (in meV)

Parameter	Nb band 1	Nb band 2
t_0	26.9	219.0
t_1	86.8	46.0
t_2	139.9	257.5
t_3	29.6	4.4
t_4	3.5	-15.0
t_5	3.3	6.0