
This is an electronic reprint of the original article.
This reprint may differ from the original in pagination and typographic detail.

Turunen, Mikko; Brotons-Gisbert, Mauro; Dai, Yunyun; Wang, Yadong; Scerri, Eleanor; Bonato, Cristian; Jöns, Klaus D.; Sun, Zhipei; Gerardot, Brian D.

Quantum photonics with layered 2D materials

Published in:
Nature Reviews Physics

DOI:
[10.1038/s42254-021-00408-0](https://doi.org/10.1038/s42254-021-00408-0)

Published: 01/04/2022

Document Version
Peer reviewed version

Please cite the original version:
Turunen, M., Brotons-Gisbert, M., Dai, Y., Wang, Y., Scerri, E., Bonato, C., Jöns, K. D., Sun, Z., & Gerardot, B. D. (2022). Quantum photonics with layered 2D materials. *Nature Reviews Physics*, 4(4), 219-236.
<https://doi.org/10.1038/s42254-021-00408-0>

This material is protected by copyright and other intellectual property rights, and duplication or sale of all or part of any of the repository collections is not permitted, except that material may be duplicated by you for your research use or educational purposes in electronic or print form. You must obtain permission for any other use. Electronic or print copies may not be offered, whether for sale or otherwise to anyone who is not an authorised user.

Quantum Photonics with layered 2D Materials

Mikko Turunen^{1†}, Mauro Brotons-Gisbert^{2†}, Yunyun Dai¹, Yadong Wang¹, Eleanor Scerri², Cristian Bonato², Klaus D. Jöns³, Zhipei Sun^{1,4}, Brian D. Gerardot^{2*}

¹Department of Electronics and Nanoengineering, Aalto University, FI-00076 Aalto, Finland

²Institute of Photonics and Quantum Sciences, SUPA, Heriot-Watt University, EH14 4AS, United Kingdom

³Institute for Photonic Quantum Systems (PhoQS), Center for Optoelectronics and Photonics Paderborn (CeOPP) and Department of Physics, Paderborn University, 33098 Paderborn, Germany

⁴QTF Centre of Excellence, Department of Applied Physics, Aalto University, Espoo, Finland

[†]These authors contributed equally to this paper.

*email: b.d.gerardot@hw.ac.uk

Abstract: Solid-state quantum devices use quantum entanglement for various quantum technologies, such as quantum computation, encryption, communication, and sensing. Solid-state platforms for quantum photonics include single molecules, individual defects in crystals, and semiconductor quantum dots, which have enabled coherent quantum control and read-out of single spins (stationary quantum bits) and generation of indistinguishable single photons (flying quantum bits) and their entanglement. In the past six years, new opportunities have arisen with the emergence of 2D layered van der Waals materials. These materials offer a highly attractive quantum photonic platform that provides maximum versatility, ultra-high light-matter interaction efficiency, and novel opportunities to engineer quantum states. In this Review, we discuss the recent progress in the field of two-dimensional layered materials towards coherent quantum photonic devices. We focus on the current state-of-the-art and summarize the fundamental properties and current challenges. Finally, we provide an outlook for future prospects in this rapidly advancing field.

H1 Introduction

High-performance quantum light sources are required to realize future quantum photonic technologies. For example, stable high-repetition-rate true single-photon sources can enable various quantum communication schemes with unconditional long-term information security^{1,2}. Scalable on-chip quantum light sources can facilitate robust photonic quantum computation with the ultimate data processing speed, which is coded into fragile quantum states of individual unperturbed photons³. Furthermore, quantum light sources are of great interest for precision optical measurements which can approach the Heisenberg limit⁴. An ideal quantum light source is deterministic, providing on-demand exactly one photon with indistinguishable properties in all degrees of freedom (polarization, spatio-temporal mode, and energy).

Building on concepts from atomic and molecular optical physics, several approaches to generate single-photons and spin-photon interfaces in solid-state materials have been discovered and developed. Solid-state quantum emitters can offer significant advantages over their atomic counterparts, including: the ability to repeatedly address a single emitter, tunable energy scales, large oscillator strengths, the capability for added semiconductor or integrated photonic functionality, and (potentially) scalability. Unfortunately, the solid-state environment also contains intrinsic sources of noise and dephasing mechanisms that must be addressed. The foremost solid-state quantum photonics platforms are colour centres in diamond and semiconductor quantum dots⁵⁻⁸.

Over the past six years, single photon emitters in 2D layered materials were shown to exhibit non-classical quantum light emission⁹⁻¹⁴. Such emitters can be deterministically positioned by local strain fields¹⁵⁻¹⁹, a feature unique to 2D materials. These materials consist of one or few atomically thin layers, inherently providing quantum confinement in one dimension, and possess unique optical and electronic properties²⁰ and a straightforward means for integration with various optical cavities²¹⁻²⁵ and waveguides²⁶⁻³⁰ for integrated photonics. In addition, one can easily stack these materials on top of each other to form devices such as

47 electrically pumped single photon light-emitting diodes (LEDs)³¹, charge-tunable devices for single spin
48 control^{32,33}, or novel artificial heterostructures³⁴⁻³⁶ with completely different chemical and physical properties
49 (electrical, optical, magnetic properties), thus possibly allowing more versatile quantum devices for various
50 applications beyond simulation, communication and computation, such as sensing, imaging, and metrology³⁷⁻³⁹.

51 In this Review, we provide an overview of the basic properties of different 2D layered materials and discuss
52 the recent advances in the field of quantum light sources based on these materials. We conclude by offering a
53 perspective on future directions and challenges in most materials advances and potential applications.
54

55 H1 Single photon sources and spin-photon interfaces

56 A single-photon emitter (SPE) is a few-level quantum system with an optical transition that emits only one
57 photon at a time (see Supplementary Information for an introduction). In the simplest case, it is a two-level
58 system with an optical transition that can be driven coherently or incoherently from the ground to its excited
59 state. Spontaneous emission from the excited state can produce a single photon with a characteristic rate γ_{sp} . In a
60 non-resonant photoluminescence (PL) spectrum, the SPE's spontaneous emission appears as a discrete peak,
61 referred to as the zero-phonon line (ZPL), with a spectral width determined purely by γ_{sp} in the ideal transform-
62 limited case (the case $T_2 = 2T_1$, where T_2 and T_1 are the emitter's coherence time and lifetime, respectively).
63 While incoherent single photons can outperform coherent input states of light for some quantum applications
64 such as quantum random generation⁴⁰, it will be difficult for incoherent SPEs to outperform the low-cost and
65 high-data-rates at telecom wavelengths obtained with faint laser pulses and decoy states for other quantum
66 applications such as a practical implementation of intra-city quantum key distribution⁴¹. However, employing
67 SPEs for quantum technologies which require indistinguishable single photons provides a compelling motivation
68 for their technological development. Photon indistinguishability, defined as the mean wavepacket overlap of two
69 photons, is characterized by the visibility of two-photon interference⁴².

70 One of the more established approaches to a secure quantum network⁴³ relies on interfacing
71 indistinguishable photons, ideal for sharing quantum states over long distances, with spins, attractive for local
72 storage and quantum processing due to their insensitivity to environmental noise⁴⁴⁻⁴⁶. Spin-active optical
73 emitters, such as quantum dots and paramagnetic defects, can provide the required spin-photon interfacing
74 capabilities. A prerequisite for spin-active optical emitters is long electron spin coherence time, which can be
75 achieved by SPEs featuring weak coupling of their states and transitions to phonons and electrical noise in
76 material systems with a low concentration of non-zero nuclear spins (Box 1). Operations such as optical spin
77 initialization and readout, and the creation of spin-photon entanglement, rely on the availability of spin-selective
78 optical transitions. These transitions originate from selection rules set by the symmetry of the system. Efficient
79 spin-photon operations require stable transitions, exhibiting no **spectral diffusion [G]** or **blinking [G]**. In
80 addition, mixing between orbital eigenstates with different spin characters should be minimal to avoid spin-flips
81 induced by optical excitation. If optical excitation generates a detectable amount of PL without causing a spin-
82 flip, single-shot spin readout can be achieved, as shown for nitrogen-vacancy^{47,48} and SiV centers⁴⁹ in diamond,
83 and for III-V quantum dots⁵⁰.

84 Generation of spin-photon entanglement requires the spin-photon coupling to be coherent⁵¹⁻⁵³. Coherence
85 can be achieved in systems with minimal inhomogeneous broadening (approaching the **transform limit [G]**) and
86 with minimal incoherent phonon sidebands, such that a large fraction of emission is in the ZPL. Spin-photon
87 entanglement is a building block for more sophisticated schemes, such as remote entanglement between spins in
88 remote nodes of the quantum network^{47,54,55}. These schemes benefit from additional long-lived qubits provided
89 by nuclear spins. Compared to electronic spins, nuclear spins have a reduced coupling to magnetic fields and
90 longer spin coherence time due to a much smaller gyromagnetic ratio. The concentration of accessible nuclear
91 spins in a given material depends on its specific isotopic composition, from the very "dense" spin bath associated
92 with GaAs and hBN (with all elemental isotopes featuring non-zero nuclear spins) to "dilute" baths for Si
93 (95.3% of isotopes have nuclear spin $I=0$), C (98.8% with $I=0$), W (85.7% with $I=0$), Mo (74.5% with $I=0$), S
94 (99.3% with $I=0$), and Se (92% with $I=0$). Control of individual nuclear spins has only been achieved for dilute

95 baths, where the nuclear spins are sufficiently far apart that their hyperfine interaction with the central electronic
96 spin is resolvable either directly in the electron spin resonance spectrum⁵⁶⁻⁵⁸ or by tailored pulse sequences^{59,60}.
97

98 **[H1] Quantum photonic sources with 2D materials**

99 The simple nature of the lattice construction of 2D materials offers unprecedented opportunities for quantum
100 photonics (see Supplementary Information for an introduction). The lack of dangling bonds (in principle) in the
101 lattice is promising for hosting transform-limited single photon sources, while the atomically thin nature offers
102 potential as a very local electronic probe of the environment or high-efficiency coupling of the radiative
103 emission to optical modes by engineering the dielectric environment. In addition, hybrid approaches to
104 integrated chip technologies benefit from the flexible fabrication processes for integration with optical
105 components (such as cavities, waveguides and others) and light coupling (Box 2). Further, efforts to use
106 nonlinear frequency conversion with 2D materials for quantum light generation and manipulation have been
107 made.

108
109 Zero-dimensional quantum confinement in bulk semiconductors is typically achieved by one of the following.
110 One option is a point defect in the crystal lattice, such as electrons bound to donor impurities in bulk GaAs⁶¹,
111 diamond⁶², or SiC⁶³. Another option is a change in material composition at the nanometer-scale, which has a
112 reduced electronic band-gap material compared to the surrounding matrix, often accompanied by local strain.
113 This change in composition can be intentional, for example, in self-assembled quantum dots⁶⁴ or can be
114 unintentionally caused by interface disorder, such as at the interface between two epitaxial layers⁶⁵. Similarly, in
115 2D materials, SPEs can potentially originate from excitons localized due to point defects in the crystal or an
116 electronic perturbation in the crystal environment, for instance, dangling bonds in the substrate material,
117 impurities at a nearby interface, or an electrostatic gate. The former is typically the case with SPEs in wide-band-
118 gap hBN which are mostly based on deep level defects, whereas the precise confinement mechanism in
119 monolayer TMDs is still under debate (a notable exception are SPEs created by He-ion induced defects in
120 MoS₂^{66,67}).

121
122 Excellent single photon purity is possible for SPEs in 2D materials, which also have the unique capability to be
123 site-controlled and arranged into arrays via localized strain or implantation. For example, moiré-heterostructures,
124 in which periodic electronic interaction between two atomic layers results in the case of a small lattice mismatch
125 or relative twist, present a novel method to create confinement in a semiconductor^{34,68}. Moreover, the 2D nature
126 of the layer hosting the SPEs removes the total internal reflection condition typical from bulk-based SPEs,
127 enabling enhanced extraction efficiency of the emitted photons. In general, SPEs based on TMDs have an
128 attractive spin-degree of freedom to realize a spin-photon interface, while only a few defect species in hBN
129 do^{69,70}. However, spectral fluctuations, inhomogeneity among emitters, and large phonon sidebands all present
130 significant challenges to realize arrays of indistinguishable single photon sources or coherent spin-photon
131 interfaces. To date, the intrinsic spin coherence and coherence of single photons generated with 2D quantum
132 emitters have yet to be systematically probed. SPEs are usually non-resonantly excited, but steps towards
133 resonance fluorescence and coherent control as well as charge state control and electrical injection using
134 heterostructure devices have been taken.

136 **[H2] Monolayer TMDs**

137
138 SPEs in TMDs were discovered in mono- and bi-layer WSe₂ in 2015^{9-13,15} and monolayer WS₂ soon after³¹.
139 These first reports identified the main features of quantum emitters with W-based TMDs, which exhibited
140 inhomogeneous spectral features at lower energy than the main free-excitons with linewidths down to 0.1 meV
141 (full width at half maximum) (Fig. 1a). The neutral localized excitons consist of a fine-structure split doublet,
142 typically (but not exclusively) with orthogonal linear polarization and a splitting of 0.4 - 0.8 meV. While detailed

143 theories about the origin of the splitting have been proposed⁷¹, in general, the **fine-structure splitting [G]** (FSS)
144 arises due to electron–hole exchange interaction⁷² and the relatively large magnitude of the FSS is due to the
145 strong Coulomb interactions in TMDs. Large gyromagnetic ratios (g-factors) of the excitons were observed for
146 out-of-plane magnetic fields (Faraday geometry), in the range of 8–10^{9-13,15}. Beyond single localized excitons, bi-
147 excitons in monolayer WSe₂ SPEs have been observed⁷³⁻⁷⁵, with unambiguous identification based on the distinct
148 polarization dependence and cross-correlation of the exciton and bi-exciton spectral peaks⁷³ (Fig 1b). At low
149 temperature (T < 10 K), high-purity single photon emission ($g^2(0) < 1\%$, ref.⁷⁶) has been demonstrated from
150 isolated emitters and time-resolved PL measurements reveal lifetimes of a few ns to few tens of ns^{9-13,15}. While
151 the fraction of zero-phonon line to total emission is variable in WSe₂ SPEs (likely related to strain conditions), it
152 is typically within the range of 50-80%^{76,77}.

153 The spatial correlation of the SPEs with local strain pockets was observed early on^{13,15}, raising the prospect
154 to spatially define the emitter position and deterministically create arrays of SPEs¹⁶⁻¹⁸. For instance, a WSe₂ flake
155 can be transferred on top of lithographically defined nanopillars to create point-like strain perturbations that
156 locally modify the electronic band-gap (Fig 1c). Density functional theory results show that a strained WSe₂
157 flake with a 200 nm tall nanopillar leads to a 50 meV shift in the bandgap⁷⁸, which agrees well with the
158 experimental results. Excitons created optically in the vicinity of the localized stressor can diffuse to the
159 potential minimum, creating an efficient exciton funnel⁷⁹ for a SPE. By optimizing the nanopillar aspect ratio, a
160 high-yield (> 90%) of deterministic positioning of SPEs with an accuracy up to 30 nm has been achieved¹⁶⁻¹⁸.
161 Sharp emission lines in PL of MoSe₂ arising at local strain sites have also been observed⁸⁰⁻⁸², which recently
162 have been shown to emit single photons⁸².

163 The precise origin of quantum confinement for TMD based SPEs has been subject to debate. Notably, the
164 local strain features (such as that created by nanopillars or nanobubbles) are typically at the scale of 100 nm¹⁶⁻
165 ^{18,83,84}, which is significantly larger than the nm scale exciton Bohr radius in TMDs²⁰. Although local wrinkles
166 around the stressor sites may localize excitons at the 10 nm scale^{74,85}, the origin for the SPE is unlikely to be
167 solely due to local strain⁸⁶, but rather the interplay or combination of local strain with disorder in the
168 environment and / or crystal defects (Box 1, Fig. 1d). There are two important observations to be made here.
169 First, the typical g-factor of the localized excitons is similar to the ground state delocalized **dark (free) exciton**
170 **[G]** g-factor (~8) in monolayer WSe₂^{20,87}. Second, the SPEs spectrally overlap with a broad band of emission in
171 flat (nominally unstrained) monolayer WSe₂ that is energetically below the free exciton emission. This low-
172 energy, broad bandwidth emission is typically associated with excitons localized at point defects⁸⁸, which can be
173 dispersed by local strain pockets¹⁵.

174 To account for these observations in a microscopic model, one proposal is that the WSe₂ SPEs are intervalley
175 defect excitons arising from hybridization of the dark excitons, modulated in energy by local strain, and defect
176 states associated with intrinsic Se vacancies⁷¹ (Fig. 1e). This theory predicts many physical features (such as the
177 g-factors, FSS, radiative lifetimes, and polarization dependence) observed experimentally for WSe₂ SPEs. Other
178 models based on W-vacancies⁸⁹, O interstitial defects⁹⁰, and dislocations⁹¹ have also been proposed. Recently,
179 the combination of controlled strain and electron-beam-induced structural defects in WSe₂ has led to the creation
180 of SPEs with a relatively high yield, biexciton formation, and single-photon emission up to 150 K⁷⁵.

181 Recognizing that point defects in WSe₂ likely contribute to the exciton localization responsible for SPEs,
182 efforts to minimize the intrinsic point defect densities (using a flux-growth technique) or deterministic defect
183 creation (using electron-beam irradiation⁹²) can be pursued. Recently, He-ion beam lithography has successfully
184 been used to create emitters in other TMDs such as MoS₂ monolayers with a lateral precision of only ~9 nm⁶⁶.
185 Encapsulation of MoS₂ monolayers between two hBN layers after irradiation led to high quality quantum
186 emitters with long excited state lifetimes, showing clear antibunching⁹³, and the realisation of gate-tuning SPE
187 arrays⁹⁴. The encapsulation shields the 2D material from ambient gases and the SiO₂/Si substrate and reduces the
188 impact by doping and surface roughness⁹⁵, as well as minimizes effects of residues from nanofabrication⁹⁶.

189 TMD SPEs can be incorporated into heterostructure devices with a range of functionality. For example, a
190 single-photon LED can be realized by tunneling carriers from a graphene layer through a hBN barrier to a gated
191 monolayer TMD containing SPEs^{31,97} (Fig. 2a-c). Alternatively, a p-i-n diode can be realized with a device that
192 keeps the TMD at intrinsic doping but uses a second graphene gate of opposite polarity to the first⁹⁸. Owing to
193 the Coulomb blockade, deterministic loading of either a single electron or a single hole from graphene into WSe₂

194 SPEs has also been achieved to realize tuning between negatively charged (X^{-}), neutral (X^0), or positively
195 charged (X^{+}), excitons³² (Fig. 2d-f). The spin-singlet of the charged excitons leads to a clear spectral signature,
196 the lack of FSS. Here, the unique advantages of vdW heterostructures are apparent — thanks to a monolayer
197 hBN tunnel barrier, strong hybridization of the WSe₂ SPE and the Fermi sea (in graphene) is possible. Such
198 devices provide opportunities to explore the potential for spin-valley locking and coherence in TMD SPEs⁹⁹,
199 where the ability to optically initialize the resident spin in a specific valley is a valuable first step³³. In principle,
200 localized excitons are not expected to have permanent electric dipoles out of the plane of the TMD - similar to
201 free excitons in TMDs¹⁰⁰, leading to minimal **DC stark tuning**³² [G]. However, in some cases, appreciable SPE
202 energy tuning can be realized with applied electric fields¹⁰¹. Additionally, an applied field can change the exciton
203 wavefunction symmetry and affect the FSS¹⁰².

204 Localized excitons in WSe₂ typically have a lifetime of several nanoseconds⁹⁻¹³. When WSe₂ is coupled to
205 **plasmonic cavities** [G], enhanced single-photon radiation is realized. Using plasmonic nanocavities the localized
206 exciton lifetime has been successfully reduced to ~100 ps, increasing the brightness of SPEs without affecting
207 the purity of SPEs^{22,23}. This has also been achieved by depositing a WSe₂ monolayer flake on a metallic surface,
208 which causes monolayer WSe₂ to become strained due to nanoscopic metal particles on the substrate, which can
209 also increase the emission rate through plasmonic interactions²¹. In this case, the effect of a plasmonic
210 nanocavity on TMDs based SPEs can be two-fold: SPEs positioning and enhancement of their emission rate.
211 Using gold nanocubes simultaneously as plasmonic cavities and as strain-inducing localization sites, a **Purcell**
212 **enhancement** [G] was recently measured²². Another approach facilitating Purcell enhancement to increase the
213 quantum efficiency and reduce the effects of dephasing on the quality of the emitted single photons are tunable
214 open cavities (Box 2). Tunable open cavities were first used to study polariton effects in 2D materials^{103,104} and
215 were later used to realise SPEs with a quantum efficiency of up to $46\% \pm 3\%$ ²⁵. Tunable open cavities enable
216 straight forward resonant coupling to the cavity mode^{25,103,105}. Otherwise, spectral overlapping of the SPE and the
217 cavity mode requires a post-growth tuning knob, such as electric field tuning¹⁰¹ or strain tuning^{106,107}. Using the
218 latter technique a reversible tuning of 18 meV for localized excitons in WSe₂ has been realized, tailoring the
219 emission properties in the same order of magnitude as the SPE ensemble energy distribution¹⁰⁸.

220 Another aspiration for the field of 2D material quantum emitters is their integration into photonic circuits
221 (Box 2)¹⁰⁹. Based on the strain-induced SPE creation using nanopillars, several groups around the world
222 proposed to use waveguide structures as the strain-inducing nanostructure. The waveguide acts not only as the
223 strain-nucleation site but also directly couples the SPE into the photonic circuit, for example, by coupling
224 emitted single-photons from a WSe₂ flake to a plasmonic **slot waveguide**²⁷ [G]. The peak seen in the PL
225 spectrum indicates coupling of generated photons into the waveguide. Another approach was to transfer a WSe₂
226 flake on the facet of a titanium-diffused lithium niobate waveguide and directional coupler²⁶, while PL into a
227 waveguide mode from a WSe₂ monolayer placed on top of a SiN waveguide has also been reported²⁹. Recently,
228 antibunching from single-photons coupled to the waveguide has been measured¹¹⁰ and this geometry also
229 allowed to perform resonance fluorescence. However, in these studies, the coupling efficiency into the
230 waveguide mode was below 10%. To increase the coupling efficiency into the waveguide mode, more complex
231 structures (such as nano-beam cavities¹¹¹ or encapsulation of the WSe₂ flake into the waveguide) would be
232 desired. Finally, techniques such as He-ion beam lithography have the potential to simplify the 2D quantum
233 emitter integration into photonic circuits. First, a large 2D material heterostructure could be transferred and
234 integrated into the circuit. In the next step, the quantum emitters would be deterministically created at specific
235 positions on the circuit. This would allow thousands of emitters to be precisely coupled to on-chip cavities with
236 one single transfer step.

237

238 [H2] Moiré heterostructures

239

240 Vertically stacked monolayer TMDs represent a useful nanoscale system to engineer quantum states and
241 correlations. TMD heterobilayers present atomically sharp interfaces and type-II band alignment^{112,113}, giving
242 rise to the formation of **interlayer excitons** [G]. A prototypical example is a WSe₂/MoSe₂ heterobilayer, in which
243 the resulting interlayer excitons inherit the valley-contrasting physics of the individual monolayers¹¹⁴⁻¹¹⁷. The

244 spatial separation of the electron and hole results in an increased exciton radiative^{114,118} and valley depolarization
245 lifetime¹¹⁵⁻¹¹⁷. The separation of the exciton carriers also results in a large permanent out-of-plane electric dipole
246 moment that enables a large tunability of the exciton transition energy¹¹⁷ and exciton lifetime¹¹⁵ by externally
247 applied electric fields. Moreover, similar to monolayer WSe₂ and WS₂^{17,18}, local strain profiles induced by
248 patterned substrates enable exciton trapping in nanoscale confinement potentials, where the mean number of
249 interlayer excitons can be controlled via the optical excitation level^{119,120}.

250 Uniquely, heterobilayers with a lattice mismatch and/or a relative angle twist between the constituent
251 monolayers feature a spatially periodic moiré superlattice¹²¹, with a periodicity that can be precisely controlled
252 by the relative crystallographic alignment of the layers for stacking beyond the theoretically proposed critical
253 angle for lattice reconstruction¹²²⁻¹²⁴. The moiré superlattice can lead to the hybridization of the intralayer and
254 interlayer excitons¹²⁵, which manifests through a pronounced exciton energy shift as a function of the
255 heterobilayer stacking angle. In addition, the moiré superlattice creates a periodic potential landscape for
256 excitons in the heterobilayer^{34,68,126}, in which three trapping sites (A, B, and C) with specific atomic registries
257 emerge, such as R_h^h (A), R_h^X (B) and R_h^M (C), where R_h^μ denotes an R-type stacking with the μ site of the electron
258 layer (either h the hexagon centre, X the chalcogen site or M the metal site) vertically aligned with the hexagon
259 centre (h) of the hole layer (Fig. 3a). For moiré periods larger than the exciton Bohr radius, these moiré trapping
260 sites can act as smooth quantum-dot-like confining potentials^{34,68}.

261 Experimental evidence of interlayer excitons trapped in a moiré potential has been reported in MoSe₂/WSe₂
262 heterobilayers with twist angles of around 0°, 21.8° and 60° at cryogenic temperatures^{35,127,128}. These localized
263 interlayer excitons present linewidths below ~100 μ eV and power-dependent emission intensities that can be
264 described by a two-level saturation model^{35,127,128}, hallmarks of a few-level quantum confined system.

265 The moiré potential minima preserve the three-fold rotational (C_3) symmetry^{34,68,129}; excitons trapped in
266 these moiré-defined sites therefore inherit the valley physics properties of the monolayer semiconductors,
267 although with optical selection rules that depend on the spin configuration of the exciton carriers (spin-
268 singlet/spin-triplet) and the atomic registry of the trapping site (Fig. 3b)¹³⁰. Polarization-resolved PL
269 measurements show that the moiré-trapped interlayer excitons retain the strong valley polarisation of the
270 constituent monolayer semiconductors and exhibit strong helical polarization due to the C_3 symmetry, which
271 results in a notable absence of observable fine structure^{35,127,128} (Fig. 3c, top). In addition, magneto-optical
272 spectroscopy experiments reveal highly uniform g-factors across several samples, dependent on relative layer
273 twist. The g-factors only take absolute values of ~15.9 and ~7 in samples with relative angle twists of 60° and
274 0°, respectively,^{35,127} clear fingerprints of the spin and valley configurations for excitons composed of band-edge
275 electrons and holes at the $\pm K$ points (Fig 3c, bottom). Moreover, in a heterostructure of bilayer 2H-MoSe₂ and
276 monolayer WSe₂, the phenomenon of locked electron spin and layer pseudospin can lead to two quantum-
277 confined interlayer exciton (IX) species with distinct spin-layer-valley configurations: the holes, localised in the
278 WSe₂ layer, are strongly Coulomb bound to electrons localised in either the lower or upper MoSe₂ layer to form
279 IX^H or IX^R species, respectively¹²⁷. IX^R (IX^H) present carriers with parallel (antiparallel) spin-valley locked
280 contributions, which results in an effective layer-locking of the Landé g-factors of the trapped IX. In addition,
281 the helical polarization of the trapped excitons appears to be determined by the atomic registry^{35,127}.
282 Unambiguous evidence of the quantum nature of the moiré-trapped IXs has recently been provided via photon
283 antibunching (Fig. 3d)¹²⁸. Furthermore, by incorporating the moiré-trapped IXs into a device that enables an
284 applied out-of-plane electric field, the large permanent dipole could be exploited to achieve ~40-meV tuning of
285 the SPE emission energy via the DC Stark effect (Fig. 3e)¹²⁸. This capability contrasts significantly with SPEs in
286 monolayers which have very small permanent dipoles in the vertical direction. Last, recent works have shown
287 that controlled electron and hole doping of the MoSe₂/WSe₂ heterobilayers results in the formation of negatively-
288 and positively-charged IXs trapped in the moiré potential¹³¹⁻¹³³ enabling the charge control of the SPEs (Fig. 3f).

289 These results highlight unique possibilities to engineer highly ordered and uniform array of quantum dots
290 with spin-valley optical selection rules^{34,68}, where the array of quantum dots (0D) can be tuned into parallel
291 stripes of quantum wires (1D) by strain¹³⁴. Moiré-induced trapping potentials loaded with one or two interlayer
292 excitons¹¹⁹ can behave as sources of single photons or entangled photon pairs, which can be exploited for
293 applications. Furthermore, the phenomenon of spin-layer locking in TMD heterostructures provides few-level
294 quantum systems in van der Waals heterostructures with a clear spin-photon interface via clean selection rules.

295 For example, the moiré-trapped IX reported in Ref. ¹²⁷ create a “vee-type” three-level system. Alternatively, a
296 three-level system analogous to a “spin-lambda” type atom, in which two ground states couple to a common
297 excited state, can be engineered using the layer-pseudospin degree of freedom in a tri-layer heterostructure
298 consisting of bilayer WSe₂/monolayer MoSe₂. Finally, the large out-of-plane permanent dipole of these excitons
299 can be exploited to energetically tune the moiré quantum emitters into resonance with a cavity for Purcell
300 enhancement for the generation of indistinguishable photons.

301

302 [H2] Hexagonal boron nitride

303

304 Bright room-temperature single photon emission in the visible has been reported in bulk crystalline and
305 monolayer hBN^{14,135}. SPEs in hBN can be very bright, with count rates exceeding a million counts per second
306 and quantum efficiency as high as 87%¹³⁶. Spectral emission covers a quite large wavelength range (1.6 – 2.5 eV
307 ^{137,138}) with different classes of defects likely responsible for the emission¹³⁹ (Fig. 4a). Tuning of the optical
308 emission wavelength can be achieved by electric fields^{140,141} and strain¹⁴². While the identification of the emitters
309 is not yet conclusive, several proposals have been investigated by ab-initio methods, including the anti-site
310 nitrogen vacancy N_BV_N⁻¹⁴, the carbon substitutional impurity at nitrogen site (C_N)¹⁴³ and the carbon anti-site
311 (C_BV_N)¹⁴⁴ defects, and dangling bonds¹⁴⁵ (Fig. 4b). The latter proposal could possibly explain why these emitters
312 are observed in as-grown material (where the high formation energy of other defects would limit their
313 concentrations) and especially near crystal edges and boundaries, where the crystal lattice might be disrupted.

314 SPEs with hBN are typically activated with a plasma treatment or by annealing^{14,135,146}, but other methods,
315 such as irradiation with electron beam^{137,146}, ultrafast laser pulses^{146,147}, and focused ion beam¹⁴⁸ have also been
316 demonstrated. Recently, it has been shown that electron beam irradiation leads to the activation of SPEs in hBN
317 with an improved accuracy of the spatial location and control of their emission wavelength¹⁴⁹. As in the case of
318 TMDs, it is possible to activate emitters by trapping carriers in the deformation potential wells created by
319 inducing a local curvature by a nanopillar¹⁹. The variety of techniques available to create emitters is a useful
320 resource to couple emitters to photonic structures. Transferring an hBN flake on plasmonic nanocavity arrays has
321 been shown to enhance single-photon emission by a factor of ~ 2 ^{24,150}. It has also been shown that photonic
322 crystal cavities can be fabricated directly into an hBN flake¹⁵¹. Having a SPE inside such a cavity with a
323 spectrally matching mode could provide an emitter-cavity system completely embedded in a single hBN flake. In
324 addition, single photon emission from a hBN flake has been successfully coupled to a tapered optical fibre with
325 10 % coupling efficiency,¹⁵² which is comparable to the other SPE platforms¹⁵³⁻¹⁵⁵. Finally, another approach has
326 been the integration of SPEs in multi-layer hBN into a tunable plano-concave optical microcavity, which has
327 shown Purcell enhanced single-photon emission by a factor of ~ 4 at room temperature¹⁵⁶, compared to non-
328 cavity SPEs (Fig. 4c). While hBN emitters are active up to room temperature, quantum interference experiments
329 require a high degree of coherence, only available at cryogenic temperature. PL measurements on individual
330 emitters at cryogenic temperature reveal a large **Debye-Waller factor [G]** (0.82). Low-temperature PL excitation
331 experiments have revealed large inhomogeneous broadening, with emitters subject to blinking and spectral
332 diffusion¹⁵⁷. Switching between bright and dark states is observed under resonant or quasi-resonant excitation,
333 with luminescence restored by a re-pump laser at a different wavelength. This switching can likely be explained
334 as photo-switching between different charge states¹⁴⁵. In the weak excitation limit, linewidths of ~ 0.6 GHz have
335 been observed (lifetime limit ~ 160 MHz) with spectral diffusion in timescales of a few tens of millisecond¹⁵⁸.
336 Scans on timescales shorter than the spectral diffusion show transform-limited linewidths down to ~ 50 MHz¹⁵⁹,
337 which, remarkably, persist as transform-limited up to room temperature¹⁶⁰. Moreover, Rabi oscillations for a
338 single emitter¹⁵⁸ and the coherent control of spin defects in hBN^{70,161,162} have been recently shown, an important
339 step towards coherent optical control of SPEs in 2D materials.

340 As is the case for other deep-level emitters in diamond and silicon carbide, the availability of optically-
341 detectable electronic spins in hBN would open the way for quantum spintronic applications. The 2D geometry
342 would, for example, enable easy integration in atomic force microscopy-type scanning probes and in
343 heterostructures with increased functionalities. In this direction, a strong dependence of optical emission on the
344 applied magnetic field at room temperature has been reported^{69,70} (Fig. 4d). These properties are consistent with
345 the presence of spin-selective intersystem crossing between triplet and singlet states, as for the nitrogen-vacancy

346 in diamond and for some intrinsic defects in SiC. More recently, a spin-dependent change in PL (optically-
347 detected magnetic resonance) was reported for an ensemble of defects emitting at around 850 nm⁷⁰, different
348 from those previously shown as single photon sources, in hBN samples irradiated by neutrons. The optically-
349 detected magnetic resonance signal corresponds to a defect with D_{3h} symmetry, hosting an S=1 electronic spin
350 ground state, with zero-field splitting D~3.5 GHz, and an almost isotropic g-factor g=2. Through electron
351 paramagnetic resonance (EPR) measurements, the defect is identified as an intrinsic defect, the negatively-
352 charged boron vacancy V_B⁽⁻⁾¹⁶³. The zero-field splitting shows a quite strong temperature dependence (changing
353 of ~120 MHz between room temperature and 4 K, as opposed to ~7 MHz for the NV centre in diamond),
354 suggesting possible applications in quantum thermometry. One challenge with quantum spintronics in hBN is
355 that all stable isotopes for both nitrogen and boron only feature non-zero nuclear spins. While the 2D geometry
356 for a suspended monolayer considerably reduces the number of nuclear spins surrounding the central electronic
357 spins, numerical simulations suggest spin coherence times T₂ limited to the microsecond scale¹⁶⁴. Interestingly,
358 decoherence is dominated by the contribution of ¹¹B nuclear spins, given their high gyromagnetic ratio (13.66
359 MHz/T, compared to 4.57 MHz/T for ¹⁰B and 3.7 MHz/T for ¹⁴N). Additionally, ¹¹B dominates the boron nuclear
360 spin bath, with ~80% concentration of ¹¹B and ~20% concentration of ¹⁰B. Numerical simulations predict that T₂
361 would increase from ~40 μs to ~90 μs when replacing all ¹¹B with ¹⁰B (ref.¹⁶⁴).

362 Despite the absence of transform-limited emission linewidths at room temperature, the bright and robust
363 single-photon emission of hBN at room temperature makes hBN SPEs as promising candidates for quantum
364 random number generation applications. The intrinsic 2D nature of the material can be harnessed to achieve
365 coupling of the generated quantum random number stream to an on-chip photonic waveguide structure¹⁶⁵.

366

367 [H2] III-VI metal chalcogenides

368 In their bulk form, GaSe and InSe present bandgaps of ~ 2 eV and 1.25 eV, respectively but, by reducing the
369 crystal thickness down to the monolayer limit, these can be increased substantially¹⁶⁶⁻¹⁶⁸. GaSe and InSe, widely
370 used in the field of nonlinear optics and terahertz generation due to their high nonlinear coefficients, even at the
371 atomic thickness limit¹⁶⁹, are also promising for electro-optical applications^{170,171}. GaSe has been used to create
372 SPEs with strain gradients (induced by local deformations created by naturally formed clusters of selenium
373 atoms) which can host localized excitons and biexcitons¹⁷². **Auto-correlation measurements [G]** confirm the
374 quantum nature of localized excitons, and **cross-correlation measurements [G]** reveal the correlation of the
375 localized excitons and biexcitons. Further, GaSe SPEs have been successfully coupled to on-chip waveguides²⁸.
376 Narrow quantum dot-like optical emission has also been observed in InSe at low temperature over a wide range
377 of energy, which was attributed to the localization of excitons around impurities and/or crystal defects¹⁶⁶.
378 However, the quantum nature of these localized excitons remains to be confirmed.

379

380 [H2] Graphene

381 Since graphene is a semimetal with no bandgap, it is a prominent material for broad-band photodetectors and
382 modulators, but its light emission properties are fairly limited. Nevertheless, the fabrication of graphene quantum
383 dots with atomic level control has been shown possible. These graphene quantum dots have been shown to emit
384 single photons at room temperature with high purity ($g^{(2)}(0) = 0.05$) and brightness (count rate at saturation
385 ~9.7 M counts/s)¹⁷³. The graphene quantum dots consist of 96 carbon atoms with a lateral size of only 2 nm.
386 During fabrication, one can introduce different functional groups to the edges of the graphene quantum dot to
387 tune the emission wavelength^{173,174}. The reported PL spectra of a graphene quantum dot and a graphene
388 quantum dot functionalized with chlorine atoms show that the chlorine atoms also induce a redshift to the
389 spectrum. This demonstration indicates the possibility of modifying physical properties (such as brightness, spin
390 structure, and photostability) through the structure, for example, through designing quantum emitters with
391 chemical engineering.

392

393 [H1] Materials Advances

394 Since the initial discoveries of SPEs in 2D materials, the field of 2D materials-based quantum emitters has
395 grown a lot. This is illustrated in a timeline of different SPE material platforms (Fig. 5). However, the research
396 field is still young and fundamental breakthroughs are still expected due to the unique nature of 2D materials
397 (including new materials not yet investigated) and the ability to realize new types of heterostructures with
398 pristine interfaces. For example, the 2D material family is still largely unexplored. The hunt for the new and
399 optimal 2D materials, such as 2D materials with bandgaps close to the fibre telecommunication bands, like
400 MoTe₂ and black phosphorus for quantum applications has just begun. In fact, a recent work has reported
401 telecom band quantum emission in MoTe₂¹⁷⁵. Other exciting avenues include new types of layered materials, for
402 example, perovskite quantum dots¹⁷⁶⁻¹⁷⁸.

403
404 The increasing theoretical understanding of 2D SPEs provides additional predictive power to aid the search for
405 new SPEs in 2D materials¹⁷⁹. In addition, the flexibility of the 2D material platform provides novel opportunities
406 to engineer quantum confinement. The ‘twist’ degree of freedom for heterostructures is an exciting approach
407 unique to this platform. However, while the theoretical description of moiré trapped excitons presented in Ref.³⁴
408 accounts for all the experimental signatures reported to date, the experimental results are still subject to debate.
409 In this regard, clear identification of hybridization and moiré effects via resonant spectroscopy of intralayer
410 excitons^{125,180,181}, the corresponding interlayer PL^{35,36,127,128,134} and its interaction with strongly-correlated carriers
411^{182,183}, and new optical nanoscopy tools (like near-field scanning microscopy) can provide valuable insights.
412 Further, while there is much excitement regarding the ability to engineer emergent properties of interacting
413 particles in the moiré superlattice, the moiré trapped excitons may provide a means to locally probe or readout
414 single spins in the dilute exciton lattice¹³². In addition to the **Fermi-Hubbard model [G]**, an array of moiré
415 trapped excitons provides a novel platform to investigate superradiance or **Bose-Hubbard [G]** physics and
416 topological collective excitations¹⁸⁴⁻¹⁸⁶. Other novel approaches to confine particles in 2D semiconductors
417 include electrostatic gating of intralayer¹⁸⁷ or interlayer excitons^{188,189}. Although reaching the quantum regime
418 with electrostatic gating will be challenging, the large Coulomb interactions and dipolar repulsion energy for
419 interlayer excitons^{119,120} provide a possible route.

420
421
422 From a material perspective, significant advances in crystal growth, including epitaxial techniques, are
423 required to move beyond mechanical exfoliation and manual stacking. Large-scale growth and cost-effective
424 fabrication¹⁹⁰ of TMD monolayers, homo- and hetero-bilayers (with tunable interlayer twist angle¹⁹¹) and
425 heterostructures have been realized for various electronic and photonic applications, and it is highly anticipated
426 that the quality and size of 2D materials will be continuously improved at a fast pace. However, in contrast to
427 many other photonic applications (such as photodetectors, modulators, lasers), the intrinsic quantum emission
428 properties and performance of 2D materials based SPEs are more sensitive to structural disorders and
429 environmental perturbations. Therefore, 2D SPEs require substantial more efforts (defect control and/or
430 engineering) for scalable (CMOS compatible growth for on-chip devices) 2D material synthesis and device
431 integration. Exfoliation and stacking are currently still essential for high quality optical devices. Recent advances
432 in large-scale exfoliation¹⁹², flake identification¹⁹³ and automated assembly¹⁹⁴ are promising for higher yield and
433 more complex heterostructure devices.

435 **H2 Purcell enhancement and integration.**

436
437 An important route to successfully bring the performance of 2D SPEs on par with other quantum emitters⁵, in
438 particular quantum dots^{8,195}, is the realization of Purcell enhanced quantum light emission. First, Purcell-
439 enhanced emission would mitigate the spectral diffusion induced inhomogeneous broadening, which is the main
440 limiting factor for the generation of indistinguishable photons. Second, it would increase the collection
441 efficiency and brightness of the 2D material single-photon source and its coupling into a specific fibre mode for
442 long-range communication applications or into a photonic circuit waveguide for on-chip operations. Current
443 approaches to transfer 2D materials on top of photonic waveguides unfortunately only result in coupling
444 efficiencies into the photonic circuits below 10%^{29,30,110}. The unique atomically thin nature of 2D materials

445 comes with advantages and disadvantages for cavity coupling. Compared to single atoms and ions, the 2D SPEs
446 are embedded in a solid-state system; this embedding removes the need for active trapping in cavities, while still
447 allowing for ultra-low cavity mode volumes, which is typically trickier for other platforms. Thanks to the
448 straightforward transfer to other materials, 2D SPEs are easy to integrate into external cavities (Box 2).
449 However, not being incorporated in a matrix also means that nanofabricating a monolithic cavity is more
450 challenging compared to quantum dots.

451 As 2D SPEs can be simulated as a simple dipole, to a first order approximation, many different cavity
452 coupling designs have been proposed and fabricated (Box 2). One possible approach is the integration of the 2D
453 SPEs in plasmonic cavities^{22,24}, which in addition to the cavity coupling simultaneously act as the strain-induced
454 nucleation site. Another approach is embedding 2D materials in tunable open cavities^{25,103,105} (for example,
455 photonic nanobeam cavities¹⁹⁶, whispering gallery-mode microcavities¹⁹⁷, and possible ring resonators¹⁹⁸ for
456 photonic circuits integration¹⁹⁹), which aim for high cavity quality factors instead of small mode confinement to
457 realize their Purcell enhancement. One challenge in designing the ideal 2D SPE cavity system is to realize
458 perfect mode overlap between the 2D SPE and the cavity mode. Typically the common transfer method to place
459 the 2D material on top of the cavity²⁰⁰ or waveguide²⁰¹ results in low coupling efficiencies. Additionally, for
460 cavities with small mode volume, a precise lateral position of the 2D SPE is crucial. One possible avenue to
461 success might be 2D SPEs generated by ion-bombardment or other methods with good emitter positioning
462 accuracy in all three axes. Another challenge is the spectral overlap of the SPE and the cavity mode, since
463 typical 2D SPEs have a broad ensemble PL. Therefore, additional tuning knobs such as electric field tuning are
464 required, further complicating the cavity based 2D material device²⁰². One approach particularly promising for
465 2D emitters which can overcome these challenges is the use of a broadband circular Bragg grating cavity²⁰³. In
466 principle, it ultimately may become possible to integrate all three key quantum technologies (such as photon
467 counters²⁰⁴⁻²⁰⁶, linear and nonlinear photonic circuits²⁰⁷, and single-photon sources) with hybrid 2D materials
468 based platforms, for example with integrated waveguides (Box 2).

469 **H1 Outlook**

470

471 **[H2] Coherence and spin-photon interfaces.**

472

473 The most obvious applications of the scalable SPEs would be deployment in quantum technologies as either
474 coherent single photon sources or spin-photon interfaces for quantum networking. However, significant
475 challenges must be overcome, such as the generation of indistinguishable single photons from 2D SPEs. To date,
476 **Hong-Ou-Mandel interference [G]** with even limited visibility at short delay times has yet to be reported with
477 any 2D material host, and thus far, time-averaged spectra for all 2D SPEs reveal significant inhomogeneous
478 broadening (typically $> 10\times$ the transform limit). In this regard, intrinsic or interface disorder is a formidable
479 obstacle in 2D materials²⁰⁸ as it can lead to dynamic environmental charging and thus SPE emission energy
480 fluctuations. There are two main strategies to mitigate this: reducing the charge noise in the SPE environment or
481 increasing the transform-limited linewidth by decreasing the emitter lifetime via Purcell enhancement. Both
482 strategies are likely needed. For TMDs, samples encapsulated in hBN have been successfully used to achieve
483 near transform-limited linewidths (meV-scale) for 2D free excitons^{95,96,209}, but similar efforts have yet to yield
484 transform-limited linewidths for SPEs (μeV -scale), even with resonant excitation. Charge tunable devices, in
485 which the Fermi level is pinned to stabilize the charge or all excess carriers are depleted^{210,211}, and higher quality
486 intrinsic 2D materials with lower defect densities²¹² are attractive options to reduce environmental charge noise
487 in 2D SPE devices. The remaining dephasing mechanisms (like interactions with phonons and nuclear spins;
488 Box 1) are material and emitter dependent. Once the spectral fluctuations are reduced to manageable levels,
489 coherent control techniques developed for trapped atoms, III-V quantum dots, and defects in wide-bandgap
490 materials such as microwave or all-optical spin echo techniques²¹³ can be applied to the 2D SPEs.

491 While coherent manipulation of spins associated with emitters in TMDs has not been yet reported, selection
492 rules do provide possible pathways towards spin-photon interfacing. The presence of heavy elements like

493 transition metals leads to strong spin-orbit coupling. Spin-orbit coupling is typically expected to reduce spin
494 relaxation timescales, by coupling the spin to orbital degrees of freedom (which is then less sensitive to phonons
495 and electric fluctuations). Recent experiments²¹⁴ have however shown that this is not necessarily the case, and
496 the full complex interplay between spin-orbit coupling and symmetry needs to be understood. In terms of nuclear
497 spin baths, TMDs are quite promising. The 2D geometry in a free-standing monolayer features a spin bath only
498 in a 2D plane. Additionally, the elements composing popular TMD materials (Mo, W, Se, S) comprise a high
499 fraction of spin-zero isotopes. It has been shown in SiC that, for a multi-isotope bath, decoherence is reduced
500 under an applied magnetic field since the Zeeman splitting associated with different gyromagnetic ratios
501 prevents flip-flops for nuclear pairs in close vicinity²¹⁵. This effect will play a role in reducing decoherence also
502 in 2D materials, most of which feature two or more different isotopes. The combination of 2D geometry and
503 multi-isotope baths with predominantly spin-zero isotopes creates a dilute spin bath, suggesting long dephasing
504 time and possibly the capability to address individual nuclear spins.

505 Finally, similar to the case of self-assembled quantum dots, the discovery of biexcitons in WSe₂ quantum
506 dots⁷³ (Fig. 5) offers some prospects towards polarisation-entangled photon pairs via the biexciton cascade.^{216,217}
507 However, two significant challenges need to be overcome. First, it is necessary to achieve a better deterministic
508 control of the quantum dot formation. Despite the observation of biexciton formation in WSe₂ quantum dots by
509 different groups⁷³⁻⁷⁵, the majority of reported WSe₂ quantum dots typically do not show biexciton emission. In
510 this sense, further efforts are required to understand the origin of biexciton formation in these quantum dots
511 together with the corresponding improvement in the reproducibility of quantum dot creation. Second, the large
512 FSS characteristic of WSe₂ quantum dots imposes additional limitations towards the creation of entangled-
513 photon pairs. In principle, since the presence of a FSS only leads to a precession of the exciton phase, the degree
514 of entanglement in the biexciton-cascade scheme is only determined by the temporal resolution with which the
515 time delay between the emitted photon pair is measured²¹⁸. Therefore, in theory, it should be possible to produce
516 entangled photon pairs from the biexciton cascade in WSe₂ regardless of the non-vanishing FSS provided that
517 the necessary temporal experimental resolution could be achieved. Unfortunately, the typical FSS values in
518 WSe₂ quantum dots impose an experimental limitation regarding the required temporal resolution of the
519 detectors. Consequently, further efforts are needed to pursue a FSS reduction by different approaches such as
520 controlled electric¹⁰² or strain tuning¹⁰⁷.

521
522
523
524

525 [H2] Quantum nonlinear optics in 2D materials.

526 2D materials exhibit extraordinarily large nonlinearities¹⁶⁹, which shows high promise for photon pair
527 generation^{219,220} (see Supplementary Information for an introduction). In principle, using atomically thin
528 nonlinear materials removes the need for phase matching^{169,221-224} to manifest several performance advantages
529 compared to traditional bulk crystals. It also has been shown that second-order optical nonlinearity can be
530 permitted in centrosymmetric 2D materials by interlayer twisting to break the symmetry²²⁵⁻²²⁷. Electrically
531 tuneable second- and third-order nonlinearities have been demonstrated²²⁸⁻²³⁴ indicating the possibility of
532 electrically-tunable quantum sources for future quantum photonics²³⁵. Nevertheless, the nonlinear optical
533 responses in 2D materials are typically limited by their atomic light-matter interaction length. Therefore, hybrid
534 2D materials^{169,233} (for example, with silicon based waveguides or silica based optical fibers²³⁶⁻²³⁸, optical
535 cavities^{233,239}, antennas²⁴⁰, or metamaterials²⁴¹, exciton-²⁴² and phonon- polariton²⁴³⁻²⁴⁵ hybrids) could be potential
536 approaches to enhance the nonlinearity in 2D materials at the quantum level. Further, monolayer TMDs can
537 exhibit near transform-limited 2D excitons. In this limit, an incoming laser resonant with the 2D exciton can be
538 perfectly reflected, and this process can be tunable by gating the TMD to change the exciton resonance^{246,247}.
539 With the freedom to freely position the mirror-like atom sheet arbitrarily in front of a dielectric mirror²⁴⁸⁻²⁵⁰, the
540 nonlinear optical regime at the quantum level or extreme light-matter interaction may become possible²⁵¹.
541 Despite a lack of successful experimental demonstration^{219,220}, so far, 2D materials and their heterostructures
542 based hybrid nonlinear optical systems make up an interesting platform for strong photon-photon interactions at

543 the few-photon level, potentially enabling a number of unique quantum photonic applications, such as
544 generation^{219,220,252}, manipulation²⁵³⁻²⁵⁶ and detection of quantum states.
545

546 [H2] Quantum sensing

547
548 The diversity of 2D materials provides exciting opportunities for investigations and applications exploiting spins
549 and valleys, such as many-body spin physics (with high-fidelity electrical injection of polarized spins²⁵⁷),
550 spintronics (by investigating Kondo-phenomena beyond metallic-like Kondo screening²⁵⁸), and quantum sensors
551 (by optically polarizing and controlling individual spins associated with quantum emitters to map quantities of
552 physical interest at the nanoscale). For some systems, in particular the nitrogen-vacancy centre in diamond, the
553 electronic structure features an intersystem crossing that results in a difference in PL intensity for different
554 ground-state spin levels (optically-detected magnetic resonance), even at room temperature. This capability has
555 opened up opportunities to study nanoscale magnetism, biological systems, and nanoscale magnetic resonance
556 imaging. The extension of this capability to a 2D geometry, with the discovery of optically-detected magnetic
557 resonance in 2D materials, could open additional exciting opportunities, given the expected ease of integration of
558 such sensors with scanning tips or directly into the surface of the sample to be studied.
559

560 References

- 561
562
- 563 1 O'Brien, J. L., Furusawa, A. & Vučković, J. Photonic quantum technologies. *Nat. Photonics* **3**, 687,
564 doi:10.1038/nphoton.2009.229 (2009).
 - 565 2 Ekert, A. K. Quantum cryptography based on Bell's theorem. *Phys. Rev. Lett.* **67**, 661-663,
566 doi:10.1103/PhysRevLett.67.661 (1991).
 - 567 3 Patel, K. A. *et al.* Coexistence of High-Bit-Rate Quantum Key Distribution and Data on Optical Fiber.
568 *Phys. Rev. X* **2**, 041010, doi:10.1103/Physrevx.2.041010 (2012).
 - 569 4 Giovannetti, V., Lloyd, S. & Maccone, L. Quantum-enhanced measurements: Beating the standard
570 quantum limit. *Science* **306**, 1330-1336, doi:10.1126/science.1104149 (2004).
 - 571 5 Aharonovich, I., Englund, D. & Toth, M. Solid-state single-photon emitters. *Nat. Photonics* **10**, 631,
572 doi:10.1038/nphoton.2016.186 (2016).
 - 573 6 Gao, W. B., Imamoglu, A., Bernien, H. & Hanson, R. Coherent manipulation, measurement and
574 entanglement of individual solid-state spins using optical fields. *Nat. Photonics* **9**, 363,
575 doi:10.1038/nphoton.2015.58 (2015).
 - 576 7 Atatüre, M., Englund, D., Vamivakas, N., Lee, S.-Y. & Wrachtrup, J. Material platforms for spin-based
577 photonic quantum technologies. *Nat. Rev. Mater.* **3**, 38-51, doi:10.1038/s41578-018-0008-9 (2018).
 - 578 8 Senellart, P., Solomon, G. & White, A. High-performance semiconductor quantum-dot single-photon
579 sources. *Nat. Nanotechnol.* **12**, 1026, doi:10.1038/nnano.2017.218 (2017).
 - 580 9 Chakraborty, C., Kinnischtzke, L., Goodfellow, K. M., Beams, R. & Vamivakas, A. N. Voltage-
581 controlled quantum light from an atomically thin semiconductor. *Nat. Nanotechnol.* **10**, 507,
582 doi:10.1038/Nnano.2015.79 (2015).
 - 583 10 He, Y. M. *et al.* Single quantum emitters in monolayer semiconductors. *Nat. Nanotechnol.* **10**, 497-502,
584 doi:10.1038/Nnano.2015.75 (2015).
 - 585 11 Koperski, M. *et al.* Single photon emitters in exfoliated WSe₂ structures. *Nat. Nanotechnol.* **10**, 503,
586 doi:10.1038/nnano.2015.67 (2015).
 - 587 12 Srivastava, A. *et al.* Optically active quantum dots in monolayer WSe₂. *Nat. Nanotechnol.* **10**, 491,
588 doi:10.1038/NNANO.2015.60 (2015).
 - 589 13 Tonndorf, P. *et al.* Single-photon emission from localized excitons in an atomically thin semiconductor.
590 *Optica* **2**, 347-352, doi:10.1364/Optica.2.000347 (2015).

591 14 Tran, T. T., Bray, K., Ford, M. J., Toth, M. & Aharonovich, I. Quantum emission from hexagonal boron
592 nitride monolayers. *Nat. Nanotechnol.* **11**, 37, doi:10.1038/Nnano.2015.242 (2016).

593 15 Kumar, S., Kaczmarczyk, A. & Gerardot, B. D. Strain-induced spatial and spectral isolation of quantum
594 emitters in mono-and bilayer WSe₂. *Nano Lett.* **15**, 7567-7573, doi:10.1021/acs.nanolett.5b03312
595 (2015).

596 16 Kern, J. *et al.* Nanoscale Positioning of Single-Photon Emitters in Atomically Thin WSe₂. *Adv. Mater.*
597 **28**, 7101-7105, doi:10.1002/adma.201600560 (2016).

598 17 Branny, A., Kumar, S., Proux, R. & Gerardot, B. D. Deterministic strain-induced arrays of quantum
599 emitters in a two-dimensional semiconductor. *Nat. Commun.* **8**, 15053, doi:10.1038/ncomms15053
600 (2017).

601 18 Palacios-Berraquero, C. *et al.* Large-scale quantum-emitter arrays in atomically thin semiconductors.
602 *Nat. Commun.* **8**, 15093, doi:10.1038/ncomms15093 (2017).

603 19 Proscia, N. V. *et al.* Near-deterministic activation of room-temperature quantum emitters in hexagonal
604 boron nitride. *Optica* **5**, 1128-1134, doi:10.1364/OPTICA.5.001128 (2018).

605 20 Wang, G. *et al.* Colloquium: Excitons in atomically thin transition metal dichalcogenides. *Rev. Mod.*
606 *Phys.* **90**, 021001, doi:10.1103/RevModPhys.90.021001 (2018).

607 21 Tripathi, L. N. *et al.* Spontaneous Emission Enhancement in Strain-Induced WSe₂ Monolayer-Based
608 Quantum Light Sources on Metallic Surfaces. *ACS Photonics* **5**, 1919-1926,
609 doi:10.1021/acsp Photonics.7b01053 (2018).

610 22 Luo, Y. *et al.* Deterministic coupling of site-controlled quantum emitters in monolayer WSe₂ to
611 plasmonic nanocavities. *Nat. Nanotechnol.* **13**, 1137-1142, doi:10.1038/s41565-018-0275-z (2018).

612 23 Cai, T. *et al.* Radiative Enhancement of Single Quantum Emitters in WSe₂ Monolayers Using Site-
613 Controlled Metallic Nanopillars. *ACS Photonics* **5**, 3466-3471, doi:10.1021/acsp Photonics.8b00580
614 (2018).

615 24 Tran, T. T. *et al.* Deterministic Coupling of Quantum Emitters in 2D Materials to Plasmonic Nanocavity
616 Arrays. *Nano Lett.* **17**, 2634-2639, doi:10.1021/acs.nanolett.7b00444 (2017).

617 25 Flatten, L. C. *et al.* Microcavity enhanced single photon emission from two-dimensional WSe₂. *Appl.*
618 *Phys. Lett.* **112**, 191105, doi:10.1063/1.5026779 (2018).

619 26 White, D. *et al.* Atomically-thin quantum dots integrated with lithium niobate photonic chips. *Opt.*
620 *Mater. Express* **9**, 441-448, doi:10.1364/OME.9.000441 (2019).

621 27 Blauth, M. *et al.* Coupling Single Photons from Discrete Quantum Emitters in WSe₂ to Lithographically
622 Defined Plasmonic Slot Waveguides. *Nano Lett.* **18**, 6812-6819, doi:10.1021/acs.nanolett.8b02687
623 (2018).

624 28 Tonndorf, P. *et al.* On-chip waveguide coupling of a layered semiconductor single-photon source. *Nano*
625 *Lett.* **17**, 5446-5451, doi:10.1021/acs.nanolett.7b02092 (2017).

626 29 Peyskens, F., Chakraborty, C., Muneeb, M., Van Thourhout, D. & Englund, D. Integration of single
627 photon emitters in 2D layered materials with a silicon nitride photonic chip. *Nat. Commun.* **10**, 4435,
628 doi:10.1038/s41467-019-12421-0 (2019).

629 30 Kim, S. *et al.* Integrated on Chip Platform with Quantum Emitters in Layered Materials. *Adv. Opt.*
630 *Mater.* **7**, 1901132, doi:10.1002/adom.201901132 (2019).

631 31 Palacios-Berraquero, C. *et al.* Atomically thin quantum light-emitting diodes. *Nat. Commun.* **7**, 12978,
632 doi:10.1038/ncomms12978 (2016).

633 32 Brotons-Gisbert, M. *et al.* Coulomb blockade in an atomically thin quantum dot coupled to a tunable
634 Fermi reservoir. *Nat. Nanotechnol.* **14**, 442-446, doi:10.1038/s41565-019-0402-5 (2019).

635 33 Lu, X. *et al.* Optical initialization of a single spin-valley in charged WSe₂ quantum dots. *Nat.*
636 *Nanotechnol.* **14**, 426-431, doi:10.1038/s41565-019-0394-1 (2019).

637 34 Yu, H., Liu, G.-B., Tang, J., Xu, X. & Yao, W. Moiré excitons: From programmable quantum emitter
638 arrays to spin-orbit-coupled artificial lattices. *Sci. Adv.* **3**, e1701696, doi:10.1126/sciadv.1701696
639 (2017).

640 35 Seyler, K. L. *et al.* Signatures of moiré-trapped valley excitons in MoSe₂/WSe₂ heterobilayers. *Nature*
641 **567**, 66-70, doi:10.1038/s41586-019-0957-1 (2019).

642 36 Tran, K. *et al.* Evidence for moiré excitons in van der Waals heterostructures. *Nature* **567**, 71-75,
643 doi:10.1038/s41586-019-0975-z (2019).

644 37 Anichini, C. *et al.* Chemical sensing with 2D materials. *Chem. Soc. Rev.* **47**, 4860-4908,
645 doi:10.1039/C8CS00417J (2018).

646 38 Chen, Z., Biscaras, J. & Shukla, A. A high performance graphene/few-layer InSe photo-detector.
647 *Nanoscale* **7**, 5981-5986, doi:10.1039/C5NR00400D (2015).

648 39 Shiue, R.-J. *et al.* High-Responsivity Graphene–Boron Nitride Photodetector and Autocorrelator in a
649 Silicon Photonic Integrated Circuit. *Nano Lett.* **15**, 7288-7293, doi:10.1021/acs.nanolett.5b02368 (2015).

650 40 Oberreiter, L. & Gerhardt, I. Light on a beam splitter: More randomness with single photons. *Laser*
651 *Photonics Rev.* **10**, 108-115, doi:10.1002/lpor.201500165 (2016).

652 41 Pirandola, S. *et al.* Advances in quantum cryptography. *Adv. Opt. Photon.* **12**, 1012-1236,
653 doi:10.1364/AOP.361502 (2020).

654 42 Hong, C. K., Ou, Z. Y. & Mandel, L. Measurement of subpicosecond time intervals between two
655 photons by interference. *Phys. Rev. Lett.* **59**, 2044-2046, doi:10.1103/PhysRevLett.59.2044 (1987).

656 43 Wehner, S., Elkouss, D. & Hanson, R. Quantum internet: A vision for the road ahead. *Science* **362**,
657 eaam9288, doi:10.1126/science.aam9288 (2018).

658 44 Abobeih, M. H. *et al.* One-second coherence for a single electron spin coupled to a multi-qubit nuclear-
659 spin environment. *Nat. Commun.* **9**, 2552, doi:10.1038/s41467-018-04916-z (2018).

660 45 Nagy, R. *et al.* High-fidelity spin and optical control of single silicon-vacancy centres in silicon carbide.
661 *Nat. Commun.* **10**, 1954, doi:10.1038/s41467-019-09873-9 (2019).

662 46 Zhong, M. *et al.* Optically addressable nuclear spins in a solid with a six-hour coherence time. *Nature*
663 **517**, 177, doi:10.1038/nature14025 (2015).

664 47 Humphreys, P. C. *et al.* Deterministic delivery of remote entanglement on a quantum network. *Nature*
665 **558**, 268-273, doi:10.1038/s41586-018-0200-5 (2018).

666 48 Robledo, L. *et al.* High-fidelity projective read-out of a solid-state spin quantum register. *Nature* **477**,
667 574, doi:10.1038/nature10401 (2011).

668 49 Sukachev, D. D. *et al.* Silicon-Vacancy Spin Qubit in Diamond: A Quantum Memory Exceeding 10 ms
669 with Single-Shot State Readout. *Phys. Rev. Lett.* **119**, 223602, doi:10.1103/PhysRevLett.119.223602
670 (2017).

671 50 Delteil, A., Gao, W.-b., Fallahi, P., Miguel-Sanchez, J. & Imamoglu, A. Observation of Quantum Jumps
672 of a Single Quantum Dot Spin Using Submicrosecond Single-Shot Optical Readout. *Phys. Rev. Lett.*
673 **112**, 116802, doi:10.1103/PhysRevLett.112.116802 (2014).

674 51 Gao, W. B., Fallahi, P., Togan, E., Miguel-Sanchez, J. & Imamoglu, A. Observation of entanglement
675 between a quantum dot spin and a single photon. *Nature* **491**, 426, doi:10.1038/nature11573 (2012).

676 52 Togan, E. *et al.* Quantum entanglement between an optical photon and a solid-state spin qubit. *Nature*
677 **466**, 730, doi:10.1038/nature09256 (2010).

678 53 De Greve, K. *et al.* Quantum-dot spin–photon entanglement via frequency downconversion to telecom
679 wavelength. *Nature* **491**, 421-425, doi:10.1038/nature11577 (2012).

680 54 Kalb, N. *et al.* Entanglement distillation between solid-state quantum network nodes. *Science* **356**, 928-
681 932, doi:10.1126/science.aan0070 (2017).

682 55 Stockill, R. *et al.* Phase-Tuned Entangled State Generation between Distant Spin Qubits. *Phys. Rev. Lett.*
683 **119**, 010503, doi:10.1103/PhysRevLett.119.010503 (2017).

684 56 Jelezko, F. *et al.* Observation of Coherent Oscillation of a Single Nuclear Spin and Realization of a
685 Two-Qubit Conditional Quantum Gate. *Phys. Rev. Lett.* **93**, 130501,
686 doi:10.1103/PhysRevLett.93.130501 (2004).

687 57 Dutt, M. V. G. *et al.* Quantum Register Based on Individual Electronic and Nuclear Spin Qubits in
688 Diamond. *Science* **316**, 1312-1316, doi:10.1126/science.1139831 (2007).

689 58 Pla, J. J. *et al.* High-fidelity readout and control of a nuclear spin qubit in silicon. *Nature* **496**, 334-338,
690 doi:10.1038/nature12011 (2013).

691 59 Taminau, T. H. *et al.* Detection and Control of Individual Nuclear Spins Using a Weakly Coupled
692 Electron Spin. *Phys. Rev. Lett.* **109**, 137602, doi:10.1103/PhysRevLett.109.137602 (2012).

693 60 Bradley, C. E. *et al.* A Ten-Qubit Solid-State Spin Register with Quantum Memory up to One Minute.
694 *Phys. Rev. X* **9**, 031045, doi:10.1103/PhysRevX.9.031045 (2019).

695 61 Fu, K.-M. C. *et al.* Ultrafast control of donor-bound electron spins with single detuned optical pulses.
696 *Nat. Phys.* **4**, 780-784, doi:10.1038/nphys1052 (2008).

697 62 Aharonovich, I. *et al.* Diamond-based single-photon emitters. *Rep. Prog. Phys.* **74**, 076501,
698 doi:10.1088/0034-4885/74/7/076501 (2011).

699 63 Lohrmann, A., Johnson, B. C., McCallum, J. C. & Castelletto, S. A review on single photon sources in
700 silicon carbide. *Rep. Prog. Phys.* **80**, 034502, doi:10.1088/1361-6633/aa5171 (2017).

701 64 Petroff, P., Imamoglu, A. & Lorke, A. Epitaxially Self-Assembled Quantum Dots. *Phys. Today* **54**, 46,
702 doi:10.1063/1.1381102 (2001).

703 65 Gammon, D., Shanabrook, B. V. & Katzer, D. S. Excitons, phonons, and interfaces in GaAs/AlAs
704 quantum-well structures. *Phys. Rev. Lett.* **67**, 1547-1550, doi:10.1103/PhysRevLett.67.1547 (1991).

705 66 Klein, J. *et al.* Site-selectively generated photon emitters in monolayer MoS₂ via local helium ion
706 irradiation. *Nat. Commun.* **10**, 2755, doi:10.1038/s41467-019-10632-z (2019).

707 67 Barthelmi, K. *et al.* Atomistic defects as single-photon emitters in atomically thin MoS₂. *Appl. Phys.*
708 *Lett.* **117**, 070501, doi:10.1063/5.0018557 (2020).

709 68 Wu, F., Lovorn, T. & MacDonald, A. H. Theory of optical absorption by interlayer excitons in transition
710 metal dichalcogenide heterobilayers. *Phys. Rev. B* **97**, 035306, doi:10.1103/PhysRevB.97.035306
711 (2018).

712 69 Exarhos, A. L., Hopper, D. A., Patel, R. N., Doherty, M. W. & Bassett, L. C. Magnetic-field-dependent
713 quantum emission in hexagonal boron nitride at room temperature. *Nat. Commun.* **10**, 222,
714 doi:10.1038/s41467-018-08185-8 (2019).

715 70 Gottscholl, A. *et al.* Initialization and read-out of intrinsic spin defects in a van der Waals crystal at
716 room temperature. *Nat. Mater.* **19**, 540-545, doi:10.1038/s41563-020-0619-6 (2020).

717 71 Linhart, L. *et al.* Localized Intervalley Defect Excitons as Single-Photon Emitters in WSe₂. *Phys. Rev.*
718 *Lett.* **123**, 146401, doi:10.1103/PhysRevLett.123.146401 (2019).

719 72 Bayer, M. *et al.* Fine structure of neutral and charged excitons in self-assembled In(Ga)As/(Al)GaAs
720 quantum dots. *Phys. Rev. B* **65**, 195315, doi:10.1103/PhysRevB.65.195315 (2002).

721 73 He, Y.-M. *et al.* Cascaded emission of single photons from the biexciton in monolayered WSe₂. *Nat.*
722 *Commun.* **7**, 13409, doi:10.1038/ncomms13409 (2016).

723 74 Chakraborty, C. *et al.* 3D Localized Trions in Monolayer WSe₂ in a Charge Tunable van der Waals
724 Heterostructure. *Nano Lett.* **18**, 2859-2863, doi:10.1021/acs.nanolett.7b05409 (2018).

725 75 Parto, K., Azzam, S. I., Banerjee, K. & Moody, G. Defect and strain engineering of monolayer WSe₂
726 enables site-controlled single-photon emission up to 150 K. *Nat. Commun.* **12**, 3585,
727 doi:10.1038/s41467-021-23709-5 (2021).

728 76 Kumar, S. *et al.* Resonant laser spectroscopy of localized excitons in monolayer WSe₂. *Optica* **3**, 882-
729 886, doi:10.1364/OPTICA.3.000882 (2016).

730 77 He, Y.-M., Höfling, S. & Schneider, C. Phonon induced line broadening and population of the dark
731 exciton in a deeply trapped localized emitter in monolayer WSe₂. *Opt. Expr.* **24**, 8066-8073,
732 doi:10.1364/OE.24.008066 (2016).

733 78 Brooks, M. & Burkard, G. Theory of strain-induced confinement in transition metal dichalcogenide
734 monolayers. *Phys. Rev. B* **97**, 195454, doi:10.1103/Physrevb.97.195454 (2018).

735 79 Feng, J., Qian, X., Huang, C.-W. & Li, J. Strain-engineered artificial atom as a broad-spectrum solar
736 energy funnel. *Nat. Photonics* **6**, 866-872, doi:10.1038/nphoton.2012.285 (2012).

737 80 Branny, A. *et al.* Discrete quantum dot like emitters in monolayer MoSe₂: Spatial mapping, magneto-
738 optics, and charge tuning. *Appl. Phys. Lett.* **108**, 142101, doi:10.1063/1.4945268 (2016).

739 81 Chakraborty, C., Goodfellow, K. M. & Nick Vamivakas, A. Localized emission from defects in MoSe₂
740 layers. *Opt. Mater. Express* **6**, 2081-2087, doi:10.1364/OME.6.002081 (2016).

741 82 Yu, L. *et al.* Site-Controlled Quantum Emitters in Monolayer MoSe₂. *Nano Lett.* **21**, 2376-2381,
742 doi:10.1021/acs.nanolett.0c04282 (2021).

743 83 Shepard, G. D. *et al.* Nanobubble induced formation of quantum emitters in monolayer semiconductors. *2D Mater.* **4**, 021019, doi:10.1088/2053-1583/aa629d (2017).

744

745 84 Rosenberger, M. R. *et al.* Quantum Calligraphy: Writing Single-Photon Emitters in a Two-Dimensional

746 Materials Platform. *ACS Nano* **13**, 904-912, doi:10.1021/acsnano.8b08730 (2019).

747 85 Darlington, T. P. *et al.* Imaging strain-localized excitons in nanoscale bubbles of monolayer WSe₂ at

748 room temperature. *Nat. Nanotechnol.* **15**, 854-860, doi:10.1038/s41565-020-0730-5 (2020).

749 86 Chirolli, L., Prada, E., Guinea, F., Roldán, R. & San-Jose, P. Strain-induced bound states in transition-

750 metal dichalcogenide bubbles. *2D Mater.* **6**, 025010, doi:10.1088/2053-1583/ab0113 (2019).

751 87 Koperski, M. *et al.* Optical properties of atomically thin transition metal dichalcogenides: observations

752 and puzzles. *Nanophotonics* **6**, 1289-1308, doi:10.1515/nanoph-2016-0165 (2017).

753 88 Jones, A. M. *et al.* Optical generation of excitonic valley coherence in monolayer WSe₂. *Nat.*

754 *Nanotechnol.* **8**, 634-638, doi:10.1038/nnano.2013.151 (2013).

755 89 Zhang, S. *et al.* Defect Structure of Localized Excitons in a WSe₂ Monolayer. *Phys. Rev. Lett.* **119**,

756 046101, doi:10.1103/Physrevlett.119.046101 (2017).

757 90 Zheng, Y. J. *et al.* Point Defects and Localized Excitons in 2D WSe₂. *ACS Nano* **13**, 6050-6059,

758 doi:10.1021/acsnano.9b02316 (2019).

759 91 Zhou, X., Zhang, Z. & Guo, W. Dislocations as Single Photon Sources in Two-Dimensional

760 Semiconductors. *Nano Lett.* **20**, 4136-4143, doi:10.1021/acs.nanolett.9b05305 (2020).

761 92 Moody, G. *et al.* Microsecond Valley Lifetime of Defect-Bound Excitons in Monolayer WSe₂. *Phys.*

762 *Rev. Lett.* **121**, 057403, doi:10.1103/PhysRevLett.121.057403 (2018).

763 93 Klein, J. *et al.* Engineering the Luminescence and Generation of Individual Defect Emitters in

764 Atomically Thin MoS₂. *ACS Photonics* **8**, 669-677, doi:10.1021/acsp Photonics.0c01907 (2021).

765 94 Hötger, A. *et al.* Gate-Switchable Arrays of Quantum Light Emitters in Contacted Monolayer MoS₂ van

766 der Waals Heterodevices. *Nano Lett.* **21**, 1040-1046, doi:10.1021/acs.nanolett.0c04222 (2021).

767 95 Wierzbowski, J. *et al.* Direct exciton emission from atomically thin transition metal dichalcogenide

768 heterostructures near the lifetime limit. *Sci. Rep.* **7**, 12383, doi:10.1038/s41598-017-09739-4 (2017).

769 96 Cadiz, F. *et al.* Excitonic Linewidth Approaching the Homogeneous Limit in MoS₂-Based van der

770 Waals Heterostructures. *Phys. Rev. X* **7**, 021026, doi:10.1103/PhysRevX.7.021026 (2017).

771 97 Schwarz, S. *et al.* Electrically pumped single-defect light emitters in WSe₂. *2D Mater.* **3**, 025038,

772 doi:10.1088/2053-1583/3/2/025038 (2016).

773 98 Clark, G. *et al.* Single Defect Light-Emitting Diode in a van der Waals Heterostructure. *Nano Lett.* **16**,

774 3944-3948, doi:10.1021/acs.nanolett.6b01580 (2016).

775 99 Liu, G.-B., Pang, H., Yao, Y. & Yao, W. Intervalley coupling by quantum dot confinement potentials in

776 monolayer transition metal dichalcogenides. *New J. Phys.* **16**, 105011, doi:10.1088/1367-

777 2630/16/10/105011 (2014).

778 100 Roch, J. G. *et al.* Quantum-Confined Stark Effect in a MoS₂ Monolayer van der Waals Heterostructure.

779 *Nano Lett.* **18**, 1070-1074, doi:10.1021/acs.nanolett.7b04553 (2018).

780 101 Chakraborty, C. *et al.* Quantum-Confined Stark Effect of Individual Defects in a van der Waals

781 Heterostructure. *Nano Lett.* **17**, 2253-2258, doi:10.1021/acs.nanolett.6b04889 (2017).

782 102 Chakraborty, C., Jungwirth, N. R., Fuchs, G. D. & Vamivakas, A. N. Electrical manipulation of the fine-

783 structure splitting of WSe₂ quantum emitters. *Phys. Rev. B* **99**, 045308,

784 doi:10.1103/PhysRevB.99.045308 (2019).

785 103 Schwarz, S. *et al.* Two-Dimensional Metal-Chalcogenide Films in Tunable Optical Microcavities. *Nano*

786 *Lett.* **14**, 7003-7008, doi:10.1021/nl503312x (2014).

787 104 Dufferwiel, S. *et al.* Valley coherent exciton-polaritons in a monolayer semiconductor. *Nat. Commun.* **9**,

788 4797, doi:10.1038/s41467-018-07249-z (2018).

789 105 Häußler, S. *et al.* Tunable Fiber-Cavity Enhanced Photon Emission from Defect Centers in hBN. *Adv.*

790 *Opt. Mater.* **n/a**, 2002218, doi:10.1002/adom.202002218.

791 106 Ye, Y. *et al.* Single photon emission from deep-level defects in monolayer WSe₂. *Phys. Rev. B* **95**,

792 245313, doi:10.1103/Physrevb.95.245313 (2017).

793 107 Kim, H., Moon, J. S., Noh, G., Lee, J. & Kim, J.-H. Position and Frequency Control of Strain-Induced
794 Quantum Emitters in WSe₂ Monolayers. *Nano Lett.* **19**, 7534-7539, doi:10.1021/acs.nanolett.9b03421
795 (2019).

796 108 Iff, O. *et al.* Strain-Tunable Single Photon Sources in WSe₂ Monolayers. *Nano Lett.* **19**, 6931-6936,
797 doi:10.1021/acs.nanolett.9b02221 (2019).

798 109 Ren, T. & Loh, K. P. On-chip integrated photonic circuits based on two-dimensional materials and
799 hexagonal boron nitride as the optical confinement layer. *J. Appl. Phys.* **125**, 230901,
800 doi:10.1063/1.5096195 (2019).

801 110 Errando-Herranz, C. *et al.* Resonance Fluorescence from Waveguide-Coupled, Strain-Localized, Two-
802 Dimensional Quantum Emitters. *ACS Photonics* **8**, 1069-1076, doi:10.1021/acsp Photonics.0c01653
803 (2021).

804 111 Deotare, P. B., McCutcheon, M. W., Frank, I. W., Khan, M. & Lončar, M. High quality factor photonic
805 crystal nanobeam cavities. *Appl. Phys. Lett.* **94**, 121106, doi:10.1063/1.3107263 (2009).

806 112 Chiu, M.-H. *et al.* Determination of band alignment in the single-layer MoS₂/WSe₂ heterojunction. *Nat.*
807 *Commun.* **6**, 7666, doi:10.1038/ncomms8666 (2015).

808 113 Wilson, N. R. *et al.* Determination of band offsets, hybridization, and exciton binding in 2D
809 semiconductor heterostructures. *Sci. Adv.* **3**, e1601832, doi:10.1126/sciadv.1601832 (2017).

810 114 Rivera, P. *et al.* Observation of long-lived interlayer excitons in monolayer MoSe₂-WSe₂
811 heterostructures. *Nat. Commun.* **6**, 6242, doi:10.1038/ncomms7242 (2015).

812 115 Rivera, P. *et al.* Valley-polarized exciton dynamics in a 2D semiconductor heterostructure. *Science* **351**,
813 688-691, doi:10.1126/science.aac7820 (2016).

814 116 Hanbicki, A. T. *et al.* Indirect Interlayer Exciton in a MoSe₂/WSe₂ van der Waals Heterostructure. *ACS*
815 *Nano* **12**, 4719-4726, doi:10.1021/acsnano.8b01369 (2018).

816 117 Ciarrocchi, A. *et al.* Polarization switching and electrical control of interlayer excitons in two-
817 dimensional van der Waals heterostructures. *Nat. Photonics* **13**, 131-136, doi:10.1038/s41566-018-0325-
818 y (2019).

819 118 Miller, B. *et al.* Long-Lived Direct and Indirect Interlayer Excitons in van der Waals Heterostructures.
820 *Nano Lett.* **17**, 5229-5237, doi:10.1021/acs.nanolett.7b01304 (2017).

821 119 Li, W., Lu, X., Dubey, S., Devenica, L. & Srivastava, A. Dipolar interactions between localized
822 interlayer excitons in van der Waals heterostructures. *Nat. Mater.* **19**, 624-629, doi:10.1038/s41563-020-
823 0661-4 (2020).

824 120 Kremser, M. *et al.* Discrete interactions between a few interlayer excitons trapped at a MoSe₂-WSe₂
825 heterointerface. *NPJ 2D Mater. and Appl.* **4**, 8, doi:10.1038/s41699-020-0141-3 (2020).

826 121 Kang, J., Li, J., Li, S.-S., Xia, J.-B. & Wang, L.-W. Electronic Structural Moiré Pattern Effects on
827 MoS₂/MoSe₂ 2D Heterostructures. *Nano Lett.* **13**, 5485-5490, doi:10.1021/nl4030648 (2013).

828 122 Weston, A. *et al.* Atomic reconstruction in twisted bilayers of transition metal dichalcogenides. *Nat.*
829 *Nanotechnol.* **15**, 592-597, doi:10.1038/s41565-020-0682-9 (2020).

830 123 Rosenberger, M. R. *et al.* Twist Angle-Dependent Atomic Reconstruction and Moiré Patterns in
831 Transition Metal Dichalcogenide Heterostructures. *ACS Nano* **14**, 4550-4558,
832 doi:10.1021/acsnano.0c00088 (2020).

833 124 Luo, Y. *et al.* In situ nanoscale imaging of moiré superlattices in twisted van der Waals heterostructures.
834 *Nat. Commun.* **11**, 4209, doi:10.1038/s41467-020-18109-0 (2020).

835 125 Alexeev, E. M. *et al.* Resonantly hybridized excitons in moiré superlattices in van der Waals
836 heterostructures. *Nature* **567**, 81-86, doi:10.1038/s41586-019-0986-9 (2019).

837 126 Zhang, C. *et al.* Interlayer couplings, Moiré patterns, and 2D electronic superlattices in MoS₂/WSe₂
838 hetero-bilayers. *Sci. Adv.* **3**, e1601459, doi:10.1126/sciadv.1601459 (2017).

839 127 Brotons-Gisbert, M. *et al.* Spin-layer locking of interlayer excitons trapped in moiré potentials. *Nat.*
840 *Mater.* **19**, 630-636, doi:10.1038/s41563-020-0687-7 (2020).

841 128 Baek, H. *et al.* Highly energy-tunable quantum light from moiré-trapped excitons. *Sci. Adv.* **6**, eaba8526,
842 doi:10.1126/sciadv.aba8526 (2020).

843 129 Du, L. *et al.* Engineering symmetry breaking in 2D layered materials. *Nature Reviews Physics* **3**, 193-
844 206, doi:10.1038/s42254-020-00276-0 (2021).

845 130 Yu, H., Liu, G.-B. & Yao, W. Brightened spin-triplet interlayer excitons and optical selection rules in
846 van der Waals heterobilayers. *2D Mater.* **5**, 035021, doi:10.1088/2053-1583/aac065 (2018).

847 131 Liu, E. *et al.* Signatures of moiré trions in WSe₂/MoSe₂ heterobilayers. *Nature* **594**, 46-50,
848 doi:10.1038/s41586-021-03541-z (2021).

849 132 Baek, H. *et al.* Optical read-out of Coulomb staircases in a moiré superlattice via trapped interlayer
850 trions. *Nat. Nanotechnol.*, doi:10.1038/s41565-021-00970-9 (2021).

851 133 Brotons-Gisbert, M. *et al.* Moiré-Trapped Interlayer Trions in a Charge-Tunable WSe₂/MoSe₂
852 Heterobilayer. *Phys. Rev. X* **11**, 031033, doi:10.1103/PhysRevX.11.031033 (2021).

853 134 Bai, Y. *et al.* Excitons in strain-induced one-dimensional moiré potentials at transition metal
854 dichalcogenide heterojunctions. *Nat. Mater.* **19**, 1068-1073, doi:10.1038/s41563-020-0730-8 (2020).

855 135 Tran, T. T. *et al.* Quantum Emission from Defects in Single-Crystalline Hexagonal Boron Nitride. *Phys.*
856 *Rev. Appl.* **5**, 034005, doi:10.1103/PhysRevApplied.5.034005 (2016).

857 136 Nikolay, N. *et al.* Direct measurement of quantum efficiency of single-photon emitters in hexagonal
858 boron nitride. *Optica* **6**, 1084-1088, doi:10.1364/OPTICA.6.001084 (2019).

859 137 Tran, T. T. *et al.* Robust Multicolor Single Photon Emission from Point Defects in Hexagonal Boron
860 Nitride. *ACS Nano* **10**, 7331-7338, doi:10.1021/acsnano.6b03602 (2016).

861 138 Wigger, D. *et al.* Phonon-assisted emission and absorption of individual color centers in hexagonal
862 boron nitride. *2D Mater.* **6**, 035006, doi:10.1088/2053-1583/ab1188 (2019).

863 139 Hayee, F. *et al.* Revealing multiple classes of stable quantum emitters in hexagonal boron nitride with
864 correlated optical and electron microscopy. *Nat. Mater.* **19**, 534-539, doi:10.1038/s41563-020-0616-9
865 (2020).

866 140 Noh, G. *et al.* Stark Tuning of Single-Photon Emitters in Hexagonal Boron Nitride. *Nano Lett.* **18**, 4710-
867 4715, doi:10.1021/acsnanolett.8b01030 (2018).

868 141 Nikolay, N. *et al.* Very Large and Reversible Stark-Shift Tuning of Single Emitters in Layered
869 Hexagonal Boron Nitride. *Phys. Rev. Appl.* **11**, 041001, doi:10.1103/PhysRevApplied.11.041001 (2019).

870 142 Grosso, G. *et al.* Tunable and high-purity room temperature single-photon emission from atomic defects
871 in hexagonal boron nitride. *Nat. Commun.* **8**, 705, doi:10.1038/s41467-017-00810-2 (2017).

872 143 Bourrellier, R. *et al.* Bright UV single photon emission at point defects in h-BN. *Nano Lett.* **16**, 4317-
873 4321, doi:10.1021/acsnanolett.6b01368 (2016).

874 144 Tawfik, S. A. *et al.* First-principles investigation of quantum emission from hBN defects. *Nanoscale* **9**,
875 13575-13582, doi:10.1039/c7nr04270a (2017).

876 145 Turiansky, M. E., Alkauskas, A., Bassett, L. C. & Van de Walle, C. G. Dangling Bonds in Hexagonal
877 Boron Nitride as Single-Photon Emitters. *Phys. Rev. Lett.* **123**, 127401,
878 doi:10.1103/PhysRevLett.123.127401 (2019).

879 146 Choi, S. *et al.* Engineering and Localization of Quantum Emitters in Large Hexagonal Boron Nitride
880 Layers. *ACS Appl. Mater. Interfaces* **8**, 29642-29648, doi:10.1021/acsnanolett.6b09875 (2016).

881 147 Hou, S. *et al.* Localized emission from laser-irradiated defects in 2D hexagonal boron nitride. *2D Mater.*
882 **5**, 015010, doi:10.1088/2053-1583/aa8e61 (2017).

883 148 Ziegler, J. *et al.* Deterministic Quantum Emitter Formation in Hexagonal Boron Nitride via Controlled
884 Edge Creation. *Nano Lett.* **19**, 2121-2127, doi:10.1021/acsnanolett.9b00357 (2019).

885 149 Fournier, C. *et al.* Position-controlled quantum emitters with reproducible emission wavelength in
886 hexagonal boron nitride. *Nat. Commun.* **12**, 3779, doi:10.1038/s41467-021-24019-6 (2021).

887 150 Yücel, O., Ateş, S. & Bek, A. *Single-Photon Nanoantenna with in Situ Fabrication of Plasmonic Ag*
888 *Nanoparticle at an hBN Defect Center*. Preprint at <https://arxiv.org/abs/2003.13824>, (2020).

889 151 Kim, S. *et al.* Photonic crystal cavities from hexagonal boron nitride. *Nat. Commun.* **9**, 2623,
890 doi:10.1038/s41467-018-05117-4 (2018).

891 152 Schell, A. W., Takashima, H., Tran, T. T., Aharonovich, I. & Takeuchi, S. Coupling Quantum Emitters
892 in 2D Materials with Tapered Fibers. *ACS Photonics* **4**, 761-767, doi:10.1021/acsp Photonics.7b00025
893 (2017).

894 153 Liebermeister, L. *et al.* Tapered fiber coupling of single photons emitted by a deterministically
895 positioned single nitrogen vacancy center. *Appl. Phys. Lett.* **104**, 031101, doi:10.1063/1.4862207 (2014).
896 154 Ahn, B.-H. *et al.* Direct fiber-coupled single photon source based on a photonic crystal waveguide. *Appl.*
897 *Phys. Lett.* **107**, 081113, doi:10.1063/1.4929838 (2015).
898 155 Daveau, R. S. *et al.* Efficient fiber-coupled single-photon source based on quantum dots in a photonic-
899 crystal waveguide. *Optica* **4**, 178-184, doi:10.1364/OPTICA.4.000178 (2017).
900 156 Vogl, T., Lecamwasam, R., Buchler, B. C., Lu, Y. & Lam, P. K. Compact Cavity-Enhanced Single-
901 Photon Generation with Hexagonal Boron Nitride. *ACS Photonics* **6**, 1955-1962,
902 doi:10.1021/acsp Photonics.9b00314 (2019).
903 157 Sontheimer, B. *et al.* Photodynamics of quantum emitters in hexagonal boron nitride revealed by low-
904 temperature spectroscopy. *Phys. Rev. B* **96**, 121202, doi:10.1103/PhysRevB.96.121202 (2017).
905 158 Konthasinghe, K. *et al.* Rabi oscillations and resonance fluorescence from a single hexagonal boron
906 nitride quantum emitter. *Optica* **6**, 542-548, doi:10.1364/OPTICA.6.000542 (2019).
907 159 Dietrich, A. *et al.* Observation of Fourier transform limited lines in hexagonal boron nitride. *Phys. Rev.*
908 *B* **98**, 081414, doi:10.1103/PhysRevB.98.081414 (2018).
909 160 Dietrich, A., Doherty, M. W., Aharonovich, I. & Kubanek, A. Solid-state single photon source with
910 Fourier transform limited lines at room temperature. *Phys. Rev. B* **101**, 081401,
911 doi:10.1103/PhysRevB.101.081401 (2020).
912 161 Gottscholl, A. *et al.* Room temperature coherent control of spin defects in hexagonal boron nitride. *Sci.*
913 *Adv.* **7**, eabf3630, doi:10.1126/sciadv.abf3630 (2021).
914 162 Chejanovsky, N. *et al.* Single-spin resonance in a van der Waals embedded paramagnetic defect. *Nat.*
915 *Mater.*, doi:10.1038/s41563-021-00979-4 (2021).
916 163 Yin, K. *et al.* An automated predictor for identifying transition states in solids. *Npj Comput. Mater* **6**, 16,
917 doi:10.1038/s41524-020-0286-9 (2020).
918 164 Ye, M., Seo, H. & Galli, G. Spin coherence in two-dimensional materials. *Npj Comput. Mater* **5**, 44,
919 doi:10.1038/s41524-019-0182-3 (2019).
920 165 White, S. J. U. *et al.* Quantum random number generation using a hexagonal boron nitride single photon
921 emitter. *Journal of Optics* **23**, 01LT01, doi:10.1088/2040-8986/abccff (2020).
922 166 Mudd, G. W. *et al.* The direct-to-indirect band gap crossover in two-dimensional van der Waals Indium
923 Selenide crystals. *Sci. Rep.* **6**, 39619, doi:10.1038/srep39619 (2016).
924 167 Brotons-Gisbert, M. *et al.* Nanotexturing To Enhance Photoluminescent Response of Atomically Thin
925 Indium Selenide with Highly Tunable Band Gap. *Nano Lett.* **16**, 3221-3229,
926 doi:10.1021/acs.nanolett.6b00689 (2016).
927 168 Andres-Penares, D., Cros, A., Martínez-Pastor, J. P. & Sánchez-Royo, J. F. Quantum size confinement
928 in gallium selenide nanosheets: band gap tunability versus stability limitation. *Nanotechnology* **28**,
929 175701, doi:10.1088/1361-6528/aa669e (2017).
930 169 Autere, A. *et al.* Nonlinear Optics with 2D Layered Materials. *Adv. Mater.* **30**, e1705963,
931 doi:10.1002/adma.201705963 (2018).
932 170 Lei, S. *et al.* Synthesis and Photoresponse of Large GaSe Atomic Layers. *Nano Lett.* **13**, 2777-2781,
933 doi:10.1021/nl4010089 (2013).
934 171 Late, D. J. *et al.* GaS and GaSe Ultrathin Layer Transistors. *Adv. Mater.* **24**, 3549-3554,
935 doi:10.1002/adma.201201361 (2012).
936 172 Tonndorf, P. *et al.* Single-photon emitters in GaSe. *2D Mater.* **4**, 021010, doi:10.1088/2053-
937 1583/aa525b (2017).
938 173 Zhao, S. *et al.* Single photon emission from graphene quantum dots at room temperature. *Nat. Commun.*
939 **9**, 3470, doi:10.1038/s41467-018-05888-w (2018).
940 174 Sandeep Kumar, G. *et al.* Amino-functionalized graphene quantum dots: origin of tunable heterogeneous
941 photoluminescence. *Nanoscale* **6**, 3384-3391, doi:10.1039/C3NR05376H (2014).
942 175 Zhao, H., Pettes, M. T., Zheng, Y. & Htoon, H. *Site-Controlled Telecom Single-Photon Emitters in*
943 *Atomically-thin MoTe2*. Preprint at <https://arxiv.org/abs/2105.00576>, (2021).

944 176 Park, Y.-S., Guo, S., Makarov, N. S. & Klimov, V. I. Room Temperature Single-Photon Emission from
945 Individual Perovskite Quantum Dots. *ACS Nano* **9**, 10386-10393, doi:10.1021/acsnano.5b04584 (2015).

946 177 Utzat, H. *et al.* Coherent single-photon emission from colloidal lead halide perovskite quantum dots.
947 *Science* **363**, 1068-1072, doi:10.1126/science.aau7392 (2019).

948 178 Pierini, S. *et al.* Highly Photostable Perovskite Nanocubes: Toward Integrated Single Photon Sources
949 Based on Tapered Nanofibers. *ACS Photonics* **7**, 2265-2272, doi:10.1021/acsp Photonics.0c00820 (2020).

950 179 Gupta, S., Yang, J.-H. & Jakobson, B. I. Two-Level Quantum Systems in Two-Dimensional Materials
951 for Single Photon Emission. *Nano Lett.* **19**, 408-414, doi:10.1021/acs.nanolett.8b04159 (2019).

952 180 Jin, C. *et al.* Observation of moiré excitons in WSe₂/WS₂ heterostructure superlattices. *Nature* **567**, 76-
953 80, doi:10.1038/s41586-019-0976-y (2019).

954 181 Hsu, W.-T. *et al.* Tailoring excitonic states of van der Waals bilayers through stacking configuration,
955 band alignment, and valley spin. *Sci. Adv.* **5**, eaax7407, doi:10.1126/sciadv.aax7407 (2019).

956 182 Liu, E. *et al.* Excitonic and Valley-Polarization Signatures of Fractional Correlated Electronic Phases in
957 a WSe₂/WS₂ Moiré Superlattice. *Phys. Rev. Lett.* **127**, 037402, doi:10.1103/PhysRevLett.127.037402
958 (2021).

959 183 Miao, S. *et al.* Strong interaction between interlayer excitons and correlated electrons in WSe₂/WS₂
960 moiré superlattice. *Nat. Commun.* **12**, 3608, doi:10.1038/s41467-021-23732-6 (2021).

961 184 Wu, F., Lovorn, T. & MacDonald, A. H. Topological Exciton Bands in Moiré Heterojunctions. *Phys.*
962 *Rev. Lett.* **118**, 147401, doi:10.1103/PhysRevLett.118.147401 (2017).

963 185 Tong, Q. *et al.* Topological mosaics in moiré superlattices of van der Waals heterobilayers. *Nat. Phys.*
964 **13**, 356-362, doi:10.1038/nphys3968 (2017).

965 186 Perczel, J. *et al.* Topological Quantum Optics in Two-Dimensional Atomic Arrays. *Phys. Rev. Lett.* **119**,
966 023603, doi:10.1103/PhysRevLett.119.023603 (2017).

967 187 Wang, K. *et al.* Electrical control of charged carriers and excitons in atomically thin materials. *Nat.*
968 *Nanotechnol.* **13**, 128-132, doi:10.1038/s41565-017-0030-x (2018).

969 188 Unuchek, D. *et al.* Room-temperature electrical control of exciton flux in a van der Waals
970 heterostructure. *Nature* **560**, 340-344, doi:10.1038/s41586-018-0357-y (2018).

971 189 Liu, Y. *et al.* Electrically controllable router of interlayer excitons. *Sci. Adv.* **6**, eaba1830,
972 doi:10.1126/sciadv.aba1830 (2020).

973 190 Hu, G. *et al.* A general ink formulation of 2D crystals for wafer-scale inkjet printing. *Sci. Adv.* **6**,
974 eaba5029, doi:10.1126/sciadv.aba5029 (2020).

975 191 Liao, M. *et al.* Precise control of the interlayer twist angle in large scale MoS₂ homostructures. *Nat.*
976 *Commun.* **11**, 2153, doi:10.1038/s41467-020-16056-4 (2020).

977 192 Liu, F. *et al.* Disassembling 2D van der Waals crystals into macroscopic monolayers and reassembling
978 into artificial lattices. *Science* **367**, 903-906, doi:10.1126/science.aba1416 (2020).

979 193 Masubuchi, S. *et al.* Deep-learning-based image segmentation integrated with optical microscopy for
980 automatically searching for two-dimensional materials. *NPJ 2D Mater. and Appl.* **4**, 3,
981 doi:10.1038/s41699-020-0137-z (2020).

982 194 Masubuchi, S. *et al.* Autonomous robotic searching and assembly of two-dimensional crystals to build
983 van der Waals superlattices. *Nat. Commun.* **9**, 1413, doi:10.1038/s41467-018-03723-w (2018).

984 195 Arakawa, Y. & Holmes, M. J. Progress in quantum-dot single photon sources for quantum information
985 technologies: A broad spectrum overview. *Appl. Phys. Rev.* **7**, 021309, doi:10.1063/5.0010193 (2020).

986 196 Fryett, T. K. *et al.* Encapsulated Silicon Nitride Nanobeam Cavity for Hybrid Nanophotonics. *ACS*
987 *Photonics* **5**, 2176-2181, doi:10.1021/acsp Photonics.8b00036 (2018).

988 197 Wang, L., Zhou, X., Yang, S., Huang, G. & Mei, Y. 2D-material-integrated whispering-gallery-mode
989 microcavity. *Photon. Res.* **7**, 905-916, doi:10.1364/PRJ.7.000905 (2019).

990 198 Maiti, R. *et al.* Loss and coupling tuning via heterogeneous integration of MoS₂ layers in silicon
991 photonics. *Opt. Mater. Express* **9**, 751-759, doi:10.1364/OME.9.000751 (2019).

992 199 Shiue, R.-J. *et al.* Active 2D materials for on-chip nanophotonics and quantum optics. *Nanophotonics* **6**,
993 1329, doi:10.1515/nanoph-2016-0172 (2017).

994 200 Fröch, J. E. *et al.* Coupling Hexagonal Boron Nitride Quantum Emitters to Photonic Crystal Cavities. *ACS Nano* **14**, 7085-7091, doi:10.1021/acsnano.0c01818 (2020).

995

996 201 Wu, Y.-C. *et al.* Up- and Down-Conversion between Intra- and Intervalley Excitons in Waveguide

997 Coupled Monolayer WSe₂. *ACS Nano* **14**, 10503-10509, doi:10.1021/acsnano.0c04397 (2020).

998 202 Lee, B. *et al.* Electrical Tuning of Exciton–Plasmon Polariton Coupling in Monolayer MoS₂ Integrated

999 with Plasmonic Nanoantenna Lattice. *Nano Lett.* **17**, 4541-4547, doi:10.1021/acs.nanolett.7b02245

1000 (2017).

1001 203 Iff, O. *et al.* Purcell-Enhanced Single Photon Source Based on a Deterministically Placed WSe₂

1002 Monolayer Quantum Dot in a Circular Bragg Grating Cavity. *Nano Lett.* **21**, 4715-4720,

1003 doi:10.1021/acs.nanolett.1c00978 (2021).

1004 204 Sprengers, J. P. *et al.* Waveguide superconducting single-photon detectors for integrated quantum

1005 photonic circuits. *Appl. Phys. Lett.* **99**, 181110, doi:10.1063/1.3657518 (2011).

1006 205 Münzberg, J. *et al.* Superconducting nanowire single-photon detector implemented in a 2D photonic

1007 crystal cavity. *Optica* **5**, 658-665, doi:10.1364/OPTICA.5.000658 (2018).

1008 206 Najafi, F. *et al.* On-chip detection of non-classical light by scalable integration of single-photon

1009 detectors. *Nat. Commun.* **6**, 5873, doi:10.1038/ncomms6873 (2015).

1010 207 Datta, I. *et al.* Low-loss composite photonic platform based on 2D semiconductor monolayers. *Nat.*

1011 *Photonics* **14**, 256-262, doi:10.1038/s41566-020-0590-4 (2020).

1012 208 Rhodes, D., Chae, S. H., Ribeiro-Palau, R. & Hone, J. Disorder in van der Waals heterostructures of 2D

1013 materials. *Nat. Mater.* **18**, 541-549, doi:10.1038/s41563-019-0366-8 (2019).

1014 209 Ajayi, O. A. *et al.* Approaching the intrinsic photoluminescence linewidth in transition metal

1015 dichalcogenide monolayers. *2D Mater.* **4**, 031011, doi:10.1088/2053-1583/aa6aa1 (2017).

1016 210 Kuhlmann, A. V. *et al.* Charge noise and spin noise in a semiconductor quantum device. *Nat. Phys.* **9**,

1017 570-575, doi:10.1038/nphys2688 (2013).

1018 211 Anderson, C. P. *et al.* Electrical and optical control of single spins integrated in scalable semiconductor

1019 devices. *Science* **366**, 1225-1230, doi:10.1126/science.aax9406 (2019).

1020 212 Edelberg, D. *et al.* Approaching the Intrinsic Limit in Transition Metal Diselenides via Point Defect

1021 Control. *Nano Lett.* **19**, 4371-4379, doi:10.1021/acs.nanolett.9b00985 (2019).

1022 213 Press, D. *et al.* Ultrafast optical spin echo in a single quantum dot. *Nat. Photonics* **4**, 367-370,

1023 doi:10.1038/nphoton.2010.83 (2010).

1024 214 Gilardoni, C. M. *et al.* Spin-relaxation times exceeding seconds for color centers with strong spin–orbit

1025 coupling in SiC. *New J. Phys.* **22**, 103051, doi:10.1088/1367-2630/abbf23 (2020).

1026 215 Seo, H. *et al.* Quantum decoherence dynamics of divacancy spins in silicon carbide. *Nat. Commun.* **7**,

1027 12935, doi:10.1038/ncomms12935 (2016).

1028 216 Benson, O., Santori, C., Pelton, M. & Yamamoto, Y. Regulated and Entangled Photons from a Single

1029 Quantum Dot. *Phys. Rev. Lett.* **84**, 2513-2516, doi:10.1103/PhysRevLett.84.2513 (2000).

1030 217 Akopian, N. *et al.* Entangled Photon Pairs from Semiconductor Quantum Dots. *Phys. Rev. Lett.* **96**,

1031 130501, doi:10.1103/PhysRevLett.96.130501 (2006).

1032 218 Winik, R. *et al.* On-demand source of maximally entangled photon pairs using the biexciton-exciton

1033 radiative cascade. *Phys. Rev. B* **95**, 235435, doi:10.1103/PhysRevB.95.235435 (2017).

1034 219 Dinparasti Saleh, H. *et al.* Towards spontaneous parametric down conversion from monolayer MoS₂.

1035 *Sci. Rep.* **8**, 3862, doi:10.1038/s41598-018-22270-4 (2018).

1036 220 Marini, L., Helt, L. G., Lu, Y., Eggleton, B. J. & Palomba, S. Constraints on downconversion in

1037 atomically thick films. *J. Opt. Soc. Am. B* **35**, 672, doi:10.1364/josab.35.000672 (2018).

1038 221 Lee, K. F. *et al.* Photon-Pair Generation with a 100 nm Thick Carbon Nanotube Film. *Adv. Mater.* **29**,

1039 1605978, doi:10.1002/adma.201605978 (2017).

1040 222 Okoth, C., Cavanna, A., Santiago-Cruz, T. & Chekhova, M. V. Microscale Generation of Entangled

1041 Photons without Momentum Conservation. *Phys. Rev. Lett.* **123**, 263602,

1042 doi:10.1103/PhysRevLett.123.263602 (2019).

1043 223 Santiago-Cruz, T., Sultanov, V., Zhang, H., Krivitsky, L. A. & Chekhova, M. V. Entangled photons

1044 from subwavelength nonlinear films. *Opt. Lett.* **46**, 653-656, doi:10.1364/OL.411176 (2021).

- 1045 224 Wang, Y. *et al.* Difference frequency generation in monolayer MoS₂. *Nanoscale* **12**, 19638-19643,
1046 doi:10.1039/D0NR01994A (2020).
- 1047 225 Yao, K. *et al.* Enhanced tunable second harmonic generation from twistable interfaces and vertical
1048 superlattices in boron nitride homostructures. *Sci. Adv.* **7**, eabe8691, doi:10.1126/sciadv.abe8691 (2021).
- 1049 226 Yang, F. *et al.* Tunable Second Harmonic Generation in Twisted Bilayer Graphene. *Matter* **3**, 1361-
1050 1376, doi:10.1016/j.matt.2020.08.018 (2020).
- 1051 227 Du, L., Dai, Y. & Sun, Z. Twisting for Tunable Nonlinear Optics. *Matter* **3**, 987-988,
1052 doi:10.1016/j.matt.2020.09.013 (2020).
- 1053 228 Alexander, K., Savostianova, N. A., Mikhailov, S. A., Kuyken, B. & Van Thourhout, D. Electrically
1054 Tunable Optical Nonlinearities in Graphene-Covered SiN Waveguides Characterized by Four-Wave
1055 Mixing. *ACS Photonics* **4**, 3039-3044, doi:10.1021/acsp Photonics.7b00559 (2017).
- 1056 229 Jiang, T. *et al.* Gate-tunable third-order nonlinear optical response of massless Dirac fermions in
1057 graphene. *Nat. Photonics* **12**, 430-436, doi:10.1038/s41566-018-0175-7 (2018).
- 1058 230 Soavi, G. *et al.* Broadband, electrically tunable third-harmonic generation in graphene. *Nat.*
1059 *Nanotechnol.* **13**, 583-588, doi:10.1038/s41565-018-0145-8 (2018).
- 1060 231 Dai, Y. *et al.* Electrical Control of Interband Resonant Nonlinear Optics in Monolayer MoS₂. *ACS Nano*
1061 **14**, 8442-8448, doi:10.1021/acsnano.0c02642 (2020).
- 1062 232 Seyler, K. L. *et al.* Electrical control of second-harmonic generation in a WSe₂ monolayer transistor.
1063 *Nat. Nanotechnol.* **10**, 407-411, doi:10.1038/nnano.2015.73 (2015).
- 1064 233 Sun, Z. Electrically tuned nonlinearity. *Nat. Photonics* **12**, 383-385, doi:10.1038/s41566-018-0201-9
1065 (2018).
- 1066 234 Bogusławski, J. *et al.* Graphene Actively Mode- Locked Lasers. *Advanced Functional Materials* **28**,
1067 1801539, doi:10.1002/adfm.201801539 (2018).
- 1068 235 Scully, M. O. & Zubairy, M. S. *Quantum optics*. (Cambridge University Press, 1997).
- 1069 236 Chen, K. *et al.* Graphene photonic crystal fibre with strong and tunable light-matter interaction. *Nat.*
1070 *Photonics* **13**, 754-759, doi:10.1038/s41566-019-0492-5 (2019).
- 1071 237 Zuo, Y. *et al.* Optical fibres with embedded two-dimensional materials for ultrahigh nonlinearity. *Nat.*
1072 *Nanotechnol.*, doi:10.1038/s41565-020-0770-x (2020).
- 1073 238 Jiang, B. *et al.* High-efficiency second-order nonlinear processes in an optical microfiber assisted by
1074 few-layer GaSe. *Light Sci. Appl.* **9**, 63, doi:10.1038/s41377-020-0304-1 (2020).
- 1075 239 Gan, X.-T. *et al.* Microwatts continuous-wave pumped second harmonic generation in few- and mono-
1076 layer GaSe. *Light Sci. Appl.* **7**, 17126-17126, doi:10.1038/lsa.2017.126 (2018).
- 1077 240 Marino, G. *et al.* Spontaneous photon-pair generation from a dielectric nanoantenna. *Optica* **6**, 1416-
1078 1422, doi:10.1364/OPTICA.6.001416 (2019).
- 1079 241 Bernhardt, N. *et al.* Quasi-BIC Resonant Enhancement of Second-Harmonic Generation in WS₂
1080 Monolayers. *Nano Lett.* **20**, 5309-5314, doi:10.1021/acsnanolett.0c01603 (2020).
- 1081 242 Wang, G. *et al.* Giant Enhancement of the Optical Second-Harmonic Emission of WSe₂ Monolayers by
1082 Laser Excitation at Exciton Resonances. *Phys. Rev. Lett.* **114**, 097403,
1083 doi:10.1103/PhysRevLett.114.097403 (2015).
- 1084 243 Guo, X. *et al.* Efficient All-Optical Plasmonic Modulators with Atomically Thin Van Der Waals
1085 Heterostructures. *Adv. Mater.* **32**, 1907105, doi:10.1002/adma.201907105 (2020).
- 1086 244 Du, L. *et al.* Strong and tunable interlayer coupling of infrared-active phonons to excitons in van der
1087 Waals heterostructures. *Phys. Rev. B* **99**, 205410, doi:10.1103/PhysRevB.99.205410 (2019).
- 1088 245 Yang, X. *et al.* Far-Field Spectroscopy and Near-Field Optical Imaging of Coupled Plasmon-Phonon
1089 Polaritons in 2D van der Waals Heterostructures. *Adv. Mater.* **28**, 2931-2938,
1090 doi:10.1002/adma.201505765 (2016).
- 1091 246 Back, P., Zeytinoglu, S., Ijaz, A., Kroner, M. & Imamoğlu, A. Realization of an Electrically Tunable
1092 Narrow-Bandwidth Atomically Thin Mirror Using Monolayer MoSe₂. *Phys. Rev. Lett.* **120**, 037401,
1093 doi:10.1103/PhysRevLett.120.037401 (2018).
- 1094 247 Scuri, G. *et al.* Large Excitonic Reflectivity of Monolayer MoSe₂ Encapsulated in Hexagonal Boron
1095 Nitride. *Phys. Rev. Lett.* **120**, 037402, doi:10.1103/PhysRevLett.120.037402 (2018).

1096 248 Wild, D. S., Shahmoon, E., Yelin, S. F. & Lukin, M. D. Quantum Nonlinear Optics in Atomically Thin
1097 Materials. *Phys. Rev. Lett.* **121**, 123606, doi:10.1103/PhysRevLett.121.123606 (2018).

1098 249 Zhou, Y. *et al.* Controlling Excitons in an Atomically Thin Membrane with a Mirror. *Phys. Rev. Lett.*
1099 **124**, 027401, doi:10.1103/PhysRevLett.124.027401 (2020).

1100 250 Horng, J. *et al.* Perfect Absorption by an Atomically Thin Crystal. *Phys. Rev. Appl.* **14**, 024009,
1101 doi:10.1103/PhysRevApplied.14.024009 (2020).

1102 251 Zeytinoğlu, S. & İmamoğlu, A. Interaction-induced photon blockade using an atomically thin mirror
1103 embedded in a microcavity. *Phys. Rev. A* **98**, 051801, doi:10.1103/PhysRevA.98.051801 (2018).

1104 252 Wang, Y., Jöns, K. D. & Sun, Z. Integrated photon-pair sources with nonlinear optics. *Appl. Phys. Rev.*
1105 **8**, 011314, doi:10.1063/5.0030258 (2021).

1106 253 Gullans, M., Chang, D. E., Koppens, F. H., Garcia de Abajo, F. J. & Lukin, M. D. Single-photon
1107 nonlinear optics with graphene plasmons. *Phys. Rev. Lett.* **111**, 247401,
1108 doi:10.1103/PhysRevLett.111.247401 (2013).

1109 254 Chai, Z. *et al.* Ultrafast All-Optical Switching. *Adv. Opt. Mater.* **5**, 1600665,
1110 doi:10.1002/adom.201600665 (2017).

1111 255 Jablan, M. & Chang, D. E. Multiplasmon Absorption in Graphene. *Phys. Rev. Lett.* **114**, 236801,
1112 doi:10.1103/PhysRevLett.114.236801 (2015).

1113 256 Sun, L. & Jiang, C. Electrically controllable single-photon switch based on graphene. *Appl. Opt.* **54**,
1114 5650-5656, doi:10.1364/AO.54.005650 (2015).

1115 257 Gong, C. & Zhang, X. Two-dimensional magnetic crystals and emergent heterostructure devices.
1116 *Science* **363**, eaav4450, doi:10.1126/science.aav4450 (2019).

1117 258 Fritz, L. & Vojta, M. The physics of Kondo impurities in graphene. *Rep. Prog. Phys.* **76**, 032501,
1118 doi:10.1088/0034-4885/76/3/032501 (2013).

1119 259 Michler, P. *et al.* A Quantum Dot Single-Photon Turnstile Device. *Science* **290**, 2282-2285,
1120 doi:10.1126/science.290.5500.2282 (2000).

1121 260 Gérard, J. M. *et al.* Enhanced Spontaneous Emission by Quantum Boxes in a Monolithic Optical
1122 Microcavity. *Phys. Rev. Lett.* **81**, 1110-1113, doi:10.1103/PhysRevLett.81.1110 (1998).

1123 261 Moreau, E. *et al.* Single-mode solid-state single photon source based on isolated quantum dots in pillar
1124 microcavities. *Appl. Phys. Lett.* **79**, 2865-2867, doi:10.1063/1.1415346 (2001).

1125 262 Santori, C., Fattal, D., Vučković, J., Solomon, G. S. & Yamamoto, Y. Indistinguishable photons from a
1126 single-photon device. *Nature* **419**, 594-597, doi:10.1038/nature01086 (2002).

1127 263 Baier, M. H. *et al.* Single photon emission from site-controlled pyramidal quantum dots. *Appl. Phys.*
1128 *Lett.* **84**, 648-650, doi:10.1063/1.1643533 (2004).

1129 264 Muller, A. *et al.* Resonance Fluorescence from a Coherently Driven Semiconductor Quantum Dot in a
1130 Cavity. *Phys. Rev. Lett.* **99**, 187402, doi:10.1103/PhysRevLett.99.187402 (2007).

1131 265 Press, D., Ladd, T. D., Zhang, B. & Yamamoto, Y. Complete quantum control of a single quantum dot
1132 spin using ultrafast optical pulses. *Nature* **456**, 218-221, doi:10.1038/nature07530 (2008).

1133 266 Faraon, A. *et al.* Integrated quantum optical networks based on quantum dots and photonic crystals. *New*
1134 *J. Phys.* **13**, 055025, doi:10.1088/1367-2630/13/5/055025 (2011).

1135 267 Moreau, E. *et al.* Quantum Cascade of Photons in Semiconductor Quantum Dots. *Phys. Rev. Lett.* **87**,
1136 183601, doi:10.1103/PhysRevLett.87.183601 (2001).

1137 268 Regelman, D. V. *et al.* Semiconductor Quantum Dot: A Quantum Light Source of Multicolor Photons
1138 with Tunable Statistics. *Phys. Rev. Lett.* **87**, 257401, doi:10.1103/PhysRevLett.87.257401 (2001).

1139 269 Warburton, R. J. *et al.* Optical emission from a charge-tunable quantum ring. *Nature* **405**, 926-929,
1140 doi:10.1038/35016030 (2000).

1141 270 Brouri, R., Beveratos, A., Poizat, J.-P. & Grangier, P. Photon antibunching in the fluorescence of
1142 individual color centers in diamond. *Opt. Lett.* **25**, 1294-1296, doi:10.1364/OL.25.001294 (2000).

1143 271 Meijer, J. *et al.* Generation of single color centers by focused nitrogen implantation. *Appl. Phys. Lett.* **87**,
1144 261909, doi:10.1063/1.2103389 (2005).

1145 272 Batalov, A. *et al.* Temporal Coherence of Photons Emitted by Single Nitrogen-Vacancy Defect Centers
1146 in Diamond Using Optical Rabi-Oscillations. *Phys. Rev. Lett.* **100**, 077401,
1147 doi:10.1103/PhysRevLett.100.077401 (2008).

1148 273 Robledo, L., Bernien, H., van Weperen, I. & Hanson, R. Control and Coherence of the Optical
1149 Transition of Single Nitrogen Vacancy Centers in Diamond. *Phys. Rev. Lett.* **105**, 177403,
1150 doi:10.1103/PhysRevLett.105.177403 (2010).

1151 274 Englund, D. *et al.* Deterministic Coupling of a Single Nitrogen Vacancy Center to a Photonic Crystal
1152 Cavity. *Nano Lett.* **10**, 3922-3926, doi:10.1021/nl101662v (2010).

1153 275 Bernien, H. *et al.* Heralded entanglement between solid-state qubits separated by three metres. *Nature*
1154 **497**, 86-90, doi:10.1038/nature12016 (2013).

1155 276 Togan, E., Chu, Y., Imamoglu, A. & Lukin, M. D. Laser cooling and real-time measurement of the
1156 nuclear spin environment of a solid-state qubit. *Nature* **478**, 497-501, doi:10.1038/nature10528 (2011).

1157 277 Hausmann, B. J. M. *et al.* Integrated Diamond Networks for Quantum Nanophotonics. *Nano Lett.* **12**,
1158 1578-1582, doi:10.1021/nl204449n (2012).

1159 278 Chejanovsky, N. *et al.* Quantum Light in Curved Low Dimensional Hexagonal Boron Nitride Systems.
1160 *Sci. Rep.* **7**, 14758, doi:10.1038/s41598-017-15398-2 (2017).

1161 279 Mahan, G. D. *Many-Particle Physics*. (Plenum, 1993).

1162 280 Efetov, D. K. & Kim, P. Controlling Electron-Phonon Interactions in Graphene at Ultrahigh Carrier
1163 Densities. *Phys. Rev. Lett.* **105**, 256805, doi:10.1103/PhysRevLett.105.256805 (2010).

1164 281 Chen, J.-H., Jang, C., Xiao, S., Ishigami, M. & Fuhrer, M. S. Intrinsic and extrinsic performance limits
1165 of graphene devices on SiO₂. *Nat. Nanotechnol.* **3**, 206, doi:10.1038/nnano.2008.58 (2008).

1166 282 Shree, S. *et al.* Observation of exciton-phonon coupling in MoSe₂ monolayers. *Phys. Rev. B* **98**, 035302,
1167 doi:10.1103/PhysRevB.98.035302 (2018).

1168 283 Vuong, T. Q. P. *et al.* Phonon-Photon Mapping in a Color Center in Hexagonal Boron Nitride. *Phys.*
1169 *Rev. Lett.* **117**, 097402, doi:10.1103/PhysRevLett.117.097402 (2016).

1170 284 Kaasbjerg, K., Thygesen, K. S. & Jacobsen, K. W. Phonon-limited mobility in n-type single-layer MoS₂
1171 from first principles. *Phys. Rev. B* **85**, 115317, doi:10.1103/PhysRevB.85.115317 (2012).

1172 285 Urbaszek, B. *et al.* Nuclear spin physics in quantum dots: An optical investigation. *Rev. Mod. Phys.* **85**,
1173 79-133, doi:10.1103/RevModPhys.85.79 (2013).

1174 286 Hong, J. *et al.* Exploring atomic defects in molybdenum disulphide monolayers. *Nat. Commun.* **6**, 6293,
1175 doi:10.1038/ncomms7293 (2015).

1176 287 Hu, Z. *et al.* Two-dimensional transition metal dichalcogenides: interface and defect engineering. *Chem.*
1177 *Soc. Rev.* **47**, 3100-3128, doi:10.1039/C8CS00024G (2018).

1178 288 Lin, Y.-C. *et al.* Three-fold rotational defects in two-dimensional transition metal dichalcogenides. *Nat.*
1179 *Commun.* **6**, 6736, doi:10.1038/ncomms7736 (2015).

1180 289 Zhou, W. *et al.* Intrinsic Structural Defects in Monolayer Molybdenum Disulfide. *Nano Lett.* **13**, 2615-
1181 2622, doi:10.1021/nl4007479 (2013).

1182 290 Davanco, M. *et al.* Heterogeneous integration for on-chip quantum photonic circuits with single
1183 quantum dot devices. *Nat. Commun.* **8**, 889, doi:10.1038/s41467-017-00987-6 (2017).

1184 291 Elshaari, A. W. *et al.* On-chip single photon filtering and multiplexing in hybrid quantum photonic
1185 circuits. *Nat. Commun.* **8**, 379, doi:10.1038/s41467-017-00486-8 (2017).

1186 292 Katsumi, R., Ota, Y., Kakuda, M., Iwamoto, S. & Arakawa, Y. Transfer-printed single-photon sources
1187 coupled to wire waveguides. *Optica* **5**, 691-694, doi:10.1364/OPTICA.5.000691 (2018).

1188 293 Kim, J.-H. *et al.* Hybrid Integration of Solid-State Quantum Emitters on a Silicon Photonic Chip. *Nano*
1189 *Lett.* **17**, 7394-7400, doi:10.1021/acs.nanolett.7b03220 (2017).

1190 294 Lombardi, P. *et al.* Photostable Molecules on Chip: Integrated Sources of Nonclassical Light. *ACS*
1191 *Photonics* **5**, 126-132, doi:10.1021/acsp Photonics.7b00521 (2018).

1192 295 Mouradian, S. L. *et al.* Scalable Integration of Long-Lived Quantum Memories into a Photonic Circuit.
1193 *Phys. Rev. X* **5**, 031009, doi:10.1103/PhysRevX.5.031009 (2015).

1194 296 Zadeh, I. E. *et al.* Deterministic Integration of Single Photon Sources in Silicon Based Photonic Circuits.
1195 *Nano Lett.* **16**, 2289-2294, doi:10.1021/acs.nanolett.5b04709 (2016).

1196 297 Khasminskaya, S. *et al.* Fully integrated quantum photonic circuit with an electrically driven light
 1197 source. *Nat. Photonics* **10**, 727, doi:10.1038/nphoton.2016.178 (2016).
 1198 298 Schuck, C. *et al.* Quantum interference in heterogeneous superconducting-photonic circuits on a silicon
 1199 chip. *Nat. Commun.* **7**, 10352, doi:10.1038/ncomms10352 (2016).
 1200 299 Bogdanov, S., Shalaginov, M. Y., Boltasseva, A. & Shalaev, V. M. Material platforms for integrated
 1201 quantum photonics. *Opt. Mater. Express* **7**, 111-132, doi:10.1364/OME.7.000111 (2017).
 1202 300 Poot, M., Schuck, C., Ma, X.-s., Guo, X. & Tang, H. X. Design and characterization of integrated
 1203 components for SiN photonic quantum circuits. *Opt. Expr.* **24**, 6843-6860, doi:10.1364/OE.24.006843
 1204 (2016).
 1205 301 Lu, T.-J. *et al.* Aluminum nitride integrated photonics platform for the ultraviolet to visible spectrum.
 1206 *Opt. Expr.* **26**, 11147-11160, doi:10.1364/OE.26.011147 (2018).
 1207 302 Desiatov, B., Shams-Ansari, A., Zhang, M., Wang, C. & Lončar, M. Ultra-low-loss integrated visible
 1208 photonics using thin-film lithium niobate. *Optica* **6**, 380-384, doi:10.1364/OPTICA.6.000380 (2019).

1209

1210 **Small Print**

1211 **Acknowledgement**

1212 The authors acknowledge funding from the European Union's Horizon 2020 research and innovation programme
 1213 (Grant No. 820423, 862721 and 965124), the ERC (no. 725920), the Academy of Finland (Grants Nos. 314810,
 1214 333982, 336144 and 336818), Aalto Centre of Quantum Engineering, the China Scholarship Council, the
 1215 EPSRC (EP/P029892/1; EP/S000550/1; EP/S000550/1); and the Leverhulme Trust (RPG-2019-388). M.B.-G.
 1216 thanks the Royal Society for a University Research Fellowship. B.D.G. was supported by a Wolfson Merit
 1217 Award from the Royal Society and a Chair in Emerging Technology from the Royal Academy of Engineering.
 1218 Z.S. thanks other Aalto group members who initiated the review's writing that later was completely led by
 1219 B.D.G.

1220

1221

Author contributions

The authors contributed equally to all aspects of the article.

1222

1223

Competing interests

The authors declare no competing interests.

1224

1225

Peer review information

Nature Reviews Physics thanks Weibo Gao, Christian Schneider and Milos Toth for their contribution to the peer review of this work.

1226

1227

Supplementary information

Supplementary information is available for this paper at <https://doi.org/10.1038/s415XX-XXX-XXXX-X>

1228

1229

1230

Key points

1231

1232

- 2D materials host quantum emitters with strong light-matter interaction that can be integrated into on-chip devices.

1233

1234

- Some 2D quantum emitters have an intrinsic spin-degree of freedom that can be harnessed for spin-photon entanglement.

1235

1236

- The ease with which 2D materials can be transferred onto photonic circuits to create hybrid devices provides new opportunities for scalable quantum photonic devices.

1237

1238

- While quantum emitters in several 2D materials have been successfully identified, there remain challenges to building functional quantum technologies.

1239

1240

1241 **Display Items**

1242
1243
1244
1245
1246
1247
1248
1249
1250
1251
1252
1253
1254
1255
1256
1257
1258
1259

Figures

Figure 1: Single photon emitters (SPEs) in WSe₂. (a) Photoluminescence (PL) spectrum of SPEs in monolayer WSe₂. Left inset shows the localized emission with fine-structure splitting (FSS) and right inset shows the higher energy free exciton emission. (b) The polarization-dependent PL spectra (normalized) from bi-exciton (XX⁰) and exciton (X⁰) of a single SPE in WSe₂. The FSS and the out-of-phase orthogonal linear polarisations of the XX⁰ and X⁰ can be observed. (c) An optical micrograph (left) of WSe₂ with mono and bi-layer regions placed onto an array of nanopillars. A 2D spatial map of the integrated PL intensity reveals enhanced emission at the location of the nanopillars due to SPEs (right). The SPEs are brightest in the monolayer regions. (d) A schematic of atomically thin WSe₂ deformed by a nanopillar to achieve a point-like elastic strain perturbation (top), where the strain locally modulates the exciton energy (bottom). Optically created excitons can efficiently funnel to an individual strain tuned localized exciton trap (due to disorder or point defect) at the nanopillar centre resulting in a single highly efficient quantum emitter. (e) A reciprocal space schematic of ‘dark’ strain-localized exciton states (dashed lines) which hybridize with a point defect (horizontal cyan line), breaking the valley selectivity to lead to efficient photoemission (dark blue and yellow arrows). K and K' indicate the WSe₂ valleys, $|c_k\rangle$ and $|c_{k'}\rangle$ ($|v_k\rangle$ and $|v_{k'}\rangle$) are strain-localised electronic excitations originating from the conduction band (valence band) in each valley, and $|d_{\uparrow,\downarrow}\rangle$ refer to defect states and their spin degree of freedom. Panel a adapted with permission from REF. ¹⁰. Panel b adapted with permission from REF. ⁷³. Panels c and d adapted with permission from REF. ¹⁷. Panel e adapted with permission from REF. ⁷¹.

1260
1261
1262
1263
1264
1265
1266
1267
1268
1269
1270
1271
1272
1273
1274
1275
1276
1277
1278
1279

Figure 2: WSe₂ single photon emitters (SPEs) in heterostructure devices. (a) An optical microscope image of a transition metal dichalcogenide (TMD) based single photon LED. The dotted lines highlight the footprint of the single layer graphene (SLG), hBN and the TMD layers individually. The Cr/Au electrodes contact the graphene and TMD layers to provide an electrical bias. (b) Heterostructure band diagram, illustrating the case for zero-applied bias (top) and the case for a finite negative bias applied to the graphene (bottom). Tuning the graphene Fermi level across the TMD conduction band edge (E_C) allows electron tunnelling from the graphene layer to the TMD, resulting in light emission via radiative recombination of the electrons with the holes residing in the p-doped TMD layer. The appearance of valence-band holes below the Fermi level is due to the natural p-doping of WSe₂. (c) An example of layered LED emission spectra (PL, photoluminescence; EL, electroluminescence, L identifies the localised exciton emission), for an optically active layer of WSe₂. Top (bottom) spectra correspond to 10 K (room temperature (RT)) operation, where the black and blue spectra are obtained by optical excitation and electrical excitation, respectively. (d) Sketch of a charge-tunable WSe₂ SPE device. (e) Schematic representation of the electron (filled circles) and hole (open circles) tunnelling through the hBN barrier from the Fermi reservoir in the graphene to the quantum dots in WSe₂. (f) Coulomb blockade in a WSe₂ SPE shows voltage control of the charge state. The diagram in the inset represents the energy levels and occupation of the electrons and holes for the pure X¹⁻, X⁰ and X¹⁺ exciton states of the WSe₂ SPE. CB, conduction band; VB, valence band; E_g , energy band gap; U_{ee} (U_{hh}), electron–electron (hole–hole) Coulomb interaction energy; QD, quantum dot. Panels a, b and c adapted with permission from REF. ³¹. Panels d, e and f adapted with permission from REF. ³².

1280
1281
1282
1283
1284

Figure 3. Moiré heterostructure based single photon emitters (SPEs). (a) Illustration of the long-period moiré superlattice formed in a transition metal dichalcogenide (TMD) heterobilayer with R-type stacking. The green diamond represents a moiré supercell. Insets are close-ups of three trapping sites (A, B, and C) with the corresponding atomic registries (R_h^h , R_h^X and R_h^M , respectively). (b) Schematic illustration of the polarisation selection rules, for K-valley interlayer excitons trapped at A, B and C trapping sites, respectively, for singlet (top

1285 panel) and triplet (bottom panel) spin configurations. **(c)** Magnetic-field-dependent photoluminescence (PL)
 1286 from interlayer excitons in an MoSe₂/WSe₂ heterobilayer with twist angles of 57° (left) and 2° (right). The top
 1287 panel shows helicity-resolved PL spectra at 3 T. The excitation is linearly polarized, and the σ^+ and σ^-
 1288 components of the PL are shown in red and blue, respectively. The bottom panels show plots of the total PL
 1289 intensity as a function of the magnetic field, showing a linear Zeeman shift of the σ^+ and σ^- polarized PL. **(d)**
 1290 Second-order photon correlation statistics of a moiré-trapped IX in a MoSe₂/WSe₂ heterobilayer, showing clear
 1291 antibunching. **(e)** PL spectra of moiré-trapped IXs in a MoSe₂/WSe₂ heterobilayer embedded in a dual gate
 1292 device for different applied electric fields, showing an energy tuning of ~ 40 meV. **(f)** Left: PL spectrum of
 1293 moiré-trapped IXs in a MoSe₂/WSe₂ heterobilayer as a function of the applied gate voltage (V_g). The prominent
 1294 IX emission peaks are labelled as A-H in each doping region. The dashed lines identify the V_g of the linecuts in
 1295 the right panel. Right panel: Representative PL spectra for trapped IX⁰, IX⁻, and IX⁺. For direct comparison with
 1296 IX⁰ PL spectrum, the IX⁻ (IX⁺) PL spectra are shifted by 6.5 (6) meV in relative photon energy. Panel a adapted
 1297 with permission from REF. ³⁴. Panel b adapted with permission from REF. ¹³⁰. Panel c adapted with permission
 1298 from REF. ³⁵. Panels d and e adapted with permission from REF. ¹²⁸. Panel f adapted with permission from Ref.
 1299 ¹³².

1300
 1301 **Figure 4. hBN based single photon emitters (SPEs).** **(a).** Photoluminescence (PL) spectra of different SPEs in
 1302 hBN **(b)** Illustration of the N_BV_N and C_BV_N crystalline defects. **(c)** Left: A schematic of a tunable plano-concave
 1303 optical microcavity. Right: A second-order correlation function, g^2 , of cavity-coupled and a free-space SPE in
 1304 hBN. **(d)** Room temperature optically detected magnetic resonance frequencies from a negatively charged boron
 1305 vacancy defect in hBN as a function of the magnetic field. Panel a adapted with permission from REF. ¹³⁸. Panel
 1306 b adapted with permission from REFS. ^{14,144}. Panel c adapted with permission from REF ¹⁵⁶. Panel d adapted with
 1307 permission from REF ⁷⁰.

1308
 1309 **Figure 5.** A development timeline of quantum photonics platforms including QDs,^{51,53,259-269} NV centers in
 1310 diamond,²⁷⁰⁻²⁷⁷ WSe₂,^{9-13,17,30,76,101} hBN,^{14,30,32,73-75,151,158,161,278} Moiré^{119,128,131-133}, MoS₂,⁹³ MoSe₂,⁸² and MoTe₂.¹⁷⁵

1311

1312 **Boxes**

1313

1314 **Box 1: Intrinsic solid-state decoherence mechanisms**

1315

1316 **Electron-phonon interactions:** Localized carriers in solid-state emitters interact with a many-body
 1317 environment, leading to non-trivial modifications of the emitter's properties. The interaction of the trapped
 1318 carrier with the surrounding lattice ions causes displacements of the latter from their equilibrium position, which
 1319 in turn leads to absorption or emission of phonons (panel a). The equilibrium position of the crystal lattice
 1320 depends on the local charge state due to the deformation potential and electron-phonon interaction. The two
 1321 main contributions to the electron-phonon interaction are the deformation potential and the piezoelectric
 1322 coupling to the long-wavelength acoustic phonons. A third type of electron-phonon coupling relevant for
 1323 semiconductors is the polar coupling to longitudinal optical phonons, which give rise to a dipole polarisation
 1324 field that interacts with the charge-carrier via the Fröhlich Hamiltonian²⁷⁹. These interactions affect several
 1325 properties of 2D materials, including charge carrier mobility²⁸⁰, resistivity²⁸¹, photon linewidth and lineshape
 1326 dependence, and a temperature-dependent fraction of the photons emitted incoherently via the phonon
 1327 sideband^{282,283}.

1328

1329 **Electron-nuclear spin interactions:** Despite the atomic thickness of 2D materials, the finite effective width of
1330 the exciton wavefunction along the axis perpendicular to the plane results not only in the Fröhlich interaction²⁸⁴,
1331 but also in non-vanishing Fermi contact and dipole-dipole interactions between the trapped charge-carrier and
1332 the surrounding nuclei (panel b; red oval represents the wavefunction of trapped charge). A charge can be
1333 trapped (wavefunction represented by red oval) at the nanoscale due to intrinsic or extrinsic defects, such as
1334 transition metal or chalcogen vacancies (empty circles in the lattice) or dangling bonds in the substrate
1335 (represented by loops with positive charges), respectively. The localized wavefunction might extend across
1336 several lattice sites and into the encapsulating hBN layers, resulting in hyperfine interactions between the
1337 electron and encapsulating and substrate nuclei (depicted by randomly oriented arrows). The interactions of the
1338 entire nuclear ensemble with the trapped electron result in a fluctuating effective magnetic field, further limiting
1339 the coherence time of the central spin²⁸⁵. This fluctuating field can vary considerably from one material to
1340 another. Furthermore, adatoms, substitutional vacancies, and defects such as metal or chalcogen vacancies
1341 (which are abundant in TMDs²⁸⁶⁻²⁸⁹) provide a rich source of electronic spins that interact with the trapped
1342 charge carrier via the hyperfine interaction, resulting in an additional source of decoherence.

1343

1344

1345

1346 **Box 2: Cavity integration and hybrid quantum photonic chips**

1347

1348 **Cavity Integration:** Optical microcavities are devices capable of enhancing the light-matter interaction by
1349 concentrating the electromagnetic field at optical frequencies into sub-wavelength volumes. The inset in the
1350 figure shows a schematic of a single photon emitter (SPE) coupled to a cavity: a two-level emitter embedded
1351 inside an optical micro-resonator with optical losses κ couples to the optical mode of the cavity with a coupling
1352 strength g . As a result of the interaction, the emitter radiates with an enhanced spontaneous emission rate $\gamma_c =$
1353 $F_p \gamma_{sp}$, where γ_{sp} is the intrinsic spontaneous emission rate of the emitter and F_p is the Purcell factor, which is
1354 inversely proportional to the volume of the optical cavity mode, V . Finally, the spontaneous emission coupling
1355 factor (β) quantifies the fraction of the light emitted that is coupled into the cavity mode ($\beta = F_p / (F_p + 1)$).

1356 The atomically-thin nature of the host crystals for 2D-based SPEs allows the integration of the SPEs with a
1357 large variety of optical cavity architectures with different properties (panel a). From left to right: engineered
1358 substrate, distributed-Bragg-reflector cavity, open dielectric cavity, plasmonic cavity, ridge waveguide, and a
1359 photonic crystal nanobeam. The colour bars show a qualitative comparison of the mode volume (V), Purcell
1360 enhancement factor (F_p), and spontaneous emission coupling factor (β) for each type of cavity. The integration
1361 of 2D SPEs in optical cavities offers potential to mitigate two of the main challenges of these emitters: SPE
1362 coherence and brightness. The enhanced radiative emission rate via the Purcell effect could simultaneously
1363 increase the photon brightness and enhance the spontaneous emission rate above the rate of dephasing processes
1364 responsible of the low coherence of these SPEs.

1365

1366 **Quantum Photonic Integrated Circuits:** For scalability reasons, most applications in quantum photonics
1367 require an on-chip solution where all components of the device are integrated on a photonic circuit (panel b).
1368 The functionality of a photonic circuit and its performance can be reconfigured using electric contacts (gold) to
1369 control active elements (like tunable ring resonators and modulators). After different gate operations and routing,
1370 the photons are detected using on-chip single-photon detectors (on the far right). Fundamental building blocks
1371 for quantum photonic circuits are quantum light sources, photonic circuits, and single photon detectors. Finding
1372 a single material platform where all building blocks are monolithically integrated with state-of-the-art

1373 performance of each component remains challenging. Another route is to take a well-developed circuit platform,
1374 such as silicon-based photonics, and deterministically integrate quantum emitters using a transfer method²⁹⁰⁻²⁹⁶
1375 Such a heterogeneous approach enables the integration of all required building blocks on a single chip^{297,298}, and
1376 perfectly matches with the pick and place exfoliation technique used for 2D materials. After a monolayer is
1377 isolated on a transfer stamp, it can be precisely placed on a photonic circuit, and first steps have already been
1378 taken^{26-30,110}. Given the hybrid approach, there is no restriction on which material platform can be used. Different
1379 platforms offer different advantages and challenges, and an overview can be found in Ref.²⁹⁹. Current preferred
1380 choices are SiN³⁰⁰, AlN³⁰¹, and LiNbO₃³⁰².

1381

1382

1383

1384

1385 **Glossary**

1386

1387 **Spectral fluctuations:** Changes in the energy levels of an emitter due to electrostatic noise in the emitter's
1388 environment.

1389

1390 **Blinking:** Random switching of bright and dark states of the emitter.

1391

1392 **Transform limit:** The ideal coherence limit: $T_2 = 2T_1$, where T_2 and T_1 are the emitter's coherence time and
1393 lifetime, respectively

1394

1395 **Fine-structure splitting (FSS):** Splitting of exciton energy levels caused by spin interactions and / or
1396 wavefunction asymmetry.

1397

1398 **Dark exciton:** In dark exciton the spins of the electron and hole are parallel and spontaneous emission is
1399 forbidden due to spin momentum conservation.

1400

1401 **DC stark tuning:** Tuning of emission spectra using an external electric field.

1402

1403 **Plasmonic cavities:** Cavity where the light is enhanced by the interaction of surface plasmons

1404

1405 **Purcell enhancement:** Environmental enhancement of light emission rate of a quantum system. Typically
1406 caused by a resonant cavity.

1407

1408 **Slot waveguide:** A waveguide, where light is confined between two slabs of high-refractive index
1409 materials.

1410

1411 **Interlayer excitons:** Electron-hole Coulomb bound states between electrons and holes spatially separated in
1412 different monolayers

1413

1414 **Debye-Waller factor:** Describes the magnitude of thermal vibrations in a crystalline lattice and is used as a
1415 measure for structural disorder of material.

1416

1417 **Auto-correlation measurements:** Second-order correlation measurement used to measure the time delay
1418 between two successive photons.

1419

1420 **Cross-correlation measurements:** Correlation measurement of two different signals

1421

1422 **Fermi-Hubbard model:** Interaction model of fermions in a lattice.

1423

1424 **Bose-Hubbard:** Interaction model of Bosons on a lattice

1425

1426 **Hong-Ou-Mandel interference:** This bosonic interference describes the situation where two photons approach
1427 a 50/50 beam splitter from different input ports. If the photons are indistinguishable and they enter the beam
1428 splitter at the same time, both photons will exit together in a superposition from the output ports of the beam
1429 splitter.

1430

1431

1432

1433 **Website summary**

1434 Quantum photonics offers an integrated and scalable approach to quantum information processing and
1435 communication. This article summarises the state-of-the-art and an outlook on future challenges and
1436 opportunities for quantum photonics based on 2D materials.

1437

1438