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# 1 Quasistatic displacement self-sensing method for cantilevered 2 piezoelectric actuators

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7 Piezoelectric meso- and microactuator systems required for manipulation or assembly of microscale  
8 objects demand reliable force and/or displacement information. Available sensors are prone to  
9 dimension restrictions or precision limitation. Self-sensing method, based on the electric charge  
10 measurement, may represent a solution in terms of cost-effectiveness and integration, the actuator  
11 performing simultaneously as its own sensor. This paper presents a self-sensing method dedicated  
12 to free uni- and bimorph piezocantilevers but can also be adapted to other piezoactuator types. The  
13 integrated electric current, used to convert the charge, can be compensated against piezoelectric  
14 material nonlinearities to provide accurate displacement information. The advantages relative to  
15 existing self-sensing methods consist in the ability to keep this displacement information for  
16 long-term periods (more than a thousand seconds) and in the reduction in signal noise. After  
17 introductory issues related to the method the base principle allowing the estimation of tip  
18 displacement is presented. Then, the identification procedure of the estimator parameters is depicted  
19 and representative experimental results are shown. Finally, a series of aspects related to electronic  
20 circuits are discussed, useful for successful system implementation.  
21

## 22 I. INTRODUCTION

23 Piezoelectric cantilevered actuators usually made up of  
24 one or two piezoelectric layers (called uni- or bimorph) are  
25 present in many micromanipulation and microrobotic appli-  
26 cations, thanks to their high displacement resolution and fast  
27 response time. The static and dynamic behaviors of piezo-  
28 electric actuators, their inherent nonlinearities (hysteresis and  
29 creep), and limits were studied and modeled<sup>1-4</sup> especially  
30 during the past 2 decades in attempting to provide more ef-  
31 ficient control solutions.<sup>5-7</sup>

32 In order to perform very accurate and fast response time  
33 closed-loop micromanipulation tasks, various sensors have  
34 been used. Unfortunately, these sensors are not ideally  
35 adapted to the micro- and nanoworld because of their sizes,  
36 performances, and limited measurement of degrees of free-  
37 dom. Table I summarizes mostly available sensors in the  
38 field. Hence, an alternative to the use of sensors is the self-  
39 sensing method. There are several advantages of the self-  
40 sensing method relative to the use of external sensors.  
41 Among them, it allows a consistent reduction in the costs by  
42 eliminating expensive sensors. As can be seen, resolution can  
43 also be submicrometric and comparable to that of external  
44 sensors. Self-sensing is based on charge conversion. In fact,  
45 charge is nearly proportional to the displacement, hence  
46 there is no need to further compensate the complex nonlin-  
47 earities (hysteresis and creep) such as in (Ref. 8).

48 The idea of self-sensing in piezoelectric cantilever has

49 been started by the work of Dosch *et al.*<sup>9</sup> While it is not a  
50 new concept on vibration damping or control,<sup>10-13</sup> more re-  
51 cently, it has shown its feasibility for piezoelectric tubes of  
52 atomic force microscopy.<sup>14,15</sup> But to our knowledge, self-  
53 sensing methods have not yet been adapted for long-term  
54 (more than hundreds of seconds) displacement measurement  
55 of cantilevered actuators, as required by micromanipulation  
56 and microrobotic tasks. In this paper, we present a compen-  
57 sated self-sensing approach especially dedicated to long-term  
58 static measurement. We especially focus on the displacement  
59 measurement of a piezoelectric cantilever beam.

60 Drawbacks of displacement self-sensing method refer to  
61 inherent charge leaks and temperature influence. With proper  
62 actuators and electronic circuits, charge information may be  
63 preserved even for thousands of seconds. However, because  
64 of the temperature variations, extra care will be required for  
65 proper thermal isolation especially in the case of nonsym-  
66 metric cantilevers (example: unimorph) to limit temperature-  
67 related uncertainties.

68 There are several self-sensing schematics depending on  
69 application. Capacitive bridges<sup>9,11</sup> are convenient for vibra-  
70 tion control but are not easy to balance for long-term mea-  
71 surements. Structures with both electrodes for actuation and  
72 electrodes for sensing are a simple solution but their incon-  
73 venience is a partial reduction in the total actuating  
74 range.<sup>14,16</sup> A current integrator was introduced in Ref. 17 for  
75 a piezostack. The disadvantage was a poor compensation of  
76 leaking resistance with a very high value potentiometer  
77 across the integrating capacitor. Another method quite related  
78 to self-sensing concept was linearization of the actuator  
79 displacement using voltage-to-charge amplifiers.<sup>18,19</sup> The ad-

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TABLE I. Displacement sensors for the microworld.

Sensor type	Advantages	Disadvantages
Triangulation lasers	High precision and resolution; fair band pass; and spot measurement	Quite expensive, large sizes, and limited measurement range
Interferometers	Very high precision resolution and range; increased band pass; and spot(s) measurement	Very expensive and large sizes
Diffraction grating target	High precision and multidimensional measurement	Large sizes, require attaching target, and expensive
Strain gages	Less expensive and millimeter size	Fragile, noisy output signal, and temperature influence
Capacitive or inductive	High sensibility, high precision, and fair price	Require linearization, from fair to quite large dimensions, and close vicinity requirements
Magnetic Hall effect, magnetoresistive, and magnetostrictive	Good precision, band pass, and fair price	Require permanent magnets often too large and close vicinity requirements.
Using image processing	Large measurement range and in-plane displacement	Expensive and limited resolution and response time
<i>Piezoelectric self-sensing</i>	Double functionality, high band pass, high resolution, and lowest price	Require nonlinear compensation and long-term charge leaking

80 vantage was a linear voltage-to-displacement characteristic.  
 81 However, the conventional HV supplier needs to be replaced  
 82 by more complex charge driven circuits. In our paper we  
 83 propose two simple schematics of current integrators (modi-  
 84 fied charge amplifiers) that can also be easily implemented  
 85 onto existing systems, avoiding requiring the redesign of ac-  
 86 tuator or HV supply.

87 The developed self-sensing systems can be divided into  
 88 three main parts, as in Fig. 1: the piezoelectric actuator, the  
 89 electronic circuit, and the data processing system. The latter  
 90 is the proposed self-sensing estimator. The estimate displace-  
 91 ment could be used for further feedback or closed-loop con-  
 92 trol systems.

93 Piezoelectric actuators are submitted to  $V_{in}$  external volt-  
 94 ages in a range of up to several hundred volts, depending on  
 95 actuators. Resulted charge  $Q$  (in fact integrated current) is  
 96 converted by the electronic amplifier to a measurable voltage  
 97  $V_{out}$ . This signal will be converted for further numerical pro-  
 98 cessing. Data is further processed on a computer or is de-  
 99 ployed into a real-time processor or microcontroller. External  
 100 signals can be provided to improve the self-sensing accuracy,  
 101 for instance temperature variation may be compensated with  
 102 a small thermistor. As the charge cannot be kept indefinitely,  
 103 external resetting before each measurement prevents satura-  
 104 tion and offsets large parts of the static error.

105 Among the contributions of this paper include: the intro-  
 106 duction of an antiparallel reference capacitance, numerical  
 107 compensations of amplifier bias currents and of piezoelectric  
 108 leaking resistance, and dielectric absorption. A step by step  
 109 approach of the identification of the self-sensing parameters  
 110 is presented as well as experimental results.

111 The paper is organized as follows. First, we present the  
 112 principle and related equations of the self-sensing estimator.

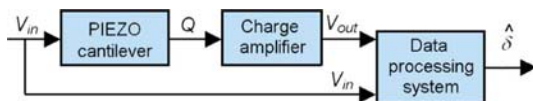


FIG. 1. (Color online) Displacement self-sensing system.

Afterwards, we detail the parameter identification. Hence, we  
 present the experimental results. Finally, we relate some is-  
 sues to be taken into account when deploying self-sensing  
 systems.

## II. DISPLACEMENT DETECTION

### A. Charge output of piezoelectric cantilever

Consider a bimorph cantilevered beam piezoactuator  
 subjected to an electrical excitation  $V_{in}$  (Fig. 2). The beam is  
 characterized by its length  $L$ , its width  $w$ , and its half-  
 thickness  $h$ .

In the absence of external force, we have a theoretically  
 linear relation between displacement and applied voltage<sup>20</sup>

$$\delta = - \frac{3d_{31}}{d_{31}^2} \frac{L^2}{h^2} V_{in}, \quad (1)$$

where  $s_{11}^E$  is the compliance coefficient along the beam ( $X$   
 direction),  $\epsilon_{33}^S$  and  $d_{31}$  are dielectric and piezoelectric mate-  
 rial coefficients.

Using the relation between the applied voltage and the  
 capacitance for bimorph piezoelectric cantilever beam

$$Q = \frac{4wL\epsilon_{33}^S}{h} V_{in}, \quad (2)$$

charge directly results and, as stated previously, is quasipro-  
 portional to free displacement  $\delta$

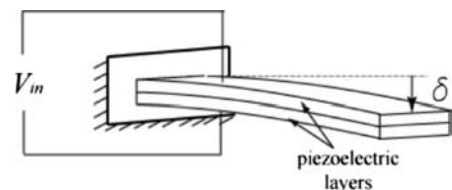


FIG. 2. A bimorph piezoelectric cantilever beam.

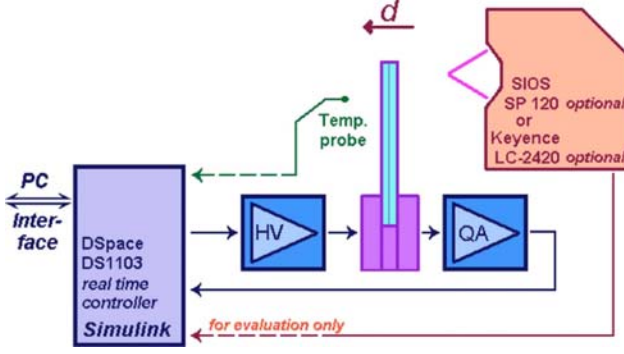


FIG. 3. (Color online) Experimental setup schematic of the self-sensing actuator. Direction for positive displacement is given.

$$Q = \frac{4wh\epsilon_{33}^S}{3d_{31}L} \left( 1 + \frac{d_{31}^2}{4s_{11}^E\epsilon_{33}^S} \right) \delta = \alpha\delta, \quad (3)$$

where  $\alpha$  is denoted as an actuator charge-displacement coefficient. In the sequel, this charge will be converted into a measurable voltage  $V_{out}$  from which the deflection  $\delta$  will be estimated, as described in Fig. 1.

### B. Experimental setup

A schematic overview of the setup is depicted in Fig. 3. Several uni- and bimorph rectangular actuators (PZT on Cu or Ni substrate) were tested, of length between 10–15 mm, width between 1–2 mm, and total thickness of 0.27–0.45 mm. A Keyence LC-2420 optical displacement reader was only used for intermediate tests on actuators displacement; for some measurements requiring better precision a SIOS SP-120 miniature plane-mirror interferometer was employed (Fig. 4). However displacement readings served only for referencing and evaluating purposes of the self-sensing method. The high voltage (HV) amplifier allowed applying a voltage up to  $\pm 150$  V. A current integrator amplifier circuit (modified charge amplifier) to be discussed next chapter provided  $V_{out}$  output signal. The Matlab Simulink detection model was deployed on a high speed DSpace DS1103 real-time controller board. A PC-based CONTROLDESK interface served for model parameterization and data acquisition/presentation.

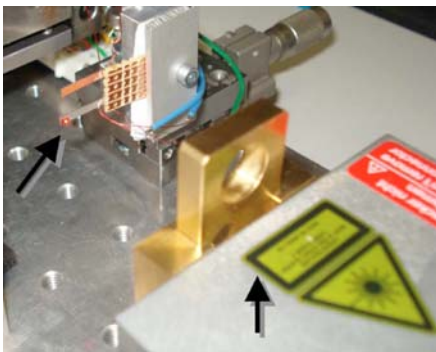


FIG. 4. (Color online) Photo of experimental setup. Actuator is placed in the upper left and SIOS interferometer is in the right side of the image.

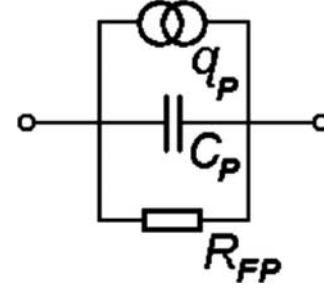


FIG. 5. Equivalent electrical schematic of a piezoactuator.

### C. Integrator amplifier

The static electrical equivalent schematic of piezoelectric bender is a charge generator in parallel with a capacitor and a leaking resistance, as seen in Fig. 5, and its electromechanical model is shown in Ref. 2.  $C_p$  capacitance is in the order of nanofarad depending on the shape and dimensions of the microactuator's structure while  $R_{FP}$  is the insulating resistance, whose order of magnitude is between  $10^9 \dots 10^{12} \Omega$ .

If we ignore nonlinear effects, charge is proportional to the applied voltage and the external force. To measure charge, we propose a precise integrator circuit scheme, as pictured in Fig. 6 and described below.

The input signal  $V_{in}$  is inverted and applied to a “reference capacitor”  $C_R$  whose the value is close to  $C_p$  value; it will “absorb” a significant part of the charge due to the applied voltage, according to the second Kirchoff law. Although  $C_R$  and HV inverter may miss from the circuit, their use is recommended. Indeed, the output will saturate at a higher  $V_{in}$  input voltage value (up to several hundred volts) while preserving the same sensitivity. Feedback capacitor  $C$  will integrate the current due to external force variation and applied voltage (depending on  $C_R/C_p$  fraction). An electro-mechanical relay-switch  $k$  (in series with several kilo ohms resistor) allows resetting  $V_{out}$  voltage from DSpace environment in order to avoid the saturation. Electronic switches are not suitable because of their “off” source/drain leakage currents. Further details and propositions are discussed in Sec. V.

Output voltage is

$$V_{out} = -\frac{1}{C} \int_0^T i(t) dt = -\frac{1}{C} Q, \quad (4)$$

where, for the free beam ( $F_{ext}=0$ ), charge is

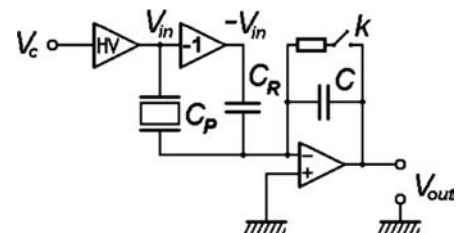


FIG. 6. Electronic circuit schematic of charge amplifier.

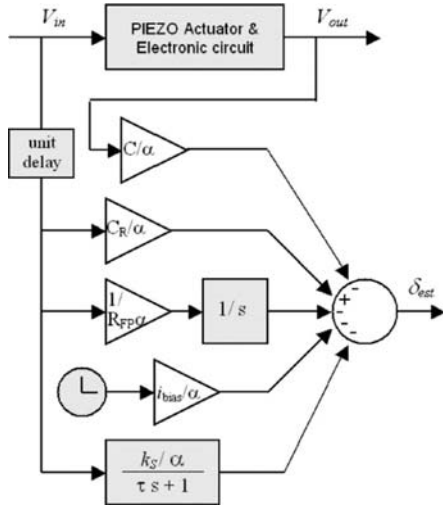


FIG. 7. Displacement detection model (Simulink).

$$Q = -C_R V_{in} + \alpha \delta, \quad (5)$$

where  $\alpha$  was introduced in Eq. (3).

If we consider a nonlinear dielectric absorption effect of piezoelectric material, we propose the following slight modification:

$$Q = -C_R V_{in} + (\alpha \delta + Q_{DA}), \quad (6)$$

where  $Q_{DA}$  is an internal amount of charge depending on  $\epsilon_{33}$  variation.

#### D. Detected displacement formula

Adding the influence of the nonzero bias current  $i_{BIAS}$  of the operational amplifier (op-amp) and finite leaking resistance  $R_{FP}$  of the piezoactuator, output voltage  $V_{out}$  of the free cantilever beam is given by

$$V_{out} = \frac{C_R}{C} V_{in} - \frac{\alpha \delta + Q_{DA}}{C} - \frac{1}{C} \int \frac{V_{in}(t)}{R_{FP}} dt - \frac{1}{C} \int i_{BIAS}(t) dt. \quad (7)$$

Extracting the displacement  $\delta$ , we obtain the estimate as follows:

$$\delta_{est} = -\frac{C}{\alpha} V_{out} - \frac{Q_{DA}(V_{in}, t)}{\alpha} + \frac{C_R}{\alpha} V_{in} - \frac{1}{R_{FP} \alpha} \int V_{in}(t) dt - \frac{1}{\alpha} \int i_{BIAS}(t) dt. \quad (8)$$

We will consider a simple relaxation effect described by a first-order transfer function for the dielectric absorption term

$$Q_{DA}^*(s) = \frac{Q_{DA}(s)}{\alpha} = \frac{k_s^*}{\tau s + 1}, \quad (9)$$

where static gain  $k_s^* = k_s / \alpha$ . Based on the previous equations, Fig. 7 presents the detailed estimation bloc-scheme. Some parameters of the identification in Eq. (8) have to be identified. It will be presented in the next section.

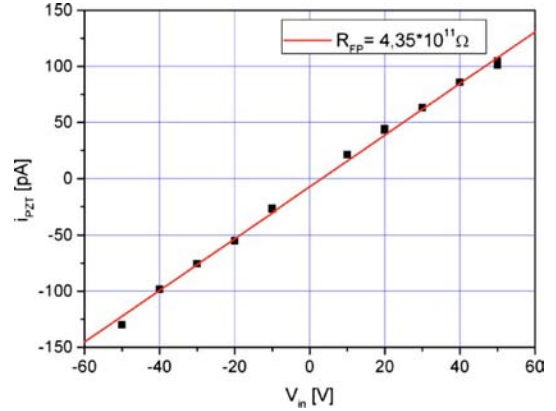


FIG. 8. (Color online) Leakage current of PZT actuator measured under constant dc voltage values. Calculated insulation resistance is 0.435 T $\Omega$ .

### III. SELF-SENSING PARAMETER IDENTIFICATION

Parameters identification of Eq. (8) can be performed under a manual or semiautomatic procedure. Capacitances are given ( $C=47$  nF and  $C_R=8.2$  nF in our case). The identification procedure for the rest of parameters ( $\alpha$ ,  $i_{BIAS}$ ,  $R_{FP}$ , and  $Q_{DA}$ ) is based on Eq. (7), where the displacement  $\delta$  is provided by the displacement sensor (optical or interferometer). The following steps describe the identification procedure.

#### A. Bias current $i_{BIAS}$ identification

Under  $F_{ext}=0$ ,  $V_{in}=0$ ,  $V_{out} \cong 0$ , and zero temperature change, there is no electric current through the piezoelectric material; the  $V_{out}$  rate of change is measured for several dozens of seconds, deriving  $i_{BIAS}$ .

#### B. Leaking resistance $R_{FP}$ identification

Under  $F_{ext}=0$ , a constant voltage  $V_{in} \neq 0$  is applied to the actuator. After several hundred seconds the creep influence becomes negligible, and the output voltage  $V_{out}$  shifts with a constant slope, depending on  $i_{BIAS}$  (identified before) and  $R_{FP}$  (to be identified).

The identification can be repeated for different  $V_{in}$  values and averaged. Each point in Fig. 8 was recorded after a 1000–2000 s delay, to eliminate residual creep influence. Linear regression was applied.

Quality piezocantilevers will exhibit  $R_{FP}$  values superior to 1010  $\Omega$ . For our actuator we identified  $R_{FP}=0.435$  T $\Omega$ .

#### C. Displacement coefficient $\alpha$ identification

A step signal is applied on the free actuator. To avoid dynamic oscillations of the actuator, the step signal is shaped with ramp of around 20 V/s (Fig. 9). Measured values of  $\delta$  and  $V_{out}$  immediately after  $V_{in}$  step signal will serve to compute  $\alpha$

$$\alpha = (-C V_{out} + C_R V_{in}) / \delta. \quad (10)$$

An alternate method for deriving  $\alpha$  is to apply one or several sinusoidal signals as in Fig. 10 and use amplitude values in Eq. (10).



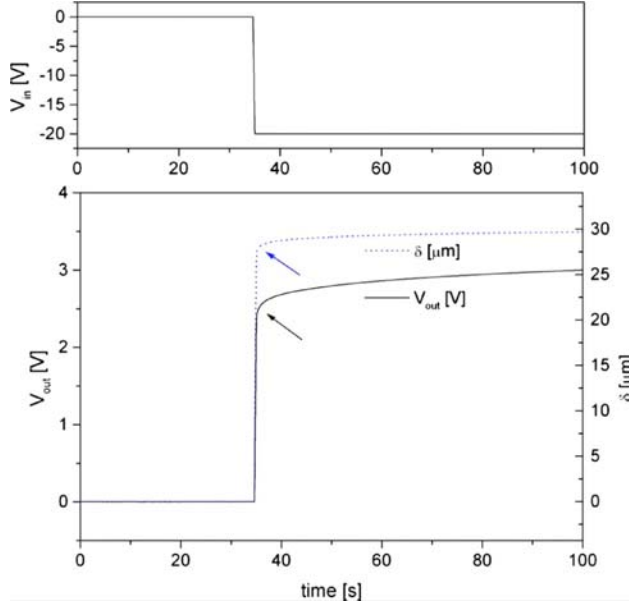


FIG. 9. (Color online) Identification of  $\alpha$  coefficient with a  $-20$  V ramped step input.

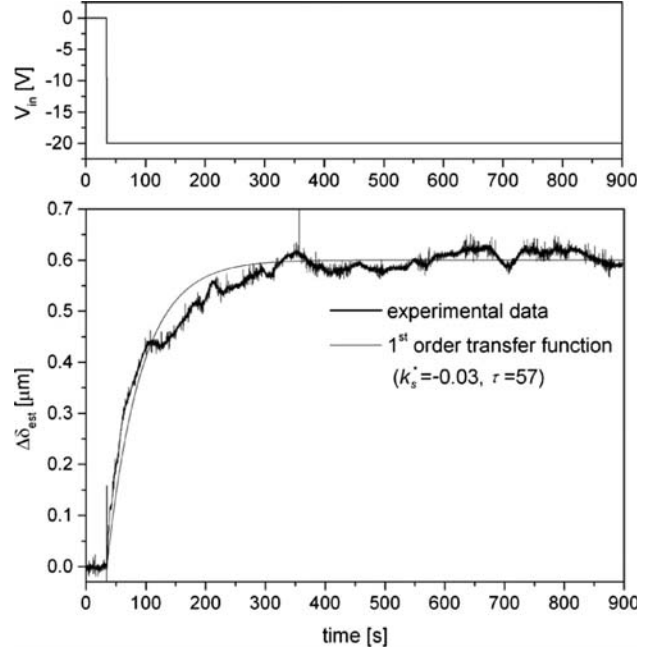


FIG. 11. Identification of dielectric absorption  $Q_{DA}^*(s)$  transfer function.

## 251 D. Identification of dielectric absorption transfer 252 function

253 The last part to be identified in displacement in Eq. (8) is  
254 the dielectric absorption  $Q_{DA}(V_{in}, t)$  of the piezoelectric  
255 material.

$$256 \quad \Delta \delta_{est}(s) = Q_{DA}^*(s) V_{in}(s), \quad (11)$$

257 where  $\Delta \delta_{est} = \delta_{est} - \delta$  is the difference between estimated (us-  
258 ing already identified parameters) and measured tip displac-  
259 ements (Fig. 11). Identification of  $k_s$  and  $\tau$  is performed on a  
260 step response, calculating the static gain and response time to  
261 reach 63.2% of final value.

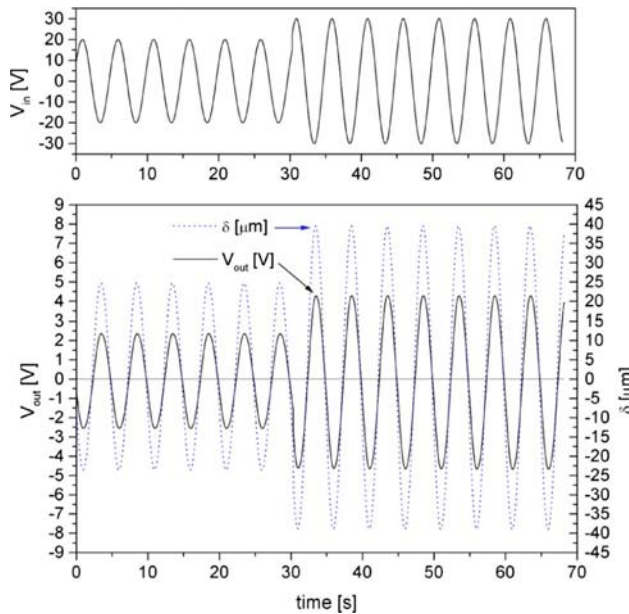


FIG. 10. (Color online) Identification of  $\alpha$  coefficient from sinusoidal signals.

## IV. SELF-SENSING RESULTS

Several tests have been performed to evaluate the accu-  
racy of the proposed self-sensing technique. Known and  
identified parameters are entered into the real-time processor,  
we have

$$\alpha = -10.05e^{-9} \text{ C/m},$$

$$C = 47e^{-9} \text{ F},$$

$$C_P = 1.74e^{-9} \text{ F},$$

$$C_R = 8.2e^{-9} \text{ F},$$

$$R_{FP} = 0.435e^{12} \Omega,$$

$$i_{BIAS} = -1.7e^{-12} \text{ A},$$

$$\tau = 57 \text{ s},$$

$$k_s = 3.02e^8 \text{ m/V}.$$

### A. Displacement self-sensing results

In Fig. 12, an input signal  $V_{in}$  was applied in several  
steps between  $+20$  and  $-25$  V, under null external force.  
Data was recorded for 1020 s—largely sufficient for most  
applications involving piezoelectric actuators. A very good  
agreement is found; measured and detected displacement  
curves almost superpose.

A comparative representation of displacement errors is  
made as follows. Three graphs are traced (Figs. 13–15) from  
uncompensated to fully compensated with respect to leaking  
resistance and dielectric absorption. Measurement with Key-  
ence optical displacement reader provided a poorer linearity  
than self-sensing signal, making it impossible for accurate  
error evaluation; SIOS interferometer was eventually em-

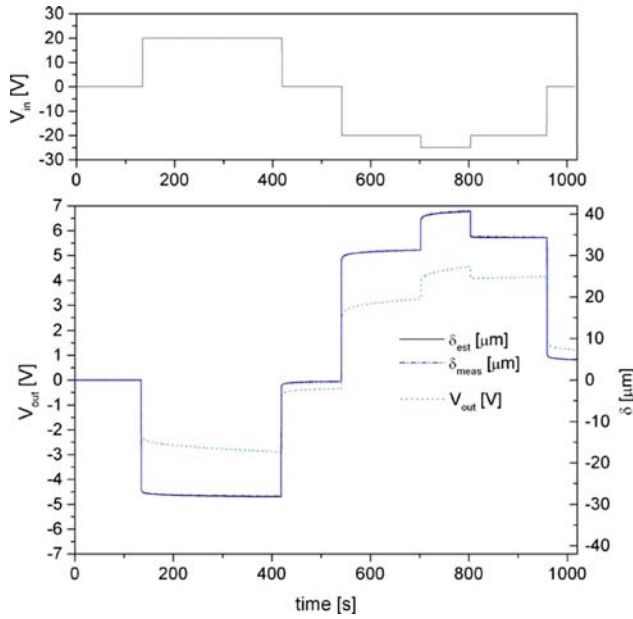


FIG. 12. (Color online) Measured and detected displacement for an arbitrary  $V_{in}$  input signal ( $F_{ext}=0$ ).

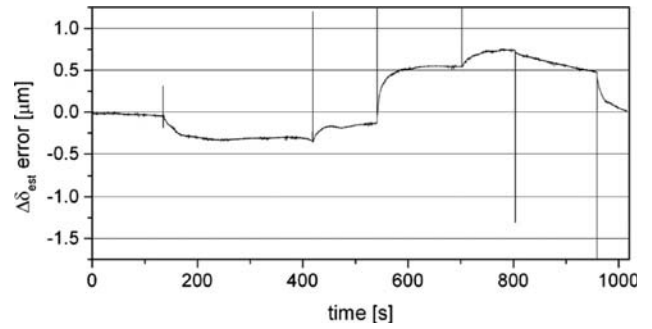


FIG. 14. Error curve of detected displacement with only leaking resistance  $R_{FF}$  compensation.

piezoelectric and passive material tend to bend the structure like a thermal bimetallic, conducting to parasitic displacement (and charges). In this case Eq. (2) between charge and displacement no longer applies ( $Q \neq \alpha \delta$ ), leading to displacement errors. To analyze the thermal influence, we compared its effects on two types of piezoelectric beams: unimorph and bimorph cantilevers. As seen in figures and as expected, unimorphs (Fig. 17) are more affected by ambient temperature than bimorphs (Fig. 18). As bimorph cantilevers are intrinsically symmetric, charges from both sides sum up and self-compensate.

If we compare the above results, we see that unimorph cantilevers are five times more sensitive to temperature than bimorphs. Errors can be limited by a proper thermal isolation or compensated with a sensitive temperature sensor like a miniature thermistor. However, temperature sensor should be in contact with the actuator for more correlate readings.

## V. CURRENT INTEGRATION RELATED ISSUES

An improper choice of charge amplifier<sup>21</sup> will significantly reduce sensing accuracy. The circuit should be protected against temperature changes, with a special care to PCB design (guard rings, sufficient space between routes, vias, and pads) otherwise unwanted leakage will easily exceed op-amp bias current.

Integrating capacitor must have primarily an extremely high insulation resistance, low dissipation factor, and good temperature stability. Polypropylene plastic film capacitors were employed in our case, with a measured leaking resistance of 24 T $\Omega$  for  $C=10$  nF, high enough to ignore its

employed. Our constraint on the utilized interferometer is that data is only available offline. Vertical error lines in the figures can be neglected and are due to the linear interpolation and sampling period mismatch between the two data sets (acquired at sampling rates of 10 and 16.11 Hz).

As seen in the Fig. 13, peak-to-peak error of uncompensated signal is 2.75  $\mu\text{m}$ . Compensation of  $R_{FF}$  leaking resistance allowed a reduction in maximum error to 1.05  $\mu\text{m}$  (Fig. 14). Adding the compensation of dielectric absorption (Fig. 15) provided a 0.38  $\mu\text{m}$  (0.55%) peak-to-peak error.

Unaveraged measured self-sensing signal noise in displacement is of only 1.6 nm (rms), being 10 times less noisy than that of filtered Keyence LC-2420 sensor (16.7 nm rms noise on 4096 averaged samples). However, as expected, SIOS SP 120 interferometer showed best results: 0.5 nm rms noise (Fig. 16).

### B. Temperature influence on displacement self-sensing accuracy

Temperature exhibits changes in dielectric and piezoelectric constants. Also, differences in thermal expansion of

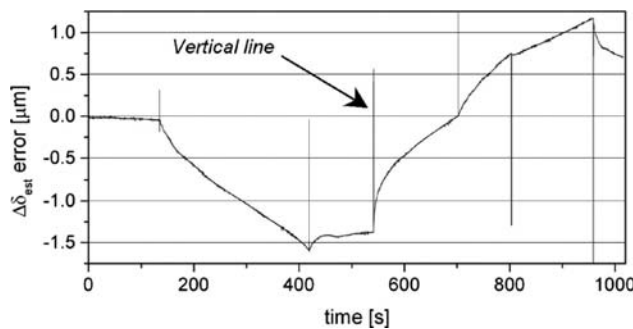


FIG. 13. Error curve of detected displacement with no leaking resistance  $R_{FF}$  and dielectric absorption  $Q_{DA}$  compensation.

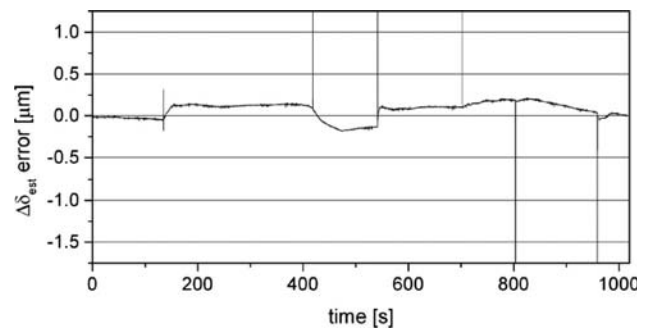


FIG. 15. Error curve of detected displacement with compensation of leaking resistance  $R_{FF}$  and dielectric absorption  $Q_{DA}$ .

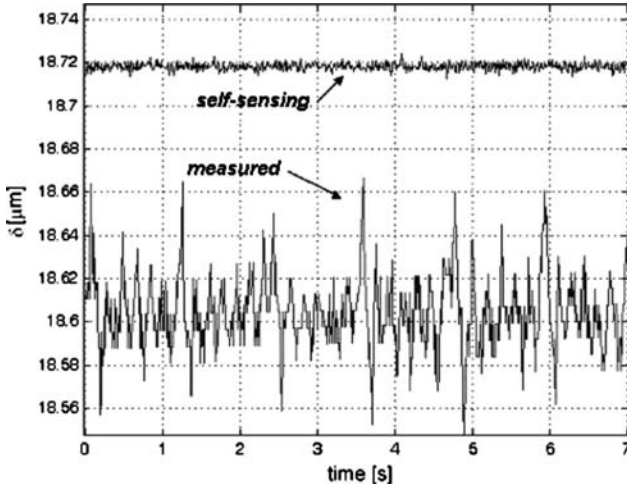


FIG. 16. Zoomed in measure (Keyence LC2420) and detected displacement for noise evaluation.

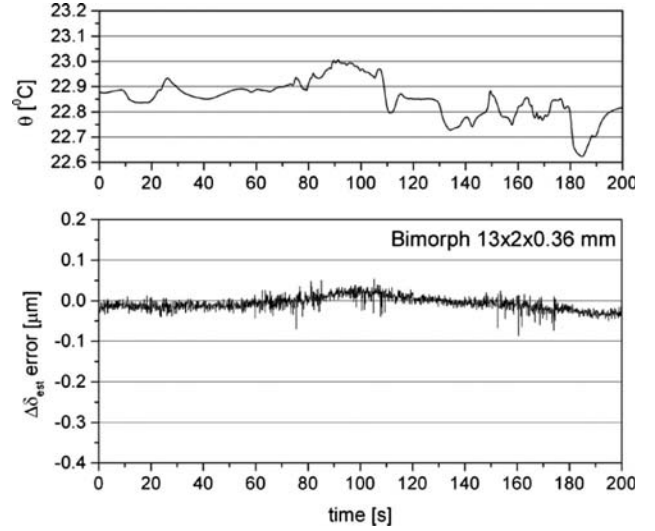


FIG. 18. Typical self-sensing displacement error due to ambient temperature change in a bimorph actuator. Error is  $\sim 0.2 \mu\text{m}/^\circ\text{C}$ .

338 leaking influence in the circuit. Polystyrene or Teflon capaci-  
 339 tors also showed better performance than ceramic or polyes-  
 340 ter film capacitors.  
 341 Precise operational amplifiers used in charge amplifiers  
 342 must be unity-gain stable; otherwise they will tend to oscil-  
 343 late. Noise and bias currents have to be as small as possible.  
 344 Several op-amp types were tested, OPA111BM Difet model  
 345 was chosen for its very small bias current (1.7 pA), small  
 346 offset voltage, small temperature drift, fair supply voltage,  
 347 and on-chip guarding ring. OPA627 model is also suitable.  
 348 Attention has must be paid to supply and input voltages.  
 349 The circuit is damaged if high input voltage is applied in the  
 350 absence of supply voltage. Also, to prevent the output satu-  
 351 ration, the  $k$  switch allows resetting when necessary. Further  
 352 increase in voltage over an already saturated op-amp will  
 353 cause damage.  
 354 Cables should be shielded properly to avoid the electro-  
 355 magnetic interference. Further noise rejection can be  
 356 achieved by modifying the electronic schematic presented in

Fig. 6. We propose the schematic pictured in Fig. 19 where  
 the current, proportional to the voltage drop across a series  
 resistance or more likely across a voltage divider (to avoid  
 op-amp damage due to HV), is buffered or preamplified and  
 then integrated. Indeed, this schematic allows noise reduction  
 thanks to the grounded series resistance  $R_{Z_2}$  connected to  
 the high impedance amplifier input.

$$V_{\text{out}} = - \frac{R_{Z_2}}{RC(R_{Z_1} + R_{Z_2})} \int_0^T i(t) dt, \quad (12)$$

For our actuator the best compromise between response time,  
 sensitivity, and noise was a series resistance of 82 k $\Omega$  ( $R_{Z_1}$   
 $+ R_{Z_2} = 82 \text{ k}\Omega$ ).

Noise was reduced by a factor of five but on the other  
 hand this schematic was much more sensitive to temperature  
 offset drifts than that of Fig. 6. As  $V_z$  voltage is in the  $\mu\text{V}$   
 range or lower, op-amp offset voltage temperature drift  
 ( $\pm 0.5 \mu\text{V}/^\circ\text{C}$ ) and supply rejection ( $\pm 3 \mu\text{V}/\text{V}$ ) limited  
 system accuracy. Usually op-amp offset is trimmed manually  
 (with potentiometers); in our case this measure was not suf-  
 ficient to compensate thermal drifts. We made an automatic  
 compensation of the offset voltage with random temperature  
 changes. This was performed by connecting DSpace DAC  
 outputs (Fig. 20) to op-amp “trim” pins and by measuring  
 and referencing the temperature to a miniature thermistor in  
 close contact with op-amp chip. This way, we preserved a  
 signal up to 100 s similar in accuracy with that of Figs.  
 12–15, however rms noise was reduced from 1.6 nm to only  
 0.4 nm, inferior to even that of SIOS SP120 interferometer.

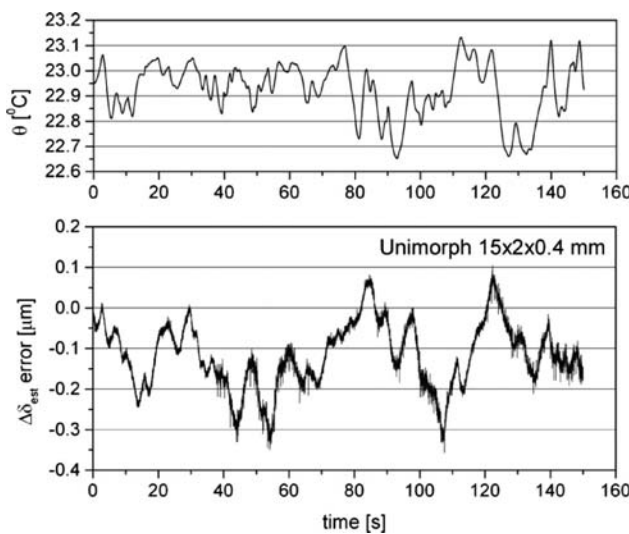


FIG. 17. Typical self-sensing displacement error due to ambient temperature change in a unimorph actuator. Error is  $\sim 1 \mu\text{m}/^\circ\text{C}$ .

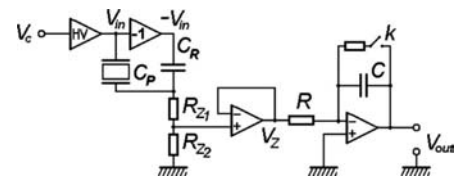


FIG. 19. Alternate schematic with voltage divider and integrator allowed noise reduction.



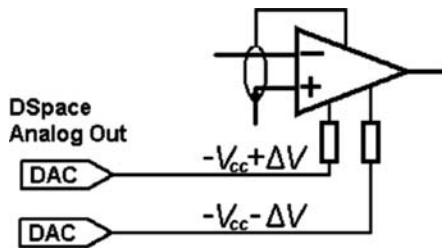


FIG. 20. Offset drift compensation connecting DSpace output to trim pins.

384 Zero-drift chopper op-amps (typically  $\pm 0.03 \mu\text{V}/^\circ\text{C}$ ) will  
 385 probably ameliorate temperature drifts but other effects such  
 386 as thermal electro motive force (EMF) (Seebeck effect) in  
 387 cable junctions will still perturbate the circuit.

388 To generally resume, charge integration is prone to non-  
 389 zero bias currents offset voltages, temperature drifts, leaking  
 390 resistance or currents, thermal EMF and electro magnetic  
 391 interference influence. However, with proper measures, their  
 392 influence can be eliminated or at least partially quantified  
 393 and compensated.

## 394 VI. CONCLUSION

395 Displacement self-sensing of uni- and bimorph cantile-  
 396 vered actuators used for meso- and microscale gripping and  
 397 manipulation is cost-effective and relatively simple to imple-  
 398 ment or upgrade to existing systems. To our knowledge it is  
 399 a first paper focusing on displacement self-sensing of these  
 400 devices. We referred to a current integration method self-  
 401 compensated against some actuator nonlinearities (hysteresis  
 402 and creep) and externally compensated to others (leaking re-  
 403 sistivity and dielectric absorption).

404 In the case of detected or *a priori*—supposed absence of  
 405 external forces, displacement is almost directly proportional  
 406 to the charge. Further compensation of nonzero amplifier  
 407 bias current, finite actuator leaking resistance, and dielectric  
 408 absorption lead to a significant reduction in errors, up to  
 409 0.55% and an increase in measurement period to more than  
 410 1000 s, sufficient enough for most tasks. Signal noise was  
 411 lower than that measured with expensive laser triangulation  
 412 sensor. Two schematics were presented, the first one based  
 413 on direct current integration showed its feasibility for long  
 414 integration periods while the second integrating shunt volt-  
 415 age drop allowed a further reduction in signal noise with a

cost of a more unstable long-term signal. Practical issues  
 related to long-term charge preservation were presented, and  
 temperature influence discussed.

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