Radiation sources based on laser-plasma interactions

By D. A. Jaroszynski^{*}, R. Bingham, E. Brunetti, B. Ersfeld, J. Gallacher, B. van der Geer, R. Issac, S. P. Jamison, D. Jones, M. de Loos, A. Lyachev, V. Pavlov, A. Reitsma, Y. Saveliev, G. Vieux and S. M. Wiggins

University of Strathclyde, 107 Rottenrow, Glasgow G4 0NG, UK

Plasma waves excited by intense laser beams can be harnessed to produce femtosecond duration bunches of electrons with relativistic energies. The very large electrostatic forces of plasma density wakes trailing behind an intense laser pulse provide field potentials capable of accelerating charged particles to high energies over very short distances, as high as 1 GeV in a few millimetres. The short length scale of plasma waves provides a means of developing very compact high-energy accelerators, which could form the basis of compact next-generation light sources with unique properties. Tuneable X-ray radiation and particle pulses with durations of the order of or less than 5 fs should be possible and would be useful for probing matter on unprecedented time and spatial scales. If developed to fruition this revolutionary technology could reduce the size and cost of light sources by three orders of magnitude and, therefore, provide powerful new tools to a large scientific community. We will discuss how a laser-driven plasma wakefield accelerator can be used to produce radiation with unique characteristics over a very large spectral range.

Keywords: laser-plasma interactions; advanced accelerators; radiation sources

1. Introduction

Particle accelerators have become ubiquitous components of advanced light sources and essential tools for exploring the structure of matter. The particle energies required for these respective applications is quite different: synchrotron light sources and X-ray free-electron lasers (FELs) require electron energies in the 100 MeV to few GeV energy range, while high-energy particle physics research requires TeV energies. However, both require accelerators capable of producing very high brightness beams. This imposes a huge challenge on the scientific community developing accelerators, and usually leads to very expensive facilities, partly because of the size of conventional radio-frequency (RF) accelerator components. A vigorous search for ways to make them more compact has driven investigations into new methods for accelerating particles to replace

*Author for correspondence (d.a.jaroszynski@strath.ac.uk).

One contribution of 15 to a Discussion Meeting Issue 'Laser-driven particle accelerators: new sources of energetic particles and radiation'.

conventional RF cavities. Plasma has long been recognized as having the potential of providing acceleration gradients that are three orders of magnitude larger than conventional RF accelerators (Tajima & Dawson 1979; Bingham 2006), which are limited by electrical breakdown of the cavity structures and multipaction. Harnessing plasma waves excited by the light forces of intense laser pulses is creating a revolution in accelerator technology. Researchers have already demonstrated gradients in excess of 100 GV m⁻¹ (Coverdale *et al.* 1995; Modena et al. 1995; Nakajima et al. 1995) in plasma using terawatt class laser pulses. Tenuous plasma with a density, $n_{\rm e}$, in the range of 10^{18} to 10^{19} cm⁻³ can potentially accelerate particles to GeV energies in a few millimetres. However, until very recently, electron beams were produced with a 100% Maxwellian energy spread due to plasma wavebreaking (Malka *et al.* 2002), which limited the usefulness of plasma based accelerators and has been a major impediment to their development. However, a recent breakthrough by several groups (Faure et al. 2004: Geddes et al. 2004: Mangles et al. 2004) reporting the acceleration of relatively high charge (10-500 pC) electron bunches to more than 100 MeV in less than 1 mm, thus unequivocally demonstrating a gradient of more than $100 \,\mathrm{GV \,m^{-1}}$. What was most surprising about these observations was that electrons were launched into the plasma wake from the background plasma, and were accelerated with a relatively small energy spread, $\delta \gamma_{\rm e} / \gamma_{\rm e} \approx 1-3\%$, where $\gamma_e = (1 - \beta^2)^{-1/2}$ is the Lorentz factor and $\beta = v_e/c$ (c and v_e are the respective velocities of light and the bunch in vacuum). Simulations (Martins et al. 2005) indicate that injection is rapidly shut off by beam loading (Trines et al. 2001), which results in both a small energy spread and an extremely short electron bunch, of the order of 10 fs or less. Although ultra-high accelerating gradients have now been unambiguously demonstrated, the length of the plasma, which is typically 1 mm, and dephasing of the electrons in the accelerating potential limit the final electron energy. This work is stimulating investigations into ways of controlling acceleration and exploring the source of pointing and shot-to-shot energy fluctuations (Faure et al. 2004; Geddes et al. 2004; Mangles et al. 2004).

Coherent and incoherent electromagnetic (EM) radiation sources have become very important research tools for both scientists and industrialists. X-ray radiation from synchrotron light sources has become one of the most successful tools of science and is used by a large user community. New light facilities providing coherent radiation based on FELs have also been built, but in spite of the huge advances in their development, they are still restricted to wavelengths longer than 30 nm (Ayvazyan et al. 2002). However, excellent progress is being made to extend the spectral range of self-amplification of spontaneous emission (SASE) FELs to less than 6 nm. The cost of light sources is determined by the size of conventional accelerator structures and their radiation-shielding infrastructure. This is creating a need to make them more compact. The recent progress in the development of wakefield accelerators is thus providing a realistic opportunity to dramatically reduce both their size and cost and, therefore, make them available to any medium sized university or research establishment. Furthermore, as will be discussed below, the ultra-short electron bunches from wakefield accelerators would make light sources unique and enable the production of brilliant EM pulses of only a few femtoseconds in duration, and over a wide spectral range from X-rays to terahertz frequencies. The ultra-short 'pre-bunched' electron bunches should also enable the sources to emit coherently,



Figure 1. Schematic layout of ALPHA-X.

thus opening up the possibility of producing single cycle pulses in the midinfrared and millimetre spectral range and attosecond pulses at shorter wavelengths. These sources would provide excellent tools for time resolved studies while at the same time create an opportunity to build facilities incorporating femtosecond lasers that are synchronized with electron beam based sources and ideal for two-colour and two-type (electron-photon) pumpprobe time resolved studies. If radiation sources based on wakefield technology are developed to maturity it could possibly revolutionize the way science is done.

In this paper, we report on progress towards producing laser wakefield driven accelerators and radiation sources, and explore some of the challenges that need to be met. As an illustration we will describe the United Kingdom advanced laser plasma high-energy accelerators towards X-rays (ALPHA-X) project (Jaroszynski & Vieux 2002) which is applying the technology to driving compact, ultra-short pulse, tuneable, bright EM sources extending from terahertz frequencies to X-rays. Figure 1 shows a schematic of the main components of the ALPHA-X project.

2. The laser-driven plasma wakefield accelerator

Electrostatic forces of a plasma with a density of $n_{\rm e} \approx 10^{18} {\rm cm}^{-3}$ are of the order of 100 GV m⁻¹ (Tajima & Dawson 1979), which is three orders of magnitude larger than that attainable with conventional RF cavities. The ponderomotive force (Kruer 1988) of an intense laser pulse drives a plasma wave in the form of a wake travelling at the group velocity, $v_{\rm g} \ (\equiv c(1-\omega_{\rm p}^2/\omega_0^2)^{1/2} \approx c(1-\omega_{\rm p}^2/2\omega_0^2))$, of the laser pulse in the plasma, where $\omega_{\rm p} = \sqrt{e^2 n_{\rm e}/\epsilon_0 m}$ is the plasma frequency and ω_0 is the radiation frequency. The Lorentz factor associated with the wake velocity is $\gamma_{\omega} = \omega_0/\omega_{\rm p}$. As the wavelength of these plasma waves is very short ($\approx 33 \ \mu m$ for $n_{\rm e} \approx 10^{18} \ {\rm cm}^{-3}$), they provide an opportunity to harness their electrostatic forces to produce a very compact travelling wave accelerating 'structure'. These structures have dimensions that are approximately $\lambda_{\rm p}^3$, where $\lambda_{\rm p} \approx 2\pi c/\omega_{\rm p}$, which is $\approx 4 \times 10^{-5} \ {\rm mm}^3$ for the above density. Furthermore, as the accelerating medium is fully ionized, i.e. already broken down, it is extremely robust. As with conventional RF accelerator cavities, the accelerating potential has both

longitudinal forces, which give rise to acceleration, and transverse forces, which cause focusing or defocusing of the electron bunches, thus many of the techniques of conventional RF accelerator physics can be applied to plasma based accelerators. However, the small dimension of the plasma 'structures' implies several significant challenges for harnessing the waves to accelerate charged particles. The most stringent of these is the requirement that electron bunches must be injected into the accelerating part of the electrostatic wave, which requires bunches to be much shorter than 100 fs for the above density. Electrons should also be injected precisely into the structure at a velocity close to the phase velocity of the wake, i.e. at the group velocity of the laser pulse, thus implying that initially $\gamma_{\rm w} \approx \gamma_{\rm e}$ (typically $\gamma_{\rm w} = 10-50$). For a plasma wave of relative amplitude, $\delta n_{\rm e}/n_{\rm e}$, electrons of the correct phase velocity are accelerated until they gain an energy $\gamma_{\rm e} = 2\gamma_{\rm w}^2 \delta n_{\rm e}/n_{\rm e}$ over a distance $l_{\rm d} = \gamma_{\rm e} \lambda_{\rm p} = 2\gamma_{\rm w}^2 \lambda_{\rm p}/\pi$, after which deceleration occurs. The rapid longitudinal variation of the accelerating potential also increases the resulting energy spread and can cause fluctuations of the mean energy of accelerated electrons. The production of high-quality electron beams with a reproducible mean energy and small energy spread implies bunch durations and synchronism between plasma wake of around 10 fs, for $\delta \gamma_e / \gamma_e < 1\%$, where γ_e and $\delta \gamma_{\rm e}$ are the respective mean and dispersion of the electron bunch energy. The maximum energy acquired by an injected electron bunch is inversely proportional to the plasma density and thus it is an advantage to accelerate particles over longer lengths using low-density plasma. The maximum charge that can be accelerated is proportional to the background plasma density (Chiou & Katsouleas 1998; Reitsma et al. 2000), giving a maximum of between 100 pC and 1 nC for 10^{18} cm⁻³. At this density the dephasing length is of the order of 1 cm. Because diffraction limits the interaction length, it is necessary to guide the laser pulse in some form of plasma waveguide to fully utilize the accelerating potential (Spence & Hooker 2001; Butler et al. 2002). To achieve sufficiently high intensities to drive a substantial plasma wave the normalized vector potential, a = eA/mc (where A is the field potential) of the laser should be ≥ 1 , which implies a laser spot size of the order of 50 μ m for a 20 TW 800 nm laser pulse. The optimum pulse duration for driving the wake is $\tau_{\rm t} \approx \lambda_{\rm p}/2c$ (Fritzler *et al.* 2004), the resonant regime, though it has become clear that laser pulses with a duration longer than $\lambda_{\rm p}/2c$ will evolve to an optimum dimension for driving the wake because of the space and time varying permittivity of the wake. The laser power rapidly evolves to the threshold for self focusing, $P_{\rm crit}(\rm GW) \approx 17 (\omega_0/\omega_p)^2$, which leads to a further increase in the laser intensity.

3. Electron injection

Currently, two general approaches to the injection of electrons into wakefield accelerators are being considered. These are injection of an externally produced ultra-short electron bunch, an approach which goes back more than a decade, and the more recent 'all-optical injection' method (Faure *et al.* 2004; Geddes *et al.* 2004; Mangles *et al.* 2004), where electrons are extracted from the background plasma. Both of these injection techniques are being explored in the ALPHA-X project. However, we will only discuss the former in this paper as

the latter approach is discussed in detail in an accompanying paper (Mangles et al. 2006), in this issue.

(a) External injection

Conventional electron beam injectors are usually based on RF photoinjector accelerators (van der Wiel *et al.* 2006). In these devices ultra-short bunches of electrons are extracted from a photocathode and accelerated in the electric fields of microwave cavities. However, producing electron bunches with durations of the order of 10 fs from photoinjectors is currently not possible because spacecharge forces cause electron bunches to rapidly expand longitudinally and transversely.

A number of methods have been suggested to counteract space charge effects, some of which show promise (Luiten et al. 2004). However, it is generally accepted that the goal of achieving 10 fs electron bunches is still far away. Stateof-the-art photoinjectors are only able to produce electron bunches of the order of 100 fs. New strategies for pre-bunching to compress the injected bunches to 10 fs or less are required. As will be discussed later, one approach adopted has been not to worry about the problem and live with a long bunch while allowing the focusing and defocusing parts of the plasma wakefield accelerator to naturally select a segment or segments of the injected electron bunches (Gordon et al. 2005). This has the disadvantage of increasing the absolute energy spread, but is still useful for accelerators achieving 1 GeV and higher energies because the relative energy spread shrinks with increase in energy. Conventional prebunching strategies used in RF accelerators usually require several accelerating structures to produce an electron energy phase correlation or chirp which is subsequently used to compress the bunches in a dispersive magnetic buncher (Raubenheimer 1995; Saldin et al. 2002; Zholents 2003; Saldin et al. 2004). In this paper, we describe a novel bunch compressor to achieve sub 100 fs electron bunches from a conventional RF accelerator and also methods of compressing electron bunches in the wake of a laser wakefield accelerator. As we will see below, maintaining a very short electron bunch is not possible in a beam transport system that includes strong focusing elements, such as quadrupoles or solenoid fields, because of path length dispersion. However, the problem can be turned into an advantage to compress electron bunches from a photoinjector while avoiding space-charge problems and emittance growth, as will be shown below.

(i) ALPHA-X photoinjector

Figures 1 and 2 show schematically the ALPHA-X photoinjector and the beamline. The injector consists of a 2.5 cell S-band RF photoinjector (McDonald 1988) with an axial RF input coupler, similar to the one described previously (Kwiet 2003; van der Wiel *et al.* 2006). A 10 MW klystron and modulator provides microwave power to the accelerating cavity, which has an on-axis electric field gradient of 100 MV m⁻¹ capable of accelerating electrons emitted from a copper photocathode to 6.25 MeV. Elliptically shaped irises reduce the field on the iris surface to below that of the cathode field to reduce breakdown problems. The electron beam in the photoinjector is transported with a constant radius by a 0.25 T solenoid field and a bucking coil nulls the magnetic field on the



Figure 2. Schematic layout of the ALPHA-X photoinjector and beam line.

cathode surface. After traversing a beam path of 1.5 m, the beam is focused by a 0.5 T solenoid magnet to a spot-size of $\approx 50 \,\mu\text{m}$ at the entrance of a plasma capillary, as shown in figure 2.

(ii) Reducing bunch lengthening of injection electrons

The current approach to create femtosecond bunches with reasonable charge is to accelerate picosecond electron bunches to high energy, in the order of 100 MeV, introduce an energy chirp by off-crest acceleration and then compress them magnetically in a chicane. High-power femtosecond UV lasers allow ultrashort (30-50 fs) electron bunches to be created directly inside a RF photoinjector. Unfortunately, these bunches cannot easily be transported due to space-charge forces. Even assuming prompt response of the cathode (e.g. copper) the bunch is stretched by space-charge forces to nearly a picosecond for reasonable bunch charge (10-100 pC). To illustrate this, we have modelled the beam transport for the ALPHA-X beam line using the particle tracking code, GPT (de Loos & van der Geer 2005). The simulation results shown in figures 3 and 4, of a 50 fs duration electron bunch starting with a large initial radius clearly show that the bunch is distorted by both space charge and path length dispersion which results in very long bunches. Space charge forces can be reduced by lowering the density, which is easily achieved by increasing the beam diameter to form a thin 'pancake-shaped' bunch. However, increasing the bunch radius has two deleterious effects—(i) the emittance of the beam will increase because $\epsilon_n = \sigma \sigma' \gamma_e$, where σ and σ' are the radius and angular dispersion, respectively, and (ii) the bunch will lengthen because of path length dispersion. All focusing systems introduce path length differences which cause bunch lengthening. This is insignificant for picosecond bunches and usually neglected. As path-length differences scale with the beam radius squared they quickly become the dominant effect at large initial radius for femtosecond bunches.



Figure 3. Comparison of bunch length evolution for flat and curved beams for 2 and 5 mm.

There is a trade-off between space-charge induced bunch-lengthening and pathlength induced lengthening. The optimum initial radius of 1.8 mm results in 330 fs bunches for ALPHA-X parameters, which is unacceptably long.

One way of compensating for path length dispersion is to shape the cathode surface and give it a curvature which precisely compensates the path length dispersion introduced by the focusing elements and accelerating fields. When this is done the focusing element behaves as a radial bunch compressor, with the advantage that the radially correlated phase delay appears as a geometric correction at the cathode, unlike velocity bunching techniques. Apart from compensating for path length induced dispersion, the curved cathode also has another very important advantage in extending the electron bunch dimensions into a domed pancake shape with a relatively large diameter thereby drastically reducing space charge effects.

To illustrate the variation of beam parameters, we have carried out simulations using the GPT code (de Loos & van der Geer 2005), of the beam transport through the RF photoinjector accelerator to the final focus at the capillary entrance. A 1 mm initial radius bunch produced by the 30 fs laser pulse is stretched to ≈ 400 fs due to space-charge forces, as shown in figures 3 and 4. The geometrically induced path-length dispersion leads to significant stretching of the bunch for large initial radii. Any focusing/defocusing of the electron beam, also near the irises of the cavity, and cyclotron motion of the bunch in the focusing solenoid result in longer path lengths. The bunch lengthening due to a focusing element for relatively small beam diameters ($D \ll f$) is given by $\delta t = D^2/4fc$, where D is the beam diameter and f is the focal length. As an example, for the ALPHA-X beam final focus onto the entrance to the plasma channel the bunch is stretched by about 120 fs, where we have assumed a beam diameter of 5 mm and a focal length of 17 cm. Further stretching occurs in the accelerating cavities.

To obtain short electron bunches, it is necessary to simultaneously minimize space charge forces while compensating geometrical path length dispersion. Space charge forces can be reduced by lowering the charge density or by using relatively complicated space-charge compensation schemes such as suggested (Luiten *et al.* 2004). The lower charge density is achievable by increasing the radial dimension to produce a 'pancake shaped' bunch from the cathode. However, this comes at the cost of increasing the geometric dispersion, as



Figure 4. Simulated time-radius projection at the entrance of the plasma channel. (a) Flat cathode case, 2 mm beam radius. (b) Curved cathode with 5 mm beam radius and 80 mm radius of curvature. (c) Curved cathode with 2 mm radius beam. The energies of particles are colour-coded to indicate their final energy.



Figure 5. Simulated evolution of the emittance along the beam line with electron beam parameters as in figure 4.

discussed above. It is thus necessary to pre-disperse the electron in bunch radial phase-space by altering the cathode shape. A radius of curvature on the cathode of ≈ 8 cm is required to alter both the initial radial phase space distribution of the electron bunch and to compensate for differences in the accelerating field close to the cathode. The dramatic improvement possible with a curved cathode is illustrated in figure 3, where the beam transport from the cathode to final focus at the position of the plasma-channel has been simulated and the radial phase-space projection is shown at the focus. The curved cathode reduces the bunch length from 330 fs to less than 100 fs FWHM, while simultaneously reducing the spot-size, energy spread and paradoxically the emittance, as can be seen in figure 5, which plots the transverse emittance evolving along the beam line. The reduction of emittance is because the 'slice emittance' is much smaller than the total emittance. For shorter bunches, the spherical concave cathode should be replaced by an elliptical shape to compensate for higher order effects.

(b) Injection and plasma based bunch compression

As mentioned above, injection of electrons into the plasma wake should occur close to the wake phase corresponding to the maximum acceleration



Figure 6. Simulated evolution of the beam energy in the plasma channel (a) at the entrance to plasma channel, (b) 1 mm into channel and (c) at 150 MeV.

potential. Furthermore, the electrons should have a duration, much less than the plasma wavelength for the production of low emittance and energy spread beams. These requirements are very challenging. All-optical injection could provide a possible solution to these stringent requirements. However, much work needs to be done to control all-optical injection to provide a reproducible injection source. It is thus prudent to explore both external and all-optical injection techniques. This is dual approach has been adopted in the ALPHA-X project and all-optical injection techniques are discussed in detail (Mangles et al. 2006). Here, we will discuss two bunching techniques utilizing the plasma wave which require externally injected electron bunches of the order of the plasma wavelength. Two distinct regimes are distinguished by the position relative to the wake at which electrons are injected. We will see below that for electron bunches with a duration $\tau_1 \geq \lambda_p$ injected directly into the wake, the bunch is compressed by a large factor at the expense of charge loss and a relatively large absolute energy spread (Gordon et al. 2005). An alternative method, where low-energy electron bunches are injected ahead of the wake, and compressed by a combination of longitudinal and transverse repulsion forces at the head of the wake is discussed in Khachatryan et al. (2004) and references therein.

(i) Long pulse injection and plasma based bunch compression

Considering the difficulty of producing an injection electron bunch with a duration substantially shorter than the plasma wavelength it is worth evaluating options for bunch compression. It is clear that reducing the bunch length using conventional RF and magnetic bunchers represents a substantial technological challenge, as we saw above. Promising but lossy bunch compression occurs when an electron bunch overlaps the whole of the accelerating and decelerating parts of the wakefield potential (Gordon et al. 2005). The repulsive parts of the accelerating fields filter out electrons, which would otherwise produce a long low energy tail. As an example, we assume an electron bunch with a duration of approximately 100 fs injected into the wake of a tenuous plasma. To model the plasma pre-buncher we have solved the quasi-static fluid equations, and have included space charge evolution of the electron beam in the wake. Modelling of the electron bunch evolution in three dimensions has, as a first attempt, been carried out using the GPT code (de Loos & van der Geer 2005), where the accelerating field has been modelled as $E(r, z) = E_0 \cos(k_{\rm p}(z - v_{\rm g}t) + \varphi)$ $\exp(-r^2/r_0^2)$, where r_0 is the transverse size of the wake and E_0 is the field strength. We have simulated a 300 µm diameter plasma channel (described below) with a density of 7×10^{17} cm⁻³, giving $\lambda_p \approx 33$ µm, resonantly driven by a laser field with a potential $a_0 = 1$. An electron energy and charge of 7 MeV and 10 pC, respectively, has been chosen to be consistent with the ALPHA-X photoinjector describe above. Figures 6 and 7 show snapshots of the electron bunch energy and spatial distributions at the entrance to the capillary, after 1 mm and when they have gained 250 MeV. It is clear from the simulations that the $\lambda_{\rm p}$ segments of electron bunch are rapidly chopped by the interaction into $\lambda_{\rm p}/2$ segments and then bunched both longitudinally and radially.

The wake accelerating structure can be used to bunch the beam by appropriately choosing the phase velocity of the wake, or alternatively, by matching electron beam energy and laser Lorentz factors. A significant fraction of electrons with the appropriate phase velocity can be trapped and electrons in the repulsive parts of the wake, expelled. Adjusting the phase velocity can be used as a way of controlling the trapping fraction, compression factor and the final energy spread, as calculated using our model and shown in figure 8. Compression of the trapped electrons into a small region of phase space leads to both a reduction in bunch length and energy spread, by reducing the potential difference across the electron bunch. Because the trapped charge fraction depends on the phase velocity of the injection electrons, so do beam loading effects (Reitsma *et al.* 2005). There is an optimal beam charge which will cause the wake variation to be ironed out and, therefore, lead to significantly smaller energy spreads (Gordon *et al.* 2005; Reitsma *et al.* 2005).

By placing the electrons in a part of the wakefield where the accelerating force at the back of the bunch is larger than the force at the front, one can effectively compress the electron bunch: the strongest compression occurs if the bunch is injected around a zero of the longitudinal field. This is essentially the same mechanism that is used to compress electron bunches in RF cavities. The reason for using plasma-based compression, rather than a conventional method, is the same reason why plasma-based acceleration is attractive, namely that the gradients are so much higher. The disadvantage of this plasma-based compression scheme is that the initial bunch length must not exceed the plasma wavelength, which for a plasma density as low as 10^{17} cm⁻³ is still a challenging requirement.

In a two-stage buncher-accelerator system a laser pulse and an electron bunch are injected into a short region of low plasma density, which is immediately followed by a somewhat longer region of higher density. The first stage is used for compression of the electron bunch: the low density is used to accept a somewhat longer electron bunch $(\lambda_p \propto n_p^{-1/2})$. The second stage is used for acceleration because of the higher gradient and shorter dephasing length offered by a higher plasma density. This assumes that the dephasing length associated with acceleration in the low-density plasma is too long to be practical.

Beam loading effects are essential to describe the energy transfer from the plasma wave to the electrons (Wilks et al. 1987): accelerated electrons can extract plasma wave energy efficiently only if the amplitude of the bunch wakefield is a significant fraction of the amplitude of the laser wakefield. Threedimensional effects also play a role in the evolution of energy spread, due to the finite bunch width and the dependence of the accelerating forces on the transverse coordinates. All these effects are taken into account in our numerical model. Figure 9 shows the influence of the electron beam wake on the radial F_r and longitudinal F_z forces, which clearly demonstrates the flattening of the accelerating force in the region of the bunch. Beam loading leads to a reduction in the energy spread and emittance. The bunch electrons induce a wakefield that is decelerating and focusing, as shown in figure 9. The magnitude of the decelerating and focusing forces is zero at the front of the bunch and increases along the bunch from front to back. The deceleration of the back of the bunch hinders longitudinal bunch compression. The decelerating force also causes a decrease of the average energy with increasing bunch charge.

Two stage buncher. Design a system with a two section plasma channel, with the first 4 mm with a density of 1.7×10^{17} cm⁻³ and a second stage with a density of 5.4×10^{17} cm⁻³. The buncher compresses to $\tau_{\text{final}} = 2\tau_{\text{initial}}^2\omega_{\text{p}}/2\pi$, therefore, if we inject close to the peak of the wave the bunch length compresses in a plasma from 42 to 14 fs with an energy gain of 8 to 33 MeV after 1.2 cm, as shown in figure 10.

In conclusion, we have found several trade-offs involved in our two-stage scheme which uses a low-density plasma for compression and a higher density plasma for acceleration of the electron bunch, in comparison with a scheme in which the same low-density plasma is used for compression and acceleration (which takes a much longer plasma channel). Firstly, due to the reduction of plasma wavelength in the second stage, it is harder to get a small energy spread. Secondly, because the bunch has to cross a defocusing region of the wakefield, the transverse emittance degrades if the bunch propagates through the density transition. Our simulation results show that both these adverse effects are mitigated by beam loading (Reitsma *et al.* 2005). Finally, we have found that the efficiency of energy transfer in the high-density region is compromised, because the beam loading in the low-density region limits the amount of charge that can be accelerated. This effect can be mitigated by focusing the laser pulse and the electron bunch such that their width is small compared to the plasma wavelength of the low-density region.



Figure 7. Simulated evolution of bunching in the plasma channel (a) at the entrance to plasma channel, (b) 1 mm into channel and (c) at 150 MeV.

4. Plasma channels

An important part of a wakefield accelerator is the plasma medium which supports the plasma wake. It has recently been shown that suitably profiled plasma channels can guide a laser pulse over many Rayleigh lengths. One method of forming a plasma waveguide is to apply a high-voltage discharge through a gas filled capillary (Spence & Hooker 2001; Bobrova *et al.* 2002; Butler *et al.* 2002). The hot plasma rapidly cools close to the wall of a capillary with a radius $r=r_{\rm m}$, and adopts a parabolic radial density distribution, $n_{\rm e}(r) = n_{\rm e}(0) + \Delta n_{\rm e}(r/r_{\rm m})^2$, with a minimum $n_{\rm e}(0)$ on axis and $\Delta n_{\rm e}$ the difference of the electron density across the channel radius (Bobrova *et al.* 2002). A Gaussian laser pulse propagates with a constant spot size $w_{\rm M}$, through the waveguide provided $w_{\rm M} = [r_{\rm m}^2/(r_{\rm e}\Delta n_{\rm e})]^{1/4}$, where $r_{\rm e}$ is the classical electron radius. The waveguiding properties make them an excellent medium for plasma wakefield acceleration.

(a) Development of robust capillaries for wakefield acceleration studies

Typical wakefield experiments require a capillary diameter of 200–300 μ m. Commercially extruded capillaries have a typical roundness of $\pm 10\%$ and a wall



Figure 8. Simulated evolution of the bunch length, emittance, energy spread and mean energy along the plasma channel.



Figure 9. Beam loading I represents the beam current, F_z the accelerating forces and F_r the radial focusing forces. The solid and dotted lines are with and without beam loading accounted for.

thickness of $150-300 \ \mu\text{m}$. Unfortunately, their thin wall sections make capillaries very fragile and susceptible to damage. Minor laser beam misalignment results in ablation of wall material and catastrophic fracture due to shock waves. One solution to this problem is afforded by ablating semicircular cross-sectioned channels in two identical substrates using a femtosecond laser and then join them to form a single hollow capillary channel, as shown in figure 11. This has many advantages including robustness, ease of handling and most importantly, the ability to form tapers and other hollow structures.

Femtosecond laser micro-machining with appropriate pulse lengths and incident fluence levels ensure a laser spot diameter small compared with the desired profile topology and thus allow a groove to be formed in the surface of any substrate with a few micron accuracy. Additional grooves machined in one of the substrates act as hydrogen gas feed lines to both ends of the capillary, as



Figure 10. The average energy γ_e , relative energy spread, bunch length and normalized emittance for two-staged buncher. The solid and dotted lines are with and without beam loading accounted for.



Figure 11. Schematic of grooves machined into capillary block.

shown in figure 11. The main hydrogen feed lines consist of simple slots with a cross-sectional area three times greater than the total link feed line area, which in this case is $\approx 400 \times 400 \,\mu$ m. This geometry ensures a static gas fill in the capillary and minimizes the risk of the electrical discharge in the hydrogen feed line. The two completed alumina substrates are finally aligned and glued together using epoxy resin. A typical machined cross-section is within 2% of a calculated convolved Gaussian semicircle, which is substantially better than the $\pm 5\%$ roundness of an extruded tube.

Plasma waveguides manufactured as described above have been extensively tested and have survived continuous usage as a plasma waveguide for more than 1 year (greater than 10^6 shots).

The waveguiding properties of the profiled capillaries have been explored using a 10 Hz CPA femtosecond laser delivering up to 250 mJ, 800 nm, 50 fs pulses



Figure 12. Front and back face of capillary after 10^6 shots.

(Jaroszynski *et al.* 2000*a*). The experimental set-up includes a suitable imaging system for examining the transverse profiles at the entrance and exit of the capillary. Ninety-five per cent of a beam is transmitted through the plasma waveguide formed by fully ionizing hydrogen gas with an electrical discharge. The capillaries are robust and do not suffer catastrophic failure due to beam misalignment. Figure 12 shows the entrance face of a capillary after 10^6 pulses. Laser machining of the surface is evident but does not appear to detrimentally modify the waveguide. In fact, we observe that waveguiding efficiency improves from $\approx 80\%$ to more than 90% with use, which suggests that tapering of the entrance improves mode matching. Evidence of tapering has also been observed in the density measurements described below.

(b) Novel technique for measuring the plasma density in a channel

Interferometry techniques have been routinely used to map the plasma distribution but usually can only be applied to small-scale plasmas. These techniques determine the permittivity of the transparent medium using arrangements like Michelson, Mach-Zehnder and less often Fabry-Perot interferometers. The density is determined from the phase change calculated from shifts in the fringe pattern. The phase change is directly related to the line integrated density along the ray path. Thus, a first limitation appears for these interferometry methods: they do not provide the local density of the plasma but rather an averaged value. Furthermore, some knowledge of the expected plasma distribution is required for the Abel transformation, which is used to deduce the localized plasma density. Also, extended plasmas cannot be probed as the laser pulse starts to interact too strongly with the plasma and becomes modulated. Here, we present a new technique based on broad-band Raman amplification to measure the density of plasmas. This method has several advantages over other methods. First, it provides a non-invasive tool for determining the electron density and, therefore, the plasma remains essentially undisturbed. Secondly, the density is measured locally and at a fixed time relative to the evolving plasma distribution, in contrast with interferometry techniques, which provide averaged values. Finally, the plasma density is determined directly and does not require extended calculations.

Stimulated Raman scattering (SRS) is a three-wave parametric instability where an incident EM wave (ω_0, \mathbf{k}_0) resonantly decays into a backscattered EM wave (ω_1, \mathbf{k}_1) and a plasma wave (ω_p, \mathbf{k}_p) satisfying the resonance conditions $\omega_0 = \omega_1 + \omega_p$ and $\mathbf{k}_0 = \mathbf{k}_1 + \mathbf{k}_p$, where ω_i and \mathbf{k}_i represent the frequency and wave vector of the waves, respectively (Kruer 1988). A seed pulse, injected into a column of under-dense plasma can, therefore, be amplified by a counterpropagating pump pulse. In the linear SRS regime, when the intensities of the seed and pump are moderate ($\leq 10^{15} \,\mathrm{W \, cm^{-2}}$ for 800 nm radiation), the amplitude of the seed grows as $q = e^{\Gamma t}$, where Γ is the growth rate and t the duration of the interaction. For monochromatic circularly polarized beams, the duration of the interaction is given by the pump duration and the gain is given by $\Gamma = a_0 (\omega_0 \omega_p / 2)^{1/2}$. This large exponential gain has led to the suggestion of stimulated Raman backscattering in plasma as an alternative parametric amplifying medium (Shvets et al. 1997; Malkin et al. 1999). In contrast with the SRS linear theory for long duration monochromatic beams, very interesting features also appear when broad bandwidth chirped seed and pump pulses with identical spectral bandwidths, broader than twice the plasma frequency. The gain factor becomes a function of the intensity of the pump beam (Ersfeld & Jaroszynski 2005; Vieux et al. submitted). Finally, if the intensity of the pump beam is much larger than the seed intensity, the plasma wave is strongly driven only when resonant excitation occurs between the central frequency of the pump ω_0 , which is the most intense, and the frequencies of the seed detuned by $\pm \omega_0$. In the seed spectrum a gain peak occurs at $\omega_0 - \omega_p$ and a loss trough at $\omega_0 + \omega_p$. The separation between the peak and trough is equal to twice the plasma frequency and directly leads to a measure of the density $n_{\rm e} = (\omega_{\rm p}^2 \epsilon_0 m/e^2)^{1/2}$. Furthermore, because the interaction time is limited to half the laser pulse length, a local measurement of the density at the position of the interaction is obtained. The timing of the collision given by the absolute and relative delays between seed and pump gives a measure of the position localized both in space and in time.

To measure the plasma density a seed and pump laser beam from a Ti : sapphire laser system with a central wavelength $\lambda = 800$ nm, and a spectral bandwidth full width at half maximum $\Delta \lambda_{\text{FWHM}} \approx 20$ nm are focused into either side of a 300 μ m diameter, $L_c = 4$ cm long plasma channel. A beam splitter partitions the energy between the two beams. Ninety per cent is used as the pump while the remaining 10% is used as a seed. A delay line in the seed beam line varies the relative time of injection of the seed into the plasma compared to the pump. In this manner, it is possible to choose the region of interaction and, therefore, the region where the density measurement will be performed. The SRS growth factor is estimated as $\Gamma = 4.2 \times 10^{12} \text{ s}^{-1}$. The duration of the interaction is limited to t' = 48 fs, leading to an expected gain of $\approx 36\%$ in intensity given by the numerical calculation. Gain measurements were obtained by recording seed spectra with and without the presence of the pump in the channel. $q(\omega)$ is calculated as $g(\omega) = (I'(\omega) - I(\omega))/I(\omega)$ and gain of $\approx 20\%$ on average is measured. The frequency difference between the Stokes and anti-Stokes satellites is observed to be constant over most of the measurement range, suggesting that the electron plasma density is constant. Figure 13 presents the results of the electron density calculated from the frequency difference between the Stokes and anti-Stokes satellites. The abscissae give the relative delay to relative position of interaction inside the capillary.



Figure 13. Plasma density measured along capillary using Raman amplification.

As expected the density, within the error measurements, is constant inside the capillary and decreases at the extremities of the measurement length. The measured density is evaluated as 6.5×10^{17} cm⁻³. The length over which it is possible to obtain experimental data is 22.5 mm, which is shorter than the actual capillary length. To explain this result it has to be remembered that a density gradient exists between the ends of the capillary and the vacuum chambers, which can reduce the plasma density. Moreover, this decrease in plasma density is accentuated by the tapering of the waveguide by the laser. The diameter of the capillary can reach 600 µm at both extremities which leads to a drop in density by a factor of four at the end of the capillary. As the Raman gain is density and intensity dependent, there is a value below which it becomes experimentally not possible to observe the Raman satellites.

5. Radiation source development

The ALPHA-X project is focused on LWFA in preformed plasma channels driven by 50 fs, 1 J, 800 nm laser pulses, and injected by 100 fs, 100 pC electron bunches derived from a conventional photoinjector described above. Alternative alloptical injection schemes are also being developed at RAL and Strathclyde. The goal will be to accelerate the short duration electron bunches to an energy of about 1 GeV. For these conservative estimates we hope to obtain an emittance $\epsilon_n < 1 \text{ mm mrad (Fritzler et al. 2004)}$. The main challenge will be to realize an energy spread $\delta \gamma / \gamma \leq 0.01$, where is the FEL gain parameter (Bonifacio et al. 1989, 1991), which is necessary to achieve a high single-pass gain in the proposed FEL amplifier. We have calculated the synchrotron radiation peak brilliance for a 6 fs electron bunch for a 17 kA beam with an emittance of 1 π mm mrad and a relative energy spread $\delta \gamma / \gamma \approx 1\%$, as shown in figure 14.

The FEL (Colson 2001) is a unique source of coherent EM radiation because of its simplicity: the amplifying medium consists of an electron beam in vacuum



Figure 14. Calculation of the X-ray beam brilliance of synchrotron radiation and FEL output as a function of photon energy for a 1 GeV beam.

subject to a spatially periodic magneto-static field (undulator) which enables transfer of energy between electrons and EM wave. The ponderomotive force arising from the Lorentz force of the combined magnetic fields of EM wave and undulator gives rise to bunching of the electron beam, which results in coherent radiation at a Doppler up-shifted frequency. The absence of a solid or gaseous amplifying medium allows the FEL to attain extremely high powers and broad tuneability. Tuning of the FEL wavelength, which is given by $\lambda_{\rm u}(1+a_{\rm u}^2)/2\gamma^2$, can be achieved by varying γ or the undulator parameters ($a_{\rm u}$ and $\lambda_{\rm u}$, respectively). Several X-ray FELs are being developed as fourth generation light sources at centres throughout the world. The ultimate goal of these projects is to reach the water window and beyond using a SASE FEL amplifier driven by a GeV electron beam. When complete, these X-ray sources will produce bright and coherent X-ray pulses with durations of the order of the electron bunch duration. One drawback of SASE amplifiers is that they are essentially noise amplifiers and have spiky and fluctuating outputs (Bonifacio 2005; Bonifacio et al. 2005) and it is not yet known whether they will have good spectral and temporal properties.

However, superradiance (Jaroszynski 1997; Jaroszynski et al. 1997, 2000b), self-amplification of coherent spontaneous emission (SACSE; McNeil et al. 1999, 2000) and amplification of an injected signal are ways of improving the temporal characteristics of the X-ray pulses. As X-ray SASE FELs are extremely expensive devices, it is very important that they produce useful output. If ways are found to produce an electron bunch microstructure with Fourier components at the resonance frequency, a large stable 'spontaneous' coherent signal will act as an (intrinsic) injection source in the FEL amplifier (i.e. SACSE FEL; Wiggins et al. 2000). This may be achievable using future laser-plasma accelerators because their predicted electron bunch durations can approach one femtosecond or less. The growth in intensity of an injected or spontaneous field in a FEL amplifier is given by $I = I_0 \exp(gz)$, where z is the propagation distance, $g = 4\pi\rho 3^{1/2}/\lambda_{\rm u}$, is the small signal gain and ρ is the FEL gain parameter (Bonifacio *et al.* 1989, 1991) which is a function of the beam energy γ , peak current $I_{\rm pk}$ and normalized emittance $\epsilon_{\rm n}$. For a matched electron beam, the FEL parameter is given by $\rho = 1.1 \gamma^{-1} B_{\rm u} \lambda_{\rm u}^{4/3} I_{\rm pk}^{1/3} \epsilon_{\rm n}^{-1/3}$, where $B_{\rm u} (\approx 1 \text{ T})$ is the undulator magnetic field. The matched electron beam radius for electron beams from laserplasma accelerators ($\epsilon_n < 1 \text{ mm mrad}$) is of the order of the plasma wake wavelength, giving $\rho \approx 0.01$ –0.02, for the electron beam parameters expected from a laser-plasma accelerator, and a gain length $L_{\rm g} = \lambda_{\rm u}/(2\pi\sqrt{3}\rho)$ of less than 10 undulator periods, which is sufficient to obtain saturation in a 200 period, $\lambda_{\rm u} =$ 1.5 cm, undulator and should be achievable over a wide wavelength range. We need $\delta \gamma / \gamma < p$ and $\epsilon_n < 4\lambda \beta \gamma \rho / \lambda_u$ or $\epsilon_n < \gamma \lambda$ (matched). A 4 nm source assuming a 1 GeV beam with 100 pC charge and a duration of 10 fs we get a peak current of $I_{\rm pk} = 10$ kA we get a $\rho \approx 0.005$, which gives a gain length of $10\lambda_{\rm u}$ and a constraint on the energy spread of $\delta \gamma / \gamma \approx 1\%$, which may be achievable. To achieve saturation we need about 100–200 undulator periods. FEL sources at X-ray wavelengths are less compact because the dependence of the gain on electron energy $\rho \propto \gamma^{-1}$ leads to a lower gain and, therefore, the requirement of a longer undulator to achieve saturation. The enhancement over the expected synchrotron radiation brilliance is shown in figure 14. To significantly shorten the undulator length SACSE could be used to enhance the start-up power. This has the additional benefit that the nonlinear regime is entered promptly and the superradiant pulses should evolve self-similarly leading to very high efficiencies and extremely short, smooth and stable pulses. Pulses as short as several attoseconds should be feasible in future X-ray FEL sources because the gain bandwidth is automatically increased in this regime. Superradiance and SACSE will be examined in the proposed research programme.

6. Conclusion

Accelerators harnessing the electrostatic forces of laser driven plasma waves have a promising future. They have the potential of producing bright, high peak current relativistic electron bunches with sub 10 fs durations, which would be ideal for driving compact light sources. In addition to reducing the size of next generation accelerators by a factor of 1000, they could also provide useful building blocks for high-energy accelerators. We have reviewed some of the challenges that still need to be met, particularly in controlling the acceleration process and injecting electron beams into a single acceleration stage. We also discussed some of the issues of transporting ultra-short electron bunches between acceleration stages. We examined several promising prebunching techniques, which utilize a laser-driven plasma wave. The main challenge is to reduce the energy spread of wakefield accelerators so as to make them useful as drivers for future compact X-ray FELs. We have used various aspects of the UK ALPHA-X project to illustrate possible solutions to many of the challenges facing developers of light sources based on plasma wakefield accelerators.

707

We acknowledge the Research Councils UK for the support of the ALPHA-X Basic Technology project.

References

- Ayvazyan, V. et al. 2002 Generation of GW radiation pulses from a vuv free-electron laser operating in the femtosecond regime. Phys. Rev. Lett. 88, 104802. (doi:10.1103/PhysRevLett. 88.104802)
- Bingham, R. 2006 Basic concepts in plasma accelerators. Phil. Trans. R. Soc. A 364, 559–575. (doi:10.1098/rsta.2005.1722)
- Bobrova, N., Esaulov, A., Sakai, J., Sasorov, P., Spence, D., Butler, A., Hooker, S. & Bulanov, S. 2002 Simulations of a hydrogen-filled capillary discharge waveguide. *Phys. Rev. E* 65, 016407. (doi:10.1103/PhysRevE.65.016407)
- Bonifacio, R. 2005 Quantum sase fel with laser wiggler. Nucl. Instrum. Meth. Phys. Res. A— Accelerators Spectrom. Detect. Assoc. Equip. 546, 634–638. (doi:10.1016/j.nima.2005.04.003)
- Bonifacio, R., McNeil, B. & Pierini, P. 1989 Superradiance in the high-gain free-electron laser. *Phys. Rev. A* 40, 4467–4475. (doi:10.1103/PhysRevA.40.4467)
- Bonifacio, R., Piovella, N. & McNeil, B. 1991 Superradiant evolution of radiation pulses in a freeelectron laser. *Phys. Rev. A* 44, R3441–R3444. (doi:10.1103/PhysRevA.44.R3441)
- Bonifacio, R., Piovella, N. & Robb, G. 2005 Quantum theory of SASE FEL. Nucl. Instrum. Meth. Phys. Res. A—Accelerators Spectrom. Detect. Assoc. Equip. 543, 645–652. (doi:10.1016/j.nima. 2005.01.324)
- Butler, A., Spence, D. & Hooker, S. 2002 Guiding of high-intensity laser pulses with a hydrogenfilled capillary discharge waveguide. *Phys. Rev. Lett.* 89, 185003.
- Chiou, T. & Katsouleas, T. 1998 High beam quality and efficiency in plasma-based accelerators. *Phys. Rev. Lett.* 81, 3411–3414. (doi:10.1103/PhysRevLett.81.3411)
- Colson, W. 2001 Short wavelength free electron lasers in 2000. Nucl. Instrum. Meth. Phys. Res. A—Accelerators Spectrom. Detect. Assoc. Equip. 475, 397–400. (doi:10.1016/S0168-9002(01)01687-4)
- Coverdale, C., Darrow, C., Decker, C., Mori, W., Tzeng, K., Marsh, K., Clayton, C. & Joshi, C. 1995 Propagation of intense subpicosecond laser-pulses through underdense plasma. *Phys. Rev. Lett.* **74**, 4659–4662. (doi:10.1103/PhysRevLett.74.4659)
- de Loos, M. & van der Geer, S. 2005 General particle tracer user manual, Pulsar physics, Soest, The Netherlands, http://www.pulsar.nl.
- Ersfeld, B. & Jaroszynski, D. 2005 Superradiant linear Raman amplification in plasma using a chirped pump pulse. *Phys. Rev. Lett.* **95**, 165002.
- Faure, J., Glinec, Y., Pukhov, A., Kiselev, S., Gordienko, S., Lefebvre, E., Rousseau, J., Burgy, F. & Malka, V. 2004 A laser-plasma accelerator producing monoenergetic electron beams. *Nature* 431, 541–544. (doi:10.1038/nature02963)
- Fritzler, S. et al. 2004 Emittance measurements of a laser-wakefield-accelerated electron beam. Phys. Rev. Lett. 92, 165006.
- Geddes, C., Toth, C., van Tilborg, J., Esarey, E., Schroeder, C., Bruhwiler, D., Nieter, C., Cary, J. & Leemans, W. 2004 High-quality electron beams from a laser wakefield accelerator using plasma-channel guiding. *Nature* 431, 538–541. (doi:10.1038/nature02900)
- Gordon, D., Hubbard, R., Cooley, J., Hafizi, B., Ting, A. & Sprangle, P. 2005 Quasimonoenergetic electrons from unphased injection into channel guided laser wakefield accelerators. *Phys. Rev. E* 71, 026404.
- Jaroszynski, D. 1997 Superradiance in a short pulse FEL oscillator and its relevance to the X-ray FEL. Towards X-ray free-electron lasers—workshop on single pass, high gain FELs starting from noise, aiming at coherent X-rays, pp. 55–79.
- Jaroszynski, D. & Vieux, G. 2002 Coherent radiation sources based on laser plasma accelerators. Adv. Accelerator Concepts 647, 902–913.

- Jaroszynski, D., Chaix, P., Piovella, N., Oepts, D., Knippels, G., van der Meer, A. & Weits, H. 1997 Superradiance in a short-pulse free-electron-laser oscillator. *Phys. Rev. Lett.* 78, 1699–1702. (doi:10.1103/PhysRevLett.78.1699)
- Jaroszynski, D. et al. 2000a The Strathclyde terahertz to optical pulse source (TOPS). Nucl. Instrum. Meth. Phys. Res. A—Accelerators Spectrom. Detect. Assoc. Equip. 445, 317–319.
- Jaroszynski, D. et al. 2000b Superradiance driven by coherent spontaneous emission in a cherenkov free-electron maser amplifier. Nucl. Instrum. Meth. Phys. Res. A—Accelerators Spectrom. Detect. Assoc. Equip. 445, 261–266. (doi:10.1016/S0168-9002(00)00080-2)
- Khachatryan, A., van Goor, F., Boller, K., Reitsma, A. & Jaroszynski, D. 2004 Extremely short relativistic-electron-bunch generation in the laser wakefield via novel bunch injection scheme. *Phys. Rev. Spec. Top.*—*Accelerators Beams* 7, 121301.
- Kruer, W. 1988 The physics of laser plasma interaction. Reading, MA: Addison-Wesley.
- Kwiet, F. 2003 Generation of ultra-short, high-brightness relativistic electron bunches. Ph.D. thesis, Eindhoven University of Technology.
- Luiten, O., van der Geer, S., de Loos, M., Kiewiet, F. & van der Wiel, M. 2004 How to realize uniform three-dimensional ellipsoidal electron bunches. *Phys. Rev. Lett.* **93**, 094802. (doi:10. 1103/PhysRevLett.93.094802)
- Malka, V. *et al.* 2002 Electron acceleration by a wake field forced by an intense ultrashort laser pulse. *Science* 298, 1596–1600. (doi:10.1126/science.1076782)
- Malkin, V., Shvets, G. & Fisch, N. 1999 Phys. Rev. Lett. 82, 4448. (doi:10.1103/PhysRevLett.82. 4448)
- Mangles, S. et al. 2004 Monoenergetic beams of relativistic electrons from intense laser-plasma interactions. Nature 431, 535–538. (doi:10.1038/nature02939)
- Mangles, S. et al. 2006 The generation of mono-energetic electron beams from ultrashort pulse laser plasma interactions. *Phil. Trans. R. Soc. A* 364, 663–677. (doi:10.1098/rsta.2005.1730)
- Martins, S., Fonseca, R., Silva, L., Tsung, F., Mori, W., Deng, S. & Katsouleas, T. 2005 Threedimensional wakes driven by intense relativistic beams in gas targets. *IEEE Trans. Plasma Sci.* 33, 558–559. (doi:10.1109/TPS.2005.845909)
- McDonald, K. 1988 Design of the laser-driven RF electron gun for the BNL accelerator test facility. *IEEE Trans. Electron. Devices* 35, 2052. (doi:10.1109/16.7427)
- McNeil, B., Robb, G. & Jaroszynski, D. 1999 Superradiance driven by coherent spontaneous emission in the Cherenkov maser. Opt. Commun. 163, 203–207. (doi:10.1016/S0030-4018(99)00135-2)
- McNeil, B., Robb, G. & Jaroszynski, D. 2000 Sacse in a fel amplifier with energy spread. Nucl. Instrum. Meth. Phys. Res. A—Accelerators Spectrom. Detect. Assoc. Equip. 445, 72–76. (doi:10.1016/S0168-9002(00)00116-9)
- Modena, A. et al. 1995 Electron acceleration from the breaking of relativistic plasma-waves. Nature 377, 606–608. (doi:10.1038/377606a0)
- Nakajima, K. et al. 1995 Observation of ultrahigh gradient electron acceleration by a selfmodulated intense short laser-pulse. Phys. Rev. Lett. 74, 4428. (doi:10.1103/PhysRevLett.74. 4428)
- Raubenheimer, T. 1995 Electron beam acceleration and compression for short wavelength fels. Nucl. Instrum. Meth. Phys. Res. A—Accelerators Spectrom. Detect. Assoc. Equip. 358, 40–43. (doi:10.1016/0168-9002(94)01502-3)
- Reitsma, A., Trines, R. & Goloviznin, V. 2000 Energy spread in plasma-based acceleration. *IEEE Trans. Plasma Sci.* 28, 1165–1169. (doi:10.1109/27.893302)
- Reitsma, A., Cairns, R., Bingham, R. & Jaroszynski, D. 2005 Efficiency and energy spread in laserwakefield acceleration. *Phys. Rev. Lett.* 94, 085004. (doi:10.1103/PhysRevLett.94.085004)
- Saldin, E., Schneidmiller, E. & Yurkov, M. 2002 An analytical description of longitudinal phase space distortions in magnetic bunch compressors. Nucl. Instrum. Meth. Phys. Res. A—Accelerators Spectrom. Detect. Assoc. Equip. 483, 516–520.

- Saldin, E., Schneidmiller, E. & Yurkov, M. 2004 Longitudinal space charge-driven microbunching instability in the tesla test facility linac. Nucl. Instrum. Meth. Phys. Res. A—Accelerators Spectrom. Detect. Assoc. Equip. 528, 355–359. (doi:10.1016/j.nima.2004.04.067)
- Shvets, G., Wurtele, J. & Shadwick, B. 1997 Analysis and simulation of Raman backscatter in underdense plasmas. *Phys. Plasmas* 4, 1872. (doi:10.1063/1.872330)
- Spence, D. & Hooker, S. 2001 Investigation of a hydrogen plasma waveguide. Phys. Rev. E 63, 015401.
- Tajima, T. & Dawson, J. 1979 Laser electron-accelerator. Phys. Rev. Lett. 43, 267–270. (doi:10. 1103/PhysRevLett.43.267)
- Trines, R., Goloviznin, V., Kamp, L. & Schep, T. 2001 Generation of fast electrons by breaking of a laser-induced plasma wave. *Phys. Rev. E* 63, 026406. (doi:10.1103/PhysRevE.63.026406)
- van der Wiel, M. et al. 2006 Laser wakefield acceleration: the injection issue—overview and latest results. Phil. Trans. R. Soc. A 364, 679–687. (doi:10.1098/rsta.2005.1731)
- Vieux, G., Ersfeld, B., Jones, D., Lyachev, A., Issac, R., Jamison, S., Reistma, A. & Jaroszynski, D. Submitted. Efficient broad-band Raman chirped pulse amplification in plasma.
- Wiggins, S. et al. 2000 Self-amplification of coherent spontaneous emission in a Cherenkov freeelectron maser. Phys. Rev. Lett. 84, 2393–2396. (doi:10.1103/PhysRevLett.84.2393)
- Wilks, S., Katsouleas, T., Dawson, J., Chen, P. & Su, J. 1987 Beam loading in plasma-waves. *IEEE Trans. Plasma Sci.* 15, 210–217.
- Zholents, A. 2003 Longitudinal phase space control in the Berkeley femtosecond X-ray light source lux. Proc. 2003 Particle Accelerator Conf, vol. 1–5, pp. 872–874.