# Rapid Near-Field Antenna Testing Via Arrays of Modulated Scattering Probes

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Abstract-Key results are summarized of efforts to reduce significantly the near-field measurement time by utilizing one- or two-dimensional arrays of modulated scattering probes in lieu of the single probe ordinarily used in conventional near-field measurement techniques. Results of analytical, numerical, and experimental investigations show that the modulated scattering technique (MST) employing arrays of hundreds or even thousand of modulated scattering probes can be used to map the complex near-field of antennas or scatterers in a few seconds or minutes. The results also strongly indicate that "classical" (nonmodulated) receiving/transmitting arrays can be adapted for rapid nearfield data collection. Major factors affecting the accuracy and speed of probe arrays for near-field measurement are delineated and discussed. Experimental results obtained via laboratory prototype MST systems are also presented and discussed.

#### I. INTRODUCTION

THE KEY results of research and development efforts to L reduce near-field scanning time significantly by utilizing arrays of modulated scatterring probes are presented and discussed in this paper. The work described herein is motivated by the fact that the measurement times associated with the conventional near-field technique employing mechanical positioning of a single probe and/or test antenna can become excessively long for electrically large or sophisticated antennas-telecommunication antennas, phased arrays, multibeam antennas, reconfigurable antennas-which have to be tested for several possible excitations or configurations. The long measurement times associated with conventional nearfield scanning have also been an impediment to the on-site testing of antennas installed on vehicles, aircraft, ships, or located at field sites.

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TABLE I ESTIMATED MEASUREMENT TIMES			
Antenna Size D/λ <sup>a</sup>	Single Probe <sup>b</sup>	1D MST <sup>c</sup>	2D MST <sup>c</sup>
1120 280 70	698 h 44 h 3 h	2 h 20 min 2 min	1.2 h 10 min 40 s
25	25 min	40 s	5 s

<sup>a</sup> NF scan plane size is 2D  $\times$  2D and sample spacing is  $\lambda/2$ . <sup>b</sup> Assumes eight points/s and 2.5 s positioning time between rows. Assumes electronic scan rate of 2000 points/s or  $(4D/\lambda)$  points/s, whichever is greater.

Dramatic reductions in measurement times for antennas as well as scatterers can be achieved via the use of the modulated scattering technique (MST), as evidenced by the estimated measurement times for conventional and MST-based near-field measurement systems presented in Table I [1]-[11]. The MST employs arrays comprised of hundreds or even thousands of electrically small scattering elements, each of whose scattering cross section is successively modulated by a low-frequency modulation signal to map the incident complex electric field of electrically large antennas or scatterers in a few seconds or minutes, depending on whether two-dimensional (2D) or onedimensional (1D) arrays are employed. MST arrays having large numbers of elements are typically more economical to build and deploy than "classical" (nonmodulated) receiving or transmitting arrays since MST arrays do not employ microwave switching networks, and hence only a lowfrequency multiplexer is needed. Some possible measurement configurations utilizing probe arrays are depicted in Fig. 1.

The use of probe arrays, whether MST or classical, introduces new sources of errors in the near-field measurement process. The potential difficulties most frequently cited against the use of probe arrays concern sensitivity and dynamic range limitations, interelement mutual coupling, and the effects of multiple interactions between the test antenna and the probe array. All of these factors may appear a priori to preclude the possibility of achieving high accuracy. However, the results of analytical, numerical, and experimental investigations show that all of the cited factors can be controlled and maintained at acceptable levels through careful design, fabrication and utilization of probe arrays and their associated electronic equipment.

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Fig. 1. Measurement setup for rapid near-field scanning via probe arrays. (a) Fixed antenna and movable test array. (b) Fixed test array and rotated antenna.

The remainder of this paper is organized as follows. The basic operating principles of MST-based measurement systems are briefly reviewed in Section II. Section III is devoted to a review of the effects of major factors affecting the accuracy and speed of MST probe arrays. This part includes previously published key results concerning dynamic range and interelement mutual coupling as well as new results on the effects of MST array-test antenna interactions. Experimental results obtained via laboratory prototype MST probe arrays are presented and discussed for horn and reflector antennas in Section IV. Concluding remarks are presented in Section V.

#### II. PRINCIPLE OF MST-BASED MEASUREMENT SYSTEMS

The MST is essentially a free-space perturbation technique. In that sense it is not the signal delivered by each probe array element to a receiver which is measured, but rather the field scattered by each probe array element. It can be shown via the reciprocity theorem that the signal resulting from the introduction of an electrically small electric field probe at a given measurement point is related to the component of the field  $Ee^{j\theta}$ at that point. In the monostatic case whereby the scattered signal is received by the antenna under test, the signal is proportional to  $E^2 e^{2j\theta}$ . In the bistatic case whereby the scattered signal is received by an auxiliary antenna, it is proportional to  $Ee^{j\theta}$ . The respective advantages of both cases have already been discussed [3], [5]. Briefly speaking, monostatic arrangements suffer from possible  $\pm \pi$  phase ambiguity and from a reduced dynamic range, both resulting from the quadratic relationship existing between the measured signal and the measured field component. However, monostatic setups can nevertheless provide relatively simple and compact solutions for some applications. Originally, the MST was developed to reduce the parasitic effect of the cable necessary to connect the probe to the receiver in conventional measurements [12], [13]. This parasitic effect was particularly disturbing for measurement of near-field aperture distributions. The modulation was thus introduced to compensate for the low sensitivity and to improve discrimination against parasitic signals. In addition to these advantages, modulation makes it possible to record the field along the probe array by sequentially modulating each of the probes. Accordingly, one no longer needs a microwave multiplexer. Instead, only a lowfrequency (LF) or high-frequency (HF) multiplexer is necessary to apply the modulating signal successively to the probes. The modulation of the scattered field by single probes can be realized by several more or less sophisticated techniques which have been abundantly described [14]. It is worth noting that the concept of a modulated probe array for antenna measurements has not been introduced, to the authors' knowledge, before 1982.

A typical MST experimental setup is depicted schematically in Fig. 2. A first coherent detection is achieved at the operating microwave frequency; a second one, at the modulation frequency, provides the real part and the imaginary part of the received signal. In such a setup, the measurement is not appreciably affected by nonmodulated signals that enter the signal channel, provided their level is less than the reference signal level or that they do not saturate the front end of the low noise amplifier, if one is used. These criteria can be satisfied in most experimental situations of practical interest.

#### III. ACCURACY AND SPEED CHARACTERISTICS

It is necessary to analyze and control major factors affecting accuracy, speed, and cost of MST systems. Engineering tradeoffs will probably have to be made to achieve specified levels of accuracy, speed, and cost for specific applications. Six basic factors that can have an impact on measurement system performances are as follows: 1) dynamic range, 2) interelement mutual coupling, 3) interactions between the MST array and test antenna, 4) parasitic signals (modulated and/or unmodulated), 5) dispersion of element scattering characteristics, and 6) probe correction. The results of numerical and

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Fig. 2. Experimental setup for modulated scattering technique for rapid NF testing of antennas.

experimental studies show that the effects of the cited factors can be kept at acceptably low levels through careful design and implementation of the MST system. The effects of dynamic range limitations, interelement mutual coupling, and test antenna-MST array interaction are discussed further in following paragraphs. The influence of parasitic scattered signals from the near-field range is significantly reduced, due to the suppression of unmodulated signals by the homodyne receiver chain. The effects of element dispersion can be removed via a calibration measurement to determine the relative response characteristics of the MST elements to a known incident field. Probe correction for bistatic MST setups employing auxiliary antennas that are more directive than the test antenna can be accomplished with the aid of existing probe correction schemes combined with the calibration of the array element to correct for dispersion in element characteristics. Probe correction for the monostatic MST setups is more complex mathematically because the complex receiver voltage is proportional to the square of the near-field electric field, and conventional probe correction schemese are not directly applicable. Alternative probe correction schemes are under study for monostatic MST setups, as well as for bistatic MST setups employing auxiliary antennas having lower directivity than the test antenna [15], [16]. Fortunately, probe correction is a second-order effect for testing of electrically large antennas using MST arrays of short dipoles or waveguide elements having high symmetry in their scattering patterns.

## A. Effect of Near-Field Dynamic Range on Far-Field Accuracy

The measurement dynamic range is related to the sensitivity and the rate of measurements. Limitation of the dynamic range τ

obviously affects the far-field accuracy. The dynamic range  $(\Delta D)^2$  and the rate of measurement  $\tau$  can be defined in the following way [1], [17], [26]:

$$(\Delta D)^2 = \frac{\Delta W_s}{W_N} \tag{1}$$

$$=\frac{(\Delta D)^2 F k T}{|\Delta \chi|^2 W_a}$$
(2)

where  $\Delta W_s$  is the useful received power related to the input power  $W_a$  of the test antenna according to the following relation:

$$\Delta W_s = |\Delta \chi|^2 W_a. \tag{3}$$

 $\Delta\chi$  can be considered as a transmission or reflection coefficient depending on whether a transmissive bistatic, reflective bistatic, or a monostatic setup is being used. It can be shown that  $\Delta\chi$  is a function of the antenna under test as well as geometrical properties (length, width) of the dipoles and the electrical properties (resistance, capacitance) of the diodes loading them [1], [3], [26]. The noise power  $W_N$  is related to the noise factor F of the receiver, the ambient temperature T, and the measurement rate  $\tau$ , according to the following approximate relation:

$$W_N \simeq \frac{FkT}{\tau} \tag{4}$$

where k is Boltzmann's constant.

A numerical simulation was performed in spherical coordinates to examine the effects of near-field dynamic range limitations on far-field pattern accuracy. This simulation is based on the work done by Jensen et al. [18] and entails the following steps. First, a test antenna is chosen, and its exact near-field is calculated on a spherical surface. In this case, a paraboloidal reflector of  $D/\lambda = 30$  and f/D = 0.5 is chosen as the test antenna, where D is the diameter and f is the focal length. Second, the exact near-field is perturbed by various errors [4] due to different sources, in this case the limitation of the dynamic range and the mutual coupling between probe elements. Third, the exact and the perturbed near fields are transformed to the far fields and the two results compared. The resulting deviations from exact values are then compared with accuracy requirements of the satellite antennas for 1980's [19]: copolarized main-beam directivity of 45  $\pm$  0.1 dBi, pointing direction of  $\pm$  0.01°, and 3-dB beamwidth of 0-0.75  $\pm$  0.01°; cross-polarized lobe of  $-45 \text{ dB} \pm 2 \text{ dB}$  below peak of copolarized main beam. The near-field distribution of the chosen test antenna has a useful dynamic range of the order of 60 dB. It is thus important to investigate the effect of limiting or truncating the near-field dynamic range on the far-field accuracy. This knowledge would also determine the rate of measurements. To simulate the limitation of the measurement dynamic range correctly, an added noise before the microwave synchronous detection is taken into account. Thus independently normally distributed noise using pseudorandom number generating subroutines is added to the real and imaginary parts of the near-field components to simulate the assumed dynamic



Fig. 3. Exact and perturbed cross-polar patterns. (a) For  $\Phi = 90^{\circ}$  for 40-dB dynamic range. (b) For  $\Phi = 45^{\circ}$  for 50-dB dynamic range.

range  $(\Delta D)^2$ . The three dynamic ranges considered are 1)  $(\Delta D)^2 = 60 \text{ dB}, 2) (\Delta D)^2 = 50 \text{ dB}, \text{ and } 3) (\Delta D)^2 = 40 \text{ dB}.$ Some typical results of the far-field characteristics are

shown in Fig. 3. For the above three cases, the copolarized components are hardly affected in the range of  $\theta$  that one is basically concerned with. For the worst case, i.e., the  $(\Delta D)^2 = 40$  dB case, the far-field error for the copolarized peak is 0.036 dBi which is smaller than the 0.1 dBi tolerance previously specified. The cross-polarized deviation is still acceptable (2.7 versus 2) for the  $(\Delta D)^2 = 50$  dB case but considerably exceeds the 2-dB tolerance for the  $(\Delta D)^2 = 40$  dB case. There is a noticeable degradation of the overall accuracy as the dynamic range is reduced from 60 to 40 dB.

Simulations have also been performed for near-field data measured on a cylindrical surface for routine testing of monopulse antennas [5]. For these simulations, the aperture width in terms of wavelength was 40.0. Plots of the far-field amplitude pattern versus angle are depicted in Fig. 4(a) and (b) for parabolic and parabolic-difference aperture distributions, respectively. Curves for dynamic ranges omitted from the plots were not graphically distinguishable from those plotted. These data indicate that even dynamic ranges of only 20 dB may be useful for some applications where the main beam and first few sidelobes of sum or difference patterns of highly directive antennas are of primary interest.

# B. Effect of Mutual Coupling on Far-Field Pattern Accuracy

The mutual coupling between array elements is a source of error in the MST measurements. To calculate this coupling, the mutual admittance matrix of the array has to be evaluated. The model chosen is a linear array of dipoles with element separation  $d = \lambda/2$ . A linear array of 11 dipoles with element length  $l = \lambda/6$ , radius  $a = \lambda/200$  is considered to yield a sufficient degree of accuracy if one wishes to calculate the cumulative effect of coupling upon the central element. Investigation of the mutual admittance matrix of the abovementioned array has shown that the contribution of the elements beyond the fifth element is indeed negligible at the position of the central element. If the measurement distance is relatively large compared to the total length of 11 dipoles, a circular array can also be reasonably approximated by a linear array so far as coupling effects are concerned.

It can be shown [4], [17] by a multiport representation of the measurement setup that the voltage variation  $\delta\rho$  ( $\Delta U0$ ) at the output terminal of the test antenna due to the modulation of the



Fig. 4. Calculated antenna patterns. (a) For parabolic illumination function. (b) For parabolic difference illumination function for indicated near-field dynamic ranges.

pth diode is given by

$$\delta\rho(\Delta U_0) = \frac{-h^2}{I_0} \sum_{m=1}^{N} \sum_{n=1}^{N} E_m E_n \delta_p Y'_{mn}$$
(5)

where  $Y'_{mn}$  is the general admittance matrix with  $\delta \rho Y'_{mn} = Y'_{mn}$  (pth diode reverse biased)  $-Y'_{mn}$  (pth diode forward biased).  $E_m$  and  $E_n$  are the electric fields at the position of the *m*th and *n*th dipole and parallel to it, *h* is the effective length of each dipole, and  $I_0$  is the current at the test antenna terminal. Note that the admittance matrix  $[Y'_{mn}]$  has to be found for each polarization orientation of the electric fields  $E_m$  and  $E_n$  corresponding to the orthogonal orientations of probe elements. Here, for example, the  $\theta$  and  $\Phi$  components of the field.

The method of moments (MM) is utilized to calculate the admittance matrix  $[Y'_{mn}]$ . For the above-specified dipole array, the coupling between two successive elements is calculated to be rather low, of the order of -50 dB [4], [20], [3]. By increasing this value by 10 dB and 20 dB, respectively, two other different cases with higher levels of coupling were simulated to take other possible sources of error into account. For example, introduction of different array elements, sub-



Fig. 5. Sketch illustrating first-order multiple scattering interaction for probe array and test antenna and showing pertinent geometrical parameters.

strate, modulation wires, etc. Three cases are thus treated in all. Measured values of mutual coupling between adjacent MST elements are about 40-45 dB.

A numerical simulation similar to the previous one for the dynamic range effect was to run to evaluate the effect of mutual coupling. After the exact near field of the test antenna is perturbed by the coupling effect, the exact and the perturbed near fields are transformed to the far fields and the deviation between the two is calculated. Comparison of these values— both for the copolarized and cross-polarized cases—with the requirements previously mentioned show that the far-field errors due to the coupling effect of the dipole array fall within the given tolerances, if the cross-polarized level is not much below 40 dB of the copolarized peak.

## C. Effects of Test Antenna-MST Array Interactions

Consideration of the basic near-field scattering and coupling mechanisms associated with MST probe arrays situated in the near field of an electrically large antenna shows that the dominant multiple scattering process for most situations is the one due to the fields designated as 1, 2, and 3 in Fig. 5. In particular, the electric field  $\bar{E}^a$  of the antenna is incident on the probe array. The field  $\bar{E}^{sc}$  scattered from the MST array is then incident on the test antenna, giving rise to the field  $\bar{E}^{sa}$  scattered from the test antenna and which is incident on the MST array. The field  $\tilde{E}^{sc}$  scattered from the MST probe array is determined from the reflected field at the array surface via the application of forward and inverse fast Fourier transforms (FFT's) in accordance with well-known plane-wave spectrum (PWS) antenna analysis integrals [21], where the composite array substrate/MST element reflection coefficient is computed via a specialized moment method code for analyzing metallic elements on dielectric substrate [22]. The field  $E^{sa}$  scattered from the test antenna is comprised of two parts, the "antenna mode" scattered field and the "structural scattering mode" scattered field. The weighting coefficients for these two scattered field constituents are determined by invoking concepts from the theory of scattering from a loaded scatterer [23]-[25]. FFT's are then used to compute the field  $\bar{E}^{sa}$  efficiently at the location of the MST



Fig. 6. Amplitude of electric field for  $20 - \lambda$  test antenna. (a) At antenna aperture. (b) On near-field scan plane at  $X_0 = 10\lambda$ , where  $\lambda$  is wavelength.

probe array, in accordance with the PWS near-field analysis technique previously cited. The computer program GTMINT and the analysis for analyzing multiple test antenna-MST probe arrays interactions are more fully described in [26].

The field  $E^{sa}$  is thus a perturbing field arising from firstorder multiple scattering of the unmodulated near-fields. The multiple scattering process can be continued to obtain the higher order field perturbations. However, the maximum value of the first-order perturbation field is found to be < 0.1 $\bar{E}^a_{\max}$  and the second-order perturbation is <0.01  $\bar{E}^a_{\max}$  for most measurement situations involving reasonably well matched test antennas measured with tall, narrow onedimensional MST arrays that are designed to have low backscatter. Accordingly, only the first-order perturbation, or "error" field  $\bar{E}^{sa}$  is computed over the length of the MST probe array for each horizontal position of the array to obtain the two-dimensional map of the error field on the entire scan plane. The effect of the unwanted error field on the far-field pattern is obtained by superposition of the error field with the unperturbed or "true" field  $\bar{E}^a$  on the scan plane and performing the near-field/far-field transformation.

Plots of relevant near-field and far-field electric field amplitudes are shown in Figs. 6–8 for a simulated measurement situation involving a 20 $\lambda$  reflector antenna and a tall, narrow MST array scanned electronically along its vertical extent and moved mechanically along the horizontal direction. The MST array consists of short ( $\lambda$ /5) dipoles mounted on a thin dielectric substrate having a composite substrate/element



Fig. 7. Amplitude of near-field error field due to first-order multiple scattering between test antenna and MST probe array, for  $X_0 = 10\lambda$ .



Fig. 8. Amplitude of far-field patterns for  $20 - \lambda$  reflector antenna.

field reflection coefficient of  $\Gamma = 0.05$  and width  $W = 0.67\lambda$ . The overall voltage reflection coefficient arising from mismatch of the test antenna with its load is  $\Gamma_L = 0.1$ . The antenna has four struts, and a  $4\lambda \times 4\lambda$  square plate to simulate feed blockage. The aperture distribution produced by the feed is  $(1 - \rho^2)$ . Inspection of the plots shown in Figs. 7 and 8 shows that the error field is marginally significant for this measurement situation. However, the magnitude of the error field can be controlled and reduced further by careful design of the scattering properties of the MST array. For example, reducing the array reflection coefficient from 0.05 to 0.025 would reduce the boresight relative gain error from about -0.5 dB to about -0.22 dB.

### **IV. MEASUREMENTS**

### A. MST Prototype Facilities and Test Antennas

Experimental prototype MST probe arrays have been built and used to conduct feasibility and proof-of-concept tests involving horn and reflector antennas at both the Ecole Supérieure d'Electricité (SUPELEC) and Georgia Tech Research Institute (GTRI) [11], [26]. The measurement setup at SUPELEC pictured in Fig. 9 employs a one-dimensional array in the cylindrical scan geometry illustrated in Fig. 1(b), while the measurement setup at GTRI (not pictured) employs a onedimensional array in a planar scan geometry as per Fig. 1(a) except that the MST array is oriented vertically and moved



Fig. 9. MST setup for rapid cylindrical scanning. (a) From vantage point near location of test antenna. (b) Close-up view of MST dipole elements.

horizontally over the scan plane. Both prototype systems are designed to function in the 4-8-GHz frequency range. The MST probe arrays at SUPELEC and GTRI each consist of 128 printed circuit dipoles mounted on thin (thickness  $\approx$  30 mils) glass epoxy substrate. For the MST array used at SUPELEC, the dipoles have length =  $\lambda/6$  and are spaced  $\lambda/2$  apart at 6.0 GHz. For the MST array used at GTRI, the dipoles have length  $\lambda/5$  and are spaced  $\lambda/2$  apart at 8.0 GHz. Each diode is connected to the LF multiplexer that sequentially applies 25 kHz modulation via resistive or resistively coated lines. However, the two MST probe arrays are configured differently to investigate performance attributes of different probe array designs. The array used at SUPELEC has the dipole probes centered on the substrate and the flat side of the substrate is oriented toward the half-space containing the test antenna. The array used at GTRI has the dipole probes mounted at the edge of the substrate, and the edge is oriented toward the test antenna half-space.

The cylindrical MST setup at SUPELEC has been used to measure the complex near-field of two different horn antennas and a prime-focus fed parabolic reflector antenna. Most of the measurements have been conducted at frequencies from 5.8 to 6.1 GHz. The first horn tested is a nonuniform pyramidal horn constructed at SUPELEC and having an aperture of  $5\lambda \times 7\lambda$ (at 6.0 GHz) in the E-plane and H-planes, respectively. The second horn is a C-band standard gain horn (Scientific Atlanta model 12-3.9) having E-plane and H-plane dimensions of about  $3.2\lambda \times 4.2\lambda$  at the test frequency of 5.8 GHz. (This horn was provided and calibrated by the Technical University of Denmark.) The reflector antenna has (F/D) ratio of 0.5, and the diameter is 43.3 in, or about  $22\lambda$  at 6.0 GHz. For the MST measurements, the test antenna is rotated continuously while the MST array is scanned electronically along its length. The electronic scanning speed is selectable between 200 and 2500 points/s. Conventional measurements were made in the usual way by mechanically positioning a dielectrically filled X-band waveguide probe in the vertical direction for each angular position of the antenna. The test antenna was measured at the same sample points for both measurement techniques.

The planar MST setup at GTRI has been used to conduct 1) monostatic and bistatic MST measurements of a commercial (SA) standard gain horn of the same type as the one tested at SUPELEC and 2) bistatic MST measurements of a 48-in diameter prime-focus fed parabolic reflector antenna fed with an azimuth-only monopulse feed. These tests were conducted at 5.5 GHz. Accordingly, the horn aperture has E- and Hplane dimensions of  $3\lambda \times 4\lambda$ , respectively, while the monopulse reflector antenna has a diameter of  $\approx 22.3\lambda$ . The f/D ratio of the reflector is 0.5. The near field measurements of the monopulse reflector antenna were conducted with the feed assembly electrically misaligned by a small amount to investigate the accuracy of MST probe array measurements vis à vis conventional measurement for characterizing the radiation patterns and tracking error curves for inadvertently misaligned antennas that may be encountered in practice. For the MST measurements, the MST array is mechanically scanned in the horizontal direction while the array is scanned electronically along its length in the vertical direction at a rate selectable between 100 and 2000 points/s. The auxiliary horn for the bistatic MST arrangements was a small horn located either below the test antenna or off to the side. Conventional measurements were also made in the usual way by moving a waveguide probe over the two-dimensional scan plane. The MST data and conventional data were typically measured at the same sample points.

#### **B.** Experimental Results

1) Pyramidal Horn Test Antennas: MST probe array and conventional results for the pyramidal horn test antennas are shown in Figs. 10–13. The data presented in Figs. 10–12 were obtained via the cylindrical scanning setup at SUPELEC, while the MST data presented in Fig. 13 were obtained via the planar scanning setup at GTRI. Close agreement is obtained between the MST probe array data and conventional data over the first 16–20 dB of dynamic range for the near-field and far-field plots. Note that the near-field measurement scanning times are indicated parenthetically on selected figure captions.

2) Reflector Antennas: MST and conventional results for the reflector antennas are shown in Figs. 14-17. Fig. 14 shows plots of the principal-plane patterns of the vertically polarized SUPELEC reflector antenna obtained via conventional and monostatic MST cylindrical scanning at SUPELEC. Numerical pattern predictions computed by the Centre National D'Etudes Spatiales (CNES) are also included. We note here that the measurement duration could be reduced to less than 1 min. by using a faster analog-to-digital converter. Similarly, Figs. 15 and 16 show azimuth patterns of the (misaligned) vertically polarized GTRI monopulse reflector antenna operating in the "difference" mode and the "sum" mode, respectively, obtained via the planar scanning setup at GTRI. Plots of the tracking error voltage versus azimuth angle are depicted in Fig. 17. The tracking voltage error  $V(\Phi)$  was computed from the equation

$$V(\Phi) = \left| \frac{E_{\Delta}(\Phi)}{E_{\Sigma}(\Phi)} \right| \cos \left[ \beta_{\Delta}(\Phi) - \beta_{\Sigma}(\Phi) \right]$$
(6)



Fig. 10. Plots of amplitude and phase of near-field electric fields  $E_z$  for SUPELEC horn. (a) Versus z. (b) Versus  $\Phi_{.}$  ---- MST (45 s); ---- conventional (50 min).



### where

- $E_{\Delta}(\Phi)$  complex far-field electric field for the difference mode,
- $E_{\Sigma}(\Phi)$  complex far-field electric field for the sum mode,
- $\beta_{\Delta}(\Phi)$  phase angle of the difference mode,
- $\beta_{\Sigma}(\Phi)$  phase angle of the sum mode.

Close agreement between the MST probe array and conventional results as well as computed results is obtained over the







Fig. 13. Far-field aximuth patterns for SA standard gain horn measured at GTR1. --- MST (45 s); ---- conventional (40 min).

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Fig. 14. Far-field patterns for 43.3-in-diameter reflector antenna measured at SUPELEC. (a) *E*-plane pattern. (b) *H*-plane pattern. — MST (7 min); ---- conventional (70 min); + + + + numerical predictions.



Fig. 15. Plots of far-field difference pattern for (misaligned) aximuth monopulse antenna measured at GTRI. — MST (3 min); ---- conventional (75 min).

first 25–30 dB of dynamic range for the SUPELEC reflector elevation pattern (Fig. 14) and the GTRI monopulse reflector azimuth difference pattern (Fig. 15). Close agreement over the first 17–22 dB is obtained for the MST probe array and conventional results for the monopulse reflector azimuth sum pattern shown in Fig. 16 as well as for the azimuth pattern for



Fig. 16. Plots of far-field sum pattern for (misaligned) aximuth monopulse antenna measured at GTRI. — MST (3 min); ---- conventional (75 min).

SIN(φ)



Fig. 17. Tracking error voltage versus azimuth angle for (misaligned) 48-in diameter monopulse antenna measured at GTRI. — MST (3 min); ---- conventional (75 min).

the SUPELEC reflector antenna shown in Fig. 14 and most other pattern cuts.

The tracking error curves (Fig. 17) derived from MST probe array data and conventional data show reasonably close agreement over the entire tracking error voltage range. The zero-crossing points for the MST and conventional curves occur at  $-0.91^{\circ}$  and  $-0.80^{\circ}$ , respectively, which yields a zero-crossing location error of  $\approx 2$  mrad for the two measurement techniques.

The experimental results presented herein do not represent optimum or limiting results, and they can evidently be improved to increase accuracy and to include both broad-band frequency sweeping and cross-polarization measurement capabilities. Nevertheless, the results serve to demonstrate the potential of modulated probe arrays for rapid near-field scanning. Analytical and numerical studies indicate that the type of MST probe arrays described herein can be successfully used at millimeter wave frequencies and that useful RF measurement frequency bandwidths spanning at least one waveguide octave can be achieved. Experimental investigations of the millimeter wave performance and the useful RF measurement frequency bandwidths are subjects for future research and development efforts in this area.

#### CONCLUDING REMARKS

The slowness of current near-field measurements constitutes a significant impediment to the progress of near-field antenna testing technology. The MST is one possible solution which does not exclude classical approaches or any other innovative solution. However, the MST offers some attractive performance/cost attributes which render it particularly well suited for antenna testing applications as well as for general near-field applications where the speed/accuracy trade-offs are favorable for probe array scanning. Additional theoretical, numerical, and experimental studies have been initiated to define performance limits better and speed/accuracy/cost trade-offs among MST probe arrays, classical (nonmodulated) probe arrays, and conventional scanning. In closing, we note also that industrial nondestructive testing and biomedical diagnostic imaging are two important non-invasive testing methods which have suffered, until now, from the absence of suitable and rapid probing devices. The rather limited development of near-field microwave imaging and near-zone RCS applications may possibly be explained to a large extent by the lack of efficient means of rapidly acquiring and displaying data [27]. MST probe arrays as well as classical (nonmodulated) probe arrays should find additional applications in these areas in the near future.

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