



BNL-113314-2016-JA

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Submitted to Journal of Physics: Condensed Matter

August 2016

Center for Functional Nanomaterials

Brookhaven National Laboratory

**U.S. Department of Energy
USDOE Office of Science (SC),
Basic Energy Sciences (SC-22)**

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1. Abstract

Block-copolymers self-assemble into diverse morphologies, where nanoscale order can be finely tuned *via* block architecture and processing conditions. However, the ultimate usage of these materials in real-world applications may be hampered by the extremely long thermal annealing times—hours or days—required to achieve good order. Here, we provide an overview of the fundamentals of block-copolymer self-assembly kinetics, and review the techniques that have been demonstrated to influence, and enhance, these ordering kinetics. We discuss the inherent tradeoffs between oven annealing, solvent annealing, microwave annealing, zone annealing, and other directed self-assembly methods; including an assessment of spatial and temporal characteristics. We also review both real-space and reciprocal-space analysis techniques for quantifying order in these systems.

2. Introduction

Self-assembly is a conceptually beautiful paradigm for constructing nanomaterials. The desired structure is encoded within the architecture of the molecules themselves. Pattern formation is spontaneous, driven by energy-minimization, with molecules organizing according to inter-molecular and intra-molecular association [1]. Because self-assembly is a stochastic process, assembly kinetics are of paramount importance. Although equilibrium thermodynamics in principle dictates the preferred structures, the actual order obtained may depend on non-equilibrium effects, local fields, kinetic traps, and pathway-dependent ordering [2]. Pragmatically, ordering timescales also influence the extent to which self-assembly can viably be scaled to widespread applications. This review thus delves into the ordering kinetics of self-assembling block-copolymer materials.

Block-copolymers (BCPs) represent a versatile and well-studied self-assembly motif [3-7]. Chemically distinct polymer segments are covalently connected. Chemically incompatible polymer chains experience a strong driving force towards macrophase separation [8]. However, the covalent attachment of the copolymer architecture frustrates this tendency. The compromise is for the chemically-distinct chain segments to segregate locally—“microphase separation”—which results in the formation of nanoscale morphologies that minimize interfacial area, and chain stretching [3]. Linear diblock-copolymer chains segregate into morphologies dictated by the relative volume fraction of the two blocks (Figure 1a) [9-11]. Symmetric diblock chains give rise to alternating lamellae morphologies. Slightly asymmetric chains give rise to cylinders (of the minority phase) arranged in a hexagonal lattice (within a matrix of the majority phase). Greater asymmetry gives rise to spheres arranged in a body-centered cubic lattice. The diblock-copolymer phase diagram can also include regions with more exotic morphologies, such as gyroid or perforated lamellae [3, 9, 12]. More complex polymer architectures, including triblock [4, 13-20], multi-block [21-23], and bottle-brush [24-27] copolymers, can give rise to yet more elaborate morphologies [11, 28, 29]. Chain stiffness also plays a role in assembly; rod-coil and rod-rod diblock systems can be generated using rigid (possibly semiconducting) polymer blocks [30-35]. The assembly of block-copolymers can be strongly influenced by local confinement [18,

20, 36-44]. Most simply, *thin films* of BCPs can exhibit new morphologies, and interface-directing ordering [5, 6, 15, 45-47]. As will be discussed at length in this review article, the order of BCP materials can in fact be influenced in a number of different ways [48-50]. BCPs are responsive to temperature [51-53] and solvent [54, 55] conditions; to thermal [56, 57], shear [58-63], electric [64-67], and magnetic [68-72] fields; and to substrate topography [73, 74] and chemical makeup [75]. One can further broaden the range of possible structures by considering blends of BCPs with other materials: especially nanoparticles [76-81], homopolymers [82-86], and other BCPs [87-96].

This elaborate landscape of morphologies has made BCPs extremely attractive as functional materials [97-99], and as a nanoscale patterning technology [23, 46, 100-104]. Furthermore, one of the key advantages of BCP self-assembly is the wide variety of established methods for converting the organic morphology into other materials [105-107]. Fixed organic structures can be obtained using various chemical treatments, including crosslinking and selective dissolution [105, 108, 109]. Metal replicas of one of the phases can be obtained *via* etching [39, 110-112], nanoparticle infiltration [113, 114], or solution-phase exposure to metal salts [115-119]. Pyrolysis can be used to generate replicas composed of amorphous carbon [114, 120-123], silica [124, 125], vanadium oxide [126], etc. [127, 128]. Selective gas-phase infiltration can load one of the blocks with a precursor, allowing the formation of various oxides (ZnO, TiO₂, Al₂O₃, etc.) [129-134]. These inorganic replicas can be used as lithographic etch-masks, thereby transferring the morphology into substrate topography (Si, Si₃N₄, SiO₂, etc.) [40, 46, 135-142]. This structural and compositional control has led to the suggestion and demonstration of a diverse array of applications [48, 49]. One of the BCP phases can be removed to generate nanoporous materials [109], which may be useful as membranes [143], or as scaffolds for synthesizing nanowires [144]. BCP-derived nanomaterials have shown promise for energy applications [145, 146], including as battery electrolytes [29, 147-153] and electrodes [154, 155], capacitors [156], solar cell materials [35, 157-160], and triboelectric generators [161]. The ability to pattern surfaces at the nanoscale [101] has been shown to be useful for generating superhydrophobic surfaces [162, 163], gas [138] or molecular [164] sensors, optical materials [112, 118], and transparent electrodes [119]. More broadly, the ability to generate nano-patterned coatings should have an impact in light-management [165, 166] layers for anti-reflection [167], improved solar cell light harvesting [168-171], and improved light-emission efficiency [172]. BCPs have been extensively investigated as a route towards higher-resolution patterning for electronics and nano-devices [23, 145, 146, 173-175]. While a BCP locally forms a well-defined nanostructure, its position and registry at larger scales can be directed [50, 73-75, 102] using topographic or chemical patterns; so-called directed self-assembly (DSA) patterning [176, 177]. It has been shown that DSA patterns can achieve density multiplication with respect to the guiding pattern [178-182], and that templates can enforce complex local patterns [183, 184] using minimal design rules [180, 185]. Progressively more complex integration of BCPs into realistic industrial microelectronic workflows has been demonstrated [39, 183, 186-191]. BCPs may thus play a role in future electronics and memory devices (resistive [192, 193], phase-change [194, 195], or magnetic bit-patterned media [137, 196, 197]). As the complexity of possible patterns increases (Figure 1b-e) [39, 119, 180, 183-185, 198-202], the range of potential applications correspondingly broadens.

In order for BCP materials to fully realize their enormous potential, a variety of outstanding challenges must be addressed [57, 203-205]. Firstly, the local nanoscale morphology must be controlled. The local *orientation* can be tuned using interfacial energy [75], film thickness, and thermal or solvent conditions. The local nanoscale *shape* is more difficult to influence [119, 141], since the morphology emerges spontaneously due to energy-minimization. On the other hand, the morphology can be influenced by confinement [44], or non-native lattice symmetries can be constructed by stacking multiple self-assembled layers [119, 141, 206-210]. This review will touch on many of these methods of local control. Secondly, self-assembly does not generically afford long-range control of the orientation or registry of the nano-objects. We note that for many applications, only relatively local (mesoscale) order matters. For instance, the optical, electrical and wettability properties of coatings is influenced by the local shape, orientation, order, and perfection of nanostructures, but not influenced by long-range order. On the other hand, anisotropic material properties require wide-area (macroscopic) control of nanoscale orientation, and device applications in microelectronics require stringent control of long-range registry. This review will discuss and distinguish the ordering in both of these regimes: mesoscale, and macroscopic. Finally, the timescales of self-assembly are frequently unacceptably long. For instance, microelectronic workflows involve numerous steps, where a timescale of only seconds or minutes can be tolerated for any given step. By comparison, conventional ordering of BCPs requires hours or days of oven annealing. This review article summarizes the state of the art with respect to block-copolymer ordering kinetics, describing both the current best fundamental understanding of the ordering process, as well as pointing towards promising techniques for accelerating BCP self-assembly. Though several challenges remain, a range of options now exist to enable rapid and efficient ordering of block-copolymers (Figure 2).

3. Fundamentals of Block Copolymer Thermal Ordering

Block-copolymer thin films have traditionally been ordered by heating them in a vacuum oven for extended periods (hours to days). BCPs must be heated above the glass-transition temperature (T_g) of both block components, so that the material has sufficient mobility for the morphology to rearrange. Thermal annealing of an as-cast (disordered) BCP film involves first a rapid and local phase-separation of the BCP components, generating a disordered BCP morphology [211]. The BCP morphology then coarsens as thermal annealing proceeds, with the average grain size increasing with time (Figure 3). The coarsening process is dominated by the diffusion and annihilation of topological defects [212-215]. The defects in the morphology (dislocations, disclinations, etc.) [48, 216] behave as quasi-particles that diffuse throughout the material [217, 218]. This diffusion requires chain mobility (for the morphology to locally rearrange), but does not require long-range migration of the chains themselves. As coarsening proceeds, the density of defects continuously decreases, reducing the probability for two defects to encounter and annihilate. Coarsening leads to an increase in grain size (ζ) that scales as $\zeta = kt^\alpha$, where t is time (Figure 3d). The prefactor k sets the overall scale of the kinetics, including the effect of temperature, while the exponent α describes the mechanism of ordering. For thin films, ordering is quasi two-dimensional (2D), and one expects $\alpha = 0.25$, with experimental values being in the

range [215, 216, 219-223] $\alpha \approx 0.25\text{--}0.28$ for sphere and cylinder morphologies, and closer to 0.1 for lamellae [213, 222] (Figure 4). By comparison, bulk materials have three-dimensional (3D) freedom, and exhibit [212, 224] $\alpha \approx 0.5\text{--}1$.

The topological defects are deviations from the idealized morphology (Figure 3a and b, example defects are highlighted by red circles), and thus inherently high-energy, requiring the underlying BCP chains to distort unfavorably. Elimination of defects is thus an energetically downhill process. Nevertheless, grain coarsening is limited by both the finite diffusivity of the defects, and an energy barrier for two defects to annihilate (since annihilation requires higher-energy intermediate configurations [225-227]). Fredrickson *et al.* quantified the thermodynamic and kinetic aspects of defects using simulations [225, 226], finding that each defect incurs an energy penalty of order 10–150 $k_B T$, and elimination of a single defect pair involves a pathway with 1–4 energy barriers, of height $\sim 1\text{--}20 k_B T$, giving rise to the observed activation energy (E_a). Increasing temperature (T) increases the diffusion velocity of defects, and also provides the necessary energy to overcome the barrier to annihilation; this dependence can be captured in an Arrhenius relation [213, 217, 228-230]:

$$k = A e^{-E_a/k_B T} \quad (1)$$

where k_B is the Boltzmann constant, E_a is the activation energy, and A is a prefactor accounting for other aspects of ordering. The prefactor accounts for the overall scale of the kinetics, including factors such as the mobility and collision frequency of defects. This parameter is thus influenced by material properties such as the diffusivity of BCP chains. For instance, high molecular-weight BCP materials have slow chain diffusion, and correspondingly slow ordering kinetics (smaller A). While the ordering exponent (α) allows one to assess the mechanism of ordering, and thus to qualitatively compare the ordering process inherent to different annealing protocols, the prefactor (A) sets the overall scale of the kinetics, and is thus crucial in assessing the viability of a given ordering protocol in, *e.g.*, an industrial setting. Different ordering methods influence not just the exponent, but also the prefactor (Figure 4). Thus, kinetic enhancements can arise both from accessing new ordering mechanisms, as well as by accelerating known pathways.

It is important to note that the temperature-dependence of BCP coarsening is not strictly Arrhenius, due to the multiple energy barriers [225, 226] and temperature-dependent material properties [228, 231, 232]. Moreover, as T is increased, the BCP approaches the order-disorder transition (ODT). That is, the segregation strength (χ) is temperature-dependent (Figure 5a), $T \sim 1/(\chi N)$, where N is chain length [233-236]. Nevertheless, BCP ordering is frequently analyzed as an Arrhenius process, where the activation energy is found to be on the order of [213, 217, 228, 229, 237, 238] 50–400 kJ/mol.

Given the favorable scaling of kinetics with annealing temperature, an obvious approach to rapid assembly is simply to increase temperature. However, one is inherently limited by the order-disorder transition temperature (T_{ODT}), above which phase separation no longer occurs and the two block materials mix freely (forming a disordered state). In practice, material degradation temperatures may also be limiting. For instance, polystyrene degrades at [239] $\sim 380^\circ\text{C}$,

polyethylene ~420°C , poly(methyl methacrylate) [240] ~330°C, polyvinylpyridine [241] ~400°C, poly(ethylene oxide) [242, 243] ~400°C, poly(dimethyl siloxane) [244] ~500°C, etc. In most cases, researchers limit themselves to $T < 250^\circ\text{C}$ to avoid possible degradation issues. Rapid thermal processing (RTP) was used to investigate high temperatures (up to 350°C) [237, 245, 246], where it was found that initial ordering was enhanced ($\alpha \approx 0.3$), quickly plateauing to the usual behavior ($\alpha \approx 0.1$). Overall, this enables significant grain sizes within ~100 s.

Ultimately, ordering of a BCP morphology results from the rearrangement of the underlying polymer chains. Thus, the microscopic molecular properties (*e.g.* polymer relaxation times) play a crucial role in dictating ordering kinetics (Figure 5). Conversely, the morphology influences molecular properties, such as the diffusion of block-copolymer chains. For instance, in lamellar systems, chains diffuse readily within the lamellar plane, but there is an energy barrier for chains to diffuse in the perpendicular direction (*i.e.* to hop between layers), giving rise to diffusion coefficients approximately one order-of-magnitude lower in this direction [222, 247-249].

Spin-cast BCP films are typically initially disordered; but this state is meta-stable, since the material is well below T_{ODT} , and will rapidly phase separate as soon as mobility is induced (by heating above T_g). Heating disordered films results in homogeneous phase separation throughout the entire material, with subsequent grain growth involving some grains growing at the expense of others (Figure 3a,b). Alternatively, BCPs can be ordered by heating the material above T_{ODT} (into the disordered phase), and cooling through the order-disorder transition. In this case, one instead observes nucleation and growth of isolated ordered grains (in a surrounding of disordered material). These grains typically grow anisotropically (yielding grains with ellipticity ~ 2) [250-253], with front velocities on the order of 10 $\mu\text{m}/\text{min}$. The kinetics of grain growth within this supercooled regime was studied in detail by Fredrickson and Binder [254]. The energy barrier for nucleation of ordered grains is quite small and decreases with quench depth; for substantial quenches, rapid homogeneous nucleation is inevitable (*i.e.* growth of individual, isolated grains occurs only in the vicinity of T_{ODT}). The timescale for conversion to an ordered state follows:

$$t_{\text{ord}} \sim \frac{N^{1/12}}{\delta^{3/4}} \tau_d e^{\Delta F / 4k_B T} \quad (2)$$

where τ_d is the polymer relaxation time, δ is proportional to the undercooling, and ΔF is the excess free energy of formation of a droplet of ordered material.

Conventional thermal annealing can only, realistically, ever offer mesoscale ordering. The kinetics of assembly are too slow for macroscopic grain sizes to be obtained over reasonable timescales. If macroscopic order is desired, some other method must be used to select a preferred orientation, or template large grains. In this review, several techniques which afford this level of control are discussed. From the point-of-view of conventional annealing, these techniques represent an enormous kinetic speedup ($\sim 10^{20}$).

The intrinsic sizescale of a BCP morphology leads to interesting commensurability effects. For instance, a BCP material confined between two hard walls will form an integer number of morphological repeats within the available space, at the expense of distorting L_0 from its bulk equilibrium value [255]. Yet this distortion is manifestly high-energy; if a BCP thin film is cast

on a substrate with a free surface, one will instead see a smooth flat surface when the film thickness admits an integer number of BCP repeats. But if the average film thickness is not commensurate, the BCP will respond by nucleating ‘holes’ or ‘islands’ at the surface [256-258]. That is, the free surface will partition itself into regions slightly thicker and thinner than the average thickness (with the quantized thicknesses having a height difference of L_0), so that any given spot admits an integer number of layers. For a lamellar film under symmetric wetting conditions (the same block wets the substrate and free surface), the film is commensurate for any thickness nL_0 , where n is an integer. For asymmetric wetting (different block wets substrate vs. surface), commensurability occurs for $(n + \frac{1}{2})L_0$. For sphere and cylinder morphologies, one must consider the correct layering distance, and account for any substrate-wetting brush [46]. If either the substrate or free interface is near-neutral, one can also form half-height ($0.5 L_0$) surface features [259].

Thicknesses slightly above commensurability have an excess of islands on their surface; those slightly below commensurability exhibit holes; intervening thicknesses can display bicontinuous surface features [260]. These surface features nucleate as small, smooth bumps/divots, which then grow in size and exhibit relatively sharp walls [261, 262]. The appearance of these features is preceded by an incubation phase [258, 263, 264]: a meta-stable state where the film is nominally flat. The timescale for initial nucleation depends sensitively on film thickness, with near-commensurate thicknesses exhibiting long (>10 hours) incubation, while ‘maximally incommensurate’ thicknesses (exactly between two commensurate conditions) nucleate rapidly (tens of minutes) [265]. The additional surface area of these surface features introduces an energy penalty, which causes these features to limit their perimeter, and to coalesce as annealing proceeds [266, 267]. Yet their evolution involves the organized motion of many polymer chains; nucleation and growth occur on timescales of hours [258, 267], with coarsening following a power law as a function of time [268].

Film thickness affects BCP morphologies. Thin film confinement can give rise to morphologies that deviate from the bulk equilibrium expectation [15, 45, 47, 269, 270], or induce reorientation [15, 271-274]. Local film thickness (*e.g.* at a step in thickness) can also induce local morphological changes [272, 275, 276]. Given this coupling between thickness and morphology, it is not surprising that film thickness also affects ordering kinetics. Generally, thicker films order more rapidly. A limiting case is to compare bulk materials, which have freedom to order in 3D, to thin films, which are confined to quasi-2D ordering. Coarsening follows $\xi \sim t^\alpha$, where bulk films exhibit [212, 224] $\alpha \approx 0.5-1$, while 2D films order with a less favorable [215, 216, 219-223] $\alpha \approx 0.25$. For thin films annealed at a certain temperature and time, the grain size is larger for thicker films, scaling as $\xi \sim h^\beta$, where h is thickness, and [223, 274, 277, 278] $\beta \approx 0.4-1$. The faster ordering in thicker films can be attributed to the decreased influence of confinement and substrate effects. Increasing ordering kinetics using thickness is not generally viable: the kinetic increase is marginal, and other aspects of a particular use/application typically restrict the film thickness that is acceptable. Moreover, beyond a certain thickness, one no longer obtains grains that span the entire film thickness, increasing the effective disorder.

4. Characterizing Order in Block Copolymer Thin Films

A key question, when assessing self-assembling ordering rates, is how best to quantify the order that develops in the system. The appropriate metrics depend on the intrinsic shape and symmetry ordering of the system, as well as the length-scale over which the order persists. For block-copolymer thin films, we can distinguish between different regimes. Early in the phase separation process, or close to the order-disorder transition (ODT) boundary, order will be only extremely local. One can characterize the system by the interfacial width (W) between the two block components [279-281]:

$$W = \frac{a}{\sqrt{6\chi}} \quad (3)$$

where a is the polymer statistical segment length. The interaction parameter (χ) is temperature-dependent, with an entropic (χ_S) and enthalpic (χ_H) contribution [234]:

$$\chi(T) = \chi_S + \frac{\chi_H}{T} \quad (4)$$

Figure 5a shows the variation in χ for various BCPs (PS-*b*-PMMA [233-235, 282], PS-*b*-PVP [283-285], PS-*b*-PEO [286], PS-*b*-PI [233], and PS-*b*-PDMS [287, 288]). Near ODT, the interfacial width increases as the two block components begin to mix, and diverges as one crosses ODT. As temperature is lowered, and effective segregation strength increases, the interfaces become sharper (W decreases). Spin-cast BCP films are frequently in kinetically-trapped disordered configurations, and require oven annealing (above T_g) to induce mobility and allow the system to evolve into an ordered state. Thus, one can use the interfacial width, W , as a measure of the extent of phase separation during this early-stage ordering.

This initial phase separation is typically extremely rapid. BCP ordering is thus dominated by the next regime, wherein the morphology has developed, defects diffuse and annihilate, and order thus improves. These states are ‘poly-grain,’ with an assortment of domains/grains of different size, separated by defective grain-boundaries. The system is well-ordered locally (at the scale of 1–20 L_0), but disordered globally; we can refer to this as the mesoscale ordering regime. One can thus characterize order using the areal or volumetric density of defects (ρ_d). The most popular metric, however, is to measure the average grain size (ζ); *i.e.* the distance over which the nanoscale morphology is coherent. In principle, the enthalpy-minimum for a BCP system is to generate a single grain throughout the entire macroscopic dimensions of the sample. In practice, such a condition requires impractically long annealing times. On the other hand, a wide variety of methods are available to direct BCP ordering. For instance, shear-alignment can break the two-dimensional powder symmetry of a thin film, giving rise to a morphology aligned along a particular direction. In this macroscale ordering regime—where long-range correlations have been established—the grain size does not provide a meaningful description of the system. Depending on how ζ is measured, it may in fact diverge to infinity in such a system, since (certain) correlations persist over arbitrary distances [57, 289]. In such cases, one can instead focus on counting the density of remaining topological defects (ρ_d); or one can measure the deviation of the system from idealized mono-domain order. For instance, the orientational spread

of the morphology, about the average alignment direction, can be considered (σ_ϕ). The Hermans order parameter (S) can be computed by averaging the local angles (ϕ) of the morphology with respect to the ‘director’ (alignment direction) [278, 290-292]:

$$S = \langle P_2(\cos \phi) \rangle = \frac{3\langle \cos^2 \phi \rangle - 1}{2} \quad (5)$$

where P_2 is the second Legendre polynomial. The order parameter allows a simple interpretation: a disordered system with completely random orientations yields $S = 0$, a perfectly-aligned system yields $S = 1$, and a perfectly anti-aligned system yields $S = -1/2$. Intermediate values of S (between 0 and 1) allow one to sensitively characterize and compare orientational order. In two-dimensions (2D) one can instead use [289]:

$$\begin{aligned} S &= 2\langle \cos^2 \phi \rangle - 1 \\ &= \langle \cos(2\phi) \rangle \end{aligned} \quad (6)$$

Once a metric has been selected, the ordering kinetics are of course established by probing this metric as a function of ordering time. As previously discussed, BCP ordering typically follows a power-law, with metrics (such as grain size) improving rapidly in initial phases, and then growing progressively more slowly as defects become more dilute.

4.1. Realspace methods to characterize order

Conceptually, the simplest way to characterize a morphology is to directly visualize it. In later stages of ordering, incommensurate BCP thin films may form island/hole surface patterns [256-258]. These can be visualized using optical microscopy,[260] and their size/shape tracked over time [267]. This allows the latest stages of assembly to be analyzed relatively easily. The nanoscale morphology of a BCP, however, is well below the wavelengths of visible light, making optical microscopy inapplicable to measuring the metrics of greatest interest (ξ , ρ_d , S , etc.). On the other hand, Ullal *et al.* [293, 294] demonstrated how stimulated emission depletion microscopy (STED) could be used to image a BCP phase doped with a block-selective fluorophore, with sub-diffraction-limit resolution. Pollard *et al.* used infrared-based scanning near-field optical microscopy (SNOM) to yield spectroscopic imaging of a BCP with nanometer spatial resolution [295]. It is conceivable that other super-resolution microscopy [296, 297] methods could be adapted to BCP imaging.

By far the most common means of assessing BCP morphologies is realspace visualization with atomic force microscopy (AFM) or scanning electron microscopy (SEM). Both techniques allow the morphology at the top-surface of a thin film to be imaged. However, both are encumbered by a perennial issue in BCP imaging: the morphology of interest may be buried under a wetting-layer of the lower surface-energy component. AFM operating in intermittent-contact (‘tapping’) mode can image the subsurface morphology; this is especially evident in the phase image. For SEM imaging, a development step is usually required, such as a brief etching (*e.g.* with O_2 plasma) to remove the surface layer and differentially consume the two block components. For some BCP materials, such as PS-*b*-PMMA, one can use UV irradiation to crosslink the PS phase,

and acetic acid exposure to remove the PMMA phase, thereby generating height contrast visible in SEM. In any case, SEM imaging of these organic materials is usually improved by depositing a thin metal layer (*e.g.* 5 nm Pt), which reduces charging effects. As demonstrated by Hexemer *et al.* [298], the throughput of these imaging modes can be enhanced by using wide-area images and analyzing the Moiré patterns. The interference between the regular pattern of the BCP morphology, and the regular grid of the microscope scanlines, gives rise to a visual ‘beating.’ These Moiré patterns can be rigorously analyzed to determine the local BCP morphology, even though the repeat-spacing is below the nominal scan resolution. As such, orientational order and grain size can be evaluated.

AFM requires no preparation of the material for imaging, and can even allow the morphology to be imaged during ordering (*e.g.* using a heated sample stage), allowing coarsening kinetics at video rate to be measured [299, 300]. In this sense, AFM provides the only truly non-destructive realtime measure of BCP ordering. SEM cannot measure structure in realtime; however, kinetic history can be established from SEM data by preparing a series of samples quenched at various points in the history. The temporal resolution possible in such a case is limited not by the technique itself, but by the quench protocol (resolution better than ~seconds is challenging).

In order to extract quantitative measures of order from AFM or SEM micrographs, image analysis can be used. A variety of techniques have been described in the literature. Murphy *et al.* provide a detailed description and integrated implementation of a suite of useful analysis tools [289]. A fast Fourier transform (FFT) of the image yields a useful reciprocal-space view of the order. The one-dimensional azimuthally-averaged FFT exhibits a peak from the BCP repeat-spacing [301]. Fitting the first peak position (q_0) allows easy computation of realspace repeat-distance ($d = 2\pi/q_0$). One must account for lattice symmetry when interpreting this value. For a lamellar phase, the BCP repeat period is simply $L_0 = 2\pi/q_0$. For hexagonally-packed cylinders [302], the scattering peak directly probes the layering distance between cylinder rows $L = 2\pi/q_0$, with the intercylinder repeat period then being $L_0 = (2/\sqrt{3})L$. The orientation distribution of the morphology can be assessed from the intensity of the FFT peak along the azimuthal direction (ϕ), from which one can compute the order parameter (S) [211, 291]. For well-oriented materials, one can fit the peak along ϕ to a Gaussian, in order to compute the spread, σ_ϕ . A more generalized fit to the orientation distribution is to use a function with circular wrapping, such as [303, 304]:

$$I(\phi) = \frac{1 - \eta^2}{(1 + \eta)^2 - 4\eta \cos^2 \phi} \quad (7)$$

where η is an orientation parameter reminiscent of the order parameter; $\eta = 0$ corresponds to complete and uniform orientational spread, $\eta = 1$ corresponds to perfect alignment, and intermediate values correspond to different amounts of alignment. Another option is to fit $I(\phi)$ to the Maier-Saupe distribution [305]:

$$I(\phi) = \frac{1}{c} \exp [m \cos^2(\phi - \phi_0)] \quad (8)$$

where c is a normalization constant, and m quantifies alignment; $m = 0$ indicates an isotropic distribution, while $m \rightarrow \infty$ indicates perfect alignment.

Images of BCP morphologies can be cleaned using Fourier filtering; *i.e.*, by suppressing or accentuating certain regions of the Fourier space, before performing an inverse Fourier transform back to a realspace image. For instance, if one suppresses all the intensity in the Fourier data outside of a narrow annulus near the morphology peaks, then the corresponding realspace image will have the morphology strongly highlighted [211]. Small-scale fluctuations in the image (large- q in Fourier space), as well as large-scale drift in the image (small- q in Fourier space), will both be rejected in this process. This greatly improves image contrast, and makes morphological features more evident. One must, however, be careful in applying this method to noisy images: by rejecting all data outside of the q presumed to correspond to the BCP morphology, the resulting realspace image will inevitably display structure at the corresponding realspace repeat-spacing. Thus, while Fourier filtering can help to highlight existing morphology, it can mislead by generating a semblance of morphology out of noise in the input image.

The average grain size can be computed from a micrograph. One could manually identify grains and grain boundaries, compute their areas, and thereby measure an area-averaged grain size (ξ_A). A more computationally tractable method is to compute the in-plane orientational correlation length (ξ_o), and use this as a representation of the grain size. The first step is such an analysis is to determine the local orientation of the morphology. For line-patterns (vertical lamellae or horizontal cylinders) this can be done using FFTs in sub-regions of the image [306], by computing the tangents of ‘objects’ identified in the image *via* thresholding and/or segmentation [289], or by measuring local image gradients [56, 215, 216, 229, 278]. In this latter method, spatial derivatives are used to compute local vector orientations for every pixel in the image. For an image with intensities $I(x, y) = I(\vec{r})$, we then compute the orientation map:

$$\phi(\vec{r}) = \frac{1}{2} \arctan \left[\frac{2(\nabla_x I)(\nabla_y I)}{(\nabla_x I)^2 - (\nabla_y I)^2} \right] \quad (9)$$

Note that care must be taken in order for the correct quadrant to be selected in computing the arctan (many programming languages have an ‘atan2’ function for this purpose). This method requires either preprocessing the image to remove features in the image at higher frequencies than the morphology (*via* Fourier filtering, or convolving with a Gaussian) [301], or taking care to compute the spatial derivatives over a length-scale of roughly L_0 . The orientation map itself is extremely valuable. If plotted as false-color, it provides a direct visualization of the grains (regions over which color is conserved), grain boundaries and defects (where color changes abruptly), and meandering of the morphology (where color changes gradually). Refer to Figure 3a,b for examples. The histogram of orientations can be used to assess order or quantify orientational spread (σ_ϕ). One can also compute the orientational correlation function:

$$g(r) = \langle \cos [2(\phi(\vec{r}) - \phi(\vec{r}'))] \rangle \quad (10)$$

where r is a separation distance, and the angle brackets denote averaging over all possible pixel pairs (at positions \vec{r} and \vec{r}') that match the given separation. The correlation function decays as a function of r , with a length-scale characteristic of the spatial persistence, in the original image, of the local orientation of the morphology. One can quantify this by fitting $g(r)$ to an exponential decay (Figure 3c):

$$g(r) = e^{-r/\xi_o} \quad (11)$$

where ξ_o is the orientational correlation length. Large values of ξ_o indicate orientational coherence over large distances (*i.e.* large grains) and good order. Small values indicate small grains and poor order. Note that ξ_o is a fairly stringent measure of order, since it includes contributions both from abrupt changes in orientation (grain boundaries), as well as more subtle meandering of the morphology. It is thus smaller than what one sees ‘by eye’ in the micrograph (*i.e.* smaller than ξ_A). On the other hand, for aligned systems ξ_o can be misleading. If there is a net alignment, then the orientational correlation never decays to zero. The correlation function can still be a useful indicator of order: the decay at small r encodes local meandering of the morphology, while the height of the plateau at large r relates to the overall orientation spread. In general, metrics other than ξ_o should be used for aligned systems (or in cases where grains are larger than the available image size).

For dot-patterns (vertical hexagonally-packed cylinders), the above image gradient method is not applicable. Instead, the locations of cylinder cores can be obtained by thresholding the image and using standard particle localization/counting methods. From there, one can obtain Voronoi plots [223, 307] of the hexagonal order (wherein cells that are not six-sided can be identified as defects), and estimate grain size from the decay of the autocorrelation function [308]. The fraction of cylinders with exactly six nearest-neighbors can be used as another measure of order. One can also compute the orientation of each cylinder core by establishing vectors to its nearest-neighbors, and then determining the angle of the average vector (one must modulo the angle into the range $-\pi/6$ to $+\pi/6$ to account for the six-fold symmetry) [57]. Once an orientation map is obtained, the correlation length can be computed as before (using a value of 6 instead of 2 for symmetry).

Individual topological defects can also be identified and counted using image analysis [309]. Processed images can be segmented into objects/particles, and then skeletonized into thin lines [289]. The connectivity of this network can be analyzed to identify defects and compute defect density (ρ_d). The skeletonized network can also be used to calculate local line-edge roughness (LER) and line-width roughness (LWR).

Some BCP thin films may exhibit a mixture of morphologies or orientations of the morphology. For instance, cylinder phases may exhibit a mixture of vertical domains (which appears as hex-dot regions) and horizontal domains (which appear as lines). These can be differentiated in image analysis using thresholding and particle-counting routines. A size cutoff can then easily differentiate between the smaller dots and the larger lines; flood-fill methods can expand these objects into domains throughout the image [95]. For lamellae, the absolute magnitude of local image gradients can be used to differentiate between regions of horizontal lamellae (which

appear featureless and thus have small gradients) and regions of vertical lamellae (which have striping that generates large gradients) [310].

Overall, image analysis provides a robust and powerful means of quantifying the ordering of BCP thin films. The main drawback is that AFM and SEM are inherently surface-sensitive techniques. It is not always clear whether the ordering observed on the surface is representative of the order through the film. Indeed examples of surface-specific phenomena in BCP ordering are known [311].

4.2. Reciprocal-space methods to characterize order

X-ray and neutron scattering have emerged as powerful tools for quantifying the order in self-assembling soft matter systems. While wide-angle experiments probe atomic or molecular scale ordering and crystallization, small-angle scattering (SAS) is sensitive to nanoscale order [312-317]. Ordered BCP phases give rise to distinct peaks or rings in small-angle scattering; these are diffraction peaks from the nanoscale repeating-structures, and are thus precisely analogous to the wide-angle diffraction peaks one observes for atomic crystals. SAS data is obtained by recording the intensity of scattering rays as a function of the angle with respect to the direct beam (2θ) on a two-dimensional detector; data is then converted into ‘reciprocal-space’ by considering the momentum transfer vector, whose magnitude is:

$$q = \frac{4\pi}{\lambda} \sin \theta \quad (12)$$

where λ is the wavelength of incident radiation. Both small-angle x-ray scattering (SAXS) and small-angle neutron scattering (SANS) have been found to be valuable for studying soft matter. The former relies on weak differences in electron density to yield scattering contrast, but can take advantage of the prodigious photon flux available at modern synchrotron facilities [318]. The latter exploits nuclear scattering, and can thus greatly enhance scattering contrast by isotopic selection (especially deuteration of one of the hydrocarbon blocks), compensating for the poorer flux of neutron reactor or spallation sources. A scattering experiment roughly returns the Fourier transform of the sample’s realspace structure; more strictly, experimentally the detector records the intensity (square of the amplitude) of the scattered waves. The lack of phase information makes direct inversion of this Fourier data impossible. Scattering data is inherently information-poor in the sense that data-fitting is ill-posed (there are multiple realspace structures that will both fit a given intensity profile). Despite the fact that scattering data is not intuitive—and is potentially difficult to analyze—these techniques have many unique advantages over realspace microscopy. Atomic and nanoscale resolution are easily obtained, and most samples can be studied without staining, etching or other preparations. X-ray and neutron beams are highly penetrating, allowing bulk samples and subsurface order to be studied, as well as *in-situ* measurements in liquids or custom sample cells. Furthermore, while microscopy is an inherently local measure of order, scattering provides complementary data by yielding quantifications of order that are averaged over large sample volumes, and are thus statistically strong. High-flux synchrotron x-ray beams allow fast (sub-second) measurements; combined with *in-situ* capabilities (heating, solvent exposure, etc.), this allows the kinetics of ordering to be measured. The low flux of neutron sources makes realtime *in-situ* monitoring of BCP coarsening kinetics

impractical (neutron scattering data collection requires minutes to hours). However, high-flux synchrotron x-ray beamlines are extremely well-suited to high-speed data acquisition (down to milliseconds), making realtime observations of BCP phase transitions, and ordering kinetics, readily possible.

Small-angle scattering has been applied extensively to studying block-copolymer materials [319-322]. Scattering data from well-ordered BCP phases will exhibit a series of rings, whose relative position and intensity can be indexed to determine the symmetry, and thus morphology. A variety of models have been presented for quantitatively fitting scattering data of nanostructures [304, 323-328]; these models can easily be adapted to fit data from BCP materials. The intensity along a scattering ring in the azimuthal direction can be used to determine the orientation distribution, from which the previously-described metrics (σ_ϕ , S , η , etc.) can be computed. One can probe a sample at different orientations with respect to the beam, allowing the orientation in three-dimensions (3D) to be assessed. More broadly, one can rotate the sample in the beam, and use images collected at various angles to reconstruct the full 3D reciprocal-space of the sample. These orientation analyses are especially important for samples with macroscopic order. A variety of methods exist to align BCP phases; however the quality of alignment can vary drastically depending on the method and processing protocol. Scattering allows this orientation distribution to be quantified.

The width of a peak in SAXS can be generically interpreted as a measure of average correlation length: large, well-ordered grains generate intense, sharp diffraction peaks; whereas small grains lead to broad scattering peaks. This can be quantified through the Scherrer equation [329-332]:

$$\xi_s = \frac{2\pi K}{\Delta q} \quad (13)$$

where Δq is the peak width in reciprocal-space, K is the Scherrer constant, and ξ_s is the correlation length (Figure 6b). The constant K is of order unity, and depends on a variety of factors, including the grain shape, the symmetry of the unit cell giving rise to scattering, and the peak width definition being used (FWHM, standard deviation, etc.) [330]. The correlation length is most frequently directly interpreted as being the average crystallite size; in the case of a BCP, this would be the grain average size (*i.e.* the typical distance over which the morphology is positionally and orientationally coherent). However, some caution is necessary, as a variety of effects can contribute to peak broadening in SAXS data. The most mundane contribution is that instrumental resolution must not be forgotten [332]. This also sets a limit to the maximum grain size that can be quantified using a Scherrer analysis. Strain in a material can give rise to a distribution in repeat-spacings, which will also broaden a peak [333, 334]. The grain size distribution also plays a role [335]. Note also that even materials without grain boundaries will have a finite ξ_s because internal disorder decorrelates the structure over large enough distances. This ‘paracrystal’ state [336-338] can often dominate in soft-matter systems. These different sources of broadening can, in principle, be distinguished based on peak shape and variation in peak width/shape in different reflections [339, 340].

Care must also be taken when comparing grain sizes calculated in different ways. The Scherrer analysis computes the volume-averaged grain size. Comparisons to orientational grain sizes can be misleading, since x-ray scattering is sensitive to both orientational and positional decorrelation. Well-aligned BCP materials (orientation correlation over infinite distances) will nevertheless have imperfect registry over long distances (finite coherence measured in scattering). In this sense, the grain size measured by scattering is a very stringent measure of order. There is an upper limit to the grain size that can be measured using a peak width analysis, since instrumental effects (beam divergence, wavelength spread, etc.) impose a minimum peak width. For a modern synchrotron beamline, this cutoff typically limits one to measuring submicron grain sizes. An alternative ‘variance scattering’ method has recently been proposed for measuring grain sizes [341, 342], wherein one quantifies the statistical variation of intensity along a scattering ring. A large population of small, randomly-oriented, grains will give rise to a uniform scattering ring (as the innumerable Bragg peaks overlap), whereas a smaller number of larger grains will give rise to a scattering ring with significant intensity variation (in the limit of just a few grains, one can in fact resolve the individual Bragg peaks). This method bypasses the peak width limit, and thus enables quantification of grain size across a wide range (nanometers to hundreds of microns). This method also probes a volume-averaged grain size, though there is a subtly different definition of grain (average number of distinguishable domains) compared to the Scherrer method (length-scale over which lattice is coherent).

X-ray scattering has been adapted to study thin films. In grazing-incidence small-angle x-ray scattering (GISAXS), a focused x-ray beam is reflected off of the sample/substrate interface (Figure 6a) [343-349]. Although x-rays are strongly penetrating, at sufficiently shallow angle (on the order of 0.1°), total external reflection of the beam is observed. In this geometry, the small x-ray beam is projected (along the beam direction) into a large stripe over the sample surface. As such, the total scattering volume is sufficiently large to resolve a signal from even just monolayers of nanomaterials. Moreover, reflection-mode effects (such as waveguiding [350-352] of the beam within the thin film) can further enhance the signal. One can also exploit the incident angle to perform ‘depth profiling’ of thin films. At sufficiently shallow angle, the beam will totally reflect from the film-ambient interface, and thus only probe (evanescently) the top few nanometers of the film. At a slightly higher angle—above the film-ambient critical angle—the beam penetrates to the substrate, and the resultant scattering pattern will be representative of the structure throughout the film. One can thus compare the structure at the surface *vs.* within a film, resolving the ambiguities inherent to AFM and SEM. With some care, one can more gradually vary the incident angle, to reconstruct the structure as a function of film depth (rather than simply the average order through the film) [47, 350, 353-357]. GISAXS has thus emerged as a powerful means for studying nanostructured soft materials, including studying them *in-situ* during assembly or conversion; block-copolymers have been extensively studied in this way [358-365]. With appropriate corrections, GISAXS data can be used to identify unit cell [366], morphology, repeat spacing, orientation distribution (Figure 6c) [367-370], grain size (Figure 6b) [332], etc. In fact, properties can be computed anisotropically (in-plane *vs.* out-of-plane). It should be noted that for a thin film the film thickness itself represents a maximum possible ‘grain size’ in the vertical direction. Very thin films thus have peaks in GISAXS that are very broad

along the film normal direction (q_z in reciprocal-space), appearing as streaks. More generally, one must be aware that in GISAXS the film thickness itself gives rise to scattering features.

Although GISAXS is a powerful technique, the data one obtains is even more difficult to analyze than conventional scattering data. In addition to the usual challenges (ill-posed data fitting), GISAXS introduces distortions and multiple-scattering effects. Because of the shallow angles, the x-ray beam is measurably refracted when it crosses the ambient-film interface; scattering is also refracted as it exits the film. These effects cause the detector image to be a ‘distorted’ version of reciprocal-space (stretched/compressed along q_z) [358, 371, 372]. The reflection-mode geometry leads to beneficial intensities; yet these enhancements can make quantitative cross-comparisons difficult [373, 374]. For example, in GISAXS one observes an intense horizontal band of intensity on the detector (which can help to highlight weak signals). This Yoneda [375] (or Vineyard [376]) scattering occurs when the exit angle matches the critical angle (where waveguide modes are greatly increasing the probability of a scattering event). It can be difficult to quantitatively account for the enhancement factor. Finally, multiple scattering must be considered. In addition to scattering from the direct beam, one also has scattering from the reflected beam. Moreover, the scattering itself can either directly reach the detector, or be reflected first. These four possible scattering events appear as two scattering images on the detector [358]. That is, each scattering peak will appear twice (shifted along q_z); these peaks may also overlap, giving rise to elongated peak shapes. Measurements at multiple angles can resolve whether a given peak arises from the direct beam or the reflected beam, since the latter shift as the reflection angle is changed. These four possible scattering events (really the first four terms in an infinite series of progressively more complex but less likely multiple-scattering combinations) can be accounted for theoretically. The first term (direct scattering) is known as the ‘Born Approximation’ (BA), whereas accounting for the first four terms can be done using the ‘Distorted Wave Born Approximation’ (DWBA) [376-378]. A variety of elegant DWBA variants have been created to account for a variety of experimentally-relevant configurations [371, 379-382]. With care, one can quantitatively fit GISAXS data (some software packages now exist for the purpose [367, 383-389]).

Several alternatives to GISAXS have been described. One can use a series of transmission-mode measurements, across a range of sample angles, to reconstruct the same slice of reciprocal-space probed in GISAXS. This technique has been termed critical dimensions SAXS (CD-SAXS) [390-395], in analogy to the CD-SEM method for quantifying the order of lithographic structures. CD-SAXS has enabled precise measurement of lithographic structures [396-399], nanoimprinted polymers [400, 401], and block-copolymers [402, 403]. CD-SAXS is unencumbered by reflection-mode distortions, enabling precise fitting to measure detailed aspects of nanostructure (size, shape, LER, etc.). For instance, in BCP materials it has been shown how the morphology slightly distorts in order to accommodate guiding chemical templates. Similar experiments can be performed using neutrons; this ‘rotational’ scattering technique (RSANS) has been used to measure the ordering of BCPs [53, 310, 404, 405]. In GISAXS mode, one can rotate the sample in-plane, in order to reconstruct reciprocal-space. This can be used to measure single crystals [406], or the orientational spread in aligned samples [211, 407]. Recently, an alternative to GISAXS has been presented, which can obtain undistorted data

without requiring lengthy reconstruction. Grazing-incidence transmission small-angle x-ray scattering (GTSAXS) [408-410] involves aligning the incident x-ray beam on the downstream *edge* of a sample/substrate, rather than directing the beam towards the center of the sample as typically done in GISAXS. This simple change enables the sub-horizon scattering (absorbed by the substrate in GISAXS) to escape and be recorded. By using a slightly larger incident angle ($\sim 1^\circ$), GTSAXS can record an image without refraction-distortions or multiple-scattering complications. Data can be fit using the Born approximation, bypassing the complications of DWBA. The main downside is that one must arrange for the sample of interest to be positioned near the edge of the substrate. Spin-cast films often have edge effects, which make these regions poor representations of the average structure. On the other hand, it is usually trivial to dice a substrate so as to expose an edge of representative material. It has been found, experimentally, that dicing does not introduce problematic changes to the structure of most nanomaterials.

An exciting development in the study of soft materials is the availability of soft x-ray beamlines. X-ray energies of 0.2 keV to 1 keV allow access to the x-ray absorption edges of C, N, O, etc. This resonant soft x-ray scattering (RSoXS) [411-414] can greatly enhance the scattering contrast between otherwise similar soft-matter components. Moreover, experiments at multiple energies can adjust the relative contrast of different constituents in multi-component systems, allowing components to be selectively contrast-matched ('made invisible'), and overall allowing the reconstruction of multi-component nanostructures. Wang *et al.* demonstrated how RSoXS could be used to unambiguously reconstruct the morphology of a triblock copolymer [17]. Sunday and Kline used resonant reflectivity to probe the interfacial width in BCPs [281]. These instruments also offer the possibility of probing molecular bond orientation, simultaneous with resolving nanostructure [415]. As soft x-ray beamlines develop, we can expect yet more powerful capabilities to become available [357].

An emerging trend in block-copolymer materials is to generate hierarchical, multi-scale patterns, where self-assembly generates nanoscale order within domains defined using a larger-scale technique. Conventional lithography allows hierarchical control *via* substrate patterns [73, 416-422] or nanoimprinting [423-426]. Annealing can be controlled locally using a scannable nozzle releasing solvent vapor [427], or with laser annealing in a raster-scan [428] or masked mode [57]. Controlled wetting [361, 429] or evaporation [430] can define film regions within which the BCP orders. Onses *et al.* demonstrated the use of jet printing to define hierarchical BCP patterns [431, 432]. These hierarchical materials create a corresponding measurement challenge: to simultaneously measure structure at many length-scales. X-ray scattering beamlines are increasingly working to offer micro-focused and nano-focused x-ray beams [433, 434]. Small beams can be used to generate realspace maps of samples [435], where each pixel can contain a scattering dataset encoding nanoscale and molecular-scale information. Coherent imaging methods are also improving, promising to allow direct imaging of materials at many length-scales [436-438].

5. Ordering Using Plasticizing Additives

Block-copolymer assembly is regulated by a delicate balance of energetic effects, especially the chemical mismatch of the block components, and chain stretching effects. Thus, a crucial means of controlling their ordering is to tune the interaction energies within the system.

5.1. Solvent vapor annealing

In solvent vapor annealing (SVA), a block-copolymer thin film is exposed to a vapor that is either a good solvent for both blocks, or a preferential solvent for one of the blocks. This solvent uptake induces swelling, plasticizing, and thus enhances ordering of the BCP morphology. The mechanism of rapid ordering under SVA with non-preferential, good solvents can be directly compared to thermal annealing, since both methods reduce the polymer viscosity and increase the mobility of the polymer chains. The SVA mechanism can be considered thermodynamically equivalent to thermal treatment, and mapped onto the BCP phase diagram as a decrease in the effective χN segregation parameter (Figure 7a); or as a kinetic effect, lowering the T_g of the system [439-441]. As reviewed by Hillmyer *et al.* [442], SVA can be conducted in various experimental setups (Figure 7b-d), but even in its simplest implementation—a closed ‘jar’ with a liquid solvent reservoir—SVA is very effective in accelerating the ordering of BCP thin films [362]. Despite its superficial simplicity, SVA can be quite difficult to control reproducibly, with results dependent on experimental factors such as chamber size and geometry, the location of the solvent reservoir, precise temperature control, and relative humidity. Moreover, care must be taken to avoid excessive swelling ratios or swelling rates, which can induce film dewetting, structural rearrangement, or topographic reconstruction [443-445]. While it is relatively straightforward to control swelling ratio (with online thickness monitoring) and exposure time, SVA ordering and morphologies are also strongly dependent on kinetic aspects such as the swelling rate, the quench rate, and the sample extraction protocol [446-452]. Solvent removal rate is particularly important for the ordering of cylindrical systems when a vertical orientation is desired, as the propagation of the drying front through the film thickness defines the ordering direction of the cylinders [448, 453]. The need for precise control of SVA parameters has driven the development of more sophisticated, multi-point thermostated, flow-through setups (Figure 7c), which permit independent control of the partial pressure and flow-rates of multiple solvents. These setups benefit from real-time closed-loop control over the film swelling ratio and morphology (through the use of interferometry, ellipsometry, or GISAXS) [54, 365, 454-457]. Despite these advances, kinetic data for BCP grain-coarsening under SVA conditions are scarce. Cross-comparison of SVA results is complicated by inconsistencies in definitions of the annealing duration (*e.g.* with or without an equilibration period), and when swelling or de-swelling rates are unreported. Stein *et al.* observed an order-of-magnitude faster grain-growth for PS-*b*-PEO annealed inside a small volume chamber *vs.* a large one, owing to differences in saturation time [458], which illustrates the difficulties inherent to hardware design, experimental reproducibility, and cross-comparison of results. Nonetheless, it can generally be concluded that in common BCP systems, a one-hour solvent vapor anneal can easily give rise to $\zeta > 1 \mu\text{m}$, which corresponds to a more than 10 \times improvement over oven annealing (PS-*b*-PMMA [459], PS-*b*-P2VP [460], PS-*b*-P4VP [362, 461-463], PS-*b*-PDMS [464, 465], PS-*b*-PEO [453, 458, 466], PS-*b*-PLA [447, 467]). SVA is one of the few methods suitable for ordering of high

molecular weight systems, which exhibit extremely slow pattern-formation kinetics. Kim *et al.* [459] used a simple bell-jar, sub-ambient temperature annealing approach to order lamellar PS-*b*-PMMA of total molecular weight $M_n = 256$ kg/mol (with defect density decreasing as $\rho_d \sim t^{-1.35}$). In combination with topographic confinement, ordering of systems with $M_n \sim 1$ million g/mol is possible. It is worth noting that SVA-processed films often require additional oven annealing to remove film wrinkles resulting from buckling during deswelling [452].

Generally speaking, ordering kinetics increase with solvent uptake. However, increasing the film swelling ratio risks crossing the solvent-defined ODT [441], erasing any existing order, or inducing film dewetting from the substrate [444]. One can avoid crossing ODT by using binary solvent mixtures where one solvent is preferential, since this increases χ and stabilizes the phase-separated state [54, 456, 458]. Condensation of bulk solvent on the polymer film (which leads to dewetting) can be avoided by increasing the temperature of the film relative to the solvent vapor; however this is ineffective as it very strongly shifts the equilibrium towards the dry state. Some groups have conditioned their films at sub-ambient temperatures [459], which increases solvent uptake but risks catastrophic solvent condensation if the film-vapor temperature differential is too high. Warm (~ 60 °C) solvent vapor was found to increase ordering kinetics; for cylinder-forming PS-*b*-PDMS in a trench pattern, the ordering time was reduced by more than an order-of-magnitude (to 30 s), compared to room-temperature SVA at the same swelling ratio ($\rho_d \sim t^{-1}$ at 23 °C *vs.* t^{-3} at 60 °C) [457]. A high-temperature combined with high-pressure approach to SVA has been proposed by Buriak *et al.*, where a sealed pressure-resistant annealing vessel was heated using microwaves (Figure 7d). The heating simultaneously increases the temperatures of the solvent and the substrate beyond the solvent boiling point, and increases pressure to several atmospheres. This provides a spectacular enhancement of the ordering kinetics in high molecular weight systems, without epitaxial guiding [117, 468].

The substantial kinetic acceleration of SVA has been coupled with other DSA methods to resolve the problem of the poly-grain ordering of BCP domains. Long-range ordering has been demonstrated when SVA is combined with graphoepitaxy [117, 454, 463, 465, 469] and chemoepitaxy [361, 460] or swelling-induced soft-shearing methods [292, 427, 461] (Figure 7e).

5.2. Plasticization during film casting

Plasticizing and ordering solvent effects can be also exploited at the stage of film casting. For example, the fast evaporation of a selective solvent can balance the chain relaxation rate and microphase separation driving force, thereby inducing rapid development of vertical cylindrical domains [448]. Perego *et al.* showed that toluene trapped in a neutral brush underlying a PS-*b*-PMMA film plays a role in enhancing subsequent ordering kinetics [470]. Such results, combined with the fact that as-cast polymer films may retain residual solvent [471], underline the necessity to scrutinize experimental protocols for BCP annealing, in particular when cross-comparing kinetic data. Ordering kinetics can also be increased by changing the temperature of the film casting. In warm (40–60 °C) spin-coating experiments, Lee *et al.* observed quick graphoepitaxial ordering of a low molecular-weight BCPs without additional annealing [472].

5.3. Direct solvent immersion

Direct immersion annealing (DIA, iDSA) is an alternative, and arguably more convenient, way of delivering small-molecule plasticizers into BCP films. In this method, the BCP film is immersed in a solvent mixture that plasticizes the BCP, without dissolving the film. Park *et al.* [473] demonstrated ordering of a high- χ PS-*b*-PDMS by combining DIA with nanolithographic guide patterns. Modi *et al.* [474] recently used DIA to investigate the optimal conditions and ordering kinetics of PS-*b*-PMMA thin films. The two-solvent mixture, consisting of a non-solvent (heptane) and a selective solvent (acetone), is chosen based on the solubility parameters of the pair and, at relatively modest swelling-ratio, facilitates increased mobility of the chain while sustaining sufficiently high χ to prevent phase-mixing. Interestingly, the acceleration of the grain-growth kinetics manifests as a large increase in the pre-exponential factor (k), compared to the value for oven annealing [56], while the kinetic exponent (α) remains relatively small.

5.4. Blending methods

The composition of a BCP film can strongly influence ordering kinetics. For instance, cylinder BCP phases order more rapidly than lamellar, owing to chain diffusion [222, 475], while novel block-polymer architectures can potentially enable vastly improved grain sizes [476]. Blends of block-copolymers [87-95] can give rise to novel structures [28, 199], and blending can also influence ordering kinetics. Blending species into a BCP phase can affect the Flory interaction parameter (χ) [477-480]. Neutral additives should reduce segregation, effectively plasticizing the material and accelerating assembly kinetics. Conversely, blending additives that have a selective affinity for one of the blocks has been demonstrated to increase segregation strength [282, 480-483], which increases ordering quality (*e.g.* sharpening interfaces) but also increases ordering timescales. Blending of short neutral (random copolymer) chains has been suggested as ‘melting’ local defects, thereby improving ordering [484]. Nanoparticles can be blended into BCP systems to create new hybrid structures [79]. Blended nanoparticles may localize to defective film regions (such as grain boundaries), stabilizing them and thereby influencing ordering kinetics [485]. The kinetics in hybrid systems may be highly non-trivial; for instance, there may be separate assembly timescales for BCP phase-separation, and the ordering of the nanoparticle fillers [486].

6. Ordering Using Interfacial Effects

Thin films are generally known to be strongly influenced by both the nanoscale confinement, as well as the presence of the film-substrate, and film-ambient interfaces. The order of BCP thin films, in particular, is strongly influenced by the interfacial energies at the substrate and top surfaces [487].

6.1. Substrate-mediated ordering

Substrate surface chemistry influences BCP assembly. Substrates with strong interaction with one of the blocks will introduce preferential wetting, which in turn templates the type and orientation of the morphology. For example, lamellar phases will orient horizontally (with the lamellar sheets parallel to the substrate plane). On the other hand, ‘neutral’ surfaces can be created whose surface energy is intermediate between the two blocks [75, 259, 488-492]. A

robust method is to graft a random copolymer brush to the substrate, with the brush composition roughly matched to the relative volume fraction of the two BCP blocks. Alternatively, intermediate surface energies can be obtained by controlling grafting density [493], controlling the ratio of species reacting with [494-496] or assembling on [497, 498] a substrate, or partially oxidizing certain hydrophobic substrates [310, 404, 499-503]. By establishing roughly equal interaction strength with the two blocks, there is no net preferential segregation. Although one might expect ‘undirected’ ordering (random orientation distribution), surface entropy instead promotes preferentially vertical orientations of morphologies [236]. For instance, cylinder phases on preferential substrates orient horizontally (long-axis parallel to substrate plane), whereas on neutral substrates they orient vertically (perpendicular to substrate). More generally, there is an interplay between substrate-directed and confinement-driven ordering, which can tune orientation [273, 504].

The strength of substrate interactions influences ordering kinetics. Generally speaking, a strong substrate interaction will slow kinetics, while unfavorable substrates will increase ordering kinetics. On a strongly-adhesive substrate, polymer molecules become pinned and diffusion is arrested [505]. Reducing the substrate interaction improves ordering. Harrison *et al.* [301] found that grafting a brush layer to the substrate with the same composition as the BCP majority phase yields a ‘self-lubricating layer,’ increasing the ordering rate, as compared to the same BCP on the native oxide of the silicon substrate. This effect is less pronounced when it is the minority block that interacts strongly with the substrate. This effect can be further enhanced by selecting a substrate-brush material that is dissimilar to the BCP phases. Quach *et al.* [191] systematically varied the BCP-substrate interaction parameter, and found that large incompatibility between BCP matrix and substrate brush (*i.e.* large $\chi_{\text{matrix-brush}}$) improved order.

A more extreme version of substrate chemical control is to use chemical patterns [506, 507], typically produced using lithography (chemoepitaxy [75, 508]). In this case, the two block components will segregate locally, registering with the substrate pattern and templating off of it. This can be used not only to enforce orientation (especially vertical), but to exactly enforce local positioning of both blocks. If the chemical template is ordered over macroscopic areas, then the templated BCP morphology is similarly ordered macroscopically. Chemoepitaxy is typically coupled with thermal annealing, which enables local phase separation, and morphological rearrangement in order to follow the guiding pattern. For a 1:1 chemical template, rearrangement need only occur over distances of $\sim L_0$, which leads to very fast ordering times (minutes). Edwards *et al.* studied in detail the ordering of a lamellar BCP on a chemical line pattern [509], identifying several intermediate states. That is, the BCP first generated hexagonally-packed domains (reminiscent of vertical cylinders), which aligned with the chemical template. These domains then fused into defective lamellar lines, with defects gradually disappearing. Notably, elimination of topological defects in this case does not require the usual diffusion and annihilation; instead, defects can be spontaneously eliminated through BCP rearrangement. Thus, the strong driving force of the underlying chemical pattern enforces order. This rapid convergence to near-perfect macroscopic order can be considered as an enormous acceleration of the self-assembly process.

Substrate topography can strongly influence self-assembly, especially by selecting the in-plane and out-of-plane orientation of the BCP morphology. This has been investigated with respect to roughness [53, 277, 310, 404, 510-512], nanoparticle monolayers [513], faceted substrates [469, 514, 515], corrugated surfaces [278, 516, 517], film-spanning particles [276, 518], and guiding trenches [519-523] (graphoepitaxy [73, 74]). In many graphoepitaxy schemes, a BCP is ordered within a trench, with the morphology rapidly aligning with the trench sidewalls (if the trench width is commensurate to the BCP repeat-spacing), or against the trench length (if the trench is incommensurate). As with chemical patterns, the formation of a BCP phase with uniaxial orientation, and even well-defined registry over macroscopic distances, represents an enormous acceleration compared to conventional oven annealing. On the other hand, one must keep in mind the labor costs of DSA methods; that is, the time spent creating the template itself. The advanced optical or electron-beam lithography used to generate the underlying pattern may require multiple stringent processing steps. Nevertheless, the degree of order and control over material registry (both locally and macroscopically) allows these DSA methods to access regimes not available with any other techniques.

6.2. Free surface-mediated ordering

Ordering of block-copolymer thin films is strongly influenced by the free surface. In general, one of the two block materials will have a lower surface tension, and will be preferentially segregated to the top surface. This propensity will then drive ordering through the depth of the thin film. For instance, this difference in surface tension generically drives lamellar phases to orient horizontally (lamellar planes parallel to substrate). Formation of robust vertical BCP orientations thus requires neutralization not only of the substrate interface, but also of the free surface. For some BCP materials, the temperature-dependence of the two surface tensions may cause them to coincide at some specific temperature. Annealing at this temperature thus removes the propensity for preferential surface segregation. For instance, polystyrene-*block*-poly(methyl methacrylate) (PS-*b*-PMMA) orients vertically [488, 492] near 230°C. Interfacial neutrality alone does not guarantee a vertical morphology orientation, since neutrality merely removes the preferential orientation induced by one component wetting an interface; *i.e.* one would naively predict that neutrality leads to a completely random and unbiased orientation distribution. However, the BCP chains and morphology are not blind to the discontinuities of interfaces. Forrey *et al.* used molecular dynamics simulations to show that a surface entropy field drives chains to orient with their long-axis in the interfacial plane, and thus promotes a vertical orientation of the BCP morphology [236].

The energetics of a thin film top surface can also be regulated by applying a neutral ‘topcoat’ material [524-529]; this strongly selects the perpendicular orientation, with well-defined morphologies forming on minute timescales. Zhang *et al.* demonstrated that this topcoat can be embedded within the BCP material [530]. That is, a polymeric surface-active additive can be added to the BCP solution that is cast. During annealing, this material spontaneously segregates to the top surface, generating a neutral interface and thus controlling film orientation. This strategy thus enables orientation control and rapid annealing, without introducing an additional film-application step.

6.3. Interplay of substrate and surface interactions

Of course, the overall ordering of a BCP film is influenced by the combined effect of the substrate and top surface driving forces. The interplay between surface energies (top and bottom interface) and film thickness were investigated in detail by Durand *et al.* [531] for the case of lamellar morphologies. Film thicknesses commensurate with an integer number of lamellar layers preferentially form horizontal/parallel orientations; similarly, preferential surface wetting promotes horizontal states. However, incommensurate confinement instead promotes perpendicular orientations; mixed phases can develop when commensurability and surface interactions are in opposition.

For an unconfined thin film, when both interfaces are preferential, lamellar phases generate horizontal lamellae, and further generate islands/holes (of height L_0) for incommensurate thicknesses. Kim *et al.* [259] demonstrated that when the neutrality of the top and bottom interfaces are in opposition, the islands/holes instead have a height of $L_0/2$. For a preferential substrate but a neutral top surface, the surface-expressed block alternates between the high and low regions (enabling the $L_0/2$ height step). The reverse condition—neutral substrate but preferential top surface—involves high and low regions that have different blocks wetting the buried substrate interface. This suggests an elegant way to direct BCP ordering: by carefully balancing commensurability, and interfacial effects.

7. Ordering Using Fields

External fields alter the process of self-assembly by imposing energetic constraints on the nucleation, growth, and stability of BCP domains. In particular, fields break symmetry by changing the relative energies of domains with different orientations [50].

7.1. Electric and magnetic fields

For electric and magnetic fields, the energetic bias originates from the anisotropy (contrast) of dielectric permittivity ($\Delta\epsilon$) or magnetic susceptibility ($\Delta\chi$) between the chemically-distinct BCP blocks [67, 71], and is proportional to the square of the applied field (E or B , respectively). The thermodynamic driving for alignment, ΔE , is also affected by the volume of domains with coherent order (V):

$$\Delta E = \frac{VB^2\Delta\chi}{2\mu_0} \quad (14)$$

where μ_0 is the vacuum permeability. In a typical Gaussian-coil BCP, both the magnetic and electric anisotropies are relatively low, and the intrinsic domain sizes are small. Thus, rather large fields are required to induce morphological alignment. As electric interactions are much stronger than magnetic ones, field-alignment of BCPs was first successfully demonstrated using static electric fields [532, 533]. The weaker driving force of magnetic fields is suitable for the alignment of bulk and semi-thin samples such as membranes [69, 70, 534]; that is, materials not dominated by surface-ordering effects [535]. The alignment direction depends on the sign of the anisotropy of a particular system. In most coil-coil BCPs with cylindrical or lamellar

morphology, this direction is parallel to cylinder long-axis or the lamellar plane, inducing ‘vertical’ orientation of the domains when the field is applied in the substrate-normal direction. Under this alignment geometry, there is no energetic bias for the in-plane direction; the in-plane energetic degeneracy thus leads to a ‘2D-powder’ (poly-grain) alignment. Nonetheless, this ordering geometry is commonly used in electric field-mediated self-assembly of BCP films due to the ease of the field application (parallel-plate condenser), and because it enforces continuity of the BCP domains through the entire film thickness [144, 536]. Conversely, an in-plane alignment of BCP cylinder or lamellar domains on neutral substrates is non-degenerate. The morphology aligns along the field, resulting in a pattern of parallel lines in the field direction [537, 538].

Field-mediated ordering is, in principle, a thermodynamic phenomenon that applies an orientational bias to the free energy landscape, as opposed to altering the grain-growth kinetics or ordering pathway. The kinetics of ordering are primarily dictated by the viscous forces impeding the reorientation of ordered grains in the polymer melt. The characteristic ordering timescale, τ , is proportional to the viscosity, η , which in turn depends exponentially on temperature [539]:

$$\tau \propto \frac{\mu_0 \eta}{B^2 \Delta \chi} \quad (15)$$

$$\eta = \eta_0 \exp [E_a / k_B T] \quad (16)$$

where E_a is the viscous flow activation barrier, and η_0 is a phenomenological variable. Given the immobility of polymer chains below the glass transition temperature, electric or magnetic field alignment of BCPs is performed at high temperatures, well-above T_g . The ordering timescales are regulated by the magnitude of the driving force (field strength, anisotropy), the size of coherently-ordered domains, and the viscosity of the system. Rapid ordering and alignment is observed in systems with accessible order-disorder transition temperatures, such as low molecular-weight or liquid-crystalline (LC) materials. These materials also possess intrinsically large grains with high anisotropies. Ordering upon cooling from the mixed into the microphase separated state can occur on timescales of minutes, provided that the optimal thermal processing window is known [540]. Surprisingly, this approach was recently shown to be effective even in the magnetic alignment of a coil-coil PS-*b*-P4VP system, with purely-intrinsic magnetic susceptibility anisotropy [342]. Sub- T_{ODT} reorientation, or alignment of nucleating grains in as-cast films, is typically much slower due to the high viscosity of a polymer melt. Electric-field alignment times for coil-coil BCPs from an as-cast melt are of the order of several hours [532], even when combined with a plasticizing vapor atmosphere [538]. In comparison, concentrated BCP solutions can be aligned in minutes [541]. These timescales are of the same order-of-magnitude as those observed by SAXS for magnetic-alignment of bulk liquid-crystalline BCPs, which proceeds through a grain rotation mechanism [539]. This again highlights the importance of viscosity in field-mediated alignment. The alignment kinetics can also be improved by modifying the material’s propensity for field-alignment by blending in a low molecular-weight anisotropic plasticizer, thereby increasing the susceptibility contrast ($\Delta \chi$) [542]. In the case of

electric field experiments, sequestering metallic nanoparticles into one of the blocks increases the permittivity anisotropy ($\Delta\epsilon$), and improves field-alignment [543].

7.2. Shear fields

Shear was historically one of the first methods used to orient lamellar or cylindrical morphologies in bulk block-copolymers [544, 545]. An advance towards shear-ordering of *thin films* was made by Angelescu *et al.*, who used a conformal layer of crosslinked PDMS to transduce the shear force to a heated BCP film [60]. The technique has been extended to shear-align various block-copolymer systems with different morphologies: spheres [546], cylinders [547], and lamellae [548]; frequently with the use of rheometric setups and high-viscosity silicone oils instead of elastomeric PDMS pads as shear transducers [549]. The timescales for alignment in shear experiments, as measured by the evolution and saturation of the orientational order parameter, are reasonably short. Typically, shear stress is applied to a sample heated above T_g for ~30 min, followed by cooling to room-temperature to immobilize the material [547, 550]. A key advantage of shear-alignment is the relatively simple experimental setup, combined with the ability to order materials over arbitrarily large areas. Thus the ‘total cost’ of shear ordering (both ordering time and sample preparation time) is quite low. Shear-aligned BCP patterns have been used as templates for fabrication of large-area single- and double-layered arrays of inorganic nanostructures [112, 139, 141, 551].

While shear-alignment offers a rapid way of obtaining globally-aligned monolayers composed of horizontal cylinders or vertical lamellae, the near-ideal line patterns are compromised by the presence of relatively sparse dislocation defects and characteristic periodic morphology undulations [550]. There is a well-recognized, negative correlation between the number density of dislocations and the orientation order parameter. Even in ‘defect-free’ (within the microscopic observation field) samples, the orientational order parameter does not reach unity, due to the presence of small-amplitude undulations. Although the order in a film can be optimized through selection of film thickness (optimum near $1 L_0$) [60], or by fine-tuning the block ratio [547], the presence of undulations may, in some regimes, be an intrinsic feature of shear-ordering.

8. Ordering Using Advanced Thermal Methods

Although a variety of elegant directed assembly strategies have been described, purely-thermal annealing methods remain attractive from the point of view of simplicity. As such, a variety of research programs have investigated the limits of thermal ordering of BCPs. An obvious approach is to increase the annealing temperature. Rapid thermal processing (RTP) typically involves irradiating a sample with an infrared light-source. This allows high temperature to be rapidly achieved, since the sample is directly heated (photo-thermally). As previously mentioned, RTP has been applied to BCP thin films, where rapid heating to high temperature (up to 350°C) [237, 245, 246] led to rapid ordering (and formation of nanostructure before the onset of polymer degradation). Another convenient method for rapidly delivering energy to BCP samples is to use microwave heating. BCP films can be heated alone [552, 553], or annealed in combination with solvent exposure and/or graphoepitaxial templates [117, 468, 554]. In this method, the final order can depend strongly on the heating rate, and the position of the sample within the microwave

field [553]. The microwave radiation may be absorbed by the silicon substrates (if the Si wafer is sufficiently doped) [555], or may be absorbed by polar solvent species [556]. Heating polymer films through irradiation allows for rapid heating and cooling, and thus controls the temporal thermal history (*c.f.* lower-right of Figure 2). However, one can also consider control of the spatial component of thermal processing.

In semiconductor manufacturing, moving thermal zones are now routinely used to generate highly-ordered atomic crystals of inorganic matter. Originally developed by Pfann, zone melting consists of moving a hot melting zone through a material; impurities will segregate into the molten region, and thus the moving melt zone sweeps away impurities, leaving behind a pure material ('zone refinement') [557]. A related phenomenon is directional solidification, where a particular crystal orientation is templated by existing solid, such that a moving thermal zone leaves behind a single-crystal material. The application of zone heating methods to organics is more recent [558]. Lovinger *et al.* used temperature gradients to control polymer crystallization [559]. Hashimoto *et al.* applied moving thermal gradients to *bulk* block-copolymers (Figure 8a), where they demonstrated the ability to form extremely large grain sizes [560-566]. In the so-called 'hot zone annealing' (HZA) conditions, the polymer film is heated above the disordering temperature (T_{ODT}); and morphology develops on the cooling front through a directional solidification process [567, 568]. In addition to the influence of the spatial thermal gradient, substrates can play a critical role in determining morphology orientation [565]. Angelescu *et al.* used a microfabricated heater to induce directional solidification in a BCP monolayer, demonstrating greatly improved grain sizes [569]. For BCP materials, it is not always possible to access T_{ODT} ; *e.g.* this temperature may be above the polymer degradation temperature. As a result, a parallel research thrust has investigated 'cold zone annealing' (CZA), where the polymer film is heated above T_g to induce mobility and thus coarsening of morphology, but remains below T_{ODT} and thus within the ordered region of the phase diagram at all times (similar to oven annealing). Berry *et al.* developed an apparatus for CZA processing of BCP thin films (Figure 8b), and discovered that the zone direction induced a weak alignment of the BCP morphology, and that zone annealing led to enhanced ordering kinetics ($\alpha = 0.46$, compared to the usual $\alpha \approx 0.25$; Figure 4 compares the scaling for CZA *vs.* oven annealing). The alignment is unexpected given the lack of a well-defined interface (*e.g.* solid-liquid or order-disorder). The enhanced kinetics were studied by generating 'frozen zone' samples; that is, by interrupting the zone annealing process, such that the entire annealing history is encoded within the sample as a function of position (relative to the thermal zone at the moment annealing was terminated). These studies found the enhanced kinetics to be related to the in-plane thermal gradients [229]. Yet it is surprising that *macroscopic* thermal gradients ($\nabla T \approx 17$ °C/mm) are able to radically influence *nanoscale* ($L_0 \approx 26$ nm) self-assembly. Self-consistent field (SCF) simulations have investigated the role of dynamic heterogeneities [570] or spatial variation of polymer mobility [571, 572]; while these studies capture important physics, the size-scale of the simulated gradients are orders-of-magnitude sharper than those produced experimentally.

CZA methods have been progressively refined, including generating sharper gradients ($\nabla T \approx 45$ °C/mm) [573], to control BCP orientation [573], coupled with graphoepitaxy [574], in nanoparticle-BCP composites [575, 576], for mesoporous materials [123, 577], and using a

rotational apparatus to generate a rotating thermal zone [578]. A particular exciting demonstration—especially from the point of view of industrial scale-up of self-assembly—is the integration of CZA methods into roll-to-roll processing (Figure 8c) [579, 580].

Recently, dynamic annealing methods have been explored in a photo-thermal mode. Majewski and Yager developed a laser zone annealing (LZA) setup, wherein a laser beam is focused into a line at the surface of a BCP thin film (Figure 8d) [57]. The substrate is coated with a thin light-absorbing layer (Ge), such that the moving laser line generates a moving hot zone. The tight laser focus allows for extreme thermal gradients ($\nabla T > 4,000 \text{ }^\circ\text{C}/\text{mm}$), while the laser-based method more generally allows for detailed control the thermal history through the laser intensity, focus, sweep velocity, etc. This detailed control of spatio-temporal annealing history allows many aspects of self-assembly to be probed (Figure 2, upper-right). It was found that LZA processing enhances ordering kinetics by $\sim 1,000\times$ compared to traditional oven annealing (whereas CZA yields a $\sim 10\times$ enhancement compared to oven annealing), allowing for millisecond ordering (Figure 4 compares the scaling law for grain growth using various methods). Two factors play a role: the thermal spike allows rapid ordering (high peak temperature) before the onset of polymer degradation (similar to RTP annealing); and, the in-plane thermal gradient additionally enhances ordering kinetics. A possible mechanism is that the thermal gradient exerts a thermophoretic force on topological defects, driving them towards the hot region of the zone (where their energy is lowered). This net force on defects will both sweep them out of the sample during annealing (similar to zone refinement), and will increase the rate of defect annihilation (by concentrating defects into the high-mobility hot zone). When ordering temperatures are sufficiently high, photo-thermal zone annealing can spontaneously induce alignment of the BCP phase, due to shearing of the polymer material [57] and/or directional solidification [581, 582]. Photo-thermal annealing is a promising means for facile ordering of BCP materials. For instance, it has already been demonstrated that one can use graphene as the light-absorbing layer, allowing ordering on flexible and curved substrates [582].

A clever extension of zone annealing methods is to exploit the annealing zone to simultaneously shear-align the BCP film. Adding a soft elastic cladding to the BCP film (typically poly(dimethyl siloxane), PDMS) allows for spontaneous shearing during CZA, owing to the differential thermal expansion between the soft cladding and the rigid substrate. It has been demonstrated for both CZA [156, 407, 583, 584] and LZA [57, 119, 211, 585] approaches that this ‘soft shear’ (SS) mode allows the rapid formation of highly-aligned morphologies. For instance, SS-LZA can generate highly-aligned ($\sigma_\phi < 1^\circ$) BCP morphologies in $< 10 \text{ s}$. SS-LZA was also used to probe the fundamental origin of BCP response to shear forces [585], where it was found that the relaxation time of the BCP morphology (τ_r , Figure 5b) plays a critical role. Soft BCP materials with relaxation times smaller than the shearing time scale (inverse shear rate) will not respond to the shear field, since they relax and dissipate the strain field faster than it is generated. Conversely, stiff materials with long relaxation times are amenable to shear-alignment. Materials with relaxation times roughly commensurate to the shearing time scale will be ‘responsive’ to the shear rate (*i.e.* alignment will depend on shear rate). Thus, while in static shear the ordering depends primarily on the shear stress [586], in dynamic shearing the shear rate plays a critical role [587].

Overall, thermal processing that is spatially heterogeneous and temporally dynamic provide a powerful means of controlling BCP ordering (Figure 2, upper-right), while employing relatively simple experimental apparatus (Figure 8). In general, these methods do not require exotic substrates or sample preparation, and thus are amenable to use in a manufacturing context. However, many questions remain unanswered regarding how self-assembly responds to non-trivial spatio-temporal thermal gradients.

9. Discussion

Figure 2 organizes the wide variety of BCP ordering methods according to the degree of spatial and temporal control. Oven annealing is the most straightforward method, but provides neither spatial nor temporal control of the ordering process. New techniques have pushed ever-further into providing more detailed control over the spatial environment and temporal history of ordering, and have thereby delivered improved (faster and more controllable) assembly. In comparing different methods of accelerating self-assembly, one must be cognizant not only of the ordering time itself, but also of additional costs of time and complexity associating with preparation of the substrate, sample, or experimental apparatus. For instance, epitaxial methods provide rigorous control of BCP assembly, and allow precise defect-free BCP patterns to be rapidly generated. However, the time associating with preparing the template must not be ignored. Similarly, BCP assembly can be controlled using interfacial energies, shear fields, dynamic annealing, etc.; however these methods require additional complexity with respect to sample preparation (*e.g.* special substrates) and annealing apparatus. Added complexity to the *annealing apparatus* is favorable in the sense that its construction is a one-time cost, whereas complex *substrates* incur a cost for every sample fabricated. In general, there is a tradeoff between the complexity of the ordering method, and the control the method provides.

There is a growing desire to transition self-assembling materials to an industrial context, where the issue of ordering timescales and processing complexity become extremely important. More complex ordering protocols are technologically undesirable owing to both increased cost, and decreased reliability. Many of methods described in the literature may not scale favorably to a high-throughput industrial context. For instance, solvent vapor (SVA) methods can be highly sensitive to processing conditions. Temperature variations vastly alter the film swelling ratio, and can even lead to catastrophic liquid condensation. This sensitivity to ambient temperature and temperature gradients may undermine the method in an industrial context. Conversely, preliminary results suggest that solvent immersion (DIA) may be a more industry-friendly alternative, accessing the same ordering mechanisms as SVA in a more robust manner. Electric and magnetic field alignment is relatively robust, and exploits well-established technology. However, the response of self-assembling materials to these fields is weak, thus limiting the industrial utility of these methods.

Industrial processing frequently benefits from being implemented as a continuous process (*e.g.* roll-to-roll) instead of a batch process. Whereas most annealing methods (oven, microwave, SVA, etc.) are a serial process, many newer methods (CZA, LZA, DIA) are very much amenable to roll-to-roll processing [579, 580]. Grapho- and chemo-epitaxy require stringent lithography to

form the guiding prepattern. In this sense, these methods are too expensive for fabrication of large quantities of ordered nanomaterials. On the other hand, these methods exploit the extremely mature and reliable infrastructure of modern micro-electronic manufacturing. It thus seems quite possible that BCP materials, ordered using lithographic templates, will play a role in future nano-electronics device manufacturing; in this context, the formation of a lithographic guiding pattern is obviously commensurate in complexity with other manufacturing steps.

Given the diversity of ordering methods, an obvious approach is to combine strategies; indeed combined annealing techniques are increasingly common. Solvent annealing techniques have been conveniently combined with other methods. A combination of SVA, thermal annealing (220 °C), and a neutral substrate demonstrated efficient ($\alpha = 0.33$) ordering [470]. Microwave annealing can be conveniently combined with SVA if solvent is included in the sealed processing vessel [117, 468, 554]. Epitaxial [588] or nanoimprint [425] methods can benefit from local solvent exposure. Local photo-thermal annealing can be performed in concert with solvent exposure to enhance ordering kinetics [428]. Vogt *et al.* have demonstrated that soft-shear (SS) alignment can be generated using solvent fields; that is, solvent uptake/evaporation induces swelling/contraction of a PDMS capping layer, which will shear an underlying BCP film [291, 292, 589]. This technique thus cleverly combines shear-alignment with SVA processing. Graphoepitaxy can be combined with CZA [574] or electric-field [590] alignment to enable synergistic ordering. It is likely that further combinations of ordering methods will yield new insights into the fundamentals of self-assembly (by comparing synergistic *vs.* antagonistic aspects), as well as further improvements in ordering kinetics. However, the increased complexity of combined approaches is not attractive in an industrial context.

The diversity of fast assembly techniques, as well as the impressively short ordering timescales that have been demonstrated, may lead one to believe that BCP ordering is a solved problem. However, as the boundaries of BCP ordering are pushed further, the issue of assembly time will reappear. For instance, there is considerable interest in materials that have a very large χN , which involves correspondingly arrested dynamics. High- N materials are attractive for pushing self-assembly to larger lengthscales. High- χ materials are of great interest because this sharpens the domain interface (presumably decreasing LER in patterning applications), and allows access to smaller repeat spacings [591]. That is, with high- χ materials, one can use a smaller N (with correspondingly smaller L_0) while still achieving proper phase separation at processing temperatures [592]. Similarly, introduction of blend components that increase χ will also slow the assembly kinetics. More elaborate polymer architectures (*e.g.* multiblocks) may also increase entanglements and hinder assembly. Thus, the kinetics of assembly remains a pertinent issue.

An emerging issue in the assembly of block-copolymers is the pathway-dependence of self-assembly. Although BCP ordering is often described in terms of the equilibrium phase diagram, and the associated equilibrium morphologies (Figure 1a), it is known that the structures observed experimentally are very often influenced by non-equilibrium aspects (kinetic trapping, metastable states, etc.). An example is shown in Figure 9a, which depicts the energy landscape for a BCP thin film. An as-cast polymer film is disordered, trapped in a high-energy configuration. Thermal annealing induces rapid phase separation, and the formation of a

nanoscale morphology. However, this results in a large number of small grains with uncorrelated orientations. Such a poly-grain sample will coarsen very slowly, owing to the innumerable energy barriers in the self-assembly landscape. By comparison, if the initially disordered film is exposed to a rapid and intense shear force, long-range orientational correlations can be imposed before phase separation has appreciably begun [211]. This ‘latent alignment’ state has long-range (macroscopic) correlations, even though the nanoscale morphology has not yet developed. Thermal annealing of this state will rapidly generate a monolithically-aligned sample, since the material will simply descend into the adjacent global energy minimum. Thus, a particularly efficient ordering pathway for a BCP sample is to use an intense shear field to break symmetry, after which conventional thermal annealing will rapidly yield a highly-ordered material. This is of course a generic phenomenon; *e.g.* suitable application of an electric or magnetic field will similarly select an efficient ordering pathway.

Deng *et al.* used simulations to study the ordering of hexagonal patterns within confinement volumes [593]. By nucleating grain growth at the corners of a confinement volume, grains growing at great distances from one another are implicitly correlated, and thus merge to form a defect-free pattern (Figure 9b). Similar motifs have been observed experimentally in graphoepitaxy experiments; in general, careful preparation of guiding templates can thus select efficient and rapid ordering pathways.

An additional non-equilibrium effect to consider in BCP assembly is the appearance of transient states; that is, during BCP assembly one frequently observes configurations that do not persist if annealing is continued. While these transient states can be viewed as a nuisance, they can also be exploited. For instance, annealing can be terminated at an appropriate moment, thereby selecting a non-equilibrium morphology or orientation. Figure 9c shows an example of a cylinder-forming BCP thin films that undergoes two reordering transitions [238]. A disordered film initially forms randomly-packed vertical cylinders, which reorder into the expected hexagonally-packed cylinder domains. This well-ordered vertical cylinder state is also transient, with a reorientation transition eventually converting the system into a horizontal-cylinder morphology. With appropriate annealing protocol, the transient vertical-cylinder state could be selected, despite the lack of neutral substrate conditions. It was also observed that the final horizontal-cylinder state was influenced by the intermediate states; *e.g.* the final grain anisotropy is influenced by the heating rate during annealing. Overall, the growing number of examples of non-equilibrium self-assembly of BCP systems suggests an opportunity: by carefully designing the ordering pathway, desired structures (including non-equilibrium structures) can be selected.

In summary, a wide variety of methods have been devised for controlling the order of BCP materials. These methods can often control the type and orientation of the BCP morphology, either by directly templating it, or by more subtly biasing the BCP assembly energetics. Simultaneously, these methods have provided improved control over the self-assembly kinetics. Whereas BCP thin films typically require hours or days of annealing under oven annealing conditions, similar levels of order can now be achieved in seconds or even milliseconds. Moreover, modern BCP processing methods allow one to align the morphology, creating macroscopically-ordered materials in mere seconds. Assembly timescales have been accelerated

to the point that wide deployment for certain applications now seems feasible. Nevertheless, continued progress is required in order to combine rapid assembly with the detailed structure control, and low defect densities, that high-performance applications demand.

10. Figures

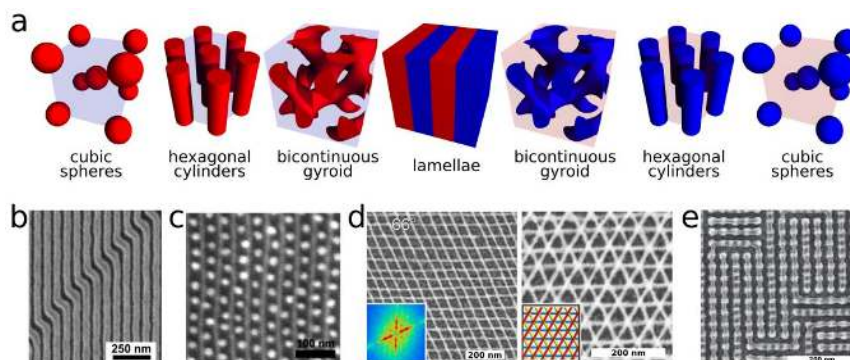


Figure 1: (a) Bulk equilibrium morphologies formed by diblock-copolymers. (b-e) Examples of more exotic structures that can be generated using BCP architectures. (b) Substrate chemical patterns can be used to direct BCP ordering, producing desired local geometries. Reproduced with permission from the American Chemical Society 2007. (c) BCP-derived patterns can be used to organize subsequent BCP materials [200]. Reproduced with permission from the American Chemical Society 2013. (d) BCP-derived nanowires can be layered to generate meshes of arbitrary symmetry [119]. Reproduced with permission from the Nature Publishing Group 2015. (e) Minimal topographic guiding patterns can be designed to enforce complex patterns in BCP assembly [185]. Reproduced with permission from the Nature Publishing Group 2014.

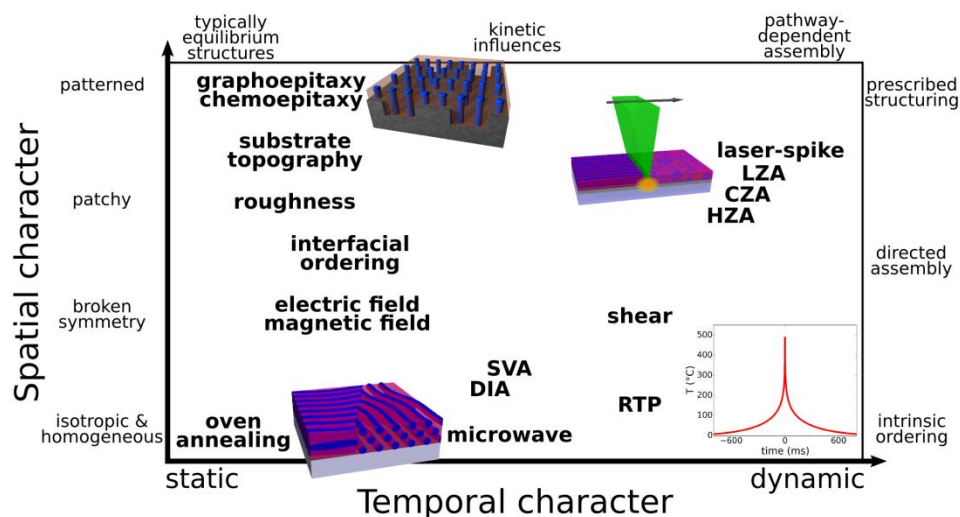


Figure 2: Methods for ordering block copolymers can be organized in terms of their spatial characteristics (homogeneous to patterned) and temporal character (static to dynamic). Oven annealing is spatially homogeneous, and temporally static (other than brief ramping/cooling phases). Solvent vapor annealing (SVA) and direct immersion annealing (DIA) are similar, though can be more sensitive to kinetic effects (*e.g.* quenching). A variety of directed self-assembly methods rely on breaking spatial symmetry, using fields, or substrate topography/chemistry. Techniques such as rapid thermal processing (RTP) use a dynamic thermal history (spatially-homogeneous thermal spike). Various zone annealing or local heating methods (possibly photo-thermal) exploit both dynamic thermal history (heating spike), and spatially non-uniform processing (spatial thermal gradients). This includes hot zone annealing (HZA), cold zone annealing (CZA), laser zone annealing (LZA), and laser-spike annealing.

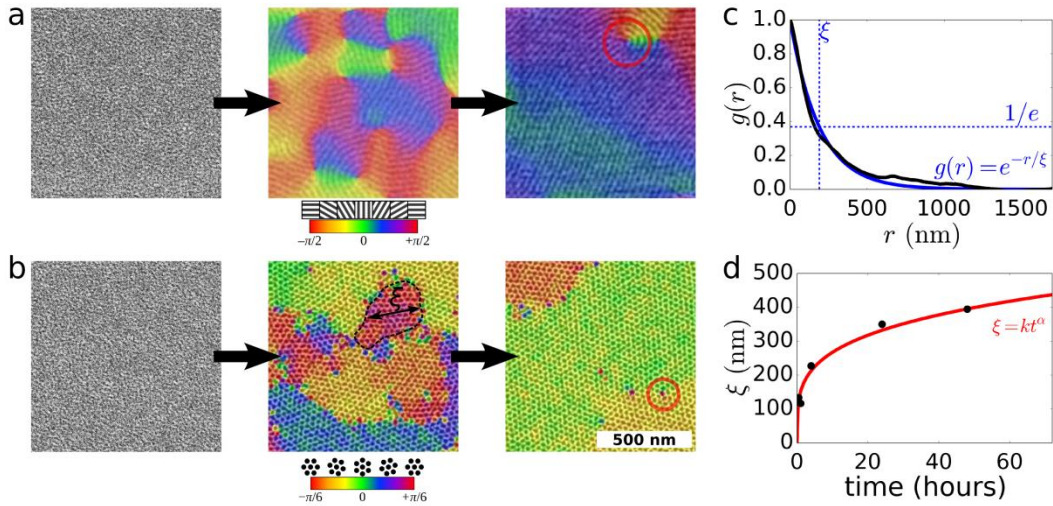


Figure 3: Examples of ordering behavior observed for BCP thin films. (a) Lamellar or horizontal cylinder morphologies appear as line patterns in microscopy (SEM or AFM), whereas (b) vertical hexagonally-packed cylinders appear as dot patterns. An as-cast film is initially disordered, but as annealing proceeds, well-defined morphologies appear. The local orientation of the morphology can be obtained using image analysis (color-coded in images). An example grain is highlighted by the dashed contour. Longer annealing times leads to larger domains of preserved orientation (larger grain sizes); though discrete topological defects may remain (red circles). (c) A quantitative grain size (ξ) can be computed from the orientation data by fitting the orientation correlation function, $g(r)$, to an exponential decay. (d) Grain growth as a function of annealing time typically follows a power-law.

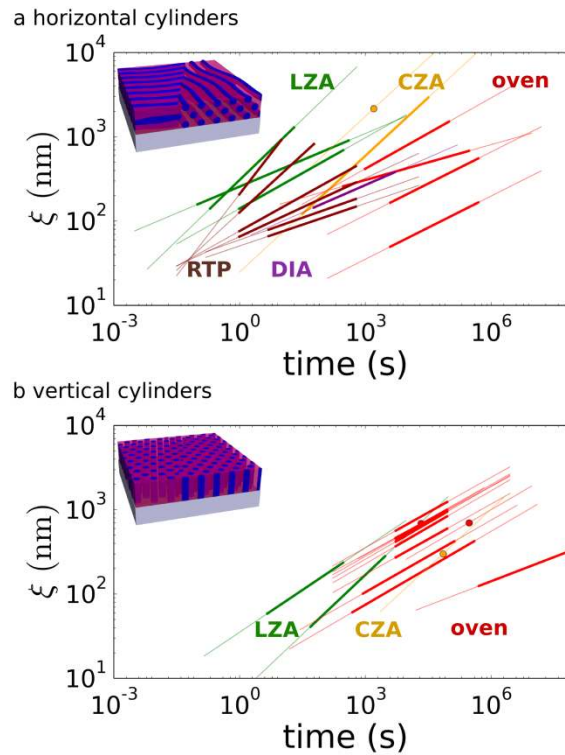


Figure 4: Grain growth curves for (a) horizontal cylinders, and (b) vertical cylinders. Data from a variety of literature sources are combined (thick lines are the power-law fits to the experimental data, thin lines are extrapolations) for oven-annealed samples (red) [57, 216, 219, 220, 223], rapid thermal processing (RTP) [237], direct immersion annealing (DIA) [474], cold zone annealing (CZA, orange) [56, 573], and laser zone annealing (LZA, green) [57]. The substantial spread in the curves comes from combining results for different materials (molecular weights) and film thicknesses; nevertheless, it is clear that dynamic annealing methods can yield improved grain sizes compared to oven annealing.

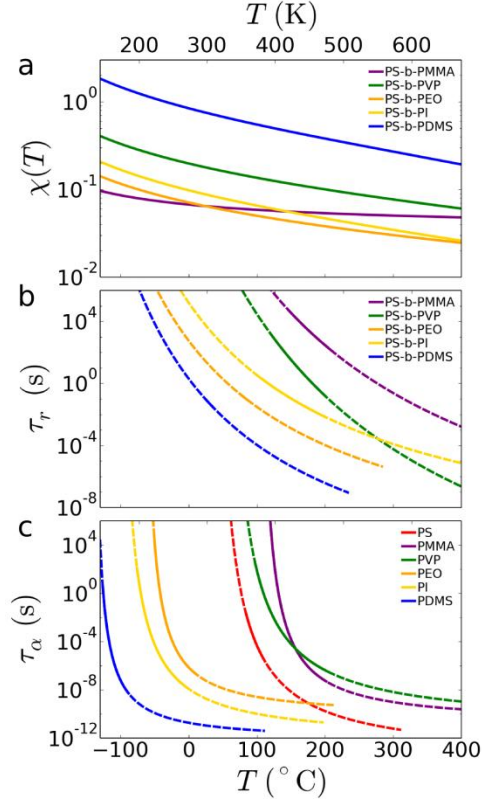


Figure 5: Intrinsic polymer and copolymer properties influence ordering timescales, including the temperature-dependence of these properties. (a) For BCPs, the segregation strength (χ) influences the sharpness of interfaces, and kinetics of assembly. A large χ promotes rapid phase separation, but hinders reordering. Annealing at higher temperature (smaller χ) instead allows larger fluctuations and more rapid assembly. (b) The fluctuation relaxation time of the morphology is estimated using: [585, 594] $\tau_r = \lambda^2 / D_0$, where λ is a characteristic lengthscale (30 nm used in figure as a representative value) and D_0 is an estimate of the polymer diffusion coefficient (PS-*b*-PMMA [595], PS-*b*-P2VP [596, 597], PS-*b*-PEO [598], PS-*b*-PI [248], PS-*b*-PDMS [598]). The BCP dynamics increase rapidly as temperature is increased (dashed lines represent extrapolations assuming $D \sim D_0 \exp(-\alpha\chi N)$ where α is a constant). For ordering to occur, there must be match between the timescale of BCP response, and the selected driving forces. (c) The intrinsic polymer segmental dynamics (relaxation times, τ_α) vary substantially for different polymer materials. Curves are based on literature values (PS [599], PMMA [600], P2VP [601], PEO [602], PI [603, 604], and PDMS [605]); dashed lines are extrapolations using the Vogel-Fulcher equation [606-609].

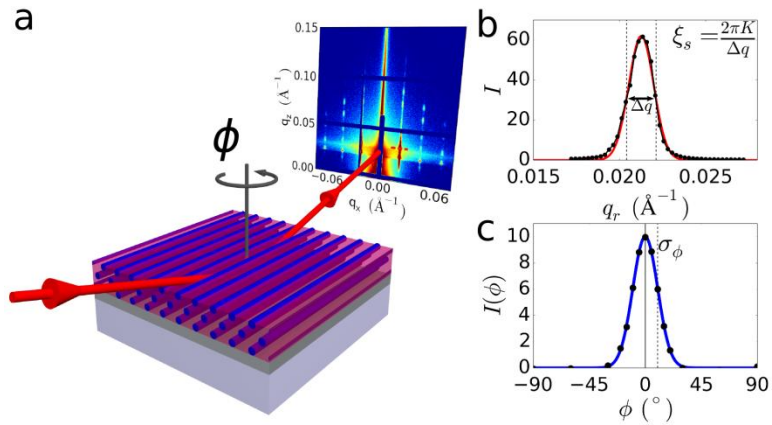


Figure 6: (a) Grazing-incidence small-angle x-ray scattering (GISAXS) can be used to measure the nanoscale structure in thin films. An x-ray beam is reflected off of substrate-supported sample at shallow angle. The peaks observed in the two-dimensional scattering image encode detailed information about structure order, including morphology type, nanostructure orientation, and average grain size. (b) A linecut through an x-ray area detector image (red dashed line) can be used to analyze the shape and width of a scattering peak. The width (Δq) can be converted into an estimate of the grain size (ξ_s). (c) Monitoring the intensity of a scattering peak as a function of the in-plane sample rotation angle (ϕ) can be used to quantify the angular spread of the morphology (σ_ϕ). For anisotropic samples, this allows the degree of alignment to be assessed.

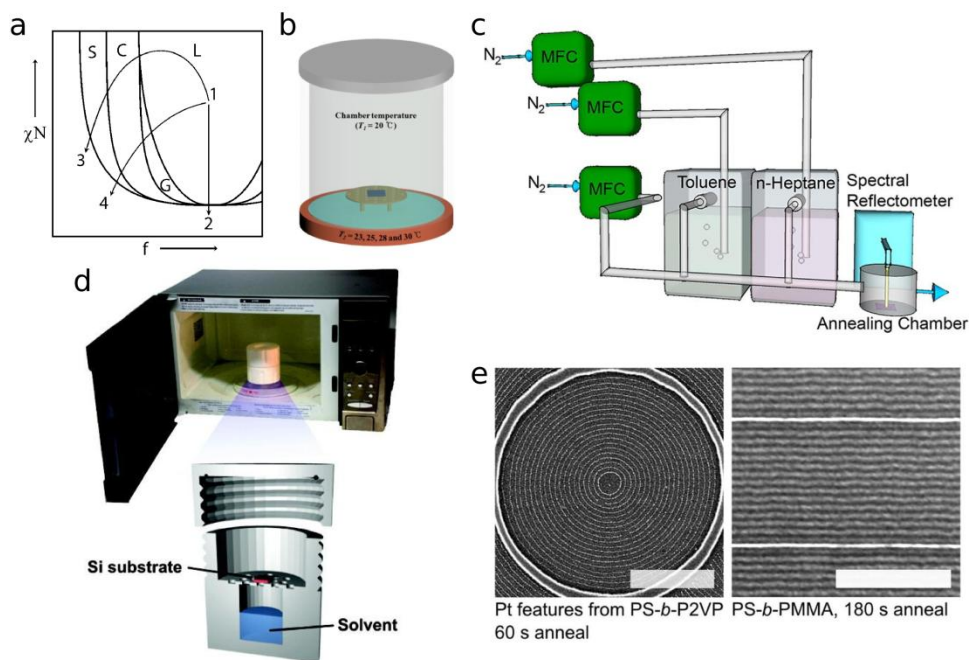


Figure 7: (a) SVA can be understood in terms of shifting the BCP material through its phase diagram. The arrows represent different swelling pathways (1–2 non-selective solvent, 1–4 partially selective, 1–3 highly selective) [439]. Reproduced with permission from the American Chemical Society 2008. (b) Typical experimental setup for chamber-based (‘jar’) SVA processing. The sample is exposed to solvent vapors within a sealed vessel; concomitant control of chamber temperatures provides additional control [452]. Reproduced with permission from the American Chemical Society 2016. (c) Example of a flow-through SVA processing setup. Mass flow controllers (MFC) are used to control the composition of the atmosphere used for annealing [456]. Film swelling can be tracked *in-situ* using interferometry. Reproduced with permission from the American Chemical Society 2012. (d) Example of microwave SVA setup, wherein a sealed Teflon vessel, including solvent reservoir, is heated inside a commercial microwave oven [468]. Reproduced with permission from the American Chemical Society 2011. (e) SEMs of BCP materials that were microwave annealed under SVA conditions, on substrates with topographic features (scale bars 500 nm) [117]. The left image shows a ring-shaped substrate feature, while the right shows the influence of two parallel topographic lines. The combination of microwave heating, solvent exposure, and topographic features, provides strong enforcement of structural order. Reproduced with permission from the American Chemical Society 2010.

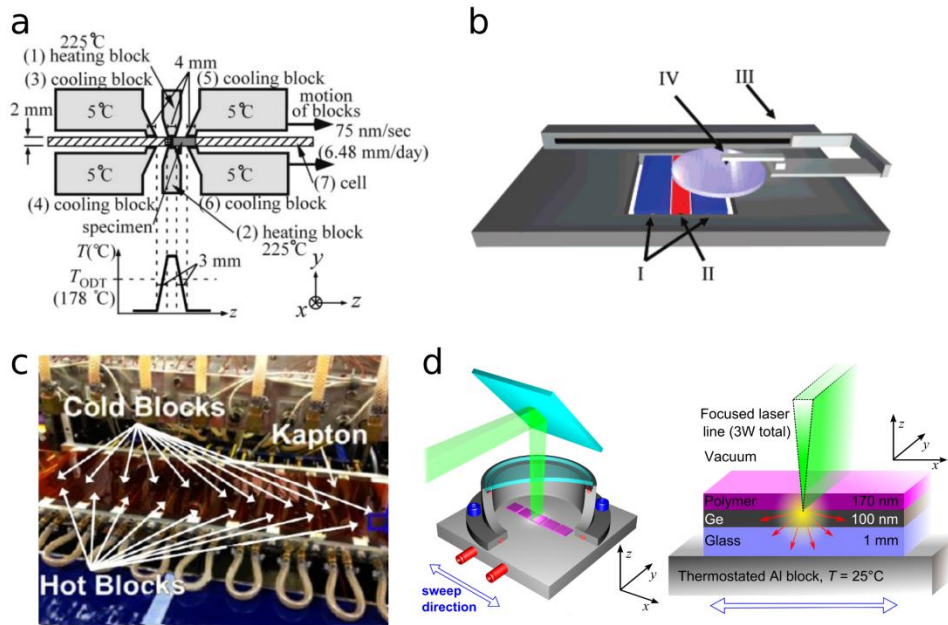


Figure 8: Experimental designs for zone annealing of block copolymers. (a) The hot zone annealing (HZA) setup described by Hashimoto *et al.* translates a thin sample chamber (containing a bulk BCP material) through a hot-zone defined by heating blocks [562]. Reproduced with permission from the American Chemical Society 2007. (b) Karim *et al.* developed a ‘cold’ zone annealing (CZA) setup for translating BCP thin films (cast on rigid substrates) across a thermal zone defined by thermostated blocks [56]. Reproduced with permission from the American Chemical Society 2007. (c) This approach was elaborated to enable roll-to-roll processing of films on flexible substrates [579]. Reproduced with permission from the American Chemical Society 2013. (d) Majewski and Yager developed a laser zone annealer (LZA) which enables zone annealing of thin films using larger thermal gradients [57]. Reproduced with permission from the American Chemical Society 2015.

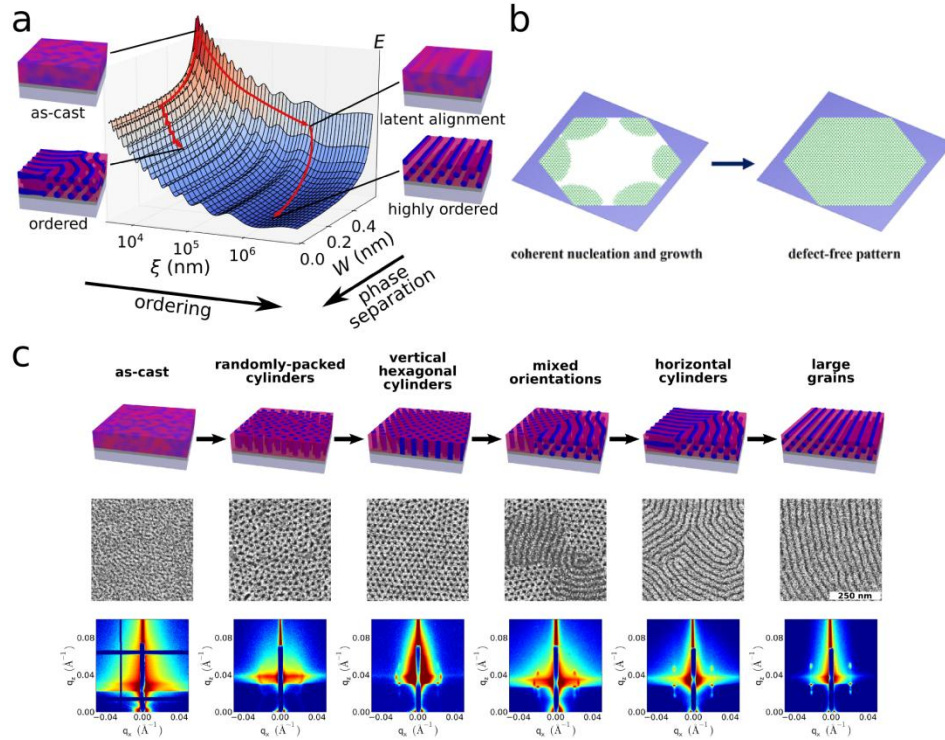


Figure 9: Examples of pathway-dependent ordering of BCPs. (a) Energy landscape for oven vs. shear ordering [211]. Reproduced with permission from the American Chemical Society 2015. Oven annealing from a disordered as-cast state induces rapid phase separation, and subsequent slow grain coarsening of an ordered state. Rapid shear can instead first break film symmetry, introducing long-range correlations (large ξ). Subsequent thermal annealing causes this ‘latent alignment’ state to spontaneously develop into a well-aligned and thus highly-ordered BCP films. (b) Simulation of corner-induced heterogeneous nucleation for a block-copolymer/homopolymer blend, where the coherence between nucleation points drives towards a defect-free final state [593]. Reproduced with permission from the American Chemical Society 2015. (c) Examples of transient states observed during thermal annealing of a BCP cylinder phase [238]. Although the final (equilibrium) state for the given thin film thickness is horizontally-ordered cylinders, one observes other states at earlier ordering times, including randomly-packed cylinders, and vertically-oriented cylinders. Reproduced with permission from the Royal Society of Chemistry 2016.

11. Acknowledgments

This work took place at the Center for Functional Nanomaterials, which is a U.S. DOE Office of Science Facility, at Brookhaven National Laboratory under Contract No. DE-SC0012704.

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