Recent advances in collisional effects on spectra of molecular gases and their practical consequences
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Highlights

- A review on the progress made in the last decade on pressure effects on absorption shapes
- High accuracy measurement techniques
- Theories, models and available data for the absorption shapes
- Consequences for remote sensing, metrology and heat transfer applications
- Over 700 references
Recent advances in collisional effects on spectra of molecular gases and their practical consequences

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ABSTRACT

We review progress, since publication of the book "Collisional effects on molecular spectra: Laboratory experiments and models, consequences for applications" (Elsevier, Amsterdam, 2008), on measuring, modeling and predicting the influence of pressure (ie of intermolecular collisions) on the spectra of gas molecules. We first introduce recently developed experimental techniques of high accuracy and sensitivity. We then complement the above mentioned book by presenting the theoretical approaches, results and data proposed (mostly) in the last decade on the topics of isolated line shapes, line-broadening and -shifting, line-mixing, the far wings and associated continua, and collision-induced absorption. Examples of recently demonstrated consequences of the progress in the description of spectral shapes for some practical applications (metrology, probing of gas media, climate predictions) are then given. Remaining issues and directions for future research are finally discussed.

Key words: pressure effects on spectral shapes; experimental techniques; theories and models; available data; consequences for applications
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<td>1D-CMDS</td>
<td>One-Dimensional Cavity-Mode Dispersion Spectroscopy</td>
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<td>ACF</td>
<td>Auto-Correlation Function</td>
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<td>BB</td>
<td>Billiard-Ball</td>
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<td>BWO</td>
<td>Backward Wave Oscillator</td>
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<td>CAVIAR</td>
<td>Continuum Absorption at Visible and Infrared wavelengths and its Atmospheric Relevance</td>
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<tr>
<td>CC</td>
<td>Close-Coupling</td>
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<td>CEAS</td>
<td>Cavity Enhanced Absorption Spectroscopy</td>
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<td>CIA</td>
<td>Collision-Induced Absorption</td>
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<td>CMDS</td>
<td>Classical Molecular Dynamics Simulations</td>
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<td>CMWS</td>
<td>Cavity Mode-Width Spectroscopy</td>
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<td>CRDS</td>
<td>Cavity Ring-Down Spectroscopy</td>
</tr>
<tr>
<td>CS</td>
<td>Coupled-States</td>
</tr>
<tr>
<td>CW</td>
<td>Continuous Wave</td>
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<td>DBT</td>
<td>Doppler Broadening Thermometry</td>
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<td>DCS</td>
<td>Dual Comb Spectroscopy</td>
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<tr>
<td>DFBL</td>
<td>Distributed Feed Back diode Laser</td>
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<tr>
<td>ECDL</td>
<td>External Cavity Diode Laser</td>
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<tr>
<td>ECS</td>
<td>Energy-Corrected Sudden</td>
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<tr>
<td>EOM</td>
<td>Electro-Optic phase Modulator</td>
</tr>
<tr>
<td>FP</td>
<td>Fabry-Pérot</td>
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<tr>
<td>FS-CRDS</td>
<td>Frequency-Stabilized CRDS</td>
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<tr>
<td>FSR</td>
<td>Free Spectral Range</td>
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<tr>
<td>FTS</td>
<td>Fourier Transform Spectrometer</td>
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<tr>
<td>FWHM</td>
<td>Full Width at Half Maximum</td>
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<tr>
<td>GP</td>
<td>Galatry Profile</td>
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<tr>
<td>HAPI</td>
<td>HITRAN Application Programming Interface</td>
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<tr>
<td>HC</td>
<td>Hard Collision</td>
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<tr>
<td>HTP</td>
<td>Hartmann-Tran Profile</td>
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<tr>
<td>ICL</td>
<td>Interband Cascade Laser</td>
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<td>IOS</td>
<td>Infinite-Order Sudden</td>
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<tr>
<td>KS</td>
<td>Kélson-Storer</td>
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<tr>
<td>LM</td>
<td>Line-Mixing</td>
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<tr>
<td>MT_CKD</td>
<td>Mlawer-Tobin_Clough-Kneizys-Davies</td>
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<tr>
<td>NICE-OHMS</td>
<td>Noise-Immune Cavity-Enhanced Optical Heterodyne Molecular Spectroscopy</td>
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<tr>
<td>OFC</td>
<td>Optical Frequency Combs</td>
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<tr>
<td>OF-CEAS</td>
<td>Optical-Feedback Cavity-Enhanced Absorption Spectroscopy</td>
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<td>pCqSDHC</td>
<td>partially-Correlated quadratic-Speed-Dependent Hard Collision</td>
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<td>QCL</td>
<td>Quantum Cascade Laser</td>
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<td>RB</td>
<td>Robert-Bonamy</td>
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<td>RP</td>
<td>Rautian Profile</td>
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<td>SC</td>
<td>Soft Collision</td>
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<tr>
<td>SDBB</td>
<td>Speed-Dependent Billiard-Ball</td>
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<td>SDVP</td>
<td>Speed-Dependent Voigt Profile</td>
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<tr>
<td>SI</td>
<td>Système International d’Unités</td>
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<tr>
<td>SNR</td>
<td>Signal-to-Noise Ratio</td>
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<tr>
<td>Abbreviation</td>
<td>Description</td>
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<tr>
<td>TCCON</td>
<td>Total Carbon Column Observatory Network</td>
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<tr>
<td>VIPA</td>
<td>Virtually Imaged Phased Array</td>
</tr>
<tr>
<td>VMR</td>
<td>Volume Mixing Ratio</td>
</tr>
<tr>
<td>VP</td>
<td>Voigt Profile</td>
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1. Introduction

In 2008, some authors of this paper completed a book [1] devoted to the effects of pressure (of intermolecular collisions) on the spectra of gas molecules. They reviewed the processes involved, the available theories, models and experimental results, and discussed the consequences for some practical applications. Considerable qualitative and quantitative progress has been made on all aspects of this subject that are discussed in this book since its publication a decade ago. The aim of the present review is to give the reader an overall view of these advances together with an update of the bibliography on the subject, including recent techniques for measurements of light absorption by gases. This rapidly growing field has many relevant publications, here we review those that we are aware of and that demonstrate new progress in one or more aspects of the research.

The remainder of this article is organized as follows: Section 2 is devoted to laboratory experimental techniques, a topic not treated in [1]. While it focuses mainly on recent developments based on the use of lasers and often of high finesse cavities, which enable measured absorption spectra with unprecedented high SNRs and accuracies, Fourier transform and terahertz techniques are also discussed. The new spectral-shape theories and models, as well as recently made comparisons between calculated and measured results are the subjects of Sec. 3. In the latter, the profiles of isolated lines, the pressure-broadening and -shifting coefficients, line-mixing processes, the (far) line wings and continua, and collision-induced absorption are successively considered (following chapters III-VI of [1]). Some recently made available spectral-shape parameters in these fields are presented in Sec. 4 together with the evolutions and current statuses of spectroscopic databases. The effects of collisions on molecular spectra are important to many applications, as discussed in Chap. VII of [1]. Section 5 is devoted to the impact of achievements on this topic in a variety of other fields. These include metrology, the probing of various media including atmospheres, and radiative transfer and climate. Remaining problems and possible directions for future research are finally discussed in Sec. 6.

2. Laboratory experimental techniques

2.1 Introduction

Molecular spectra reveal collisional effects through changes in their shapes recorded along a frequency axis. To properly test the most advanced theories and models it is mandatory to minimize experimental biases, at least below the expected precision of the predictions. In addition, some applications (Sec. 5) require extremely reliable simulations or analysis of spectra. These constraints call for accuracy in both the frequency and absorption axes, which are intimately linked by the spectral profile, as well as for the accurate determination of the composition, temperature and pressure of the sample gas (Sec. 5.2.2). As an example, consider a direct absorption experiment in which a laser probes a gas and the transmission is recorded. Any uncontrolled laser-intensity noise would obviously convert into an effective absorption noise, impairing the fast and precise determination of a line contour. To some extent, this may be corrected for by stabilizing the instantaneous laser power that irradiates the gas sample, for example by using an acousto-optic modulator in a servo configuration [2]. However, while such a method can lead to baseline relative intensity noise levels approaching $10^{-5}$, going below this degree of intensity stabilization is practically impossible. In addition, fluctuations in the optical frequency of the probe laser that occur on time scales shorter than the characteristic data-acquisition rate are known as “frequency-jitter” and are manifest as noise in acquired spectra, particularly in regions of steep absorption. Worse, if the laser source, or the measurement of its optical frequency, slowly drifts during an experiment, the absorption spectrum is irreversibly deformed. Nevertheless, probe-laser jitter
can be substantially reduced by active stabilization methods that incorporate a reference oscillator. These remarks show that an optimized classical spectrometer for absorption measurements should use an optical source having low amplitude and frequency noises, with a stable emission frequency that must be accurately monitored and determined.

Nowadays, the most accurate and sensitive techniques for absorption measurements use CW lasers as the light source and resonant optical cavities surrounding the sample gas. When compared to classical incoherent sources and pulsed lasers, CW lasers provide relatively low intensity noise and narrow emission widths capable of probing individual cavity resonances (modes). Resonant optical cavities comprise two or more high-reflectivity dielectric mirrors that sustain standing-wave or traveling-wave intra-cavity fields. Using such a resonator to enclose the gas sample increases the sensitivity by enhancing the path length of the photons trapped inside the cavity. This enhancement increases with the mirror reflectivities, as explained later. Also, because of the relatively long photon lifetime ($\tau$) in the cavity and coherent nature of the excitation, these cavities are highly efficient frequency filters that can potentially overcome the effect of residual laser-frequency jitter. Indeed, the optical resonances manifest as a comb of sharp transmission features whose width ($\Delta \nu$) and spacing ($\nu$) are typically in the ranges of kHz and 100 MHz, respectively. For instance, an optical cavity comprising two mirrors of reflectivity $R=0.99999$ separated by 1 m, corresponds to $\tau = 333 \mu$s, $\Delta \nu = 477$ Hz and an effective path length of 100 km. This example illustrates the long photon lifetime, narrow mode width and extensive path length achievable with laboratory-scale high-finesse cavities.

Optical cavities are most commonly used to interrogate molecular absorption in two different ways. One can measure either the steady-state transmission of incident light through the cavity or the photon lifetime, both of which are sensitive to light absorption by the cavity medium. In both cases, the highest spectral resolution is achieved using mode-by-mode cavity excitation to yield spectra sampled at well-defined frequency intervals. The first approach leads to cavity-enhanced absorption spectroscopy (CEAS, Sec. 2.2) and the second to cavity ring-down spectroscopy (CRDS, Sec. 2.3). Importantly, unlike CEAS, CRDS is immune to intensity noise in the light source and to absorption outside the cavity. There are advanced versions of CRDS in which the resonant frequencies are made immune to laser-frequency drift and/or external perturbations via active cavity or laser stabilization methods. These include the frequency-stabilized CRDS (FS-CRDS) technique [3,4] and optical feedback frequency-stabilized CRDS (OFFS-CRDS) [5,6]. Both approaches are insensitive to laser-intensity and -frequency noises, and are based on precise and accurate observations of mode-frequency intervals ($x$-axis) and time ($y$-axis). They can provide line profiles with minimal instrumental distortion and SNRs routinely ranging from $10^3$ to $2\times10^4$ [7-10] with exceptional cases in the $2\times10^3$ to $10^6$ range [5,11,12]. Other cavity-enhanced methods include (Sec. 2.5) cavity mode-width spectroscopy (CMWS) which measures absorption-dependent widths of individual cavity resonances, and one-dimensional cavity-mode dispersion spectroscopy (1D-CMDS) [13] which measures frequency shifts of the cavity resonances to quantify gas-induced dispersion. We note that CMWS is a high-resolution variant of CEAS that uses the mode width instead of the amplitude decrease to measure absorption and thus overcomes the need for spectrally broadband intensity normalization. The 1D-CMDS also shares this property and yields spectra where both axes are based upon measurements of the optical frequency.

Interestingly, optical cavities also can be simultaneously probed at several wavelengths in a multiplexed manner. For this, femto-second laser sources or electro-optic modulated CW lasers that consist of combs of phase-locked narrow emitters [14] can be efficiently coupled to an optical cavity. This can be achieved in a raw (cavity-enhanced optical frequency comb spectroscopy) [15-19], one-by-one (Vernier effect) [20,21], or in self- or multi-heterodyne
configurations [22] to yield both field amplitude and phase information quantifying complex-valued line shapes.

In the remainder of Sec. 2.1 we provide a general description of light-matter interaction in an enhancement cavity. For simplicity, we consider a FP interferometer having two identical dielectric (absorption-free) mirrors with reflectivity $R$, and transmission $T$ such that $R=1-T$. Neglecting intracavity-medium scattering or other losses, considering a single transverse mode and in the limit of a linear absorption process, the complex-valued transmittance $\tilde{y}(\nu)$ of the incident field at frequency $\nu$ is given by the Airy formula:

$$\tilde{y}(\nu) = \frac{T \exp[-(\alpha l + i\Delta \phi)/2]}{1 - R_c \exp(-i\Delta \phi)}, \quad (1)$$

where all variables (except for $l$) on the right-hand-side depend upon $\nu$. $\alpha$ is the intensity-based absorption coefficient, $l$ is the resonator length, $\Delta \phi = 2\pi\nu t_r$ is the phase shift corresponding to the round-trip time $t_r = 2l/c$ (with $c$ the speed of light), and $R_c = R \exp(-\alpha l)$ is the effective mirror reflectivity that incorporates the single-pass absorption loss of the medium. The resonant frequencies occur when $\Delta \phi$ is a multiple of $2\pi$. In the absence of absorption and dispersion effects, the modulus squared of the Airy formula reduces to a comb of equidistant peaks of unity transmission separated by the free spectral range (FSR) denoted by $\nu_f$. Absorption reduces the peak transmission and broadens the resonances, whereas dispersion in the medium shifts the positions of the resonances relative to the empty-cavity case (cf Sec. 2.5).

With the incorporation of models for absorption and dispersion, the preceding formulas can be used to calculate the cavity transmission (amplitude and phase) by summing over all relevant electromagnetic field components at one or more frequencies. Both heterodyne and intensity-based transmission measurements can be modeled. In the former case, the field transmitted by the cavity is combined with that of a local oscillator (generally either a single- or multi-frequency laser such as an OFC), which results in a complex-valued transmission signal at one or more heterodyne beat frequencies. Similarly, for intensity-based measurements at a given frequency, the real-valued transmission is obtained by squaring the modulus of Eq. (1).

Note that the complex Airy formula, which is a comb-like function of $\Delta \phi$ representing a series of resonances, can be reduced to a complex Lorentzian profile near an individual resonance. This is a good approximation when the cavity finesse $F$, given by $\pi \sqrt{R_c}/(1-R_c)$, is large and when $\Delta \phi \ll 1$. In this limit, we can write the complex field transmission for excitation of a single cavity mode as:

$$\tilde{y}(\nu) = \frac{T}{1 - R_c} \times \frac{\exp(-i\Delta \phi/2)}{1 - i(F/\pi \Delta \phi)}, \quad (2)$$

where $\Delta \phi = (2\pi\Delta \nu)/\nu_f$ and $\Delta \nu$ is the frequency detuning of the light source about the local resonance. Furthermore, for measurements of photon lifetime of the resonator (e.g., CRDS, Sec. 2.3), the time-dependent ring-down decay signal $s(t)$ is found by squaring the modulus of the Fourier transform of Eq. (2) which gives:

$$s(t) = s_0 \exp(-t/\tau), \quad (3)$$

with a frequency-dependent time constant

$$\tau(\nu) = \frac{l}{c[1 - R \exp(-\alpha l)]}. \quad (4)$$
These results illustrate the simple correspondence between the frequency- and time-domain responses for excitation of a single cavity mode. Assuming high mirror reflectivity ($R \sim 1$) and weak intra-cavity absorption ($\alpha l \ll 1$), Eq. (4) reduces to $1/[c t(v)] = \alpha(v) + 1/[c \tau_0(v)]$, where $\tau_0(v) = 1/[c(1 - R)]$ is the time constant in the absence of absorption. This relation indicates that the $x$ and $y$ axes of CRDS absorption spectra can be determined from measurements of frequency and time, respectively, without explicit determination of path length. The power transmitted by the cavity, $P_t(v)$ as detected by a photodiode placed after the resonator and assuming perfect mode matching, is given by the square of the modulus of Eq. (1). Assuming on-resonant excitation ($\Delta \phi = 0$), one has:

$$P_t(v) = P_0 \frac{T^2}{[1 - R \exp(-\alpha l)]^2} \exp(-\alpha l) ,$$

(5)

where all variables on the right-hand-side depend upon $v$ and $P_0$ is the incident power. For high mirror reflectivity and weak intra-cavity absorption, Eq. (5) can be expanded to first order in $\alpha l$, leading to:

$$P_t(v) = (1 - \alpha l_{\text{eff}}) P_0 ,$$

(6)

with

$$l_{\text{eff}} = 2l/(1 - R) .$$

(7)

Eq. (7) explicitly highlights the path length enhancement induced by the resonant cavity as mirror reflectivity and cavity finesse increase. This enhancement effect is referred to in the cavity-enhanced absorption spectroscopy (CEAS, Sec. 2.2) acronym.

Although the first mention of the use of a FP assembly to enhance intra-cavity absorption is by Jackson [23], O’Keefe and Deacon [24] were the first to use CRDS (cf Sec. 2.3) to measure molecular absorption spectra. In general, the reader may refer to Chapt. 1 of [25] for a deeper understanding of the CEAS process and to [26] for CRDS.

Except for Secs. 2.9 and 2.10, the next sub-sections describe recent experimental efforts toward accurate spectroscopy, essentially disregarding low-resolution or large-apparatus-function setups. We consider CW laser-based techniques with cavities to enhance sensitivity and/or resolution, which measure the cavity transmission (Sec. 2.2), the lifetime of photons trapped in the cavity (Sec. 2.3) or the cavity mode width (Sec. 2.5). The referencing of probe laser frequencies to an OFC for absolute calibration is also presented (Sec. 2.4). Laser-comb sources, which can be used with (Sec. 2.7) or without an enhancement cavity (Sec. 2.6), offering broadband coverage and/or multiplexed approaches also are discussed. Then, we evaluate (Sec. 2.8) the performance of dual-laser direct-absorption methods for high-precision line shape studies. Finally, the interests of Fourier transform spectroscopy and terahertz techniques for spectral-shape studies are discussed in Secs. 2.9 and 2.10, respectively.

Before discussing these various techniques, it is important to recall that obtaining spectra of very high quality is not the only criterion for accurate spectroscopic studies of pressure effects. Indeed, the reliability of the tests of theories and models as well as that of the spectral-shape parameters retrieved from fits of measurements also depend on the knowledge of the sample (composition, pressure, temperature, path length). Obviously, uncertainties on these experimental parameters can spoil many of the efforts made to improve the set-up and the quality of the data that it produces. While this rather technical and difficult issue is beyond the scope of this review, some discussions concerning the determination of the temperature can be found in some of the references cited in Sec. 5.2.1, the importance of knowing the gas composition being addressed in Sec. 5.2.2.

2.2 Cavity Enhanced Absorption Spectroscopy (CEAS)
An intuitive way to take advantage of the absorption-enhancement effect of a FP cavity consists in monitoring the frequency dependence of its on-resonance transmission as expressed in Eq. (5). This provides (within the limit of weak absorption) direct access to the absorption coefficient \( \alpha \) through a Beer-Lambert-like law that exhibits an enhanced path length [Eq. (7)]. Note that, for studies of narrow absorption lines and accurate determinations of their areas, the base length \( l \) and mirror properties must be accurately known because they govern the mode spacing and effective path length. Actually, the FP cavity length differs from a basic ruler-based measurement according to Gaussian mode theory [27,28] and may be determined from measurements of the local FSR (cf. Sec. 2.5). The mirror reflectivity can be determined from a CRDS measurement (Sec. 2.3) or by a cavity-mode width measurement (cf. Sec. 2.5). To address the problem of measuring absorption continua (Sec. 4.3), the mirror- and gas-dependent losses must also be independently characterized. Let us emphasize that the cavity mirrors’ properties are generally frequency dependent because of the present coating technology (dielectric films), but also because of the refractive nature of the intra-cavity probed medium. From [29], the magnitude of the absorption-induced mode shift is \( \approx 0.3c\alpha(v) \).

Referring again to a one-meter long FP cavity with 99.999% reflectivity mirrors (Sec. 2.1), a local absorption coefficient of \( 3.4 \times 10^{-7} \text{cm}^{-1} \) is sufficient to shift an FP resonance by its mode width. Furthermore, at wavelength of 1.6 \( \mu \text{m} \) for instance, a 1 nm variation of the cavity length (\( 10^{-9} \) relative) shifts all the FP resonances by about 200 kHz, which is more than 100 times the mode width. The use of high reflectivity mirrors therefore requires stable FP assemblies. On the other hand, typical tunable semiconductor lasers (e.g., telecommunications type) have line widths of the order of 1 MHz (jitter), obviously leading to extremely noisy cavity transmission under CW excitation. However, the optical cavity and laser noise sources are of different physical origin and act on different time scales. An optical cavity, as any mechanical assembly, exhibits a slow thermo-mechanical expansion (~1s scale) that sums with acoustic noise (<20 kHz) yielding time constants ranging from s to ms timescales, respectively. This makes it rather easy to control the cavity length, typically with piezoelectric transducers. Telecommunications semiconductor lasers typically exhibit white noise that extends over several MHz, making it difficult, but possible [30-32], to actively cancel the frequency noise on time scales comparable to the buildup time of the optical cavity. Note that external cavity diode lasers (ECDL) have narrower short-term line widths (< 500 kHz) than semiconductor lasers and are therefore better suited for electronic control loops that directly actuate laser current [33].

Several strategies have been developed to overcome highly intermittent laser-to-cavity-longitudinal mode overlap which occurs when the probe laser frequency and cavity resonance are not coupled. These methods include: (i) averaging a series of passages through resonance to reduce the intensity noise, known as Integrated Cavity Output Spectroscopy (ICOS) [34]. (ii) Off-axis injection of a FP cavity (OA-ICOS) [35] to induce the excitation of a series of higher-order transverse modes having various resonant frequencies. With an appropriate FP geometry, this results in quasi-continuous transmission, smoothing out the peaks of the Airy formula. Unfortunately, these two strategies are still limited in terms of SNR, essentially because of residual optical fringes, transverse-mode-dependent mirror losses and laser phase noise which manifests itself as fluctuations in the transmitted power. They are, therefore, not recommended for accurate line-profile determinations. (iii) Electronic or optical locking of the laser emission of an ECDL to a stable FP or other frequency reference is an efficient CEAS approach for accurate line-profile determination (Sec. 2.5). Several methods can serve this purpose, e.g., PDH [36], tilt-lock [37] and NICE-OHMS [38]. An alternative attractive method consists in optical-feedback locking (OF-CEAS) [39]. Under certain conditions, the laser self-locks to the mode of the FP to which it is injected and remains locked even if one tries to detune it. This behavior results from counter-propagating cavity photons that seed the
laser with the proper optical phase. Such a condition is achieved by precise control of the laser-to-FP distance, which typically requires a piezoelectrically actuated steering mirror and simple electronics. A drastic reduction of the laser emission line width occurs, well below the FP mode width, leading to near-perfect mode injections and allowing the laser frequency to be hopped over successive longitudinal modes of the FP. This technique can be applied to virtually any single-frequency semiconductor laser including DFBLs [40], ECDLs [41], QCLs [42] and ICLs [43].

For CEAS, the lowest limit of detection ($1 \times 10^{-14}$ cm$^{-1}$ for 1 s of averaging) was obtained using the NICE-OHMS method [38]. It was calculated from the noise level observed in a 1 MHz-wide saturation-dip structure having a peak absorbance of $4 \times 10^{-9}$ and SNR equal 7700. For a broadband OF-CEAS spectrum spanning 30 GHz, $8 \times 10^{-11}$ cm$^{-1}$ was obtained based on the noise in the spectrum baseline [44].

2.3 Cavity Ring-Down Spectroscopy (CRDS)

In CRDS, the ring-down events [Eq. (3)] are insensitive to laser intensity fluctuation, enabling extremely high SNR spectra [6,11,12] and low detection limits [45] to be attained. However, laser jitter and/or cavity length fluctuation impair precise laser frequency determination and photon coupling into the cavity. The former affects the frequency axis, while the latter limits the data throughput and sets the ultimate reachable sensitivity, governed by photon shot noise. Consequently, the implementation of frequency locking mechanisms is mandatory for the acquisition of high fidelity absorption profiles. The first CRDS effort (with CW probe lasers) towards this goal involved a dual-laser scheme [3]. The length of the CRDS cell was actively locked to a frequency-stabilized reference laser, while a probe laser was brought into resonance, mode by mode, resulting in spectra having a precise optical detuning axis. This technique, called Frequency-Stabilized CRDS (FS-CRDS) was used in many line-shape studies (eg [4,8,12,46]) and had sufficient spectral resolution to reveal MHz-wide saturation dips [46]. The acquisition rate of ring-down events was greatly improved by locking the laser to the cavity with PDH frequency locking schemes [47-50]. This approach was refined [51] using a dual-polarization configuration and EOM-based frequency shifting, leading to robust locking of the probe laser to the ring-down cavity with a 130 Hz relative line width, 5 kHz-level ring-down acquisition rates, minimal dead-time between cavity mode excitations and decay-time measurement precision better than 1 part in $10^4$. Alternatively, a dual-cavity approach was used [5] which transferred the stability of a reference cavity to the ring-down cavity. First, the source laser was locked to individual modes of the reference cavity by optical feedback [39], with capability for mode by mode scanning. This step stabilizes the probe laser frequency and renders its bandwidth narrow by comparison to that of the ring-down cavity mode. Second, continuous optical tuning is realized up to 20 GHz using a single-sideband optical modulator, transforming the stabilized single-frequency light source into an arbitrarily tunable probe laser [52]. Third, the ring-down cavity is locked to the probe laser allowing CRDS spectra to be acquired with fully adjustable resolution and high SNR. This approach has been used for applications to line metrology [5,6,53] and more recently to $^{17}$O isotopic ratio measurements in CO$_2$ [54]. Here, $\Delta^{17}$O = ln($\delta^{17}$O+1) - $\lambda_R$ ln($\delta^{18}$O+1) - $\lambda_R$, where $\delta^{17}$O and $\delta^{18}$O are the usual "$\delta$" values for relative isotopic abundance and $\lambda_R$ is the slope of a reference line $R$, which is used to quantify non-mass-dependent isotopic anomalies from an assumed mass-dependent fractionation law. An unprecedented precision of 10 parts-per-million for $\Delta^{17}$O was demonstrated [54].

The quality of the spectra retrieved by CRDS makes active frequency stabilization techniques perfectly adapted for ultra-precise line-shape recordings of weakly absorbing lines
with SNRs as high as $10^6$ [5,11,12]. In all these studies, the source laser optical frequency was measured against or locked to one tooth of an OFC for an absolute frequency determination as explained in the next section.

2.4 Frequency-comb assisted methods

The highly coherent and broadband nature of OFCs makes these devices appealing as light sources for high resolution spectroscopic experiments that require rapid and wide spectral coverage with a well-defined frequency axis (cf Secs. 2.6 and 2.7). Typically, the OFC repetition rate and carrier-envelope offset frequency are stabilized relative to an absolute frequency standard (eg, Rb or Cs clock), thus providing a comb of known laser frequencies with stabilities at the sub-kHz level. However, unlike the extremely high stability of OFC frequencies, the intensity can vary substantially with time and from tooth-to-tooth, thus driving the limit of detection and often resulting in highly structured spectral baselines that alter the observed line shape. These effects can be reduced (but not completely eliminated) by signal averaging and intensity normalization.

Another important use consists in referencing a probe laser to one tooth of a frequency-stabilized OFC. An early example includes CRDS line-shape measurements of the S(0) and S(1) transitions of deuterium near 3 μm, where a Cs-clock-referenced OFC was used to provide absolute frequencies of the pump and signal beams in a difference-frequency generation probe laser [55]. These experiments yielded line positions and intensities with relative uncertainties of $6 \times 10^{-8}$ and 1 %, respectively. In several other line shape experiments [7,30,53,54,56-59], the OFC was used as an optical frequency reference for a single-frequency probe laser or for measuring the mode spacing of an optical resonator [60]. The OFC-assisted technique yields a much more accurate and precise (< 100 kHz) frequency axis than conventional techniques using a wavelength meter (> 1 MHz precision). Thus, this approach is especially attractive for measurements of absolute line positions and pressure-shifting coefficients with levels of performance that are substantially improved by comparison to those achieved with traditional FTS instruments.

Another possibility consists in locking the probe laser to a tooth of the OFC that is slowly tuned by changing its repetition rate [30,61-63], for instance.

2.5 Cavity mode-width and mode-dispersion spectroscopies

Progress in phase-locking CW lasers to high-finesse cavities has recently enabled the development of cavity-enhanced spectroscopic techniques based on high-precision measurements of the cavity mode widths and positions. As derived above, the exponentially decaying intensity measured in CRDS [Eqs. (3),(4)] is the time-domain equivalent of the cavity-mode width measured under CW excitation in the frequency domain, see Fig. 1. Specifically, the FWHM of a Lorentzian FP mode is given by $(2\pi\tau)^{-1}$. This property is exploited in CMWS [64-66] where the absorption spectrum is retrieved from the widths of the cavity modes measured in transmission. Because the spectral interval probed is so narrow, this measurement is also relatively insensitive to the frequency-dependence of the probe laser intensity. The properties of CMWS make it complementary to CRDS (Sec. 2.3) in terms of achievable accuracies at various levels of intra-cavity absorption. For low absorption, where the ring-down time is long and the modes are narrow, a higher precision is expected with CRDS. For high absorption, the ring-down time is short while the modes are broad and the precision of CMWS tends to be higher. Considered together, the CRDS and CMWS methods provide a wider dynamic range of measurable absorption levels than those associated with either method considered alone. It is important to recall that, in the context of line-shape measurements, short ring-down times associated with strong absorption may lead to systematic errors caused by the finite bandwidth of the detection system. Therefore, CMWS
potentially has a higher dynamic range than CRDS provided that the frequency axis of the cavity-mode spectrum is sufficiently accurate, as indicated in [64] and demonstrated in [67]. Experimental setups for CMWS require ultra-narrow probe laser line widths and sub-kHz resolutions of the frequency tuning to measure the kHz-level mode widths of high-finesse cavities. This can be achieved in a dual-beam configuration, where two orthogonal polarizations of the laser beam are used: the first for phase-locking the laser to the cavity mode and the second for scanning through the neighboring cavity-mode shapes [51,65,66]. This technique also eliminates the influence of the cavity acoustic noise on the mode spectrum.

The measurement of dispersive mode shifts provides another interesting approach for quantitative spectroscopy because frequency is the physical observable that can be measured with the highest precision and lowest uncertainty. Furthermore, the determination of absolute or relative mode frequencies in the One-Dimensional Cavity Mode Dispersion Spectroscopy (1D-CMDS) [13] eliminates potential systematic errors in measured line-shapes caused by nonlinearities of the detection system. Contrary to "usual" spectra, which have absorption and frequency axes, in 1D-CMDS both axes of the dispersion or differential-dispersion spectrum are created from the same measurements of mode-center frequencies. They can thus be directly linked to primary frequency standards, as demonstrated in [67].

Comparisons of spectra obtained with different cavity-enhanced techniques also enable the quantification of potential systematic instrumental errors at the sub-percent level of uncertainty. For example, simultaneous measurements of both absorption and dispersion spectra provide a precise method to check the self-consistency of experimental line shapes. In [68], the accuracy of FS-CRDS (in the limit of strong absorption) was studied by comparison with 1D-CMDS. The line-shape fits revealed sub-percent level inconsistency between absorption and dispersion for high absorption, which could not be detected and were not manifest in the residuals of the individual fits, see Fig. 2. The above-described frequency-based cavity-enhanced techniques are thus particularly useful in applications (eg studies of self-broadened line-shapes over a wide pressure range) that require highly accurate measurements spanning a broad range of absorption. For applications that require extremely high accuracy and SI traceability of measurements (eg Sec. 5.2), the frequency-based 1D-CMDS should be an attractive alternative to traditional absorption techniques. So far both CMWS and 1D-CMDS were used for measurements of the shapes and absolute positions of

Fig. 1: (a) – transmission spectrum of the empty optical cavity (red) and cavity filled with a gas (blue) having an absorption line (green); (b) – principles of absorption spectroscopies in the time (CRDS) and frequency (CMWS) domains, and dispersion spectroscopy (1D-CMDS) in the frequency domain. After [13].
CO lines with SNRs exceeding $10^4$ [67]. CMWS was also applied to low-pressure CO spectra [69] using a NICE-OHMS experimental setup. It was recently demonstrated [70,71] that the CMWS and 1D-CMDS methods also can be combined with optical frequency comb single-tooth resolved spectroscopy [72]. In this case a broadband frequency-based absorption and dispersion spectrum can be measured with a kHz-level resolution (cf Sec. 2.7).

![Complex spectra (absorption from FS-CRDS and differential dispersion from 1D-CMDS) of $^{13}C^{16}O (3\rightarrow0)$ band P3 line measured at two CO pressures $p$. Below residuals from the complex speed-dependent Nelkin-Ghatak profile fits (red) reveal perfect agreement between FS-CRDS and 1D-CMDS at $p = 20$ Torr and considerable disagreement at $p = 60$ Torr. Residuals from the individual absorption or dispersion fits (blue) do not allow detection of this systematic line-shape distortion. After [73].](image)

### 2.6 Direct frequency-comb spectroscopy

For OFCs, the extremely high stability of the frequency axis combined with their broadband spectrum makes them attractive light sources for absorption measurements. A review of various experimental schemes of direct OFC-based spectroscopy can be found in [74]. For line-shape investigations, single-tooth resolved methods, which provide a spectral resolution limited only by the OFC stability, are particularly attractive. Indeed, FTS combined with an OFC source is suitable to line-shape studies since it combines extremely high resolution with a broad spectral coverage. Two approaches to this experimental scheme were developed: dual comb and mechanical FTS comb spectroscopy.

- **Dual Comb with two femto-second lasers**: The idea of Dual Comb Spectroscopy (DCS) [75] is to interfere two OFCs having slightly different repetition rates, see Fig. 3. When both OFCs are combined and transmitted through a gas sample, the down-converted heterodyne beat spectrum of slightly detuned comb teeth provides an intensity absorption spectrum, similar to traditional FTS [76,77]. If only one OFC passes through the sample and the other serves as a local oscillator [78,79], both the absorption (amplitude) and dispersion (phase) spectra of the sample can be measured, analogous to dispersive FTS [80]. Note that for high SNR measurements using DCS, it is crucial to normalize the spectra for frequency- and time-dependent variations in both OFC amplitudes [79,81]. Coherent signal averaging also requires that the relative line width between corresponding teeth of the two combs is not larger than the inverse of the averaging time, which in practice requires phase-locking of both combs to the same optical reference [81]. Several studies of molecular spectra with DCS have demonstrated its potential for line-shape investigations. For instance, absorption and
dispersion spectra of HCN with SNRs up to 4000 were measured [81]. DCS was also used to detect variations in atmospheric CO$_2$, CH$_4$ and H$_2$O [82]. In this case, the high-resolution spectra enabled comparison of the fit results obtained using the VP and SDVP with line-mixing for CO$_2$ lines. Another example is given by [83] in which the positions of CH$_4$ lines in the $\nu_3$ band were accurately determined from absorption and dispersion spectra having SNRs up to 3500 and a spectral point spacing 4 times smaller than the OFC repetition frequency.

**Fig. 3:** Principle of the DCS using multi-heterodyne detection. Interference between two slightly detuned OFCs (having repetition frequencies $f_{\text{rep}}$ and $f_{\text{rep}} + \Delta$) creates a new comb down-converted to RF, with frequencies equal to the differences between the optical comb teeth frequencies ($nf_{\text{rep}}$). This new comb contains information on amplitude and phase change caused by molecular absorption of one OFC. After [77].

- **Dual Comb with mini-combs:** An alternative approach to DCS uses frequency combs generated from a single continuous-wave laser radiation [14] by two electro-optic phase modulators with slightly different modulation frequencies. Such combs have a high relative coherence and enable over 2 hours of real-time signal averaging. The achieved 50 GHz span of the comb spectrum in the near infrared enabled simultaneous measurement of CO$_2$, CO, H$_2$O and HDO lines at atmospheric pressure [84]. When compared to the femto-second OFCs, this system has a low cost and easily adjustable comb spacing but a relatively narrow bandwidth. It can potentially provide higher SNR due to the extremely high coherence of the two combs and high power per tooth. These features make it suitable for accurate line-shape measurements.

- **Comb-based FTS with sub-nominal resolution:** As recently shown [72], Fourier-transform comb spectroscopy based on a single OFC and a Michelson interferometer can deliver the resolution of a comb-tooth, surpassing the natural limits of traditional FTS because of the unique properties of the OFC. When the travel length $\Delta$ of the Michelson interferometer moving mirror equals $c/f_{\text{rep}}$, where $f_{\text{rep}}$ is the repetition frequency of the comb, crosstalk between frequency elements (the comb teeth) after Fourier transformation is completely eliminated (Fig. 4). Any spectral points between the comb teeth can be probed in consecutive scans with different $f_{\text{rep}}$ and $\Delta$. This technique enables the construction of relatively low-cost and compact FT spectrometers with a resolution limited only by the comb line width. Proof-of-principle line-shape measurements were made in the fundamental band of CO and $3\nu_1 + 3\nu_3$ band of CO$_2$ with SNR of several hundred [72]. In the latter case, a high-finesse cavity locked to the comb was used to enhance the path length. This method was used recently to study non-Voigt spectral shapes of CO$_2$ lines [85]. With a SNR of about 250 the effects of the speed dependence of the broadening were clearly observed.
Fig. 4: Principle of the comb-based FT spectroscopy with sub-nominal resolution. When the length of the FT interferogram \( \Delta \) equals \( c/f_{\text{rep}} \) the instrumental sinc function (red curve) of given transformed comb tooth crosses zero at multiples of \( f_{\text{rep}} \) which correspond to consecutive comb teeth (black curve). In this case FT instrumental function does not influence the measured spectrum. When \( \Delta \) differs from \( c/f_{\text{rep}} \), the corresponding sinc function (green dashed curve) has non-zero values at the comb teeth frequencies and influences the spectrum. After [72].

2.7 Cavity-enhanced direct frequency-comb spectroscopy

The use of a high-finesse cavity to improve the sensitivity of DCS is attractive. However, mirror- and gas-induced dispersions in the cavity affect the cavity-mode spacing and preclude the perfect matching with the equally spaced teeth of the OFC over a broad spectral range. Because this frequency mismatch affects the transmission spectrum, it must be properly modeled [86] so that dispersion must be accounted for when tightly locking a high-finesse enhancement cavity to a broadband OFC [87]. The problem may be also solved, at the cost of lower transmitted power and effective enhancement, using a dither locking scheme [15-18] in which the cavity length oscillates around the resonance with the comb and the oscillation amplitude is larger than the dispersive mode shifts.

Direct frequency comb based Fourier-transform spectroscopy methods described in the previous section were also used with enhancement cavities. A Michelson interferometer based FT was used to record CO\(_2\) line shapes with SNRs of several hundred [72] and cavity-enhanced DCS for high-resolution spectroscopy was demonstrated in [14].

In comb-based Vernier spectroscopy [20,88] the cavity is used to filter the comb modes by setting the cavity FSR to a value slightly different than the comb-teeth spacing \( f_{\text{rep}} \). Such a filtered comb contains a reduced number of teeth with increased distance between them. Every \( n \)th tooth is transmitted through the cavity while all others are reflected. Here \( n \) must be large enough to enable single-tooth resolution by a dispersive grating or VIPA etalon. Their transmission may be measured simultaneously by a detector array, eg CCD. By precisely tuning the cavity length, an arbitrary set of filtered comb teeth can be selected in consecutive measurements. This method is competitive with the previously described direct FT-comb spectroscopies. This approach provides equally high resolution and a higher power-per-spectral element, but lower spectral coverage of the parallel measurement. For quantitative absorption measurements, one must account for the mismatch between the cavity modes and the comb teeth caused by broadband and resonant dispersion in the cavity [86]. Examples of spectra with individual line shapes having SNR over 100 were presented for CO [86] and HCN [89]. In the latter case, both absorption and dispersion spectra were recorded.

Broadband CMWS and 1D-CMDS measurements (Sec. 2.5) with an OFC as a light source were recently demonstrated. This experimental scheme significantly increases the
acquisition rate of broadband spectra (by comparison to CW-laser setups) by the parallel measurement of hundreds of the cavity mode widths and shifts. In these methods of absorption and dispersion spectroscopy achieving single comb tooth resolution is critical. Both subnominal-resolution FT [71] and optical Vernier with a VIPA etalon [90] schemes yielded sub-kHz precision of the cavity mode and position measurements. The two approaches are based solely on frequency measurements and the recorded spectra therefore are insensitive to OFC power variations. Note that these methods have uncertainties that are unaffected by dispersion in the enhancement cavity [86]. They are thus promising for high-precision spectral line-shape measurements covering entire molecular bands.

**2.8 Dual-laser absorption spectroscopy**

Recording a line with high precision necessitates a stable and narrow optical frequency reference to which the probe laser can be referenced. Rather than using the tooth of an expensive self-referenced frequency comb (Sec. 2.4), an alternative solution was proposed [91] in which a kHz-linewidth-master laser (ML) is locked to a saturated absorption feature [33,92]. The probe laser is then forced to maintain a precise frequency-offset, provided by a radiofrequency (RF) synthesizer which is phase locked to an ultra stable Rb oscillator, from the ML. By tuning the RF frequency, it is possible to perform continuous, highly linear and accurate frequency scans of the probe laser around a given center frequency [91]. This feature, in conjunction with the extremely high linearity of the detection electronics, makes it possible to avoid any instrumental distortion in measured absorption line shapes, reaching an experimental accuracy limited only by the shot noise.

This dual-laser method has been used to investigate the shape of H$_2^{18}$O lines in the Doppler regime [93], evidencing the influence of speed-dependences of the pressure-broadening and shifting coefficients. Subsequently, the quality of the quadratic and hypergeometric models for these speed dependences was tested [94] (cf Sec. 3.2.4c). A recent improvement of the dual-laser technique involves a reference laser and the NICE-OHMS approach, making it possible to reduce the uncertainty associated with the frequency scale and allowing locking on weaker reference lines [95]. This technique was applied to measurements of spectroscopic parameters of C$_2$H$_2$ leading, in particular, to a determination of the $2v_3+v_5$ band $P_7(14)$ line strength with a combined uncertainty of 0.22 % [96]. Apart from molecular spectroscopy, the dual-laser technique has been successfully applied to the fields of Doppler thermometry and isotope research, as described in Secs. 5.2.1 and 5.2.2.

Finally note that the technique of offset-frequency locking of a pair of diode lasers is extensively used in atomic physics experiments, while it has been almost ignored in the field of molecular spectroscopy, until the work described in [97], in which the authors propose a dual laser method for water-vapor differential absorption sensing (cf also [98]).

**2.9 Fourier-transform spectroscopy (FTS) methods**

With the exception of direct frequency-comb-based methods (cf Sec. 2.6), the spectral resolution of most FT spectrometers is generally lower than that of laser-based systems. Nevertheless, these instruments typically provide more global spectral-shape information than can be obtained using relatively narrowband laser methods. Key attributes of FTS include the applicability to optically thick samples and the realization of accurate frequency axes with spectral coverage that is sufficient to investigate entire absorption bands. These attributes of FTS are most effectively exploited by carrying out physically constrained, multispectrum analyses [99] of several measured spectra that are acquired at known values of sample composition, pressure and temperature. In the last decade and before, such methods have provided a wealth of measured spectra for the test of theories and models, as well as for the determination of absorption-shape parameters from their fits. Given their broad spectral
coverage and high data throughput, they have been, and remain, the workhorse for populating line-by-line spectroscopic databases. Numerous references cited in Secs. 3 and 4 demonstrate the interest of FTS and, in many cases, its advantages. An example can be found in [100] where information on individual line shapes, on line mixing and on collision-induced absorption in the O₂ A band has been simultaneously retrieved from FTS and CRDS spectra. This study shows the complementarity of these two experimental methods and the interest of investigating an extended spectral range that is analyzed through the simultaneous fit of spectra recorded at various pressures. The interest of such a method when the FTS is coupled to coolable cells (eg [101]) is further illustrated by [102], where multispectrum fits of broadband CH₄ spectra recorded for various pressures and temperatures enabled the retrieval of information on line-broadening, -shifting and -mixing coefficients together, for some lines, with the speed dependence. In addition, FTS has brought a lot of experimental information on the broadband water vapor continuum and on collision-induced absorption spectra, as shown by many references cited in Secs. 4.3.1 and 4.4. Let us finally mention a study [103], which is to our knowledge the first in which FT spectra have enabled the investigation of the effects of temperature on the parameters of a very refined individual line-shape model. Indeed, the T dependences of not only the line-broadening and -mixing coefficients but also those of the speed dependence of the width and of the Dicke narrowing parameter have been determined from fits of measured spectra.

### 2.10 Advances in coherent terahertz spectroscopy

The measurement of light-matter interaction in the terahertz spectral region (roughly 0.1-10 THz) is a fertile research area with numerous applications in spectroscopy. Although many materials that are opaque or absorb at infrared and visible wavelengths are transparent for THz (also known as mm-wave), there are species, such as water vapor, which have strong rotational absorption fingerprints there. Given the relatively small Doppler widths of transitions in this region, the line shapes are dominated by collisional effects at relatively low pressure.

Coherent sources required for THz spectrometers can be produced by photomixing of infrared lasers, backward wave oscillators or by frequency multiplication of radiofrequency (RF) sources [104]. These types of sources typically provide output powers no greater than a few microwatts, which has hindered more widespread implementation of high-resolution spectroscopy in the THz region. Recently, compact quantum-cascade lasers (QCLs) are emerging as attractive sources with emission frequency down to 5 THz, output powers as high as 10 mW and line widths from 100 Hz to 500 kHz [105-108]. The first high-resolution absorption spectroscopic measurement with a THz QCL was in 2006 and involved measurement of CH₃OH [105]. More recently, a frequency-comb-assisted THz QCL spectrometer resulted in an SNR of approximately 3000 and line centers measured with an uncertainty of 10 kHz [108]. These experiments clearly demonstrate the potential of QCL technology for realizing new high-precision line-shape studies in the THz region, although the stability of cryogenic detection schemes often remains a limiting factor in measurement precision.

Numerous THz line-shape studies were carried out prior to the development of THz-QCL sources. A spectrometer employing a custom-built coherent radiation source (based on photo mixing of two near-infrared lasers) provided temperature-dependent collisional width and shift coefficients of water vapor [109]. These measurements were made over the temperature range 263-340 K, yielding a spectral resolution of 15 MHz and relative uncertainty in the broadening coefficient from 1 to 3 %. In [110-112], a coherent source comprising a phase-locked, frequency-multiplied RF diode was developed to measure self-, nitrogen- and oxygen-broadened pure rotational lines of HNO₃ and H₂O. Absorption spectra
were acquired using intensity- and frequency-modulation methods with phase-sensitive detection, and various line shapes were fit to the data to yield pressure-broadening and -shifting coefficients as well as speed-dependent broadening and collisional narrowing parameters. Recently, a coherent THz source based on frequency-multiplied RF synthesizer signals with a resolution of 5-10 MHz was used to measure absorption by water vapor within a multipass cell [113]. A global, multispectrum fit of 145 spectra yielded line positions, shift and broadening parameters as well as continuum coefficients for several line profiles.

An experiment using a phase-locked Gunn diode source [114] demonstrated the feasibility of CRDS measurements in the 75-100 GHz region. Subsequently, high-resolution determinations of N$_2$ and O$_2$ continua and H$_2$O rotational lines in the THz region were made using a fast-scanning (30 GHz/s) BWO source with a tuning range of 170-260 GHz [115]. This experiment employed a 10-m-long cavity, with finesse of 1000, line width of 13 kHz and resulted in a spectrum baseline noise of $2 \times 10^{-7}$ cm$^{-1}$. Also using a FP resonator, cavity line width measurements straddling the microwave and THz regions were used to measure O$_2$ and H$_2$O absorption line shapes, with baseline noise levels of $4 \times 10^{-9}$ cm$^{-1}$ and spectrum SNRs approaching 1000. Recently, cavity-enhanced measurements of N$_2$O near 0.1 THz were realized with a low-mass, CMOS-based instrument having a 3-cm-long resonator, finesse of 200 and mode width of 20 MHz [116]. Fourier transforming the echo induced by the pulsed source yielded pressure-broadened N$_2$O line shapes nominally 1 MHz wide and a detection limit of $5 \times 10^{11}$ molec. cm$^{-3}$. It is worth noting that although cavity enhancement in these long wavelength regions increases measurement sensitivity compared to direct absorption methods, the maximum finesse of metallic-reflector-based resonators is typically diffraction limited and nominally two orders of magnitude lower than that achieved with the super-polished dielectric mirrors available for visible and near-infrared systems.

3. Theories, models, results

3.1 Introduction and selection criteria

This section is devoted to theories, models and results concerning pressure effects on absorption spectra, which are to be understood as follows: "Theories" means theoretical approaches that enable direct predictions of some measured quantities (spectra, line widths, etc). Within this topic we limit ourselves to those proposed since [1], ie 2007. "Models" refers to those assumptions and resulting equations that enable the description of experimental results based on parameters that are fitted to measured data. Here again, we focus on those proposed in the last decade. "Results" must be understood in the sense of comparisons between the predictions of "theories" and experiments, or tests of the ability of "models" to represent measurements. We consider those results obtained since 2007, regardless of when the theory or model used was published.

The remainder of Sec. 3 is divided into five parts in which we try to update the information given in chapters III-VI of [1]. Section 3.2 focuses on "isolated lines" that are not affected by neighboring transitions but are influenced by various effects leading to non-Voigt profiles. The calculations of "pressure-broadening and -shifting coefficients", primary ingredients of their shapes, are discussed in Sec. 3.3. "Line-mixing", through which the transfer of population between rotational levels has spectral consequences not too far from line centers, is the subject of Sec. 3.4. Section 3.5 then focuses on the spectral regions of the "far wings and associated continua" to which many processes, including the finite duration of collisions, contribute in a complex manner. Finally, "collision-induced absorption", when the interaction of molecules with light results from the dipole that only exists during intermolecular collisions, is considered in Sec. 3.6.

Note that most of the studies discussed in this section have been made at or near room temperature. In the following, we will thus generally give information on the temperature-
range investigated only when the latter is broad enough to enable a significant test of the ability of a theory or model to describe the $T$ dependence.

### 3.2 Isolated line shapes

As in Chapt. III of [1], we consider here "isolated transitions", ie those sufficiently distant from others for their core region not to be influenced by their neighbors under the considered gas conditions. Describing their shapes requires simultaneously accounting for the Doppler effect, the collision-induced velocity changes of the radiating molecule, and the pressure-induced speed-dependent line broadening and spectral shifting. With regard to this topic, the last decade has witnessed several advances, largely based on the high quality of spectra recorded with laser techniques (Sec. 2). Various phenomenological line-shape models have been proposed and/or tested, while theories for predictions of the line shape were developed. In the first part of this section, we present a new approach for the direct calculation of isolated line profiles (Sec. 3.2.1). Other approaches evaluating the spectral shapes by using a kinetic equation describing the time evolution of the dipole auto-correlation function (ACF) are presented in Sec. 3.2.2. Models and methods developed or used to compute the velocity collision kernels involved in this equation are also reviewed in Sec. 3.2.2. Approaches proposed that account for relativistic and dispersion effects on the line shape are the subjects of Sec. 3.2.3. Finally, recent advances concerning phenomenological line-profile models are reviewed in Sec 3.2.4.

#### 3.2.1 Direct and empirically corrected predictions from Molecular Dynamics Simulations

A new theory for the direct prediction of isolated line shapes of linear molecules was proposed in [117]. It uses classical dynamics and an assumed intermolecular potential to compute the translational and rotational evolutions of a large number of molecules. These Classical Molecular Dynamics Simulations (CMDS) provide the center-of-mass position $\mathbf{q}_m(t)$ and velocity, as well as the axis orientation $\mathbf{u}_m(t)$ and rotational angular momentum, of each molecule $m$ at all times $t$. For the linear species considered, the dipole moment lies along the molecular axis and its ACF is proportional to the average $(\mathbf{u}(0) \cdot \mathbf{u}(t))$. The Doppler effect is introduced through the relative displacement $[\mathbf{q}_m(t) - \mathbf{q}_m(0)] \cdot \mathbf{z}$ along the radiation-propagation direction $\mathbf{z}$. The Laplace-Fourier transform of this ACF (ie multiplying the ACF by $\exp(-i\omega t)$ and integrating from $t=0$ to $+\infty$) then yields the absorption spectrum. However, because CMDS lead to a continuous distribution of rotational speeds, this spectrum shows no line structure. In order to solve this problem, a requantization procedure was proposed [117]. As first demonstrated for pure CO$_2$ [117,118] and confirmed for other systems [119,120], these requantized CMDS (rCMDS) closely predict the observed relative deviations of line shapes from the VP without adjusting parameters. Note that an alternative requantization was proposed in [121], which is more suitable for light rotors and was successfully applied to HCl [121] and CH$_4$ [122] lines. It also enables one to constrain the positions and intensities of the lines in the calculated spectrum to literature values (taken from a database, for instance), a possibility that was used in [123,124].

While rCMDS accurately predict the relative deviations of line shapes from the best VP fits, the line shapes themselves are not as well described because the line widths in rCMDS-calculated spectra may deviate from measured values by several percent (eg [117,120,121]). An approach to empirically correct for these discrepancies was proposed in [125] and successfully tested for some CO lines. The idea is to multiply the rCMDS-calculated dipole ACF for line $\ell$ at pressure $P$ by the correction factor $\exp(-2\pi c \Delta \gamma_{\ell} P t)$. Here, $\Delta \gamma_{\ell}$ is the
difference between the pressure-broadening coefficients obtained from fits, with the same line shape, of a measured spectrum of line $\ell$ at a single pressure $P_0$ and of that obtained from uncorrected rCMDS for the exact same conditions. With this simple correction, differences with experiments may become as small as a few times 0.1% of the peak absorption over a broad range of $P$. This is illustrated by Fig. 5 which also shows the large errors obtained when the VP is used. Note that the results in this figure are for room temperature and that the ability of the proposed approach to accurately represent spectra at various temperatures remains to be proven. However, since the model offers the possibility to introduce an ad hoc temperature-dependent correction $\Delta \gamma_i(T)$ we expect it to lead to results of similar quality below and above room temperature.

![Fig. 5: Peak-to-peak amplitudes (relative to the absorption peak values) of the residuals of multispectrum Voigt-fits of measured spectra of the P(17) line of the 3-0 band of CO at room temperature (full symbols) and relative deviations between measured and corrected-rCMDS spectra (open symbols) for CO diluted in He (squares), Ar (triangles) and Kr (circles). After [125].]

3.2.2 Using a kinetic equation

An alternative approach to direct rCMDS is to use a set of (vectorial) kinetic equations that drive the time evolution of the dipole ACF ([126-129] and Sec. II.5 of [1]). A general review on this topic can be found in [130]. In a purely theoretical study, using the $1/r^n$ potential form, [131] solved these kinetic equations and showed the influence of the interaction potential (ie of $n$) on the calculated spectral shape. Within the "isolated-line approximation" (no transfer of intensity between the various transitions) this set of kinetic equations becomes diagonal in the line space with one independent differential equation for each transition. The latter involves, besides the Doppler contribution, a collision kernel for the changes of the radiator velocity together with a collisional width (and shift) that depends on the radiator speed. It is also possible to introduce [126] a parameter describing the correlation between the collision-induced changes of the molecular translational and rotational motions. While the speed-dependent pressure-broadening and -shifting coefficients can be obtained from calculations (Sec. 3.3), several approaches have been proposed for the velocity collision kernels. The latter have been modeled in recent studies by using the Keilson-Storer (Sec. 3.2.2a) and the billiard-ball (Sec. 3.2.2b) models, as well as directly calculated using CMDS (Sec. 3.2.2c). Note that, with the exception of the billiard-ball model which was tested (for H₂) in a wide temperature range, all other recent results discussed in this section are limited to room temperature. This stresses the need for further tests of the models described below over extended temperature conditions.

3.2.2a The Keilson-Storer model for the velocity collision kernel

The Keilson-Storer (KS) model [132] was used for the first time in [133] to describe the effects of collision-induced velocity changes on line shapes (of H₂ in Ar). The KS kernels are based on two parameters [132,133]: The velocity-changing collision frequency $\nu_{vc}$, and
\( \alpha \) which parameterizes the efficiency with which collisions change the velocity. The latter quantity takes on values between 0 and 1, which correspond to two physical limits. For \( \alpha = 0 \), there is no correlation between the velocities before and after collision. This is the hard collision model \([126, 134]\) for which the molecular velocity is completely thermalized after each collision. For \( \alpha = 1 \), the velocities before and after a collision are completely correlated and this is equivalent to the soft collision model \([135]\). The KS kernel is thus more general than these two extreme cases. Because collisions may change the velocity modulus and orientation with different efficiencies, a more general version was proposed \([136]\) based on two distinct \( \alpha_m \) and \( \alpha_o \) parameters. In \([137]\), it was shown that the three parameters of this extended KS approach can be determined by using CMDS. The resulting line-shape model, built from the corresponding collision kernels and completed by speed-dependent widths and shifts deduced from experiments, was successfully compared to measured Raman lines of \( \text{H}_2 \) in \( \text{N}_2 \) and \( \text{Ar} \) \([136, 138, 139]\). The same approach was then applied to pure \( \text{H}_2 \text{O} \) and \( \text{H}_2 \text{O} \) in \( \text{N}_2 \) \([140-142]\). For these systems, where the decay times of the auto-correlation functions of the velocity modulus and orientation are close to each other \([140, 141]\), a single \( \alpha \) parameter was used. Its value and that of \( \nu_{\text{VC}} \) were deduced from CMDS. These calculations also enabled \([140, 141]\), for the first time, quantification of a parameter that describes the correlation between collision-induced changes of the translational and rotational motions. The speed-dependent widths and shifts, other components of the kinetic equation, were calculated \([140, 141]\) using the RB formalism (Sec. 3.3.4). The resulting line shapes are in excellent agreement with those measured for many transitions of pure \( \text{H}_2 \text{O} \) and \( \text{H}_2 \text{O} \) in \( \text{N}_2 \), under various pressure conditions \([140-143]\). It was in particular shown, using an empirical correction procedure similar to that applied to the CMDS predictions of CO line-shapes (cf \([125]\) and Sec. 3.2.1), that this approach leads to absolute predictions of the profiles of \( \text{H}_2 \text{O} \) lines broadened by \( \text{N}_2 \) \([143]\) within better than 0.5%. For completeness, recall that the (mono-parametric) KS model was used to describe the collision kernel of pure \( \text{H}_2 \) in \([144]\). In this study, a purely numerical solution \([145]\) of the kinetic equation was implemented for the first time and satisfactory agreement with measured spectra was obtained over a broad pressure range.

### 3.2.2b The billiard-ball (BB) approximation for the velocity collision kernel

The billiard-ball (BB) model was derived assuming a hard-sphere interaction potential \([146, 147]\) and the associated velocity collision kernels are given in analytical form \([148]\). In an analysis of \( \text{O}_2 \) spectra measured via FS-CRDS \([149]\), it was shown that the use of the BB model for the description of velocity changes yielded the highest quality-of-fit (as defined in Ref. \([11]\)) ever reached for a molecular line. The speed-dependent billiard-ball (SDBB, \([150]\)) profile was used to quantify the ability of various line-shape models to reproduce a benchmark theoretical profile \([151]\). It also enabled to estimate possible systematic errors on Doppler width measurements \([149]\) for the spectroscopic determination of the Boltzmann constant (cf also Sec. 5.2.1) and to determine the frequencies of unperturbed rovibrational transitions \([152]\). This profile was also used \([153]\) to rescale the narrowing parameter of the HC model and improve the treatment of velocity-changing collisions in the Hartmann-Tran profile (Sec. 3.2.4a). Note that the large discrepancy between quantum computations of the line widths and those measured for \( \text{H}_2 \) perturbed by \( \text{Ar} \) obtained in \([154]\) was solved \([155]\) by using the SDBB profile which properly handled velocity- and speed-changing collisions (cf Fig. 6). Using the SDBB model for lines of \( \text{H}_2 \) perturbed by \( \text{He} \), it was shown \([156]\) that comparisons of measured and calculated full line shapes enable to discriminate various PESs while considering only pressure-broadening and -shifting coefficients is not sufficient.
3.2.2c Velocity collision kernel calculated from CMDS

CMDS were used to obtain the velocity collision kernel for pure H\textsubscript{2} in [144]. As mentioned in Sec. 3.2.1, these calculations provide the time evolution of the center-of-mass velocity of each molecule. It is thus possible to follow the number of molecules, among those having a given velocity at time \( t \), which have changed to another velocity at time \( t' \). This gives detailed information on the velocity changes from which the associated kernels can be deduced [144]. The latter were compared with those calculated using the KS model (Sec. 3.3.2a) showing that this last approach does not well describe velocity-to-velocity changes (Fig. 7) although it leads to (practically) the same averaged correlation function of the molecular velocity [144]. Comparisons between measured line shapes of Raman and quadrupole lines of pure H\textsubscript{2} and those calculated using the KS and CMDS collision kernels showed that the latter lead to better and very satisfactory agreement with measurements [144].

Figure 7 shows a comparison between velocity collision kernels computed for H\textsubscript{2}-H\textsubscript{2} interactions using CMDS, the BB and KS models. As demonstrated in [159] and shown by this plot, for H\textsubscript{2}-H\textsubscript{2} (and also H\textsubscript{2}-Ar), the kernels calculated with the BB model are in excellent agreement with those predicted by CMDS, while the KS function leads to values which are independent of the relative orientation change between the velocities before and after the collision.
3.2.3 Relativistic and dispersion correction to line-shape models

Models have been proposed recently to account for some refined effects that affect the line shapes. The proposed corrections, discussed below, will likely be crucial for ultra-precise Doppler thermometry (cf Sec. 5.2.1) and molecular spectroscopy for fundamental studies. Although these effects have not yet been experimentally verified, it may become possible in the future to observe them through measurements capable of detecting relative changes of the line shape at the typical $10^{-6}$ level (see below).

The relativistic formula for the Gaussian profile was given in [160] and an extension to the VP was derived in [161]. It was demonstrated that relativistic effects lead to a line asymmetry and can modify the profile at the $10^{-6}$ level [161] at room temperature (with modifications that increase with temperature). Equivalent formulas for more advanced (non-Voigt) relativistic profiles have not been proposed so far.

The dependence of the Doppler shift on frequency, caused by dispersion [162,163] and by light frequency variation over the spectral line shape, is another refined effect that needs experimental demonstration. A model taking this into account was derived for a Gaussian line shape [163], showing that it leads to a line asymmetry, affects the line shape at the level of $10^{-5}$ and may influence line-position measurements at the kHz level. Again, for future applications, dispersion corrections are needed for profiles also influenced by collisional effects.

3.2.4 Phenomenological line-shape models

Models that explicitly express the line shape analytically as a parameterized function with a few (adjustable) parameters are very useful. They can be fitted to measured spectra (Sec. 4.1), providing parameters which can be archived in databases (Sec. 4.5), opening the route for use in practical applications (Sec. 5). In this section, we review some recent advances and results obtained with various phenomenological profiles used to represent the shape of isolated lines.

The simplest line shapes are the Doppler and Lorentz profiles. They depend on the Doppler width and on the “usual” pressure-broadening and -shifting coefficients, respectively. The convolution of these two profiles results in the Voigt (V) profile, which captures the inhomogeneous collision-induced line broadening that encompasses all velocity classes. It is then possible to account for the collision-induced changes of the radiating-molecule velocity by assuming Soft (SC) or Hard (HC) Collisions. These assumptions lead to the Galatry [135] and Rautian [126,134] line-shapes, respectively. Concerning the Speed Dependences (SD) of
the collisional width and shift, they are usually modeled using a quadratic (q) [164,165] or a hypergeometric (h) [166,167] law. Then, models for velocity-changes and speed-dependences can be combined, leading to a large variety of models such as (using the acronyms introduced above) the qSDVP, the qSDHC and the hSDSC profiles, for instance. Note that it is also possible to introduce a partial Correlation (pC) [126] between the collision-induced changes of the radiator velocity and those of its rotational (speed and phase) state. Figure 8 (see also that in Sec. 5.2.2) shows examples of fits of measured spectra with a variety of phenomenological lineshape models (in which LM has been included). As can be seen, the VP leads to large, but not atypical, residuals. Furthermore, Fig. 8 shows that not only the speed-dependence but also the velocity changes and the correlation must be taken into account in order to obtain the best fit of the high quality observed line-profiles.

Many models can be found in Table III.6 and Sec. III.3 of [1] and in Table 1 of [169] with detailed descriptions in the references therein. All of these approaches have existed for awhile, but the most sophisticated ones were seldom used until recently only because they involve numerous parameters. Indeed, since measurements carry noise, the solutions to make the retrieval of all the model parameters as unambiguous as possible are [169]: to use spectra of the best quality achievable, to record them over a pressure range as broad as possible (ideally from the practically purely Doppler to the almost purely collisional behavior of the line shape), and to treat them using a multispectrum fitting procedure [99,170].

3.2.4a The Hartmann-Tran profile

Starting from the partially-correlated speed-dependent hard-collision model [171], Hartmann, Tran and co-workers combined it [169] with quadratic speed dependences [164,165] for the line width and shift. The resulting pCqSDHC profile accounts for the Doppler effect, the influence of velocity changes caused by collisions, the speed dependences of the line width and shift and the correlation between velocity- and internal-state changes. Using \textit{ab initio} calculated line shapes of various molecular systems as references, [169] showed that the pCqSDHC can reproduce most of them over a wide pressure range with a precision better than \( \approx 0.1 \) %. Furthermore, [169] demonstrated that this line profile can be written as a combination of complex error functions for which many computer-efficient routines are available (\textit{eg} [172-177]). Therefore, the pCqSDHCP can be easily and quickly computed [178], contrary to most of the other sophisticated line shapes, which enables the use
of this profile for computationally intensive calculations required for radiative transfer and remote sensing applications. In addition, by setting some parameters to zero, the pCqSDHC profile reduces to several simpler line shapes [169], including the widely used qSDVP and the HC model. Because of its numerous useful attributes, the pCqSDHC profile was recommended by an IUPAC task group as the reference line shape to be used in high-resolution spectroscopy [179]. Now known as the "Hartmann-Tran" profile (HTP), it is increasingly used (Sec. 4.1) and the HITRAN database now enables the storage of its parameters (Sec. 4.5.1).

3.2.4b Temperature dependence of the line-shape parameters

Relatively little has been done on the temperature dependences of the line-shape parameters other than the usual broadening and shifting coefficients associated with the VP (as confirmed by the table in Sec. 4.1).

Concerning the speed-dependence, a relation between the temperature dependence of the collisional broadening and that of the parameter describing its quadratic speed dependence was given in [180]. It was obtained assuming that the dependence on the relative speed of the collisional broadening is also quadratic. In this particular case, it was shown [181] that the ratio of the broadening speed-dependence parameter to the pressure-broadening coefficient should be independent of \( T \). This result was experimentally confirmed to within a few percent for variable-temperature measurements of CO\(_2\) line shapes in the 1.6 \( \mu \)m region [181]. However, some other experimental studies [103,182-184] have shown that the temperature dependences of the line broadening and of its quadratic speed-dependent component are significantly different. For the Dicke-narrowing parameter (generally denoted by \( \nu_{VC} \)), a power law for its temperature dependence was used in a few studies (eg [103,182,185,186]) that have investigated this issue. The corresponding experimental results show that the temperature dependence exponent of \( \nu_{VC} \) can be significantly different from that of the line broadening (eg 1.2 versus 0.75 on average in [103]). Finally, to the best of our knowledge, there is no experimental or theoretical result available for the temperature dependences of the speed dependence of the pressure shift and of the correlation parameter.

This sub-section shows that the influence of temperature on the collisional parameters of refined isolated line profiles (beyond the VP) remains poorly known. New (very careful) experimental investigations are needed to clarify this important issue to which the theoretical approach of Secs. 3.2.1, 3.2.2 and 3.3 may also bring interesting information.

3.2.4c Quadratic versus hypergeometric speed dependences

The quadratic speed-dependence (qSD) [164,165] is different from the hypergeometric (hSD) model [166,167]. The latter is more physically based since it results from an assumption directly concerning the intermolecular potential. Using high quality spectra of O\(_2\) lines at low pressure, it was shown [187] that the pChSDHC model leads to slightly better fits of the observed line-shapes than the HTP (ie pCqSDHCP). Similarly, in situations involving large speed-dependence effects, such as a high rotational quantum number line and/or a light active molecule interacting with a heavy perturber, the hypergeometric model also better reproduces the measured spectra than does the quadratic model [188]. A detailed comparison between the pChSDHC and the pChSDHC profiles was also made in [189] using high quality spectra of H\(_2\)O lines in the Dicke-narrowed regime. The same fit qualities were obtained with the two models. For the retrieved parameters, while the integrated absorbances and speed-averaged pressure-broadening and -shifting coefficients are very consistent, the other parameters are quite different [189]. With respect to the hypergeometric model, the line narrowing due to the speed dependence is underestimated by the quadratic approximation whereas the velocity-changing frequency is overestimated [189]. In other measurements of self-broadened H\(_2\)O lines, it was shown that HC profiles with the quadratic and
hypergeometric speed dependences gave nearly identical results, reproducing the spectra with residuals at the 0.01% level [8].

3.2.4d Kochanov's approach

In [190] and references therein, a new line-profile model was proposed. It is based on quantum mechanical collision-integral kernels calculated for an intermolecular interaction potential proportional to $1/r^2$, with $r$ the intermolecular distance (thus much simpler that those that can be implemented in the codes, such as MOLSCAT [191], discussed in Sec. 3.3.1). Specifically, the collisional kernels were modeled and then fitted to the quantum-mechanical calculated kernels. This model accounts for the Dicke narrowing, the effects of small- and large-angle scattering collisions [192], and the speed dependences of the collisional relaxation rates. The resulting profile involves a plethora of parameters likely to be fitted to experiments but, to the best of our knowledge, its ability to accurately describe measurements has not been proven so far.

3.3 Pressure-broadening and -shifting coefficients

The pressure-broadening ($\gamma$) and -shifting ($\delta$) coefficients are the first quantities to be known for calculations of spectra when the Doppler effect is not dominant. Thus, for decades, efforts have been made to determine these parameters and subsequently populate databases. Until relatively recently, the VP was mostly used and knowledge of the values $<\gamma>$ and $<\delta>$ averaged over the velocity distribution was sufficient. With the increase of precision requirements and the now well-recognized fact that speed-dependence effects are important, these two parameters have become insufficient to capture the pressure dependence of line shapes. One then needs to know the dependences of $\gamma$ and $\delta$ on the absorbing-molecule speed, which are ingredients of a variety of refined line-shape models (Sec. 3.2 above and III.4 of [1]). We focus here on their calculation for which we review recent theories and results, while available experimental determinations are presented in Sec. 4.1.

When an intermolecular potential is available, many formalisms exist for calculations of $\gamma(v_r)$ and $\delta(v_r)$, where $v_r$ denotes the relative speed. They are adapted to systems of various complexity, in terms of the symmetry of the molecules, of the number and nature of the significantly populated levels and of the parameterization of the intermolecular potential. For instance, while fully quantum computations are tractable for He-broadened rotational lines of CO at 10 K, they cannot be made for transitions of high overtones of pure H$_2$O at 2000 K, a case that can be treated with (much simpler and approximate) semi-classical models. The resulting dependences on the absorbing-molecule speed are then obtained by averaging $\gamma(v_r)$ and $\delta(v_r)$ over the perturber velocity [167]. Until recently, limitations in computing power have restricted the use of fully quantum approaches to very simple collisional pairs, a constraint progressively relaxed as shown in the next section. For more complex systems, progress has been made thanks to improvements of the RB theory brought by the inclusion of line-coupling, as discussed in Sec. 3.3.2. At the same time, Gordon's fully classical method was resurrected by S. Ivanov and enabled calculations of pressure-broadening coefficients for linear molecules (Sec. 3.3.3). Finally, for (very complex) molecular pairs for which other methods are inapplicable or too costly, the “usual” RB approach remains useful as shown in Sec. 3.3.4. Note that, while the refined RB approach has been tested only at room temperature, it is not the case of the other theories discussed below. For instance, the broadening of C$_2$H$_2$ and N$_2$ lines by H$_2$ was studied from 77 K to 2000 K [193,194] while broadening of pure N$_2$ and of CO$_2$ in Ar was investigated [195,196] in the 77-2400 K and 77-765 K ranges, respectively. In these references, quantum, fully classical and the usual RB semi-classical approaches were used for comparisons with measured values. Agreement within experimental uncertainties was obtained in most cases except with the RB formalism. However, if some
intermolecular-potential parameters are tuned, the latter provides a satisfactory description of the temperature dependence. This may explain why this computationally cheap method remains so popular from a pragmatic point of view (cf Sec. 3.3.4).

3.3.1 Quantal approaches

The approaches, such as the close-coupling (CC) method, in which all degrees of freedom (translation, rotation, etc) are treated quantum mechanically provide the most reliable predictions of $\gamma(v_f)$ and $\delta(v_f)$ if an accurate intermolecular potential is used. A description of the CC method and of various decoupling approximations, such as the coupled states (CS), the decoupled $l$-dominant and the effective potential methods, as well as the infinite-order sudden (IOS) approximation, can be found in [197] and Sec. IV.3.5 of [1]. Several computer codes have been developed (eg MOLSCAT and PMP MOLSCAT [191], MOLCOL [198], HIBRIDON [199]) to calculate the matrix elements of scattering operators at various levels of accuracy. MOLSCAT and its parallelized version PMP MOLSCAT treat collisions between closed-shell species ranging from rigid diatom-atom to rigid diatom-asymmetric top. HIBRIDON and MOLCOL solve the close-coupled equations for both closed- and open-shell systems. From the scattering-matrix elements provided by such codes, built-in functions or post-processor programs generate relative kinetic-energy-dependent pressure-broadening and -shifting generalized cross sections for the considered type of spectroscopy. They can then be transformed [167] into values that depend on the speed of the radiating molecule. In addition, the averaged broadening and shifting coefficients at various temperatures can be obtained assuming a Maxwell-Boltzmann distribution.

Because of its computational cost, the CC formalism was mainly applied to simple systems [diatom-atom or (light) diatom-(light) diatom] while more approximate methods, like the CS or IOS, were used for more complicated cases (symmetric top-atom or asymmetric top-atom). The increase in computer speed, the use of clusters, of parallelization, of job arrays, etc, in conjunction with the availability of more accurate full-dimensional potential-energy surfaces (PES) now permit more rigorous treatments of all kinds of systems. For instance, these advanced computational capabilities have enabled, for H$_2$-He, consideration of the effects of the centrifugal distortion of the PES or of rovibrational potential coupling terms [156,200]. PESs for the active molecule in the ground state or in an excited electronic state also have enabled calculations of pressure-broadening and -shifting coefficients for rotational, rovibrational and rovibronic lines [201,202]. Furthermore, CC predictions for asymmetric-top molecules in a bath of diatomics are nowadays feasible. Good examples are calculations for H$_2$CO and H$_2$O in H$_2$ [203-206], systems that were never investigated at this level of accuracy before. Let us mention in particular the CC pressure-broadening and -shifting (which are more difficult to converge) coefficients of pure rotational lines of H$_2$O in H$_2$ calculated over a wide temperature range [204]. The next challenge would be to repeat such calculations for rovibrational lines while taking the centrifugal distortion of the potential into account. Finally note a recent work [207] in which the broadening and shifting coefficients as well as the real and imaginary parts of the Dicke narrowing parameter have been calculated for H$_2$ in He. This opens the route to refined simulations of isolated lines shapes following [208,209]. Table 1 regroups references in which various types of quantum calculations are presented. In some of these studies, both measurements and calculations were made, while the others compare theoretical results with previously published experimental data. The temperature dependences are also investigated in a few of them [156,193,194,210-212]. Generally speaking, when the calculations are performed using an accurate \textit{ab initio} PES, the CC values for the widths and the shifts are accurate, to within about 1%, at all temperatures except for very low ones. Indeed, there is an unexplained significant overestimation of the broadening by predictions in
the very low temperature domain (below ~ 10 K), as shown in [213] and further discussed in Sec. IV.3.5b of [1]. Finally, an example of the quality of predictions in the case of N$_2$-broadened C$_2$H$_2$ lines is given in Sec.3.3.3.

<table>
<thead>
<tr>
<th>System</th>
<th>Refs.</th>
<th>Method</th>
<th>Details</th>
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<td>[210#]</td>
<td>CC/CS (*)</td>
<td>PBC for infrared R lines. 77 and 1000 K.</td>
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<tr>
<td>C$_2$H$_2$H$_2$</td>
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<td>PBC for infrared R lines. 77-2000 K.</td>
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<td>CC (*)</td>
<td>PBC for the R(j=0-20) IR lines. 173, 195 and 295 K.</td>
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<tr>
<td>C$_2$H$_2$H$_2$</td>
<td>[215]</td>
<td>CC (*)</td>
<td>PBC for isotropic Raman lines at 143 K and IR lines at 173 and 295 K.</td>
</tr>
<tr>
<td>C$_2$H$_2$N$_2$</td>
<td>[193]</td>
<td>FC/SC/CC/CS (*)</td>
<td>PBC for isotropic Raman lines. 77-2000 K.</td>
</tr>
<tr>
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<td>PBC for IR and Raman lines. 150 and 300 K.</td>
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<td>CO-H$_2$</td>
<td>[205#]</td>
<td>CC (+RPA)</td>
<td>PBC for the R(10) and P(2) IR lines. 85-300 K.</td>
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<td>CC/CS (*)</td>
<td>PBC for rotational, vibrational and electronic rotational transitions.</td>
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<td>[203]</td>
<td>CC</td>
<td>PBC for the $1_{11}$$\rightarrow$0$<em>{10}$ and $1</em>{10}$$\rightarrow$1$_{01}$ rotational lines. 65-220 K</td>
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<td>CC</td>
<td>PBC &amp; PSC for the $1_{10}$$\rightarrow$0$<em>{00}$, $1</em>{10}$$\rightarrow$1$<em>{01}$ and $1</em>{11}$$\rightarrow$2$_{02}$ rotational lines. 20-250 K</td>
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<td>PBC for 228 H$_2$O transitions between 10 and 20000 GHz. 200-3000 K.</td>
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<td>PBC for 21 transitions between the eight lowest rotational levels of ortho and para H$_2$O. 20-120 K.</td>
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<td>[213#]</td>
<td>CC</td>
<td>PBC &amp; PSC for hyperfine components of the j=1$\rightarrow$0 and 2$\rightarrow$1 rotational lines. 1.3-20 K.</td>
</tr>
<tr>
<td>H$_2$O-$^1$H$_2$</td>
<td>[206]</td>
<td>CC/CS</td>
<td>PBC for infrared R lines. 77 and 1000 K.</td>
</tr>
<tr>
<td>HCO-$^1$H$_2$</td>
<td>[220#]</td>
<td>CC</td>
<td>PBC &amp; PSC for the j=1$\rightarrow$0 to 6$\rightarrow$5 rotational lines. 88 K.</td>
</tr>
<tr>
<td>H$_2$-Ar</td>
<td>[154]</td>
<td>CC</td>
<td>PBC and PSC for the S$_v$(0) line of H$_2$ and v=1$\rightarrow$0 rotational lines. 10-3000 K.</td>
</tr>
<tr>
<td>(H$_2$D$_2$)-He</td>
<td>[155]</td>
<td>CC</td>
<td>PBC and PSC for the S$_v$(0) line of H$_2$ and v=1$\rightarrow$0 rotational lines. 10-3000 K.</td>
</tr>
<tr>
<td>H$_2$-He</td>
<td>[207]</td>
<td>CC</td>
<td>PBC &amp; PSC and narrowing parameters for v=0$\rightarrow$1 to 5 and Q(0)$\rightarrow$0 to 5 lines. 10-2000 K.</td>
</tr>
<tr>
<td>N$_2$-H$_2$</td>
<td>[221#]</td>
<td>CC/CS (*)</td>
<td>PBC for isotropic Raman lines. 77-580 K.</td>
</tr>
<tr>
<td>N$_2$-H$_2$</td>
<td>[194]</td>
<td>FC/SC/CC/CS (*)</td>
<td>PBC for isotropic Raman lines. 77-2000 K.</td>
</tr>
<tr>
<td>N$_2$-N$_2$</td>
<td>[227#]</td>
<td>CC/CS (*)</td>
<td>PBC for isotropic Raman lines. 77-298 K.</td>
</tr>
<tr>
<td>N$_2$-N$_2$</td>
<td>[195]</td>
<td>FC/SC/CC/CS (*)</td>
<td>PBC for isotropic Raman lines. 77-2400 K.</td>
</tr>
<tr>
<td>N$_2$H'-He</td>
<td>[223#]</td>
<td>CC</td>
<td>PBC &amp; PSC for the j=3$\rightarrow$2 to 6$\rightarrow$5 hyperfine rotational transitions. 88 K.</td>
</tr>
<tr>
<td>OH-Ar</td>
<td>[202]</td>
<td>CC</td>
<td>PBC &amp; PSC for rotational, vibrational and electronic transitions. PESs for X-$^1$T$_1$ and A-$^3$Σ$^+$ states 296 K.</td>
</tr>
<tr>
<td>O$_3$-He</td>
<td>[201#]</td>
<td>CC (Hund case b.)</td>
<td>PBC &amp; PSC for transitions of the oxygen A-band. Different PESs in the ground and excited states. 296 K.</td>
</tr>
</tbody>
</table>

Table 1: Bibliography in which quantal calculations of pressure-broadening (PB) and/or -shifting (PS) coefficients (C) or cross-sections (XS) are presented. In column three FC stands for fully classical (Sect. 3.3.3.), SC for the semi-classical RB formalisms (Sect. 3.3.2 and 3.3.4), CC for close-coupling and CS for coupled states. (*) in column 3 denotes calculations with no vibrational dependence of the potential energy surface and thus no PSC. The references marked with a hash (eg [210#]) are those in which both measurements and calculations have been made.
3.3.2 Refined semi-classical Robert-Bonamy (RB) formalism

The RB formalism (Sec. 3.3.4) is the most widely used method for calculating collisional widths and shifts of isolated lines for complex molecules. However, although the non-diagonality of the Liouville scattering operator within the line space was known for years, the “usual” RB formalism ignores this property. As a first consequence, it significantly overestimates the line widths when compared with quantum calculations using the same intermolecular potential [193-195]. In addition, it does not enable prediction of the line couplings that result from the abovementioned non-diagonality. One of the most important contributions toward a refined formalism was presented in [224]. The proposed theory was applied to pure NH₃ [225] and to NH₃ diluted in Ar and He [226]. In both cases, the refinement of the RB formalism leads to a large decrease of the calculated widths. At the same time, a slightly different approach was proposed [227], based on the coordinate representation. It was first applied to isotropic Raman transitions of pure N₂ [227,228] for which a comparison with benchmark quantum results [195,229] was possible. This analysis showed that accounting for the line coupling reduces the line widths by about 15 % with a much better agreement with the quantum results. However, discrepancies remain, because of the semi-classical assumption which ignores exchanges between translational and internal degrees of freedom. Similar results were obtained for other linear molecules [230]. Finally, the case of symmetric tops with inversion symmetry, previously studied in [225,226] with a different model, was investigated recently using the coordinate representation approach [231,232], with applications to parallel and perpendicular bands of pure NH₃. Again, the improvement of the RB formalism leads to significant decreases (up to 30 % in some cases) of the calculated widths and to much better agreement with experimental results [231,232], as shown in Fig. 9 (and 10 for a linear molecule).

Fig. 9: Relative differences between measured pressure-broadening coefficients of the \( 'Q(j,k=j) \) lines of the \( v₁ \) band of pure NH₃ [233] and those calculated with (red) and without (black) taking into account the non-diagonality of the scattering operator (i.e., the line-coupling terms). After [231].

3.3.3 Fully classical approach

A series of papers [193-196,234-238] has resurrected the purely classical approach proposed by R.G. Gordon fifty years ago [239,240]. For several linear molecules, the resulting line-width predictions compare well with both experimental and quantum-calculated values, in much better agreement than the “usual” RB approach described in Sec. 3.3.4, as illustrated by Fig. 10. Another application of classical trajectories deserves to be mentioned: the demonstration of the influence of classically allowed quasi-bound complexes on the calculation of the widths and shifts for several molecular systems [241].
3.3.4 Some recent applications of the “usual” Robert-Bonamy (RB) formalism

The "usual" RB formalism, being based on the isolated-line approximation, only enables calculations of the widths and shifts. Despite its weaknesses (Sec. 3.3.2), this theory remains widely used because it can treat (very) complex molecular pairs, yielding reasonably good agreement with measurements at the price, in most cases, of some ad hoc adjustments of the intermolecular potential. Since its first version for linear molecules [243], extensions to other types of molecules and improvements (of the trajectory model and of the potential expansion) have been made, as reviewed in [244]. The bibliography on “RB pressure-broadened widths and shifts” is too vast to be exhaustively reported here, but Table 2 points to some recent or representative studies. For more information, the reader is invited to follow the bibliographical paths indicated in these studies, as well as those in [244] and Sec. IV.3.4e of [1].

<table>
<thead>
<tr>
<th>Radiator →</th>
<th>Linear</th>
<th>Symmetric-top</th>
<th>Asymmetric-top</th>
<th>Spherical-top</th>
</tr>
</thead>
<tbody>
<tr>
<td>Linear</td>
<td>[193-195,245-252]</td>
<td>[257-259]</td>
<td>[268-282]</td>
<td>[288-291]</td>
</tr>
<tr>
<td>Symmetric-top</td>
<td>---</td>
<td>[260]</td>
<td>---</td>
<td>---</td>
</tr>
<tr>
<td>Asymmetric-top</td>
<td>[253-256]</td>
<td>---</td>
<td>[142,282-286]</td>
<td>---</td>
</tr>
<tr>
<td>Spherical-top</td>
<td>---</td>
<td>---</td>
<td>[287]</td>
<td>---</td>
</tr>
</tbody>
</table>

Table 2: Some applications of the "usual" RB formalism to the calculation of pressure-broadening and -shifting coefficients.

3.4 Line mixing

We consider here, as in [292] and Chapt. IV of [1], the line-mixing (LM) process (also sometimes denoted as line coupling) in which exchanges of intensity between the lines result from the collision-induced transfers of populations between rotational levels. Except for recently proposed approaches in which the spectrum itself is directly computed (Sec. 3.4.1) or predicted based on some adjustable parameters (Secs. 3.4.7 and 3.4.8), all others rely on calculation of the so-called relaxation matrix $W$ (which is constructed in the line space and whose off-diagonal elements describe the LM process) from which the spectrum can be obtained (Sec. IV.2.1 of [1]). For this purpose, all available methods were proposed a while ago...
ago, except for the one presented in Sec. 3.4.3. It is important to recall that, except for that of Sec. 3.4.1, all the other approaches assume the “impact approximation” and are thus limited to calculation of LM effects not too far from line centers. In addition, and again with the exception of those presented in 3.4.1, all calculations disregard the effects of the speed dependence and of the collision-induced changes of the radiator velocity which have been investigated for isolated lines only (Sec. 3.2). The remainder of this section is organized as follows. We first present approaches that enable a direct prediction of the spectrum (Sec 3.4.1) or of the relaxation matrix \( W \) (Secs. 3.4.2-3.4.4) from knowledge of the intermolecular potential. We then consider those with which \( W \) elements can be computed using some parameters that are deduced from fits of measured data (Secs. 3.4.5 and 3.4.6). Finally, other semi-empirical and less commonly used models are presented in the last two sections.

The remainder of this section shows that significant advances have been made in the last decade for the development of new theories and models as well as for the further test of existing ones. However, except for the approaches discussed in Secs. 3.4.1 and 3.4.5, all others have been recently tested by comparisons with experiments at room temperature only. Quantifying the ability of the promising refined Robert-Bonamy and fully classical models to describe the effects of temperature is thus of interest for future studies.

### 3.4.1 Requantized Classical Molecular Dynamics Simulations

The requantized CMDS proposed in [117] (Sec. 3.2.1) for calculations of isolated-line shapes were extended in [123] to enable direct prediction of the absorption over an entire band. For this, the direction of molecular rotation is considered to discriminate between P- and R-branch lines, and corrections are introduced so that the line positions and intensities match some chosen (true) values. The resulting model, limited to linear absorbing molecules, was tested [123] by comparison with measured spectra of CO\(_2\) at elevated pressures, for some infrared bands from 296 K to 480 K and for an isotropic Raman Q branch from room temperature up to 700 K. In most cases, the predictions agree with measurements within 5\%, regardless of temperature, as illustrated by Fig. 11.

![Fig. 11: Area-normalized intensities (in arbitrary units) in the 2\(v_2\) isotropic Raman Q branch of pure CO\(_2\) at: (a) 295 K and 0.5 amagat and (b) 700 K and 1.0 amagat. Red symbols are measured values from [293], while the lines are calculated results obtained with the rCMDS model (blue) and neglecting LM (black). After [123].](image)

### 3.4.2 Quantal approaches

As discussed in Sec. 3.3.1, computer codes have been developed for quantum calculations of matrix elements of the scattering operators at various levels of accuracy. Post-processing programs then provide the diagonal and off-diagonal elements of the relaxation matrix \( W \), depending on the type of spectroscopy (isotropic Raman diffusion, absorption, etc.). While these tools have long existed, constructing a full \( W \) matrix for molecular pairs using
refined quantal approaches was intractable until recently. Thanks to the advances in computing power, this has progressively become feasible. A fully quantum calculation for the isotropic Raman spectrum of N$_2$ at room temperature was made in [229] where it was shown that, for moderate values of the rotational quantum number, the convergence of CC/CS off-diagonal $W$ elements could be achieved, in good agreement with experimental data, therefore providing benchmark results for the test of more approximate formalisms (Secs. 3.4.3 and 3.4.4). Note that the case of isotropic Raman Q branches of linear molecules is “simple” when vibrational effects are neglected, because the real off-diagonal elements of $W$ are then simply the negative of the usual inelastic state-to-state collisional transfer rates. The oxygen A-band perturbed by helium was studied theoretically and experimentally in [201]. For the first time for an electronic transition, the relaxation matrix was obtained from a fully quantum mechanical approach, leading to good agreement with measurements. This is a significant and difficult step since it requires computations using (very complex) wave functions taking into account the rotational, vibrational and electronic degrees of freedom. The above-mentioned computations are thus close to the current limit of feasibility, which explains the rarity of applications of fully quantal approaches to LM processes.

**3.4.3 Refined semi-classical Robert-Bonamy formalism**

As discussed in Sec. 3.3.2, refinements of the “usual” RB formalism have been proposed, which do not neglect the non-diagonality of the Liouville scattering operator. This leads to better line-width predictions (Sec. 3.3.2), but also enables the calculation of the off-diagonal elements of the relaxation matrix $W$. Cherkasov investigated the case of molecules exhibiting hyperfine structure caused by the nuclear quadrupole interaction, by using his semi-classical theory, with applications to CH$_3$I [294] and CH$_3$Cl [295]. In most cases LM effects are weak. He later published a new version of his theory [224] which was successfully applied to the $^2$Q(j,k) doublets in the v$_1$ band of pure NH$_3$ [225] and to the calculation of $W$ elements for NH$_3$ in Ar and He [226]. A slightly different approach, based on the use of the coordinate representation and choosing the orientations of pairs of molecules as a basis set in the Hilbert space (ie that of the states), was proposed in [227] in order to construct $W$ in the Liouville space (ie that of the lines). It was first applied to isotropic Raman spectra of pure N$_2$ [228] with successful comparisons with benchmark quantum calculations of the $W$ matrix [229] (see figure in Sec. 3.4.4). Note that, as a consequence of the semi-classical assumption, a "sum rule" (eg [296] and Sec. 4.2.1 of [1]) that should be verified by the columns of the $W$ matrix is not satisfied. In order to correct this discrepancy, a "renormalization procedure" was proposed [296], in which the off-diagonal elements of $W$ are multiplied by factors determined from knowledge of the line-broadening coefficients. When this is done, the refined RB predictions compares well with quantum calculations, as mentioned above. However, without introducing this renormalization, the refined RB formalism can still provide semi-quantitative information on LM for complex systems. This approach was then extended to infrared spectra of linear molecules [230] with applications to parallel and perpendicular bands of CO$_2$ in N$_2$ [297]. By properly accounting for the influence of the vibrational angular momentum, the formalism leads to predictions of LM effects in good agreement with both measurements and ECS (Sec. 3.4.5) predictions for different types ($\Sigma \leftrightarrow \Sigma$, $\Pi \leftrightarrow \Sigma$, etc) of bands. The further extension to asymmetric tops has allowed the analysis of line couplings within H$_2$O vibrational bands [298] and quantitative tools have been developed to determine the relative importance of the off-diagonal elements of $W$. This showed that most of the H$_2$O lines in the pure rotational band are practically uncoupled while a few lines exhibit small but significant couplings. The case of symmetric tops with inversion symmetry, previously studied in [225,226] with a different model, was investigated recently using the coordinate representation approach, with applications to parallel and perpendicular bands of pure NH$_3$. 


The results show that this theory reproduces well the LM signatures (e.g., Fig. 12) and W elements observed in some spectral regions of the \( \nu_1 \) and \( \nu_4 \) bands [299,300], as well as the influence of the vibrationally dependent inversion splitting [232].

![Fig. 12: LM signatures in the self-broadened R(3,k) manifold of the \( \nu_1 \) band of pure NH\(_3\) at 50 Torr. The upper curve is the calculated transmittance. The bottom red (resp. blue) curve is five times the difference between the measured (resp. calculated) transmission and that fitted (resp. calculated) without the inclusion of LM. After [299].](image)

### 3.4.4 Fully classical formalism

The classical approach proposed by R.G. Gordon fifty years ago [239,240,301] not only enables calculations of the pressure-broadening and -shifting coefficients (Sec. 3.3.3) but also of the off-diagonal elements of the relaxation matrix. This possibility has been used recently for predictions of LM effects in isotropic Raman spectra of pure N\(_2\) [237]. For this system, good agreement was obtained (Fig. 13) with results of a benchmark quantum calculation [229], thus opening the route to the treatment of more complex molecular pairs.

![Fig. 13: Computed relaxation-matrix elements \( W(j'\leftarrow j=6) \) between the Q(6) lines and various Q(j') for N\(_2\)-N\(_2\) at 298 K. CC/CS denote the quantum results from [229], cRB the corrected-RB predictions from [228] and C3D(db) the results of classical calculations. After [237].](image)

### 3.4.5 Dynamically based scaling laws

The Infinite-Order Sudden (IOS) approximation and the more refined Energy-Corrected Sudden (ECS) scaling law have been used for the modeling of LM effects within various spectral features and for many molecular systems (Sec. IV.3.3 and Table IV.9 of [1]). These approaches construct the real-valued elements of the relaxation matrix \( W \) from a limited set of parameters whose values can be calculated but are generally deduced from fits of measured line-broadening data.

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The quality of the ECS approach was further tested in studies devoted to a few linear molecules. For CO$_2$, the models described in [296] and [302,303] were used for quite successful further comparisons with measurements in the central regions of many bands over wide ranges of temperature and pressure [304-315]. A successful application was also made to some bands of OCS in He at elevated pressures [316]. For O$_2$, which requires accounting for the spin-orbit interaction effect, an ECS approach was proposed for the pure Hund's case b in [317]. It was then empirically improved (by using other ECS parameters and a modified sum rule) and applied to the A-band in [318]. Good agreements with high pressure laboratory spectra and measured atmospheric transmissions were obtained. The same approach enabled an accurate description of LM effects in the O$_2$ rotational band around 60 GHz [319], a region also modeled using the memory function formalism [320]. Many of the abovementioned studies present comparisons between measured and computed spectra at various temperatures, roughly between 200 K and 300 K. These show that the quality of predictions is generally within 5% or less and does not significantly change with temperature.

In addition to these applications of previously published theories, a new approach has been proposed for LM between $M$ components. In other words, line-mixing was considered among lines not only defined by the total rotational quantum number $J$ only, but by both the value of $J$ and that of $M$ (magnetic quantum number) that quantifies the projection of $J$ on the space-fixed axis. As it is well known, the lines associated with the same $J$ but different $M$ values can be spectrally separated by an electric field and the Stark effect. Starting from [321], an adapted IOS model was developed in [322] and applied to spectra of CH$_3$F with lines separated through the Stark effect. This revealed, with good agreement with measured spectra, the overly simplified approximation made in [323] where discrepancies between measurements and calculations were obtained. Similarly, a model based on the IOS approximation and the developments in [324] was proposed [325] and successfully applied to line-broadening and -mixing within nuclear spin hyperfine components of He-broadened lines of HI at room temperature. From a purely theoretical point of view, Buffa and Tarrini have corrected [218,326] an error in the method elaborated in [324] which rendered it self-inconsistent. However, as stated in [326], this correction does not change the predicted LM effects and "the equations used by Flaud et al. [325] yield the same line shape as our equations."

3.4.6 Energy-gap fitting laws and state-to-state cross sections

Empirical approaches are obviously of interest when more physically based models are not available or too costly to implement. Here, the central idea is to express a given off-diagonal real-valued element of the relaxation matrix in terms of the state-to-state inelastic cross-section connecting the lower (and/or upper) levels of the two interfering lines. This requires switching from the two-dimensional (the two connected states) space of the state-to-state rates to the four-dimensional (the two lower states of the lines and the branches to which the lines belong) space of the absorption lines, an operation achieved by introducing a (P, Q, R) branch-dependent empirical scaling factor. Considering the state-to-state rates, they are often modeled using energy-gap fitting laws (IV.3.2 of [1] and [327]) based on a few parameters that are generally deduced from fits of line-broadening data. New applications of this type of approach to LM effects for a variety of molecules can be found in [238,245,272,304-308,315,328-332]. Note that there is a rarely used alternative solution. Indeed, several computer codes exist, from semi-classical up to CC, to calculate these state-to-state rates, which can therefore be directly introduced to the LM model (or compared to the fitted ones). Examples are given in IV.3.4f of [1] and [333,334]. This remark also applies to the ECS model where the so-called basic rates can be calculated (eg [335,336]) instead of being modeled with parameters obtained by fits to measured data.
3.4.7 The ovoid sphere and hard collision models

Despite the simplicity of the classical ovoid sphere model ([337] and Sec. IV.3.1b of [1]), this approach, in which an effective collision frequency is empirically adjusted for agreement with measured line widths, provided an accurate description (comparable with the results obtained with the ECS model) of LM in spectra of OCS diluted in He at elevated pressures [316]. It was also applied to the A band of $\text{O}_2$ in [338,339]. Similar remarks can be made for the application of the extended strong collision model ([340] and IV.3.1a of [1]) to the $2\nu_3$ isotropic Raman band and depolarized Raman spectra of $\text{CO}_2$ [341,342].

3.4.8 Kochanov’s approach

A line-profile model was recently developed by Kochanov, allowing comparison of the influences of the collisional and Doppler broadenings, Dicke narrowing, velocity dependence of the widths and shifts as well as of the LM process [190,343]. The latter appears through a speed-independent first-order LM coefficient [344]. The resulting model involves many parameters likely to be fitted to experiments but, to the best of our knowledge, its ability to accurately describe measurements has not been proven so far.

3.5 Far wings and associated continua

We consider here, as in Chapt. V of [1], the spectral regions significantly far from line centers where the absorption manifests as a continuum. We here restrict ourselves to those to which the far wings of monomer lines make a significant contribution, the continua caused by the transient dipole induced during collisions being considered in Sec. 3.6. As noted in [1], first-principles calculations of the contributions of the far wings of allowed (meaning due to the molecule intrinsic dipole) transitions is an extremely difficult problem because many processes must simultaneously be taken into account: the speed dependent line-broadening and -mixing, the finite duration of collisions and initial correlations. The so-called impact approximation breaks down and models such as those described in the preceding sections cannot be used. Recall (cf Sec. II.3.4 of [1]) that this approximation assumes that the differences $|\omega - \omega_0|$ between the photon frequency and those of the optical transitions of the molecule which make the dominant local contribution to the spectrum are much smaller than the inverse of the duration $\tau_c$ of efficient collisions (ie $|\omega - \omega_0|\tau_c << 1$). In this case, intermolecular collisions can be considered as instantaneous (impact) and the spectrum is not sensitive to details of what happens during collisions but only to the difference between the molecular state before and after a collision. This simplification can thus be used not to far away from line centers. Various approaches have been proposed, those published before 2007 being described in Chapt. V of [1]. From the theoretical point of view, little progress has been made since that time, with the exception of the approach described in Sec. 3.5.1. For the empirical models that rely on adjustments to measured spectra, the main advances concern the $\text{H}_2\text{O}$ continuum (Sec. 3.5.4).

3.5.1 Direct predictions from Classical Molecular Dynamics Simulations

In [345], CMDS were carried for pure $\text{CO}_2$. These provide (cf Secs. 3.2.1 and 3.4.1) the center-of-mass positions and orientations of many (rigid) linear molecules interacting though an input anisotropic potential. For parallel bands, the allowed-dipole vector $\vec{\mu}^A$ is along the molecule axis. Its auto-correlation function (ACF) is thus directly calculated from the CMDS, after a proper spectroscopic scaling factor [345] and the choice of time $t=0$ in the calculations. The spectrum is then obtained from the Fourier-Laplace transform of the ACF (ie multiplying the ACF by $\exp(-i\omega t)$ and integrating from $t=0$ to $+\infty$). A comparison was made [322]
between the resulting predictions, free of any scaling factor deduced from experiments, and measurements in the wings of the $v_3$ band of CO$_2$ at 200 K and 296 K. A good (in the log scale used for the comparison) agreement was obtained at 296 K that degrades slightly at lower temperature. Errors locally reach a factor of two but on a quantity that varies over almost four orders of magnitude (cf Fig. 14). Shortly thereafter, the contribution of the collision-induced dipole $\mu^I$ was introduced [346] (calculated as in [347], cf Sec. 3.6.4) and the ACF of the full dipole (including the allowed and induced components) was computed. The results agree quite well with measurements, as illustrated by Fig. 14, and demonstrate that the cross-term $\mu^A(0)\mu^I(t) + \mu^I(0)\mu^A(t)$ in the ACF makes a significant contribution. Note that similar results were very recently obtained in the same region of CO$_2$ absorption but in the case of collisions with water vapor [348]. Finally, the approach was also applied to the wing of the depolarized Rayleigh roto-translational spectrum of pure CO$_2$ in [346].

![Fig. 14: Squared-density normalized absorption in the wings of the pure CO$_2$ $v_3$ band. The symbols are experimental values, the blue line is the result of a purely Lorentzian calculation, and the red line represents the CMDS results. After [346].](image)

The same type of approach, limited to the contribution of the allowed dipole but improved through a requantization of the CMDS ([121] and Sec. 3.2.1) was applied [124] to spectra of HCl in Ar at room temperature. These direct calculations of the entire spectrum show that the absorption in the troughs between lines is super-Lorentzian in the central part of the bands and becomes sub-Lorentzian when going toward the bands wings. Super- (resp. sub-) Lorentzian here mean that the absorption is greater (resp. lower) than that calculated by summing the contributions of all lines with a Lorentz profile. Their analysis demonstrates that this behavior is intimately connected to the evolution of the dipole ACF at very short times (finite duration of collisions) and to the increasing contribution of LM when going away from the band center. Note that the computed values of the relative deviation from the purely Lorentzian behavior agree, within experimental uncertainties, with those deduced from measurements, and that this is achieved without use of any adjustment.

### 3.5.2 Non Markovian Energy-Corrected Sudden approach

A non-Markovian extension of the Energy-Corrected Sudden model for the construction of the relaxation matrix was proposed in [302,349] (see also V.5 of [1]). It goes beyond the impact (Markovian) approximation by taking into account the fact that, in the wings, the energy defect associated with the difference between the frequency of the photon and those of the resonant molecular transitions cannot be neglected. As discussed therein, it enables, in principle, a better description of the far wings than the “usual” ECS model (Sec. 3.4.5) which fails because the impact approximation breaks down. This approach was recently applied to
CO₂ anisotropic Raman scattering spectra [350], showing a good agreement with measurements in the central regions of the bands but a significant underestimation in the wings which is consistent with the previous studies.

### 3.5.3 Asymptotic line shape and χ-factor empirical models

An asymptotic approach for the description of the far line wings was proposed in [351] and applied to CO₂ [352] and to the water-vapor continuum in several spectral regions [351,353,354]. Good agreement with measurements was obtained at various temperatures, but this required the ad hoc adjustment of some parameters. The proposed model thus has limited predictive capabilities and it should be considered as empirical, as the χ-factor approach of [311,355,356] (see also V.2 of [1]) and the MT_CKD continuum discussed below.

### 3.5.4 The MT_CKD water-vapor continuum

The absorption spectrum of water vapor contains not only narrow rovibrational lines whose spectroscopic parameters are tabulated in databases but also a relatively weak underlying broadband continuum with a slow frequency dependence. In the Earth’s atmosphere, this continuum (see also Sec. 4.3.1, [357] and appendix V.A of [1]) can be decomposed into a “self” component due to water-water intermolecular interactions and a “foreign” component due to water-nitrogen and water-oxygen interactions. According to the usual definition, these continua are obtained after subtraction, from the total absorption coefficient, of the contribution of the H₂O lines calculated using Voigt profiles truncated at ±25 cm⁻¹ from their centers [358]. For a binary mixture of water vapor and nitrogen, for instance, the quantity obtained after this exercise has a component that increases quadratically with the water partial pressure and another one proportional to the product of the H₂O and N₂ partial pressures. These are the so-called self- and foreign-continuum contributions (Cₛ and Cₓ) to the total absorption coefficient α(T) of the preceding equation has generally been the pragmatic approach of Clough-Kneizys-Davies (CKD) [358] and its successor Mlawer-Tobin-CKD (MT_CKD) [359,360]). It is a semi-empirical formulation based on ad hoc (line-profile) parameters adjusted to measured spectra. The latter consist mainly of laboratory (eg [361-364], see [357]) and field (eg [365]) measurements in spectral regions that have [366,367] the strongest impact on the radiative fluxes in the Earth atmosphere. The 10 µm window has been studied for decades (eg [357,362,368-370]) and a strong constraint of the MT_CKD self continuum (ie pure H₂O) in this region comes from field measurements (eg [371]). In the mid- and near-infrared regions, the MT_CKD continuum is mostly an extrapolation, which up to recently was lacking experimental validation. In recent years, considerable experimental efforts have been devoted to this issue as discussed in Sec. 4.3.1. The recent changes made to the MT_CKD continua are described in [359,360] and the current versions for both the self (H₂O-H₂O) and foreign (H₂O-air) contributions can be downloaded at [372] where more information on the continua is given. A comparison between several sets of measurements of the self-continuum and the last version (V3.0) of the MT_CKD model is plotted in Fig. 15. If one excludes the FTS experiments from CAVIAR and Tomsk [373-375], which are in striking disagreement (as further discussed in Sec. 4.3.1a), the MT_CKD3.0 general evolution is well supported by recent CRDS and OF-
CEAS measurements [376-381], with very good agreement in the 1.6 µm and 1.25 µm windows but significant deviations at the center of the 2.1 µm and 4.0 µm windows.

Fig. 15: Comparison between the MT_CKD(v3.0) self-continuum cross section $C_s$ of H$_2$O at room temperature (line) and measurements with grating spectrograph [362] (light blue circles); by calorimetric interferometry [382] (full and open blue diamonds) [383] (green star); by FTS from [373] (blue squares), [384] (orange open squares), [374] and [375] (open grey and light green circles); by CRDS and OF-CEAS from [376-381] (open red circles).

The origin of the temperature dependence of the water continuum in the MT_CKD model is detailed in [359]. In particular, it is indicated that the MT_CKD temperature dependence of the self continuum relies on the measurements by Burch et al. in the 700-1200 cm$^{-1}$ and 2400-2800 cm$^{-1}$ windows [361-363, 385]. To the best of our knowledge, the much more recent results of [384] were not taken into account to adjust the MT_CKD model. For the foreign continuum, the MT_CKD values are practically independent of temperature in the infrared, consistently with what was experimentally found [386-388].

### 3.6 Collision-induced absorption (CIA)

We consider here CIA where it is the transient dipole created during the interaction of molecular pairs that leads to light-matter interaction and produces a spectrum, as discussed in [389,390] and Chapt. VI of [1]. Note that the terms interaction-induced, or supermolecular absorption may also be used, and it is sometimes more appropriate since dimers may also contribute to the absorption. A discussion on the definition of CIA in the context of the water vapor continuum can be found in [391]. We focus below on theoretical treatments of CIA involving molecules, ie not rare-gas mixtures, and in general disregard collision-induced light scattering. We begin with the state-of-the-art coupled quantum scattering treatments in Sec. 3.6.1. After that comes a brief presentation of new findings in intra-collisional interference, a phenomenon where a coupled scattering-treatment is needed (Sec. 3.6.2). The “standard” binary-collision treatment, which normally entails one-dimensional quantum scattering, and sometimes classical two-body collision calculations, is covered in Sec. 3.6.3. Progress in classical many-body treatments, so-called molecular dynamics simulations, is described in Sec. 3.6.4. Finally, integrated spectra, or spectral moments, are discussed in Sec. 3.6.5.

#### 3.6.1 Quantum scattering advances
Refined quantum-dynamical calculations, based on the CC method and including the full anisotropic potential, were made in [392] for CIA spectra of H\textsubscript{2}. The free-free dipole matrix elements are obtained on-the-fly, which gives this new method an advantage by comparison to a previous study [393] that also included the anisotropy of the interaction potential in CIA calculations. The more challenging case of nitrogen [394] was then considered and, since the N\textsubscript{2}-N\textsubscript{2} pair potential supports many bound (dimer) states, the dimer contribution to the absorption was also taken into account. This enabled quantification of the various contributions to the spectrum, as illustrated by Fig. 16. Full CC calculations of N\textsubscript{2} CIA, with an anisotropic potential, are barely feasible. Nevertheless, the authors performed one such benchmark calculation, at low energy and for one representative photon frequency, which was compared with CS calculations. They concluded that the latter capture most of the effect from the anisotropy of the potential, and thus the CS approximation was applied in the final calculations of absorption coefficients. The studies [392] and [394] both include comparisons with measurements at temperatures ranging from 77 K to 300 K. While excellent agreement is obtained above ~150 K, the calculations increasingly underestimate the peak absorption with decreasing temperature (by about 20% at 78 K [394]).

From the same group as the works described above come remarkable studies of the spin-forbidden A-band transition in O\textsubscript{2}, induced by collisions with a second oxygen [395] or a nitrogen [396] molecule. For the former work, new dipole and potential energy surfaces were computed [397]. In the comparison of O\textsubscript{2} and N\textsubscript{2} as a collisional partner the authors conclude that there are large differences between the two, in agreement with measurements, but contrary to what has previously been believed [389]. The reason is that an exchange mechanism, which is allowed for O\textsubscript{2}-O\textsubscript{2} but not for N\textsubscript{2}-O\textsubscript{2}, is responsible for much of the absorption in pure oxygen. In a comparison of the computed and measured absorption spectra the absolute absorptions agree within an order of magnitude and, through scaling of the various contributions, good agreements between for both the magnitudes and shapes of measured and calculated spectra are obtained.

### 3.6.2 Intra-collisional interference effects

CIA provides a convenient case for the study of intra-collisional effects, a phenomenon reviewed in [398]. In systems like HD, which has a rather small dipole moment, interference can be observed between the permanent and the interaction-induced dipoles (cf. VI.6.2 of [1] and references therein). An equivalent mechanism, the interference of Raman-allowed S-lines...
and the collision-induced light scattering, has been studied in pure H₂ [399] and in a H₂-Xe mixture [400].

### 3.6.3 Standard binary-collision treatments

Frommhold and co-workers have made several computational studies of CIA in hydrogen-containing gases, at temperatures from hundreds to thousands of K. These works are of importance for further studies of some stellar atmospheres where the level of ionization is low, such as those of cool white dwarfs. Their method is usually quantum mechanical, but ignores anisotropic components of the intermolecular potential ("isotropic approximation"). Investigations were made for pure H₂ [401-403] and for H₂ with He [404], with corresponding studies for deuterium and tritium in [405-407]. Most of those studies include comparisons with laboratory measurements at several different temperatures, and they are done using recent \textit{ab initio} potential and dipole data. The agreement with measurements is generally considered as very good, at least in the log-scales used for comparisons of absorption coefficients which vary by several orders of magnitude throughout the considered spectral range. El-Kader and coworkers pursued studies at a similar level of theory for H₂-(Ar,He) [408,409], CF₄-He mixtures [410], pure methane [411], pure N₂ [412], and pure O₂ [413]. A classical trajectory study of CIA in CO₂-(Ar,Xe) mixtures can be found in [414].

### 3.6.4 Direct predictions from Classical Molecular Dynamics Simulations

The CMDS proposed in [415] for the far infrared CIA by CO₂ was revisited in [347] which demonstrated the importance of vibrational and back-induction contributions. Taking these effects into account largely obviated the need for the \textit{ad hoc} short-range overlap contributions empirically introduced in [415]. Subsequently, this approach enabled the first analysis [346] of the respective contributions of allowed and induced dipoles, and the so-called intra-collisional interference, in the wings of the CO₂ v₃ band (Sec. 3.5.1). The predictions of the far infrared roto-translational CIA band of N₂ [416] were, at the time, the first in which the spectral effects of the intermolecular anisotropy and of (\textit{ab initio}) short-range dipole components were studied for N₂. Since then, much more refined computations have been made [394] (Sec. 3.6.1). CMDS also enabled the modeling of CIA in the region of the first overtone of N₂ with the analysis (Fig. 17) of the spectral contributions of the single and double (or simultaneous) transitions [417]. The comparisons with measurements made in [417] also show that, while the CMDS slightly overestimate absorption at room temperature, they strongly underestimate (~40 %) it around 90 K. Note that CMDS were very recently made for the fundamental band of N₂ colliding with H₂O [348]. Agreement within the uncertainties of measurements [418] was obtained and the calculations confirm the considerable enhancement of the peak value and width of the CIA spectrum for N₂-H₂O collisions with respect to those for pure N₂.
3.6.5 Integrated CIA intensities

CIA may be studied theoretically without computing spectra, but rather integrated spectra or so-called spectral moments. These can in general be calculated with less effort using sum formulas [389], and may be used in combination with line-shape models (eg [420,421]) to provide spectra. Recent studies of spectral moments include those in the N$_2$ fundamental for pure N$_2$ [422] and water-nitrogen [418], pure methane [423], methane-argon mixtures [424] and CO$_2$ (pure and with rare gases) [425]. In all those studies, new potential and/or dipole data were also developed. Predictions generally agree with measurements within typically 10% and correctly describe the influence of temperature (eg [422,425]). Spectral moments for CO$_2$ have been computed in [426] where formulas including the anisotropy of the potential are given and the importance of the vibrational dependence of the polarizability is established. In a study of water vapor [427], spectral moments were computed and used in combination with the line shape of [420] to produce CIA spectra. Finally, expressions for spectral moments which can be used to separate bound-state contributions from the free-to-free component have been derived [424,428].

4. Available data

This section proposes a number of references in which data are provided (either directly or on request from the authors) that can be used in order to calculate absorption spectra. The associated experimental or calculated results enable simulations of isolated-line shapes (Sec. 4.1), of line-mixing effects (Sec. 4.2), of the far wings and associated continua (Sec. 4.3), and of collision-induced absorption (Sec. 4.4). Although the tables in these sections may not be exhaustive, they give numerous starting points for bibliographical searches, while data and other references are also given in [1,244,429-433]. Finally, the recent evolution of spectroscopic databases is discussed in Sec. 4.5.

For the extraction of spectral-shape parameters from measured spectra, several sophisticated fitting programs have been developed (eg [99,170,434]). It here is important to recall the importance, when the model involves many parameters, of using least-squares fitting methods where parameters are simultaneously adjusted to fit multiple spectra. Good examples in which multispectrum fitting methods have been used to retrieve many spectral parameters can be found in [9,100,168,435-437] for instance. Furthermore, when (over)simplified fitting profiles and/or noisy experiments are used, one should very carefully consider the overall uncertainty on the retrieved parameters, including those due to both the model approximations and the
measurement errors and noise. Otherwise hasty conclusions may be drawn, as shown in [438] for instance.

4.1 Isolated lines

The bibliography providing isolated-line shape parameters deduced from laboratory measurements is much too vast to be exhaustively reviewed, even when restricted to the publications of the decade. We have thus decided to only retain, in Table 3, those in which line profiles more refined than the VP were used. Readers searching for pressure-broadening and -shifting coefficients adapted to the VP can consult the broad bibliography provided with spectroscopic databases [430,431,439]. It is important to note that most of the studies cited below are limited to room temperature. Furthermore, many of those in which various temperatures were investigated used fits with “simple” non-Voigt profiles such as the SC, HC and qSDV. Only a few pioneers [103,153,181,440] have tested sophisticated line-shape models including the HTP.

<table>
<thead>
<tr>
<th>Molecule Region</th>
<th>Perturber</th>
<th>Model</th>
<th>Refs.</th>
</tr>
</thead>
<tbody>
<tr>
<td>H₂O</td>
<td>0.81-0.83 μm</td>
<td>H₂O,air</td>
<td>HC,qSDV</td>
</tr>
<tr>
<td></td>
<td>0.93 μm</td>
<td>N₂,air</td>
<td>SC,HC,qSDV</td>
</tr>
<tr>
<td></td>
<td></td>
<td>H₂O,N₂</td>
<td>SC</td>
</tr>
<tr>
<td></td>
<td></td>
<td>N₂,SF₆</td>
<td>HT</td>
</tr>
<tr>
<td></td>
<td>1.28 μm</td>
<td>H₂O</td>
<td>SC,HC,qSDV,qSDHC,HT,pChSDHC</td>
</tr>
<tr>
<td></td>
<td>1.39 μm</td>
<td>H₂O</td>
<td>pChSDHC,HT</td>
</tr>
<tr>
<td></td>
<td></td>
<td>H₂O</td>
<td>SC,HC,qSDV,qSDHC</td>
</tr>
<tr>
<td></td>
<td></td>
<td>N₂</td>
<td>SC,HC,qSDV</td>
</tr>
<tr>
<td>H₂O</td>
<td>1.4 μm</td>
<td>H₂O,Ar</td>
<td>SC</td>
</tr>
<tr>
<td></td>
<td></td>
<td>H₂O,N₂</td>
<td>SC,HC,qSDV</td>
</tr>
<tr>
<td></td>
<td></td>
<td>H₂O,N₂</td>
<td>SC,qSDV</td>
</tr>
<tr>
<td></td>
<td></td>
<td>H₂O,N₂,He</td>
<td>SC,qSDV</td>
</tr>
<tr>
<td></td>
<td></td>
<td>He</td>
<td>SC</td>
</tr>
<tr>
<td></td>
<td>1.39-1.47 μm</td>
<td>H₂O</td>
<td>HC,qSDV</td>
</tr>
<tr>
<td></td>
<td>1.6 μm</td>
<td>H₂O</td>
<td>HT</td>
</tr>
<tr>
<td></td>
<td>2.5 μm</td>
<td>H₂O,CO₂,N₂</td>
<td>SC</td>
</tr>
<tr>
<td></td>
<td>2.6 μm</td>
<td>N₂</td>
<td>HT</td>
</tr>
<tr>
<td></td>
<td>2.5-2.9 μm</td>
<td>Air</td>
<td>qSDV</td>
</tr>
<tr>
<td></td>
<td>2.5-5.4 μm</td>
<td>H₂O,air</td>
<td>qSDV</td>
</tr>
<tr>
<td></td>
<td>2.5-5.4 μm</td>
<td>H₂O</td>
<td>SDV</td>
</tr>
<tr>
<td></td>
<td>2.7, 6.25 μm</td>
<td>H₂O</td>
<td>HC</td>
</tr>
<tr>
<td></td>
<td>22 GHz</td>
<td>H₂O,air</td>
<td>SDV</td>
</tr>
<tr>
<td>HDO</td>
<td>2.7 μm</td>
<td>CO₂,HDO</td>
<td>qSDV</td>
</tr>
<tr>
<td></td>
<td>3.6 μm</td>
<td>CO₂,HDO</td>
<td>qSDV</td>
</tr>
<tr>
<td></td>
<td>7.4 μm</td>
<td>CO₂</td>
<td>qSDV</td>
</tr>
<tr>
<td>HCl</td>
<td>3.5 μm</td>
<td>N₂,He,Ar,Xe,He</td>
<td>SC,HC,RG</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Ar</td>
<td>qSDHC</td>
</tr>
<tr>
<td>CH₄</td>
<td>7.7 μm</td>
<td>Ar,He,N₂,CO₂</td>
<td>SC,HC,qSDV,qSDHC,HT</td>
</tr>
<tr>
<td></td>
<td>3.3 μm</td>
<td>Ar,He,H₂O,N₂,CO₂</td>
<td>SC,HC,qSDV,qSDHC,HT</td>
</tr>
<tr>
<td></td>
<td>1.7 μm</td>
<td>CH₄,air</td>
<td>qSDV</td>
</tr>
<tr>
<td></td>
<td></td>
<td>air</td>
<td>HT</td>
</tr>
<tr>
<td></td>
<td>2.2 μm</td>
<td>CH₄,air</td>
<td>qSDV</td>
</tr>
<tr>
<td></td>
<td>1.6 μm</td>
<td>CO₂,air</td>
<td>qSDV</td>
</tr>
<tr>
<td></td>
<td></td>
<td>CO₂</td>
<td>HC,qSDV,qSDHC,HT</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Air</td>
<td>SC,HC,qSDV,qSDHC</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Air</td>
<td>qSDV,qSDHC</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Air</td>
<td>HT</td>
</tr>
</tbody>
</table>
Table 3: Bibliography providing data from fits of measured isolated line shapes using various profiles more refined than the usual Voigt or Lorentz ones. Acronyms: “SC”: Soft Collisions;
“BB”: Billiard Ball; “B”: Blackmore, “RG”: Rautian-Galatry; “V”: Voigt; “SD”: Speed Dependent; “q”: quadratic; “h”: hypergeometric; “pC”: partially Correlated; “HT”: Hartmann-Tran. The references marked with an asterisk (eg [415*]) are those in which the temperature dependence of line-shape parameters other than the usual broadening (and shifting) were investigated.

4.2 Line mixing

Table 4 completes tables IV.5 and IV.6 of [1] by giving a list of recent references providing data that enable the inclusion of LM effects in spectra calculations. The available parameters, which can be used as explained in Sec. IV.2 of [1], consist either of relaxation-matrix elements or first-order LM coefficients within the so-called “Rosenkranz approximation” [344].

<table>
<thead>
<tr>
<th>Molec</th>
<th>Region</th>
<th>Techn</th>
<th>Refs.</th>
</tr>
</thead>
<tbody>
<tr>
<td>C$_2$H$_2$</td>
<td>1.5 µm</td>
<td>Exp &amp; Calc</td>
<td>[330*]</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Exp</td>
<td>[486]</td>
</tr>
<tr>
<td>CH$_3$D</td>
<td>7.66 µm</td>
<td>Exp</td>
<td>[259*]</td>
</tr>
<tr>
<td>CH$_4$</td>
<td>1.6 µm</td>
<td>Exp</td>
<td>[9,102*,455*,497,498]</td>
</tr>
<tr>
<td></td>
<td>2.2 µm</td>
<td>Exp</td>
<td>[333]</td>
</tr>
<tr>
<td></td>
<td>3 µm</td>
<td>Exp</td>
<td>[456*,499*]</td>
</tr>
<tr>
<td></td>
<td>6.4 µm</td>
<td>Exp</td>
<td>[500*,501]</td>
</tr>
<tr>
<td></td>
<td>8 µm</td>
<td>Exp</td>
<td>[502]</td>
</tr>
<tr>
<td>CO</td>
<td>2.3 µm</td>
<td>Exp &amp; Calc</td>
<td>[238,332*]</td>
</tr>
<tr>
<td></td>
<td>1.6 µm</td>
<td>Exp</td>
<td>[477*,478*]</td>
</tr>
<tr>
<td></td>
<td>Exp</td>
<td>[10]</td>
<td></td>
</tr>
<tr>
<td>CO$_2$</td>
<td>All in HITRAN</td>
<td>Calc</td>
<td>[509*,311*,314*]</td>
</tr>
<tr>
<td></td>
<td>3 µm</td>
<td>Exp &amp; Calc</td>
<td>[313*]</td>
</tr>
<tr>
<td></td>
<td>1.6 µm</td>
<td>Exp</td>
<td>[304,305,308*,457*,460,506,507]</td>
</tr>
<tr>
<td></td>
<td>2.05 µm</td>
<td>Exp</td>
<td>[304,305,307*,308*]</td>
</tr>
<tr>
<td></td>
<td>2.3 µm</td>
<td>Exp &amp; Calc</td>
<td>[508,466*]</td>
</tr>
<tr>
<td></td>
<td>4.3 µm</td>
<td>Exp</td>
<td>[315]</td>
</tr>
<tr>
<td></td>
<td>Exp</td>
<td>[103*]</td>
<td></td>
</tr>
<tr>
<td>N$_2$O</td>
<td>4.5 µm</td>
<td>Exp</td>
<td>[470]</td>
</tr>
<tr>
<td>HCN</td>
<td>14 µm</td>
<td>Exp</td>
<td>[509]</td>
</tr>
<tr>
<td>HDO</td>
<td>2.7 µm</td>
<td>Exp</td>
<td>[286*]</td>
</tr>
<tr>
<td></td>
<td>3.6 µm</td>
<td>Exp</td>
<td>[285*]</td>
</tr>
<tr>
<td></td>
<td>7.4 µm</td>
<td>Exp</td>
<td>[281*]</td>
</tr>
<tr>
<td>H$_2$O</td>
<td>Some doublets</td>
<td>Exp</td>
<td>[510*,511]</td>
</tr>
<tr>
<td></td>
<td>2.5-2.9 µm</td>
<td>Exp</td>
<td>[282*]</td>
</tr>
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<td></td>
<td>2.5-5.4 µm</td>
<td>Exp</td>
<td>[440*,447]</td>
</tr>
<tr>
<td>NH$_3$</td>
<td>3 µm</td>
<td>Calc</td>
<td>[231,299,300]</td>
</tr>
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<td>N$_2$O</td>
<td>3 µm</td>
<td>Calc</td>
<td>[228,229,237].</td>
</tr>
<tr>
<td>O$_2$</td>
<td>0.76 µm</td>
<td>Calc</td>
<td>[318*,306,245]</td>
</tr>
<tr>
<td></td>
<td>118 GHz</td>
<td>Exp</td>
<td>[100*,494,245,306]</td>
</tr>
<tr>
<td>PH$_3$</td>
<td>4.5 µm</td>
<td>Exp</td>
<td>[512*,488]</td>
</tr>
</tbody>
</table>

Table 4: Bibliography providing data in order to describe line-mixing effects. The references marked with an asterisk (eg [254*]) are those in which LM parameters were investigated at various temperatures.

4.3 Far wings and associated continua

This section reviews the data available for the modeling of the continuum-like absorptions to which the far line wings make a significant contribution (the CIA continua due
to the dipole induced during collisions are the subject of Sec. 4.4). It completes the information given in Tables IV.5 and IV.6, as well as in Appendix V.A of [1], by providing references of studies for H$_2$O and CO$_2$ (which are, to our knowledge, the only species for which new values have been made available in the last decade).

4.3.1 The water-vapor continua

More than one century after its discovery (cf [513,514] and the review in [357]), the strength and physical origin of the absorption continua of water vapor remain an open question. In particular, the question of the respective contributions of the monomer line wings, of the stable and metastable dimers and of collision-induced absorption is not yet settled, as discussed in appendix V.A of [1] and in [391,427,515-521]. On this issue, note that water dimers have been recently found to contribute to the continuum in the 14-35 cm$^{-1}$ wave number region [522]. Partly resolved absorption features due to water dimers have also been identified in room-temperature spectra in the millimeter-wave range [523], the water dimer relative abundance being on the order of $10^3$ at room temperature and 1.7 kPa.

A better characterization of the amplitude and temperature-dependence of the continuum is needed because of its contribution to the radiative budget of the Earth and thus to climate change through feedback effects [524-528] as well as its influence on the estimated extensions of the habitable zone of stars [529-531] (see also Sec. 5.3). Before describing recent results on the water-vapor continua, recall that they are generally divided into the so-called self-continuum for pure H$_2$O and the foreign continuum when H$_2$O is mixed with another gas (generally N$_2$ or air).

4.3.1a The self-continuum

Table 5 presents a review of (recent) measurements of the self-continuum, which is believed to be mostly exhaustive above (and including) the 10 $\mu$m window (readers are invited to consult [357,370] for longer wavelengths). Recall that, because of the weakness of the broadband absorptions to be measured, high sensitivity methods and/or long paths must be used. We have thus separated, in Table 5, the studies using long (multipass) cells and covering large spectral intervals mostly with FTS instruments from laser-based methods probing narrow spectral intervals. The main recent FTS studies were carried out by the CAVIAR consortium [373,532] with a 512.7 m path length at 293 K in England, with a 612 m path length at room temperature in Russia (Tomsk) and with a 100 m path length ($T= 311$ K to 363 K) in the USA (NIST). Concerning laser-based methods, they have been used in the water-vapor transparency windows because of their inherent higher sensitivity. They include calorimetric-interferometry and cavity-enhanced methods (cf Sec. 2) such as CRDS and OF-CEAS.

### Long path cell methods

<table>
<thead>
<tr>
<th>Spectral range (cm$^{-1}$)</th>
<th>Technique</th>
<th>Path length (m)</th>
<th>T (K)</th>
<th>Refs.</th>
</tr>
</thead>
<tbody>
<tr>
<td>10-90</td>
<td>Interferometric spectrometer</td>
<td>23.3</td>
<td>293-333</td>
<td>[533]</td>
</tr>
<tr>
<td>14-200</td>
<td>FTS</td>
<td>151.75</td>
<td>296</td>
<td>[522]</td>
</tr>
<tr>
<td>800-1250</td>
<td>FTS</td>
<td>68-116</td>
<td>326, 339, 352, 363</td>
<td>[370]</td>
</tr>
<tr>
<td>800-1250</td>
<td>FTS</td>
<td>100</td>
<td>311, 326, 352</td>
<td>[387]</td>
</tr>
<tr>
<td>2400-2640</td>
<td>Spectrograph</td>
<td>707</td>
<td>296-428</td>
<td>[363]</td>
</tr>
<tr>
<td>1900-3500</td>
<td>FTS</td>
<td>100</td>
<td>311-363</td>
<td>[384]</td>
</tr>
<tr>
<td>1900-2600 and 3900-4600</td>
<td>Spectrograph</td>
<td>0.0529</td>
<td>500-875</td>
<td>[534]</td>
</tr>
<tr>
<td>1200-8000</td>
<td>FTS</td>
<td>128 and 512</td>
<td>296-351</td>
<td>[518,535]</td>
</tr>
<tr>
<td>2500-10000</td>
<td>FTS</td>
<td>512.7, 17.7</td>
<td>293</td>
<td>350-472</td>
</tr>
</tbody>
</table>
The measured values of the self-continuum absorption cross-sections between wave numbers of 1500 cm⁻¹ and 10500 cm⁻¹ are compared to the last version (V3.0) of the MT_CKD model in Fig. 15 (Sec. 3.5.4). A striking fact is the strong disagreement (up to two orders of magnitude near 6200 cm⁻¹) between the FTS and laser-based methods in the transparency windows. Furthermore, the Tomsk and CAVIAR values are almost constant throughout the 1.6 µm, 2.1 µm and 4.0 µm wavelength regions, with a value (about 4×10⁻²³ cm² molec⁻¹ atm⁻¹) largely above the MT_CKD predictions. Conversely, the OF-CEAS and CRDS measurements follow the general MT_CKD3.0 evolution with frequency, exhibiting very good agreement in the 1.6 µm and 1.25 µm windows but deviations by factors from 2 to 5 at the center of the 2.1 µm and 4.0 µm windows. Detailed discussion of this puzzling situation can be found in [380,537]. Note that during the derivation of the absorption cross section from OF-CEAS and CRDS spectra, the pressure-squared dependence of the self-continuum was systematically checked to insure the gas phase origin of the measured losses. Except for [384], all other FTS determinations near room temperature rely on spectra recorded for a single pressure.

The evolution of the self continuum near and below room temperature is obviously an important issue in studies of the atmosphere of the Earth, but it is difficult to measure because of the limitation imposed by the saturation pressure. Thus, the use of high temperatures makes the determinations easier. From this point of view, the most complete studies (cf Table 5) were performed at NIST between 311 K and 363 K [370,384,387] and by the CAVIAR consortium [373] in the 350 K to 472 K range. Interestingly, in the 4.0 µm and 2.1 µm wavelength windows, these high temperature measurements are consistent with room temperature results by OF-CEAS and CRDS [380,381], as shown in Fig. 18. In addition, as

<table>
<thead>
<tr>
<th>Measurement points (cm⁻¹)</th>
<th>Technique</th>
<th>Laser source</th>
<th>T (K)</th>
<th>Refs.</th>
</tr>
</thead>
<tbody>
<tr>
<td>931, 944, 969</td>
<td>CRDS</td>
<td>CO₂</td>
<td>294-297</td>
<td>[364]</td>
</tr>
<tr>
<td>944</td>
<td>CRDS</td>
<td>CO₂</td>
<td>270-315</td>
<td>[369]</td>
</tr>
<tr>
<td>2283</td>
<td>OF-CEAS</td>
<td>QCL</td>
<td>296, 301, 312</td>
<td>[380]</td>
</tr>
<tr>
<td>2491</td>
<td>OF-CEAS</td>
<td>ICL</td>
<td>297, 312, 325</td>
<td>[381]</td>
</tr>
<tr>
<td>4249-4257</td>
<td>CRDS</td>
<td>DFBL</td>
<td>298</td>
<td>[379]</td>
</tr>
<tr>
<td>4301</td>
<td>CRDS</td>
<td>DFBL</td>
<td>297-323</td>
<td>[378]</td>
</tr>
<tr>
<td>4341-4367</td>
<td>CRDS</td>
<td>VECSEL</td>
<td>297</td>
<td>[380]</td>
</tr>
<tr>
<td>4427-4441</td>
<td>CRDS</td>
<td>DFBL</td>
<td>296.2</td>
<td>[381]</td>
</tr>
<tr>
<td>4516-4532</td>
<td>CRDS</td>
<td>DFBL</td>
<td>297</td>
<td>[380]</td>
</tr>
<tr>
<td>4605</td>
<td>Calorimetric interferometry in air</td>
<td>Raman-shifted alexandrite</td>
<td>298</td>
<td>[382]</td>
</tr>
<tr>
<td>4723</td>
<td>OF-CEAS</td>
<td>DFBL</td>
<td>298-323</td>
<td>[382]</td>
</tr>
<tr>
<td>5875-6665 (10 pts)</td>
<td>CRDS</td>
<td>DFBL</td>
<td>302-340</td>
<td>[376,377]</td>
</tr>
<tr>
<td>6112-6165</td>
<td>Calorimetric interferometry in air</td>
<td>Raman-shifted alexandrite</td>
<td>298</td>
<td>[382]</td>
</tr>
<tr>
<td>7500-7920</td>
<td>CRDS</td>
<td>DFBL</td>
<td>297</td>
<td>[380]</td>
</tr>
<tr>
<td>7920-8300</td>
<td>CRDS</td>
<td>ECDL</td>
<td>297</td>
<td>[380]</td>
</tr>
<tr>
<td>9466</td>
<td>Calorimetric interferometry in N₂</td>
<td>Nd:glass</td>
<td>303</td>
<td>[383]</td>
</tr>
<tr>
<td>11495</td>
<td>Pulsed CRDS (upper limit in air)</td>
<td>Dye laser</td>
<td>295</td>
<td>[536]</td>
</tr>
</tbody>
</table>

noted in [378,381], the measured values, including the earlier results of [363] (up to 428 K) and of [534] (up to 875 K), nicely follow a \( \exp\left[-D_0/(k_B T)\right] \) law with a \( D_0 \) value close to the dissociation energy of the water dimer (1100 cm\(^{-1}\) [538]). However, as discussed in [378], the interpretation of this experimental result as an evidence of the dimer origin of the water continuum in the considered windows, seems hazardous in absence of a theoretical support. Indeed, theoretical calculations based on the far wings theory yield a \( D_0 \) value of 1800 K near 944 cm\(^{-1}\) [516], which is close to that of 1842 K retrieved from measurements between 270 K to 315 K [369] and to those of 1870 K, 1705 K, and 1680 K obtained with three CO\(_2\)-laser lines between 276 K and 366 K [368]. More generally, as mentioned at the very beginning of Sec. 4.3.1, the relative contribution of dimers and far wings of the monomer lines to the continuum is still an opened question. Finally note that Fig. 18 shows that the MT_CKD model predicts stronger temperature dependences, and that [373] provides other comparisons of this model with measurements at various temperatures.

Fig. 18: Temperature dependence of the water vapor self-continuum cross-sections near 2490 and 4301 cm\(^{-1}\) obtained by FTS (green squares from [373]; orange diamonds from [384]; black star and squares from [374] and [375], respectively), using a grating spectrograph (blue diamonds from [385] and [362], red full stars from [534]) and OF-CEAS (open red stars from [379] and open red squares from [378]). The MT_CKD3.0 values (grey line) which are normalized to the number density at 1 atm and 296 K have been multiplied by the factor 296/T. The \( D_0 \) slope (black line) corresponds to an \( \exp(-D_0/k_B T) \), \( D_0 \approx 1100 \text{ cm}^{-1} \) being the dissociation energy of the water dimer molecule [538].

### 4.3.1b The foreign-continua

In our atmosphere, the air-continuum contribution to the absorption can be of the same order as the self-continuum contribution [379] and it represents a major source of uncertainty in Earth atmospheric radiative transfer models [386]. The analysis of atmospheric spectra thus provides valuable constraints to validate the continuum amplitude and its temperature dependence, in particular for the infrared and microwave regions. Nevertheless, the retrieval of water-vapor continuum absorption from atmospheric spectra is challenging due to the difficulty in discriminating it from aerosol scattering and absorption. Recent atmospheric validation in the infrared can be found in [539-543].

Table 6 regroups the few recent laboratory studies of the foreign continuum associated with mixtures of H\(_2\)O with N\(_2\) (or air). The concordant experimental results obtained at NIST
[387,388], by the CAVIAR consortium [386] and by CRDS in the 2.1 µm window [379] have led to a significant increase of the MT_CKD foreign-continuum model in the transparency windows. Note that the foreign-continuum has been found to be mostly independent of temperature in the broad-band CAVIAR FTS measurements between 350 K and 430 K [386]. Similar results were reported in the infrared between 296 K and 363 K [387,388]. Finally, the review of [544] concludes that the laboratory and field measurements of the continuum absorption coefficients at 183 GHz, do not exhibit a temperature dependence in the 260-360 K range.

### Long path cell methods

<table>
<thead>
<tr>
<th>Spectral range (cm⁻¹)</th>
<th>Technique</th>
<th>Path length (m)</th>
<th>Foreign gas</th>
<th>T (K)</th>
<th>Refs.</th>
</tr>
</thead>
<tbody>
<tr>
<td>1000-2500</td>
<td>FTS</td>
<td>100</td>
<td>N₂</td>
<td>296, 326</td>
<td>[387]</td>
</tr>
<tr>
<td>2000-3230</td>
<td>FTS</td>
<td>100</td>
<td>N₂</td>
<td>326, 339, 352, 363</td>
<td>[388]</td>
</tr>
<tr>
<td>2000-10000</td>
<td>FTS</td>
<td>17.7</td>
<td>air</td>
<td>350, 372, 402, 431</td>
<td>[386]</td>
</tr>
</tbody>
</table>

### Laser-based methods

<table>
<thead>
<tr>
<th>Spectral range (cm⁻¹)</th>
<th>Technique</th>
<th>Path length (m)</th>
<th>Foreign gas</th>
<th>T (K)</th>
<th>Refs.</th>
</tr>
</thead>
<tbody>
<tr>
<td>3.5-4.7</td>
<td>BWO</td>
<td>0.35-0.7</td>
<td>N₂</td>
<td>261-328</td>
<td>[545]</td>
</tr>
<tr>
<td>4249-4257</td>
<td>CRDS</td>
<td>DFBL</td>
<td>air</td>
<td>298</td>
<td>[379]</td>
</tr>
<tr>
<td>10611 and 10685</td>
<td>CRDS</td>
<td>ECDL</td>
<td>N₂</td>
<td>278 and 296</td>
<td>[546]</td>
</tr>
<tr>
<td>14397-14401</td>
<td>Photoacoustic</td>
<td>single-pulse ruby laser</td>
<td>N₂</td>
<td>295</td>
<td>[547]</td>
</tr>
</tbody>
</table>


### 4.3.2 The CO₂ far-wings continua

As for the H₂O continua, the far wings continua of CO₂ play a major role in radiative transfer exchanges in planetary atmospheres (eg Sec. 5.3.3). In Table 7 are given several mostly recent studies in which the far-wings continua of CO₂ have been determined from experiments. These involve different spectral regions and temperatures and were carried for pure CO₂ and/or various mixtures including N₂ and H₂O. Note that some of the references also provide empirical models.

<table>
<thead>
<tr>
<th>Spectral range (cm⁻¹)</th>
<th>Technique</th>
<th>P range (atm)</th>
<th>T range (K)</th>
<th>Path length (m)</th>
<th>Refs.</th>
</tr>
</thead>
<tbody>
<tr>
<td>800-30000</td>
<td>FTS</td>
<td>0-200</td>
<td>296-650</td>
<td>0.02</td>
<td>[548]</td>
</tr>
<tr>
<td>2750-6000</td>
<td>FTS</td>
<td>3-57</td>
<td>298-550</td>
<td>2.00-2.15</td>
<td>[311]</td>
</tr>
<tr>
<td>2380-2460</td>
<td>FTS</td>
<td>1</td>
<td>230-296</td>
<td>20</td>
<td>[355]</td>
</tr>
<tr>
<td>2400-2600</td>
<td>FTS</td>
<td>1-3</td>
<td>295-339</td>
<td>100</td>
<td>[549]</td>
</tr>
<tr>
<td>2500-2600</td>
<td>FTS</td>
<td>0-1</td>
<td>325-366</td>
<td>7.2</td>
<td>[356]</td>
</tr>
<tr>
<td>3900-4600</td>
<td>FTS</td>
<td>1-22</td>
<td>297</td>
<td>120</td>
<td>[550]</td>
</tr>
<tr>
<td>3900-4600</td>
<td>grating</td>
<td>15-20</td>
<td>290-293</td>
<td>32-482</td>
<td>[550]</td>
</tr>
<tr>
<td>3750-3900</td>
<td>FTS</td>
<td>10-40</td>
<td>299-301</td>
<td>3</td>
<td>[551]</td>
</tr>
<tr>
<td>3750-3850</td>
<td>grating</td>
<td>10-60</td>
<td>292</td>
<td>0.07</td>
<td>[552]</td>
</tr>
<tr>
<td>4320-4380</td>
<td>CRDS</td>
<td>0.3-1</td>
<td>296</td>
<td></td>
<td>[553]</td>
</tr>
<tr>
<td>5850-5960</td>
<td>CRDS</td>
<td>0-8.4</td>
<td>296</td>
<td></td>
<td>[554]</td>
</tr>
<tr>
<td>5693-5795</td>
<td>CRDS</td>
<td>0-10</td>
<td>296</td>
<td></td>
<td>[555]</td>
</tr>
<tr>
<td>8448-8482</td>
<td>CRDS</td>
<td>0-40</td>
<td>293</td>
<td></td>
<td>[556]</td>
</tr>
</tbody>
</table>

Table 7: Recent laboratory studies of far wings continua of CO₂.
4.4 Collision-induced absorption

Several relatively recent references, in which CIA data obtained from measurements and/or calculations are presented, are regrouped in Table 8. In addition to those given below, other older studies can be found by consulting [389,432,433] and Sec. 3.6.

<table>
<thead>
<tr>
<th>System</th>
<th>Region</th>
<th>T (K)</th>
<th>Techn</th>
<th>Refs.</th>
</tr>
</thead>
<tbody>
<tr>
<td>CH₂-CH₄</td>
<td>0-700 cm⁻¹</td>
<td>126-295</td>
<td>Meas</td>
<td>[411]</td>
</tr>
<tr>
<td>CO₂-CO₂</td>
<td>3000 cm⁻¹</td>
<td>300-650</td>
<td>Meas</td>
<td>[309,555]</td>
</tr>
<tr>
<td></td>
<td>300-650</td>
<td>Meas</td>
<td>[548,556]</td>
<td></td>
</tr>
<tr>
<td>CO₂-CO₂</td>
<td>Fermi diad</td>
<td>300</td>
<td>Meas</td>
<td>[557]</td>
</tr>
<tr>
<td>CO₂-(Ar,Xe)</td>
<td>0-250 cm⁻¹</td>
<td>241-351</td>
<td>Calc</td>
<td>[414]</td>
</tr>
<tr>
<td>CF₄-He</td>
<td>0-400 cm⁻¹</td>
<td>213</td>
<td>Calc</td>
<td>[410]</td>
</tr>
<tr>
<td>D₂-D₂</td>
<td>0-7000 cm⁻¹</td>
<td>200-600</td>
<td>Calc</td>
<td>[405]</td>
</tr>
<tr>
<td>D₂-He</td>
<td>0-20000 cm⁻¹</td>
<td>150-9000</td>
<td>Calc</td>
<td>[406,407]</td>
</tr>
<tr>
<td>D₂-Kr</td>
<td>Fundamental</td>
<td>298</td>
<td>Meas</td>
<td>[558]</td>
</tr>
<tr>
<td>HD-HD</td>
<td>2.3 μm</td>
<td>297.5</td>
<td>Meas</td>
<td>[559]</td>
</tr>
<tr>
<td>H₂-H₂</td>
<td>1800-2400 cm⁻¹</td>
<td>77.5, 297</td>
<td>Calc</td>
<td>[401]</td>
</tr>
<tr>
<td>H₂-H₂</td>
<td>0-1000 cm⁻¹</td>
<td>77-292</td>
<td>Calc</td>
<td>[392]</td>
</tr>
<tr>
<td>H₂-H₂</td>
<td>First overtone</td>
<td>296</td>
<td>Meas</td>
<td>[560]</td>
</tr>
<tr>
<td>H₂-H₂</td>
<td>Second overtone</td>
<td>77</td>
<td>Meas</td>
<td>[561]</td>
</tr>
<tr>
<td>H₂-H₂</td>
<td>0-15000 cm⁻¹</td>
<td>300-3000</td>
<td>Calc</td>
<td>[402,403]</td>
</tr>
<tr>
<td>H₂-He</td>
<td>0-20000 cm⁻¹</td>
<td>300-9000</td>
<td>Calc</td>
<td>[404,407]</td>
</tr>
<tr>
<td>H₂O-H₂O</td>
<td>0-500 cm⁻¹</td>
<td>240-330</td>
<td>Calc</td>
<td>[427]</td>
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<tr>
<td>N₂-N₂</td>
<td>0-300 cm⁻¹</td>
<td>78-300</td>
<td>Calc</td>
<td>[394]</td>
</tr>
<tr>
<td>N₂-N₂</td>
<td>0-300 cm⁻¹</td>
<td>228</td>
<td>Calc</td>
<td>[412]</td>
</tr>
<tr>
<td>N₂-N₂</td>
<td>2-0 band</td>
<td>200-300</td>
<td>Meas/Calc</td>
<td>[417]</td>
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<tr>
<td>N₂-H₂O</td>
<td>N₂ fundamental</td>
<td>326,363</td>
<td>Meas/Calc</td>
<td>[418]</td>
</tr>
<tr>
<td>O₂-O₂</td>
<td>0-400 cm⁻¹</td>
<td>300</td>
<td>Calc</td>
<td>[413]</td>
</tr>
<tr>
<td>O₂-N₂</td>
<td>760 nm</td>
<td>200-300</td>
<td>Meas</td>
<td>[317]</td>
</tr>
<tr>
<td></td>
<td></td>
<td>300</td>
<td>Meas</td>
<td>[317]</td>
</tr>
<tr>
<td></td>
<td></td>
<td>200-300</td>
<td>Meas</td>
<td>[317]</td>
</tr>
<tr>
<td></td>
<td></td>
<td>300</td>
<td>Meas</td>
<td>[339]</td>
</tr>
<tr>
<td></td>
<td></td>
<td>300</td>
<td>Meas</td>
<td>[100,494]</td>
</tr>
<tr>
<td></td>
<td></td>
<td>300</td>
<td>Meas</td>
<td>[562]</td>
</tr>
<tr>
<td>O₂-air</td>
<td>760 nm</td>
<td>300</td>
<td>Calc</td>
<td>[396]</td>
</tr>
<tr>
<td>O₂-CO₂</td>
<td>1270 nm</td>
<td>300</td>
<td>Calc</td>
<td>[396]</td>
</tr>
<tr>
<td>O₂-N₂</td>
<td>B band (670 nm)</td>
<td>300</td>
<td>Meas</td>
<td>[563]</td>
</tr>
<tr>
<td>O₂-(O₃,N₂)</td>
<td>922 nm</td>
<td>200-300</td>
<td>Meas</td>
<td>[564]</td>
</tr>
<tr>
<td>O₂-O₂</td>
<td>340-630 nm</td>
<td>203-295</td>
<td>Meas</td>
<td>[565]</td>
</tr>
<tr>
<td>O₂-O₂</td>
<td>20400-21500 cm⁻¹</td>
<td>184-294</td>
<td>Meas</td>
<td>[566]</td>
</tr>
<tr>
<td>O₂-N₂</td>
<td>1400-1900 cm⁻¹</td>
<td>89</td>
<td>Meas</td>
<td>[567]</td>
</tr>
<tr>
<td>O₂-Ar</td>
<td>1400-1900 cm⁻¹</td>
<td>89</td>
<td>Meas</td>
<td>[567]</td>
</tr>
<tr>
<td>T₂-He</td>
<td>0-20000 cm⁻¹</td>
<td>150-9000</td>
<td>Calc</td>
<td>[407]</td>
</tr>
</tbody>
</table>

Table 8: Recent bibliography providing data on collision-induced absorption.

4.5 Spectroscopic databases

Since their creation almost fifty years ago, the (most) widely used spectroscopic databases HITRAN [430] and GEISA [431] have evolved constantly. However, until relatively recently, the provided line-shape information was quite limited and suitable only for calculations using the VP. As discussed below, significant advances have been made in the last decade to provide data for calculations under more general conditions.

4.5.1 The HITRAN database
For many decades, the HITRAN spectroscopic database [430] included only the air- and self-broadening coefficients at 296 K. The temperature dependences of air-broadened half-widths and the air pressure-induced shifts (at 296 K) were added later. It was not until the 2012 edition [429] that some non-Voigt profile parameters were tabulated (SDVP parameters for the first overtone of CO and GP parameters for HF, HCl and the O$_2$ A-band). A breakthrough in the ability to seamlessly provide non-Voigt line-shape parameters, as well as LM (so far in the first-order parameterization [344]) and pressure-broadening and -shifting coefficients by planetary gases, came with changing the database from static ASCII files to a relational database [568]. The structure of interconnected tables (corresponding to every parameter and set of quantum numbers) enables the introduction of unlimited numbers of parameters and to query these quantities in a user-defined fashion and order. In order to ease this querying process, an online interface, called HITRANonline [439], was recently developed [569].

Since the HTP (cf Sec. 3.2.4a) was recommended [179] as a reference line-shape that is more and more frequently used in fits of measured spectra, an effort is underway to store its parameters (and thus also those of more simple profiles which are particular cases of the HTP) in HITRAN. A detailed description of how this is done is given in [153] where the H$_2$ molecule was taken as a test case. Thanks to numerous measurements of the electric quadrupole lines of pure hydrogen, a complete dataset was obtained for every transition. Not only were all the HTP parameters accommodated but they were divided into different temperature domains. It is important to note that although the HTP can be reduced to several other models [169], it cannot replace all the profiles (eg GP) that already exist in the database. In addition, because every line in HITRAN retains a Lorentzian pressure-broadening coefficient which is traditionally determined and used with the VP, these parameters remain available. This result is important to remember since the half-widths values generally differ when extracted from measurements by fits with different line profiles (see below). Indeed, because it will take a long time before all radiative transfer codes are upgraded to use non-Voigt profiles, there is a danger of errors being introduced by applying the widths determined with a sophisticated line shape to the VP.

The top panel of Fig. 19 exemplifies the output format created to retrieve air-broadened SDVP parameters together with first-order LM coefficients (along with the line positions, and "usual" Lorentz-broadening coefficient derived with the VP). Here a tab-delimited output was chosen (for better visualization) and the available possibility to display the uncertainties was not used. The bottom panel of Fig. 19 shows the corresponding output for the first overtone of $^{12}$C$^{16}$O [477,478]. One can see that the air-broadening coefficients (at 296 K) for the VP ($\gamma_{\text{air}}$) are available for every line, unlike the SDVP parameters ($\gamma_{\text{SDV,air}}^0$ and $\gamma_{\text{SDV,air}}^2$). It is also clear that the values ($\gamma_{\text{air}}$ and $\gamma_{\text{SDV,air}}^0$) determined with different line-shapes (here VP and SDVP) are not identical.
In order to aid users in applications of non-Voigt line shapes, special libraries for the HITRAN Application Programming Interface (HAPI) [570] were created. As explained in [570], HAPI can download data from HITRANonline [439] with the option of retrieving all line-shape parameters, specific ones, or bundles of parameters (e.g., all those corresponding to a specific line shape). One can also employ the provided functions to calculate absorption cross-sections using any line-profile data available in the database. It is also possible to use a priority scheme whereby the program will first check whether the HTP parameters are available, then for the SDVP, and finally for the VP parameters. In this manner, one can run a calculation in which the best available profile is selected for every transition.

As detailed in [430], the HITRAN2016 edition provides parameters of the HTP for some transitions of H$_2$O, N$_2$O, O$_2$ (B-band) and H$_2$, of the SDVP for CO and O$_2$ (A-band), and of the GP for HF, HCl and O$_2$ (A-band). First-order line-mixing data at different temperatures have also been added in the database for some transitions of several molecules including H$_2$O, N$_2$O, CO and O$_2$. The full line-mixing (relaxation matrix approach) is provided for CO$_2$ through auxiliary program from [314] adjusted to work with the HITRAN2016 data. Another important recent development is that VP parameters caused by collisions with CO$_2$, H$_2$ and He were introduced for CO, SO$_2$, NH$_3$, HF, HCl, OCS and C$_2$H$_2$. 

![HITRANonline](https://example.com/hitranonline)
This was done for applications to planetary atmospheres and these parameters can be easily retrieved from HITRAN [439] and through HAPI. Note that HAPI also enables calculations of the absorption cross-sections for mixtures of perturbing gases. Finally recall that, in 2012, a new section providing CIA data was added to the HITRAN database [432], now being updated [433].

4.5.2 The GEISA database and 4A/OP code

As with the HITRAN database described above, GEISA [431] has included for many decades air- and self-broadening coefficients at 296 K, while the air-pressure shift and the temperature dependences of air-broadened half-widths were introduced later. Since the 2011 edition, the statistical uncertainty (precision) of these parameters has been added. Contrary to HITRAN, GEISA still only provides parameters for the VP, even in its 2015 edition [431]. This is because the choice was made to let radiative transfer codes account for other line profiles, LM and CIA. This is the case, for example, of the spectrum calculation code that builds the look-up tables feeding the 4A/OP radiative-transfer algorithm [572-574] which is developed by the research group in charge of GEISA. Using the link between GEISA and 4A/OP, a quasi-automatic chain has been developed for the validation not only of the radiative-transfer calculation but also of the spectroscopic parameters including those for the line shape [575]. This enables to carry comparisons between computed and measured spectra and to eventually point out discrepancies due to improper spectroscopic data. When it is the case, the values of the relevant parameters are, when possible, improved and changed in the database.

The current GEISA and 4A/OP package includes numerous spectrum-computation possibilities going beyond the VP. The latter have been selected for their importance in the treatment of the observations of several satellite-based instruments in which the group in charge of these tools is/was deeply involved (e.g. IASI [576], MicroCarb [577] and MERLIN [578]). They are the following: (i) LM and SDVP for CO₂ lines (including the effects of collisions with dry air and water vapor), as described in [314] but starting from the GEISA line list. (ii) LM in the O₂ A band following [318]. (iii) LM and HTP for the R(6) manifold of the 2ν₃ band of CH₄ from [9]. (iv) CIA by O₂ in the 0.76 μm [318], 1.27 μm [579] and 6.3 μm [580] regions. (v) CIA in the fundamental band of N₂ built from an improved version [581] of the tools proposed in [582]. Note that the currently implemented LM models for CO₂ and O₂ have been recently completed by the possibility to use parameters from other sources [100,466,506,507] for some bands. For CH₄, the implementation of LM for the ν₄, ν₁ and 2ν₃ bands is currently under progress, based on updates of [333,583]. Finally, for water vapor, the VP is used up to 300 cm⁻¹ away in the line wings. As a consequence, the corresponding 4A/OP water vapor continuum is not the “MT_CKD” (which uses a 25 cm⁻¹ cut-off distance and is described in Sec. 3.5.4) but something that has been refitted based on the validation tools described in [575].

5. Consequences for applications

The fact that the information contained in molecular spectra can be used to probe gases has been used for decades. The associated remote-sensing studies investigate (Sec. 5.1) a large variety of media, including planetary atmospheres and combustion environments, involving very diverse pressure and temperature conditions. In addition to these applications, advances in both experimental techniques and line-shape models have opened the possibility of using spectroscopy for some metrology purposes which require extreme accuracies (Sec. 5.2), such as the determination of the Boltzmann constant from precise measurements of the Doppler width. The success of such studies, which often requires extreme precision and
accuracy, relies on the quality of the description of the spectral shapes and constitutes a great challenge to this research field. Finally, gases participate in radiative heat exchange in various systems at different spatial scales (Sec. 5.3). It is the case in combustion engines, for instance, where gaseous emission and absorption influence the hydrodynamics and the energy fluxes to bounding solid surfaces. At much larger spatial scales, they contribute to the greenhouse effect, for instance, and the accuracy of models involving absorption by atmospheric gases affects the reliability of climate predictions. These examples show that a description of the effects of pressure, temperature and composition on molecular-gas spectra is required in a variety of other research fields tackling diverse issues. The latter being too numerous to be all considered here, we have limited ourselves to some illustrative examples (as in Chapt. VII of [1]) highlighting the practical advances achieved because of recent spectral-shape studies.

5.1 Remote sensing

5.1.1 Probing atmospheres

5.1.1a The Earth

A striking recent evolution of some Earth-observation satellite-based experiments is the considerably increased retrieval accuracy that is required for their success. This is the case, for instance, of current or upcoming missions for the study of greenhouse gases [577,578,584-587]. Indeed, reliable and scientifically worthwhile inversions of sources and sinks of CO$_2$ and CH$_4$ determined from atmospheric column amounts require spatially resolved measurement biases less than 0.1 % and 0.2 %, respectively. Enabled by highly precise forward models for O$_2$ and CO$_2$ absorption, the OCO-2 mission recently reported an unprecedented precision in the measured CO$_2$ VMR of ~0.1 %, sufficient to reveal previously unobserved regional and temporal trends in the global carbon cycle [588]. We now discuss how recent progress in the spectral-shape description (including isolated lines, LM, far wings and associated continua as well as CIA) has improved various optical soundings of the Earth atmosphere. Some general comments on the spectral-shape issue in atmospheric retrievals are made at the end of this section.

- Isolated line shapes: While it is obvious that errors in the input pressure-broadening and -shifting coefficients can generate large atmospheric-spectra fit residuals and subsequent errors in the targeted retrieved quantity, there are relatively few demonstrations of the need to go beyond the VP. The reasons for this are likely that non-Voigt effects (Sec. 3.2) are generally small and/or masked by the noise and limited spectral resolution of many observations and/or smaller than residuals caused by the incorrect accounting of other effects (such as line-mixing). Furthermore, in some retrieval methods, the molecular amount-of-substance information depends mainly on the line area, so that refined line-shape effects are generally small. This was first shown by *in situ* measurements of atmospheric H$_2$O using a balloon-borne diode-laser spectrometer [589]. A RP (hard collisions), which accounts forDicke narrowing, gave significantly better fits to the spectra, but the change in the retrieved H$_2$O VMR was only 0.15 %. More recently, the effect of the SDVP on water vapor profiles retrieved from ground-based FTIR solar-absorption spectra was investigated [590]. A better agreement with *in situ* sonde profiles was obtained than when using a purely VP. The effects of the speed-dependence of the pressure broadening was also investigated (theoretically) in the case of O$_3$ retrievals [591] from limb occultation, limb emission, and ground-based observations. The conclusion of this study is that the effect is minor (<1 %) in all three cases. Following [592], who pointed out the effects of Dicke narrowing in retrievals of HCl and HF from ground-based solar absorption FTIR spectra, a similar study was made [593] for HF only. It showed that use of the GP, rather than the VP, results in a substantial improvement in the HF fitting residuals, with smoother retrieved HF VMR profiles between 25-40 km, but differences in the total column abundances of only ~1 %. Finally, TCCON (Total Carbon
Column Observatory Network, see [594]) retrievals of atmospheric CO$_2$ VMR, which rely on column-integrated observations of the O$_2$ 'A' band at 1.27 µm, showed reduced airmass dependence and bias with a forward model for O$_2$ absorption that used the SDVP instead of the VP [595] (the airmass being defined as the ratio of the total number of molecules within the considered line of sight to that for a vertical column). Empirical corrections for these two effects were reduced by factors of 6 and 2.6, respectively.

- Line-mixing: The fact that taking LM effects into account may improve calculations and analyses of atmospheric spectra has been discussed in Sec. VII.4 of [1] and references therein. This has since been confirmed in the spectral regions used by several satellite missions for the retrieval of column amounts of CO$_2$ and CH$_4$ and the determination of surface pressure from O$_2$ absorption, as discussed below.

For the P- and R-branch manifolds of the 2$\nu_3$ band of CH$_4$ used for satellite monitoring [578,584], LM effects were investigated using laboratory spectra in [333]. This study also showed that taking LM into account leads to improved fits of TCCON atmospheric transmission spectra and to a reduced airmass dependence of the retrieved column amounts. Earlier, large fitting residuals, and retrieved CH$_4$ column abundances at noon that are 6 % larger than those at high airmasses (in the early morning and late afternoon), were obtained [596] and explained by the use of wrong line widths. Fits of laboratory spectra in the 2$\nu_3$ band using the VP were then performed [597], leading to "effective" pressure-broadening and -shifting coefficients. Although this is a crude way [333] to take LM into account, it is more convenient and can still lead to accurate column abundances, at least for pressures of 101 kPa (1 atm) and below [333]. For the SCIAMACHY satellite instrument, the changes in the widths and shifts implied a latitudinal and seasonally varying bias of 1 % in the total CH$_4$ column when using the HITRAN 2004 line list [597]. Very recent results on CH$_4$ retrievals using the 2$\nu_3$ band can be found in [598] where LM and SDVP derived from laboratory spectra are used, showing that the former is the major player in the observed improvements. Note that atmospheric CH$_4$ measurements were also made using a balloon-borne diode-laser spectrometer centered on the R(6) manifold of the $\nu_3$ band [500]. It was shown that use of LM together with a RP gave improved fits to the atmospheric spectra and caused 3 % to 7 % decreases in the retrieved CH$_4$ at 8 km to 18 km altitude (in better agreement with the in situ cryo-sampler on board the same gondola), relative to a VP without LM (but, contrary to what was done in [596], here using the "true" broadening parameters). The relative contributions of the RP versus LM to the CH$_4$ changes were not discussed. For completeness, recall a somehow similar study for the P(9) manifold of the $\nu_3$ band [599].

For CO$_2$, the importance of LM in the bands commonly used for observations from space [577,584-586] was first demonstrated in [600]. This study showed that including LM in the forward model leads to a significant reduction of the residuals in the 2.1 µm band (from up to 2% down to typically 0.5%). It also reduces the dependence of the retrieved CO$_2$ on the airmass and improves the consistency between values obtained independently from spectra in the 1.6 µm and 2.1 µm bands. That study, in which calculated LM coefficients were used, was subsequently improved by taking the speed dependence into account and using LM data obtained from fitting laboratory spectra [436,601]. [436] confirmed that, by using LM and a SDVP, the CO$_2$ spectral fitting residuals in ground-based TCCON spectra are improved and the airmass dependences of the retrieved CO$_2$ total columns are substantially reduced (from a few % down to a few 0.1%). As for the case of CH$_4$ discussed above and in [598], LM is the main factor in these improvements. Indirect consequences of LM in CO$_2$ have also been pointed out in the ground-based observations of CCl$_4$. Indeed, the total columns of this species retrieved from its $\nu_3$ band signature at 794 cm$^{-1}$ depend on the quality of the modeling of the nearby (791 cm$^{-1}$) CO$_2$ Q-branch and are on average 15 % higher when the influence of LM on the CO$_2$ absorption is disregarded in the forward model [602]. Finally, the importance
of LM for the determination of CO\textsubscript{2} amounts using the LIDAR instrument CO2LAS is discussed in [508].

For O\textsubscript{2}, the importance of LM (and CIA, see below) in the A band used for the determination of surface pressure from space [577,584-586], was first demonstrated in [318] using TCCON spectra. As for CH\textsubscript{4} and CO\textsubscript{2} (see above), both the fitting residuals and the airmass dependence of retrieved O\textsubscript{2} were reduced. This study, in which calculated LM coefficients were used, was subsequently improved by taking the speed dependence into account and using LM and CIA data obtained from theory and by fitting laboratory (CRDS and FTS) as well as atmospheric (TCCON) spectra [100].

Finally, the effects of LM on atmospheric O\textsubscript{3} retrievals were investigated [603] through simulations done for solar transmission and nadir emission. The results show that LM effects lead to systematic signatures in the fit residuals of typically ~2 % whose magnitude depend on the spectral resolution of the observation. The consequences for the retrieved total column ozone amount are quite modest, with errors of 2% in the worst situation, a result explained by the fact that O\textsubscript{3} is primarily a stratospheric gas.

- Far wings and associated continua: We have found no paper discussing the influence of far wings and associated continua on retrievals from atmospheric absorption spectra. The reason is likely that, in this case, the former only appear as a constant (that is adjusted) multiplying the transmission over the relatively narrow spectral intervals selected for the retrieval. This is not the case in atmospheric emission in which a precise modeling of the broad-band contribution to the absorption/emission in the various atmospheric layers is required even though only a narrow interval is used for analysis. This issue, which is relevant for the H\textsubscript{2}O and CO\textsubscript{2} continua only, is discussed from several remote sensing points of view in [544,604-608] and references therein.

- Collision-induced absorption: Concerning the importance of the correct modeling of CIA in remote sensing studies of the Earth atmosphere, there have been relatively few studies in the last decade. However, the need to include CIA in the O\textsubscript{2} A band for accurate retrievals of surface pressure from space was demonstrated in [318,609]. Recently, a model for the CIA in the weak 2-0 band of N\textsubscript{2} was proposed and validated using ground-based atmospheric transmission measurements [417]. It was there shown that disregarding the CIA leads to errors in the retrieved amounts of several trace gases. A quite original use of the N\textsubscript{2} CIA in the fundamental band was proposed in [610] for the determination of the pointing in limb-viewing measurements. This enables [610,611], once the pointing is known, an independent determination of the CO\textsubscript{2} vertical profile.

- Some general comments on the spectral-shape issue in atmospheric retrievals: The ACOS OCO-2 retrieval algorithm [601,612,613] for the treatment of OCO-2 [585] spectra uses a full-physics forward model that includes LM and a SDVP. This is despite the fact that the OCO-2 resolution (0.25 cm\textsuperscript{-1} at 6200 cm\textsuperscript{-1}; 0.7 cm\textsuperscript{-1} at 13100 cm\textsuperscript{-1}) is insufficient to see any difference in the residuals obtained with the VP and SDVP. However, because many of the observed CO\textsubscript{2} and O\textsubscript{2} lines are saturated, the non-Voigt line shape does change the equivalent widths of the lines, which is reflected in the retrieved column amounts. In contrast, the official TCCON retrievals [594] are performed with a VP and no LM, despite having a spectral resolution of 0.02 cm\textsuperscript{-1} and a SNR of 600 sufficient to discern the subsequent degradation in the residuals [436,598]. The resulting airmass dependence of the column amounts is corrected post-retrieval by exploiting the fact that the retrieval error in the TCCON windows caused by the neglect of LM (along with other factors that also cause airmass-dependent artifacts) is linear for small airmasses and consistent between summer and winter, as illustrated in Fig. 20.
Fig. 20: Relative differences between the CO$_2$ mole fractions retrieved from TCCON obtained when line-mixing is taken into account (XCO$_2$\textsuperscript{LM}) and disregarded (XCO$_2$) in the forward model for the strong CO$_2$ band centered at 4853 cm\textsuperscript{-1} (top panels) and the weak CO$_2$ band centered at 6220 cm\textsuperscript{-1} (lower panels). The results for summer (orange) and winter (blue) are plotted versus local time (left), solar zenith angle (middle), and airmass (i.e., the ratio of the total number of molecules within the considered line of sight to that for a vertical column, right).

Recurrent themes in the above literature survey is that line-width errors and neglect of LM lead to significant residuals in the spectral fits and errors in retrievals gases (e.g., CO$_2$, CH$_4$) requiring high precision. In retrievals that try to exploit the line shape to derive a vertical VMR profile (e.g., HCl, HF, H$_2$O), the assumed line shape is also important, but less so if the total vertical column suffices. The effects of speed dependence are more subtle than those of width errors or LM and harder to discern among the other confounding factors that can affect the shapes of atmospheric open-path absorption lines (e.g., the assumed T/P/VMR profiles, the field of view, the instrument line shape, zero-level offsets). Their effect on the retrieved gas amounts cannot be easily generalized since it depends on the measurement technique and analysis method. Consider a simple case of a DIAL LIDAR measuring at narrow and discrete wavelengths on and off the absorption line of interest. The inferred gas amount will obviously be sensitive to the values of the assumed line shape at the spectral points sounded. Even when measurements cover the entire line profile (e.g., FTS spectra, newer LIDARs (e.g., [614])) they can be analyzed in different ways. With analyses that use only the areas of the absorption lines, the inferred gas amounts are less sensitive to the line-shape details, especially when the lines are unsaturated. On the other hand, techniques that try to retrieve a vertical VMR profile from the shape of the spectral lines tend to be much more sensitive to the assumed line profiles.

Let us finally recall that, since the atmosphere on Earth involves temperatures as low as about 190 K, forward models should include a precise description of the effects of temperature on all spectral features used for retrievals. However, testing the needed information brought by theory and laboratory experiments (Sec. 4) by comparisons between computed and measured atmospheric spectra is not so easy. Indeed, except when collected in situ, the latter involve contributions from numerous atmospheric layers that are at different temperatures. This problem can be partly solved by using limb recordings for various viewing angles, since the tangent layer makes a large contribution. But this approach has its limits since, as the temperature goes down with increasing tangent height, so does the pressure and the resulting collisional effects. For ground-based measurements, in which the lower layers
generally make the largest contributions to the total absorption, a solution is to use spectra measured on warm and cold days, as in the example of Fig. 20.

5.1.1b Other planets

Spectroscopic databases such as HITRAN [430] or GEISA [431] still provide, for many absorbing molecules and lines, only the self- and air-broadened half widths (but an effort is underway [571] to complete HITRAN with parameters for other collision partners, cf Sec. 4.5). However, these parameters are rarely relevant to planetary atmospheres that involve different major gases (eg CO2 for Venus and Mars, H2 for gas giants) and/or temperature and pressure conditions that are more extreme than on Earth. Nevertheless, there has been much experimental and theoretical effort in the past decade to derive parameters appropriate to various planetary environments, resulting in significant and accessible datasets. This is particularly the case for the pressure-broadening and -shifting coefficients induced by collisions with CO2 (relevant for Mars and Venus) of various molecules including (not exhaustively) CO [615], H2O [268], HDO [278,616], HCl and DCl [617] (see also Tables 2 and 3). These data are now routinely used in the analysis of visible and infrared observations to derive the VMRs of these species and/or isotopic ratios in the atmospheres of Mars (eg [618-620]) and Venus (eg [621-623]). In particular, [624] discusses the sensitivity of the 1.38-μm absorption band of water (and the subsequent retrieved water vapor content in the atmosphere of Mars) to spectroscopic databases and CO2-broadening coefficients.

Another hot topic is the detection (and retrieval) of CH4 in the atmosphere of Mars, which has consequences for its current biological or geological activity. This molecule might be present at the parts-per-billion level and detecting it requires highly sensitive observations at high spectral resolution together with very accurate spectroscopic parameters. This has motivated several studies to derive CO2-broadening line widths and LM effects in CH4 to prepare for upcoming observations (eg [453,454,501]). Despite the low surface pressure on Mars (600 Pa on average), LM effects are visible in CH4 spectra at the spectral resolution of the NOMAD spectrometer (0.1 cm⁻¹) onboard ExoMars Trace Gas Orbiter [453] and they will be taken into account. Finally, since temperatures on Mars span the 150-290 K range, correct modeling of the effects of collisions with CO2 on individual lines and manifolds of all relevant absorbing species is needed below room temperature.

Regarding the lower atmosphere of Venus, where the pressure reaches 9 MPa and the temperature 730 K, experimental and theoretical efforts are still needed to correctly describe absorption in the far wings of CO2. Indeed, [625] evaluated several line-shape models (including a LM approach in the strong-collision approximation) that all failed to reproduce the observed CO2 absorption in the 1.10 and 1.18 μm atmospheric windows. The authors thus derived their own empirical χ-factor for the sub-Lorentzian CO2 line wings from fitting the spectra collected by the Spectroscopy for Investigation of Characteristics of the Atmosphere of Venus Infrared Red instrument (SPICAV_IR) (Fig. 21). In addition, to fit the observations, [625] and [626] also had to add an ad hoc continuum opacity, which probably results from collision-induced processes. Several recent high-pressure (but room temperature) CRDS experiments have been built to evaluate this continuum opacity and measure binary absorption coefficients in several transparency windows relevant to the atmosphere of Venus [551-554] (see also Sec. 4.4.2). In these experiments, there was also evidence of LM effects, which would have to be accounted for in future studies. As outlined in a recent review [627], additional theoretical models, predictions and experiments at high pressures but also high temperatures are needed to improve the existing databases of spectroscopic parameters for Venus conditions.
Titan, Saturn's largest satellite, has a nitrogen-dominated atmosphere (with ~5% of CH₄ and ~0.1% of H₂) with a surface pressure of 0.15 MPa. Many spectroscopic studies performed for the Earth's atmosphere are thus valid, provided that the spectral shape parameters are known (or can be extrapolated) down to below 100 K. In the near-infrared, Titan's spectrum is dominated by methane absorption (and aerosol extinction). With accurate spectroscopic methane data, it is possible to see through the veil of Titan's opaque atmosphere in several spectroscopic windows and derive properties of Titan's surface albedo [628]. Given the importance of methane, a lot of work has been made (e.g. [629]) in the past decade to complement the existing databases with line parameters. However, the analysis of ground- or space-based observations in the near-infrared is hampered by the (sub-Lorentzian) behavior of the methane line wings, which remains poorly known and plays an important role. Further work on methane line wings is clearly needed.

Regarding the atmospheres of giant planets, recent experiments have focused on measuring absorption properties of ammonia and water vapor under Jovian conditions that are found in its deep troposphere, ie in a hydrogen-helium atmosphere, up to 10 MPa and 500 K (e.g. [630,631]) or even 600K [632], in support of a microwave remote sensing instrument onboard the Juno spacecraft. Such experiments are crucial to derive microwave absorption coefficients that are then used to retrieve the abundances of these species in Jupiter's deep troposphere [633,634]. Experiments have also been conducted to characterize the effects of collisions with H₂, He as well as H₂O [630] and CH₄ [632] on the ammonia opacity in the 5 cm to 20 cm wavelength region. Based on these measurements, new models for pressure-broadened line shapes have been developed. These laboratory data and models show that broadening by water vapor has a measurable effect on the opacity of ammonia under Jovian conditions [630]. The broadening by CH₄ is found to be considerably larger than those by H₂ and He, but its effect on the microwave spectrum which will be observed by Juno is expected to be minimal, owing to methane’s relatively low abundance on Jupiter (~0.2 % by volume) [632]. However, the influence of methane broadening on the ammonia absorption spectrum is expected to be more important on Uranus and Neptune where CH₄ is of greater abundance (~2 % to 4 % by volume).

Even more extreme environments can be found in the atmospheres of exoplanets or substellar objects such as brown dwarfs. Exoplanets observed with ground-based or space-based telescopes and for which molecular signatures can be detected in their atmospheres with
current techniques are mainly “hot Jupiters” or “mini-Neptunes”, with H$_2$-rich atmospheres and temperatures in the range 500 K to 3000 K. To adapt to such high temperatures, several molecular line lists have been developed in recent years, including the HITEMP [635] and the ExoMol [636,637] databases. Both these databases provide a compilation of high-temperature line lists and line-broadening parameters for molecules such as H$_2$O, CO, CO$_2$, CH$_4$ and NH$_3$. However, the H$_2$ pressure-broadening data are insufficient despite being critical to correctly model infrared spectra of brown dwarves, hot-Jupiter or mini-Neptune planets [638]. In [638], water vapor in a H$_2$-rich exoplanetary atmosphere was used as a case study and synthetic transmittance spectra of water were computed at various spectral resolutions (from $10^2$ to $10^5$) and temperatures (500 K to 3000 K). The authors showed that neglecting pressure-broadening effects induces errors of up to 40% in calculated spectra at the medium resolution (R = 3000) representative of the future James Webb Space Telescope capabilities, with even higher errors (greater than 100%) obtained at high spectral resolution. There is thus a strong need for accurate pressure-broadening data in the case of collisions with H$_2$ up to very high temperatures. This is the topic of many recent theoretical studies. A comprehensive compilation of existing data can be found in a recent update of the ExoMol database, which to this date includes H$_2$-, He-, air- and self-broadening parameters relevant to eight molecules and high temperature (cf [637,639] and references therein).

5.1.2 Probing combustion gases
Laser techniques have been used for decades for the probing of combustion gases. A variety of gas-phase systems, which involve wide ranges of pressure, temperature and composition, have been probed for steady-state and time-resolved determinations of temperature, pressure, velocity, relative amounts of molecular species, etc. In most cases the accuracy of the retrieved results highly depends on the quality of the spectroscopic data and spectral shapes used. On this topic, the reader is invited to consult several recent reviews [640-642] and the references contained therein.

5.1.3 Probing confined gases
It was predicted many years ago that the (tight) confinement of molecular gases inside enclosures where they are free to move (and not adsorbed) induces a modification of the shapes of absorption lines through the increased contribution of molecule-surface collisions [643,644]. However, not until around 2010 did measurements clearly demonstrate these confinement effects [645-647]. These experiments showed that lines of H$_2$O vapor inside an aerogel sample [645] and of O$_2$ gas inside ceramics [647] are significantly broader than those observed for the same pressures and species under unconfined conditions. This is also shown in [648,649] and Fig. 22, where the broad feature caused by the confinement of CO gas in an aerogel sample, is more than 30 times broader than the narrow peak which is its counterpart in the free gas phase.
These findings led to the conclusion that the observed line widths of confined gases can be used to measure the size of microscopic pores [650]. The relation between broadening and confinement [644] was then confirmed by both CMDS [119,651] and experiments under well-controlled confinement conditions [652]. This established the applicability of line-width measurements to porosimetry. Indeed, it was recently shown that infrared absorption by gases within the pores of several samples gives reliable information on the percentage and dimensions of open pores [649,653]. Spectroscopy thus appears [649] as an interesting tool complementary to more commonly-used techniques such as mercury intrusion/extrusion or N₂ sorption/desorption isotherms. Note that, besides line-broadening, spectra of molecular gases within porous samples have also been analyzed from other points-of-view, including the effects of molecule-surface collisions on LM effects [334] and induced absorption [654,655]. Finally, let us mention studies [656,657] in which the absorption in the ν₃ band of CO was used to probe nano-bubbles of this gas formed at the interface between water and a hydrophobic solid.

5.2 Metrology

5.2.1 Doppler thermometry

In the last decade, significant efforts have been devoted worldwide to the determination of the Boltzmann constant (k_B) with the aim of redefining the Kelvin unit [658]. Indeed, the new SI and its implementation will be formally adopted by the end of 2018. This includes the Kelvin which will be redefined as the change of thermodynamic temperature ΔT resulting in a change of thermal energy by k_BΔT, thus implying that the Boltzmann constant should be known as accurately as possible. For this reason, several primary thermometry methods, based upon the measurement of a thermodynamic property of a macroscopic system at the temperature of the triple point of water, have been improved enormously in the last few years [659], yielding relative uncertainties in k_B at the parts-per-million level. Doppler broadening thermometry (DBT) was proposed as an optical technique [660] to determine k_B from measurement of the Doppler width Δν_D of an absorption line of a gas. Indeed, k_B and Δν_D are related by Δν_D = (ν₀/c)\sqrt{2\ln2k_BT/M} , where ν₀ is the central frequency of the line, M is the absorber (atomic or molecular) mass and T is the temperature. Inverting this equation thus leads to the determination of the thermal energy and, consequently, of either the gas temperature or the Boltzmann constant.
After the first successful experiment [661], the international community of fundamental metrology widely recognized the importance of developing an optical method that links the thermodynamic temperature to an optical frequency, to obtain an independent confirmation of the results provided by more established methods. So far, the most accurate implementation of DBT has been performed on a line of H$_2^{18}$O vapor at 1.39 $\mu$m [662]. Using the dual-laser spectrometer described in Sec. 2.8 and a sophisticated spectral analysis procedure, $k_B$ was determined with a combined uncertainty of 24 parts-per million (ppm) [663].

While the current status and new frontiers of research of DBT have been reviewed in [162], it is noteworthy that, in addition to the quality of the detection system, the line-shape model used for the spectral analysis and retrieval of $\Delta\nu_D$ from measured spectra is a key issue, as discussed in [664]. In the first determinations, the spectral analysis was performed by using either a Gaussian or a Voigt profile [62,661,665]. Subsequently, improvements of the experimental setups have been accompanied by using increasingly refined line shapes. Great attention has been paid to the roles of velocity-changing collisions and speed-dependence of relaxation rates [469,666-668]. Both effects have been accounted for in [662], in which a partially correlated speed-dependent hard-collision model [171] was used. In order to go further, a global (or multispectrum) analysis approach was then adopted for a simultaneous fit to a manifold of experimental profiles across various pressures. As explained in [669], this global analysis should reduce the uncertainty associated with the line-shape model, as well as the fluctuations resulting from statistical correlations among the adjusted parameters. Another way to reduce the uncertainty caused by the approximate modeling of collisional effects (i.e., the line-shape model) is to use a highly sensitive detection technique capable of probing samples at very low pressures. This is possible by using long-path absorption techniques or cavity-enhanced methods, as recently done in [670] where acetylene spectra near 787 nm were recorded using CRDS at pressures as low as 1.5 Pa. Nevertheless, large systematic deviations (of about 800 ppm) remained, mostly ascribed to weak hidden lines overlapping with the selected transition. Very recently, a comb-assisted highly sensitive CRDS spectrometer, operating at 1.578 $\mu$m, has been developed [671] using pure CO$_2$ as a molecular gas target since, as discussed in [162], this molecule turns out to be an excellent choice for DBT measurements. It was subsequently shown that the combination of high sensitivity, absolute frequency calibration, and extremely dense sampling of the absorption profiles leads to a statistical uncertainty of 8 ppm over a measurement time of only 5 h. Thermodynamic temperature determinations have been demonstrated by using this approach, with the spectroscopically unprecedented combined uncertainty of 14 ppm [671].

**5.2.2 Amount of gas metrology**

Linear absorption spectroscopy of isolated transitions is a versatile and potentially absolute method for measuring the gas-phase amount of a substance (cf Sec. 5.1) that can be modeled by the Beer-Lambert law. This approach is species- and isotopologue-specific (contrary to mass spectrometry), linear in concentration (assuming that saturation effects are negligible), and suitable for both inert and reactive gases. The line intensity plays the role of an intrinsic molecular standard provided this quantity and the line shape (a key issue as discussed below) are accurately known, thereby supplanting the routine need for calibration gases. Also, ratios of spectral-peak areas can be used to measure the relative abundance of isotopologues in terms of known line intensities, without the need for an arbitrary reference material as required in mass spectrometry.

Concerning the line intensity, it can be computed using *ab initio* predictions of the wave functions and dipole-moment surfaces (DMSs) (e.g. [672,673]) or it can be determined from effective DMSs and Hamiltonians that have been fitted to numerous measured values with one goal being to average over independent biases among experiments (e.g. [674]). Laboratory
measurements of line intensities are potentially more accurate than predictions and, in any case useful for assessing uncertainties. However, except for rotational transitions in the far infrared for which Stark and Zeeman measurements can be made, accurate experimental determinations of line intensities must meet several technical challenges. The first, for which possible solutions are discussed in Sec. 2, is that high-fidelity measurements of both the spectrum detuning and absorbance axes are required. The second is that the composition, pressure (or number density) and temperature of the gas sample introduced in the spectrometer must be stable and accurately known. This can be solved by using accurate and precise $P$ and $T$ sensors and certified mixtures that are commercially available for numerous gases or which can be prepared using various SI-traceable methods (eg [675-678]). For the most stable gases, mixtures with relative standard uncertainties of less than 0.1 % are generally available. Note that, particularly when $\text{H}_2\text{O}$ is involved, steady flows of humidified gas conditions are preferable over cylinder-based sources which tend to exhibit long-term drift [435,679]. Finally, to retrieve the line intensity from fits of measured spectra the normalized line profile used must be carefully chosen. The profile enables optimal exploitation of the experimental information, in addition to enabling interpolation between data points and ensuring the extrapolation necessary to account for the peak area underneath the line wings outside of the measurement domain. From this point of view it has been shown that using the VP leads to systematic and pressure-dependent errors (up to several %) on the retrieved line intensity that are usually larger than experimental uncertainties [46,188,284,435,489,680,681]. Furthermore, the fitted results are much more sensitive to the spectral range considered [435] by comparison to results obtained with higher-order line profiles. However, when using more advanced profiles involving several floated parameters (speed-dependence and/or velocity-changing frequency, etc), differences between fitted areas decrease strongly and may become as small as 0.05 % (eg [46,682,683]). Given the availability of low-uncertainty SI-traceable gas standards and the capability to measure spectra with SNRs far greater than 1000 and analyze them with advanced line-shapes, the last decade has seen the emergence of absolute line-intensity measurements with relative uncertainties approaching 0.1 % [8,60,96,683,684].

Obviously, when the line intensity is assumed known in order to determine the relative or absolute density of a given molecule (or isotopologue) from an absorption measurement, the use of an improper line shape in the fits leads to errors on the retrieved value. Discussions on this issue in the context of isotopic-ratio determinations can be found in [680,685-687]. In particular, Fig. 23 shows the measured spectra and associated fit residuals used [687] to retrieve the $\text{H}_2^{17}\text{O}/\text{H}_2^{16}\text{O}$ amount ratio. While the VP is clearly inadequate, the GP, Nelkin-Ghatak profile (NGP or RP) and SDVP lead to comparable and much smaller residuals. As for the $^{17}\text{O}/^{16}\text{O}$ ratio, that obtained with the VP is unrealistically large ($\approx$581 ppm), while the GP and SDVP provide the same results which are about 0.8 % smaller than those obtained with the NGP ($\approx$368 ppm) [687]. It should be noted that the literature on isotopic-ratio measurements by means of laser spectroscopy, as an alternative to mass spectrometry, is quite broad. An exhaustive coverage of this field would be outside the scope of the present review article, also considering that in many cases a refined line-shape model is not required [688].
Another particularly important field requiring accurate line-intensity data involves the remote sensing of greenhouse gases from satellite and terrestrial platforms. Examples include NASA’s OCO-2 satellite [577,585,588], ground-based TCCON [594] observations of O\textsubscript{2} and CO\textsubscript{2}, and the planned MERLIN satellite for measuring CH\textsubscript{4} [578]. These applications have concentration retrieval targets with uncertainties at the 0.25 % level or below and therefore motivate low-uncertainty laboratory measurements that incorporate advanced line profiles (e.g. [9,100,689] and references therein; see also Sec. 5.1.1a).

5.3 Radiative heat transfer and climate modeling

In radiative heat transfer problems, one generally wishes to predict the power locally lost or gained by the gas (e.g. in W/m\textsuperscript{3}) and the local net fluxes (e.g. in W/m\textsuperscript{2}) to solid surfaces. This is obviously relevant for industrial systems where these quantities may affect the hydrodynamics and efficiencies of combustion processes, as well as the longevity of the solid parts of the system. It is also crucial for correct predictions of climate and radiative forcing, with the example of predicting the degree to which warming of the Earth can be attributed to anthropogenic greenhouse gases. For such problems, the quantities of interest are integrated over the entire thermal emission spectrum of the medium and, eventually, also over that of an external source of radiative energy (e.g. the Sun). Because of this broad integration, the results are generally almost insensitive to refined pressure effects affecting narrow spectral intervals (e.g. the deviations from the VP in the core regions of the lines discussed in Sec. 2.2). However, this may not be the case at (very) elevated pressures for which LM can significantly change the shape of entire bands after the line structure has vanished. In addition, the far wings of lines and CIA may then play a non-negligible role, particularly when they affect the regions of relative transparency between the strongly absorbing bands.

5.3.1 Heat transfer in "industrial" devices

In systems of human scale, the path lengths and gas densities are generally too low to make far wings and CIA significant. Furthermore, when at elevated pressure, gases in industrial devices are often also at high temperature. The resulting densities are then moderate so that LM effects in the central regions of the bands remain small. These elements, and the computer-cost inherent to the use of sophisticated line-shapes, explain why radiative transfer calculations for industrial-type applications mostly use line-by-line approaches with VPs.
(eventually corrected by a $\chi$ factor in the wings), or even simpler models built from them. [690-692] present such simplified approaches and examples of their use in heat-transfer calculations can be found in papers cited therein as well as in studies among those that cite these three references.

### 5.3.2 Modeling atmospheres observed in the solar system

High pressure atmospheres are found on the giant planets Jupiter, Saturn, Uranus and Neptune ($H_2$ and $He$), Venus (9 MPa, 95 % $CO_2$) and, to some extent, Titan (0.15 MPa, 95 % $N_2$). The past ten years have seen an increased interest in the accurate numerical simulation of radiative transfer within high-pressure planetary atmospheres with the development of a new generation of Global Climate Models (GCM) for most solar system atmospheres, supported by space missions equipped with atmospheric sounders like Venus Express, Cassini (Saturn, Titan) and Juno (Jupiter).

Among the terrestrial planets, Venus remains challenging because of its high-pressure and high-temperature atmosphere. The available spectroscopic data for individual lines, complemented by the high-pressure $CO_2$ data and the $H_2O$ continuum parameterizations discussed in Sec. 4.3, have allowed the main behavior of the observed temperature profiles to be reproduced using physical models (eg [693-695]). The thermal structure is found to be primarily controlled by energy exchanges taking place in the infrared, especially in windows where the opacities are smallest, and thus not well known. Specifically, [694] showed that to model the Venustian atmosphere, uncertainties in the air opacity are crucial in two spectral regions which remain poorly known: (i) Between 20 $\mu$m and 30 $\mu$m, in the window between the 15 $\mu$m $CO_2$ band and the $CO_2$ roto-translational CIA. Light-matter interactions in these spectral regions control the temperature in the cloud convective layer (45 km to 60 km). (ii) In the infrared region, energy exchange between the deep atmosphere, the cloud base and within the deep atmosphere occurs mostly in the 3 $\mu$m to 4 $\mu$m and 5 $\mu$m to 7 $\mu$m intervals. The calculated thermal structure was also found to depend in the solar energy deposited below the clouds and thus on the assumed cloud properties, which can be adjusted. Errors in the thermal radiative transfer can be partly compensated, and it is therefore not straightforward to constrain the gaseous opacities when fitting the observed atmospheric temperatures. Nevertheless, as reported in [694] it was concluded that, when using the latest data on $CO_2$ and $H_2O$ absorption in the 3 $\mu$m to 7 $\mu$m spectral region, the opacity is not quite enough to reach the observed surface temperatures in the model when the cloud-base temperature is consistent with observations: "additional laboratory measurements of $CO_2$ absorption in the conditions of the deep atmosphere of Venus (1-10 MPa, 500 K to 750 K) are needed".

Titan is, in theory, easier to model than Venus since, like the Earth, it has a nitrogen-dominated atmosphere (with ~5 % of $CH_4$ and ~0.1 % of $H_2$) with a surface pressure of only 0.15 MPa. Except for the very low temperatures (<100 K) of the troposphere and lower stratosphere, for which measurements and/or calculations are still needed, many spectroscopic studies performed for the Earth's atmosphere are thus valid. Nevertheless, CIA plays a stronger role on Titan than on the Earth, with contributions from $N_2-N_2$, $N_2-CH_4$, $N_2-H_2$ and $CH_4-CH_4$. Nowadays the relevant data can be obtained from HITRAN [432,433], which are notably based on the relatively old studies of [696-698]. Radiative heating occurs through the absorption of visible and near-infrared light by methane and aerosols. As mentioned in section 5.1.1b, methane spectroscopy beyond 0.8 $\mu$m has been improved recently [629] but a remaining issue is related to the (sub-Lorentzian) behavior of the methane line wings, which remains poorly known. It is currently derived [628] from observations of the Titan atmosphere by the Cassini Visual and Infrared Mapping Spectrometer (VIMS) in the near infrared.
In giant-planet atmospheres, radiative cooling primarily occurs through the thermal emission of minor species (e.g., methane, ethane, acetylene) along with CIA by H₂-H₂ and H₂-He in the thermal infrared (see Sec. 5.1.1b for further details and [699] for a recent work on Saturn).

### 5.3.3 New challenges: simulating exoplanets and ancient atmospheres

More and more studies are conducted to model "new" kinds of atmospheres which are thought to have existed in the past in the solar system, or to be present on extrasolar planets. Within this context, the need for a good understanding of the effect of pressure on the spectra of gases in a wide range of conditions is stronger than ever. The number of possible cases is countless. Indeed, while the atmospheres of most extrasolar planets have not been characterized yet, it is known that the diversity of exoplanets is huge, including giant planets, mini-Neptunes, volatile rich rocky planets, in all possible ranges of temperatures (e.g. [700]). For both the ancient solar system planets and the exoplanets, there is a special interest in the modeling of the conditions that control habitability at the surface (i.e., allowing the existence of liquid-water lakes or oceans) and the limit of the "habitable zone". Such studies usually involve high-pressure atmospheres and challenging spectroscopic issues.

On strongly irradiated planets (early Venus or exoplanets near the inner edge of the habitable zone), a key concern is the greenhouse effect of warm H₂O-rich atmospheres and the uncertainties in the water-vapor continuum which controls the "runaway greenhouse effect" that defines the limit of habitability [529-531, 701].

On the opposite, in order to investigate the possible climates on weakly irradiated terrestrial planets (early Mars or exoplanets near the outer edge of the "habitable zone") most studies have focused on the radiative effect of 0.1 to 1 MPa CO₂-rich atmospheres. Interestingly, such atmospheres have been found difficult to model, and many problems have arisen. For instance, until 2010, to calculate the far infrared collision-induced opacity in a multi-bar CO₂ atmosphere, almost all published studies (e.g., [701-704]) relied without modification on a parameterization originally derived for the Venus atmosphere in [705] (see detailed description in [706]). It was based on the measurements of [707] from 7 cm⁻¹ to 250 cm⁻¹, and on a simple parameterization of collision-induced opacity in the other spectral domains described in an unpublished PhD thesis [708], still available as a NASA report. This parameterization included significant opacities between 295 cm⁻¹ and 526 cm⁻¹ actually resulting from the pressure-broadened wings of the 15 μm bands! Unfortunately, this feature was kept in subsequent models, despite the fact that these opacities were probably overestimated and, in most cases, already accounted for in the codes chosen to calculate the radiative transfer in the 15 μm band. As a result, all studies overestimated the greenhouse warming of CO₂ by several K. [709] later combined the results of [415] and [710] to propose a more up-to-date method to account for the CIA when using modern spectroscopic databases for CO₂.

More recently [711] claimed that explicitly including the effect of CO₂ collisional LM in their radiative transfer calculations yielded CO₂ atmospheres that are more transparent to infrared radiation than when spectra calculations are made using χ-corrected Lorentzian line shapes, thus generating much colder temperatures than previously estimated. However [712] later showed that this relative cooling was rather due to the wrong choice of broadening species (air instead of CO₂) and that when using properties derived for self-broadened CO₂ [311] no significant change could be noticed. Understanding why the early Martian climate could have been warm enough for liquid water to flow on the surface remains one of the major enigmas of planetary science [713] and no consensus scenario has yet been reached. The solution certainly lies in experiments for long paths and/or elevated gas pressures, capable of probing spectral regions where the (weak) absorption is proportional to the squared

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Original file: [http://www.scribd.com/doc/123456789/Accepted-Manuscript](http://www.scribd.com/doc/123456789/Accepted-Manuscript)

total density. For instance, the most promising recent theory is the study from [714] where it was suggested that methane or hydrogen could have acted as powerful greenhouse gases in the early Martian atmosphere because of CH₄-CO₂ and H₂-CO₂ CIA. In atmospheres of 50 kPa CO₂ or more, percent levels of H₂ or CH₄ were shown to raise the annual mean surface temperatures by tens of K, with temperatures reaching 273 K for pressures of 0.125 MPa to 0.2 MPa and 2% to 10% of H₂ and CH₄. Such solutions had been previously explored [715], but the CIA-induced greenhouse effect was probably underestimated because of the use of CIA data adapted for an N₂ atmosphere rather than a CO₂ atmosphere. In fact, the coefficients used by [714] remain theoretical and measurements are urgently needed. The same conclusions can be reached for many of the ongoing climate studies in planetary science. In particular, even for heavily studied molecules like CO₂ or H₂O, much remains to model the extreme environment on some exotic exoplanets [700], in protoatmospheres [716] or terrestrial atmospheres that are subject to asteroid impacts [717].

6. Remaining issues and directions for future research

This review shows that considerable progress has been made in the last decade in the determination of spectral-shape parameters from laboratory measurements. These advances, particularly significant for isolated lines, result from the unprecedented accuracy of modern experiments and the analysis of measurements with multispectrum fitting techniques using refined models. In many cases, the absorption can now be measured and represented in a broad pressure range with fit residuals of a few 0.1% or lower. At the same time, promising theoretical approaches have been proposed for the prediction of pressure effects from the intermolecular interaction potential. Together with more empirical approaches in which some parameters are adjusted, these capabilities often enable accurate descriptions of numerous mechanisms affecting the spectral shape, from individual lines to entire (allowed or collision induced) absorption bands. Despite these achievements, many issues remain, from both the experimental and theoretical points of view, in conjunction with the needs of practical applications or of our understanding of physical processes. These remaining issues are far too numerous to be all discussed here, but we below discuss some possible directions for future research.

6.1 Experiments

Despite considerable progress, current laboratory experimental set-ups remain limited for the following reasons: (i) The first is that the accessible temperatures are often limited to room temperature or, when variable, within typically 220 K to 350 K. Furthermore, when the sample temperature can be varied, the path length is generally quite limited. (ii) In addition, only sub-atmospheric pressures can often be studied. (iii) Finally, tunable-laser experiments, which provide the most accurate and sensitive measurements, are limited to relatively narrow spectral intervals and low generated-data throughputs. These limitations are generally not too constraining with regard to applications in radiative transfer and remote sensing in the atmosphere of the Earth, but this is not the case for many planetary studies. Indeed, exoplanets or early (paleo) objects in the solar system often involve high temperatures and/or pressures together with atmospheres that are extremely optically thick in the central regions of many bands. The absorption in the windows of relative transparency must then be accurately modeled and providing the relevant quantitative information may require measurements under conditions that are not yet obtainable in the laboratory. There is thus a need to develop experimental set-ups in which absorption for very large optical paths at elevated pressure and temperature can be investigated. Considering the extension of spectral ranges that can be
studied, we are relatively confident that it will broaden with the development of new laser sources and high reflectivity mirrors.

As it appears from the preceding sections, a relatively limited number of spectra have been recorded over broad temperature intervals. Consequently, the available comparisons between measurements and predictions remain often insufficient for a thorough assessment of the quality of some theories or models. For the same reason, the temperature dependence is known for relatively few of the spectral-shape parameters deduced from fits of measured spectra. We thus believe that efforts should be made both for the development of new set-ups and the use of existing ones for the investigation of pressure effects over extended temperature ranges. In doing this, as recalled at the end of Sec. 2.1, much care should be taken for the precise determination of the characteristics of the gas sample (and particularly its temperature and pressure) so that associated uncertainties do not degrade the quality of the results.

6.2 Theories and models

With regard to theories, the modified Robert-Bonamy approach, the use of molecular dynamics simulations and some recent quantum mechanical approaches for CIA are, in our opinion, the main recent advances. Their extensions to other molecular systems are obviously relevant for future studies, and their ability to describe the effects of temperature, which was seldom studied so far, must be further tested. Together with the other approaches also presented in Sec. 3, they provide a broad set of tools for predictions of the various collisional effects influencing the absorption shapes. However, although the predicted trends afforded by these models are quite good in most cases, absolute predictions (ie those achieved without adjustment of any parameter) remain significantly less reliable than laboratory measurements. In addition, they also generally do not fulfill the accuracy required by various applications. From this point of view, we are quite pessimistic regarding the question of whether theories will be able to catch up with experiments and predict spectra at the typical uncertainty of 0.1 %. However, there are two reasons why predictive theories should not be disregarded. First, for the situations where no measurements are available or feasible, theory is the only option. It is, for instance, the case of the far infrared CIA by CO$_2$+H$_2$O mixtures, needed for planetary studies (Sec. 5.3.3), which is extremely difficult (if not impossible) to measure but can be predicted by CMDS (Sec. 3.6.1). Other examples are given by spectral-shape parameters at very high temperature, which can only be obtained (eg [207,404]) from calculations. Second, theories can be used to identify and quantify the respective contributions of the physical processes involved in the spectral-shape issue under consideration. This provides a tool to develop empirical or phenomenological models, helping to identify which are the key parameters and their behaviors. For instance, calculations using the approaches described in Sec. 3.3, or fits of CMDS calculated spectra (Sec. 3.2.1) with the HTP (Sec. 3.2.4a), may provide information on how to parameterize the influence of temperature on the speed-dependence and narrowing parameters. In addition, theories can bring valuable information to help in the analysis of experiments by identifying which are the most influential processes and parameters. For instance, the modified RB formalism (Sec. 3.4.3) can indicate which lines are significantly affected by LM in order to reduce the number of unknowns in fits to measured spectra. Predictions can also be used to constrain those parameters used in sophisticated profiles that cannot be reliably fitted because of the noise on measured spectra and/or of the limited pressure range investigated, and/or because of the large numbers of known and unknown variables, as well as the poorly defined correlations among them.

6.3 Databases
The current version of the HITRAN database [430] provides parameters for the HTP (and less refined non-Voigt line-shapes) only for some transitions of a limited set of molecules, due to the relatively recent incorporation of this line shape into the analysis of experiments. As new measurements become available they will undergo thorough evaluation before inclusion into the database. In addition, only first-order (Rosenkranz) LM parameters are currently provided (except for CO₂). This is mostly because the various multi-spectrum fitting softwares employed in laboratories worldwide use slightly different formalisms when fitting LM along with correlated parameters. This situation makes it difficult to deliver consistent LM data to users. Ideally one should be able to provide codes (for instance within HAPI) for users to calculate absorption coefficients themselves from archived parameters. What constitutes the most efficient solution for this problem is still an open question under discussion in the spectroscopic and atmospheric communities. The number of planetary-relevant molecules that have broadening and shift parameters caused by collisions with CO₂, H₂ and He needs to be extended. Similarly, data for line-broadening by water vapor of some important atmospheric gases will also have to be introduced. For all these topics there is a clear need for more information concerning the effects of temperature. Furthermore, for line-mixing and some of the parameters (the speed dependence, the Dicke narrowing, etc) of refined individual line shapes, a consensus is still to be found on how to parameterize their temperature dependences. This also stands for the usual widths and shifts, for which the use of the single 296 K reference to parameterize their variations with T needs to be questioned if one wants to provide data suitable for very broad temperature ranges. Finally, note that there is an effort underway [433] to substantially update the CIA section of the database described in [432].

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