Reduction of Total Harmonic Distortion in Cascaded H-Bridge Inverter by Pattern Search Technique

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Article Info	ABSTRACT
<i>Article history:</i> Received Aug 25, 2016 Revised Sep 8, 2017 Accepted Sep 29, 2017	Pattern Search technique can be used to find the solution for the optimization problem. In this paper, pattern search algorithm has been utilized to calculate the switching angles for the cascaded H-bridge inverter with the consideration of minimizing total harmonic distortion. Mathematical equations for the optimization problem were formulated by fourier analysis technique. Lower order harmonics such as third, fifth, seventh, ninth and eleventh order harmonics were taken into account to mitigate the total harmonic distortion of the inverter. Simulations have been carried out for thirteen level, fifteen level and seventeen level cascaded H-bridge inverter using matlab software. Total harmonic distortion of voltage and current for resistive load, resistive-inductive load and motor load were analyzed.
<i>Keyword:</i> Cascaded HBridge inverter Optimization techniques Pattern search algorithm	
Switching angle Total harmonic distortion	Copyright © 2017 Institute of Advanced Engineering and Science. All rights reserved.

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1. INTRODUCTION

In developing countries, electrical power deficit is a major problem. The gap between the supply and the demand widens with the advent of new machines and devices which rely on electricity. Most of the machines used in the manufacturing sector and home appliances by the consumers like air-conditioner, refrigerator, iron boxes, heaters, etc. require power for its operation. To cope up with the demand, immense research is being carried out in the field of producing electrical power from solar energy, wind energy etc. Power produced from the renewable energies is of direct current. But electricity of alternating current type is utilized by many machines in the automation industry. Hence it is necessary to boost the direct current [1] and convert it into alternating current. When converting the d.c into a.c by the inverters, distortions were produced known as harmonics. A harmonic component in a power system is a sinusoidal component of a periodic waveform having a frequency that is an integral multiple of the fundamental frequency [2]. These harmonic components give rise to undesirable effects [3] on conductors, transformers, circuit breakers, fuses, rotating machines, telephone lines, etc. Harmonics can measured by a parameter called Total Harmonic Distortion (THD) [4]. Since THD affects the operation of machines, it is important to mitigate them.

Numerous inverters were designed by the researchers with the intention of reducing harmonics. One such inverter is the multilevel inverter. For medium and high power applications multilevel inverters are applied. Various topologies of multilevel inverters such as cascaded H-bridge inverter, diode-clamped inverter, capacitor-clamped inverter were discussed [5]. THD generated by the diode-clamped inverter and capacitor-clamped inverter is more compared to the cascaded H-bridge inverter for the same number of levels [6]. Hence cascaded H-bridge inverters were considered for analysis.

Cascaded H-bridge inverter gets the input from several dc sources and converts it into stepped ac waveform. The steps are called level. As the number of level increases, the sinusoidal waveform will be produced with reduced THD. The switching angles for the inverter have to be estimated with the aim of minimizing harmonics. Many techniques were proposed in the literature to mitigate harmonics. In [7] Newton-Raphson method was used to calculate switching angle for the multilevel inverter. The NR method is capable of finding solution only in the limited range and possibility of getting stuck at local optima. Ant colony optimization [8], Firefly algorithm [9], Bacterial Foraging algorithm [10] Frog Leaping algorithm [11], Artificial Bee Colony algorithm [12], Particle Swarm Optimization algorithm [13], Simulated Annealing [14] and Genetic algorithm [15] were applied for harmonic reduction in multilevel inverter. But the THD reduction does not comply with the IEEE standard 519. Walsh function method has been reported in [16]. Here switching angles are obtained by solving linear equations. The method fails [17] if it is required to find more angles in the same interval. The energy management system with cascaded multilevel inverter has been reported in [18]. Harmonic analysis of seven and nine level inverter were carried out in [19]. The optimization methods applied for harmonic reduction one way or the other leads to premature convergence, difficulty in finding the initial guess, THD not compliance with the IEEE 519 standard, inconsistency of the optimal solution for the varying modulation index were the major problems faced.

In this paper pattern search algorithm has been utilized to calculate the switching angle for the cascaded H-bridge inverter with the aim to minimize the total harmonic distortion. Matlab software was used to simulate the thirteen level, fifteen level and seventeen level inverter with resistive load, resistive-inductive load and motor load.

2. CASCADED H-BRIDGE INVERTER

Cascaded H-bridge inverter acquires the input from manyl DC sources and generates a stepped waveform. As the number of levels of the inverter increases, the waveform approaches sinusoid reducing the total harmonic distortion. A k-level inverter consist of (k-1)/2 H-bridges. Four switching devices are required for each bridge. Switching devices can be of IGBT, Power MOSFET, SCR etc. Here SCR has been used as a switching device. Thirteen level inverter with resistive inductive load is shown in the Figure 1. The inverter consist six H-bridges connected in series and hence it contains twenty four switches.

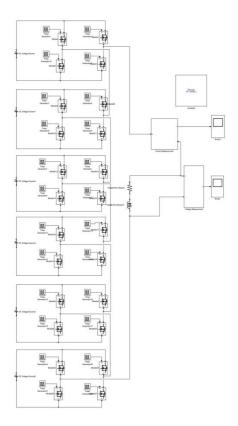


Figure 1. 13-level inverter with RL load

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Mathematical equations for minimizing the harmonics have been formulated by fourier analysis The following equation represents fundamental component, third harmonics, fifth harmonics, seventh harmonics, ninth harmonics and eleventh harmonics for the 13-level inverter Fundamental Component

$$\frac{4}{\pi\sqrt{2}} (V_1 \cos \theta_1 + V_2 \cos \theta_2 + V_3 \cos \theta_3 + V_4 \cos \theta_4 + V_5 \cos \theta_5 + V_6 \cos \theta_6) = 2303$$

Third Harmonic Equation

$$V_1\cos 3\theta_1 + V_2\cos 3\theta_2 + V_3\cos 3\theta_3 + V_4\cos 3\theta_4 + V_5\cos 3\theta_5 + V_6\cos 3\theta_6 = 0;$$

Fifth Harmonic Equation

$$V_1\cos 5\theta_1 + V_2\cos 5\theta_2 + V_3\cos 5\theta_3 + V_4\cos 5\theta_4 + V_5\cos 5\theta_5 + V_6\cos 5\theta_6 = 0;$$

Seventh Harmonic Equation

 $V_1 cos7\theta_1 + V_2 cos7\theta_2 + V_3 cos7\theta_3 + V_4 cos7\theta_4 + V_5 cos7\theta_5 + V_6 cos7\theta_6 = 0;$

Ninth Harmonic Equation

 $V_1\cos9\theta_1+V_2\cos9\theta_2+V_3\cos9\theta_3+V_4\cos9\theta_4+V_5\cos9\theta_5+V_6\cos9\theta_6=0;$

Eleventh Harmonic Equation

 $V_1 cos 11\theta_1 + V_2 cos 11\theta_2 + V_3 cos 11\theta_3 + V_4 cos 11\theta_4 + V_5 cos 11\theta_5 + V_6 cos 11\theta_6 = 0;$

Where V₁, V₂, V₃, V₄, V₅ & V₆ are the input dc voltages for six H-brdge inverters. θ_1 , θ_2 , θ_3 , θ_4 , θ_5 & θ_6 are the switching angles for six H-bridge inverters

3. PATTERN SEARCH ALGORITHM

Pattern search algorithm can be used to find the minimum of the function called objective function with constraints. It takes the objective function with the initial random values. Pattern search method performs the sequence of iterations for convergence. Once finite number of iteration is reached it switches to the lower cost function. Mesh size plays a role in setting the search along the search direction. The default value of the mesh size is one. Sometimes solution got may not be optimum. So to improve optimality of the solution mesh scaling has to be done. The number of function evaluation will be minimum with appropriate scaling, reducing the computation time. The Pattern Search algorithm [20] is given by

Let $x_0 \in \mathbb{R}^n$ and $\Delta_0 > 0$ be given. For k = 0, 1, ...,

(a) Compute $f(x_k)$.

(b) Determine a step s_k using an exploratory moves algorithm.

(c) Compute $\rho_k = f(x_k) - f(x_k + s_k)$.

(d) If $\rho_k > 0$ then $x_{k+1} = x_k + s_k$. Otherwise $x_{k+1} = x_k$.

(e) Update C_k and Δ_k .

To define a particular pattern search method, it is necessary to specify the basis matrix B, the generating matrix C_k , the exploratory moves to be used to produce a step s_k , and the algorithms for updating C_k and Δ_k . Here pattern search algorithm has been applied to determine the switching angles of the cascaded H-bridge inverter with the aim to minimize total harmonic distortion.

4. RESULTS AND DISCUSSION

The switching angles for the cascaded H-bridge inverter have been obtained by pattern search method through Matlab software. Fitness function based on fundamental component and constraint function based on harmonic components were formulated using fourier analysis simulation was done for thirteen

level, fifteen level and seventeen level inverter considering various loads such as resistive load, resistive-inductive load and motor load.

Simulation results for the cascaded H-bridge inverter with various levels with R load, RL load and motor load were shown in Figure 2, Figure 3 and Figure 4 respectively. Voltage THD and current THD with associated waveforms for 13-level inverter RL load were shown in Figure 5 and Figure 6 respectively. To investigate the consistency of the pattern search algorithm, it has been run many times and the correspond THD values are plotted in Figure 7 and Figure 8. From the results it is clear that as the level of the inverter increases THD decreases. The pattern search method of calculating the switching angles for the inverter is effective in reducing the total harmonic distortion in compliance to the IEEE 519 standard.

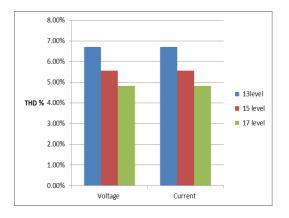


Figure 2. Comparison of voltage and current THD for 13, 15 and 17-level inverter for R load

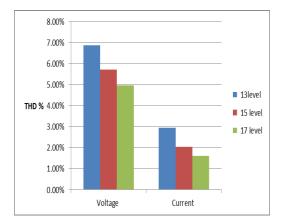
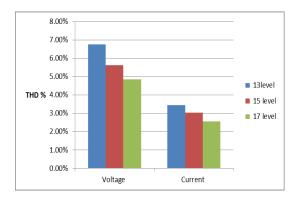
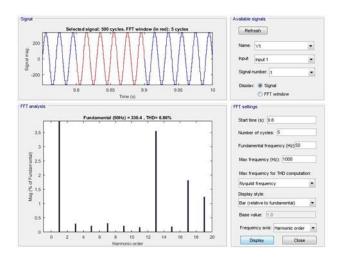


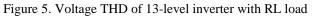
Figure 3. Comparison of voltage and current THD for 13, 15 and 17-level inverter for RL load





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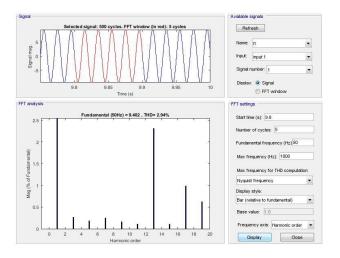


Figure 6 Current THD of 13-level inverter with RL load

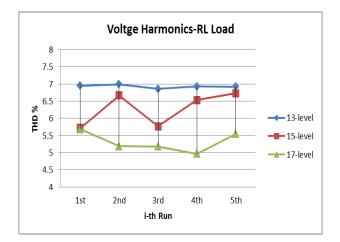


Figure 7. 13,15,17 Level inverter RL load -Voltage THD% comparison

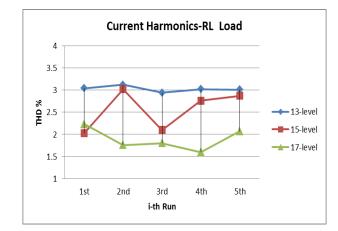


Figure 8. 13,15,17 Level inverter RL load -Current THD% comparison

5. CONCLUSION

Cascaded H-bridge inverters with thirteen level, fifteen level and seventeen level have been simulated with matlab for harmonic mitigation. The switching angles for the inverter calculated by pattern search optimization algorithm. The results conforms the effectiveness of the pattern search algorithm to find out the switching angles with the objective of THD minimization.

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