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**Regional productivity variation and the impact of public capital stock: an analysis with spatial interaction, with reference to Spain**

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# Regional productivity variation and the impact of public capital stock: an analysis with spatial interaction, with reference to Spain

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3 Abstract:  
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6 In this paper we examine whether variations in the level of public capital  
7 across Spain's Provinces affected productivity levels over the period 1996-2005. The  
8 analysis is motivated by contemporary urban economics theory, involving a  
9 production function for the competitive sector of the economy ('industry') which  
10 includes the level of composite services derived from 'service' firms under  
11 monopolistic competition. The outcome is potentially increasing returns to scale  
12 resulting from pecuniary externalities deriving from internal increasing returns in the  
13 monopolistic competition sector. We extend the production function by also making  
14 (log) labour efficiency a function of (log) total public capital stock and (log) human  
15 capital stock, leading to a simple and empirically tractable reduced form linking  
16 productivity level to density of employment, human capital and public capital stock.  
17 The model is further extended to include technological externalities or spillovers  
18 across provinces. Using panel data methodology, we find significant elasticities for  
19 total capital stock and for human capital stock, and a significant impact for  
20 employment density. The finding that the effect of public capital is significantly  
21 different from zero, indicating that it has a direct effect even after controlling for  
22 employment density, is contrary to some of the earlier research findings which leave  
23 the question of the impact of public capital unresolved.  
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Keywords: Public capital, urban economics, spatial econometrics.

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3 1. INTRODUCTION  
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7 One way that the World's current economic malaise can be addressed is  
8 by an enhanced level of investment by Governments that is focussed on the  
9 public infrastructure. Of course, the impact of such a policy needs to be  
10 evaluated in order to see whether it is cost effective. This paper contributes the  
11 literature on policy impact evaluation by examining the extent to which public  
12 infrastructure investment can potentially enhance productivity, using the  
13 recent history of investment in the Spanish regions as a guide to likely impacts  
14 elsewhere. There is no single approach to evaluating the impact of public  
15 infrastructure on productivity growth, and four main approaches have  
16 appeared in the literature, namely the cost function or dual approach,  
17 autoregressive vectors (VAR) models, frontier analysis and the production  
18 function approach. As will become evident, our approach comes closest to a  
19 production function approach, but is sufficiently different to be considered to  
20 be a fifth approach to the problem.  
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40 Under the dual approach most of the analyses show that public  
41 investment reduces entrepreneur costs<sup>1</sup>. However, evidence using VAR models  
42 is more ambiguous. For instance the papers by Flores de Frutos (1998) and  
43 Batina (1999) show a positive effect, whereas Otto and Voss (1996) and Voss  
44 (2002) find a negative impact. Application of frontier analysis to the Spanish  
45 case suggests a positive effect<sup>2</sup>. But the most frequently applied approach is  
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55 <sup>1</sup> Bosca et al (2002), Moreno et al (2002), Avilés et al (2003), and Cohen and Morrison  
56 (2004), Matmazakis (2007).

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58 <sup>2</sup> Maudos et al (1998), Martín and Suárez (2000), Pedraja et al (2002), Salinas- Jiménez  
59 (2004) and Delgado and Álvarez (2007).  
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3 based on the neoclassical production functions, commencing with Ratner's  
4 (1983) analysis of the relation between infrastructure and private productivity  
5 in the US economy. Ratner introduced public capital stock as an input in the  
6 aggregate production function, and found that it had a small but significant  
7 effect on the level of production. Subsequently Aschauer (1989a) also found a  
8 similar (albeit larger) effect, and by breaking public capital stock down into its  
9 constituent parts, he was able to show that the components with the biggest  
10 impact on productivity were transport infrastructure, energy and water  
11 supply. Subsequently, Aschauer (1989b) estimated a panel data model for  
12 seven industrialized countries, obtaining similar results under a first  
13 differences specification. However Evans and Karras (1994), again using panel  
14 data for seven countries, found that the effect of infrastructure on economic  
15 growth differed according to the set-up of their model.  
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34 From a regional perspective, much of the analysis has been carried out  
35 for the American states and for the Spanish regions<sup>3</sup>. In the case of the US,  
36 Munell (1990a) estimated an amplified production function, with panel data  
37 for the American states. When the model was specified with the variables in  
38 levels and without fixed effects, the impact of public capital on productivity  
39 was positive and significant, but smaller than the Aschauer (1989a) estimate.  
40 Building on this, Munell (1990b) broke down public capital stock into its  
41 different types, showing that the biggest impacts were attributable to road and  
42 water supply infrastructures. In contrast, García-Milá et al (1996), who  
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57 <sup>3</sup> There are very few countries where regional public investment data are available, one  
58 exception are Germany and Italy, where recently Marrocu and Paci (2010) obtained a positive  
59 and significant but variable public investment effect on production.  
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3 estimated, for the period 1970-1983, a Cobb-Douglas production function with  
4 data for the 48 American states, found no relation between public capital  
5 stock and productivity given the presence of region fixed effects. Likewise  
6 Holtz-Eakin (1994) concluded that, once fixed regional effects are introduced,  
7 public capital stock is not significant.  
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16 With regard to the Spanish regions, most papers suggest a positive  
17 effect, for example, Marquez et al (2009), De la Fuente (2008), Cantos et al  
18 (2005), Ezcurra et al (2005), Moreno et al (2002), Boscá et al (2002), Mas et  
19 al (1996), Bajo-Rubio and Sosvilla-Rivero (1993), Flores de Frutos et al (1998)  
20 and Gómez-Antonio and Fingleton (2010). However some papers, such as  
21 Gorostiaga (1999) and Gonzalez-Páramo and Martinez (2003) do not find a  
22 significant effect of public capital stock on economic growth. One of the  
23 reasons suggested in the literature for the inconclusiveness of the results is  
24 that many analyses do not take into account the existence of spillover effects.  
25 Negative as well as positive inter-regional spatial spillovers may occur, for  
26 instance Mas et al (1996), using the production function approach, and Avilés  
27 *et al* (2003), based on duality theory, find positive spillovers. Pereira and  
28 Roca-Sagales (2003), applying a vector autoregressive model, show similar  
29 results. Moreno and López-Bazo (2007) interestingly obtain a negative  
30 spillover effect due to transport infrastructure that counterbalances its  
31 positive effect on manufacturing productivity within each region. The  
32 existence of negative spillovers suggests that a region's public capital raises its  
33 comparative advantage, thereby attracting production factors from other  
34 regions.  
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3 With regard to the results obtained in countries other than Spain,  
4 Holtz-Eakin and Schwartz (1995) provide no evidence of spatial infrastructure  
5 spillovers in the US context. However, Owyong and Thangavelu (2001) find  
6 that US public capital positively affects Canadian productivity. Cohen and  
7 Morrison (2004) and Bronzini and Piselli (2009), also find significant positive  
8 spatial spillovers for the US, and Italy, respectively. However, Boarnet (1998)  
9 using data for California's counties, finds that the output of counties is  
10 negatively affected by neighbouring counties' infrastructure, likewise Sloboda  
11 and Yao (2008) for the US, and Pereira and Andraz (2006) for Portuguese  
12 regions.  
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27 To summarise the above, the literature on the effects of public  
28 infrastructure is inconclusive, although there is a general consensus on the  
29 need for a certain level of public infrastructural provision, the results obtained  
30 differ substantially once this level is achieved. More recent studies have  
31 partially discredited the results obtained in early research. Many researchers  
32 agree that the apparently positive impact of public capital stock might be due  
33 to inadequate model specifications which cause spurious relations or fail to  
34 appropriately control for region or country heterogeneity.  
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47 The period analysed in this paper is the decade from 1996 to 2005. We  
48 avoid analysing earlier data because of the substantial transformation of the  
49 Spanish economy over the longer period, which makes model specification  
50 particularly difficult. For instance, in a fixed effects panel, the fixed effects  
51 may not capture some variables that vary over time given a longer time period,  
52 leading to omitted variable bias. We thus restrict our period of analysis to a  
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3 shorter time-span during which we have greater confidence that our model  
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5 will be appropriate.  
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9 As mentioned above, our approach differs from the four approaches  
10 that can be found in the literature, and can be seen as a fifth approach that  
11 extends the public capital literature by basing the evaluation of public  
12 infrastructure on a different theoretical paradigm to that which dominates the  
13 literature, namely neoclassical constant returns to scale technology. Our  
14 model is rooted in contemporary Urban Economics theory, which provides  
15 formal general equilibrium solutions with each agent solving a clearly defined  
16 economic problem within the context of a monopolistic competition market  
17 structure. One of the most distinctive aspects of this theory is the possibility of  
18 increasing returns to scale. By incorporating imperfect competition,  
19 increasing returns and externalities in the form of market interdependence,  
20 there is an added realism in these models, without compromising rigour and  
21 the logic of a closed general equilibrium approach. To our knowledge this  
22 theory has not previously underpinned attempts to test the impact of public  
23 capital.  
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44 In addition to the direct effect on productivity of the mechanisms  
45 embodied in our urban economics theory, we also allow for the direct within-  
46 province effects of variations in worker efficiency, and also for spillovers in  
47 efficiency levels across provinces, with efficiency depending on the level of  
48 public capital and also the level of human capital. Spillover effects operating  
49 across provinces are technological externalities that could also play a key role  
50 in regional economic performance, since changes in one region may affect  
51 over regions, cascading across the whole country and rebounding back to the  
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3 initial province. These impacts might be positive or negative. For example,  
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5 changes in one region could affect production in other regions by raising the  
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7 comparative advantage of that region compared with others, and could  
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9 therefore attract production factors from other locations where output or  
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11 productivity might as a consequence diminish. On the other hand there are  
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13 reasons to believe that capital investment in neighbouring provinces might  
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15 have a positive impact on productivity within a given province as it might  
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17 enhance connections such as roads, railways or airports.  
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23 Although our approach differs somewhat from that of the previous  
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25 literature, nevertheless our main conclusions are in line with what has been  
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27 found previously for the Spanish economy. We find that, controlling for inter-  
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29 province heterogeneity, human capital and spillover between provinces, public  
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31 capital, in our case working via labour efficiency, has a significant positive  
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33 direct impact on the level of GDP per worker. The presence of the spillover  
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35 effect enables us to avoid model misspecification which would otherwise occur  
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37 if we chose to ignore spatial interaction, and therefore we are able to obtain  
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39 unbiased estimates and also take into account the total impact effect. Within  
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41 the positive spillover of labour efficiency, there may be a negative spillover  
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43 effect of public capital, as has been detected in some other papers, but our  
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45 model set-up does not allow us to identify this specifically and it is not a focus  
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47 for our investigation in this paper. The positive spillover effect we identify is  
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49 the net effect of the spillover of public and human capital spillover and of  
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51 other unmodelled factors captured by model disturbances.  
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59 The paper is divided into the following sections. Section 2 specify the  
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theoretical background of the model and derive the specific reduced form that

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3 is going to be estimated. Section 3 details the data set and the data sources  
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5 utilised for the estimation procedure. Section 4 comments on the main results  
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7 obtained in the estimation and section 5 concludes.  
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## 10 11 12 13 14 **2. THE MODEL: THEORETICAL BACKGROUND**

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17 At the core of this model is the concept of increasing returns to scale,  
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19 which has become popular in recent years within both urban and geographical  
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21 economics (Rivera-Batiz, 1988; Abdel-Rahman and Fujita, 1990; Quigley,  
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23 1998; Fujita et al 1999). All of this literature allows increasing returns in the  
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25 region or city while at the same time the decision problem for each actor is  
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27 explicitly stated as one of profit or utility maximization. Due to the increase in  
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29 diversity or variety in producer inputs, increasing density of economic activity  
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31 can yield external scale economies, even though firms are just earning normal  
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33 profits. The monopolistic competition model developed by Dixit-Stiglitz allows  
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35 an equilibrium solution in the context of competitive producers but with  
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37 increasing returns to the economy as a whole. The approach adopted differs  
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39 from pro-competitive effects leading to agglomeration. Porter (1990, 1998)  
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41 suggests that competition causes firms to be better innovators or faster  
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43 adopters of others' innovations than they otherwise would be, which enhances  
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45 the growth rate. To ensure full access to competitors' spillovers, an optimal  
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47 strategy is for firms in the same sector to cluster together. A similar  
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49 competitive stimulus is provided by Jacobs (1969) externalities, but based on  
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51 spillovers between sectors.  
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3 The model in this paper, following Rivera-Batiz (1988) and Abdel-  
4 Rahman and Fujita (1990), and Ciccone and Hall (1996), considers two  
5 sectors, industry (including manufacturing and traded services) and producer  
6 services and follows the arguments of some of the urban economics literature.  
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8 The non-traded producer service sector (hereafter ‘services’) comprises local  
9 services that are not traded in national or international markets and are  
10 identified as the array of input requirements that industry demands, such as  
11 repair and maintenance of all kinds, transportation and communication  
12 services, advertising, engineering and legal support, etc. We assume a  
13 monopolistic competition market structure for services<sup>4</sup>, which is a direct  
14 result of the fact that the market for services are generally highly competitive,  
15 and face relatively minor barriers to entry and exit, while at the same time  
16 consumers and producers have highly specialized demands making each  
17 service sector firm differentiated with respect to the others. So firms in the  
18 service sector are assumed to be typically numerous, small, independent and  
19 heterogeneous. Industry on the other hand is assumed to have a competitive

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45 <sup>4</sup> The Dixit-Stiglitz theory of monopolistic competition provides the reason why an increase in  
46 service labour maps to an increase in service variety, rather than more of the same variety.  
47 Monopolistic competition envisages a large number of services firms producing differentiated  
48 services and firms freely entering the sector until profits go to zero. The existence of fixed  
49 costs means that firms prefer to concentrate on a single variety and reap internal economies of  
50 scale; there is no advantage in a variety’s production being split between two or more firms.  
51 On the other hand if there were no fixed costs, average costs would not decrease with  
52 increasing output so no internal economies of scale would be realized. Since each firm is the  
53 producer of its own differentiated services, the ensuing monopoly power allows prices to be a  
54 mark up on marginal cost. The number of firms supplying services is an endogenous variable  
55 in the model instead of being an ad-hoc restriction. There is an equilibrium level of output and  
56 therefore equilibrium labour requirement per service firm that is a constant, and as will be  
57 stated later we have an equilibrium number of firms. These equilibrium values depend on  
58 exogenous parameters.  
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3 market structure, and demands a wide array of different types of services  
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5 performing highly specialized tasks.  
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9 In order to get to an empirically tractable reduced form we follow  
10 closely the presentation of the model given in Fingleton (2001, 2003, 2004).  
11 First we derive the reduced form linking output ( $Q$ ) to the intensity of activity  
12 in a unit area given by the total labour force ( $N$ ) and land ( $L$ ). Capital, in the  
13 form of public capital or human capital comes through via its impact on  
14 labour efficiency. By substituting the level of composite services  $I$  into the  
15 Cobb-Douglas production function we obtain the industry production  
16 technology. In this the level of industry output ( $Q$ ) is a function of the input of  
17 industry labour  $M$ ,  $I$  and  $L$ . Note that industry is competitive, with constant  
18 returns to scale.  
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$$Q = (M^\beta I^{1-\beta})^\alpha L^{1-\alpha} \quad (1)$$

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36 For simplicity the level of composite services is determined by the CES  
37 production function. This is what determines the level of composite services  $I$ .  
38 It is not simply the sum of each firm's output; it is more, depending on the  
39 number of separate varieties. The assumption is that there is a 'love of variety',  
40 which means that the varieties produced by differentiated firms results in a  
41 higher level of composite services than would otherwise be the case from firms  
42 with identical, perfectly substitutable, products.  
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$$I = \left[ \int_{d=1}^D i(d)^{\frac{1}{\mu}} \mathcal{A} d \right]^\mu \quad (2)$$

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55 In (2)  $i(d)$  is the "typical" output of a service variety, and there are  $D$  varieties.  
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60 The level of monopoly power in the service sector is given by the exogenous

parameter  $\mu$ <sup>5</sup>. The higher  $\mu$  is the less one service substitutes for others and the more monopoly power the producer of that service has. As  $\mu$  increases, we see rising monopoly power and falling elasticity of substitution. More monopoly power enhances the level of composite services providing an input to industry output. As  $\mu$  falls back towards 1, the level of composite services approaches the number of firms times the equilibrium level of output per firm.

Since we assume a very large number of varieties we approximate the continuous integral by the discrete summation. At equilibrium  $i(d)$  is a constant across all varieties and therefore we can reduce the summation to a product as follows:

$$I = \left[ \sum_{d=1}^D i(d)^{\frac{1}{\mu}} \right]^{\mu} = \left[ Di(d)^{\frac{1}{\mu}} \right]^{\mu} = D^{\mu} i(d) \quad (3)$$

Broadly speaking, services are relatively labour intensive. We thus assume, for simplicity that each firm producing composite service uses only labour as an input whose requirements are given by

$$\tilde{L}_i = ai(d) + s \quad (4)$$

In (4),  $s$  represent the fixed labour input requirement and  $a$  the marginal input requirement. Following the Chamberlinian framework, the technology used by all firms is considered identical, implying that  $a$  and  $s$  are the same for all the composite service sector firms.

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<sup>5</sup> This is the substitution parameter of the CES production function, which determines the elasticity of substitution, the price elasticity of demand, and the internal returns to scale given by the average cost to marginal cost for producer services in equilibrium.

Given the simplified form in equation (3), we substitute for  $I$  and use the equilibrium values for the number of varieties  $D$  and  $M$  to obtain the relationship between  $Q$ ,  $N$  and  $L$ . We will write the equation in terms of production per unit area, so we restrict  $L = 1$ , eliminating land as an input since  $1 = 1^{1-\alpha}$ : By doing this we are implicitly including the effect of congestion in the equation, since by eliminating land production will be less than it would otherwise be.

$$Q = (M^\beta I^{1-\beta})^\alpha$$

$$I = D^\mu i(d)$$

$$Q = \left[ M^\beta (D^\mu i(d))^{1-\beta} \right]^\alpha$$

If we assume that the economy is at a competitive equilibrium and workers are paid the value of their marginal product, at equilibrium the wage rate ( $w$ ) equal to the marginal product of  $M$  labour is given by

$$w = \frac{dQ}{dM} = \frac{Q\alpha\beta}{M} \quad (5)$$

If we assume also that the share of  $Q$  going to all labour ( $N$ , equal to industry plus services) is given by  $\alpha$ , from standard Cobb-Douglas theory, we have wages (considered to be the same as for industry) times number of workers as a share of  $Q$  is

$$\frac{wN}{Q} = \alpha \quad (6)$$

The assumption here is that the inputs are (all types of) labour (coefficient  $\alpha$ ), capital and land and the marginal product of each input



(wages, returns on capital and land rents) are given by the respective derivatives, and the shares are the marginal products times the amounts (of labour, capital, land) as a proportion of total output  $Q$ . The marginal product of all types of labour is

$$w = \frac{Q\alpha}{N} \quad (7)$$

From this it follows that

$$\begin{aligned} \frac{wM}{wN} &= \frac{Q\alpha\beta}{Q\alpha} \\ \frac{M}{N} &= \beta \end{aligned} \quad (8)$$

Hence service workers ( $N-M$ ) as a share of total workers is  $1 - \beta$ .

At equilibrium all firms are the same size so the number of firms  $D$  is the total services workforce,  $(1 - \beta)N$ , divided by the workers per service firm.

$$D = \frac{(1 - \beta)N}{ai(d) + s} \quad (9)$$

So utilising equilibrium values we have:

$$\begin{aligned} Q &= \left[ (\beta N)^\beta \left[ \left( \frac{(1 - \beta)N}{ai(d) + s} \right)^\mu i(d) \right]^{1 - \beta} \right]^\alpha \\ Q &= N^{\beta + \mu\alpha(1 - \beta)} \beta^{\beta\alpha} i(d)^{\alpha(1 - \beta)} (ai(d) + s)^{-\mu\alpha(1 - \beta)} (1 - \beta)^{\mu\alpha(1 - \beta)} = N^\gamma \Phi \end{aligned} \quad (10)$$

Where:

$$\begin{aligned} \gamma &= \beta\alpha + \mu\alpha(1 - \beta) = \alpha[1 + (1 - \beta)(\mu - 1)] \\ \Phi &= \beta^{\beta\alpha} i(d)^{\alpha(1 - \beta)} (ai(d) + s)^{-\mu\alpha(1 - \beta)} (1 - \beta)^{\mu\alpha(1 - \beta)} \end{aligned} \quad (11)$$

1  
2  
3 Increasing returns to scale are implied by  $\gamma > 1$ , so from equation (11) it is  
4  
5 apparent that this will occur if  $\beta < 1$  and  $\mu > 1$  provided  $\alpha$  is not too small.  
6  
7 This means that assuming that the loss of production as a result of restricting  
8  
9 land is not too severe, then we also need differentiated intermediate goods to  
10  
11 be relevant to the output of the competitive sector ( $\beta < 1$ ) and for them to be  
12  
13 imperfect substitutes for each other ( $\mu > 1$ ) with a degree of monopoly power.  
14  
15 With a higher enough  $\mu$  and a low enough  $\beta$ , the production function could  
16  
17 have increasing returns, where the favourable effect of density outweighs the  
18  
19 congestion effects.  
20  
21  
22  
23  
24

25 In order to move closer to a convenient reduced form, we log-linearize  
26  
27 equation (7) by taking natural logarithms, hence  
28  
29

$$30 \ln w = \ln Q + \ln \alpha - \ln N \quad (12)$$

31  
32  
33 And substituting for  $Q$  gives  
34  
35

$$36 \ln w = \gamma \ln N + \ln \Phi + \ln \alpha - \ln N$$

$$37$$

$$38 \ln w = k_1 + (\gamma - 1) \ln N \quad (13)$$

39  
40  
41 Assuming the number of labour efficiency units ( $N$ ) is equal to the total  
42  
43 employment ( $E$ ) times the level of efficiency ( $A$ ), we have  
44  
45  
46  
47  
48

$$49 \ln w = k_1 + (\gamma - 1) \ln E + (\gamma - 1) \ln A \quad (14)$$

## 50 51 52 53 54 55 56 **The Level of Efficiency**

57  
58 In line with Fingleton (2003b) we assume that the level of efficiency  
59  
60 depends on 'within region' effects and effects that spillover from

1  
2  
3 'neighbouring' regions. Within regions, assume that what is important is the  
4  
5 level of human capital ( $H$ ), the level of public capital ( $K$ ), plus an  
6  
7 autonomous rate reflecting "learning by doing" which proceeds regardless of  
8  
9 the other factors. Regions with relatively better-developed human capital are  
10  
11 expected to make faster technical progress since human capital facilitates  
12  
13 research, development and the spillover of knowledge. Likewise superior  
14  
15 infrastructures (communications, urban facilities, health facilities, etc.) will  
16  
17 provide the basis for a more efficient labour force. We will utilise as indicator  
18  
19 of human capital the number of people with high degree level qualifications in  
20  
21 the region. Public capital measures will be outlined below. The spillover effect  
22  
23 is determined by the scalar parameter  $\rho$  and by a so-called weights matrix,  $W$ ,  
24  
25 which is a square  $n$  by  $n$  matrix for  $n$  regions with cell values denoting the  
26  
27 strength of interregional interaction, and zeros on the main diagonal. This  
28  
29 idea of capturing spillovers by means of a weight matrix has been widely used  
30  
31 in the literature, since the appearance of spatial econometrics techniques, for  
32  
33 instance under a neoclassical production function approach in Moreno and  
34  
35 López-Bazo (2007).  
36  
37  
38  
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42

43  
44 Combining the factors outlined above produces the following  
45  
46 specification:  
47  
48  
49

$$50 \ln A_i = b_0 + b_1 \ln H_i + b_2 \ln K_{pi} + \rho \sum_{r=1}^R W_{ir} \ln A_r + \varepsilon \quad (15)$$

51  
52  
53  
54 Rearranging, and assuming  $(I - \rho W)$  is non-singular, we obtain the equivalent  
55  
56 matrix expression  
57

$$58 \ln A = (I - \rho W)^{-1} (Xb + \varepsilon) = (I - \rho W)^{-1} Xb + (I - \rho W)^{-1} \varepsilon \quad (16)$$

In which  $X$  is the  $n$  by  $k$  matrix of right hand side variables (the constant,  $\ln H$  and  $\ln K$ ) and  $\varepsilon$  is an independent and identically distributed disturbance term representing measurement error and exogenous shocks to the level of efficiency, hence,  $\varepsilon \sim iid(0, \Omega^2)$

Part of the contribution to area  $i$ 's efficiency level is given by row  $i$  of vector  $W \ln(A)$  which contains the sum of the weighted efficiency levels of other provinces. Note that by making  $\ln(A)$  depend on  $W \ln(A)$  and not simply on the constant,  $\ln H$  and  $\ln K$ , we capture the totality of the effects influencing the efficiency level, including those represented by the random shocks. Assuming that  $|\rho| < 1$ , given our preferred (standardised)  $W$  matrix (see below) it then follows that  $(I - \rho W)^{-1} = \sum_{i=0}^{\infty} \rho^i W^i$ , with  $W^0$  equal to the identity matrix  $I$ ,  $W^2$  equal to the matrix product of  $W$  and  $W$ , and in general  $W^i$  equal to the matrix product of  $W^{i-1}$  and  $W$ . This means that

$$\begin{aligned} \ln A_i &= Xb + \varepsilon + \rho W X b + \rho W \varepsilon + \rho^2 W^2 X b + \rho^2 W^2 \varepsilon \\ &\quad + \rho^3 W^3 X b + \rho^3 W^3 \varepsilon + \dots \\ \ln A_i &= \sum_{i=0}^{\infty} \rho^i W^i (Xb + \varepsilon) \end{aligned}$$

This shows that  $\ln A_i$  is equal to the weighted sum of the matrix products<sup>6</sup> of the matrices  $W^i (i = 0, \dots, \infty)$  and exogenous variables  $X$  and  $\varepsilon$ . The log level of efficiency  $\ln A_i$  in Province  $i$  depends on levels of  $\ln H$  and  $\ln K$  and on shocks

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<sup>6</sup> Note that as  $i$  becomes large,  $W^i$  tends to a matrix in which each cell in a column contains the same value, columns differ, and each row of  $W^i$  is identical. This means that the matrix products tend to constant vectors.

1  
2  
3  $\varepsilon$  in regions  $i,j,k,l,\dots$ . The actual mechanism causing evidently remote  
4 interactions is the direct mutual interaction between Province  $i$  and its  
5  
6  
7  
8  
9 'neighbours' as defined by  $W$ , as indicated by the presence of  $\sum_{r=1}^R W_{ir} \ln A_r$  in  
10  
11  
12 equation (15), so that a high (low) efficiency level in Province  $i$  causes, and is a  
13  
14 response to, high (low) efficiency in 'nearby' Provinces.  
15  
16  
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### 21 **The $W$ Matrix**

22  
23  
24 We considered several alternatives candidates as our preferred weights  
25 matrix<sup>7</sup>  $W$ . A first order binary geographical contiguity matrix, in which the  
26 elements are one when regions share a common border, and zero otherwise<sup>8</sup>,  
27  
28 is one option considered. However, while this may prove informative in  
29  
30 helping to detect localised cross-border spillovers, the main aim of this paper  
31  
32 is simply to explore the existence of a direct causal effect using a more general  
33  
34 approach to modelling spatial interaction effects, via  $W$ , that would otherwise  
35  
36 not be present in our specification<sup>9</sup>. Thus we adopt a  $W$  matrix in which the  
37  
38 value allotted to cell  $(i,j)$  is a function<sup>10</sup> of the road distances  $d_{ij}$  between the  
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41  
42  
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48 <sup>7</sup> See Fingleton (2003a) for further discussion of alternative assumptions about  $W$ .

49 <sup>8</sup> The elements of the main diagonal are set to zero by convention.

50  
51  
52 <sup>9</sup> If the basic theoretical model was New Economic Geography rather than our urban  
53 economics specification, then that would automatically capture spatial dependencies based on  
54 the size of economies, similar to those embodied in our  $W$  matrix as defined below.  
55

56  
57 <sup>10</sup> This way of capturing interactions weighted by distance is used very often in spatial  
58 econometrics literature. Fingleton (2003b) hypothesized that the efficiency of the labour force  
59 employed within an area will be in part determined by commuting, the frequency of which  
60 falls as distance increases. The rate at which this fall-off in commuting frequency occurs is

capitals of the provinces and the GDP of the region<sup>11</sup>. Since we subsequently standardise the  $W$  matrix so that the total in each row sums to 1, the resulting standardised matrix will be the same irrespective of whether we include both origin and destination provinces in our equation, or whether we just include the destination.

$$\begin{aligned}
 W_{ij} &= \frac{GDP_j^{\tilde{\alpha}}}{d_{ij}^{\tilde{\beta}}} & i \neq j \\
 W_{ij} &= 0 & i = j \\
 \tilde{\alpha} &= 1; \tilde{\beta} = 2
 \end{aligned}$$

Thus we also take into account the (economic) size of the (remote) province in order to measure the interaction between regions. Economic size (GDP) is considered relevant because of the extensive trade and labor market that a large and diverse local economy naturally generates.<sup>12</sup>

## The Reduced Form

Combining equations 14 and 16 gives

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embodied within the matrix  $W$ , which is determined by the varying rate of decline-with-distance of commuting in each individual area. So a scalar that reflects the commuting of people between different regions is selected to weight distances. As this information is not available for the Spanish provinces we weighted using the square to make relation more intense as the distance becomes shorter. Additionally, controlling for distance, we assume that commuting between provinces will be greater the larger the provincial economies.

<sup>11</sup> We use, somewhat arbitrarily, the GDP in 1971, but other years could have been used with very little impact on the outcome. Using a previous year ensures that the resulting  $W$  matrix comprises fixed exogenous quantities with no possibility of feedback from the level of productivity.

<sup>12</sup> The estimation results were similar when we used different  $W$  matrices, the coefficient varied slightly and all the signs were as expected from theory. The alternative  $W$ s were obtained using  $\tilde{\alpha} = 2; \tilde{\beta} = 2$  and  $\tilde{\alpha} = 1; \tilde{\beta} = 3$ .

$$\begin{aligned} \ln w &= k_1 + (\gamma - 1) \ln E + (\gamma - 1)(I - \rho W)^{-1}(Xb + \varepsilon) \\ (I - \rho W) \ln w &= (I - \rho W)k_1 + (I - \rho W)(\gamma - 1) \ln E + (\gamma - 1)(Xb + \varepsilon) \end{aligned} \quad (17)$$

On rearranging, making the exogenous variables explicit, and introducing a time subscript, we then have

$$\begin{aligned} \ln w_t &= \rho W \ln w_t + (I - \rho W)k_1 + (\gamma - 1)(\ln E_t - \rho W \ln E_t) + c_0 + c_1 \ln H_{t-1} + c_2 \ln K_{t-1} + \psi \\ \psi &\sim N(0, (\gamma - 1)^2 \Omega^2) \end{aligned} \quad (18)$$

Consistent estimation of the model is not possible via OLS because of the presence of the endogenous variable  $W \ln w$  on the right hand side of equation 18. Moreover we also may have two-way causation involving employment density and our dependent variable, with employment density increasing (due to migration and enhanced participation rates) as wage rates increase. Consequently the composite variable  $(\ln E - \rho W \ln E)$  is likely to be endogenous also. Note that this composite variable entails a parameter restriction because of the presence of  $\rho$ . In order to guard against any potential inconsistency, our model is estimated using instrumental variables<sup>13</sup>. We assume that human capital and public capital stocks are exogenous, in the case of human capital ( $H$ ) this is because we assume complex determinants of educational attainment levels, so that any direct feedback from wage levels will be relatively weak. We note that in Spain inter-province migration in response to wage differentials is not strong. In the case of Public capital stock ( $K$ ), the assumption is that this is mainly controlled by government policy and

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<sup>13</sup> Specifically we use the `xtivreg` available in Stata for estimating panel data models with endogenous variables.

1  
2  
3 this is not driven by wage levels. However we also decide to lag these variables  
4  
5 by one year, guaranteeing exogeneity, since they pre-date the year of analysis.  
6  
7 These assumptions are supported by model diagnostics, as explained  
8  
9 subsequently. Over-identification is achieved by additional instrumental  
10  
11 variables, namely the spatial lags of our exogenous variables together with  
12  
13 three other measures of public capital, namely social, local and transport  
14  
15 infrastructure, each again lagged by one year. We subsequently test for the  
16  
17 legitimate exclusion and validity of these instruments.  
18  
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22  
23 The restriction in equation (18) relating to  $\rho$  is caused by the spillover  
24  
25 of labour efficiency levels between provinces. To take into account this  
26  
27 constraint we use iterated 2SLS, in which each iteration provides an updated  
28  
29 value for  $\rho$  from the  $W \ln w$  term which is then used to update  
30  
31  $(\ln E - \rho W \ln E)$  for the subsequent iteration, until  $\rho$  reaches a steady state as in  
32  
33 Fingleton (2003b). At the first iteration, with no initial estimate for  $\rho$ , we  
34  
35 assume an arbitrary value for  $\rho = 0$ . In order to avoid an explosive model, the  
36  
37 estimated value of  $\rho$  should be in the interval  $\frac{1}{e_L} < \rho < \frac{1}{e_U} = 1$ , where  $e_L$  and  
38  
39  $e_U = 1$  are the largest negative and largest positive eigenvalues of  $W$   
40  
41 respectively. This region of parameter space is devoid of singular points, but  
42  
43 the matrix  $(I - \rho W)$  becomes singular at these singular points and beyond<sup>14</sup>.  
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56  
57 <sup>14</sup> The range of  $\rho$  is automatically bounded in Maximum Likelihood estimator but under 2SLS  
58 can fall outside this stable range and thus encounter singular points. Fortunately, in our  
59 estimates the estimated  $\rho$  lies within the stable bounds.  
60



1  
2  
3 As explained in Fingleton (2003b), because here we are using a standardized  
4  
5 W matrix,  $(I - \rho W)k_1$  is a constant.  
6  
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### 10 11 12 **3. DATA** 13 14

15 Our analysis is based on a panel of data for the decade 1996 to 2005,  
16  
17 with the individuals comprising the Spanish provinces<sup>15</sup>. We confine attention  
18  
19 to this decade because earlier periods cover an era of substantial economic  
20  
21 transformation. For example in the 1970s and 1980s the level of government  
22  
23 capital endowment and economic activity in the Spanish regions was far below  
24  
25 that typical of most Western European economies, but by the mid-1990s this  
26  
27 was no longer the case. In 1980 per capita public capital stock endowment was  
28  
29 only 40% of the average of the European Union, but this figure increased to  
30  
31 only 40% of the average of the European Union, but this figure increased to  
32  
33 60% in 1990 and reached 89% in 2005. Since Spain joined the European  
34  
35 Union, there has been a very intensive period of capital investment by the  
36  
37 Spanish government, and in the decade under study, the ratio of public to  
38  
39 private capital increased constantly with no perceptible effect due to economic  
40  
41 cycles. This progress can be explained not only because the large amount of  
42  
43 funding received from the structural funds<sup>16</sup>, as the European Union has  
44  
45 devoted a substantial fraction of its regional policy funding (known as the  
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47  
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51  
52 <sup>15</sup> Spanish provinces correspond to level 3 of the Nomenclature of Territorial Units for  
53  
54 Statistics (NUTS) of EUROSTAT, the Statistical Office of the European Union. The average  
55  
56 surface of a representative province is 10,120 km<sup>2</sup> (range 1,980 km<sup>2</sup> to 21,766 km<sup>2</sup>).  
57

58  
59 <sup>16</sup> During the period analyzed Spain has received a sustained increasing amount of funding  
60  
61 from the Structural and Cohesion funds. During the period 1994-1999 Spain received the  
62  
63 “Delors II” package and during 2000-2006 the “Agenda 2000” package, receiving a yearly  
64  
65 average amount of 5.900 and 8.900 million of Euros respectively.  
66

1  
2  
3 Structural Funds) to the financing of infrastructure projects, but also as a  
4  
5 consequence of a higher domestic rate of growth of public investment in  
6  
7 Spain<sup>17</sup>.  
8  
9

10  
11 We proxy the wage level by the productivity level based on Gross Value  
12 Added, in thousands of constant (1995) euros, data which were provided by  
13 Fundación BBVA (*La Renta Nacional de España y su Distribución*  
14 *Provincial*) until 1997, and thereafter by Fundación de las Cajas de Ahorro  
15 Confederadas (FUNCAS)<sup>18</sup> as documented in their “*Balance Económico*  
16 *Regional*”.  
17  
18

19  
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21  
22 The employment density variable ( $E$ ) is constructed by dividing the  
23 total employment, taken from “*La Renta Nacional de España y su*  
24 *Distribución Provincial*”, by the provincial area in square kilometres. Data on  
25 the geographic area of each province and on population were provided by the  
26  
27 *Office of National Statistics* (INE).  
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34  
35 Our human capital variable ( $H$ ) is the proportion of people in each  
36 province with higher education, data published in “*Human Capital in Spain*  
37 *and its distribution by provinces (1977-2007)*” by *Instituto Valenciano de*  
38 *Investigaciones Económicas* (IVIE).  
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49 <sup>17</sup> Eurostat reported for the period 1995-2005 an average rate of growth of public investment  
50 in Spain of 3.37% while in the euro area it was of 2.5%. This higher rate has been sustained  
51 throughout the decade even though public expenditure has reduced as a proportion of GDP.  
52 At the same time provincial differences have also been reduced during the period thanks to  
53 the Structural and Cohesion funds. Most of the Spanish regions were Objective 1 regions and  
54 received European funds to finance infrastructure projects.  
55

56  
57 <sup>18</sup> In order to make the Gross Value Added and employment series homogeneous we took the  
58 rates of growth of the variable in FUNCAS database and applied it to the variable produced by  
59 FBBVA. Previously we had to transform the valued added into constant euros of 1995 using  
60 the Implicit Index Prices facilitated by both organisations.

1  
2  
3 Public capital stock ( $K$ ) was taken from the publication “*Series*  
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*Históricas de Capital Publico en España y su distribución territorial 1900-2005*” which detailed work done by FBBVA in collaboration with IVIE.

Our excluded instruments comprise three separate elements of public capital stock, namely the transportation infrastructure, the social infrastructure stock and the local public capital stock. Transportation includes airports, ports, road and railways infrastructures, the social infrastructure includes public capital stock in education and health facilities and local public capital stock comprises local government infrastructures of various kinds, infrastructure relating to water supply and management, plus other residual investments. Our assumption is that these have an indirect effect working via urbanisation, overall public capital and human capital, but they have no direct individual effect on wage levels. We test this exclusion assumption below. Our additional instruments are obtained by the matrix product of matrix  $W$  and the vectors of  $\log \text{public}^{19}$  and  $\log \text{human capital}$ . As with the exogenous variables, all instruments are lagged by one year.

#### 4. ECONOMETRIC RESULTS

The results in Table 1 show the estimates<sup>20</sup> of the panel model with fixed province effects, estimated with endogenous variables  $W \ln w$

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<sup>19</sup> To satisfy the diagnostic tests described below, the matrix product  $W \ln K$  has been dichotomised, being equal to 1 for values exceeding the median value, and 0 otherwise.

<sup>20</sup> After having eliminated the spatial lag of log total capital as an instrument, as is necessary in order to pass the test of over-identifying restrictions.

1  
2  
3 and  $(\ln E - \rho W \ln E)$ , and iterating to satisfy the constraint on the parameter  $\rho$ .  
4  
5  
6 Our analysis rests on the assumption that these two variables are indeed  
7  
8 endogenous, that  $\ln K$  and  $\ln H$  are exogenous, and that the instruments are  
9  
10 valid. Our diagnostic tests support these assumptions. In our endogeneity  
11  
12 test<sup>21</sup>, the null hypothesis is that  $W \ln w$  and  $(\ln E - \rho W \ln E)$  are exogenous,  
13  
14 and we reject this null since the test statistic is equal to 31.779, which is highly  
15  
16 significant when referred to the  $\chi^2$  distribution, with the two degrees of  
17  
18 freedom being determined by the fact that there are two variables under test.  
19  
20 The test of the exogeneity of  $\ln K$  and  $\ln H$  is provided by the C statistic<sup>22</sup>. The  
21  
22 null hypothesis is that the full set of instruments, including the included  
23  
24 instruments  $\ln K$  and  $\ln H$  are exogenous. Under the null, the test statistic is  
25  
26 distributed as  $\chi^2$  (again with two degrees of freedom appropriate for a two  
27  
28 variable test). Rejecting this null in favour of the alternative would indicate  
29  
30 that the included ‘exogenous’ variables, which are the specific instruments  
31  
32 being tested, are endogenous, but the test statistic is equal to 2.418, with p-  
33  
34 value equal to 0.2985 in  $\chi^2$ . We therefore fail to reject the null and conclude  
35  
36 that we have no evidence that  $\ln K$  and  $\ln H$  are endogenous. Our initial  
37  
38 assumption that  $\ln K$  and  $\ln H$  are exogenous has support from our diagnostic  
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40 tests.  
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55 <sup>21</sup> This is an option (endog) available within Stata’s xtvreg2 command (Schaffer, 2010), and  
56 under conditional homoscedasticity, the test statistic is equal to that provided by a Hausman  
57 test.  
58

59 <sup>22</sup> Option orthog in xtvreg2.  
60

## TABLE 1: HERE

The test of the overall validity of the instruments is related to the C statistic described above. In fact the test statistic, the Sargan-Hansen statistic, is calculated twice in order to obtain the C statistic. The C statistic is the difference between the Sargan-Hansen test statistic calculated for the full set of instruments and the Sargan-Hansen test statistic calculated for the reduced set of instruments (that is excluding those that are suspected of being endogenous). The Sargan-Hansen test statistic for the reduced set is equal to 0.221 (p-value equals 0.6384 in  $\chi_1^2$ ) and the Sargan-Hansen test statistic for the full set of instruments is equal to 2.639, which has a p-value of 0.4507 in the appropriate  $\chi_3^2$  reference distribution (five excluded instruments minus two endogenous variables). The latter provides our test of over-identifying restrictions<sup>23</sup>, with the null being a hypothesis of valid instruments, which is not rejected thus indicating that the instruments are appropriate. We would reject if instruments are correlated with the disturbances, or if excluded instruments should be included in the set of regressors, so that the model is misspecified. This provides justification for our exclusion of the instruments transportation infrastructure, the social infrastructure stock and the local public capital stock from the model specification.

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<sup>23</sup> Also obtained by the Stata command `xtoverid`, see Schaffer and Stillman (2010).

1  
2  
3 While our instruments appear to be valid, they could still be weak and  
4 therefore lead to biased estimates and inference. However we find that our  
5 instruments are strong. Our test statistic is the Cragg-Donald Wald F statistic  
6 which is referred to the critical values given by Stock and Yogo (2005). The  
7 critical values are determined by the number of instruments and by the  
8 number of included endogenous variables, and also by the maximum amount  
9 of bias that is acceptable, where bias is relative to bias under OLS. The value of  
10 13.889 lies between the 10% and 5% maximal instrumental variables relative  
11 bias critical values of 8.78 and 13.97, being close to the 5% value. We conclude  
12 that the maximum bias in our estimator is less than 10% of the bias that would  
13 be incurred by OLS estimation. The second element of our test of weak  
14 instruments relates to the size of the test. If the true size of the conventional  
15 Wald test, with nominal size of 5%, exceeds this by a certain amount, in our  
16 case by a maximum of 10%, so that the true size is up to 15%, then we would  
17 also conclude that we had weak instruments. The test statistic lies between  
18 the critical values for 15% and 10% maximal size (nominal size plus size  
19 distortion), equal to 11.22 and 19.45 respectively. With size distortion of no  
20 more than 10%, and our earlier evidence of small relative bias, we conclude  
21 that our instruments are not weak.  
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48 To summarize, our main result given in Table 1 is that public capital  
49 has a significant positive effect on productivity, with an elasticity equal to  
50 approximately 0.14, having controlled for employment density, human capital,  
51 labour efficiency spillovers, and for the significant effects of province  
52 heterogeneity captured by the fixed effects.  
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### **Effects of public capital stock**

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There are several channels through which public investment is usually considered to affect regional per capita income. Macroeconomists typically emphasize three “conventional” channels. Public investment is considered to have a direct productivity effect on private production inputs and to have a complementarily effect on private investment. In the short term, however, it is hypothesised that public investment might crowd out private spending, and adversely affect growth if it persists. In this paper we hypothesise that the effect of public capital operates through its effect on worker efficiency, in the same way as human capital. However we acknowledge that the effects of public infrastructure may work through diverse channels and may be indirect, sector-specific and time-specific. For instance while Holtz-Eakin and Lovely (1996) find that infrastructure has no significant direct effects, they do find evidence that public capital may alter productivity through its effect on the number and variety of manufacturing establishments in the local manufacturing base. Likewise Moreno and López-Bazo (2007) demonstrate that public capital has a greater effect on Spain's industrial productivity than on any other economic sector, particularly during the period when Spain experienced rapid economic growth, and increased openness to trade and greater economic liberalization. Also, as we have indicated above, Moreno and López-Bazo (2007) and others suggest a more complex relationship between public capital and productivity which involves a negative spillover effect. However we are unable to identify this in our model set-up which simply captures the net effect of public and human capital and unmodelled spillovers as part of the labour efficiency spillover. In this paper we focus on the direct effect of public capital, which we find is significant and positive.

This leads to one additional consideration, the evaluation of true total effects in models involving spatial processes, as highlighted by LeSage and Pace (2009). Assuming that our parameter estimates apply equally to a single cross-section, when we take account of the spillover effects on account of the presence of the spatial lag  $W \ln w$  with  $\rho \neq 0$  in the model, then the derivative

$$\frac{\partial \ln w_t}{\partial \ln K_{t-1}} \neq c_2 = 0.1386 \text{ as implied by Table 1. It can be shown that the total}$$

effect is given by  $\frac{\partial \ln w_t}{\partial \ln K_{t-1}} = (I - \rho W)^{-1} I c_2$ , and since this is a matrix, it is

recommended that we consider the mean total effect given

$$\text{by } N^{-1} \sum_{ij} \frac{\partial \ln w_{it}}{\partial \ln K_{jt-1}} = N^{-1} \iota' (I - \rho W)^{-1} I c_2 \iota, \text{ in which } N = 47, \iota \text{ is an } N \text{ by } 1 \text{ vector of}$$

ones,  $I$  is an  $N$  by  $N$  identity matrix and  $\rho = 0.1806355$  as given by Table 1.

Evaluating this quantity gives an implied mean total effect equal to 0.1692,

compared with 0.1386 given  $\rho = 0$ . These results are broadly within the range

of variation of the elasticities obtained in other papers. Mas *et al* (1994, 1996)

obtained an elasticity associated with productive public infrastructures of 0.23

and 0.08, respectively. However in other papers the reported elasticity is

lower, as in Goerlich and Mas (2001) which reported an elasticity of 0.02 or

Boscá *et al* (1999) who obtained an output elasticity of 0.026 for public

infrastructures (0.035 in the long run).

## 5. CONCLUSIONS

In this paper we have examined the effect of public capital on the variation in wage (productivity) levels across the Spanish Provinces, over the



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3 period 1996-2005. The analysis is underpinned by contemporary urban  
4 economics theory and the methodology of spatial econometrics, which leads to  
5 a reduced form in which wage levels depend on ‘nearby’ wage levels,  
6 employment density, educational attainment and public capital. Endogeneity  
7 and constraints on parameter values lead to an iterative 2SLS panel  
8 estimation routine. The model supports the theory motivating the reduced  
9 form, so that there does appear to be increasing returns to scale. There are  
10 also significant positive effects due to educational attainment which support  
11 the thesis that labour efficiency is highly relevant to wage variations across  
12 Provinces. The model estimates also indicate that there is a significant  
13 relationship between wage levels and ‘nearby’ wage levels, supporting the  
14 hypothesis of positive spatial spillovers and the necessity for a spatial  
15 econometric approach.  
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34 Although the theoretical provenance of our paper is somewhat  
35 different, Ashauer’s hypothesis has not been rejected for the Spanish  
36 economy during the period analyzed. However we remain cautious in our  
37 conclusion that public capital is relevant, for we are conscious that the  
38 estimates may be affected by a more complex relationship between public  
39 capital and productivity, involving both positive and negative impacts of  
40 public capital stock, which are concealed when we simply observe is the net  
41 effect of the spillover of labour efficiency, which embodies the effect of public  
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56 Further work is needed to detangle the spillover effects of the variables  
57 affecting the labour efficiency level, either based on new data or new  
58 methodology, or both. Therefore in terms of policy involvement at a national  
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3 scale, in the absence of more detailed information on how the spillover effects  
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5 of public investment balance out, we still have to be prudent about the global  
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7 effects on economic activity. In the presence of negative spillovers, provinces  
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9 might be competing with each other attempting to obtain more infrastructures  
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11 than would otherwise be provided. By altering infrastructure investment  
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13 relative to that of neighbouring regions, each region has the ability to modify  
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15 the size of its infrastructure stock at the expense of its neighbour. If some  
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17 regions follow a “beggar-thy-neighbour” policy, all regions will be dragged into  
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19 fiscal competition. This can lead to gaming behaviour among regions in a  
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21 national economy. If local and national governments ignore the possible  
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23 existence of negative spillovers and overestimate the positive effects of public  
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25 policies, this can lead to inefficiency.  
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32 The comparisons of the return to different types of infrastructure are  
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34 on our research agenda for the future.  
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Table 1: Fixed effects panel estimates with endogenous regressors (T=10, n=47)

REGRESSORS	Parameter Estimates <sup>#</sup>	Standard error
Productivity Spatial Lag $W \ln w$	<b>0.1806355 **</b> (4.28)	<b>0.0421943</b>
Employment Density ( $\ln E - \rho W \ln E$ )	<b>0.1055751 **</b> (3.40)	<b>0.0310767</b>
Public Capital $\ln K$	<b>0.1386397 **</b> (7.26)	<b>0.0190934</b>
Human Capital $\ln H$	<b>0.0180546 **</b> (2.14)	<b>0.0084188</b>
R squared	<b>0.5265</b>	
Estimation Method	Instrumental variables	
Instruments	$\ln\_Kh, \ln\_Ktot,$ $WX\_ln\_Ktot, WX\_ln\_Kh, \ln\_Ktpte, \ln\_Ksoc,$ $\ln\_Kloc$	

Notes:

<sup>#</sup> z-ratios given in brackets beneath the estimates

\*\*\* Significant at 5% and 10% level, respectively

<sup>2</sup> Between fixed effects and covariates

Time sub-indices have been omitted from the table and from the comments to simplify notation.