REINFORCEMENT LEARNING: AN INTRODUCTION

lanis Lallemand, 24 octobre 2012

This presentation is based largely on the book:

Reinforcement Learning: An Introduction, Richard S. Sutton and Andrew G. Barto, MIT Press, Cambridge, MA, 1998

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GENERAL DEFINITION "Reinforcement learning is learning what to do – how to map situations to actions – so as to maximize a numerical reward signal. The learner is not told which actions to take, as in most forms of machine learning, but instead must discover which actions yield the most reward by trying them." GENERAL DEFINITION "Reinforcement learning is learning what to do – how to map situations to actions – so as to maximize a numerical reward signal. The learner is not told which actions to take, as in most forms of machine learning, but instead must discover which actions yield the most reward by trying them." GENERAL DEFINITION "Reinforcement learning is learning what to do – how to map situations to actions – so as to maximize a numerical reward signal. The learner is not told which actions to take, as in most forms of machine learning, but instead must discover which actions yield the most reward by trying them."

SUPERVIZED LEARNING Reinforcement learning is different from supervized learning (pattern recognition, neural networks, etc).

Supervized learning is learning from examples provided by a knowledgeable external supervizor.

In reinforcement learning the agent learns from his own behavior.

AGENTS

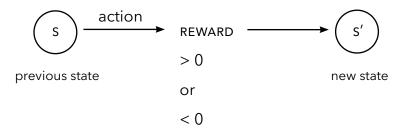
The AGENT performs the reinforcement learning task.

- 1. It has explicite goals (problem for music...).
- 2. It can sense aspect of the ENVIRONMENT (environment described in terms of STATES).
- 3. It performs ACTIONS to influence the environment.

REWARD FUNCTION

It defines the goal in a reinforcement learning problem.

It gives the agent a sense of what is good in an immediate sense (pleasure / pain).



VALUE FUNCTION It gives the agent a sense of what is good in the long run.

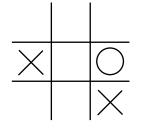
It is either:

- 1. A function of the environment's states (state value function).
- 2. A function of the environment's STATES and of the agent's ACTIONS (ACTION VALUE FUNCTION).

INTERPRETATIONThe VALUE of a state is the total amount of reward an agent can expect
to accumulate over the future, starting from that state.

MODEL OF THEIt is used to predict the states the environment will be in after the agentENVIRONMENTperforms its actions.

In reinforcement learning, the agent often uses the model to compute series of potential state-action sequences: it projects himself in the future to decide which action to perform in the present.



APPROACH Reinforcement learning with approximate value functions.

REWARD +1 for winning the game.

VALUE FUNCTION A table storing the last estimated probability of our winning from each state of the game (init at 0.5).

GREEDY MOVES

- 1. Look at states that could result from our possible moves.
- 2. Look at VALUE FUNCTION values in those states (expected reward from these states).
- 3. Select action leading to state with highest value (GREEDY MOVE).

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EXPLORATORY MOVES Once in a while, perform a random move (EXPLORATORY MOVE).

Important to force the agent to explore new solutions (avoid local maximum).

LEARNING

Play many games.

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UPDATE

After each move, change the value of the state prior to the move (re-estimate our probability of winning from that state)

s' S

previous state

new state

LEARNING Play many games.

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$$s \longrightarrow s'$$

previous state

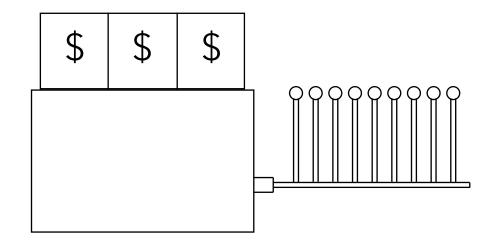
new state

BACK-UP

V(s) = V(s) + a (V(s') - V(s))

a: STEP-SIZE

If a decreases over time, converges to true probabilities of winning.



 SYSTEM
 An *n*-armed "bandit" casino machine.

 Each arm gives a numerical reward sampled from its own stationary probability distribution.

GOAL Find the best way to play (find the best arm).

REMARK Since distributions are stationary, the system is always in the same state. Rewards are not associated with values alone, but with ACTIONS AND VALUES.

VALUE FUNCTION The value function is an ACTION-VALUE FUNCTION.

It gives the expected reward after selecting an action (which arm to pull).

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VALUE FUNCTION The value function is an ACTION-VALUE FUNCTION.

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APPROACH Reinforcement learning with tabular ACTION-VALUE FUNCTION.

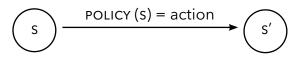
Store in a table the current estimated values of each action.

The true value of an action is the average reward received when this action is selected (i.e. the mean of the arm's stationary distribution).

POLICY (π) It is the fourth basic element of reinforcement learning.

It is a mapping from environment states to actions.

It defines the agent's way of behaving at a given time.



previous state

new state

RETURN It is the expected total reward in the long run.

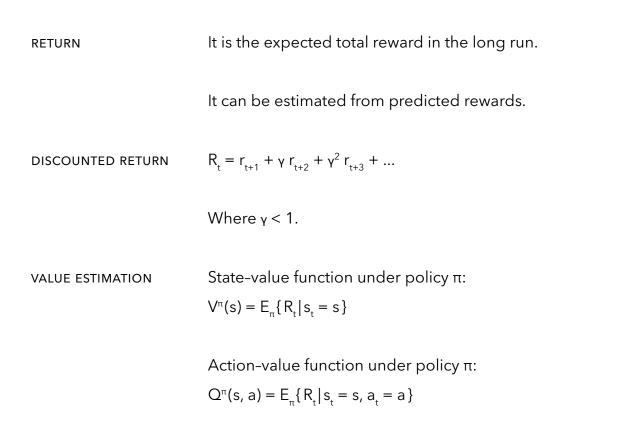
It can be estimated from predicted rewards.

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discounted return $R_t = r_{t+1} + \gamma r_{t+2} + \gamma^2 r_{t+3} + ...$

Where $\gamma < 1$.



KEY IDEA Use of value functions to organize and structure the search for good policies.

POLICY ITERATION Alternate between:

- 1. POLICY EVALUATION: iterative computation of value functions for a given policy.
- 2. POLICY IMPROVEMENT: computation of an improved policy given the value function for that policy.

POLICY EVALUATION Goal: computing the state-value function for a given policy.

BELLMAN OPTIMALITY The value of a state under an optimal policy π^* must equal the expected return FOUATION for the best action from that state under this policy :

 $V^{*}(s) = \max Q^{\pi^{*}}(s, a)$

Where **max** is computed amongst all actions that can be taken from s.

ITERATIVE POLICY Iterative version of Bellman optimality equation.

EVALUATION

The update of V (s) is based on old estimates of V (s) : BOOTSTRAPPING.

 $Q^{\pi}(s, a) > V^{\pi}(s)$

Then we should change the policy π to select action a each time s is encountered.

THEOREM For deterministic policies π and π' ,

if $Q^{\pi}(s, \pi'(s)) \ge V^{\pi}(s)$ (π' would be built from π as explained above)

Then π' must be as good, or better than, π (i.e. $V^{\pi'}(s) \ge V^{\pi}(s)$ for all s)

Policy improvement gives better policies except when the current policy is already optimal.

MONTE CARLO Learn value functions and optimal policies in the form of SAMPLE EPISODES.

(only for EPISODIC TASKS: task for which there exists a final state, e.g. Tic-Tac-Toe)

GENERAL IDEA If an agent:

- 1. follows π and maintains an average of actual returns that have followed each encountered state, the average converges to the STATE-VALUE FUNCTION for policy π .
- maintains an average of actual returns that have followed each action taken from all encountered states, the average converges to the ACTION-VALUE FUNCTION for policy π.

CONSTANT- Q MONTE CARLO	Perform actions until the end of the episode is reached.
INTERPRETATION	At the end of the episode, R _t is known for all t (all rewards are known).
	For all t, update the state-value function with:
	$V(s_t) = V(s_t) + \alpha (R_t - V(s_t))$
	Update V (s _t) towards R _t , which is the average reward received starting from state t in the episode.
	(recall that V (s_t) should be equal to the true average reward received starting from state s_t , which we estimate here in the sample episode by R_t)

TD LEARNING METHODS	Combination of ideas from Monte Carlo and Dynamic Programming.
	They can learn without a model of the environment (like Monte Carlo), through sampling.
	They bootstrap (like Dynamic Programming).
BASIC EXAMPLE	When in state s _{t+1} , update V (s _t) by:
	V (s_t) = V (s_t) + α (r_{t+1} + γ V (s_{t+1}) - V (s_t))
	(note that r_{t+1} is received <i>before</i> reaching state s_{t+1})

SARSA SARSA is an ON-POLICY CONTROL method.

CONTROL: estimating ideal policies through the action-value function.

ON-POLICY: evaluate or improve the policy that is used to make decisions.

UPDATE RULE
$$Q(s_{t'}, a_t) = Q(s_{t'}, a_t) + \alpha(r_{t+1} + \gamma Q(s_{t+1}, a_{t+1}) - Q(s_{t'}, a_t))$$

 $s_{t}^{}$, $a_{t}^{}$, $r_{t+1}^{}$, $s_{t+1}^{}$, $a_{t+1}^{}$: sarsa

Q-LEARNING Q-LEARNING is an OFF-POLICY CONTROL method.

OFF-POLICY: use two different policies. The policy used to generate behavior (BEHAVIOR POLICY) may be unrelated to the policy that is evaluated and improved (ESTIMATION POLICY).

UPDATE RULE
$$Q(s_{t'}, a_{t}) = Q(s_{t'}, a_{t}) + \alpha(r_{t+1} + \gamma \max Q(s_{t+1}, a) - Q(s_{t'}, a_{t}))$$

E.g.:

- 1. Use a EPSILON-GREEDY policy (behavior policy) to select a, from s,
- Update is performed by greedy selection of action a = max Q (s_{t+1}, a).
 Action a_{t+1} is not taken (it will be taken at next iteration following the EPSILON-GREEDY policy).