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# Resource Allocation for Energy Harvesting-Powered D2D Communications Underlying NOMA-Based Networks

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**ABSTRACT** This paper investigates the resource allocation problem in device-to-device (D2D) communications underlying a non-orthogonal multiple access (NOMA)-based cellular network with energy harvesting, where the energy harvesting-powered D2D communications share the downlink resources of the cellular network. To fully exploit the high-data-rate D2D links in this system, a two-phase framework is proposed for D2D users. In particular, the D2D users harvest energy from the base station (BS) in the first phase and then transmit their own information using the harvested energy in the second one. Meanwhile, the D2D communications could cause severe interference to cellular users (CUs) and hence probably ruin the SIC decoding order of the CUs. To deal with this issue, joint power allocation and time scheduling scheme is proposed to maximize the throughput of the D2D links while guaranteeing the quality of service (QoS) for each CU. Through rigorous derivation, the optimal power control and time scheduling parameters are analyzed to simplify the optimization problem formulation. The closed-form optimal solution is derived in some cases. In other cases, a gradient-based algorithm is employed to find an appropriate sub-optimal solution. The simulation results are demonstrated to validate the superiority of the proposed scheme over the conventional orthogonal multiple access (OMA) scheme.

**INDEX TERMS** D2D, NOMA, energy harvesting, resource allocation, cellular networks.

## I. INTRODUCTION

The device-to-device (D2D) communications deployed in wireless cellular networks allow users in close proximity to communicate directly instead of via base stations (BSs), and have been considered as a promising way to alleviate the upcoming traffic pressure on core networks [1]–[3]. The D2D users can share the same spectrum resources with cellular users (CUs) under control of the cellular network, which can effectively improve the spectral efficiency. In general, the overlay and underlay spectrum sharing techniques are commonly used for D2D and cellular communication links [4]. With the overlay spectrum sharing, D2D users can only employ the idle spectrum that are not currently utilized by the CUs, whereas the underlay spectrum sharing technology allows D2D links to reuse the resource of the cellular

links. It can further improve spectral efficiency at the cost of resulting in the co-channel interference between the D2D and cellular links. Therefore, it is important to investigate the resource allocation problems in D2D communications underlying the cellular networks, which have been extensively studied in [5]–[7]. In [5], the authors proposed a power allocation algorithm to maximize the sum rate of D2D links, and guarantee the performance of the cellular link at the same time. Power allocation for both cellular and D2D links was studied to maximize the rate of the single D2D link in [6]. In [7], the authors studied the system with multiple cellular and D2D links.

Apart from invoking the D2D technique to improve the system spectral efficiency, non-orthogonal multiple access (NOMA) is also a promising technology to improve the spectral efficiency, on the standpoint of providing power dimension for multiple access [8], [9]. It is considered as a key

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technology to meet the challenging requirements of the fifth generation (5G) wireless networks. With the aid of NOMA, multiple CUs are allowed to share the same sub-channels via different power levels, and successive interference cancellation (SIC) is adopted at the receivers for decoding [10]. In [11], the authors considered a general downlink NOMA transmission scenario in which the BS communicates with multiple randomly deployed CUs. The power allocation techniques were studied to ensure fairness among the downlink CUs under the constraints of instantaneous and average channel state information (CSI) in [12]. In [13], the authors developed a novel power allocation scheme in the downlink and uplink NOMA scenarios with two users while the strict quality of service (QoS) was guaranteed.

Recently, several approaches have been proposed to combine the D2D communications and NOMA technologies [14]–[17]. In [14], the authors proposed a full-duplex D2D-aided cooperative NOMA scheme to improve the system performance of the NOMA-weaker CU. The D2D users were grouped through the NOMA way in [15] to achieve a better D2D rate performance using sophisticated power control. A D2D aided cooperative relaying system with NOMA was considered in [16], where a power allocation strategy was introduced to achieve the maximum scaling capacity according to the signal-to-noise ratio (SNR) conditions. The power control and channel assignment problem for D2D communications underlying a NOMA-based cellular network was investigated to maximize the sum rate of D2D pairs subject to the minimum rate requirements of the NOMA-based CUs in [17].

It is noted that the system throughput in D2D underlying cellular networks is seriously limited by the battery lifetime budget of users. Hence, in order to prolong the network lifetime, energy harvesting from radio frequency has been applied to D2D underlying cellular networks [18], [19]. In [18], joint time scheduling and power control was considered for a D2D underlying cellular network, where the D2D transmitters were powered by energy harvested from the uplink transmission of CUs and the signal-interference-noise ratio (SINR) requirements of CUs were guaranteed. The resource allocation problem in a D2D underlying NOMA-based cellular network was investigated in [19], where both CUs and D2D users harvested energy from the BS in the downlink and transmitted their information in the uplink. Both [18] and [19] considered the communication scenarios that the D2D pairs reused the uplink spectrum of the CUs for the transmission. In such cases, the BS performs the SIC decoding according to the uplink SINR of the CUs. When the D2D users reutilize the downlink spectrum with NOMA-enabled CUs, the SIC decoding at the receiver of each CU becomes complicated, since the excessive co-channel interference from the D2D link may change the relative SINR at each CU and probably destroy the original SIC decoding order of the CUs. How to protect the SIC decoding order of the CUs subject to the co-channel interference should be carefully considered.

Motivated by the above works, we consider a joint power control and time scheduling problem for the D2D pair underlying NOMA-based cellular networks with energy harvesting. Our target is to maximize the throughput of the D2D communication while the minimum rate requirements of the CUs are strictly guaranteed. By power control and time scheduling, the D2D users can efficiently reuse the downlink spectrum of CUs without causing any trouble to CUs that employ NOMA and SIC decoding techniques. In particular, the contribution of this paper is three-fold:

- A joint power allocation and time scheduling problem is properly formulated to maximize the throughput of the D2D link while guaranteeing the minimum rate requirement for each CU.
- The corresponding resource optimization problem is mathematically solved. First, the optimal power control and time scheduling parameters are analyzed to simplify the optimization problem formulation through rigorous derivation. Second, the closed-form optimal solution is derived in some cases. In the other cases, a sub-optimal solution with low complexity by employing the gradient algorithm is obtained.
- The conventional orthogonal multiple access (OMA) scheme is provided as a benchmark. The simulation results show that the proposed scheme outperforms the OMA scheme.

The rest of this paper is organized as follows. In Section II, we introduce the system model and formulate the problem of joint power control and time scheduling. The formulated problem is analyzed and solved to find the optimal solution in Section III. In Section IV, the conventional OMA scheme is described. Section V presents the simulation results and the conclusions are drawn in Section VI.

## II. SYSTEM MODEL AND PROBLEM FORMULATION

Consider a NOMA-based cellular network with one BS communicating with  $K$  CUs ( $U_i, i \in \mathcal{K} = \{1, \dots, K\}$ ). The CUs are uniformly distributed in a disc with radius  $D$ , and the BS is located in the center. There exists one pair of D2D users that can utilize the downlink spectrum resource of the CUs. We assume that all the users and the BS are equipped with one single antenna. A two-phase transmission framework with time interval of  $T$  seconds is adopted. The BS serves all the CUs by employing the NOMA-based scheme in both two phases, whereas the D2D transmitter (DTX) harvests energy from the BS in the first phase and communicates with the D2D receiver (DRX) during the second phase. The lengths of the two phases are denoted by  $\tau_e$  and  $\tau_t$ , respectively. The time intervals  $\tau_e$  and  $\tau_t$  should satisfy

$$\tau_e + \tau_t \leq T. \quad (1)$$

In this paper, we assume that the perfect CSI is available and constant during each framework. Define  $h_i$ ,  $h_D$ ,  $h_{B,D_i}$ ,  $h_{B,D_r}$  and  $h_{D,i}$  as the channel from the BS to the  $i$ -th CU, from the DTX to the DRX, from the BS to the DTX, from the BS to

the DRX, and from the DTX to the  $i$ -th CU, respectively. The background noise is modeled as the additive white Gaussian noise (AWGN) with zero mean and variance  $\sigma^2$ . Without loss of generality, we assume  $|h_1| \geq |h_2| \geq \dots \geq |h_K|$ . Hence, based on the principle of the SIC process, the cellular user  $U_i$  can successfully decode and remove the interference from  $U_j$  for any  $j > i$ .

In the first phase, the composite transmit signal  $x_B^1$  from the BS can be expressed as

$$x_B^1 = \sum_{k=1}^K \sqrt{\omega_k P_B} s_k, \quad (2)$$

where  $s_k$  is the transmit signal for  $U_k$ ,  $P_B$  is the total transmit power of the BS,  $\omega_k$  is the power allocation coefficient for  $U_k$ , and  $\omega = [\omega_1, \dots, \omega_K]$  is the power allocation vector. We assume that the BS broadcasts the signal  $x_B^1$  with its maximum transmit power  $P_B$  to maximize the spectrum efficiency, namely

$$\sum_{k=1}^K \omega_k = 1. \quad (3)$$

At the receiver side, following the principle of NOMA, each cellular user  $U_i$  can successfully decode the signal of  $U_j$  ( $j > i$ ), treating the signals of  $U_1, U_2, \dots, U_{j-1}$  as interferences. Accordingly, the received SINR at  $U_i$  for decoding the signal  $s_j$  ( $j > i$ ) is given by

$$SINR_{i,j}^1 = \frac{\omega_j |h_i|^2 \rho_B}{\sum_{k=1}^{j-1} \omega_k |h_i|^2 \rho_B + 1}, \quad (4)$$

where  $\rho_B = \frac{P_B}{\sigma^2}$  is the transmit signal-to-noise ratio (SNR) at the BS. Since  $|h_i| > |h_j|$  ( $i < j$ ),  $SINR_{j,j}^1 < SINR_{i,j}^1$  holds for any  $j > i$ .

Meanwhile, the DTX harvests energy from the BS when it transmits with power  $P_B$ . The total amount of energy harvested by the DTX in the first phase can be calculated as

$$E_D^h = \tau_e \eta P_B |h_{B,D_t}|^2, \quad (5)$$

where  $\eta$  is the energy transformation efficiency.

In the second phase, the transmit signal  $x_B^2$  from the BS can be accordingly expressed as

$$x_B^2 = \sum_{k=1}^K \sqrt{\alpha_k P_B} s_k, \quad (6)$$

where  $\alpha_k$  is the power allocation coefficient for  $U_k$ , and  $\alpha = [\alpha_1, \dots, \alpha_K]$  is the power allocation vector. Then  $\alpha$  should satisfy

$$\sum_{k=1}^K \alpha_k \leq 1, \quad \alpha_k \geq 0, \quad \forall k \in \mathcal{K}. \quad (7)$$

At the same time, the DTX utilizes the harvested energy to transmit information with power  $p_D$  over the downlink spectrum. For the DTX, energy consumption should not exceed

the harvested energy

$$\tau_e p_D^e + \tau_i p_D + \tau_i p_D^i \leq E_D^h, \quad (8)$$

where  $p_D^e$  and  $p_D^i$  denote the constant circuit power in the first and second phases. In practice, considering the fact that the circuits of signal processing and transmission are more complex than those of energy harvesting [19], we set  $p_D^i > p_D^e$ .

The received SINR at the DRX can be calculated as

$$SINR_D^2 = \frac{|h_D|^2 \rho_D}{\sum_{k=1}^K \alpha_k |h_{B,D_r}|^2 \rho_B + 1}, \quad (9)$$

where  $\rho_D = \frac{p_D}{\sigma^2}$  is the transmit SNR at the DTX. Meanwhile, each cellular user suffers interferences from the DTX and other cellular users. Similarly, when SIC is adopted with the same decoding sequence at each cellular user  $U_i$ , the received SINR for decoding the signal  $s_j$  ( $j > i$ ) is expressed as

$$SINR_{i,j}^2 = \frac{|h_i|^2 \alpha_j \rho_B}{\sum_{k=1}^{j-1} \alpha_k |h_i|^2 \rho_B + |h_{D,i}|^2 \rho_D + 1}. \quad (10)$$

To decode the signal  $s_j$  successfully, the received SINR at  $U_i$  should be no less than the received SINR at  $U_j$  itself, i.e.,  $SINR_{i,j}^2 \geq SINR_{j,j}^2$  ( $j > i$ ). From (10), we have

$$\frac{|h_{D,i}|^2 \rho_D + 1}{|h_i|^2} \leq \frac{|h_{D,j}|^2 \rho_D + 1}{|h_j|^2}, \quad K \geq j > i \geq 1. \quad (11)$$

Note that the inequalities in (11) can be equivalently expressed as

$$\frac{|h_{D,i}|^2 \rho_D + 1}{|h_i|^2} \leq \frac{|h_{D,i+1}|^2 \rho_D + 1}{|h_{i+1}|^2}, \quad K - 1 \geq i \geq 1. \quad (12)$$

According to the theory of Shannon capacity, we can obtain the achievable rates of  $U_i$  in the two phases, and the achievable rate of the D2D link in the second phase as

$$\begin{aligned} R_i^1 &= \log_2(1 + SINR_{i,i}^1), \\ R_i^2 &= \log_2(1 + SINR_{i,i}^2), \\ R_D^2 &= \log_2(1 + SINR_D^2), \end{aligned} \quad (13)$$

where the bandwidth is normalized. Meanwhile, the minimum rate requirements of the CUs should be guaranteed for both two phases, namely

$$R_i^1 \geq \gamma_i, \quad R_i^2 \geq \gamma_i, \quad \forall i \in \mathcal{K}, \quad (14)$$

where  $\gamma_i$  denotes the target rate of  $U_i$ .

To maximize the throughput of the D2D communication under the constraint of the QoS for each CU, we can formulate a resource allocation problem as follows

$$\max_{\tau_e, \tau_i, \alpha, \omega, \rho_D} U_D = \tau_i R_D^2, \quad (15a)$$

$$\text{s.t. (1), (3), (7), (8), (12), (14)}. \quad (15b)$$

Problem (15) is a non-convex optimization problem, since its objective and constraints are both non-convex functions of the

variables. To make it tractable, we then analyze the optimal solution to (15), and reformulate a simplified optimization problem just with variables  $\rho_D$  and  $\tau_t$  in the next section.

### III. ANALYTICAL FRAMEWORK

In this section, we first discuss the relationship among the variables so as to simplify the constraints of (15). Then, the original optimization problem (15) can be reformulated as an optimization problem just with  $\rho_D$  and  $\tau_t$  being the variables. Finally, the optimal solution can be obtained in two different scenarios according to the feasible values of  $\tau_t$ .

#### A. PROBLEM REFORMULATION

First, from (4) and (10), we can see that  $R_i^1 > R_i^2$  for  $\omega = \alpha$ . Therefore, if  $\alpha^*$  satisfies  $R_i^2 \geq \gamma_i$  for all  $i \in \mathcal{K}$ , we can set  $\omega_1^* = 1 - \sum_{k=2}^K \omega_k^*$ ,  $\omega_2^* = \alpha_2^*$ ,  $\dots$ ,  $\omega_K^* = \alpha_K^*$ , which means that  $\omega^*$  naturally satisfies  $R_i^1 \geq \gamma_i$  for all  $i \in \mathcal{K}$ . Hence, the constraint (14) can be recast as

$$R_i^2 \geq \gamma_i, \quad \forall i \in \mathcal{K}. \quad (16)$$

Accordingly, the problem (15) can be equivalently written as

$$\max_{\tau_e, \tau_t, \alpha, \rho_D} U_D = \tau_t R_D^2, \quad (17a)$$

$$\text{s.t. (1), (7), (8), (12), (16).} \quad (17b)$$

Next, we analyze the optimal solution to (17), and reformulate a simplified problem just with variables  $\rho_D$  and  $\tau_t$ .

*Theorem 1: The optimal solution of problem (17) can be obtained when the equalities in constraints (1) and (16) hold, namely*

$$\tau_e^* + \tau_t^* = T, \quad (18)$$

$$R_i^{2*} = \gamma_i, \quad \forall i \in \mathcal{K}. \quad (19)$$

*Proof:* See Appendix A. ■

From (19), the optimal power allocation vector  $\alpha$  can be obtained by the following theorem.

*Theorem 2: The optimal  $\alpha^*$  can be derived as*

$$\alpha_i^* = \frac{\sum_{j=1}^{i-1} \left\{ \left[ \prod_{t=j+1}^{i-1} (1 + \phi_t) \right] \phi_i \phi_j (\delta_j \rho_D^* + \theta_j) \right\} + \phi_i (\delta_i \rho_D^* + \theta_i)}{\rho_B}, \quad (20)$$

where  $\phi_i = 2^{\gamma_i} - 1$ ,  $\delta_i = \frac{|h_{D,i}|^2}{|h_i|^2}$ ,  $\theta_i = \frac{1}{|h_i|^2}$ ,  $\forall i \in \mathcal{K}$ . Note that

$$\sum_{j=1}^{i-1} \left\{ \left[ \prod_{t=j+1}^{i-1} (1 + \phi_t) \right] \phi_i \phi_j (\delta_j \rho_D^* + \theta_j) \right\} = 0 \text{ for } i = 1, \text{ and}$$

$$\prod_{t=j+1}^{i-1} (1 + \phi_t) = 1 \text{ for } j + 1 > i - 1.$$

*Proof:* See Appendix B. ■

*Theorem 2* represents the relationship between the optimal  $\alpha_i^*$  and  $\rho_D^*$ . Then, from *Theorem 2* and its proof, we can analyze the feasible region of variable  $\rho_D$ . By substituting (20),

we define  $H(\rho_D) = \sum_{i=1}^K \alpha_i = \frac{\sum_{j=1}^K \left\{ \left[ \prod_{t=j+1}^K (1 + \phi_t) \right] \phi_j (\delta_j \rho_D + \theta_j) \right\}}{\rho_B} = \bar{A} \rho_D + \bar{B}$ , where  $\bar{A} = \frac{\sum_{j=1}^K \left\{ \left[ \prod_{t=j+1}^K (1 + \phi_t) \right] \phi_j \delta_j \right\}}{\rho_B}$ , and  $\bar{B} = \frac{\sum_{j=1}^K \left\{ \left[ \prod_{t=j+1}^K (1 + \phi_t) \right] \phi_j \theta_j \right\}}{\rho_B}$ . Due to the fact that  $\phi_i > 0$ ,  $\delta_i > 0$ ,  $\theta_i > 0$ ,  $\forall i \in \mathcal{K}$ , we can easily conclude that  $\bar{A} > 0$ ,  $\bar{B} > 0$ , and  $H(\rho_D)$  increases linearly with  $\rho_D$ .

*Remark 1:* From the inequality (7), we have  $\bar{A} \rho_D + \bar{B} \leq 1$ , and equivalently

$$0 \leq \rho_D \leq \frac{1 - \bar{B}}{\bar{A}}. \quad (21)$$

Recall that Eq. (12) can be expressed as

$$(\delta_i - \delta_{i+1}) \rho_D \leq \theta_{i+1} - \theta_i, \quad 1 \leq i \leq K - 1. \quad (22)$$

This inequality (22) naturally holds if  $\delta_i \leq \delta_{i+1}$ . Otherwise, the power variable  $\rho_D$  satisfies  $0 \leq \rho_D \leq \frac{\theta_{i+1} - \theta_i}{\delta_i - \delta_{i+1}}$ .

Combing (21) and (22), we can further obtain

$$0 \leq \rho_D \leq \min \left\{ \frac{1 - \bar{B}}{\bar{A}}, \min_{j \in \mathcal{I}} \frac{\theta_{j+1} - \theta_j}{\delta_j - \delta_{j+1}} \right\}, \quad (23)$$

where  $\mathcal{I} = \{i | \delta_i > \delta_{i+1}, 1 \leq i \leq K - 1\}$ .

Furthermore, we discuss the relationship between the variables  $\tau_t$  and  $\rho_D$ . By substituting (18) into (8), we have

$$0 \leq \tau_t \rho_D \leq \bar{D} - \bar{C} \tau_t, \quad (24)$$

where  $\rho_D^e = \frac{p_D^e}{\sigma^2}$ ,  $\rho_D^t = \frac{p_D^t}{\sigma^2}$ ,  $\bar{C} = \rho_D^t - \rho_D^e + \eta \rho_B |h_{B,D_r}|^2$ , and  $\bar{D} = T \eta \rho_B |h_{B,D_r}|^2 - T \rho_D^e$ . As  $\rho_D^t > \rho_D^e$ , we can conclude that  $\bar{C} > 0$ , and  $\bar{D} - \bar{C} \tau_t$  decreases with  $\tau_t$ .

Based on the above analysis, the resource optimization problem (17) is reduced to the following one

$$\max_{\tau_t, \rho_D} U_D = \tau_t \log_2 \left( 1 + \frac{|h_D|^2 \rho_D}{\bar{E} \rho_D + \bar{F}} \right), \quad (25a)$$

$$\text{s.t. (23), (24),} \quad (25b)$$

where  $\bar{E} = \bar{A} |h_{B,D_r}|^2 \rho_B$ , and  $\bar{F} = \bar{B} |h_{B,D_r}|^2 \rho_B + 1$ . In this problem (25), the variables  $\rho_D$  and  $\tau_t$  are still deeply coupled. In the sequel, we discuss the optimal solution by dividing the feasible region of  $\tau_t$  into two sub-intervals.

#### B. THE OPTIMAL SOLUTION TO PROBLEM (25)

First, the feasible conditions of problem (25) are provided.

*Theorem 3: The optimization problem (25) is feasible if and only if  $\bar{B} \leq 1$  and  $\eta \rho_B |h_{B,D_r}|^2 \geq \rho_D^e$ .*

*Proof:* From Eq. (21), we have  $\frac{1 - \bar{B}}{\bar{A}} \geq 0$ , and equivalently  $\bar{B} \leq 1$ . Meanwhile, from Eq. (24), we can conclude that  $\bar{D} - \bar{C} \tau_t \geq 0$  should be strictly guaranteed. Hence, we should set  $\bar{D} \geq 0$ , namely  $\eta \rho_B |h_{B,D_r}|^2 \geq \rho_D^e$ . ■

Next, the range of  $\tau_t$  is divided into two intervals to simplify the constraint (25b). Combing (23) and (24), if  $\bar{D} - \bar{C} \tau_t \geq \rho_D^{\max} \tau_t$ , namely  $0 \leq \tau_t \leq \frac{\bar{D}}{\bar{C} + \rho_D^{\max}}$ , the constraint (25b) can be reduced as  $0 \leq \rho_D \leq \rho_D^{\max}$ . Otherwise, if  $0 \leq$

$\bar{D} - \bar{C}\tau_t \leq \rho_D^{max} \tau_t$ , namely  $\frac{\bar{D}}{\bar{C} + \rho_D^{max}} \leq \tau_t \leq \frac{\bar{D}}{\bar{C}}$ , the constraint (25b) becomes  $0 \leq \rho_D \leq \frac{\bar{D} - \bar{C}\tau_t}{\tau_t}$ . Hence, the optimal solution of (25) can be achieved in the following two cases:

1) CASE I ( $0 \leq \tau_t \leq \frac{\bar{d}}{\bar{c} + \rho_D^{max}}$ )

For this case, the constraint (25b) can be simplified as

$$0 \leq \rho_D \leq \rho_D^{max}, \quad 0 \leq \tau_t \leq \frac{\bar{D}}{\bar{C} + \rho_D^{max}}. \quad (26)$$

Referring to (25a), we can obtain that  $U_D$  increases with both  $\rho_D$  and  $\tau_t$ . Therefore, the optimal solution of (25) can be easily achieved as  $\rho_{D,1}^* = \rho_D^{max}$ ,  $\tau_{t,1}^* = \frac{\bar{D}}{\bar{C} + \rho_D^{max}}$ . The corresponding throughput of the D2D communication is  $U_{D,1}^* = \tau_{t,1}^* \log_2(1 + \frac{|h_D|^2 \rho_{D,1}^*}{E \rho_{D,1}^* + F})$ .

2) CASE II ( $\frac{\bar{d}}{\bar{c} + \rho_D^{max}} \leq \tau_t \leq \frac{\bar{d}}{\bar{c}}$ )

For this case, the constraint (25b) can be reduced as

$$0 \leq \rho_D \leq \frac{\bar{D} - \bar{C}\tau_t}{\tau_t}, \quad \frac{\bar{D}}{\bar{C} + \rho_D^{max}} \leq \tau_t \leq \frac{\bar{D}}{\bar{C}}. \quad (27)$$

As  $U_D$  increases with  $\rho_D$ , we set the optimal  $\rho_{D,2}^*$  as  $\frac{\bar{D} - \bar{C}\tau_t}{\tau_t}$ . Then the optimization problem (25) can be rewritten as

$$\max_{\tau_t} U_D(\tau_t) = \tau_t \log_2\left(\frac{m_1 \tau_t + n_1}{m_2 \tau_t + n_2}\right), \quad (28a)$$

$$\text{s.t.} \quad \frac{\bar{D}}{\bar{C} + \rho_D^{max}} \leq \tau_t \leq \frac{\bar{D}}{\bar{C}}. \quad (28b)$$

where  $m_1 = \bar{F} - \bar{C}\bar{E} - \bar{C}|h_D|^2$ ,  $n_1 = \bar{D}\bar{E} + \bar{D}|h_D|^2$ ,  $m_2 = \bar{F} - \bar{C}\bar{E}$ , and  $n_2 = \bar{D}\bar{E}$ .

It is still difficult to obtain the closed-form optimal solution to (28) because the property of function  $U_D(\tau_t)$  depends on the parameters ( $m_1, m_2, n_1$  and  $n_2$ ). In some cases as presented in the following theorems, the objective function  $U_D(\tau_t)$  is either a concave one or monotone. Thus, the optimal solution of problem (28) can be easily found.

**Theorem 4:** If the parameters  $m_1, m_2, n_1$  and  $n_2$  satisfy one of the following two constraints, the function  $U_D(\tau_t)$  is concave and the problem (28) becomes a convex optimization problem, whose optimal solution can be obtained by using mature algorithms: i)  $m_1 n_2 + m_2 n_1 \geq 0$ ; ii)  $m_1 n_2 + m_2 n_1 < 0$  and  $\frac{\bar{D}(m_1 n_2 + m_2 n_1)}{\bar{C}} + 2n_1 n_2 \geq 0$ .

*Proof:* See Appendix C. ■

**Theorem 5:** Assuming that i)  $\bar{F} - \bar{C}\bar{E} < 0$  ii) the circuit power consumption is small enough compared to the transmit power consumption, namely  $\rho_D^e = \rho_D^t = 0$ , we can derive that  $U_D(\tau_t)$  in Eq. (28a) increases with  $\tau_t$ , and the optimal solution is  $\tau_{t,2}^* = \frac{\bar{D}}{\bar{C}}$ .

*Proof:* See Appendix D. ■

For the general cases, as the derivation of  $U_D(\tau_t)$  with respect to  $\tau_t$  exists, we can always find a sub-optimal solution by employing the gradient method [21], as shown in Algorithm 1. In this algorithm,  $\epsilon$  is an accuracy control parameter,  $\Delta$  is the step size,  $G = \nabla U_D(x) =$

$\frac{1}{\ln 2} \left[ \ln\left(\frac{m_1 x + n_1}{m_2 x + n_2}\right) + x\left(\frac{m_1}{m_1 x + n_1} - \frac{m_2}{m_2 x + n_2}\right) \right]$ . Note that if there exists at most one saddle point for  $U_D(\tau_t)$  in the interval  $[\frac{\bar{D}}{\bar{C} + \rho_D^{max}}, \frac{\bar{D}}{\bar{C}}]$ , the solution  $\tau_{t,2}^*$  obtained from the Algorithm 1 is indeed the optimal solution of the problem (28). Correspondingly,  $\rho_{D,2}^* = \frac{\bar{D} - \bar{C}\tau_{t,2}^*}{\tau_{t,2}^*}$ , and  $U_{D,2}^* = \tau_{t,2}^* \log_2(1 + \frac{|h_D|^2 \rho_{D,2}^*}{E \rho_{D,2}^* + F})$ .

In summary, the optimal solution of (25) can be achieved as  $(\rho_D^*, \tau_t^*) = \begin{cases} (\rho_{D,1}^*, \tau_{t,1}^*), & \text{if } U_{D,1}^*(\rho_{D,1}^*, \tau_{t,1}^*) \geq U_{D,2}^*(\rho_{D,2}^*, \tau_{t,2}^*) \\ (\rho_{D,2}^*, \tau_{t,2}^*), & \text{otherwise} \end{cases}$ .

**Algorithm 1** Searching for the Optimal Time Scheduling Parameter  $\tau_t^*$

**Input:**

$\{h_i, h_{D,i}, \gamma_i, i = 1, \dots, K\}, h_D, h_{B,D_t}, h_{B,D_r}, T, P_B, \sigma^2, \eta, p_D^t, p_D^e, \Delta, \epsilon;$

**Output:**

$\tau_t^*;$

- 1: Initialization:  $\tau_t^p = \frac{\bar{D}}{\bar{C} + \rho_D^{max}} + \epsilon, \tau_t = \frac{\bar{D}}{\bar{C} + \rho_D^{max}};$
- 2: Calculate  $m_1, m_2, n_1$ , and  $n_2;$
- 3: **while**  $|\tau_t - \tau_t^p| \geq \epsilon$  **do**
- 4:   Set  $\tau_t^p = \tau_t;$
- 5:   Calculate  $\tau_t = \tau_t^p + \Delta * G;$
- 6:   **if**  $\tau_t > \frac{\bar{D}}{\bar{C}}$  **then**
- 7:     Set  $\tau_t = \frac{\bar{D}}{\bar{C}};$
- 8:   **end if**
- 9:   **if**  $\tau_t < \frac{\bar{D}}{\bar{C} + \rho_D^{max}}$  **then**
- 10:     Set  $\tau_t = \frac{\bar{D}}{\bar{C} + \rho_D^{max}};$
- 11:   **end if**
- 12: **end while**
- 13: **return**  $\tau_t^* = \tau_t;$

**IV. THE OMA SCHEME**

In this section, the conventional OMA scheme is investigated. For comparison, we adopt the orthogonal frequency division multiple access (OFDMA) system as the benchmark. As to the OFDMA scheme, a two-phase transmission framework is also introduced. The process for the first phase is same with that in the NOMA-based scheme, while for the second phase, the total bandwidth is equally divided into  $K$  units and each CU is only allowed to access single unit. Then the energy consumption constraint of the DTX can be expressed as

$$(T - \tau_t^o) p_D^e + \tau_t^o p_D^o + \tau_t^o p_D^t \leq (T - \tau_t^o) \eta P_B |h_{B,D_t}|^2. \quad (29)$$

Furthermore, the SINR at the  $U_i$  and DRX during the second phase can be respectively calculated as

$$SINR_i^2 = \frac{\alpha_i^o |h_i|^2 \rho_B}{|h_{D,i}|^2 \rho_D^o + 1}, \quad SINR_{D,i}^2 = \frac{|h_D|^2 \rho_D^o}{(\sum_{i=1}^K \alpha_i^o) |h_{B,D_r}|^2 \rho_B + 1}, \quad (30)$$

where  $\alpha_i^o$  should satisfy

$$\sum_{i=1}^K \alpha_i^o \leq 1, \alpha_i^o \geq 0, \forall i \in \mathcal{K}. \quad (31)$$

Correspondingly, the transmission rate of  $U_i$  during the second phase should be guaranteed, namely

$$R_i^2 = \frac{1}{K} \log_2(1 + SINR_i^2) \geq \gamma_i. \quad (32)$$

To maximize the achievable throughput of the DTX, the resource allocation problem can be formulated as

$$\max_{\alpha^o, \rho_B^o, \tau_i^o} U_D = \tau_i^o R_{D,i}^2, \quad (33a)$$

$$\text{s.t. (29), (31), (32)}. \quad (33b)$$

Similarly, by holding the equalities in the constraint (32), the problem (33) can be equally recast as

$$\max_{\tau_i^o, \rho_D^o} U_D = \tau_i^o \log_2(1 + \frac{|h_D|^2 \rho_D^o}{\bar{E}^o \rho_D^o + \bar{F}^o}), \quad (34a)$$

$$0 \leq \tau_i^o \rho_D^o \leq \bar{D} - \bar{C} \tau_i^o, \quad (34b)$$

$$0 \leq \rho_D^o \leq \frac{1 - \bar{B}^o}{\bar{A}^o}. \quad (34c)$$

where  $\phi_i^o = 2^{K\gamma_i} - 1$ ,  $\bar{A}^o = \frac{\sum_{i=1}^K \phi_i^o \delta_i}{\rho_B}$ ,  $\bar{B}^o = \frac{\sum_{i=1}^K \phi_i^o \theta_i}{\rho_B}$ ,  $\bar{E}^o = \bar{A}^o |h_{B,Dr}|^2 \rho_B$ , and  $\bar{F}^o = \bar{B}^o |h_{B,Dr}|^2 \rho_B + 1$ .

The problem (34) is similar to the problem (25), and the optimal solution of (34) can be achieved by applying the same algorithm analyzed in the NOMA-based scheme.

### V. NUMERICAL RESULTS

In this section, numerical results are presented to evaluate the performance of our proposed NOMA-based scheme. The cell is a 100m × 100m disc with BS being located in the center. The maximum distance between the D2D transmitter and receiver is 10m. Meanwhile, the channel is modeled as  $h = g d^{-\frac{\beta}{2}}$ , where  $g$  is the Rayleigh fading channel coefficient,  $d$  is the distance, and  $\beta$  is the path loss exponent. We assume that  $g$  follows complex normal distribution with zero mean and unit variance, namely  $g \sim \mathcal{CN}(0, 1)$ . The detailed system parameters setting are presented in Table 1. Note that all

TABLE 1. Simulation parameters.

Parameter	Value
$D$ (radius of the disc)	100 m
$K$ (number of cellular users)	4
$\beta$ (path loss exponent)	2
$p_D^e$ (circuit power consumption for the energy-harvesting)	5 mW
$p_D^t$ (circuit power consumption for the transmitting)	10 mW
$\sigma^2$ (noise power)	$2 * 10^{-6}$ W
$P_B$ (BS's transmit power)	2 W
$\eta$ (energy transformation efficiency)	0.9
$T$ (time of one frame)	10 s
$\gamma_i = \gamma_{th}, \forall i \in \mathcal{K}$ (rate requirement of CUs)	0.1 bps/Hz
$\epsilon$ (accuracy control parameter)	$10^{-7}$
$\Delta$ (step size)	Backtracking line search

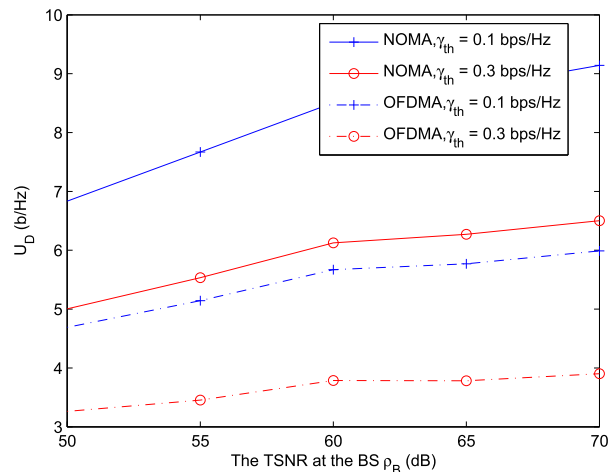


FIGURE 1. The relationship between  $U_D$  and  $\rho_B$ .

the numerical results are acquired by averaging over  $10^6$  realizations.

Fig. 1 investigates the relationship between the DTX's throughput  $U_D$  and the transmit SNR (TSNR)  $\rho_B$ . The observations are threefold. First, the throughputs  $U_D$  of both the NOMA and OFDMA schemes increases with  $\rho_B$  and decreases with  $\gamma_{th}$ , which can be easily explained as follows. From (23) and (24), a larger  $\rho_B$  and smaller  $\gamma_{th}$  expand the feasible range of the variable  $\rho_D$ , and thus leading to a higher throughput  $U_D$ . Second, the throughput  $U_D$  of the NOMA-based scheme is larger than that of the OFDMA scheme, which demonstrates the superiority of our proposed NOMA-based scheme over the traditional OMA scheme. The reason lies on that all the CUs and the D2D pair can share the entire spectrum resource for the NOMA-based scheme, which greatly improves the spectrum efficiency. Particularly, when  $\rho_B = 70$  dB and  $\gamma_{th} = 0.1$  bps/Hz, our proposed NOMA-based scheme can achieve 50% throughput gain over the OFDMA scheme. Third, the throughput gap between the NOMA and OFDMA schemes increases with  $\rho_B$ . This means that the advantage of our proposed NOMA-based scheme is more obvious when the SNR  $\rho_B$  becomes larger.

Fig. 2 presents the curves of the throughput  $U_D$  vs  $\gamma_{th}$ . Similar to Fig. 1, the D2D throughput decreases with the SNR threshold  $\gamma_{th}$ , since the D2D transmit power should be lowered to reduce interference to the CUs in this case. Again, thanks to the advantage of NOMA, our proposed scheme can achieve 20% throughput gain over the OFDMA scheme especially when  $\rho_B = 70$  dB and  $\gamma_{th} = 0.6$  bps/Hz.

Fig. 3 illustrates how the D2D throughput  $U_D$  changes with the number of CUs that share the same spectrum simultaneously. The throughputs of the two schemes both decrease with  $K$ , since the feasible region of the SNR at the D2D transmitter  $\rho_D$  becomes narrower when the number of CUs  $K$  increases. Furthermore, our proposed scheme outperforms the OFDMA scheme for  $K \leq 5$ , and is inferior to the OFDMA scheme for  $K > 5$ . The reason lies on that the scenario with large

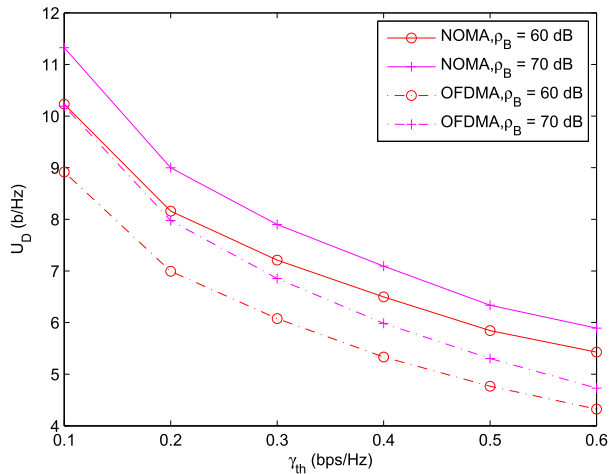


FIGURE 2. The relationship between  $U_D$  and  $\gamma_{th}$ .

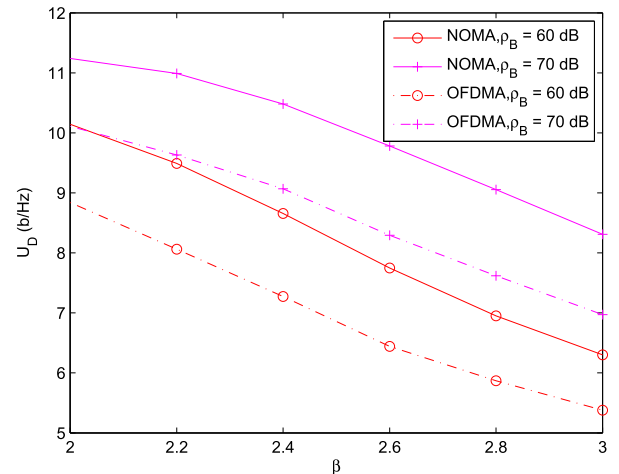


FIGURE 4. The relationship between  $U_D$  and  $\beta$ .

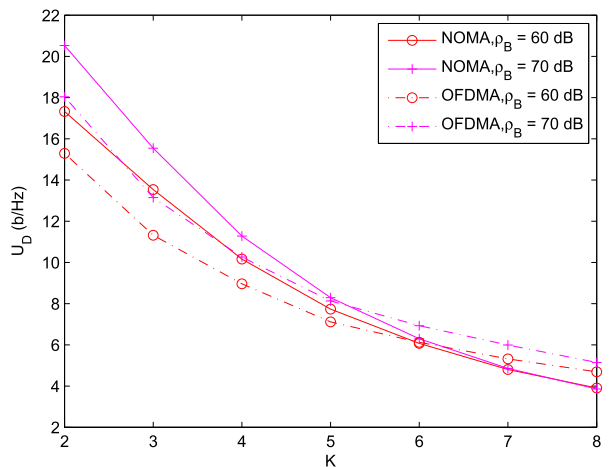


FIGURE 3. The relationship between  $U_D$  and  $K$ .

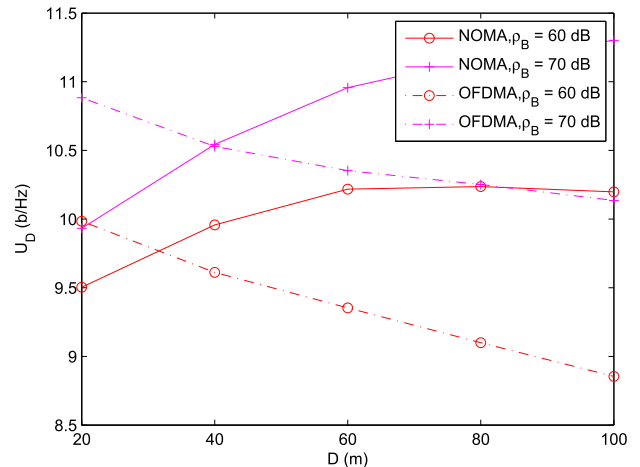


FIGURE 5. The relationship between  $U_D$  and  $D$ .

$K$  is typically interference-limited while that with small  $K$  is bandwidth-limited. Thus, the OFDMA scheme achieves better performance due to the proper interference cancellation among the cellular users under the large  $K$ , and the NOMA-based scheme shows advantages under the small  $K$  due to the fact that all cellular users can share the entire spectrum resource.

Fig. 4 analyzes the relationship between the throughput  $U_D$  and  $\beta$ . It is easy to find that the throughputs of both two schemes decrease with  $\beta$ . As  $\beta$  gets large, the path loss becomes severe, leading to a small  $U_D$ . Meanwhile, our proposed NOMA-based scheme shows great advantages over the OFDMA scheme. In particular, when  $\rho_B = 70$  dB and  $\beta = 2$ , the throughput of the NOMA-based scheme is almost 10 percentage higher than that of the OFDMA scheme.

Fig. 5 shows the relationship between the throughput  $U_D$  and  $D$ . A surprising observation is that the throughput of the NOMA-based scheme increases with  $D$  while that of the OFDMA scheme decreases with  $D$ , which can be explained as follows. The performance loss of large  $D$  results from the

increasing path loss, and the performance gain of large  $D$  benefits from the interference decrement between the DTX and the CUs, and between the BS and the DRX. The interference decrement is dominated for the NOMA-based scheme while the path loss is dominated for the OFDMA scheme. Meanwhile, we can conclude that the NOMA-based scheme shows great advantages over the OFDMA scheme for  $D \geq 40$  m. Particularly, when  $D = 100$  m and  $\rho_B = 70$  dB, the throughput of the NOMA-based scheme is nearly 10 percentage larger than that of the OFDMA scheme.

## VI. CONCLUSION

In this paper, we have studied the resource optimization problem of a D2D underlying NOMA-based cellular network with energy harvesting. The throughput of the D2D communication is maximized while the minimum rate requirement of each cellular user is guaranteed. We derived the optimal conditions for power control of cellular users and time allocation of energy harvesting, and achieved the optimal solution by solving the simplified optimization problem

under some cases. Otherwise, a suboptimal power control and time scheduling solution is found using a gradient-based algorithm. Simulation results show that our proposed NOMA-based scheme yields larger throughput than the corresponding OFDMA scheme.

**APPENDIX A**

**PROOF OF THEOREM 1**

First, the optimal solution of (17) satisfies  $\tau_e^* + \tau_t^* = T$ , which can be demonstrated by the contradiction method. Here we assume that  $\tau_e^* + \tau_t^* < T$ , and constraints (7), (8), (12), (16) are all guaranteed. Then we can construct a new solution  $(\bar{\tau}_e, \bar{\tau}_t, \bar{\alpha}, \bar{p}_D)$  as  $\bar{\tau}_e = \frac{T\tau_e^*}{\tau_e^* + \tau_t^*}$ ,  $\bar{\tau}_t = \frac{T\tau_t^*}{\tau_e^* + \tau_t^*}$ ,  $\bar{\alpha} = \alpha^*$ , and  $\bar{p}_D = p_D^*$ . Therefore, it is easy to see  $R_D^2(\bar{\alpha}, \bar{p}_D) = R_D^2(\alpha^*, p_D^*)$ . From (17a), as  $\bar{\tau}_t > \tau_t^*$ , we can easily conclude that  $U_D(\bar{\tau}_e, \bar{\tau}_t, \bar{\alpha}, \bar{p}_D) > U_D(\tau_e^*, \tau_t^*, \alpha^*, p_D^*)$ , which contradicts our assumption.

Second, we show that the optimal solution of problem (17) satisfies (19). In the similar way, we assume that for the optimal solution  $(\tau_e^*, \tau_t^*, \alpha^*, p_D^*)$ , constraints (1), (7), (8), (12) are all satisfied, and there exists at least one inequality in (16). Without loss of generality, we set  $R_k^2(\alpha^*, p_D^*) > \gamma_k$ , and  $R_i^2(\alpha^*, p_D^*) \geq \gamma_i, i \in \mathcal{K} \setminus \{k\}$ . Correspondingly, we construct a new solution  $(\bar{\tau}_e, \bar{\tau}_t, \bar{\alpha}, \bar{p}_D)$  as  $\bar{\tau}_e = \tau_e^*, \bar{\tau}_t = \tau_t^*, \bar{p}_D = p_D^*$ , and

$$\bar{\alpha}_i = \alpha_i^*, \forall i \in \mathcal{K} \setminus \{k\}, \bar{\alpha}_k = \frac{(2^{\gamma_k} - 1)(\sum_{j=1}^{k-1} \bar{\alpha}_j |h_k|^2 \rho_B + |h_{D,k}|^2 \rho_D + 1)}{|h_k|^2 \rho_B}.$$

Note that  $R_k^2(\bar{\alpha}, \bar{p}_D) = \gamma_k$ . It is easy to find that  $\bar{\alpha}_k < \alpha_k^*$ , and thus  $R_i^2(\bar{\alpha}, \bar{p}_D) \geq R_i^2(\alpha^*, p_D^*), \forall i \in \mathcal{K}$ . Therefore, the solution  $(\bar{\tau}_e, \bar{\tau}_t, \bar{\alpha}, \bar{p}_D)$  satisfies all the constraints. Similarly, since  $\bar{\alpha}_k < \alpha_k^*$ , we can conclude from Eq. (9) that  $R_D^2(\bar{\alpha}, \bar{p}_D) > R_D^2(\alpha^*, p_D^*)$ , and  $U_D(\bar{\tau}_e, \bar{\tau}_t, \bar{\alpha}, \bar{p}_D) > U_D(\tau_e^*, \tau_t^*, \alpha^*, p_D^*)$ , which contradicts our assumption that  $(\tau_e^*, \tau_t^*, \alpha^*, p_D^*)$  is the optimal solution.

The *Theorem 1* is completely proved.

**APPENDIX B**

**PROOF OF THEOREM 2**

The constraint (19) can be further simplified as

$$\frac{\rho_B \alpha_i}{\sum_{j=1}^{i-1} \rho_B \alpha_j + \delta_i \rho_D + \theta_i} = \phi_i, \quad \forall i \in \mathcal{K}, \quad (35)$$

where  $\phi_i = 2^{\gamma_i} - 1, \delta_i = \frac{|h_{D,i}|^2}{|h_i|^2}, \theta_i = \frac{1}{|h_i|^2}$ , and  $\sum_{j=1}^{i-1} \rho_B \alpha_j = 0$  for  $i - 1 < j$ . Then  $\alpha_1$  can be easily obtained as

$$\alpha_1 = \frac{\phi_1(\delta_1 \rho_D + \theta_1)}{\rho_B}. \quad (36)$$

As to  $U_i, i \in \mathcal{K} \setminus \{1\}$ ,  $\alpha_i$  can be given by

$$\alpha_i = \frac{\phi_i(\sum_{j=1}^{i-1} \alpha_j \rho_B + \delta_i \rho_D + \theta_i)}{\rho_B}, \quad i \in \mathcal{K} \setminus \{1\}. \quad (37)$$

Then, we define  $S_i = \sum_{j=1}^i \alpha_j \rho_B$ . A recursive expression of  $S_i$  can be obtained from (37)

$$\begin{aligned} S_i &= S_{i-1} + \alpha_i \rho_B = S_{i-1} + \phi_i(S_{i-1} + \delta_i \rho_D + \theta_i) \\ &= (1 + \phi_i)S_{i-1} + \phi_i(\delta_i \rho_D + \theta_i) \\ &= \left[ \prod_{j=2}^i (1 + \phi_j) \right] S_1 \\ &\quad + \sum_{j=2}^i \left\{ \left[ \prod_{t=j+1}^i (1 + \phi_t) \right] \phi_j(\delta_j \rho_D + \theta_j) \right\} \\ &= \sum_{j=1}^i \left\{ \left[ \prod_{t=j+1}^i (1 + \phi_t) \right] \phi_j(\delta_j \rho_D + \theta_j) \right\}, \quad (38) \end{aligned}$$

where the last equality comes from that  $S_1 = \phi_1(\delta_1 \rho_D + \theta_1)$ , and  $\prod_{t=j+1}^i (1 + \phi_t) = 1$  for  $j + 1 > i$ . Therefore,  $\alpha_i = \frac{S_i - S_{i-1}}{\rho_B}$  ( $i \geq 2$ ) can be calculated as

$$\alpha_i = \frac{\sum_{j=1}^{i-1} \left\{ \left[ \prod_{t=j+1}^{i-1} (1 + \phi_t) \right] \phi_j \phi_j(\delta_j \rho_D + \theta_j) \right\} + \phi_i(\delta_i \rho_D + \theta_i)}{\rho_B}, \quad (39)$$

where  $i \geq 2$  and  $\prod_{t=j+1}^{i-1} (1 + \phi_t) = 1$  for  $j + 1 > i - 1$ .

Referring to (36) and (39), the optimal  $\alpha^*$  can be represented by (20), and *Theorem 2* is completely proved.

**APPENDIX C**

**PROOF OF THEOREM 4**

The second derivative of  $U_D(\tau_t)$  with respect to  $\tau_t$  can be calculated as

$$\nabla^2 U_D(\tau_t) = \frac{(m_1 n_2 - m_2 n_1)[(m_1 n_2 + m_2 n_1)\tau_t + 2n_1 n_2]}{(m_1 \tau_t + n_1)^2 (m_2 \tau_t + n_2)^2}. \quad (40)$$

By substituting  $m_1, n_1, m_2, n_2$ , the expression  $m_1 n_2 - m_2 n_1$  can be further derived as  $m_1 n_2 - m_2 n_1 = -\bar{D}\bar{F}|h_D|^2$ . Since  $\bar{D} > 0, \bar{F} > 0$ , and  $|h_D|^2 > 0$ , we can obtain that  $m_1 n_2 - m_2 n_1 < 0$ .

The concavity of  $U_D(\tau_t)$  can be analyzed as follows. First, if  $m_1 n_2 + m_2 n_1 \geq 0$ , as  $n_1 > 0, n_2 > 0$  and  $\tau_t > 0$ , the expression  $(m_1 n_2 + m_2 n_1)\tau_t + 2n_1 n_2$  is greater than zero, and  $\nabla^2 U_D(\tau_t) < 0$ . Second, if  $m_1 n_2 + m_2 n_1 < 0$ , as  $\frac{\bar{D}}{C + \rho_D^{max}} \leq \tau_t \leq \frac{\bar{D}}{C}$ , we can find that  $\nabla^2 U_D(\tau_t) \leq 0$  for any  $\tau_t$  when  $\frac{\bar{D}(m_1 n_2 + m_2 n_1)}{C} + 2n_1 n_2 \geq 0$ .

In summary, if  $m_1, m_2, n_1$  and  $n_2$  satisfy one of the following two constraints, the function  $U_D(\tau_t)$  is concave: i)  $m_1 n_2 + m_2 n_1 \geq 0$ ; ii)  $m_1 n_2 + m_2 n_1 < 0$  and  $\frac{\bar{D}(m_1 n_2 + m_2 n_1)}{C} + 2n_1 n_2 \geq 0$ .



APPENDIX D

PROOF OF THEOREM 5

When  $\rho_D^e = \rho_D^l = 0$ , we can obtain that  $m_1 = \bar{F} - \bar{C}(\bar{E} + |h_D|^2)$ ,  $n_1 = \bar{D}(\bar{E} + |h_D|^2)$ ,  $m_2 = \bar{F} - \bar{C}\bar{E}$ , and  $n_2 = \bar{D}\bar{E}$ . Note that  $n_1 > 0$ , and  $n_2 > 0$ .

Define  $s_1 = \frac{n_1}{m_1}$ ,  $s_2 = \frac{n_2}{m_2}$ , and  $z = \frac{m_1}{m_2}$ . As  $\bar{F} - \bar{C}\bar{E} < 0$ , we have  $m_1 < m_2 < 0$ . Meanwhile, we can find that  $n_1 m_2 - n_2 m_1 = \bar{D}\bar{F}|h_D|^2 > 0$ . Correspondingly, the following inequalities can be derived as

$$z > 1, \quad s_1 < s_2 < 0. \tag{41}$$

Then  $\nabla_{\tau_t} U_D(\tau_t)$  can be calculated as

$$\begin{aligned} &\nabla_{\tau_t} U_D(\tau_t) \\ &= \frac{1}{\ln 2} \nabla_{\tau_t} \left[ \tau_t \ln \left( z \frac{\tau_t + s_1}{\tau_t + s_2} \right) \right] = \frac{\ln z}{\ln 2} \\ &\quad + \frac{1}{\ln 2} \left\{ \underbrace{\left[ \ln(\tau_t + s_1) - \frac{s_1}{\tau_t + s_1} \right] - \left[ \ln(\tau_t + s_2) - \frac{s_2}{\tau_t + s_2} \right]}_{\mathcal{L}_1} \right\}. \end{aligned} \tag{42}$$

Define  $Q(s) = \ln(\tau + s) - \frac{s}{\tau + s}$ ,  $s < 0$ . Deriving  $Q(s)$  with respect to  $s$ , we can see that

$$\nabla_s Q(s) = \frac{s}{(\tau + s)^2} < 0, \quad s < 0. \tag{43}$$

Hence,  $Q(s)$  decreases with  $s$  for  $s < 0$ . Correspondingly,  $\mathcal{L}_1 > 0$  and  $\ln z > 0$ . We can conclude that  $\nabla_{\tau_t} U_D(\tau_t) > 0$ , and  $U_D(\tau_t)$  increases with  $\tau_t$ . Therefore, the optimal solution of (28) is  $\tau_{t,2}^* = \frac{\bar{D}}{\bar{C}}$ , and  $\rho_{D,2}^* = \frac{\bar{D} - \bar{C}\tau_{t,2}^*}{\tau_{t,2}^*} = 0$ .

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