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Review and Statistical Analysis of the Ultrasonic Velocity Method for Estimating the Porosity Fraction in Polycrystalline Materials

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REVIEW AND STATISTICAL ANALYSIS OF THE ULTRASONIC VELOCITY METHOD FOR ESTIMATING THE POROSITY FRACTION IN POLYCRYSTALLINE MATERIALS

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SUMMARY

A review and statistical analysis of the ultrasonic velocity method for estimating the porosity fraction in polycrystalline materials is presented. Initially, a semi-empirical model is developed showing the origin of the linear relationship between ultrasonic velocity and porosity fraction. Then, from a compilation of data produced by many researchers, scatter plots of velocity versus percent porosity data are shown for Al₂O₃, CuO, MgO, porcelain-based ceramics, PZT, SiC, Si₃N₄, steel, tungsten, UO2, (U_{0.30}Pu_{0.70})Č, and YBa₂Cu₃O_{7-x}. Linear regression analysis produced predicted slope, intercept, correlation coefficient, level of significance, and confidence interval statistics for the data. Velocity values predicted from regression analysis for fully-dense materials are in good agreement with those calculated from elastic properties.

INTRODUCTION

The physical behavior of components manufactured from polycrystalline materials is in many cases directly dependent on the porosity fraction (volume fraction of pores). As examples concerning key properties of technologically-important materials, porosity fraction has been shown to affect: (1) the strength, toughness and modulus of structural and refractory materials such as steel (ref. 1), tungsten (ref. 2), SiC (ref. 3), Si₃N₄ (ref. 3), and Al₂O₃ (ref. 3), (2) the strength of nuclear fuel materials such as UO_2 (refs. 4 and 5), (3) the thermal shock behavior and strength of porcelain-based ceramics (refs. 6 and 7), (4) the dielectric and elastic properties of piezoelectric materials such as PZT (ref. 8), and (5) the critical current density, diamagnetic response, and modulus of superconducting ceramics such as YBa₂Cu₃O_{7-X} (refs. 9 to 11). In the latter case, reference 9 has shown that porosity

fraction variations on the order of l percent in $YBa_2Cu_3O_{7-X}$ samples can result in an order of magnitude variation in critical current density. In such cases where physical properties are directly dependent on porosity fraction, the measurement of porosity fraction becomes important in the quality assurance process for the material.

Currently, various methods are available for measuring the porosity fraction of polycrystalline materials. The most common include dry-weight dimensional and liquid immersion (ref. 12). Other methods for obtaining porosity fraction include estimates from optical areal analysis measurements (ref. 13) and estimates from x-ray attenuation measurements (ref. 14). The choice of method is dependent on experimental conditions including sample geometry and whether additional investigation is required with the sample. For example, the dry-weight dimensional method can only be used for regularly-shaped samples with uniform dimensions such as cubes and rods, while liquid immersion is potentially destructive due to liquid infusion into the sample. Because of the lack of a truly universal porosity fraction measurement method, it seems worthwhile to consider additional measurement/estimation methods that may be useful and convenient in certain laboratory and industrial situa-In this study, we consider the ultrasonic velocity measurement method for estimating porosity fraction.

Ultrasonic velocity is a relatively simple measurement that requires the material specimen to have one pair of sides flat and parallel (ref. 15). The advantages of this method are that it is nondestructive and measurements can be made on different regions of a single specimen. Smith (ref. 2) and Nagarajan (ref. 16) were two of the first researchers to establish empirical correlations between porosity fraction and ultrasonic velocity for polycrystalline materials. The correlations appeared relatively linear over

the porosity fraction ranges investi-Smith's work concerned metallic samples while Nagarajan's work concerned ceramic samples. Other researchers began to investigate similar correlations with different materials. Here. we review and statistically analyze these empirical correlations between ultrasonic velocity and porosity fraction for polycrystalline materials. Initially, a semi-empirical model is developed showing the origin of the linear relationship between ultrasonic velocity and porosity fraction. Then, scatter plots of velocity versus percent porosity data are shown for Al₂O₃, CuO, MgO, porcelain-based ceramics. PZT, SiC, Si₃N₄, steel, tungsten, UO₂, $(U_0.30Pu_0.70)C$, and $YBa_2Cu_3O_{7-x}$. Linear regression analysis produced predicted slope, intercept, correlation coefficient, level of significance, and confidence interval statistics for the data. Additionally, velocity values predicted from regression for fullydense materials are compared with those calculated from elastic properties.

SEMI-EMPIRICAL MODEL

When there are no boundary effects present, the velocity of a longitudinal ultrasonic wave traveling in a solid is related to the elastic properties and density of the solid by (ref. 17):

$$V = \{ [E(1 - v)]/[\rho(1 + v)(1 - 2v)] \}^{1/2}$$

(1)

where V, E, ρ , and ν are the velocity, elastic modulus, bulk density, and Poisson's ratio, respectively, of the material. (The velocity of a shear ultrasonic wave traveling in a solid is related to the elastic properties and density of the solid by:

$$V = \{E/[2\rho(1 + v)]\}^{1/2} \qquad (1(a))$$

An "apparent" modulus (ref. 3) for porous materials can be considered which depends on the porosity fraction.

Several early empirical investigations provided evidence that the modulus increases exponentially with decreasing porosity fraction according to (refs. 18 and 19):

$$E = E_0 \exp(-bP') \tag{2}$$

where E_O is the elastic modulus of a fully-dense (nonporous) material, b is an empirically-determined constant related to pore shape, pore distribution, and the ratio of open-to-closed pores, and P' is the porosity fraction. The use of equation (2) to evaluate E_O by extrapolation from fitted experimental data has sometimes resulted in large discrepancies between the extrapolated and observed values (ref. 20). An alternative to equation (2) has been suggested to describe the relationship between elastic modulus and porosity fraction (ref. 21):

$$E = E_0(1 - P')^{2n+1}$$
 (3)

where n, like b, is an empirically-determined constant that depends on pore distribution and pore geometry factors.

Porosity fraction, P', can be expressed as:

$$P' = (1 - (\rho/\rho_0))$$
 (4)

where ρ_O is the theoretical (nonporous material) density. Rearranging equation (4) allows us to express bulk density as a function of porosity fraction:

$$\rho = \rho_0(1 - P') \tag{5}$$

Substituting equations (3) and (5) into equation (1) allows velocity to be expressed as:

$$V = V_0(1 - P')^n$$
 (6)

where V_O is a constant for a given material equal to:

$$V_{O} = \{ [E_{O}(1 - v)]/[p_{O}(1 + v)(1 - 2v)] \}^{1/2}$$
(7)

V_O is the velocity in a fully-dense (nonporous) material, i.e., the "theoretical" velocity. (For shear waves:

$$V_0 = \{E_0/[2\rho_0(1 + \nu)]\}^{1/2}$$
 (7(a)))

The general case for all n can be shown by expanding the right-hand side of equation (6) using the binomial theorem (ref. 22) so that:

$$V = V_{O}\{1 + [n(-P')] + [n(n-1) \\ \times (-P')^{2}/2!] + ... + [n(n-1) \\ \times ... (n-k+1)(-P')^{k}/k!] + ...\}$$
(8)

From the ratio test, equation (8) is absolutely convergent for |P'| < 1.

Setting n = 1 in equations (3) and (8) results in good agreement for a number of materials over a wide porosity fraction range (0.1 < P' < 0.7) (ref. 21). In this case, the right-hand side of equation (8) is reduced such that:

$$V = V_0(1 - P')$$
 (9)

Equation (9) shows a linear relationship between velocity and porosity fraction and is the basis for selecting linear regression to analyze the empirical correlations reported in this study.

Concerning the relationship between Poisson's ratio and porosity fraction, most of the limited studies of Poisson's ratio show it decreasing with increasing porosity fraction less rapidly than for elastic modulus (ref. 3). In this development, it is assumed that Poisson's ratio is independent of porosity fraction.

It is sometimes convenient to discuss the relationship between velocity and percent porosity, %P, where:

$$%P = (P')100$$
 (10)

Solving equation (10) for P' and substituting into equation (9) gives:

$$V = m(%P) + V_O$$
 (11)

where

$$m = -V_0/100$$
 (12)

Equation (11) shows a linear relationship between V and %P where m and $V_{\rm O}$ are the slope and intercept, respectively.

We can also define a "percent theoretical velocity," %TV, where:

$$%TV = (V/V_O)100$$
 (13)

Solving equation (13) for V and substituting into equation (11) gives:

$$%TV = m'(%P) + 100$$
 (14)

where

$$m' = (m)100/V_O$$
 (15)

Equation (14) shows a linear relationship between %TV and %P where m and 100 are the slope and intercept, respectively. Presenting the velocity versus porosity fraction relationship in terms of equation (14) is essentially a normalization procedure in that the theoretical velocity of a material and the type of wave (longitudinal or shear) used in the velocity measurement are "removed" as variables. From the derivative of equation (14), the following quantity can be defined:

$$(1/m') = (\Delta \%P/\Delta \%TV) \qquad (16)$$

where Δ is "change in."

DATA EXTRACTION PROCEDURE

Almost all of the data presented in this study were obtained from previously-published studies. The policy employed was that all of the available data should be tabulated and analyzed. In most cases, the reference provided V versus ρ data, either in the form of a table or plot. In some cases, the reference provided percent theoretical density (% ρ_0) or P values instead of ρ values. Where necessary, ρ and % ρ_0 values were converted to %P values with the aid of equations (4) and (10).2

STATISTICAL ANALYSIS METHOD

Linear regression analysis and its associated statistics utilized in this study are briefly described in the next several paragraphs. The authors felt that a comprehensive set of statistics was necessary for this analysis because of the variation among data sets in the number of velocity measurements and the porosity fraction range over which those measurements were made.

Linear regression analysis is concerned with the problem of predicting or estimating the value of a (dependent) variable (V and %TV in equations (11) and (14), respectively) on the basis of another (independent) variable (%P in equations (11) and (14)). For the sake of simplicity, we have applied the classical regression model (ref. 23) which involves the following assumptions. V (and %TV) has been assumed to contain all the error while %P has been assumed to contain no

 $^{^2}$ In most cases, the references provided V and ρ data to 3 or 4 significant figures. For the sake of uniformity, all data and subsequent calculations including statistical values are presented in this report to at most 3 significant figures.

error.³ The variance in V (and %TV) has been assumed to be constant for all values of %P, and the distribution about V has been assumed to be normal with mean values lying exactly on the regression line. It also has been assumed that only one V value was measured at a particular %P.

Linear regression analysis results in predicted slope (m and m in egs. (11) and (14), respectively) and intercept $(V_O \text{ in eq. (11)})$ values that describe the relationship between V (and %TV) and %P. The Pearson product-moment correlation coefficient and level of significance statistics describe the quality of the regression. The correlation coefficient measures the strength of the linear relationship for the sample data. The level of significance, determined by the number of data points and the value of the correlation coefficient, determines an acceptance or confidence region for the regression. A level of significance of 0.025 corresponds to a 95 percent confidence region. The smaller (better) the level of significance, the lower the probability that the value of the correlation coefficient can be attributed to chance.

Confidence intervals for the predicted slope, intercept, and mean velocity values (the mean of further velocity measurements obtained at some

%P value) are also presented. The 95 percent symmetric confidence interval was chosen for the analysis. 4 In practical terms, the 95 percent confidence interval means that in 95 percent of the cases, the true value of the parameter will fall within the calculated interval.

REVIEW AND ANALYSIS

The review and statistical analysis are presented in Table I and figures 1 to 61. Most of the figures show scatter plots of V versus %P data for Al₂O₃ (refs. 16, 24 to 27), CuO (ref. 28) MgO (ref. 29), porcelainbased ceramics (refs. 7, 30 and 31), PZT (ref. 8), SiC (refs. 26, 32 to 35). Si₃N₄ (refs. 36 to 38), steel (ref. 39), tungsten (ref. 2), UO₂ (ref. 40), (U_{0.30} Pu_{0.70})C (ref. 41), and YBa₂Cu₃O_{7-X} (refs. 11, 42 to 45). The table presents the linear regression statistics corresponding to the scatter plots. The 95 percent confidence interval for the predicted slope and intercept values are presented in table I while the 95 percent confidence interval for mean predicted velocity values is shown by

 $^{^3}$ An analysis assuming errors in both variables is significantly more complicated. For some data sets, the uncertainty in 8 P may in fact be comparable to that of 9 V. The total uncertainties in each of 8 P and 9 V including experimental uncertainties, uncertainties in extracting data from plots, and different assumed values of 9 O are estimated to be less than 5 percent in all cases.

⁴The choice of a particular size confidence interval is "economic" rather than mathematical. It depends directly on the cost of an error, and hence on the frequency with which one can afford to be wrong. High confidence intervals lead to wide limits, and if these limits are too wide to be useful, the gap between them must be reduced either by accepting less confidence or by increasing the amount of data (ref. 23).

dashed lines on the scatter plots.⁵ The quantity $(\Delta \%P/\Delta \%TV)$ is provided for all plot lines in the corresponding table entries. (Note that this quantity also has a confidence interval associated with it, the width of which is similar to that for m').

Pertinent information concerning the reference's study including ultrasonic technique, measurement uncertainties, 6 microstructural anisotropy, material processing techniques, and velocity variation within specimens is also included in the table. A blank

⁵Several issues concerning the 95 percent confidence intervals for predicted intercept, slope, and mean velocity values need to be noted. First, the assumption of only one V value for a particular %P value is a conservative assumption that we know is false for some of the data sets in this review (see "comments" in table I). This assumption tends to make the limits of the confidence interval wider (worse) than if the confidence interval was calculated based on the mean of several velocity measurement values at a particular %P value. Second, the confidence intervals for predicted slope and intercept may not appear exactly symmetric in table I due to the round off procedure. Third, the 95 percent confidence interval for mean predicted velocity values is in most cases drawn (dashed line) over the entire %P range shown. In several cases, the interval extends beyond the %P range where velocity data exists. In these cases, the interval widens (worsens) as expected where no data exists.

⁶In most cases, the experimental uncertainties in the velocity and density measurements were provided by the reference. In the event that they were not, the uncertainties were estimated from the reference's description of samples and measurement techniques, and from our experience.

table entry indicates that the information was unavailable. The "comments" in the table give the number of data points for that particular reference and in some cases point out a major conclusion determined by the reference concerning the V versus %P data.

The figures are organized as follows. Figures 1 to 4, 6 to 9, 12 to 15, 17 to 23, 25, 26, 28, 29, 33 to 36, 38, 40 to 42, 44, 45, 48 to 50, 52 to 54, 57 to 59, show scatter plots of V (and %TV) versus %P for a single reference's data. 7 Results of multiple investigations for a specific material were also combined and analyzed as one data set in figures 5, 10, 37, 43, 46, 55, and 60. Additionally, plots comparing predicted (in most cases) regression lines obtained for a specific material from different investigations are given in figures 11, 16, 24, 27, 30 to 32, 39, 47, 51, 56, and 61. Where applicable for a material, scatter plots of longitudinal wave velocity data are presented before plots of shear wave velocity data. For most scatter plots, the solid line drawn is the linear regression line determined from the least-squares technique. For the plots with only two data points, a line is drawn through the points. In this case, the correlation coefficient, level of significance, and confidence interval statistics are not applicable.

⁷Because the range of %P values for which velocity measurements were obtained varied from reference to reference, the ranges shown on the horizontal and vertical axes of the plots differ from one to the next, i.e., the plots are not standardized. In some cases, the plot axes had to be adjusted to allow the presentation of the 95 percent confidence interval for mean predicted velocity values.

DISCUSSION

General Observations

Correlation coefficients with magnitudes greater than 0.95 were obtained in 31 out of 42 cases. Levels of significance with magnitudes less than 0.025 were obtained in 36 out of 42 cases. For longitudinal wave velocity, predicted intercepts (V_O) ranged from 0.443 cm/µs for unpoled PZT4 and unpoled PZT5 of reference 8 to 1.23 cm/ us for SiC of reference 33. For shear wave velocity, predicted intercepts (V_O) ranged from 0.313 cm/ μ s for YBa₂ Cu_3O_{7-X} to 0.786 cm/ μs for SiC of reference 26. The quantity $(\Delta %P/\Delta %TV)$ ranged from -0.52 for porcelain of reference 7 and poled PZT4 of reference 8 to -8.26 for porcelain T2 of reference 31. It is understandable that these quantities vary from one material to the next since each material has different elastic properties and density (eq. (1)). Predicted intercepts (V_0) for a specific material from different investigations agree fairly well (see the plots and tabular entries for Al₂O₃, SiC, and Si₃N₄). Predicted slopes for a specific material from different investigations agree fairly well in most cases. However, significant slope disparity is evident for Al₂O₃; this may be due to the limited porosity range for the data of references 26 and 27 and the inclusion of green and prefired sample data in the cases of references 24 and 25. For reference 26, the limited porosity range over which data was obtained is manifested in extremely wide 95 percent confidence limits for predicted slope, intercept and mean velocity values. In fact, one of the bounds for the confidence limits for predicted slope is a positive value.

Table II compares $V_{\rm O}$ predicted from regression analysis with that calculated from equations (7) (longitudinal wave velocity) and (7a) (shear wave velocity) for several materials. Values of elastic modulus, Poisson's

ratio, and density for fully-dense (single crystal and/or polycrystalline) materials used in the calculation are presented. The values of $V_{\rm O}$ predicted from regression and those obtained from calculation agree within approximately 17 percent in 16 out of 16 cases, and within approximately 6 percent in 11 out of 16 cases.

Other Microstructural Variables Affecting Velocity

Although porosity fraction seems to be a significant and perhaps the major microstructural feature affecting ultrasonic velocity, several references point to other microstructural variables having an impact on velocity. These include slight compositional variations (ref. 31), preferred domain orientation (ref. 8), particle contact anisotropy (ref. 39), pore size distribution and geometry (ref. 2), and type of agglomeration (ref. 25). These variables may result in differences in predicted intercept (V_O) and slope for what is believed to be the same material from different investigations. Thus, the authors feel that the most accurate and precise application of the ultrasonic velocity method for estimating porosity fraction first requires the development of accurate velocity versus porosity fraction relationships/ calibrations for the specific material of interest.

Ramifications

The estimation of batch-to-batch, sample-to-sample and within-sample %P variations for a material can be accomplished if the quantity (Δ %P/ Δ %TV) is known with reasonable confidence for that material. The nondestructive mapping of spatial porosity fraction variations within a sample by means of an ultrasonic scanning technique has been reported recently (refs. 50 and

51). This approach may also be useful in the analysis of the uniformity of composite materials (ref. 34).

CONCLUSION

A review and statistical analysis of the ultrasonic velocity method for estimating the porosity fraction in polycrystalline materials is presented. First, a semi-empirical model was developed showing the origin of the linear relationship between ultrasonic velocity and porosity fraction. Then, from a compilation of data produced by many researchers, scatter plots of velocity versus percent porosity data were shown for Al₂O₃, CuO, MgO, porcelain-based ceramics, PZT, SiC, Si3N4, steel, tung-sten, UO₂, (U_{0.30}Pu_{0.70})C, and YBa₂Cu₃O_{7-x}. Linear regression analysis produced slope, intercept, correlation coefficient, level of significance, and confidence interval statistics for the data. Velocity values predicted from regression analysis for fullydense materials are in good agreement with those calculated from elastic properties. The estimation of batchto-batch, sample-to-sample, and withinsample variations in porosity fraction for a material can be accomplished with ultrasonic velocity measurements if reasonable confidence exists in the velocity versus percent porosity linear relationship.

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LIST OF SYMBOLS AND ABBREVIATIONS FOR TABLE I.

 $V = Velocity (cm/\mu sec)$

 $SV = Shear wave velocity (cm/\mu sec)$

LV = Longitudinal wave velocity (cm/ μ sec)

%TV = Percent theoretical velocity

%P = Percent porosity

Wt. = Weight

 β_0 = Predicted value of intercept (Theoretical velocity)

 β'_0 = Predicted value of intercept (Percent theoretical velocity)

 β_1 = Predicted value of slope (Velocity/percent porosity)

 β'_1 = Predicted value of slope (Percent theoretical velocity/percent porosity)

N/A = Not applicable

RBSN = Reaction-bonded silicon nitride

 Δ = Change in

(A blank appearing in a table entry indicates that the author did not mention the subject or the information was otherwise unavailable.)

Material	Reference	Processing Notes/ Chemical Additives		Velocity Measurement Technique	Velocity Measurement Uncertainty (%)	Density Measurement Technique	Density Measurement Uncertainty (%)	Theoretical Density, \(\rho_0, \) Used to Calculate % Porosity (g/cc)	
Al ₂ O ₃	24	1.5 mol % Sintering aids	Insignificant	Longitudinal waves, 10 MHz	≤ 0.1	Dry-wt. dimensional	≤ 1	3.98	LV = -0.018 • %P +
Ai ₂ O ₃	25	Sintering aid, Binder, Plasticizer, Water		Thru-transmission and pulse-echo overlap, Longitu- dinal waves, Dry and wet coupling, 5 MHz	≤ 0.8	Dry-wt. dimensional and liquid- immersion	s 2	3.98	LV = -0.019 • %P +
Al ₂ O ₃	16	Starting powders of various mean particle size, Binder		Pulse-echo transit time, Longitudinal waves, 10 MHz	≤ 1	Dry-wt. dimensional	< 0.5	3.98	LV = -0.007 • %P + 1
AI ₂ O ₃	26	Lubricants, Plasticizer, Water	Insignificant	Pulse-echo/cross- correlation, Longitudinal waves, 50 MHz	≤ 0.2	Liquid- immersion	≤ 2	3.98	EV = -0.004 • %P + 1
Al ₂ 0 ₃	16, 24-26			Longitudinal waves				3 98	LV = -0.016 • %P + 1
Al ₂ O ₃	27		Insignificant	Puise-echo overlap, Shear waves, 5 MHz	s 1	Dry-wt. dimensional	s 1	3 98	SV = -0.003 • %P + 0
Ai ₂ O ₃	24	1.5 mol % Sintering aids	Insignificant	Shear waves, 5 MHz	≤ 0.2	Dry-wt. dimensional	≤ 1	3.98	SV = -0.012 • %P + 0 6
Al ₂ O ₃	25	Sintering aid, Binder, Plasticizer, Water		Thru-transmission and pulse-echo overlap, Shear waves, Ory and wet coupling, 1-5 MHz	≤ 18	Dry-wt. dimensional and liquid- immersion	s 2	3 98	SV = -0010 • %P + 06
Al ₂ O ₃	16	Starting powders of of various mean particle size, Binder		Pulse-echo transit time, Shear waves, 10 MHz	s 1	Dry-wt. dimensional	< 05	3 98	SV = -0 004 • %P + 0 62
Al ₂ O ₃	16, 24, 25, 27			Shear waves				3.98	SV = -0 0009 • 96P + 0 69
Al ₂ O ₃	16, 24-27								
CuO	28	Starting powders different for each of 2 disks	1	Pulse-echo/cross- correlation, Longitudinal waves, Dry coupling, 5 MHz	≤ 04	Dry-wt. dimensional	s 1	6.40	LV = -0.006 • %P +0.47
"Green" MgO		20 wt.% Binder	i t	Pulse-echo overlap. Longitudinal waves, 2.25 MHz	≤ 0.5	Dry-wt. dimensional	≤ 1	2.70	LV = -0.014 • 96P + 0.81

NA # 15 1

(ر	Predicted Line Equation (%TV = $\beta'_1 \cdot \%P + \beta'_2$)	Correlation Coefficient Level of Significance	95% Confidence Intervals for Predicted Intercept $(\beta_{\mathbf{p}})$ and Slope (β_{1})	95% Confidence Intervals for Predicted Intercept (3' ₀) and Slope (3' ₁)	Δ% P Δ% TV	Largest Velocity Variation Across One Surface of Specimen (%)	Comments	Corresponding Figure Number
1.09	%TV = -1.65 • %P + 100	<u>- 0.999</u> 0.0001	$1.07 \le \beta_0 \le 1.12$ $-0.019 \le \beta_1 \le -0.017$	$97.7 \le \beta'_0 \le 102$ $-1.77 \le \beta'_1 \le -1.52$	- 0.61	15	5 data points lumped together in low % porosity region separated widely from 1 data point in high % porosity (Partially-fired specimen)	1
1.13	%TV = -1.64 • %P + 100	<u>- 0.992</u> 0.0001	$0.994 \le \beta_0 \le 1.27$ -0.022 \le \beta_1 \le -0.015	$87.8 \le \beta'_0 \le 112$ $-1.94 \le \beta'_1 \le -1.34$	- 0.61	1	Velocity may be very slightly sensitive to the type of agglomerates found in ceramic samples, which may depend on whether sample is calcined or not, 2 data points in low % porosity region widely separated from other 4 data points in high % porosity region (Green samples)	2
1 00	%TV = -0.736 • %P + 100	<u>- 0 928</u> 0 0001	$0.987 \le \beta_0 \le 1.02$ $-0.008 \le \beta_1 \le -0.007$	$98.3 \le \beta'_0 \le 102$ $-0.818 \le \beta'_1 \le -0.654$	- 1.36		16 data points	3
1.01	%TV = -0 377 • %P + 100	<u>- 0.698</u> 0.302	$0.923 \le \beta_0 \le 1.09$ $-0.016 \le \beta_1 \le 0.008$	$92.2 \le \beta'_0 \le 108$ $-1.54 \le \beta'_1 \le 0.782$	- 2.65	1	Limited data region; 4 data points	4
1.10	%TV = -1.43 • %P + 100	<u>- 0 949</u> 0 0001	$1.06 \le \beta_0 \le 1.15$ $-0.018 \le \beta_1 \le -0.013$	$95.7 \le \beta'_0 \le 104$ $-1.61 \le \beta'_1 \le -1.25$	0.699		32 data points, all longitudinal wave data	5
) 669	%TV = -0 477 • %P + 100	<u>-0.94</u> 0.006	$0.646 \le \beta_0 \le 0.692$ $-0.005 \le \beta_1 \le -0.002$	$96.7 \le \beta'_0 \le 103$ $-0.669 \le \beta'_1 \le -0.284$	- 2.10	2	6 data points	6
) 655	%TV = −1 87 • %P + 100	<u>- 1.0</u> 0 0001	$0.648 \le \beta_0 \le 0.663$ $-0.013 \le \beta_1 \le -0.012$	$98.9 \le \beta'_0 \le 101$ $-1.93 \le \beta'_1 \le -1.81$	- 0.53	15	5 data points lumped together in low % porosity region separated widely from 1 data point in high % porosity region (Partially-fired specimen)	7
) 666	%TV = -1.55 • %P + 100	<u>- 0 987</u> 0 0003	$0.571 \le \beta_0 \le 0.762$ $-0.008 \le \beta_1 \le -0.013$	$85.7 \le \beta'_0 \le 114$ -1.90 \le \beta'_1 \le -1.20	- 0.65	1	Velocity may be very slightly sensitive to the type of agglomerates found in ceramic samples, which may depend on whether sample is calcined or not, 2 data points in low % porosity region widely separated from other 4 data points in high % porosity region (Green samples)	8
628	%TV = -0.662 * %P + 100	0.990 0.0001	$0.622 \le \beta_0 \le 0.635$ $-0.005 \le \beta_1 \le -0.004$	$99.0 \le \beta'_0 \le 101$ $-0.705 \le \beta'_1 \le -0.610$	- 1.51		17 data points	9
693	%TV = -1 35 • %P + 100	<u>- 0 910</u> 0 0001	$0.656 \le \beta_0 \le 0.729$ $-0.011 \le \beta_1 \le -0.008$	$94.8 \le \beta'_0 \le 105$ $-1.57 \le \beta'_1 \le -1.14$	- 0.741		35 data points, all shear wave data	10
			· · · · · · · · · · · · · · · · · · ·				Comparison	11
474	%TV = -134 • %P + 100	<u>- 0 990</u> 0 0100	$0400 \le \beta_0 \le 0549$ $-0009 \le \beta_1 \le -0004$	$84.3 \le \beta'_0 \le 116$ $-1.92 \le \beta'_1 \le -0.760$	- 0.746		4 data points, 4 specimens cut from 2 disks, CuO phase confirmed from x-ray diffraction	12
817	N/A	<u>-10</u> 0012	$0.673 \le \beta_0 \le 0.961$ $-0.017 \le \beta_1 \le -0.010$	N/A	- 0 60	2	3 data points; material is unsintered, green compact	13



TABLE I.—ULTRASONIC VELOCITY VERSUS PERCENT POROSITY

Material	Reference	Processing Notes/ Chemical Additives		Velocity Measurement Technique	Velocity Measurement Uncertainty (%)	Density Measurement Technique	Density Measurement Uncertainty (%)	Theoretical Density, pe, Used to Calculate % Porosity (g/cc)	Predicted Line Equation (V = β_1 • %P + β_2)	(4)
Porcelain	7		Preferred granular orientation	Pulse-echo overlap, Longitudinal waves, 2 MHz	≤ 0.1	Dry-wt. dimensional	≤ 1	2.6	LV = -0 013 • %P + 0.728	961
Porcelain	7		Preferred granular orientation	Pulse-echo overlap. Shear waves. 2 MHz	≤ 0.1	Dry-wt. dimensional	≤ 1	26	SV = -0 009 • %P + 0 448	9611
Porcelain	7									ļ
Porcelain	30			Longitudinal waves, 1.5-3 MHz				2.60	LV = -0 006 • %P + 0 618	%TV
Porcelain P1 (See ref.)	31	(See ref.)		Longitudinal waves, 15 MHz	≤ 1	Dry-wt. dimensional	≤ 1	2 51	LV = -0.002 • %P + 0.611	%TV
Porcelain P2 (See ref.)	31	(See ref)		Longitudinal waves, 15 MHz	≤ 1	Dry-wt. dimensional	≤ 1	2.56	LV = -0 005 • %P + 0 615	%TV
Porcelain T1 (See ref.)	31	(See ref.)		Longitudinal waves, 15 MHz	≤ 1	Dry-wt. dimensional	≤ 1	2.58	LV = -0.001 • %P + 0.623	% T∨
Porcelain T2 (See ref.)	. 31	(See ref.)		Longitudinal waves, 15 MHz	≤ 1	Dry-wt. dimensional	s 1	2.64	LV = -0 0008 • %P + 0 626	%TV :
Unpoled PZT4	8		Insignificant	Pulse-echo overlap, Longitudinal waves, 50 MHz	≤ 0.1	Liquid- immersion	≤ 2	8 0	LV = -0.007 • %P + 0.443	%TV
Poled PZT4	8		Preferred electrical domain orientation	Pulse-echo overlap. Longitudinal waves. 50 MHz	≤ 0.1	Liquid- immersion	≤ 2	8.0	LV = -0 009 • %P + 0 483	%TV :
PZT4	8									
Unpoled PZT5	8		Insignificant	Pulse-echo overtap, Longitudinal waves, 50 MHz	≤ 0.1	Liquid- immersion	≤ 2	8.0	LV = -0.008 • %P + 0.443	%TV =
Poled PZT5	8		Preferred electrical domain orientation	Pulse-echo overlap. Longitudinal waves, 50 MHz	≤ 0.1	Liquid- immersion	≤ 2	8.0	LV = -0 010 • %P + 0 486	%TV =
PZT5	8									

FOLDOUT FRAME 1

(x,y,y) = (x,y)



	Predicted Line Equation (%TV = $\beta'_1 \circ \text{%P} + \beta'_0$)	Correlation Coefficient Lavel of Significance	95% Confidence thtervals for Predicted intercept (β_{θ}) and Slope (β_{η})	954: Confidence Intervals for Predicted Intervals (β'_{-1}) and Slope (β'_{-1})	Δ% P Δ% TV	Largest Velocity Variation Across One Surface of Specimen (%)	Comments	Corresponding Figure Numbe
28	%TV = -1.78 • %P + 100	<u>- 0.993</u> 0.0001	$0.713 \le \beta_0 \le 0.743$ $-0.0014 \le \beta_1 \le -0.0012$	$97.9 \le \beta'_0 \le 102$ $-1.87 \le \beta'_1 \le -1.70$	- 0.56		27 data points, multiphase ceramic; sample composition and thus theoretical density vary slightly with firing temperature; measurements made along extrusion axis	14
48	%TV = -1.93 • %P + 100	<u>- 0.998</u> 0.0001	$0.442 \le \beta_0 \le 0.454$ $-0.009 \le \beta_1 \le -0.008$	$98.7 \le \beta'_0 \le 101$ $-1.98 \le \beta'_1 \le -1.88$	- 0.52			15
							Comparison	16
18	%TV = -0.935 • %P + 100	<u>- 0.987</u> 0.0001	$0.606 \le \beta_0 \le 0.630$ $-0.007 \le \beta_1 \le -0.005$	$98.1 \le \beta'_0 \le 102$ -1.11 \le \beta'_1 \le -0.760	- 1.07		7 data points, multiphase ceramic, sample composition and thus theoretical density vary slightly with firing temp	17
511	%TV = -0.312 • %P + 100	<u>- 0.586</u> 0.414	$0.553 \le \beta_0 \le 0.668$ $-0.010 \le \beta_1 \le 0.006$	$90.5 \le \beta'_0 \le 109$ $-1.34 \le \beta'_1 \le -1.28$	- 3.21		4 data points, multiphase ceramic, sample composition and thus theoretical density vary slightly with firing temp.	18
515	%TV = -0.740 • %P + 100	<u>- 0.983</u> 0.017	$0.598 \le \beta_0 \le 0.631$ $-0.007 \le \beta_1 \le -0.002$	$97.3 \le \beta'_0 \le 102$ $-1.04 \le \beta'_1 \le -0.436$	- 1.35	,		19
623	%TV = −0.167 • P + 100	<u>- 0.894</u> 0.106	$0.612 \le \beta_0 \le 0.632$ $-0.003 \le \beta_1 \le 0.0005$	$98.6 \le \beta'_0 \le 101$ $-0.422 \le \beta'_1 \le 0.088$	- 5.99			20
626	%TV = -0 121 • %P + 100	<u>- 0.947</u> 0.053	$0.621 \le \beta_0 \le 0.631$ $-0.002 \le \beta_1 \le 0.003$	$99.2 \le \beta'_0 \le 101$ $-0.246 \le \beta'_1 \le 0.004$	- 8.26			21
443	%TV = -168 • %P + 100	N/A N/A	-0.002 \$ p ₁ \$ 0.000	N/A	- 0.60		2 data points for each set, PZT4, PZT5, and PZT7 are each different solid solution combinations of PbZr0 ₃ and PbTr0 ₃ but theoretical density is ~8 0 g/cc for each, poling orients electric domains, velocity	22
483	%TV = -1.93 • %P + 100	N/A N/A	N/A	N/A	- 0.52		measured along polanzed direction for poled specimens; no correlation coefficient is given since only 2 data points for each set; all poled sets have higher theoretical velocity than corresponding unpoled set	23
							Comparison	24
443	%TV = -185 • %P + 100	N/A N/A	N/A	N/A	- 0.54		2 data points for each set, PZT4, PZT5, and PZT7 are each different solid solution combinations of PbZr0 ₃ and PbTi0 ₃ but theoretical density is ~8.0 g/cc for each, poling orients electric domains, velocity	1
486	%TV = -2.12 + %P + 100	N/A N/A	N/A	N/A	- 0.47		measured along polarized direction for poled specimens, no correlation coel- ficient is given since only 2 data points for each set, all poled sets have higher theoretical velocity than corresponding unpoled set	26
					<u> </u>	1	Comparison	27

		,	

tical Predict Predict to ρ_0 . Line Equation (V = β_1 • %) where		Density Measurement Uncertainty (%)	Density Measurement Technique	Velocity asurement ncertainty (%)	nt Meas Unc	Velocity Measuremen Technique	Microstructural Anisotropy	Processing Notes Chemical Additives	Reference	Material
LV = -0.004 • q	8.0	≤ 2	Liquid- immersion	s 0.1	- 1	Pulse-echo overlap, Longitudinal wavi	Insignificant		8	Unpoled PZT7
LV = -0 005 • 94	8.0	≤ 2	Liquid- immersion	≤ 0.1	ı		Preferred electrical domain orientation		8	Poled PZT7
					+				8	Р2Т7
					1				8	Unpoled PZT
LV = -0.007 • %p	3 22	≤ 2	Liquid- immersion	- 1	S	Thru-transmission transit time, Longitudinal waves, 500 KHz		Binder	32	Poled PZT "Green" α-SiC
LV = -0.014 • %P	3 22	s 1	Dry-wt imensional		≤ 0.	Pulse-echo/cross- correlation, Longitudinal waves, 100 MHz	ave preferred ore orientation	arbonaceous	1.	α-SiC
LV = -0.011 • %P	3 22	≤ 2	Liquid- nmersion	- 1	S 1	Pulse-echo overlap, Longitudinal waves, 25 MHz	0		34	α-SiC
LV = -0011 • %P	3 22	≤ 1	Dry-wt. nensional	1 '	<u>s</u> 1	Pulse-echo iverlap, ongitudinal waves, O MHz	Ov Lo	Ins	35	α-SiC
LV = -0011 • %P+	3 22					ongitudinal waves	Lo		33-35	α-SiC
SV = -0 009 • %P +	3 22	≤ 2	iquid- nersion	, -	≤ 0.1	ulse-echo/cross- errelation, Shear eves, 20 MHz	preferred cor	onaceous hav	car	x-SiC
									26. 33-35	-SiC 2
LV = -0 015 • %P +	3 30	≤ 1 3	y-wt. nsional		≤ 1	ise-echo orlap, igitudinal waves, 45 MHz	over Lone	de has 196 sintening aid 0.5-196 impu- RBSN has 96 impunties various nts of unre-	nitric MgC and rities < 1 and	i ₃ N ₄



IT POROSITY: REVIEW AND STATISTICAL ANALYSIS—CONTINUED

)	Predicted Line Equation (%TV = $\beta'_1 \circ \%P + \beta'_0$)	Correlation Coefficient Level of Significance	95% Confidence intervals for Predicted Intercept (β_q) and Slope (β_1)	95% Confidence intervals for Predicted intercept (β', β) and Slope (β', γ)	Δ% P Δ% TV	Largest Velocity Variation Across One Surface of Specimen (%)	Comments	Corresponding Figure Number
) 464	%TV = -0.760 • %P + 100		N/A	N/A	– 1. 32		2 data points for each set, PZT4, PZT5, and PZT7 are each different solid solution combinations of PbZr0 ₃ and Pb TiO ₃ but theoretical density is -8.0 g/cc for each; poling orients electric domains, velocity	28
0.494	%TV = -0.952 • %P + 100	N/A N/A	N/A	N/A	- 1.05		measured along polarized direction for poled specimens; no correlation coef- ficient is given since only 2 data points for each set, all poled sets have higher theoretical velocity than corresponding unpoled set	29
				_			Comparison	30
							Comparison	31
							Comparison	32
1464	N/A	<u>- 0 974</u> 0 0001	$0.397 \le \beta_0 \le 0.535$ $-0.009 \le \beta_1 \le -0.006$	N/A	- 0.633	30	8 data points, material is unsintered green compact, large velocity variation even though small density variation within specimen; quality of contact between individual powder particles may affect velocity	33
23	%TV = -1 16 • %P + 100	<u>- 0 993</u> 0 0001	$1.22 \le \beta_0 \le 1.24$ -0.016 \le \beta_1 \le -0.013	$99.4 \le \beta'_0 \le 101$ $-1.29 \le \beta'_1 \le -1.03$	- 0 862	≤ 0.1	8 data points, each data point is for a particular batch and is the average of ~ 24 measurements on ~ 8 specimens. Velocity not greatly sensitive to mean pore size, mean pore orientation, and mean grain size	34
21	%TV = -0 916 • %P + 100	<u>- 0 999</u> 0.0001	$121 \le \beta_0 \le 122$ $-0.012 \le \beta_1 \le -0.011$	$99.8 \le \beta'_0 \le 100$ $-0.962 \le \beta'_1 \le -0.870$	- 1.09	< 5	6 data points	35
22	%TV = -0 883 • %P + 100	<u>- 0 957</u> 0 0001	$1.22 \le \beta_0 \le 1.22$ $-0.011 \le \beta_1 \le -0.010$	$99.9 \le \beta'_0 \le 100$ $-0.939 \le \beta'_1 \le 0.832$	- 1.13	< 1	194 data points	36
22	%TV = -0912 • %P + 100	<u>- 0.964</u> 0.0001	$1216 \le \beta_0 \le 1220$ $-0.012 \le \beta_1 \le -0.011$	$99.9 \le \beta'_0 \le 100$ $-0.939 \le \beta'_1 \le -0.832$	- 1.10		208 data points, all longitudinal wave data	37
786	%TV = -1.16 • %P + 100	<u>- 0 991</u> 0 0001	$0.711 \le \beta_0 \le 0.859$ $-0.010 \le \beta_1 \le -0.008$	$99.0 \le \beta'_0 \le 101$ $-1.32 \le \beta'_1 \le -1.01$	- 0.86	≤ 0.1	8 data points, most specimens from same batches used by Baaklini	38
							Comparison	39
11	%TV = -134 • %P + 100	N/A N/A	N/A	N/A	- 0.75		No correlation coefficient is given since only 2 data points, but each point is average of measurement on 25 specimens, data point in low 9σ porosity region is for hot-pressed Si_3N_4 while data point in high 9σ porosity is for reaction-bonded Si_3N_4	40

Materi a l	Reference	Processing Notes/ Chemical Additives	Microstructural Anisotropy	Velocity Measurement Technique	Velocity Measurement Uncertainty (%)	Density Measurement Technique	Density Measurement Uncertainty (%)	Theoretical Density, po. Used to Calculate % Peresity (g/cc)	Predicted Line Equation (V = β_1 • %P + β_2)
Si ₃ N ₄	37	Injection-molded, slip-cast, and hot- pressed specimens		Thru-transmission transit time, Longitudinal waves, 5 MHz				3.30	LV = -0 016 + %P + 1
Si ₃ N ₄	38	RBSN has < 1% impurities and various amounts of unreacted silicon	Insignificant	Pulse-echo overlap, Longitudinal waves, 15 MHz	≤ 0.1	Dry-wt dimensional	≤ 0.1	3.30	LV = -0.013 • %P + 1
Si ₃ N ₄	36-38			Longitudinal waves				3.30	LV = -0.014 • 96P + 1
Si ₃ N ₄	37	Injection-molded, slip-cast, and hot- pressed specimens		Thru-transmission transit time, Shear waves, 5 MHz				3.30	SV = -0.008 • %P + 0 6
Si ₃ N ₄	38	RBSN has < 1% impurities and various amounts of unreacted silicon	Insignificant	Pulse-echo overlap, Shear waves, 15 MHz	≤ 01	Dry-wt dimensional	≤ 01	3 30	SV = -0 007 • %P + 0 6
Si ₃ N ₄	37, 38			Shear waves				3.30	SV = -0.007 • %P + 0.64
Si ₃ N ₄	36-38					· · · · · · · · · · · · · · · · · · ·			
Steel A-direction (See ref.)	39		Possibly particle contact anistropy (≤ 5%) based on	Thru-transmission pulse-echo overlap, Dry coupling, Longi- tudinal waves, 1 5–2 25 MHz	≤ 0.01	ASTM B-328-60	Undetermined probably ≤ 296	7 85	LV = -0 007 • %P + 0 56
Steel B-direction (See ref.)	39		pressing direction	Thru-transmission pulse-echo overlap, Dry coupling, Longi- tudinal waves, 1.5-2.25 MHz	≤ 0 01	ASTM B-328-60	Undetermined, probably ≤ 24a	7.85	LV = -0 009 • %P + 0 58
Steel C-direction (See ref.)	39			Thru-transmission pulse-echo overlap, Dry coupling, Longi- tudinal waves, 1.5-2 25 MHz	≤ 0 01	ASTM B-328-60	Undetermined. probably ≤ 2%	7.85	LV = -0 009 • %P + 0 59
Steel	39								



IT POROSITY: REVIEW AND STATISTICAL ANALYSIS—CONTINUED

	Predicted Line Equation (%TV = $\beta'_1 \circ \%P + \beta'_0$)	Correlation Coefficient Level of Significance	95% Confidence Intervals for Predicted Intercapt (eta_{eta}) and Slope (eta_{eta})	95% Confidence Intervals for Predicted Intercept (β_{-1}^*) and Slope (β_{-1}^*)	Δ % P Δ % TV	Largest Velocity Variation Across One Surface of Specimen (%)	Comments	Corresponding Figure Numbe
.14	%TV = -1.41 • %P + 100	<u>- 0.997</u> 0.0001	$1.12 \le \beta_0 \le 1.16$ $-0.017 \le \beta_1 \le -0.015$	$98.6 \le \beta'_0 \le 101$ $-1.48 \le \beta'_1 \le -1.34$	- 0.71		13 data points	41
12	%TV = -1:15 • %P + 100	<u>- 0 991</u> 0 001	$0.928 \le \beta_0 \le 1.25$ $-0.016 \le \beta_1 \le -0.010$	$88.0 \le \beta'_0 \le 111$ $-1.44 \le \beta'_1 \le -0.864$	- 0.87		5 data points	42
12	%TV = -1.27 • %P + 100	<u>- 0.981</u> 0.0001	$1.08 \le \beta_0 \le 1.15$ $-0.016 \le \beta_1 \le -0.013$	$97.1 \le \beta'_0 \le 103$ $-1.40 \le \beta'_1 \le -1.15$	- 0.787		20 data points, all longitudinal wave data	43
652	%TV = -1.18 • %P + 100	<u>- 0 991</u> . 0.0001	$0.636 \le \beta_0 \le 0.667$ $-0.008 \le \beta_1 \le 0.007$	$97.6 \le \beta'_0 \le 102$ $-1.30 \le \beta'_1 \le -1.06$	- 0.85		11 data points	44
675	%TV ≈ -1.10 • %P + 100	<u>- 0 984</u> 0 002	$0.574 \le \beta_0 \le 0.776$ $-0.011 \le \beta_1 \le -0.004$	$85.0 \le \beta'_0 \le 115$ $-1.62 \le \beta'_1 \le -0.580$	- 0.91		5 data points	45
645	%TV = -1.07 • %P + 100	<u>- 0.973</u> 0.0001	$0.624 \le \beta_0 \le 0.666$ $-0.008 \le \beta_1 \le -0.006$	$96.6 \le \beta'_0 \le 103$ -1.22 \le \beta'_1 \le \cdot -0.928	- 0.935		16 data points, all shear wave data	46
							Companson	47
563	%TV ≈ -1.19 • %P + 100	<u>- 0 972</u> 0.0001	$0.551 \le \beta_0 \le 0.574$ $-0.007 \le \beta_1 \le -0.006$	$98.0 \le \beta'_0 \le 102$ -132 \le \beta'_1 \le -1.06	- 0.84		Measurements made in 3 directions (A, B, C) with respect to pressing direction for sintered steel rectangles; some residual particle contact anistropy may be responsible for small directional	48
588	%TV = -1.53 • %P + 100	<u>- 0 985</u> 0 0001	$0.573 \le \beta_0 \le 0.602$ $-0.010 \le \beta_1 \le -0.008$	$97.6 \le \beta'_{0} \le 102$ $1.68 \le \beta'_{1} \le -1.37$	- 0.65		dependence of velocity, velocity also may be path-length dependent 22 data points for A-direction 16 data points for B-direction 18 data points for C-direction	49
590	%TV = -1 48 • %P + 100	<u>- 0 996</u> 0 0001	$0.583 \le \beta_0 \le 0.597$ $-0.009 \le \beta_1 \le -0.008$	$98.8 \le \beta_0' \le 101$ -1.54 $\le \beta_1' \le -1.41$	- 0 68			50
1							Companson	51

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TABLE I.-ULTRASONIC VELOCITY VERSUS PERCENT POROSITY: RE

Materiai	Reference	Processing Notes/ Chemical Additives	Microstructural Anisotropy	Velocity Measurement Technique	Velocity Measurement Uncertainty (%)	Density Measurement Technique	Density Measurement Uncertainty (%)	Theoretical Density, Pa. Used to Calculate % Porosity (g/cc)	Predicted Predicted Line Equation $(V = \beta_1 \cdot \text{ %P} + \beta_0)$	Pred (%TV
Tungsten	2	Kenna nominal 4 micron starting powder size		Thru-transmission pulse-echo overlap. Longitudinal waves. 1 MHz	≤ 0.5	ASTM C20-46 Liquid- immersion	≤ 2	19 3	LV = -0 005 • %P + 0 520	%TV =
Tungsten	2	G E. nominal 4 micron starting powder size		Thru-transmission pulse-echo overlap, Longitudinal waves.	≤ 0.5	ASTM C20-46 Liquid- immersion	≤ 2	19 3	LV = -0 006 • %P + 0 558	%TV =
Tungsten	2	G E nominal 18 micron starting powder size		Thru-transmission pulse-echo overlap, Longitudinal waves, 1 MHz	≤ 0.5	ASTM C20-46 Liquid- immersion	≤ 2	19.3	LV = -0 008 • %P + 0 554	%TV =
Tungsten	2			Longitudinal waves				19 3	LV = -0 006 • %P + 0.533	%TV =
Tungsten	2									
NO ⁵	40			Thickness-cum- velocity meter, Longitudinal waves, 10 MHz	≤ 1	ASTM C-753-88	≤ 2	10 96	LV = -0.008 • %P + 0.550	%TV =
(U _{0 30} Pu _{0 70})C	41			Thickness-cum- velocity meter, Longitudinal waves, 15 MHz	≤ 1	ASTM C-753-88	≤ 2	12 19	LV = -0 004 • %P + 0 460	%TV = -
YBa ₂ Cu ₃ O _{7 - x}	43	Different starting powders		Pulse-echo/cross- correlation, Longitu- dinal waves, Dry and wet coupling, 5-20 MHz	≤ 0.4	Dry-wt dimensional	≤ 1	6.38	LV = ~0 007 • %P + 0 565	%TV



POROSITY: REVIEW AND STATISTICAL ANALYSIS—CONTINUED

	Predicted Line Equation (%TV = $\beta'_1 \circ \text{%P} + \beta'_0$)	Correlation Coefficient Level of Significance	95% Confidence intervals for Predicted intercept (β_{θ}) and Slope (β_{1})	95% Confidence Intervals for Predicted Intercept (β'_{0}) and Slope (β'_{1})	44 TV	Largest Velocity Variation Across One Surface of Specimen (%)	Comments	Correspondin Figure Numbe
520	%TV = -0.939 • %P + 100	<u>- 0 960</u> 0.010	$0.465 \le \beta_0 \le 0.575$ $-0.007 \le \beta_1 \le -0.003$	$89.4 \le \beta'_0 \le 111$ $-1.38 \le \beta'_1 \le -0.501$	1.06		Velocity shown to be sensitive to pore size distribution/mean pore size and grain size distribution/mean grain size which is a function of starting powder size distributions.	52
558	%TV = -1.13 • %P + 100	<u>- 0.918</u> 0.028	$0.387 \le \beta_0 \le 0.729$ $-0.007 \le \beta_1 \le -0.006$	$69.3 \le \beta'_0 \le 131$ $-1.92 \le \beta'_1 \le -0.351$	- 0 88		bution. These results show different theoretical velocity for tungsten depending on the starting powder size. 5 data points for Kenna 4 µm powder. 5 data points for GE 4 µm powder. 4 data points for GE 18 µm powder.	53
554	%TV ≈ -1.38 • %P + 100	<u>- 0.992</u> 0 008	$0.471 \le \beta_0 \le 0.637$ $-0.011 \le \beta_1 \le -0.005$	$85.1 \le \beta'_0 \le 115$ $-1.92 \le \beta'_1 \le -0.832$	- 0.72		Each data point is average of 17 meas- urements across sample	54
533	%TV = -1.11 • %P + 100	<u>- 0.916</u> 0.0001	$0.482 \le \beta_0 \le 0.583$ $-0.008 \le \beta_1 \le -0.004$	$90.5 \le \beta'_0 \le 109$ $-1.41 \le \beta'_1 \le -0.802$	- 0.901		14 data points, all longitudinal wave data	55
							Comparison	56
550	%TV = -1 49 • %P + 100	<u>- 0.997</u> 0.0001	$0.547 \le \beta_0 \le 0.552$ $-0.009 \le \beta_1 \le 0.008$	$99.5 \le \beta'_0 \le 100$ $-2.09 \le \beta'_1 \le -0.883$	- 0 67		17 data points	57
160	%TV = -0 958 • %P + 100	<u>- 0.949</u> 0.051	$0.422 \le \beta_0 \le 0.496$ $-0.009 \le \beta_1 \le 0.00003$	$92.0 \le \beta'_0 \le 108$ $-1.92 \le \beta'_1 \le 0.005$	- 1.04		4 data points	58
.65	%TV = -1 28 • %P + 100	<u>- 0 991</u> 0 0001	$0.554 < \beta_0 < 0.576$ $-0.008 < \beta_1 < -0.007$	$98.0 < \beta'_0 < 102$ $-1.39 < \beta'_1 < -1.16$	- 0.781		13 data points	59

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TABLE I.-ULTRASONIC VELOCITY VERSUS PERCENT P

Material	Reference	Processing Notes/ Chemical Additives	Microstructural Anisotropy	Velocity Measurement Technique	Velocity Measurement Uncertainty (%)	Density Measurement Technique	Density Measurement Uncertainty (%)	Theoretical Density, p ₀ . Used to Calculate % Porosity (g/cc)	Predicted Line Equation (V = $\beta_1 \circ {}^{4}\!\!\!/ \mathrm{P} + \beta_0$)
	43		Insignificant	Pulse-echo/cross- correlation, Shear waves, 10 MHz	≤ 0.4	Dry-wt dimensional	≲ 1	6 38	SV = -0 002 • %P + 0 31
	42			Phase comparison method, Shear waves, 50 MHz	≤ 2				
YBa ₂ Cu ₃ O _{7 - x} Superconductor	11			Pulse-echo overlap, Shear waves, 3-10 MHz	≤ 1 dimensional	Dry-wt	≤ 1		
	44			Pulse-echo matchup, Shear waves, 3-4 MHz	≤ 1	Dry-wt dimensional	≤ 1		
	45			Thru-transmission pulse-echo overlap, Shear waves, 5 MHz	≤ 3	Eiquid- immersion	≤ 2		
YBa ₂ Cu ₃ O _{7 - x}	11, 42-45								

POROSITY: REVIEW AND STATISTICAL ANALYSIS—CONCLUDED

	Predicted Line Equation (%TV = $\beta'_1 \circ \%P + \beta'_8$)	Correlation Coefficient Level of Significance	95% Confidence Intervals for Predicted Intercept (β_0) and Stope (β_1)	95% Confidence Intervals for Predicted Intercept (3° ₄) and Slope (6° ₁)	Δ% P Δ% TV	Largest Velocity Variation Across One Surface of Specimen (%)	Comments	Corresponding Figure Number
	Î						data point, sample was single-phase, untextured, and free of nonuniform stress data point	
:13	%TV = -0.768 • %P + 100	<u>- 0 814</u> 0 0486	$0.252 \le \beta_0 \le 0.373$ $-0.005 \le \beta_1 \le -0.00002$	$81.6 \le \beta'_0 \le 119$ $-1.53 \le \beta'_1 \le -0.007$	-1.30		2 data points, samples are not composi- tionally homogeneous 1 data point	60
							1 data point	
							Comparison	61

TABLE II.—COMPARISON OF V₀ PREDICTED FROM REGRESSION ANALYSIS WITH THAT CALCULATED FROM EQUATIONS 7 (LONGITUDINAL VELOCITY) AND 7a (SHEAR WAVE VELOCITY)

		צ	Longitudinal Wave Velocity	elocity		Shear Wave Velocity	ify	Vaiues sul (For Longitud (7a) (For !	Values substituted into eqs. (7) [For Longitudinal Wave Velocity] and (7a) [For Shear Wave Velocity] to obtain V _{oC}	(7)] and [y]
Material	Single crystal (S) or poly- crystalline (P)	Average V _o from regression (V _{OR}) [cm/µsec]	Calculated Vo from eq. (7) (Voc) [cm/µsec]	% Variation between V_{0c} and V_{0q} = 100 · $V_{0c} - V_{0q} \cdot \int V_{0c}$	Average Vo from regression (V _{oR}) [cm/µsec]	Calculated Vo from eq. (7a) (Vo _C) [cm/ _s sec]	% Variation between V_{oc} and V_{oR} = 100 · V_{oc} — V_{oR} / V_{oc}	Fully-dense elastic modulus, E _o (x 10-6) psi //ref.)	Poisson's ratio, v/(ref.)	Theoretical density, Po (g/cm ³)
Al ₂ 0 ₃	S		1.10	3.6		0.643	2.2	58.4/(Ref. 3)	0.25/(Ref. 48)	3.98
	۵	90-	1.12	5.4	0.657	0.659	0.30	61.2/(Ref. 3)	0.25/(Ref. 48)	3.98
SiC	s		1.16	5.5		0:730	7.7	58.2/(Ref. 3)	0.17/(Ref. 49)	3.22
	٩	1.22	1.22	0.0	0.786	0.769	2.2	64.6/(Ref. 3)	0.17/(Ref. 49)	3.22
Si ₃ N ₄	a.	1.12	0.977	15.4	29'0	0.585	12.3	40.0/(Ref. 3)	0.22/(Ref. 3)	3.30
200	S		0.558	1.4				33.4/(Ref. 3)	0.33/(Ref. 3)	10.69
	۵	0.550	0.551	0.2				32.6/(Ref. 3)	0.33/(Ref. 3)	10.69
YBa ₂ Cu ₃ 0 _{7 - x}	d.	0.565	0.594	4.8	0.313	0.374	16.3	32.8/(Ref. 46)	0.27/(Ref. 11)	6.38
Steel	d	0.580	0.614	5.5				29.0/(Ref. 47)	0.33/(Ref. 47)	7.85
Tungsten	۵	0.541	0.509	6.1				58.0/(Ref. 47)	0.27/(Ref. 47)	19.3

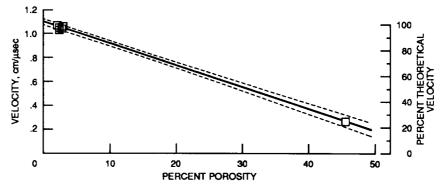


Figure 1. - Longitudinal velocity versus percent porosity for Al_2O_3 (ref. 24). Velocity = -0.018 x percent porosity + 1.09. Percent theoretical velocity = -1.65 x percent porosity + 100. Correlation coefficient = -0.999.

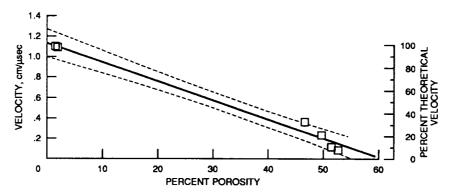


Figure 2. - Longitudinal velocity versus percent porosity for Al_2O_3 (ref. 25). Velocity = -0.019 x percent porosity + 1.13. Percent theoretical velocity = -1.64 x percent porosity + 100. Correlation coefficient = -0.992.

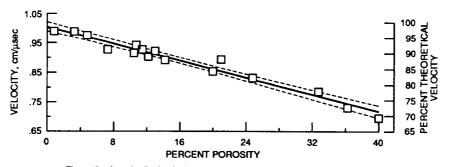


Figure 3. - Longitudinal velocity versus percent porosity for Al_2O_3 (ref. 16). Velocity = -0.007 x percent porosity + 1.00. Percent theoretical velocity = -0.736 x percent porosity + 100. Correlation coefficient = -0.982.

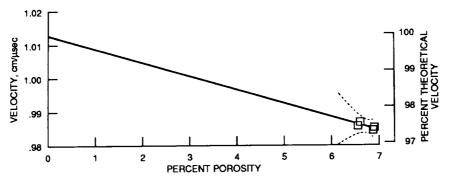


Figure 4. - Longitudinal velocity versus percent porosity for Al_2O_3 (ref. 26). Velocity = -0.004 x percent porosity + 1.01. Percent theoretical velocity = -0.377 x percent porosity + 100. Correlation coefficient = -0.698.

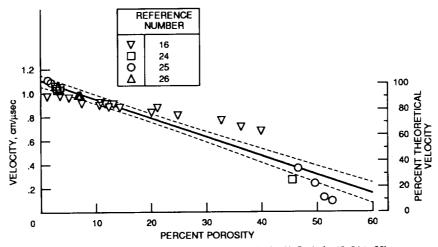


Figure 5. - Longitudinal velocity versus percent porosity for Al_2O_3 (refs. 16, 24 to 26). Velocity = -0.016 x percent porosity + 1.10. Percent theoretical velocity = -1.43 x percent porosity + 100. Correlation coefficient = -0.949.

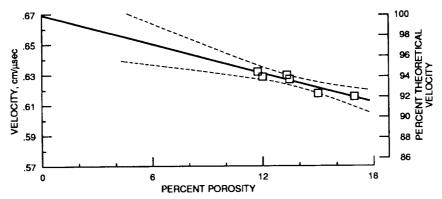


Figure 6. - Shear velocity versus percent porosity for Al_2O_3 (ref. 27). Velocity = -0.003 x percent porosity + 0.669. Percent theoretical velocity = -0.477 x percent porosity + 100. Correlation coefficient = -0.936.

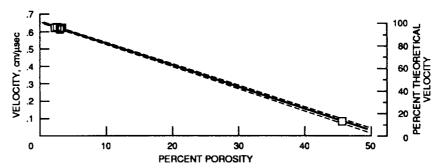


Figure 7. - Shear velocity versus percent porosity for Al_2O_3 (ref. 24). Velocity = -0.012 x percent porosity + 0.655. Percent theoretical velocity = -1.87 x percent porosity + 100. Correlation coefficient = -1.00.

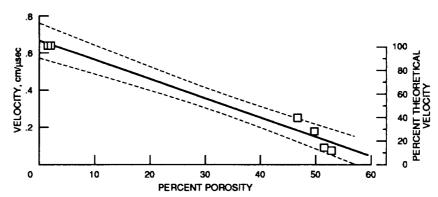


Figure 8. - Shear velocity versus percent porosity for Ai_2O_3 (ref. 25). Velocity = -0.010 x percent porosity + 0.666. Percent theoretical velocity = -1.55 x percent porosity + 100. Correlation coefficient = -0.987.

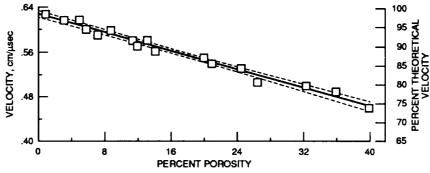


Figure 9. - Shear velocity versus percent porosity for Al_2O_3 (ref. 16). Velocity = -0.004 x percent porosity + 0.628. Percent theoretical velocity = -0.662 x percent porosity + 100. Correlation coefficient = -0.990.

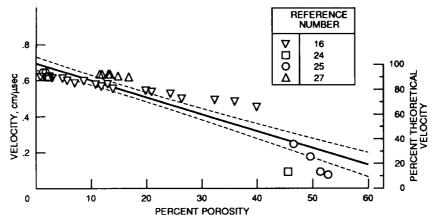


Figure 10. - Shear velocity versus percent porosity for Al_2O_3 (refs. 16, 24, 25, 27). Velocity = -0.009 x percent porosity + 0.693. Percent theoretical velocity = -1.35 x percent porosity + 100. Correlation coefficient = -0.910.

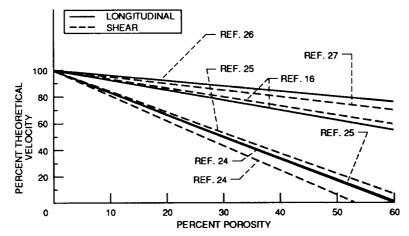


Figure 11. - Ultrasonic velocity versus percent porosity for Al₂O₃ (refs. 16, 24 to 27).

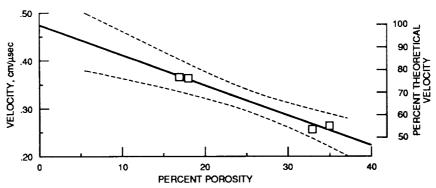


Figure 12. - Longitudinal velocity versus percent porosity for CuO (ref. 28). Velocity = -0.006 x percent porosity + 0.474. Percent theoretical velocity = -1.34 x percent porosity + 100. Correlation coefficient = -0.990.

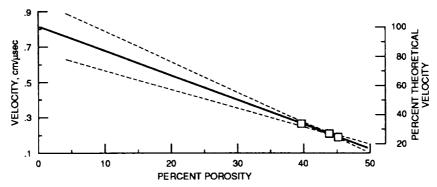


Figure 13. - Longitudinal velocity versus percent porosity for "green" M_gO (ref. 29). Velocity = -0.018 x percent porosity + 0.817. Correlation coefficient = -1.00.

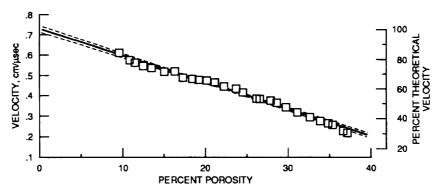


Figure 14. - Longitudinal velocity versus percent porosity for porcelain (ref. 7). Velocity = -0.013 x percent porosity + 0.728. Percent theoretical velocity = -1.78 x percent porosity + 100. Correlation coefficient = -0.994.

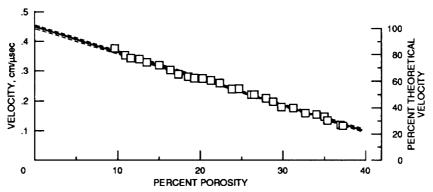


Figure 15. - Shear velocity versus percent porosity for porcelain (ref. 7). Velocity = -0.009 x percent porosity + 0.448. Percent theoretical velocity = -1.93 x percent porosity + 100. Correlation coefficient = -0.998.

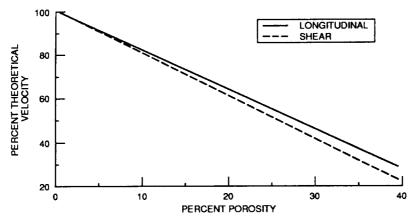


Figure 16. - Ultrasonic velocity versus percent porosity for porcelain (ref. 7).

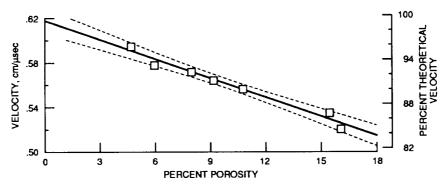


Figure 17. - Longitudinal velocity versus percent porosity for porcelain (ref. 30). Velocity = -0.006 x percent porosity + 0.618. Percent theoretical velocity = -0.935 x percent porosity + 100. Correlation coefficient = -0.987.

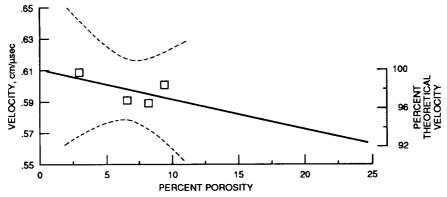


Figure 18. - Longitudinal velocity versus percent porosity for porcelain P1 (ref. 31). Velocity = -0.002 x percent porosity + 0.611. Percent theoretical velocity = -0.312 x percent porosity + 100. Correlation coefficient = -0.586.

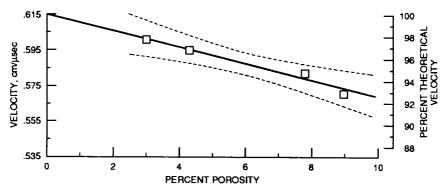


Figure 19. - Longitudinal velocity versus percent porosity for porcelain P2 (ref. 31). Velocity = -0.005 x percent porosity + 0.615. Percent theoretical velocity = -0.740 x percent porosity + 100. Correlation coefficient = -0.983.

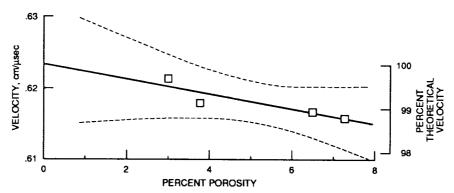


Figure 20. - Longitudinal velocity versus percent porosity for porcelain T1 (ref. 3). Velocity = -0.001 x percent porosity + 0.623. Percent theoretical velocity = -0.167 x percent porosity + 100. Correlation coefficient = -0.894.

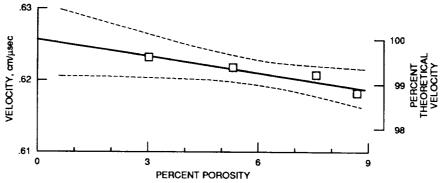


Figure 21. - Longitudinal velocity versus percent porosity for porcelain T2 (ref. 31). Velocity = -0.001 x percent porosity + 0.626. Percent theoretical velocity = -0.121 x percent porosity + 100. Correlation coefficient = -0.947.

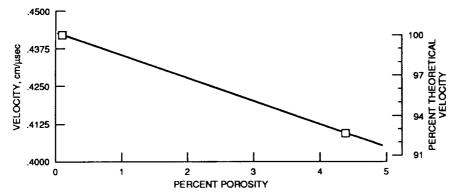


Figure 22. - Longitudinal velocity versus percent porosity for unpoled PZT4 (ref. 8). Velocity = -0.007 x percent porosity + 0.443. Percent theoretical velocity = -1.68 x percent porosity + 100.

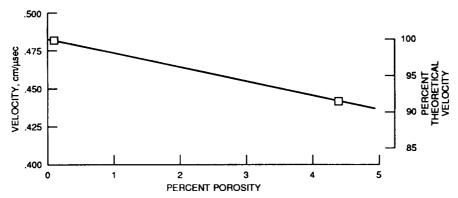


Figure 23. - Longitudinal velocity versus percent porosity for poled PZT4 (ref. 8). Velocity = -0.009 x percent porosity + 0.483. Percent theoretical velocity = -1.93 x percent porosity + 100.

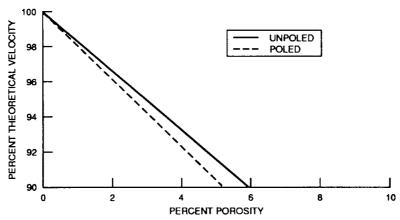


Figure 24. - Ultrasonic velocity versus percent porosity for PZT4 (ref. 8).

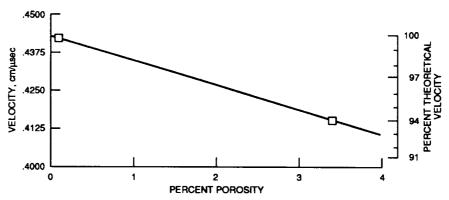


Figure 25. - Longitudinal velocity versus percent porosity for unpoled PZT5 (ref. 8). Velocity = -0.008 x percent porosity + 0.443. Percent theoretical velocity = -1.85 x percent porosity + 100.

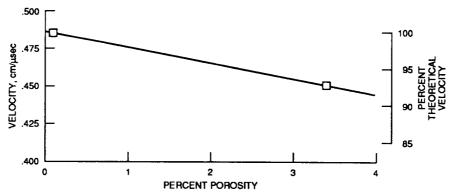


Figure 26. - Longitudinal velocity versus percent porosity for poled PZT5 (ref. 8). Velocity = -0.010 x percent porosity + 0.486. Percent theoretical velocity = -2.12 x percent porosity + 100.

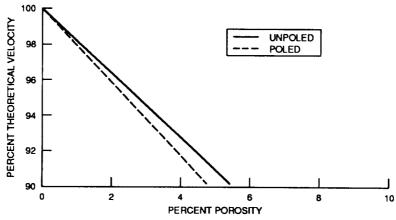


Figure 27. - Ultrasonic velocity versus percent porosity for PZT5 (ref. 8).

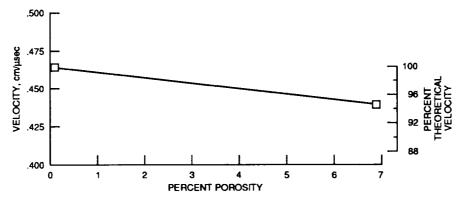


Figure 28. - Longitudinal velocity versus percent porosity for unpoled PZT7 (ref. 8). Velocity = -0.004 x percent porosity + 0.464. Percent theoretical velocity = -0.760 x percent porosity + 100.

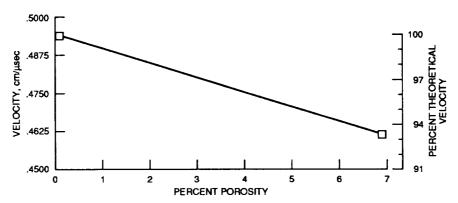


Figure 29. - Longitudinal velocity versus percent porosity for poled PZT7 (ref. 8). Velocity = -0.005 x percent porosity + 0.494. Percent theoretical velocity = -0.952 x percent porosity + 100.

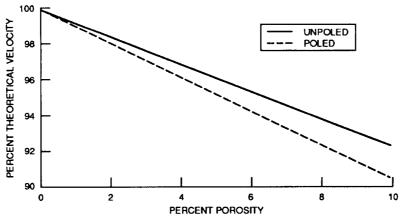


Figure 30. - Ultrasonic velocity versus percent porosity for PZT7 (ref. 8).

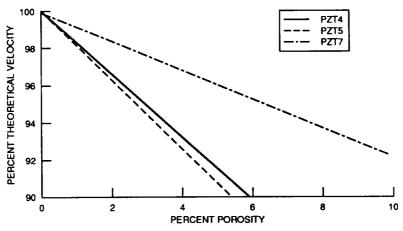


Figure 31. - Ultrasonic velocity versus percent porosity for unpoted PZT (ref. 8).

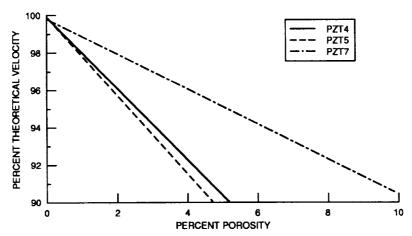


Figure 32. - Ultrasonic velocity versus percent porosity for poled PZT (ref. 8).

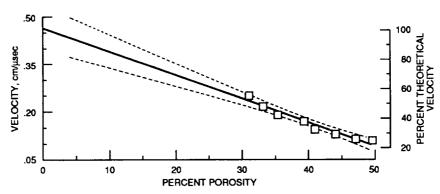


Figure 33. - Longitudinal velocity versus percent porosity for green SiC (ref. 32). Velocity = -0.007 x percent porosity + 0.464. Correlation coefficient = -0.974.

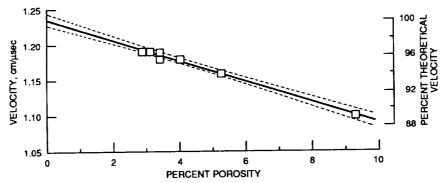


Figure 34. - Longitudinal velocity versus percent porosity for SiC (ref. 33). Velocity = -0.014 x percent porosity + 1.23. Percent theoretical velocity = -1.16 x percent porosity + 100. Correlation coefficient = -0.993.

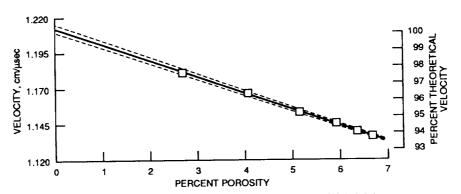


Figure 35. - Longitudinal velocity versus percent porosity for SiC (ref. 34). Velocity = -0.011 x percent porosity + 1.21. Percent theoretical velocity = -0.916 x percent porosity + 100. Correlation coefficient = -0.999.

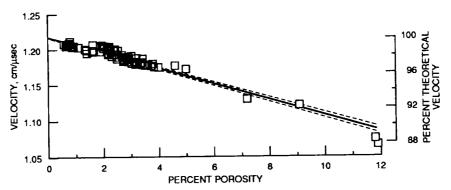


Figure 36. - Longitudinal velocity versus percent porosity for SiC (ref. 35). Velocity = -0.011 x percent porosity + 1.22. Percent theoretical velocity = -0.883 x percent porosity + 100. Correlation coefficient = -0.957.

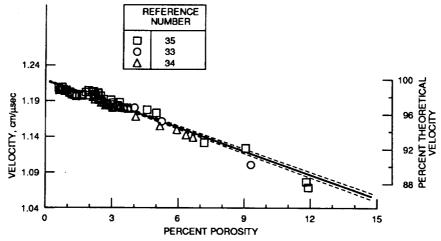


Figure 37. - Longitudinal velocity versus percent porosity for SiC (refs. 33 to 35). Velocity = -0.011 x percent porosity + 1.22. Percent theoretical velocity = -0.912 x percent porosity + 100. Correlation coefficient = -0.964.

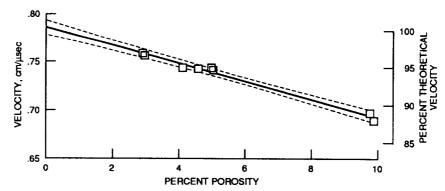


Figure 38. - Shear velocity versus percent porosity for SIC (ref. 26). Velocity = -0.009 x percent porosity + 0.786. Percent theoretical velocity = -1.16 x percent porosity + 100. Correlation coefficient = -0.991.

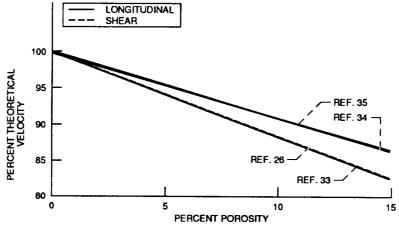


Figure 39. - Ultrasonic velocity versus percent porosity for SiC (refs. 26, 33 to 35).

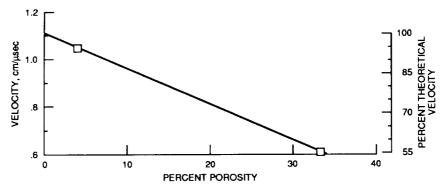


Figure 40. - Longitudinal velocity versus percent porosity for $\mathrm{Si}_3\mathrm{N}_4$ (ref. 36). Velocity = -0.015 x percent porosity + 1.11. Percent theoretical velocity = -1.34 x percent porosity + 100.

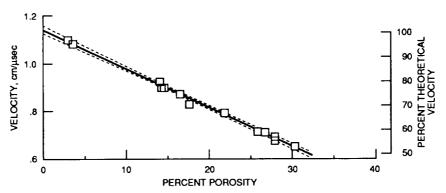


Figure 41. - Longitudinal velocity versus percent porosity for Si_3N_4 (ref. 37). Velocity = -0.016 x percent porosity + 1.14. Percent theoretical velocity = -1.41 x percent porosity + 100 Correlation coefficient = -0.997.

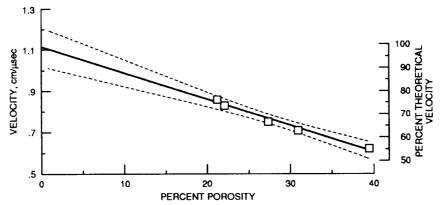


Figure 42. - Longitudinal velocity versus percent porosity for $\mathrm{Si}_3\mathrm{N}_4$ (ref. 38). Velocity = -0.013 x percent porosity + 1.12. Percent theoretical velocity = -1.15 x percent porosity + 100 Correlation coefficient = -0.991.

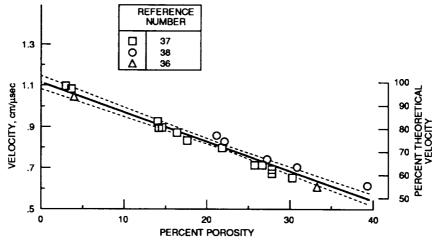


Figure 43. - Longitudinal velocity versus percent porosity for $\mathrm{Sl}_3\mathrm{N}_4$ (refs. 36 to 38). Velocity = -0.014 x percent porosity + 1.12. Percent theoretical velocity = -1.27 x percent porosity + 100 Correlation coefficient = -0.981.

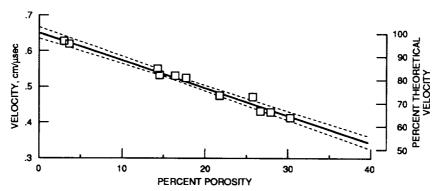


Figure 44. - Shear velocity versus percent porosity for $\mathrm{Si}_3\mathrm{N}_4$ (ref. 37). Velocity = -0.008 x percent porosity + 0.652. Percent theoretical velocity = -1.18 x percent porosity + 100 Correlation coefficient = -0.991.

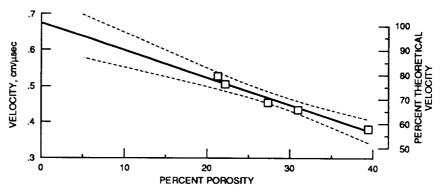


Figure 45. - Shear velocity versus percent porosity for $\mathrm{Si}_3\mathrm{N}_4$ (ref. 38). Velocity = -0.007 x percent porosity + 0.675. Percent theoretical velocity = -1.10 x percent porosity + 100 Correlation coefficient = -0.984.

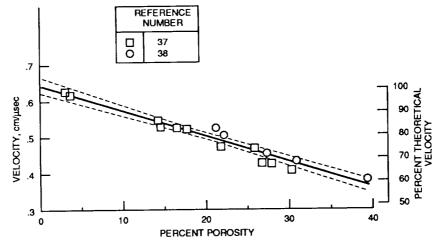


Figure 46. - Shear velocity versus percent porosity for Si_3N_4 (refs. 37, 38). Velocity = -0.007 x percent porosity + 0.645. Percent theoretical velocity = -1.07 x percent porosity + 100 Correlation coefficient = -0.973.

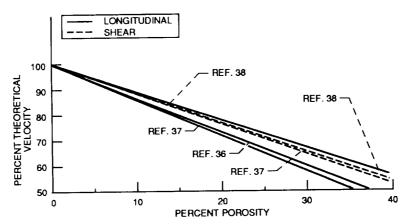


Figure 47. - Ultrasonic velocity versus percent porosity for $\mathrm{Si}_3\mathrm{N}_4$ (refs. 36 to 38).

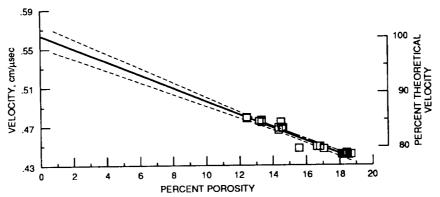


Figure 48. - Longitudinal velocity measured in the A direction versus percent porosity for steel (ref. 39). Velocity = -0.007 x percent porosity + 0.563. Percent theoretical velocity = -1.19 x percent porosity + 100. Correlation coefficient = -0.972.

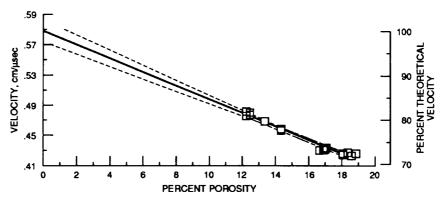


Figure 49. - Longitudinal velocity measured in the B direction versus percent porosity for steel (ref. 39).

Velocity = -0.009 x percent porosity + 0.588.

Percent theoretical velocity = -1.53 x percent porosity + 100.

Correlation coefficient = -0.985.

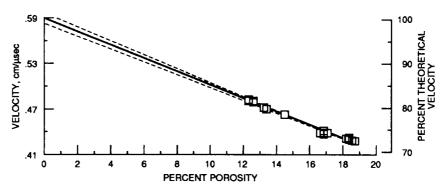


Figure 50. - Longitudinal velocity measured in the C direction versus percent porosity for steel (ref. 39). Velocity = $-0.009 \times \text{percent porosity} + 0.590$. Percent theoretical velocity = $-1.48 \times \text{percent porosity} + 100$. Correlation coefficient = -0.996.

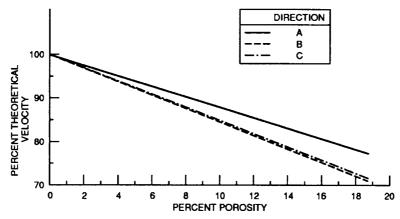


Figure 51. - Ultrasonic velocity versus percent porosity for steel (ref. 39).

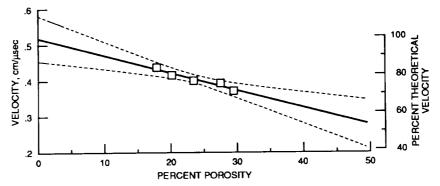


Figure 52. - Longitudinal velocity versus percent porosity for tungsten (ref. 2) with Kenna nominal 4 µm starting powder size.

Velocity = -0.005 x percent porosity + 0.520.

Percent theoretical velocity = -0.939 x percent porosity + 100.

Correlation coefficient = -0.960.

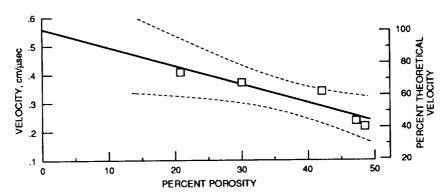


Figure 53. - Longitudinal velocity versus percent porosity for tungsten (ref. 2) with General Electric nominal 4 μ m starting powder size. Velocity = -0.006 x percent porosity + 0.558. Percent theoretical velocity = -1.13 x percent porosity + 100. Correlation coefficient = -0.918.

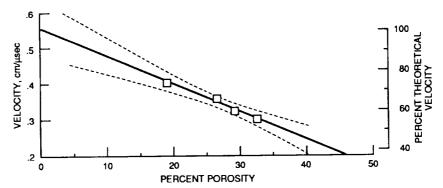


Figure 54. - Longitudinal velocity versus percent porosity for tungsten (ref. 2) with General Electric nominal 18 µm starting powder size. Velocity = -0.008 x percent porosity + 0.554. Percent theoretical velocity = -1.38 x percent porosity + 100. Correlation coefficient = -0.992.

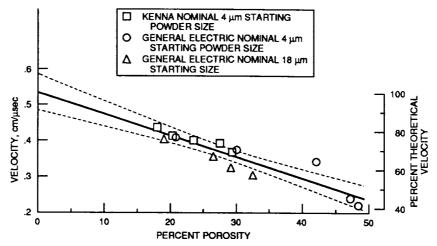


Figure 55. - Longitudinal velocity versus percent porosity for tungsten (ref. 2). Velocity = -0.006 x percent porosity + 0.533. Percent theoretical velocity = -1.11 x percent porosity + 100. Correlation coefficient = -0.916.

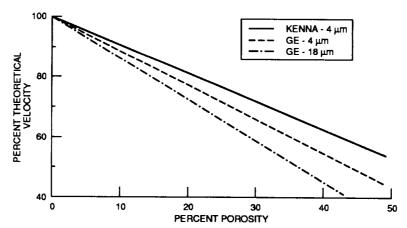


Figure 56. - Longitudinal velocity versus percent porosity for tungsten (ref. 2).

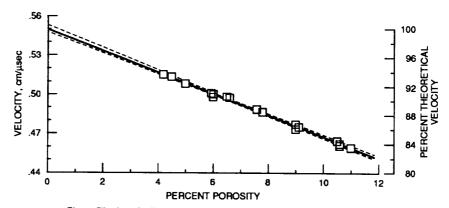


Figure 57. - Longitudinal velocity versus percent porosity for UO₂ (ref. 40). Velocity = -0.008 x percent porosity + 0.550. Percent theoretical velocity = -1.49 x percent porosity + 100. Correlation coefficient = -0.997.

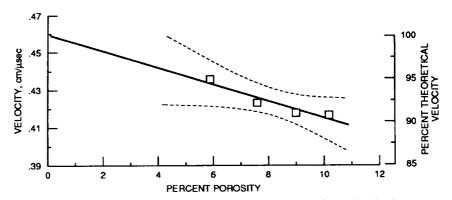


Figure 58. - Longitudinal velocity versus percent porosity for $(U_{0.30}Pu_{0.70})C$ (ref. 41). Velocity = -0.004 x percent porosity + 0.480. Percent theoretical velocity = -0.958 x percent porosity + 100. Correlation coefficient = -0.949.

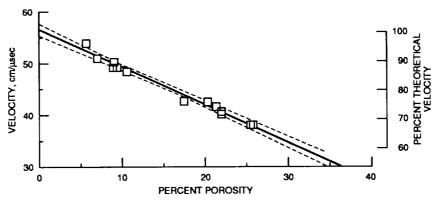


Figure 59. - Longitudinal velocity versus percent porosity for $YBa_2Cu_3O_{7-x}$ (ref. 43). Velocity = -0.007 x percent porosity + 0.565. Percent theoretical velocity = -1.28 x percent porosity + 100. Correlation coefficient = -0.991.

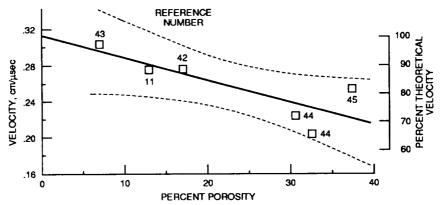


Figure 60. - Shear velocity versus percent porosity for $YBa_2Cu_3O_{7-x}$ (refs. 11, 42 to 45). Velocity = -0.002 x percent porosity + 0.313. Percent theoretical velocity = -0.768 x percent porosity + 100. Correlation coefficient = -0.814.

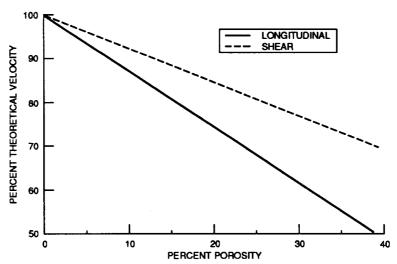


Figure 61. - Ultrasonic velocity versus percent porosity for YBa $_2$ Cu $_3$ O $_{7-x}$ (refs 11, 42 to 45).

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A review and statistical analysis of crystalline materials is presented. relationship between ultrasonic velor many researchers, scatter plots of porcelain-based ceramics, PZT, Si regression analysis produced prediction confidence interval statistics for the materials are in good agreement were materials.	Initially, a semi-empirical locity and porosity fraction velocity versus percent pic, Si ₃ N ₄ , steel, tungsten cted slope, intercept, core data. Velocity values percent in the context of the context	on Then, from porosity data ar , UO ₂ , (U _{0.30} Porelation coeffic predicted from)	eloped showing the original a compilation of data e shown for Al ₂ O ₃ , Cu _{0.70})C, and YBa ₂ Cu ₃ O itent, level of significant regression analysis for	gin of the linear produced by iO, MgO, b_{7-x} . Linear
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