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Robust and Secure Digital Image Watermarking Technique Using Arnold Transform and Memristive Chaotic Oscillators

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ABSTRACT

With the advent of technology and multimedia production, the world has witnessed a tremendous increase in digital media attacks, which duplicates, forges and tamper the data leading to the violation of copyright laws. In this paper, a robust and secure digital image watermarking is proposed, which exploits the chaotic behaviour of the non – linear oscillators realized through Memristive diodes. The proposed scheme relies on a Human Visual System (HVS) model in order to mimic the real-life scenario. To improve the robustness of the proposed approach and to further increase the security of the digital watermarked media whilst still retaining compatibility with the real-time events, Histogram of Oriented Gradients (HOG) and extreme learning machine (ELM) is implemented. Secure key generation by means of scrambling through Arnold Transform and the coefficients of Memristive Chaotic Oscillator ensures extreme security. The watermark embedding followed the pixel transformation based on discrete cosine coefficient modification, and a semi-blind watermarking extraction procedure was carried out through trained ELM models. A detailed analysis has been presented to evaluate the tradeoff between imperceptibility, security and robustness using performance metrics like PSNR, NC, SSIM, and BER. To establish a real-time implementation of the proposed architecture, the simulated results were verified using real-time chaotic signals generated from the chaotic oscillator, which dictates excellent performance against watermarking attacks and image processing tasks.

INDEX TERMS Chaotic Encryption, Memristor, Arnold Transform, Histogram of Oriented Gradients (HOG), Human Visual Systems (HVS), Extreme Machine Learning (ELM), Discrete Cosine Transform (DCT)

I. INTRODUCTION

The rapid developments in the computer era have led to an exponential increase in digital media production and usage. Consequently, the cases of data duplication forging and tampering have significantly raised a concern towards data encryption and security and ultimate copyright protection of the digital media. Out of the several possible solutions, copy detection, steganography, and digital watermarking

techniques are one such method that targets this problem and aims at embedding the information into more protected information in a characteristic manner [1]. The embedded data replicates the host image visually but makes it more secure by encrypting the information prone to malicious image processing attacks [2]. Whenever a copyright issue is encountered, the media is extracted using a watermarking technique.

These techniques can be broadly classified into two types: (1) Spatial based, which operates on the pixel location by embedding the watermark into the least significant bit (LSB) of the original image, and (2) Frequency – based, which first converts the signal into the frequency domain and embeds and modifies the frequency coefficients after the transforms. However, spatial transforms are less robust but are computationally less complex and have a better payload capacity than the frequency domain, which is found to be more robust, more secure, and offers better invisibility [3]. Literature has demonstrated several techniques like which involves frequency and spatial domain analysis. Frequency domain based transforms like discrete Fourier Transforms (DFT), discrete wavelet transforms (DWT), discrete cosine transforms (DCT) etc., have been studied rigorously. However, it has been well established that using two or more transforms (hybrid) can yield better results. Fazil *et. al.* [4] and Singh *et. al.* [5] has proposed a robust technique based on DWT, DCT with Singular Value Decomposition (SVD). Hwai and his group [6] have proposed that using sign correction, level shifting, mixed modulation, and orthogonal restoration, the process can be made more effective by improving invisibility and robustness. Recently, Liu and his group [7] have demonstrated a hybrid integer wavelet transform (IWT) and DCT to show the double encryption technique. Najafi *et. al.* [8] proposed a watermarking technique in which the group proposed a watermarking algorithm based on sharp frequency localized contourlet transform (SELCT) with SVD, which proved to solve the false positive problem and is resistant to ambiguity attacks. Several people have analyzed different matrix decomposition methods like Schur decomposition, SVD and LU decomposition. Makbol *et. al.* [9] demonstrated a block-based DWT and SVD image watermarking scheme in which they consider entropy as the HVS feature. Over the past few years, people have used fractal dimensions. Mishra *et. al.* [10] have proposed a robust and secure watermarking architecture based on fractal dimensions using the human visual system (HVS) model and Mamdani based Fuzzy Interface System (FIS). Over the past few years, several other techniques like using semi – blind Human Visual System [11], Dual Tree Complex Wavelet Transform – Discrete Cosine Transform (DTCWT – DCT) [12] and 2 Dimensional – Discrete Cosine Transform (2D – DCT) [13] have been introduced and studied. Hosny *et. al.* [14] have demonstrated a fractional order exponent moment watermarking technique. Quaternion based techniques have also emerged as a promising method in image watermarking [15][16]. To make the watermarking more effective and faster, researchers have now moved to various machine learning and deep learning techniques. Extreme Learning Machine (ELM) which can be considered as a special case of neural network with single layer feed – forward, has gained enormous interest due to its better generalization capability and good payload capability to handle large data and is widely used nowadays [17-19]. Ding *et. al.* [20] have recently proposed a generalized deep neural

network approach used for watermarking. One major limitation of the neural network approach is the high computational time in case of heavy net with large number of hidden neurons and more vulnerability to statistical attacks like JPEG compressions [20][21]. Recently a parallel multi-core CPU and GPU has been proposed targeting medical images which shows a promising research trend setup in the domain [22]. Several works have also demonstrated extraction of watermark coefficient directly from the host image itself using different processing tasks [10][23].

From the security perspective, chaotic systems are widely used for information encryption as chaotic cryptography over the conventional encryption algorithms like data encryption standard (DES), advanced encryption standard (AES) etc. which are known to have redundancy and correlation problem [23-29]. Chaotic signals are the non – linear signals which are highly sensitive to the system parameters and initial conditions. The random and unpredictable nature of such signals meets the requirements such as diffusion and mixing hence facilitates them to act as encryption keys. Hu *et. al.* [24] have proposed a blind watermarking algorithm where the robustness of the proposed algorithm is tested in the chaotic sequence generated by the logistic system. Bhatti *et. al.* [25] had discussed a hybrid watermarking algorithm using Clifford algebra and Arnold transform. Due to pseudorandom and ergodic properties, the chaotic system is gaining great interest among researchers to study data encryption for better security against geometric attacks [26-29].

Over the past few years, extensive research has been done on utilizing mathematical tools and formulating theoretical approaches for building an effective digital watermarking model. However, there is still a gap when it comes to practical implementations which can be summarized as follows:

- Usage of complex image transformation methods or complex encryption algorithms for enhancing the security unnecessarily leads to extremely high computational complexities and operation cost.
- During data embedding, it is important to capture the features of image in efficient manner while taking care of the security. However, previous reported works either use a large block sized image or considers a very small portion of image which fails to capture the data appropriately; or leading to severe data protection and security concerns.
- While dealing with the DC coefficients, it is necessary to handle the high frequency components in order to maintain the robustness and imperceptibility.
- Further, enhancing and optimizing the pre – processing steps and improving the masking ability while maintaining the payload, computational time and operating cost is one of the major focus of the current research trend.

With this regard, this work proposes a watermarking scheme based on Arnold transform, HOG features, HVS and ELM. With the low computational complexities of the used

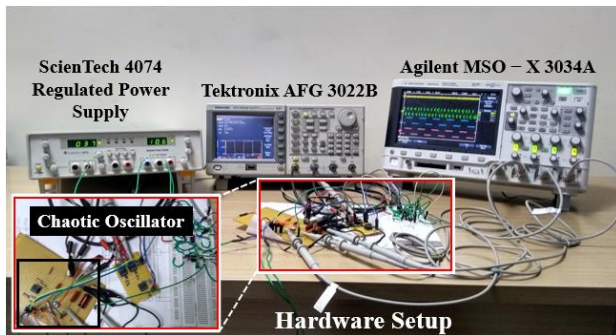


FIGURE 1. Experimental Setup of the chaotic system consisting of oscillator, and OPAMP realization of Chua's Diode for chaotic signal generation.

algorithms and extreme secure key generations, high processing speed, robustness, and security can be guaranteed.

The contributions of the presented work can be summarized as follows:

- The proposed architecture exploits block coding and computationally efficient algorithms like Arnold transform for scrambling which ensures a good robustness.
- The architecture involves human visual system (HVS), Histogram of Oriented Gradients and Extreme Learning Machine (ELM) which not only supports the real – life implementations but also improves the robustness and security.
- Secure key generation is implemented at various stages: (a) Arnold transform; (b) Initial conditions and chaotic oscillator coefficients, and (c) Final watermarking generation using trained ELM. Incorporating these features and as dictated from the metrics has remarkably improved the security.
- A detailed insights on robustness, security, imperceptibility, and computational complexities is developed using metrics like peak signal to noise ratios, structural similarity index, bit error rate, normalized cross – correlation for signed images and extracted watermark.
- Experimental validations for chaotic encryption using memristor based chaotic oscillator is presented so as to access the performance of the proposed technique on real – time chaotic signals.

In this work, a novel digital watermarking architecture is presented. The images are first block coded in order to reduce the processing load. The blocks are first analyzed by calculating the fractal dimensions, which are then scrambled using Arnold Transform for encryption. Consequently, the HOG features are extracted. The transformed signals were passed to the Mamdani FIS system to extract the key indexes using which one of the ELM model is trained. The chaotic signals generated using Memristors are utilized for training the second ELM model. The watermark embedding and extraction have been carried out using the weighted mean of

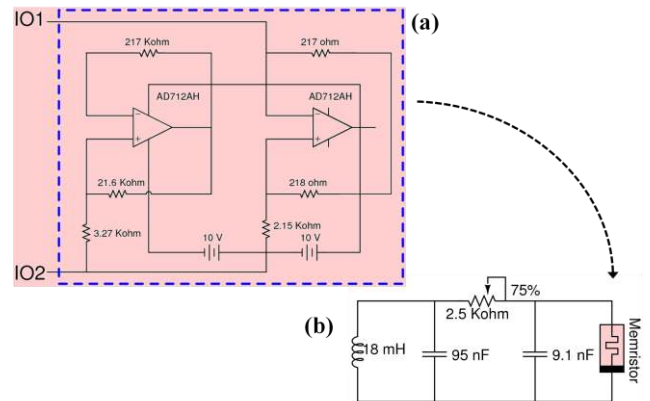


FIGURE 2. (a) Equivalent Circuit for Memristor realized using op-amp (b) Chaotic oscillator realized using memristor.

both the data obtained from models. Finally, the semi – blind watermark extraction procedures and performance analysis were carried out to comment on the robustness and security of the proposed algorithm.

The paper is organized as follows: Section II gives preliminary information about the algorithms used in the architecture. The complete methodology followed in the work is summarized in Section III, and Section IV compiles all the results and discusses the various features and performance of the watermark technique. Finally, the work is concluded in Section V.

II. PRELIMINARIES

This section provides an essential mathematical background of the algorithms used in the proposed architecture and details about the experimental setup.

A. MEMRISTOR & HARDWARE SETUP OF THE CHAOTIC SYSTEM

Memristor, which is popularly known as Chua's diode, is considered to be the missing fourth circuit element. It is a passive circuit element that behaves like a resistive memory. Memristor is a non-linear memory element that found compatibility in many applications like oscillators, information encryption, memory etc. In this work, a Memristor based chaotic oscillator is constructed based on the basic piecewise linear (PWL) ($\varphi - q$) characteristics using operational amplifier and off the shelf elements. Figure 1 shows the experimental setup of the chaotic system, and Figure 2 shows the equivalent circuit of Memristor and oscillator realized both in hardware setup and simulation setup in NI MultiSim [30]. The hardware setup consists of a Chua's Diode realized through general-purpose OPAMPs [31]. The diode was realized on a custom perf board for simplicity, and its response was validated on Agilent MSO – X 3034A through the signals generated by Tektronix AFG 3022B.

The chaotic signals generations in Chua's circuit are governed by the basic set of three nonlinear ordinary differential equations (ODE) of state variables and 3 –

segment piecewise – linear equations as summarized in Equation 1.

$$\begin{aligned} \frac{dx}{dy} &= \alpha[y - x - f(x)] \\ RC_2 \frac{dy}{dx} &= x - y + Rz \\ \frac{dz}{dt} &= -\beta y \end{aligned} \quad (1)$$

The characteristics of the signals can be controlled using the coefficients of ODEs. The Chaotic signals, due to their properties of pseudo-randomness and dynamicity, are widely used in digital media encryption. The chaotic system’s output is similar to white noise with correlation and complexity as defined by Equation 2 [32]:

$$C_{n+1} = \mu \times C_n \times (1 - C_n) \quad (2)$$

Here, $0 < \mu < 4$ and C_n is the n^{th} value generated from Equation 1. Generally, μ is 3.9 for high randomness. By varying the initial conditions using μ and C_n , and value of n , the different chaotic signal can be generated, which is demonstrated in later sections.

In this work, four different sets of oscillator’s coefficients $\{x_1 = 0.01, 0.02, 0.03, 0.04; x_2 = -0.1, x_3 = -0.01, x_4 = 0.01\}$ and initial conditions are used to understand the effect of parameters on the chaos as well on the architecture. The initial condition and the coefficient together act as a secret – user defined keys. Figure 3 (a) – (d) shows the various combinations of chaotic signals generated and studied for the above set of parameters. Figure 3(e) – (g) depicts the chaotic

double scroll attractor pattern obtained for the different conditions. These signals so generated are utilized later in Section III while training the ELM model II. Also, the unique key in the chaotic signal generation is utilized while assessing the security concerns in key sensitivity and space analysis in Section IV.

B. FRACTAL DIMENSIONS AND HIGUCHI ALGORITHM

Fractal dimensions (FD) are the characteristic non – integer numbers which are used to characterize features like texture, degree of surface coarseness etc., of an image. The fractal dimensions of a digital image are relative to the pixel value of the image. Considered as a tool to calculate the image’s complexity, according to the Mandelbrot’s Hausdorff dimensions [33], FD can be defined using Equation 2 as

$$\begin{aligned} A(r) &= \mathcal{A}r^{2-D} \\ f &= \mathcal{A}D/C \end{aligned} \quad (2)$$

Where, $A(r)$ represents the curve surface, \mathcal{A} denotes the true area of the surface, D depicts the FD, C is the present constant, and f is a factor to determine FD of the image. The advantage of using fractal dimensions is that it becomes really infeasible to identify the watermark bits in the cover image. There exist various methods of calculating fractal dimensions like box-counting, spectral analysis, Katz algorithm, Higuchi’s algorithm etc. [34-41]. In this work, Higuchi’s algorithm is used to calculate the FD of the image blocks [35].

Higuchi’s algorithm is a technique which is generally used to calculate the fractal dimension, D of the time series

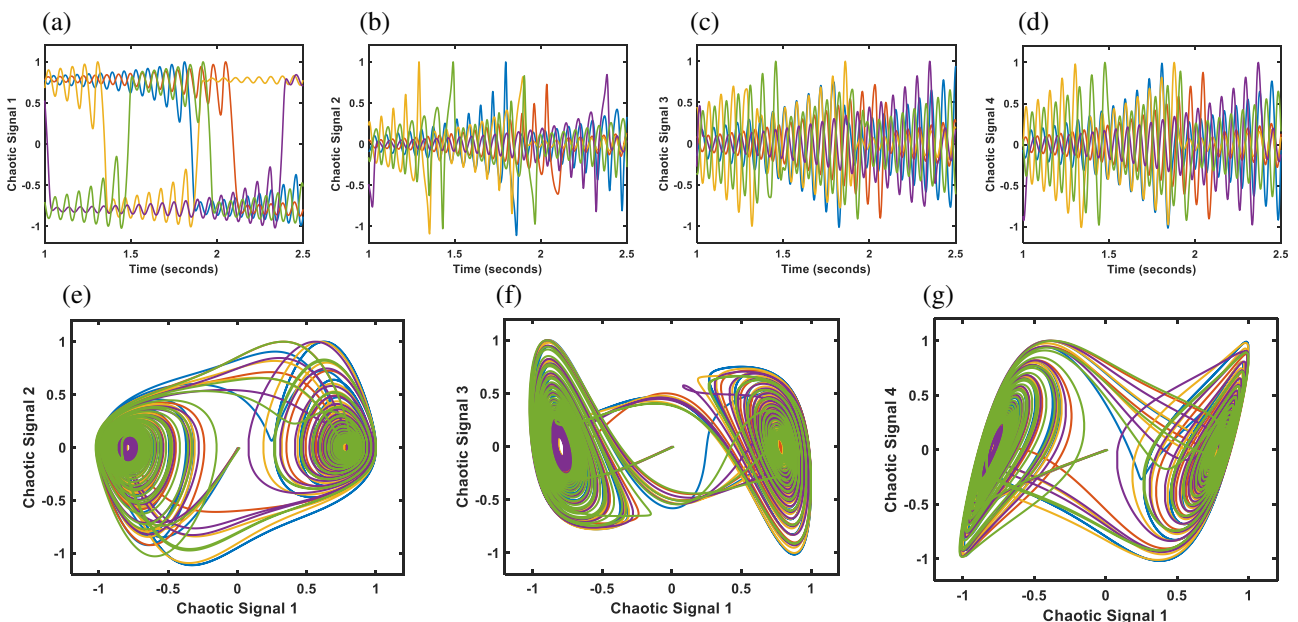


FIGURE 3. (a)-(d) Five different chaotic signals generated for four different initial configurations and user defined keys (e)-(g) Signal 2,3 and 4 as a function of Signal 1 depicting double scroll attractor pattern in the generated chaotic signals.

data. Consider N samples of finite series at regular intervals as described in Equation (3):

$$X(1), X(2), X(3) \dots, X(N) \quad (3)$$

From this series, X_k^m can be obtained as defined in Equation 4 as:

$$X_k^m = \{X(m), X(m+k), \dots, X\left(m + \left\lfloor \frac{N-m}{k} \right\rfloor k\right)\} \quad (4)$$

Where $m \in [1, k]$ which denotes the initial time, k is the interval time and $\lfloor \cdot \rfloor$ denotes the Gauss notation. Thus, k set of new time series is obtained, which defines the FD of the original series. Further, the length of each curve associated with X_k^m is defined by Equation 5 as:

$$L_m(k) = \frac{\left(\sum_{i=1}^{\left\lfloor \frac{N-m}{k} \right\rfloor} (X(m+ik) - X(m+(i-1)k))\right) \left(\frac{N-1}{\left\lfloor \frac{N-m}{k} \right\rfloor}\right)}{k} \quad (5)$$

where $\frac{N-1}{\left\lfloor \frac{N-m}{k} \right\rfloor}$ is the normalization factor for the curve X_k^m .

According to Higuchi, the average length of the curve follows the power law i.e. $\langle L(k) \rangle \propto k^{-D}$, and thus the curve is fractal with dimensions D . In the curve of $\ln(L(k))$ versus $\ln(1/k)$, the slope of the least squares linear best fit is the estimate of the fractal dimension.

C. ARNOLD TRANSFORM

Due to simplicity and periodicity, Arnold Transform is widely used in digital image scrambling [42-45]. Image scrambling is a method of rearranging the entire pixel array of the image, thus resulting in a completely disorganized and encrypted image. The transform follows one to one mapping and has one significant feature of periodicity, according to which the original image after scrambling can be restored back after several cycles. The number of permutations performed while rearranging is of significant importance as it acts as a secret key. This pseudo – random behavior of Arnold transform is characteristic and is of utmost importance as without knowing the number of cycle or sequence used, one cannot decrypt the image [46].

Consider a square image of $N \times N$ representing a 2 – D image, then the transformation of the pixel point (x, y) of the original image to pixel point (x', y') of the encrypted image can be represented by Equation 6 as:

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} 1 & 1 \\ 1 & 2 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} \text{ mod } (N) \quad (6)$$

where mod is the mathematical modular operator. The factor N is the image's size dependent parameter which decides the transformation's periodicity or the period p . The cover image is first scrambled in iterative procedures of n cycles, which acts as a key in the de – scrambling process, and the scrambled image is retrieved using iterative inverse Arnold transform for $p - n$ cycles. The inverse Arnold Transform,

which can be used to restore back the original image, can be represented by Equation 7:

$$\begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 1 & -1 \\ -1 & 2 \end{bmatrix} \begin{bmatrix} x' \\ y' \end{bmatrix} + \begin{bmatrix} N \\ N \end{bmatrix} \text{ mod } (N) \quad (7)$$

Figure 4 depicts the procedure of Arnold transform. It can be understood as an iterative process of stretching and shearing, and translating back to the square matrix, resulting in an invertible matrix that preserves the image features but looks distorted. The inverse Arnold transform follows the same steps but in reverse order.

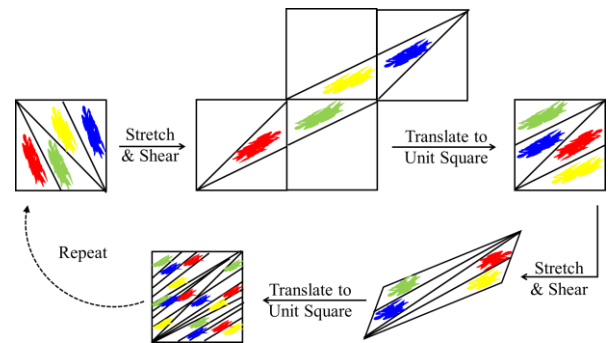


FIGURE 4. Illustration showing scrambling through Arnold Transform.

D. HUMAN VISUAL SYSTEM MODEL & MAMDANI FIS

The Human Visual System (HVS) model is one of the widely used techniques in image processing for analyzing subjective qualities and to improve the imperceptibility of the image. It helps strengthen the technique by making the watermark adaptive to the original image's features, thus ensuring excellent imperceptibility. Literature has reported various approaches for calculating the HVS like Barni *et. al.* [47] has proposed three rules of disturbs and sensitivities to texture and regions of the image. Delaigle *et. al.* [48] proposed FFT based HVS masking procedural, and Martin *et.al.* [49] has used isotropic contrast function with frequency to spatial domain transformation. In the Watson model, three feature: luminance, edge and contrast, are considered while defining the perpetual quality of the image [50]. The luminance sensitivity and edge sensitivity are computed using a threshold value, and contrast sensitivity computed using a variance.

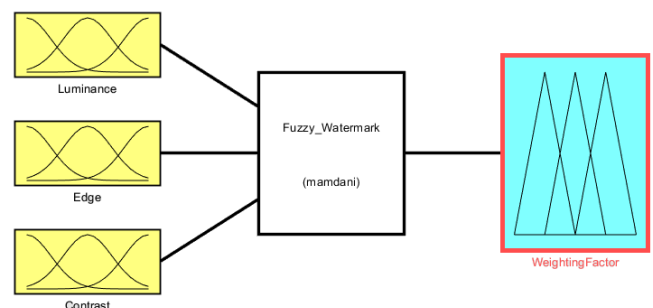


FIGURE 5. Block diagram for Mamdani Based Fuzzy Interface System.

In a Mamdani Fuzzy Interface System, the output, which is a fuzzy set, is controlled using a linguistic control rules. The fuzzy set is derived using the output membership function and the implication method of FIS. The multiple fuzzy sets so obtained are then combined using the FIS aggregation method. Finally, defuzzification is carried out to get the final crisp values. A Mamdani type FIS system setup in Matlab is depicted in Figure 5.

E. HISTOGRAM OF ORIENTED GRADIENTS

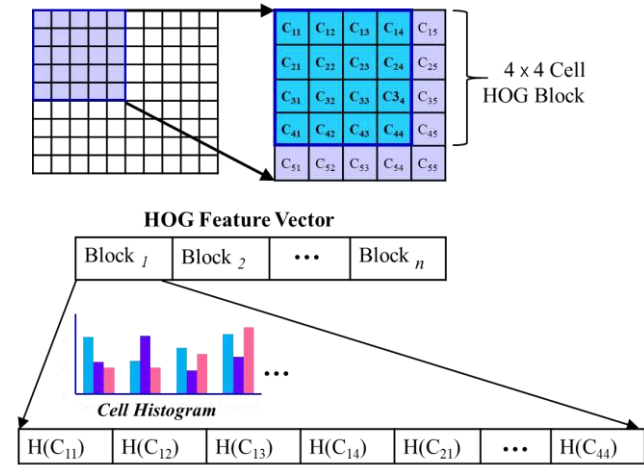


FIGURE 6: Illustration showing Histogram of Oriented Gradients (HOG) feature calculations.

The Histogram of oriented gradients (HOG) is used as a feature descriptor in image recognition domains where the image features are extracted from the edges of the local regions of the target image. This characterizes the orientation and magnitude values of the pixels in the two-dimensional planes. The HOG can be realized using a grid of $(2 \times$

Number of Bins) rose plots spaced uniformly. The rose plot depicts the gradient orientation distribution in a HOG cell, and in each cell, the contribution of each orientation is depicted by the length of each petal.

Consider the image shown in Figure 6 with 4×4 cells constituting a HOG block. The HOG feature extraction considers this as $m \times n$ block and generates a feature vector consisting of HOG blocks arranged in sequential order. Each HOG block is represented using a cell histogram which is $(1 - \text{Number of Bins})$ where the number of bins represents the dimensions of orientation histogram. The larger the number of bins, the better is the orientation details. Figure 5 illustrates the HOG feature extraction procedure.

C. EXTREME LEARNING MACHINES

Extreme Learning Machine (ELM) is a single layer feed – forward neural network (SLFN). The ELM works on allocating the input weights and hidden layers biases using continuous determined probability distribution systems, and finally, the output weights are calculated using the Moore – Penrose method [51][52]. Consider the training samples $(x_i, y_i)_{i=1,2,...,N}$ with $x^i \in \mathbb{R}^n$, $y^i \in \mathbb{R}^m$ and N is the number of hidden neurons. The output of the single hidden layer feed – forward neural network with activation function $g: \mathbb{R} \rightarrow \mathbb{R}$ can be modeled using Equation 8:

$$\sum_{k=0}^N \beta_k g(\langle w_{k1}, x_i \rangle + b_k) = y_i \quad \forall i \in 1, 2 \dots N \quad (8)$$

where $w_k = (w_{k1}, w_{k2}, \dots, w_{kn})$ defines the weighting vector connecting k^{th} hidden neuron to the input node and $\beta_k = (\beta_{k1}, \beta_{k2}, \dots, \beta_{kn})$ is the weighting factor connecting the k^{th} hidden neuron to the output node and b_k is the threshold bias of k^{th} hidden neuron. The factors w_k and β_k are randomly selected in accordance with the continuous probability distribution function. Thus, Equation 8 can be interpreted as Equation 9:

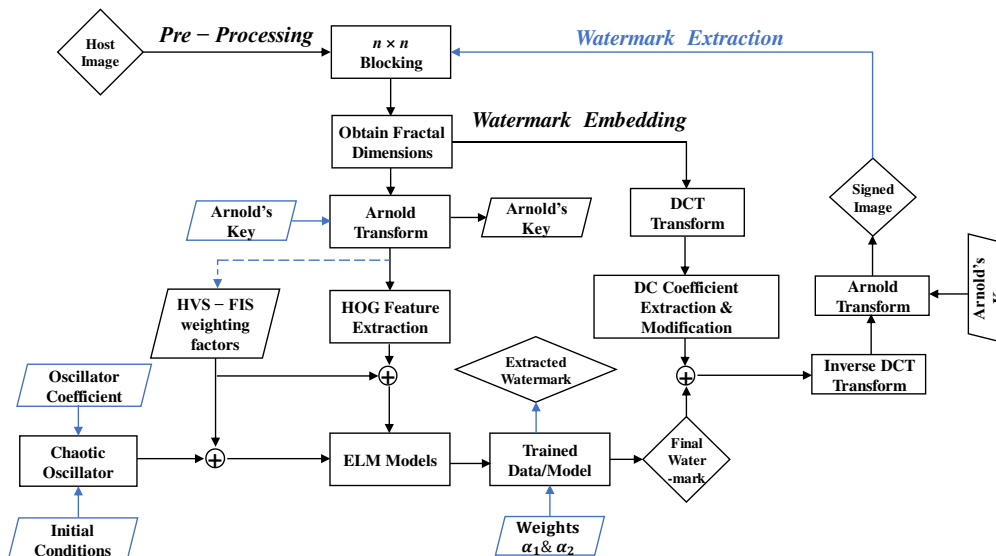


FIGURE 7: Flowchart of the proposed watermarking technique.

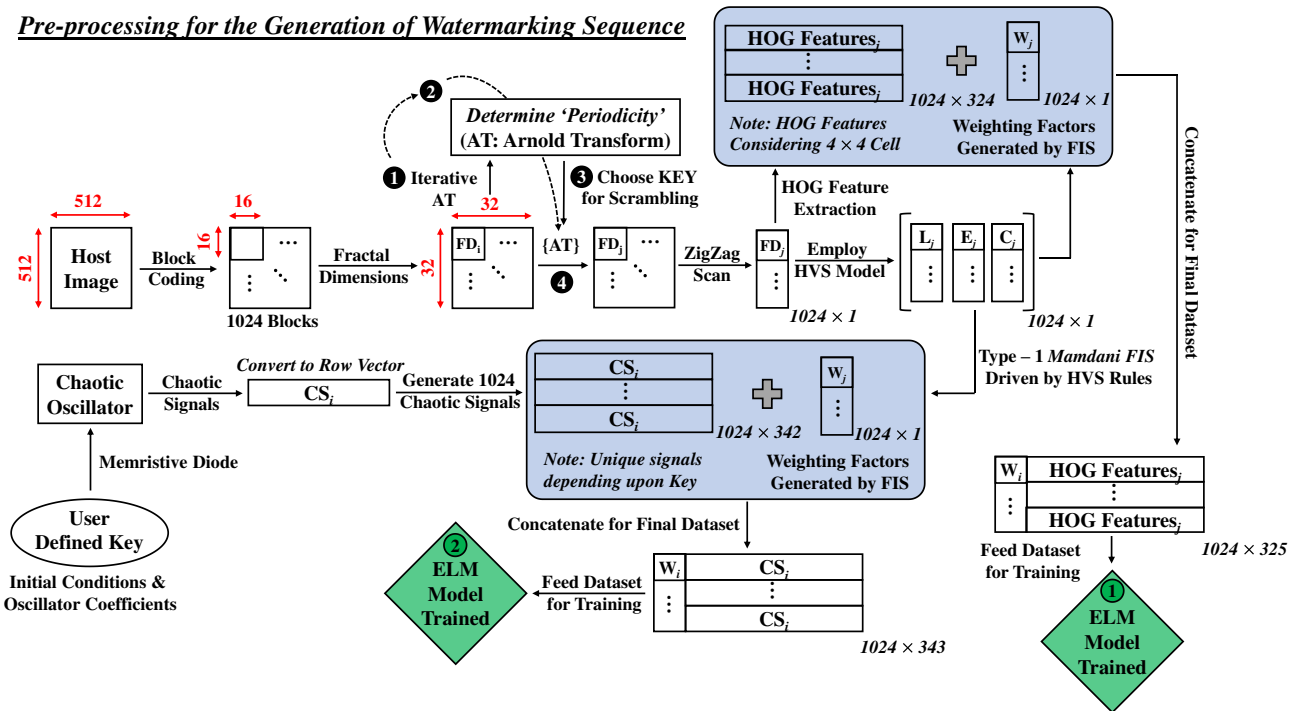


FIGURE 8: Flowchart explaining pre-processing steps for the watermark sequencing.

$$H\beta = Y \quad (9)$$

The solutions of Equation 8 can be described using Equation 10:

$$\beta' = H^*Y \quad (10)$$

where H^* is the Moore – Penrose inverse of the hidden – layer output matrix H .

III. METHODOLOGY

Figure 7 presents the flowchart of the proposed watermarking methodology and is illustrated in detail through Figure 8, 11 and 12. The simulations are carried using MathWorks MATLAB [53]. Four different grayscale host images - Lena, Airfield, Peppers and Mandrill were used for watermark embedding. The complete drill followed in this work can be categorized into three groups: (1) Pre – processing for the generation of watermarking sequence, which is covered in subsection A – F; (2) Watermark Embedding to obtain the final signed image, which is covered in subsection G; and (3) Semi – Blind Watermark extraction to retrieve back the watermarking coefficients from the signed image which is covered in subsection H.

A. CALCULATIONS OF FRACTAL DIMENSIONS

At first, the 512×512 sized host images is subjected to block coding, which generates 1024 blocks of size 16×16 . Each of this block is then featured into their respective unique fractal

dimensions ($[FD_i]$) using Higuchi’s algorithm and stored in a 32×32 matrix.

To ensure better security, two-level encryption has been introduced in the proposed watermarking scheme, first using Arnold transform and second using the chaotic sequence used to train the ELM Model 2.

B. SCRAMBLING USING ARNOLD TRANSFORM

The 32×32 blocks are iteratively passed to the scrambling system, and the corresponding periodicity is determined. The image’s periodicity is a function of image size and dimensions. For the present work, a periodicity of 24 is obtained. The fractal matrix can then be scrambled for any number or iterations, which then act as the unique key for image encryption. The transformed matrix ($[FD_j]$) is converted into a vector of size 1024×1 using zig – zag scan ($(32 \times 32) \rightarrow (1024 \times 1)$), which forms the base for all the further processing.

C. HUMAN VISUAL SYSTEM AND FUZZY INTERFACE

The three features – luminosity, edge and contrast terms are obtained and stored in $[L_j]$, $[E_j]$ and $[C_j]$ respectively. These blocks are then fed to the Mamdani FIS system driven by a set of 10 interference rule as proposed by Lou *et. al.* [50], and the 1024×1 matrix representing single weighted output is obtained. Figure 8 shows the interference process illustrating the role of membership functions and weighting factors. Figure 9 shows the weighting factor generated as a function of the three indices: Luminous, edge and contrast. The weighting factors as generated by the FIS system is of utmost importance as it is later used as labels or weight for

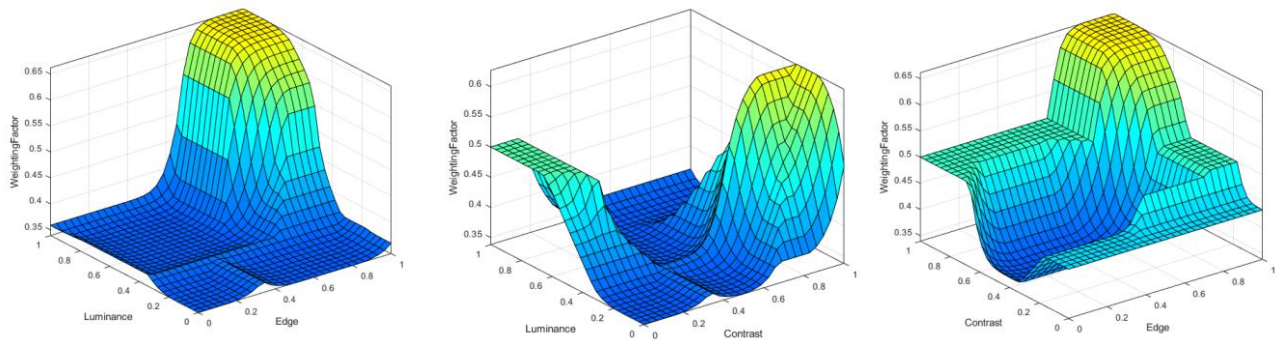


FIGURE 10: Evolution of weighting factor as a function of luminous, edge and contrast terms.

individual elements and is used in the preparation of the training data for the neural network.

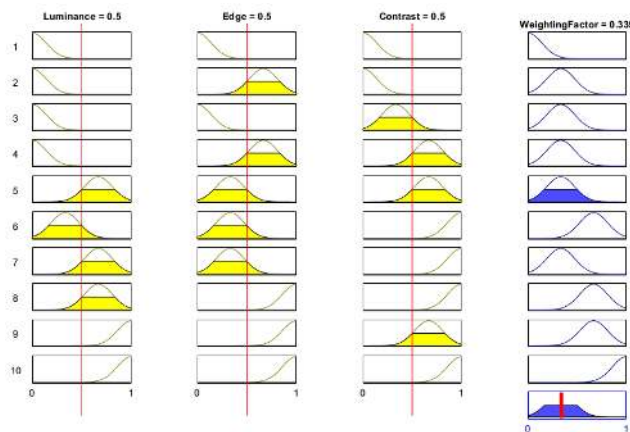


FIGURE 9: Illustration explaining the role of membership functions and effect on weighting factors in HVS-FIS.

D. HISTOGRAM OF ORIENTED GRADIENTS

The image blocks corresponding to the fractal array after zig-zag scan is parsed for extracting HOG features. The

features are extracted using 4×4 cells and using 9 bins. Since the input is 1024×1 , $1/3rd$ of the total size, i.e. 324, results in the output of size 1024×324 . This array is concatenated with the weighting factor earlier generated using the FIS Mamdani system and is fed into the ELM Model 1 for training.

E. CHAOTIC SIGNALS GENERATION AND DATA PREPARATION

The chaotic signals generated through Memristor based non-linear oscillators are further used for improving the robustness of the proposed scheme. The signals are stored in a row vector, and a total of 1024 unique signals are generated. For each signal, 342 sample points are taken for building up the training dataset. The so obtained 1024×342 matrix is modified by concatenating the weighting factor matrix generated by FIS, and the final dataset is fed to the ELM Model 2 for subsequent training and testing.

F. EXTREME LEARNING MACHINE MODEL

In this work, two ELM models are used. One machine is trained with the matrix obtained from the HOG feature extraction procedure, and the other ELM model is trained with

Watermark Embedding Methodology

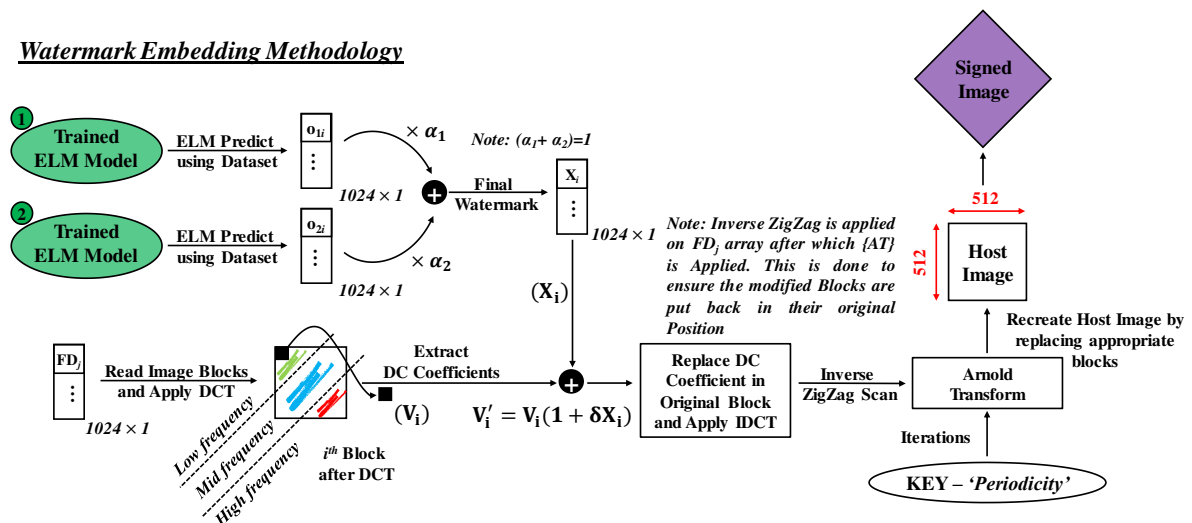


FIGURE 11: Flowchart explaining water embedding methodology.

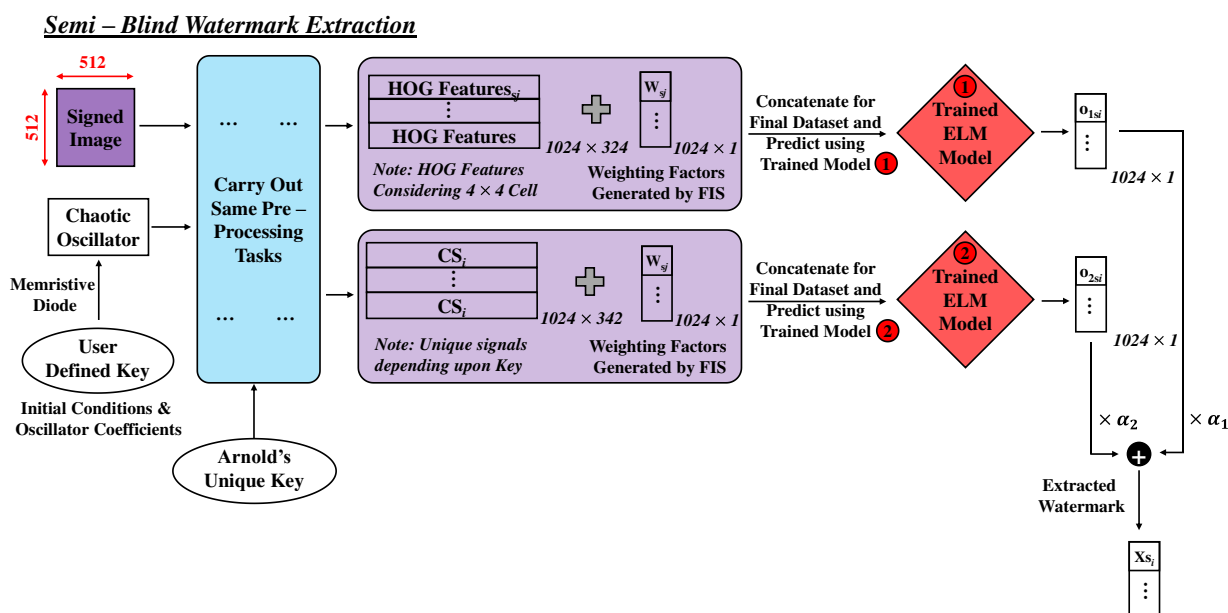


FIGURE 12: Flowchart explaining the procedure for semi-blind watermarks extraction.

the unique sets of chaotic signals. The ELM is a single-layer network with 10 hidden neurons, and the sigmoid activation function is used. The output of each ELM is a 1024×1 vector. The two ELM dataset obtained as output are combined using the weighted sum method, and the final matrix sequence is obtained. The output so obtained is the required watermarked sequence (X_i).

G. WATERMARK EMBEDDING

The ELM Model 1 and 2 so trained using HOG features and chaotic signals, respectively, were used in weights of 50% to generate the final watermarking coefficients denoted by (X_i). Consequently, for watermark embedding, each block of $[FD_j]$ is read in order as dictated using zig – zag scan and transformed using discrete cosine transform (DCT). The 2D – DCT converts the image block from Spatial to Frequency domain that can be categorized into low, mid and high frequency bands. The entire block in the frequency domain consists of AC coefficients, except at the (0,0) index, which corresponds to the DC coefficient. The said DC coefficient for all the blocks are extracted for embedding the watermarking coefficients. The watermark embedding method used here is the one proposed by Cox *et. al.* [55]. The formula used is described in equation 11 as:

$$V'_i = V_i(1 + \delta X_i) \quad (11)$$

where V_i represents the host image coefficient and δ is the scaling factor. The extracted DC coefficient is used as V_i in the above Equation. The modified value of the DC coefficient so obtained is used to replace the previous DC coefficients, and inverse discrete cosine transform (IDCT) is performed to retransform the signal back to the spatial domain. Since

Arnold Transform was used in the preliminary stages for scrambling, inverse zig – zag scan is applied and, the original block locations are obtained after subjecting it to the Arnold Transform for the remaining iterations. This restores the original image.

H. SEMI – BLIND WATERMARK EXTRACTION

Watermark extraction involves the same set as pre – processing tasks and prediction using ELM. The signed image and the chaotic signal generated using Chua’s circuit are subjected to the same pre – processing tasks described in subsection A – F. The HOG features-based dataset and the chaotic signal dependent dataset is generated, and the prepared data is tested using the trained ELM models. The 1024×1 sized output of the ELM models are added using a sum of weighted mean, and finally, the watermark is extracted.

IV. RESULTS AND DISCUSSION

The proposed approach discusses a double encryption technique for image watermarking. The architecture uses several distinguishing features enhancing its robustness, imperceptibility and security. Not only this, but the processing time is also found to be competitive with state – of – the – art watermarking techniques.

Arnold transform used for image scrambling eliminates the spatial correlation of image pixel, making the watermarking process distinguishably robust. The unique key so generated forces a layer of encryption, thus enhances the security. Furthermore, the presented approach is based on using index features of the image – luminance, edge and contrast, which ensures a high level of security and excellent resistance to watermarking attacks. Considering the geometric attacks, the

proposed scheme has HOG features as one of the base for training models as histogram distribution of an image are generally invariant under attacks. Considering the need to have efficient processing of color images in copyrights, the proposed algorithm can also be used for colored images. It is due to this feature; the proposed algorithm is reliable and applicable to a vast variety of digital media. The second level of encryption is based on the chaotic signals, which usually is based on using the pseudo – random and dynamic property of signals. A chaotic oscillator is developed using Memristor, which acts as a chaotic signal generator. Since training is also based on these signals, another key is required in order to perform proper decryption, which further makes the system secure. The results so presented are experimentally validated using hardware setup with the simulation deck, which proves the proposed technique's possible implementations in real-time applications.

Imperceptibility or invisibility can be related to the concealment of digital watermarks. If a watermark can't be visually detected by the human visual system, it is said to be imperceptible. Watermark imperceptibility can be evaluated using metrics like Peak Signal to Noise Ratio (PSNR), Mean Square Error (MSE) and Structural Similarity Index (SSIM). The security depicts how much encrypted the process is. If the watermark is somehow extracted, it is impossible to embed it back to its original form without the encryption key, thus the watermark is said to be secure. The watermark's robustness is its ability to resist change in the embedded watermark due to changes in the watermark carrier data. Watermark robustness is generally measured with metrics like Normalized Cross-Correlation (NC).

The performance analysis in terms of robustness, security and imperceptibility of the proposed architecture is tested on digital attack benchmarks. The signed images are applied to 21 StirMark benchmarks [56], and then the watermark is extracted from the attacked images. The performance of the technique was assessed using various metrics discussed below.

A. STRUCTURAL SIMILARITY INDEX

The Structural Similarity Index (SSIM) is the quality assessment index for measuring the similarity between the host image and the watermarked image. Numerically, SSIM lies in the range of 0 to 1 with 1 perfect structural similarity between two images and 0 being the worst case depicting that the two images doesn't share the similarity. Equation 12 realizes the SSIM metric as follows:

$$SSIM(I, I') = [l(I, I')]^\alpha \cdot [c(I, I')]^\beta [s(I, I')]^\gamma \quad (12)$$

Where $I(i, j)$ denotes the host image, $I'(i, j)$ denotes the signed image, α, β and γ are the exponents for luminance, contrasts and structural terms respectively and $l(I, I'), c(I, I')$ and $s(I, I')$ can be described by Equation 13:

$$\begin{aligned} l(I, I') &= \frac{2\mu_I\mu_{I'}+C_1}{\mu_I^2+\mu_{I'}^2+C_1} \\ c(I, I') &= \frac{2\sigma_I\sigma_{I'}+C_2}{\sigma_I^2+\sigma_{I'}^2+C_2} \\ s(I, I') &= \frac{\sigma_{II'}+C_3}{\sigma_I\sigma_{I'}+C_3} \end{aligned} \quad (13)$$

where μ_I and $\mu_{I'}$ are the local means, σ_I and $\sigma_{I'}$ are the local standard deviation and $\sigma_{II'}$ are the cross – covariance for images I and I' . When $\alpha = \beta = \gamma = 1$ and $c_3 = c_2/2$, the SSIM metric simplifies to and is expressed in Equation 14.

$$SSIM(I, I') = \frac{(2\mu_I\mu_{I'}+C_1)(2\sigma_{II'}+C_2)}{(\mu_I^2+\mu_{I'}^2+C_1)(\sigma_I^2+\sigma_{I'}^2+C_2)} \quad (14)$$

For a 2D image, the SSIM is generally calculated using a sliding Gaussian window or block and is made to traverse the image pixel by pixel generating the SSIM quality map. Figure 12 depicts the SSIM as a function of the scaling factor. As observed from the figure, the SSIM factor for all the four images under consideration lies well near 1, indicating that the watermarked images are similar and hence offers an excellent imperceptibility and invisibility to the watermarked image. Table 1 shows the objective metrics for different host image with watermark with respect to the scaling factor. Near to 1 value of SSIM over the entire range of scaling factor point towards the excellent imperceptibility achieved.

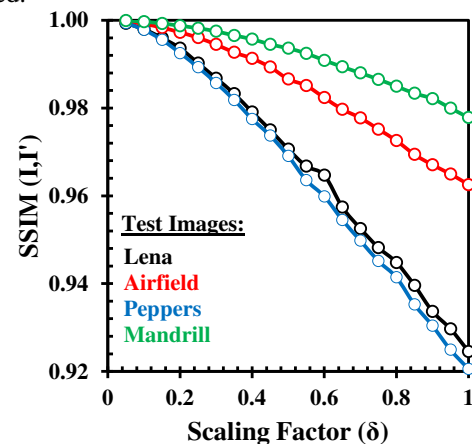


FIGURE 13: SSIM metric for different images under consideration as a function of scaling factor.

B. NORMALIZED CROSS CORRELATION

Normalized Cross Correlation (NC) is used to judge the image similarity between two images. Since the NC is found to be less sensitive to linear change in the amplitude of illumination, it is one of the most commonly used metric in image processing tasks. Generally confined in the range between -1 and 1, the NC provides an edge over cross correlation by easing the threshold value selection and in other analysis. In this work, the cross – correlation of the watermark and signed image both before and after attacks are studied. The

former is done to assess the robustness of the semi – blind watermarking technique, while the latter is done to assess the overall performance of the proposed scheme on the image containing the watermarking coefficients. NC metrics can be represented using Equation 15:

$$NC(W, W') = \frac{\sum_{i=1}^m \sum_{j=1}^n [W(i,j) * W'(i,j)]}{\sum_{i=1}^m \sum_{j=1}^n [W(i,j)]^2}$$

$$NC(I, I') = \frac{\sum_{i=1}^m \sum_{j=1}^n [I(i,j) * I'(i,j)]}{\sum_{i=1}^m \sum_{j=1}^n [I(i,j)]^2} \quad (15)$$

where, p and q are the rows and columns of the watermarking sequence. $W(i, j)$ and $W'(i, j)$ are the watermarking coefficients of the original and watermarked sequence, respectively and $I(i, j)$ and $I'(i, j)$ denotes the host and the signed image respectively. The higher the value of NC, the better is the system's robustness to the vulnerable digital attacks. More specifically, a higher value of $NC(W, W')$ dictates that the watermark so embedded into the original sequence and that extracted using semi – blind extraction routine shares a high degree of correlation with the original version indicating robustness of the extraction procedure. After subjecting the signed image to various attacks, the attacked image will lose its correlation with the original image, which is evident from the PSNR, $NC(I, I')$, SSIM, and BER values indicated in Table 2. This is done deliberately in an attempt to destroy the embedded watermark. However, when the watermarking coefficients are extracted from the attacked image, the cross – correlation of the watermark i.e. $NC(W, W')$, still remains close to unity, indicating the robustness of the proposed scheme.

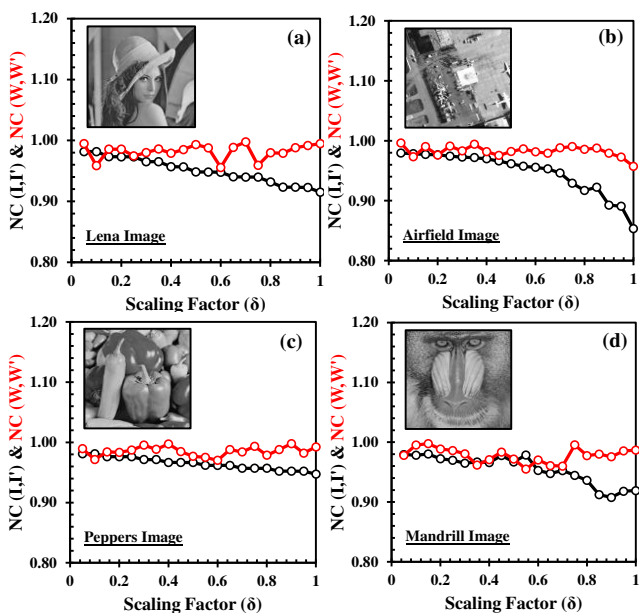


FIGURE 14: NCC metric for signed image (black) and watermarked image (red) under consideration as a function of scaling factor.

Figure 14 shows the NC of the signed and original image. As clearly visible, the high values of NC's for all four images prove the robustness of the proposed watermarking technique. In the presented scheme, the NC's value is above 90% in almost all cases depicts excellent robustness, and hence the resilience of the proposed algorithm. It is because, in the proposed scheme, the watermark embedding is carried out by modifying the DC coefficients of the adjacent blocks. This results in an invariably small change in the pixel domain hence leading to a better quality. Moreover, it is worthy to note that if AC coefficient from mid – frequency sub – band are chosen instead of the DC coefficient, the pixel domain changes can be further minimized, and the image quality can be enhanced. However, most image processing attacks are directed towards the mid – and high – frequency coefficients, which significantly deteriorates the watermarking coefficients, thereby defeating the main objective of robust image watermarking scheme.

C. BIT ERROR RATE

The bit error rate (BER) represents the number of error bits received per unit time. Mathematically, it can be obtained by dividing the number of bits that have been altered while processing by the total of transferred bits. Mathematically, BER can be described using equation 16 as:

$$BER(I, I') = \frac{1}{mn} [\sum_{i=1}^m \sum_{j=1}^n I(i, j) \oplus I'(i, j)] \quad (16)$$

Where I and I' represent the original and the signed image, respectively. Ideally, BER is zero, which shows that the two images share a good proportion of resemblance. The various BER metrics of the images under consideration are summarized in Figure 14. The BER lies well below 0.50 for all scaling factors, which proves highly robust for the image processing operations and even close to 0 for the small scaling factor. Further, it is evident from the figure that as the scaling factor's value decreases, the system's robustness is also increased as far as the BER is concerned. However, the strength of watermarking coefficients gets significantly affected and becomes vulnerable to image processing attacks.

D. PEAK SIGNAL TO NOISE RATIO

Peak Signal to Noise is the ratio of the signal's maximum possible power to the power of corrupting noise signal. PSNR is generally expressed in terms of the logarithm of mean square error.

$$MSE(I, I') = \frac{1}{mn} [\sum_{i=1}^m \sum_{j=1}^n [I(i, j) - I'(i, j)]^2] \quad (17)$$

$$PSNR(I, I') = 10 \log_{10} \left(\frac{2^v - 1}{MSE} \right) \quad (18)$$

where v is the minimum number of bits depicting the maximum intensity in a given image, $I(i, j)$ and $I'(i, j)$ denotes the host and the watermarked image, respectively, and m and n represent the number of rows and columns in the original image. The evolution of PSNR as a function of the

scaling factor is depicted in Figure 14. An intersection between the PSNR and BER curves is used to determine the optimum scaling factor ($\delta_{Optimum}$) which is later used to assess the proposed watermark scheme through StirMark attacks. Further, if the intersection point of the PSNR and BER is traced, a shift in optimum scaling factor is obtained, enabling us to adjust the other parameters to enhance the overall system performance. The shift and the values of various metric can be related to the random weight allocation in the ELM [10]. It is worth mentioning that the ELM training and testing time in all the cases are extremely small and lies in the range of mili – seconds (70 – 90 msec for 20 iterations) which prompts the extremely high computational speed and testing time.

For watermark embedding procedure, the $NC(I,I')$ lie close to unity, indicating that the signed image still has a high degree of correlation with the host image. Under semi blind extraction, $NC(W,W')$ as observed, lies close to unity, indicating that the proposed scheme is able to extract the watermark, and that the extracted watermarking coefficients have a high degree of correlation with the coefficients that were embedded in the initial phase. Further, after deliberately subjecting the signed images to heavy image processing attacks, evident from the seriously degraded PSNR, BER, SSIM, and $NC(I,I')$ values, the extracted watermark still has a high degree of correlation with the original watermarking coefficients.

Table 1: Computed SSIM, PSNR, BER and NC metric as a function of scaling factor (δ)

IMAGE: LENA						IMAGE: AIRFIELD					
Scaling	SSIM(I,I')	PSNR	BER(I,I')	NC(I,I')	NC(W,W')	Scaling	SSIM(I,I')	PSNR	BER(I,I')	NC(I,I')	NC(W,W')
0.05	0.999328	65.28387	0.036629	0.981698	0.994682	0.05	0.999764	63.5187	0.050499	0.979444	0.99622
0.1	0.997955	59.14479	0.096039	0.98165	0.958774	0.1	0.999198	57.65621	0.124928	0.978305	0.973102
0.15	0.995981	56.04389	0.138351	0.973252	0.985741	0.15	0.99834	54.19128	0.182003	0.977174	0.990176
0.2	0.993631	53.66393	0.170708	0.973132	0.985701	0.2	0.99727	51.97557	0.220226	0.976489	0.976068
0.25	0.990224	51.53457	0.196701	0.973108	0.974542	0.25	0.996034	49.91912	0.255089	0.974388	0.990943
0.3	0.986785	49.93501	0.214005	0.965197	0.979981	0.3	0.994492	48.28276	0.283337	0.972698	0.983087
0.35	0.983263	48.7579	0.230629	0.965076	0.985906	0.35	0.992689	46.99864	0.307251	0.971836	0.994036
0.4	0.979071	47.54181	0.248665	0.956999	0.978981	0.4	0.991309	45.98438	0.323921	0.969789	0.981759
0.45	0.975014	46.50796	0.263985	0.956599	0.985055	0.45	0.98933	45.00636	0.340172	0.966141	0.975452
0.5	0.970629	45.58403	0.279602	0.948331	0.993136	0.5	0.986604	43.84746	0.356365	0.961671	0.981975
0.55	0.966744	44.84779	0.290146	0.948204	0.987827	0.55	0.98512	43.31841	0.362415	0.957495	0.986487
0.6	0.964679	44.66727	0.294899	0.947791	0.955592	0.6	0.982369	42.35925	0.371441	0.955648	0.981361
0.65	0.957403	43.39412	0.311218	0.940279	0.988642	0.65	0.979719	41.70847	0.382233	0.95299	0.979242
0.7	0.952541	42.66457	0.319344	0.939889	0.997524	0.7	0.977757	41.23108	0.386551	0.946277	0.988136
0.75	0.948202	42.05109	0.325455	0.939808	0.959141	0.75	0.975174	40.57445	0.394634	0.929115	0.990356
0.8	0.944813	41.65563	0.33168	0.931776	0.979719	0.8	0.972573	40.03375	0.398029	0.917049	0.985677
0.85	0.939597	40.97029	0.338982	0.923226	0.978955	0.85	0.969424	39.48496	0.40443	0.922522	0.987675
0.9	0.933649	40.43767	0.34713	0.923221	0.988045	0.9	0.967054	39.06541	0.408562	0.892613	0.97911
0.95	0.929661	40.05302	0.351585	0.922814	0.991674	0.95	0.964968	38.71499	0.409695	0.890757	0.972787
1	0.924527	39.55364	0.357666	0.915114	0.994659	1	0.962557	38.37611	0.4119	0.853191	0.957295
IMAGE: PEPPER						IMAGE: MANDRILL					
Scaling	SSIM(I,I')	PSNR	BER(I,I')	NC(I,I')	NC(W,W')	Scaling	SSIM(I,I')	PSNR	BER(I,I')	NC(I,I')	NC(W,W')
0.05	0.999362	64.48765	0.04261	0.981052	0.989643	0.05	0.999943	67.60804	0.022774	0.979446	0.977927
0.1	0.997795	58.74412	0.10112	0.981052	0.971526	0.1	0.999664	59.47459	0.127434	0.978232	0.995257
0.15	0.995525	55.40029	0.144318	0.976197	0.984167	0.15	0.999274	56.26978	0.210762	0.980287	0.997608
0.2	0.992522	52.83352	0.177231	0.976193	0.983405	0.2	0.998742	53.98757	0.262131	0.972306	0.988732
0.25	0.989278	50.9982	0.204247	0.976152	0.98709	0.25	0.998182	52.34074	0.298889	0.969862	0.986089
0.3	0.985714	49.54127	0.225899	0.97146	0.995407	0.3	0.99748	50.8346	0.324287	0.964872	0.980703
0.35	0.981832	48.30797	0.242081	0.971413	0.988358	0.35	0.996535	49.3733	0.3507	0.966997	0.961839
0.4	0.977482	47.07869	0.259277	0.966678	0.99731	0.4	0.995693	48.33636	0.367294	0.965885	0.970867
0.45	0.973706	46.1935	0.271194	0.966572	0.984689	0.45	0.994499	47.1766	0.380981	0.977665	0.983578
0.5	0.969081	45.23497	0.280869	0.96649	0.97686	0.5	0.993616	46.36271	0.390648	0.967068	0.971919
0.55	0.96355	44.32647	0.298157	0.961805	0.975092	0.55	0.992441	45.64674	0.400566	0.978669	0.955079
0.6	0.959869	43.71914	0.303299	0.961749	0.9701	0.6	0.990872	44.75621	0.411041	0.952646	0.970331
0.65	0.954511	43.03996	0.316307	0.961713	0.988062	0.65	0.989391	44.12213	0.416847	0.947627	0.960897
0.7	0.949803	42.33428	0.323837	0.956986	0.984002	0.7	0.987996	43.4267	0.422462	0.952625	0.96003
0.75	0.945146	41.75548	0.330841	0.956954	0.993501	0.75	0.986538	42.90274	0.430283	0.944572	0.995528
0.8	0.941414	41.35166	0.338371	0.956949	0.978633	0.8	0.984965	42.30331	0.435211	0.936181	0.977584
0.85	0.935252	40.75559	0.346115	0.952202	0.987912	0.85	0.983358	41.81809	0.437599	0.912235	0.980045
0.9	0.930385	40.33894	0.354378	0.952124	0.997778	0.9	0.982141	41.50226	0.441505	0.907735	0.975702
0.95	0.924925	39.83766	0.359962	0.952122	0.982115	0.95	0.97999	40.93978	0.447456	0.918014	0.985511
1	0.920535	39.43099	0.368782	0.947338	0.992456	1	0.977836	40.41583	0.450058	0.91908	0.986692

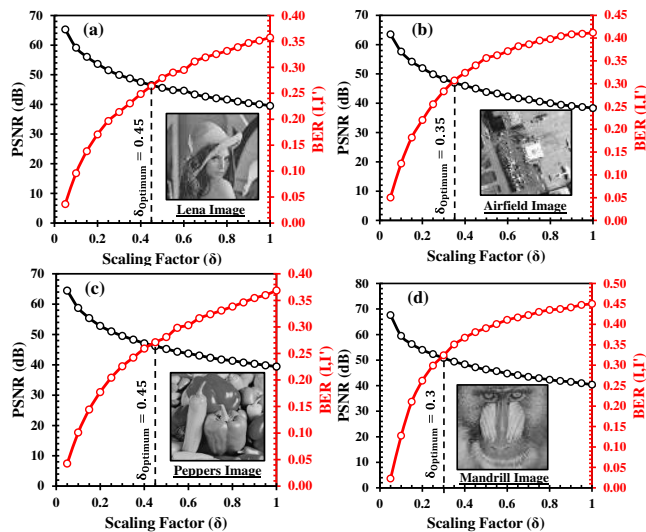


FIGURE 15: PSNR and BER metrics for different images under consideration and optimization of the scaling factor.

E. PERFORMANCE ANALYSIS UNDER ATTACKS

Table 3 shows the computational performance of the images on StirMark benchmark when signed images are subjected to various image processing tasks. Two main cases are considered: (1.) Single attack and (2.) Hybrid attacks where the image is subjected to more than 1 attack at a time. The benchmark so chosen de – synchronizes the algorithm using random bilinear geometrical distortion and is one of the simplest tools for testing the robustness of the digital watermark architecture. Seriously degraded PSNR, SSIM, BER, and NC values for the image justify the StirMark attacks carried out on the image in a deliberate attempt to destroy the watermark and hence are an effective way to evaluate the performance of the algorithm [10]. Figure 16 depicts the hybrid attack. To comment on the robustness in severe conditions of digital attack, the signed image is subjected to 5 combined attack and the attacked image is visualized in Figure 16. The seriously degraded values of PSNR, SSIM, BER, and NC(I,I') demonstrate the intensity of image processing attacks so studied to evaluate the robustness of the proposed scheme. From the NC(W,W') metrics, only 1.5% degradation is observed in case of image resizing which depicts excellence resilience of the technique to resizing attacks. In case of cropping and replacing which seems to be the worst case amongst all the single attack, the maximum degradation of 8.42% in NC(W,W') is recorded with is accompanied with 0.087, 0.250 and 27.16 dB change in BER, PSNR and SSIM index. While in case of filtering and noise, the algorithm is still able to extract the recognizable watermarking coefficients from the attacked images. Same can also be concluded from the subjective quality of the image as depicted.

To test the performance under extreme conditions, the proposed technique was tested under 5 simultaneous attacks. To the best of authors knowledge, a maximum of 2 – 3

combined attacks have been studied in [2] and there has been no work reported which deals with such extreme cases of 5 attacks covering blurring, filtering and noise operations simultaneously. The seriously degraded values of PSNR, SSIM, BER, NC(I,I') justify the worst case image processing attacks that were deliberately applied to destroy the watermarking coefficients in the signed image. However, a high value of NC(W,W') justifies the robustness of the proposed scheme against vulnerable attacks. To assess other traits, SSIM and PSNR have also been studied. SSIM which is originally based on image distortion model utilizes features like loss of correlation, luminance distortion and contrast distortion while the PSNR metrics are based on the mean square error are more consistent in studying the effect of gaussian noises [57]. However, since a variety of cases other than gaussian noise have also been considered, so it becomes crucial to understand the evolution of both the metrics under various conditions and obtain a tradeoff. In our case, the random weight allocation may be the reason to such sensitivity in SSIM and PSNR values. Overall, based on SSIM and PSNR metrics of image under attack, the visual quality of the image is distorted because of which it loses its correlation and structural similarities and the objective quality is slightly degraded. While a good value of NC(W,W) even after attacks reflects the extraction of original watermark is achievable and that the proposed scheme is robust and resilient to attacks.

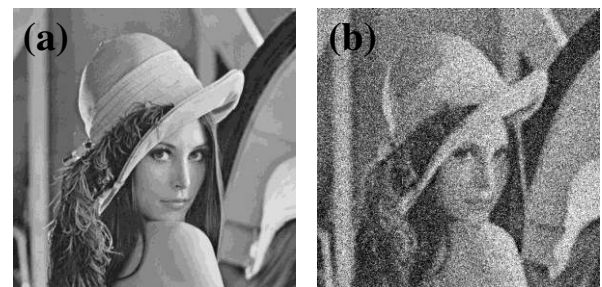


FIGURE 16: Visualization of (a) Original host (Lena) Image (b) Attacked Lena image under hybrid attack (Gaussian Blur 2std dev + Median Filter (Aperture 5) + Salt and Pepper (5 % Noise) + Gaussian Noise (Var=0.05) + Speckle Noise (Var=0.05)).

Table 2: Evaluation of Stirmark Attacks on the Signed Images for different Host Images.

(a) IMAGE:LENA					
Attacks	SSIM (I,I')	PSNR	BER (I,I')	NC (I,I')	NC (W,W')
No Attack	46.50796	0.975014	0.263985	0.956599	0.985055
Gaussian Blur 0.5 std dev	44.7357	0.929786	0.374512	0.766944	0.975721
Gaussian Blur 1 std dev	39.07138	0.69975	0.439423	0.760608	0.981301
Gaussian Blur 1.5 std dev	36.44224	0.576745	0.447742	0.753414	0.981155
Gaussian Blur 2 std dev	34.76434	0.492118	0.451866	0.753277	0.970236
Resizing (512->256->512)	39.44511	0.703132	0.441662	0.780613	0.980725

Crop and Replace by 0 (1st Quarter)	17.99436	0.723865	0.209938	0.667611	0.916334
Crop and Replace by 0 (2nd Quarter)	16.8827	0.724864	0.203987	0.68718	0.959997
Crop and Replace by 0 (3rd Quarter)	19.57468	0.72302	0.176643	0.512134	0.902041
Crop and Replace by 0 (4th Quarter)	16.90798	0.724347	0.197239	0.185562	0.915208
Crop and Replace by 255 (1st Quarter)	17.60123	0.723177	0.455109	0.364769	0.965691
Crop and Replace by 255 (2nd Quarter)	17.98768	0.726073	0.45166	0.773957	0.990717
Crop and Replace by 255 (3rd Quarter)	15.8804	0.722346	0.430199	0.766801	0.966513
Crop and Replace by 255 (4th Quarter)	18.12537	0.72442	0.449089	0.165056	0.986961
Crop Right Half and Replace by 0	13.89417	0.481912	0.137611	0.011014	0.934375
Crop Right Half and Replace by 255	15.05882	0.482552	0.640224	0.336588	0.942151
Crop Left Half and Replace by 0	15.71487	0.477499	0.124802	0.0303	0.932215
Crop Left Half and Replace by 255	13.65684	0.47763	0.620415	0.02544	0.909443
Crop Top Half and Replace by 0	14.40665	0.481356	0.148666	0.303795	0.937184
Crop Top Half and Replace by 255	14.78896	0.481227	0.650696	0.356329	0.956216
Crop Bottom Half and Replace by 0	15.04208	0.48069	0.114197	0.01146	0.935854
Crop Bottom Half and Replace by 255	13.85742	0.479558	0.614933	0.335225	0.933472
Median Filter (Aperture 3)	40.54053	0.687026	0.408997	0.323202	0.901306
Median Filter (Aperture 5)	37.09303	0.55275	0.429844	0.342411	0.986891
Salt and Pepper (2% Noise)	28.48008	0.498009	0.270176	0.877821	0.990378
Salt and Pepper (5% Noise)	24.46047	0.253429	0.277779	0.85816	0.901752
Gaussian Noise (Var=0.01)	26.08309	0.201363	0.49342	0.661472	0.964417
Gaussian Noise (Var=0.05)	19.71037	0.079789	0.497383	0.654308	0.919121
Speckle Noise (Var=0.01)	31.57855	0.41068	0.475464	0.75034	0.997434
Speckle Noise (Var=0.05)	24.86664	0.228578	0.489159	0.706485	0.922088
Rotate 90° Anticlockwise	17.16607	0.107029	0.513157	0.425617	0.977994
Rotate 180° Anticlockwise	16.82567	0.103229	0.49707	0.49127	0.967727
Rotate 270° Anticlockwise	17.16682	0.101436	0.481873	0.27259	0.961753
Gaussian Blur 2std dev + Median Filter (Aperture 5) + Salt and Pepper (5 % Noise) + Gaussian Noise (Var=0.05) + Speckle Noise (Var=0.05)	18.19022	0.028897	0.463955	0.190371	0.868516

(b) IMAGE: AIRFIELD					
Attacks	SSIM (I,I')	PSNR	BER (I,I')	NC (I,I')	NC (W,W')
No Attack	46.99864	0.992689	0.307251	0.971836	0.994036
Gaussian Blur 0.5 std dev	40.21519	0.941193	0.425785	0.789518	0.989273
Gaussian Blur 1 std dev	32.42935	0.64835	0.455547	0.759776	0.977642
Gaussian Blur 1.5 std dev	30.00568	0.477403	0.460854	0.751798	0.996658
Gaussian Blur 2 std dev	28.58221	0.361408	0.463734	0.757064	0.955167
Resizing (512->256->512)	32.66961	0.658211	0.454712	0.807615	0.982503
Crop and Replace by 0 (1st Quarter)	18.06318	0.739076	0.217331	0.642429	0.905661
Crop and Replace by 0 (2nd Quarter)	14.68989	0.737749	0.241173	0.669916	0.918845
Crop and Replace by 0 (3rd Quarter)	18.12552	0.739094	0.221333	0.618322	0.91356
Crop and Replace by 0 (4th Quarter)	15.57428	0.737913	0.235321	0.101424	0.962962
Crop and Replace by 255 (1st Quarter)	16.48988	0.739586	0.463032	0.729635	0.901668
Crop and Replace by 255 (2nd Quarter)	22.01176	0.740097	0.482147	0.690327	0.992229
Crop and Replace by 255 (3rd Quarter)	16.82641	0.739256	0.469723	0.710463	0.941931
Crop and Replace by 255 (4th Quarter)	19.2331	0.740843	0.47369	0.145056	0.962049
Crop Right Half and Replace by 0	12.11178	0.490421	0.167957	0.083865	0.932025
Crop Right Half and Replace by 255	17.40206	0.49155	0.649887	0.113814	0.958451
Crop Left Half and Replace by 0	15.09571	0.490928	0.131523	0.690967	0.925136
Crop Left Half and Replace by 255	13.65379	0.491432	0.628658	0.660544	0.888134
Crop Top Half and Replace by 0	13.0586	0.490101	0.152805	0.694583	0.935882
Crop Top Half and Replace by 255	15.42507	0.491112	0.638657	0.659265	0.905156
Crop Bottom Half and Replace by 0	13.66389	0.489331	0.154182	0.087134	0.940327
Crop Bottom Half and Replace by 255	14.86717	0.492822	0.636536	0.068593	0.913149
Median Filter (Aperture 3)	33.49103	0.639618	0.435936	0.120415	0.999819
Median Filter (Aperture 5)	30.03254	0.437871	0.454655	0.119048	0.984948
Salt and Pepper (2% Noise)	28.03788	0.680522	0.312439	0.642973	0.984851
Salt and Pepper (5% Noise)	24.16729	0.446003	0.315498	0.641987	0.982815
Gaussian Noise (Var=0.01)	26.29173	0.405914	0.476814	0.309781	0.956684
Gaussian Noise (Var=0.05)	19.96853	0.191405	0.481586	0.218869	0.902811
Speckle Noise (Var=0.01)	30.57089	0.614661	0.456928	0.569419	0.961548
Speckle Noise (Var=0.05)	23.9128	0.373482	0.471809	0.775895	0.886692
Rotate 90° Anticlockwise	15.30807	0.101532	0.512699	0.421124	0.995651

Rotate 180° Anticlockwise	14.65399	0.102047	0.497646	0.527501	0.995045
Rotate 270° Anticlockwise	15.31122	0.101833	0.48103	0.480128	0.957886
Gaussian Blur 2std dev + Median Filter (Aperture 5) + Salt and Pepper (5 % Noise) + Gaussian Noise (Var=0.05) + Speckle Noise (Var=0.05)	17.77562	0.045185	0.451057	0.134961	0.872051
(c) IMAGE: PEPPER					
Attacks	SSIM (I,I')	PSNR	BER (I,I')	NC (I,I')	NC (W,W')
No Attack	46.1935	0.973706	0.271194	0.966572	0.984689
Gaussian Blur 0.5 std dev	43.59527	0.902218	0.411102	0.954767	0.992837
Gaussian Blur 1 std dev	37.98662	0.642255	0.446003	0.947694	1.000017
Gaussian Blur 1.5 std dev	35.87764	0.54251	0.449184	0.937962	0.986577
Gaussian Blur 2 std dev	34.40202	0.475947	0.449642	0.927963	0.987919
Resizing (512->256->512)	37.37498	0.63783	0.452942	0.969443	0.981094
Crop and Replace by 0 (1st Quarter)	18.02933	0.723854	0.202629	0.901575	0.944601
Crop and Replace by 0 (2nd Quarter)	17.03702	0.722264	0.199154	0.915801	0.963796
Crop and Replace by 0 (3rd Quarter)	17.61236	0.722924	0.208836	0.915726	0.934425
Crop and Replace by 0 (4th Quarter)	18.77836	0.722337	0.199913	0.900392	0.933271
Crop and Replace by 255 (1st Quarter)	16.97384	0.723011	0.453835	0.915114	0.975468
Crop and Replace by 255 (2nd Quarter)	17.90226	0.722214	0.45097	0.915239	1.000822
Crop and Replace by 255 (3rd Quarter)	16.77587	0.722541	0.460968	0.901511	0.974543
Crop and Replace by 255 (4th Quarter)	16.22294	0.721318	0.45039	0.929924	0.94844
Crop Right Half and Replace by 0	14.82174	0.477226	0.12936	0.310157	0.93883
Crop Right Half and Replace by 255	13.98327	0.477307	0.629692	0.298993	0.925329
Crop Left Half and Replace by 0	14.81779	0.481239	0.143036	0.161373	0.938528
Crop Left Half and Replace by 255	13.87392	0.479892	0.641678	0.148206	0.930975
Crop Top Half and Replace by 0	14.50228	0.480911	0.132965	0.162313	0.943185
Crop Top Half and Replace by 255	14.41703	0.480956	0.631363	0.149011	0.952007
Crop Bottom Half and Replace by 0	15.15661	0.478602	0.139301	0.032161	0.936491
Crop Bottom Half and Replace by 255	13.49122	0.477916	0.640186	0.298936	0.917342
Median Filter (Aperture 3)	40.23302	0.636505	0.423611	0.904701	0.977683
Median Filter (Aperture 5)	38.05011	0.532768	0.438004	0.904681	0.990717
Salt and Pepper (2% Noise)	28.1799	0.506766	0.274563	0.801505	0.962378

Salt and Pepper (5% Noise)	24.31545	0.261639	0.282997	0.771512	0.976992
Gaussian Noise (Var=0.01)	26.18434	0.20622	0.491333	0.893283	0.983873
Gaussian Noise (Var=0.05)	19.82711	0.084706	0.495605	0.728862	0.907096
Speckle Noise (Var=0.01)	31.64505	0.441033	0.468826	0.757381	0.99272
Speckle Noise (Var=0.05)	24.91428	0.243569	0.481167	0.669836	0.954434
Rotate 90° Anticlockwise	16.4794	0.112083	0.50642	0.126578	0.986287
Rotate 180° Anticlockwise	16.90851	0.120504	0.497471	0.156952	0.99178
Rotate 270° Anticlockwise	16.47869	0.11164	0.490543	0.283956	0.98075
Gaussian Blur 2std dev + Median Filter (Aperture 5) + Salt and Pepper (5 % Noise) + Gaussian Noise (Var=0.05) + Speckle Noise (Var=0.05)	18.22476	0.033351	0.464767	0.307428	0.850535
(d) IMAGE: MANDRILL					
Attacks	SSIM (I,I')	PSNR	BER (I,I')	NC (I,I')	NC (W,W')
No Attack	50.8346	0.99748	0.324287	0.964872	0.980703
Gaussian Blur 0.5 std dev	37.79769	0.949584	0.451973	0.652473	0.991784
Gaussian Blur 1 std dev	29.87719	0.632381	0.483749	0.783224	0.976952
Gaussian Blur 1.5 std dev	28.14575	0.430244	0.489082	0.843479	0.97433
Gaussian Blur 2 std dev	27.33262	0.307486	0.490646	0.88074	0.987898
Resizing (512->256->512)	29.6846	0.640205	0.482456	0.873878	0.967229
Crop and Replace by 0 (1st Quarter)	17.97788	0.742716	0.240761	0.819321	0.934412
Crop and Replace by 0 (2nd Quarter)	17.29128	0.742393	0.24218	0.847154	0.978103
Crop and Replace by 0 (3rd Quarter)	17.09279	0.741396	0.251293	0.851018	0.984276
Crop and Replace by 0 (4th Quarter)	17.79154	0.740594	0.252766	0.842445	0.984986
Crop and Replace by 255 (1st Quarter)	17.15238	0.743205	0.489601	0.786474	0.92147
Crop and Replace by 255 (2nd Quarter)	17.94106	0.74141	0.49268	0.839919	0.97482
Crop and Replace by 255 (3rd Quarter)	18.22283	0.741894	0.502693	0.838879	0.988169
Crop and Replace by 255 (4th Quarter)	17.6576	0.740444	0.502743	0.800531	0.955298
Crop Right Half and Replace by 0	14.53374	0.492056	0.166252	0.255322	0.94631
Crop Right Half and Replace by 255	14.79622	0.490637	0.664871	0.363466	0.983404
Crop Left Half and Replace by 0	14.51201	0.492763	0.163612	0.296784	0.937844
Crop Left Half and Replace by 255	14.65437	0.493842	0.662651	0.296105	0.995125
Crop Top Half and Replace by 0	14.61918	0.49343	0.15242	0.266478	0.934161

Crop Top Half and Replace by 255	14.5288	0.493426	0.653595	0.296544	0.980978
Crop Bottom Half and Replace by 0	14.42756	0.491552	0.173676	0.220073	0.941885
Crop Bottom Half and Replace by 255	14.92921	0.491721	0.672848	0.559735	0.996536
Median Filter (Aperture 3)	29.78747	0.641115	0.448967	0.780235	0.978819
Median Filter (Aperture 5)	27.37619	0.350543	0.470036	0.79391	0.996561
Salt and Pepper (2% Noise)	28.56558	0.731682	0.317188	0.771794	0.949707
Salt and Pepper (5% Noise)	24.59975	0.518284	0.335457	0.755571	0.937836
Gaussian Noise (Var=0.01)	26.09482	0.503124	0.492325	0.681406	0.964656
Gaussian Noise (Var=0.05)	19.59942	0.237642	0.496025	0.561678	0.995004
Speckle Noise (Var=0.01)	31.44182	0.714189	0.480965	0.828966	0.985137
Speckle Noise (Var=0.05)	24.56973	0.47168	0.491634	0.811121	0.879708
Rotate 90° Anticlockwise	18.87803	0.105965	0.505821	0.61348	0.99931
Rotate 180° Anticlockwise	18.89277	0.105194	0.497177	0.698274	0.932344
Rotate 270° Anticlockwise	18.87788	0.100886	0.488358	0.393969	0.993063
Gaussian Blur 2std dev + Median Filter (Aperture 5) + Salt and Pepper (5 % Noise) + Gaussian Noise (Var=0.05) + Speckle Noise (Var=0.05)	17.64072	0.025453	0.467468	0.796696	0.83836

F. COMPUTATIONAL TIME ANALYSIS

The evolution of PSNR, SSIM, BER, and NC metrics over 20 iterations has been depicted in Fig. 17. It is to be noted that the real – time performance of the proposed scheme is ensured by adopting a fast single layer feed – forward neural network (SLFN) called the ELM, which relies on random weight allocation in the ELM Model [10][51][52] which gives training and testing time spans for the trained models within 70 – 90 msec range. It is due to the random weight allocation, that the PSNR, SSIM, BER, and NC metrics so presented will vary with each iteration. However, it is to be noted that the variation in each metric is small, and in some iterations, outperform all the metrics when compared with the published literature, already summarized in Table 3. Further, since Memristors are not available yet as a commercial product, the OP – Amp realization of the Chua’s diode, will demonstrate slight variations in the Chaotic Signals, which will depend on both the slew rate of the OP – Amp ICs and the tolerance of the circuit components so used for realizing the memristive oscillators.

Figure 17 depicts the evolution of different performance metrics for the different host images so considered in this work. Also presented is the computational time complexity for the embedding and semi – blind extraction procedures. From

the analysis, it can be seen that embedding time spans over few seconds and semi – blind extraction routine which involves the entire routine depicted in Figure 12, including the generation of chaotic dataset spans within a few seconds. This lies in the expected range as previously reported in the literature [59][60]. As far as the payload is concerned, since the proposed scheme relies on the watermark sequence and not on the embedded image, a better payload capability can be inferred.

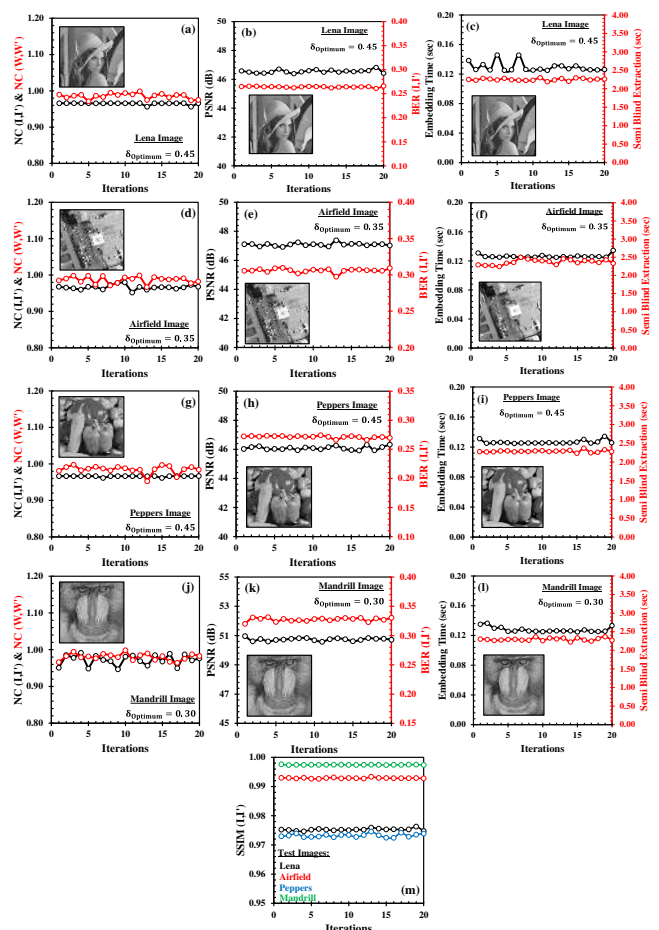


FIGURE 17: Evolution of different performance metrics for the various host images over a set of 20 iterations. Also presented is the computational time analysis for embedding and semi – blind extraction procedures.

G. SECURITY CONCERNS

In order to test the security concerns, the scheme is tested in a number of false conditions. Table 3 summarizes the results of the key space and key sensitivity analysis performed on the Lena Image. In the complete method, three main keys enforces the security. First during the scrambling using Arnold transform which decides the Arnold’s periodicity. As depicting in case 6, a mismatch in the Arnold’s key greatly reduces the NC metric of the watermark to the value of 0.1964 which demonstrates inaccurate extraction of the watermarking coefficients. The initial conditions and the coefficients of the

memristive based chaotic oscillator acts as a second key. On varying these secure keys, again a large degradation in the $NC(W,W')$ metric is observed, which depicts the security of the proposed scheme. The third secure is generated during the final watermark generation using the trained data of the two ELM models. Table 3 discusses the four cases of weights mismatch from which it can be concluded that the random weight allocation in the ELM too enforces a high degree of security. It is worth mentioning that, these cases have been studied separately here. In actual scenario, all these will combine and further strengthen the key sensitivity of the proposed scheme.

Table 3: Security testing on the Lena Image for Scaling Factor = 0.45 with PSNR = 46.50, SSIM = 0.97, BER = 0.26 and NC = 0.95

Sl No.	Cases	NC (W,W')
1	Watermark Weights Mismatch [$\alpha_1 = 0.0, \alpha_2=1.0$]	0.2784
2	Watermark Weights Mismatch [$\alpha_1 = 1.0, \alpha_2=0.0$]	0.2696
3	Watermark Weights Mismatch [$\alpha_1 = 0.2, \alpha_2=0.8$]	0.2675
4	Watermark Weights Mismatch [$\alpha_1 = 0.8, \alpha_2=0.2$]	0.2719
5	Mismatch in Circuit Components used for Memristive Oscillators [$R = 2k\Omega, C_1 = 68nF, C_2 = 6.8nF$]	0.2697
6	Mismatch in Initial Conditions used to Model Memristive Oscillators [Reversed initial conditions (ic_n) i.e. $ic_{1024}, ic_{1023} \dots ic_2, ic_1$]	0.1603
7	Incorrect Key used for Descrambling the Fractal Array [Arnold's Descrambling Key = 15]	0.1964

H. COMPARISON WITH PUBLISHED LITERATURE

The watermarking scheme proposed in this work based on Memristive Chaotic signals is compared with some state – of – the – art techniques. A comparison is presented in Table 4, which compares the NC values of the watermark after subjecting the signed images to StirMark attacks. Table 5 compares the PSNR and SSIM metric before subjecting the image to processing attacks, with various recent works. It is to be noted that the comparison with published literature is done ensuring similar host images and similar dimensions. All the references consider a host image of size 512×512 . From Table 5 and 6, it can be concluded that the presented technique offers competitive performance in terms of robustness and imperceptibility in comparison to the semi – blind watermarking techniques published in literature. The table further establishes the superiority of the proposed technique in comparison to the state – of – the – art algorithms.

Table 4: Comparison of $NC(W,W')$ in presence of image processing attacks with state – of – the – art techniques. Comparison is drawn considering similar host images with dimensions 512×512 .

Attack	Host Image: Lena			
	Ref. [8]	Ref. [10]	Ref. [17]	This Work
Gaussian Blur	-	0.970	-	0.981
Resizing	0.975	0.980	0.997	0.981
Crop & Replace	0.920	0.890	-	0.960
Median Filter	0.969	0.970	0.918	0.987
Salt & Pepper	0.956	0.950	-	0.990
Gaussian Noise	0.921	0.950	0.983	0.981
Speckle	0.899	0.960	-	0.997
	Host Image: Peppers			
	Ref. [11]	Ref. [10]	Ref. [17]	This Work
Gaussian Blur	-	0.980	-	1.000
Resizing	-	0.980	0.989	0.982
Crop & Replace	0.940	0.950	-	1.000
Median Filter	0.890	0.990	0.911	0.999
Salt & Pepper	0.860	0.960	-	0.977
Gaussian Noise	0.940	0.960	0.980	0.984
Speckle	-	0.970	-	0.992

Table 5: Comparison of PSNR and SSIM in absence of image processing attacks with state – of – the – art techniques

(a) PSNR				
Image	Ref. [8]	Ref. [10]	Ref. [17]	This Work
Leena	44.320	54.260	45.433	46.508
Airfield	-	-	-	46.999
Peppers	-	53.060	45.154	46.193
Mandrill	-	54.560	32.492	50.835
(b) SSIM				
Image	Ref. [8]	Ref. [10]	Ref. [17]	This Work
Leena	0.960	0.990	0.994	0.975
Airfield	-	-	-	0.993
Peppers	-	0.990	0.983	0.974
Mandrill	-	0.990	0.961	0.997

V. CONCLUSION AND FUTURE SCOPE

In this work, a novel secure and robust digital image watermarking technique is proposed. Double encryption is implemented using Arnold transform and Memristive chaotic signals. The proposed embedding technique is based on fractal dimensions extracted using Higuchi's algorithm, which is scrambled using Arnold transform. The unique key is stored for embedding and extraction procedures. To establish experimental validations, the chaotic signals were generated using Memristor based chaotic oscillator. The proposed scheme incorporates two ELM models trained using HOG

features and chaotic signals, and the output was combined using a sum of weighted averages. Semi – Blind Watermark embedding and extraction were followed, and an in-depth analysis using various figure of metrics were carried out. From the results presented, the proposed technique is proved to be robust and secure and establishes its significance in various applications.

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