Robust Execution of Contingent, Temporally Flexible Plans *

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Abstract

Many applications of autonomous agents require groups to work in tight coordination. To be dependable, these groups must plan, carry out and adapt their activities in a way that is robust to failure and uncertainty. Previous work has produced contingent plan execution systems that provide robustness during their plan extraction phase, by choosing between functionally redundant methods, and during their execution phase, by dispatching temporally flexible plans. Previous contingent execution systems use a centralized architecture in which a single agent conducts planning for the entire group. This can result in a communication bottleneck at the time when plan activities are passed to the other agents for execution, and state information is returned.

This paper introduces the plan extraction component of a robust, distributed executive for contingent plans. Contingent plans are encoded as Temporal Plan Networks (TPNs), which use a non-deterministic choice operator to compose temporally flexible plan fragments into a nested hierarchy of contingencies. To execute a TPN, the TPN is first distributed over multiple agents, by creating a hierarchical ad-hoc network and by mapping the TPN onto this hierarchy. Second, candidate plans are extracted from the TPN using a distributed, parallel algorithm that exploits the structure of the TPN. Third, the temporal consistency of each candidate plan is tested using a distributed Bellman-Ford algorithm. Each stage of plan extraction distributes communication to adjacent agents in the TPN, and in so doing eliminates communication bottlenecks. In addition, the distributed algorithm reduces the computational load on each agent. The algorithm is empirically validated on a range of randomly generated contingent plans.

Introduction

The ability to coordinate groups of autonomous agents is key to many real-world tasks, such as a search and rescue mission, or the construction of a Lunar habitat. Achieving this ability requires performing robust execution of contingent, temporally flexible plans in a distributed manner. Methods have been developed for the dynamic execution (Morris & Muscettola 2000) of temporally flexible plans (Dechter, Meiri, & Pearl 1991). These methods adapt to failures that fall within the margins of the plan and hence add robustness to execution uncertainty.

To address plan failure, (Kim, Williams, & Abramson 2001) introduced a system called *Kirk*, that performs dynamic execution of temporally flexible plans with contingencies. These contingent plans are encoded as alternative choices between functionally equivalent sub-plans. In Kirk, the contingent plans are represented by a Temporal Plan Network (TPN) (Kim, Williams, & Abramson 2001), which extends temporally flexible plans with a nested choice operator. To dynamically execute a TPN, Kirk continuously extracts a plan from the TPN that is temporally flexible, given the execution history, and dispatches the plan, using the methods of (Tsamardinos, Muscettola, & Morris 1998). Dynamic execution of contingent plans adds robustness to plan failure.

However, as a centralized approach, Kirk can be brittle to failures caused by communication limitations. This is because the agent performing planning must communicate the plan with all other agents before execution. This leads to a communication bottleneck at the lead agent.

We address this limitation through a distributed version of Kirk, which performs distributed dynamic execution of contingent temporally flexible plans. The distributed approach evens out communication requirements and reduces the brittleness to a single communication bottleneck.

This paper focuses on a method for dynamically selecting a feasible plan from a TPN. A subsequent method for performing distributed execution of the plan is presented in (Block, Wehowsky, & Williams 2006). Our key innovation is a distributed, hierarchical algorithm for searching a TPN for a feasible plan. This algorithm shares the computational load of plan extraction between all agents, thus reducing the computational complexity for each agent, and exploits parallelism through concurrent processing. Our plan selection algorithm, Distributed-Kirk (D-Kirk), is comprised of three stages.

- 1. Distribute the TPN across the processor network,
- 2. Generate candidate plans through distributed search on the TPN, and
- 3. Test the generated plans for temporal consistency.

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This paper begins with an example TPN and an overview of the way in which D-Kirk operates on it. We provide a formal definition of a TPN and then discuss the three stages of D-Kirk. Finally, we discuss the complexity of the D-Kirk algorithm and present experimental results demonstrating its performance.

Example Scenario

In this section, we discuss at a high level the three step approach taken by D-Kirk to execute a contingent plan. Throughout this paper we use a simple, pedagogical example TPN to aid understanding of the key concepts.

This TPN is represented as a graph in Fig. 1, where nodes represent points in time and arcs represent activities. Each activity is labeled with upper and lower time bounds that represent the temporal constraints on its duration. A pathway through the TPN is a thread of activity. A node representing a non-deterministic choice for the target of its pathway is called a *choice node* and is shown as an inscribed circle.



Figure 1: Example TPN

The plan is to be executed by a group of seven processors, $p1, \ldots, p7$. To perform distributed plan selection, the first step is to distribute the TPN itself over the processors. A TPN is built as a hierarchy of nested subnetworks, and we exploit this hierarchy when distributing the plan selection problem.

To facilitate TPN distribution, a leader election algorithm is used to arrange the processors into a hierarchy (Fig. 2). The hierarchical structure of the TPN is then used to map subnetworks to processors. For example, the master processor p1 handles the composition of two subnetworks of the plan at the start node (node A) and the end node (node B). It passes responsibility for each of the two main subnetworks to the two processors immediately beneath it in the hierarchy. Nodes C,D,E,F,G,H are passed to p2 and nodes I,J,K,L,M,N are passed to p3.

In the remaining two steps the processors work together to extract a plan from the TPN that is temporally consistent. Step two generates a candidate plan. This involves selecting a single thread of execution from the plan. This step coordinates in a hierarchical fashion, where each processor sends messages to its neighbors in the hierarchy corresponding to the subnetworks of the TPN. Neighbors are requested to make selections in the subnetworks for which they are responsible and in this way, selections are made concurrently. In the example, only the subnetwork owned by p2



Figure 2: A three-level hierarchy formed by leader election

(nodes C,D,E,F,G,H) contains a choice, that is, p2 must decide between ActivityA and ActivityB, whereas p3 has no choice to make.

Having generated a candidate plan, the third and final step of D-Kirk is to test the candidate plan for consistency. Again, this is performed in a hierarchical fashion, where consistency checks are first made at the lowest level and successful sub-plan candidates are then checked at an increasingly higher level. For example, p2 and p3 simultaneously check that their subnetworks are internally consistent. If so, p1 then checks that the parallel execution of the two candidates is consistent.

Throughout the plan generation and consistency checking phases of D-Kirk, processors exchange messages to coordinate their activities. These messages are distributed between all processors, avoiding the communication bottleneck at the leader node which is present in a centralized architecture. In addition, candidate generation (Step 2) and consistency checking (Step 3) are interleaved, such that some of the processors are generating candidates while others are simultaneously checking consistency. This use of parallel processing improves the efficiency of the algorithm.

Temporal Plan Networks

A TPN is used to represent a contingent, temporally flexible plan. The primitive element of a TPN is an activity[l, u], which is an executable command with a simple temporal constraint. The simple temporal constraint [l, u] places a bound $t^+ - t^- \in [l, u]$ on the start time t^- and end time t^+ of the network to which it is applied. A TPN is built from a set of primitive activities and is defined recursively using the choose, parallel and sequence operators, taken from the Reactive Model-based Programming Language (RMPL) (Williams *et al.* 2003), (Kim, Williams, & Abramson 2001). These operators are defined below. A TPN encodes all executions of a non-deterministic concurrent, timed program, comprised of these operators.

• choose (TPN_1, \ldots, TPN_N) introduces multiple subnetworks of which only one is to be chosen. A choice variable is used at the start node to encode the currently selected subnetwork. A choice variable is *active* if it falls within the currently selected portion of the TPN. The choose operator allows us to specify nested choices in the plan, where each choice is an alternative sub-plan that performs the same function.

- parallel $(TPN_1, \ldots, TPN_N)[l, u]$ introduces multiple subnetworks to be executed concurrently. A simple temporal constraint is applied to the entire network. Each subnetwork is referred to as a *child* subnetwork.
- sequence(TPN₁,...,TPN_N) [l, u] introduces multiple subnetworks which are to be executed sequentially. A simple temporal constraint is applied to the entire network. For a given subnetwork, the subnetwork following it in a sequence network is referred to as its *successor*.

Graph representations of the activity, choose, parallel and sequence network types are shown in Fig. 3. Nodes represent time events and directed edges represent simple temporal constraints.



Figure 3: TPN Constructs

A *temporally consistent* plan is obtained from the TPN if and only if a *feasible choice assignment* is found. See (Wehowsky 2003) for a more precise definition.

Definition 1 A temporally flexible plan is **temporally consistent** if there exists an assignment of times to each event such that all temporal constraints are satisfied.

Definition 2 A feasible choice assignment is an assignment to the choice variables of a TPN such that 1) all active choice variables are assigned, 2) all inactive choice variables are unassigned, and 3) the temporally flexible plan (program execution) corresponding to this assignment is temporally consistent.

TPN Distribution

Recall that the first step of D-Kirk is to distribute the input TPN over the available processors. The TPN may be provided by a high-level generative planner or by a human operator, but plan generation is outside the scope of this paper.

To support this and the subsequent two steps, the processors must first be able to communicate. To accomplish this, D-Kirk begins by establishing a hierarchical, ad-hoc communication network. In addition, an overall leader is selected, in order to initiate plan extraction and to communicate with the outside world.

Ad-Hoc Processor Network Formation

We use the leader election algorithm in (Nagpal & Coore 1998) to arrange the processors into a hierarchical network, an example of which is shown in Fig. 2. For each processing node, the node immediately above it in the hierarchy is its leader, those at the same level within that branch of the hierarchy are its *neighboring leaders* and those directly below it in the hierarchy are its followers. The leader election algorithm forms a hierarchy using a message passing scheme that ensures that every node can communicate with its leader, as well as with all neighboring leaders and followers. Note that the hierarchical communication structure lends itself well to distributing the TPN, which is also hierarchical. It may be possible to improve the performance of the plan selection algorithm by using the TPN structure to guide the formation of the processor hierarchy. This is an interesting direction for future work.

TPN Distribution over the Processor Network

A TPN is distributed by assigning to each processor the responsibility for zero or more nodes of a TPN graph, such that each node is assigned to exactly one processor. During the subsequent two steps of D-Kirk, each processor maintains all data relevant to its assigned nodes.

This distribution scheme requires that two processors be able to communicate whenever they have been assigned two TPN nodes that are linked by a temporal constraint. This requirement is satisfied by D-Kirk's TPN distribution algorithm, shown in Fig. 4. See (Wehowsky 2003) for further explanation. Note that the algorithm allows the TPN to be distributed down to a level at which a processor handles only a single node; this permits D-Kirk to operate on heterogeneous systems that include computationally impoverished processors.

We now demonstrate this distribution algorithm on the TPN of Fig. 1 and the processor hierarchy of Fig. 2. The TPN is supplied from an external source, which establishes a connection with the top-level leader, p1. The TPN is a parallel network at the highest level, hence processor p1 assigns the start and end nodes (nodes A,B) to itself (line 7). There are two subnetworks, which p1 assigns to its two followers, p2 and p3 (lines 15-18). p1 passes the choose subnetwork (nodes C, D, E, F, G, H) to p2 and the sequence subnetwork (nodes I, J, K, L, M, N) to p3. p2 and p3 then process their subnetworks in parallel. p2 assigns the start and end nodes (nodes C,D) to itself (line 7). This network has two subnetworks, which p2 assigns to two of its followers, p4 and p5 (lines 15-18). p2 passes ActivityA (nodes E,F) to p4 and ActivityB (nodes G,H) to p5. Since activities can not be decomposed, p4 and p5 assign nodes E,F and G,H, respectively, to themselves (lines 3-4). Meanwhile, p3receives the sequence subnetwork and assigns the start and end nodes (nodes I, J) to itself (line 7). This network has two subnetworks, which p3 assigns to two of its followers, p6and p7 (lines 15-18). p3 passes ActivityC (nodes K,L) to p6 and ActivityD (nodes M,N) to p7. p6 and p7 then assign nodes K,L and nodes M,N, respectively, to themselves (lines 3-4).

1:	wait for TPN
2:	$n \leftarrow$ number of followers of p
3:	if TPN is of type activity then
4:	assign start and end nodes of TPN to p
5:	else
6:	$k \leftarrow$ number of subnetworks
7:	assign start and end nodes to p
8:	if $n = 0$ then
9:	if p has a neighbor leader v then
10:	send $\frac{k}{2}$ subnetworks of TPN to v
11:	assign $\frac{k}{2}$ subnetworks of TPN to p
12:	else
13:	assign TPN to p
14:	end if
15:	else if $n \ge k$ then
16:	for each of k subnetworks of TPN do
17:	assign subnetwork of TPN to a follower of p
18:	end for
19:	else if $n < k$ then
20:	for each of n subnetworks of TPN do
21:	assign subnetwork to a follower of p
22:	end for
23:	assign remaining $(k - n)$ subnetworks of TPN to p
24:	end if
25:	end if

Figure 4: TPN Distribution Algorithm for node p

Candidate Plan Generation

Having distributed the TPN across the available processors, D-Kirk's second step generates candidate plans. These candidates correspond to different assignments to the choice variables at each choice node, and can be viewed as a restricted form of a conditional CSP (Mittal & Falkenhainer 1990). D-Kirk uses parallel, recursive, depth first search to perform these assignments. This use of parallel processing is one key advantage of D-Kirk over a traditional, centralized approach.

D-Kirk operates on three network types formed from the four types fundamental to a TPN. These are activity, parallel-sequence and choose-sequence, as shown in Fig. 5, where the subnetworks A_i, \ldots, Z_i are of any of these three types. We handle the simple temporal constraint present on a sequence network by considering a sequence network as a special case of a parallel-sequence network, in which only one subnetwork exists.

Note that while a simple temporal constraint [l, u] is locally inconsistent if l > u, we assume that the TPN is checked prior to running D-Kirk, to ensure that all temporal constraints are locally consistent. This assumption means that only parallel-sequence networks can introduce temporal inconsistencies.

D-Kirk uses the following messages for candidate plan generation.

- findfirst instructs a network to make the initial search for a consistent set of choice variable assignments.
- findnext is used when a network is consistent internally, but is inconsistent with other networks. In this case, D-Kirk uses findnext messages to conduct a systematic search for a new consistent assignment, in order



Figure 5: Constructs for D-Kirk

to achieve global consistency. findnext systematically moves through the subnetworks and returns when the first new consistent assignment is found. Therefore, a successful findnext message will cause a change to the value assigned to a single choice variable, which may in turn cause other choice variables to become active or inactive. Conversely, findfirst attempts to make the first consistent assignment to the choice variable in every choice node in the network.

- fail indicates that no consistent set of assignments was found and hence the current set of assignments within the network is inconsistent.
- ack, short for acknowledge, indicates that a consistent set of choice variable assignments has been found.

Whenever a node initiates search in its subnetworks, using findfirst or findnext messages, the relevant processors search the subnetworks simultaneously. This is the origin of the parallelism in the algorithm.

The following three sections describe the actions carried out by the start node of each network type on receipt of a findfirst or findnext message. Pseudo-code for each section of the algorithm is shown in Figs. 7 through 11 in the appendix. A more detailed description of the algorithm, including a walk-through of the pseudo-code for an example TPN, can be found in (Wehowsky 2003).

Activity

During search, an activity node propagates request messages forward and response messages backward.

Parallel-Sequence Network

On receipt of a findfirst message, the start node v of a parallel-sequence network initiates a search of its subnetworks and of any successor network, in order to find a temporally consistent plan. The pseudo-code is in Fig. 7.

First, the start node sends findfirst messages to the start node of each child subnetwork of the parallel-sequence structure (lines 2-4) and to the start

node of the successor network, if present (lines 5-7). These searches are thus conducted in parallel. If any of the child subnetworks or the successor network fails to find a locally consistent assignment (line 12), then no consistent assignment to the choice variables exists and the start node returns fail (line 13).

Conversely, suppose that all child subnetworks and the successor network find variable assignments such that each is internally temporally consistent. The start node must then check for consistency of the entire parallel-sequence network (line 15). This is performed by a distributed Bellman-Ford consistency checking algorithm, which is explained in the next section. If the consistency check is successful, the start node returns an ack message to its parent (line 16) and the search of the parallel-sequence network is complete.

If, however, the consistency check is not successful, the start node must continue searching through all permutations of assignments to the child subnetworks for a globally consistent solution (line 18). The pseudo-code for this search is in Fig. 8. The start node sends findnext messages to each subnetwork (lines 1-2). If a subnetwork fails to find a new consistent solution then the start node sends a findfirst message to that subnetwork to reconfigure it to its original, consistent solution (lines 11-12) and we move on to the next subnetwork. If at any point, a subnetwork successfully finds a new consistent solution, the start node tests for global consistency and returns true if successful (lines 4-6). If the consistency check is unsuccessful, we try a different permutation of variable assignments (line 8) and continue searching. If all permutations are tested without success, then no globally consistent assignment exists (line 15).

When the start node v of a parallel-sequence network receives a findnext message, it systematically searches all consistent assignments to its subnetworks, in order to find a new globally consistent assignment, just as described above. The pseudo-code is in Fig. 9.

If the search for a new globally consistent assignment (line 1) is successful, the start node sends ack to its parent (line 2). If it fails, however, the start node attempts to find a new assignment to the successor network. If a successor network is present, the start node sends a findnext message and returns the response to its parent (lines 3-6). If no successor network is present, then no globally consistent assignment exists and the node returns fail (line 8).

Choose-Sequence Network

When the start node of a choose-sequence network receives a findfirst message, it searches for a consistent plan by making an appropriate assignment to its choice variable and by initiating search in its successor network, if present. The pseudo-code is in Fig. 10.

The start node begins by sending a findfirst message to any successor network (lines 2-4). It then systematically assigns each possible value to the network's choice variable and, in each case, sends a findfirst message to the enabled subnetwork (lines 5-7). If a subnetwork returns fail, indicating that no consistent assignment exists, the current value of the choice variable is trimmed from its domain to avoid futile repeated searches (line 18), and the next value is assigned. As soon as a subnetwork returns ack, indicating that a consistent assignment to the subnetwork was found, the start node forwards the response from the successor network to its parent and the search terminates (line 12). If no successor network is present, the network is consistent and the start node returns ack to its parent (line 14). If all assignments to the network's choice variable are tried without receipt of an ack message from a child subnetwork, the start node returns fail to its parent, indicating that no consistent assignment exists (line 21).

When the start node of a choose-sequence network receives a findnext message, it first attempts to find a new consistent assignment for the network while maintaining the current value of the choice variable. The pseudo-code is in Fig. 11.

The start node does this by sending findnext to the currently selected subnetwork (lines 1-2). If the response is ack, a new consistent assignment has been found, so the start node returns ack to its parent and the search is over (lines 4-6). If this fails, however, the start node searches unexplored assignments to the network's choice variable, in much the same way as it does on receipt of a findfirst message (lines 8-18). Finally, if this strategy also fails, the start node attempts to find a new consistent assignment in any successor network, by sending a findnext message (lines 19-20).

Temporal Consistency Checking

In the third and final step, each plan generated by candidate generation must be tested for temporal consistency. Consistency checking is implemented using a distributed Bellman-Ford Single Source Shortest Path (SSSP) algorithm (Lynch 1997), and is run on the distance graph corresponding to the portion of the TPN that represents the current candidate. Temporal inconsistency is detected as a negative weight cycle (Dechter, Meiri, & Pearl 1991). Consistency checking is interleaved with candidate generation, such that D-Kirk simultaneously runs multiple instances of the distributed Bellman-Ford algorithm on isolated subsets of the TPN.

Use of the distributed Bellman-Ford algorithm has two key advantages. First, it requires only local knowledge of the TPN at every processor. Second, when run synchronously, it runs in time linear in the number of processors. This completes the development of the three stages of D-Kirk involved in plan extraction.

Discussion

We conclude by discussing the performance of D-Kirk. In the centralized case, the time complexity of TPN plan extraction is determined by the complexity of the SSSP algorithm, used to detect temporal inconsistencies and the number of consistency checks that must be conducted. In the worst case, N^e checks must be made, where N is the number of nodes and e is the size of the domain of the choice variables. A centralized Bellman-Ford SSSP algorithm has time complexity NE, where E is the number of edges, giving an overall worst case time complexity of $N^{e+1}E$.

D-Kirk uses the distributed Bellman-Ford algorithm, whose computational complexity is linear in the number of nodes, since each node communicates only with its local neighbors. D-Kirk begins consistency checking at the deepest level in the TPN hierarchy, progressing to higher levels only if consistency is achieved. Therefore, in the worst case, N consistency checks are required for each permutation of choice variable assignments; one initiated at each node. However, the number of variables involved in each consistency check is reduced as the depth of the check is increased. If the graph hierarchy is assumed to be of depth m, with branching factor b, then a consistency check initiated at a node at depth x involves $O(b^{m-x})$ nodes. Each node communicates with its b + 1 neighbors, hence the time complexity is $O((b+1)b^{m-x})$. The number of searches at depth x is b^x , thus the total complexity is $O((b+1)b^m)$. Averaging over all nodes, the computational complexity per node is $O((b+1)b^{m(e+1)})$.

Compared to the computational complexity of centralized plan extraction, $N^{e+1}E = b^{m(e+1)}b^{m-1}$, we see that D-Kirk is more efficient provided that $b + 1 < b^{m-1}$; this is true for typical plans.

Furthermore, the time complexity of D-Kirk is likely to be far better than the worst-case estimates, since the fast consistency checks performed on smaller plans at deeper levels may prevent unnecessary, more expensive consistency checks at higher levels.

The run time performance of D-Kirk was tested empirically on randomly generated TPNs, using a C++ implementation that simulates execution on an array of processors. Exactly one TPN node was assigned to each processor and the number of nodes in each randomly generated TPN was varied between 1 and 100. For each TPN instance, the number of TPN constructs (parallel, sequence or choose) was varied between 3 and 30 and the maximum recursive depth was varied between 4 and 10. Run time was measured by the number of listen-act-respond cycles completed by the processor network.

Fig. 6 shows a plot of the average number of cycles against the average number of nodes. The results show that the variation in the number of cycles is roughly linear with the number of nodes. This suggests that in practice, the run time will be dominated by the distributed Bellman-Ford consistency checking algorithm, which is linear in the number of nodes, as opposed to backtrack search, which is exponential. The reason for this is that the worst-case exponential time complexity of D-Kirk occurs only when the TPN is composed entirely of choose subnetworks.

To summarize, this paper introduced the Distributed Temporal Planner (D-Kirk), the plan extraction component of a distributed executive that operates on contingent, temporally flexible plans. D-Kirk operates on a Temporal Plan Network (TPN), by distributing both data and algorithms across available processors. D-Kirk employs a series of distributed algorithms that exploit the hierarchical structure of a TPN to, first, form a processor hierarchy and assign TPN subnetworks to each processor; second, search the TPN for candidate plans, and, finally, check for candidate temporal con-



Figure 6: Number of cycles vs. number of nodes

sistency. This distributed approach spreads communication more evenly across the processors, helping to alleviate the communication bottleneck present in a centralized architecture. Furthermore, D-Kirk reduces the computational load on each processor and allows concurrent processing.

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Appendix : D-Kirk Pseudo-Code

1: $parent \leftarrow sender of msg$

- 2: for each child do
- 3: send findfirst to w
- 4: end for
- 5: if successor B exists then
- send findfirst to B 6:
- 7: end if
- 8: wait for all responses from children
- 9: if successor \hat{B} exists then
- 10: wait for response from B
- 11: end if
- 12: if any of the responses is fail then
- send fail to parent 13:
- 14: else
- 15: if check-consistency(v) then
- send ack to parent 16:
- 17: else
- 18: if search-permutations(v) then
- 19: send ack to parent
- 20: else
- 21: send fail to parent
- 22: end if
- 23: end if
- 24: end if

Figure 7: parallel-findfirst (node v)

- 1: for w = child-0 to child-n do
- 2: send findnext to w
- 3: wait for response
- if response = ack then 4:
- 5: if check-consistency(v) then
- 6: return true
- 7: else
- 8: $w \gets \mathsf{child-0}$
- 9: end if
- 10: else
- 11: send findfirst to w
- 12: wait for response end if
- 13:
- 14: end for
- 15: return false

Figure 8: search-permutations (node v) function

- 1: if search-permutations() then
- send ack to parent 2:
- 3: else if successor B exists then
- 4: send findnext to B
- 5: wait for response
- send response to parent 6:
- 7: else
- 8: send fail to parent

```
9: end if
```

Figure 9: parallel-findnext (node v) function

- 1: $parent \leftarrow sender of msg$ 2: if successor B exists then send findfirst to B 3. 4: **end if** 5: for w = child-0 to child-n do $choicevariable \gets w$ 6: send findfirst to w 7: 8: wait for response from child wif response = ack then 9: if successor B exists then 10: 11: wait for response from successor B12: send response to parent 13: else 14: send ack to parent 15: end if 16: return 17: else 18: remove w from child list 19: end if 20: end for 21: send fail to parent
 - Figure 10: choose-findfirst() function
- 1: $w \leftarrow \text{current assignment}$
- 2: send findnext to w
- 3: wait for response
- 4: if response = ack then
- 5: send ack to parent
- 6: return
- 7: **end if**
- 8: while w < child-n do
- 9: $w \leftarrow \text{next child}$
- 10: send findfirst to w
- 11: wait for response
- **if** response = ack **then**
- send ack to parent
- remove w from child list
- 18: end while
- 19: if successor *B* exists then
- 20: send findnext to B
- for w = child0 to child-n do 21:
- 22: choice variable $\leftarrow w$
- 23: send findfirst to w
- 24: wait for response from child w
- 25: if response = ack then
- 26: break
- end if 27:
- 28: end for 29:
- wait for response from B30: send response to parent
- 31: else
- 32: send fail to parent
- 33: end if

Figure 11: choose-findnext() function

- 12: 13: 14: return 15: else 16:
 - 17: end if