

# Robust Midsagittal Plane Extraction from Coarse, Pathological 3D Images

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**Abstract.** This paper focuses on the evaluation of an ideal midsagittal plane (iMSP) extraction algorithm. The algorithm was developed for capturing the iMSP from 3D normal and pathological neural images. The main challenges are the drastic structural asymmetry that often exists in pathological brains, and the sparse, nonisotropic data sampling that is common in clinical practice. A simple edge-based, cross-correlation approach is presented that decomposes the iMSP extraction problem into discovery of symmetry axes from 2D slices, followed by robust estimation of 3D plane parameters. The algorithm's tolerance to brain asymmetries, input image offsets and image noise is quantitatively measured. It is found that the algorithm can extract the iMSP from input 3D images with (1) large asymmetrical lesions; (2) arbitrary initial yaw and roll angle errors; and (3) low signal-to-noise level. Also, no significant difference is found between the iMSP computed by the algorithm and the midsagittal plane estimated by two trained neuroradiologists.

**Keywords:** midsagittal plane, asymmetry, robust estimation

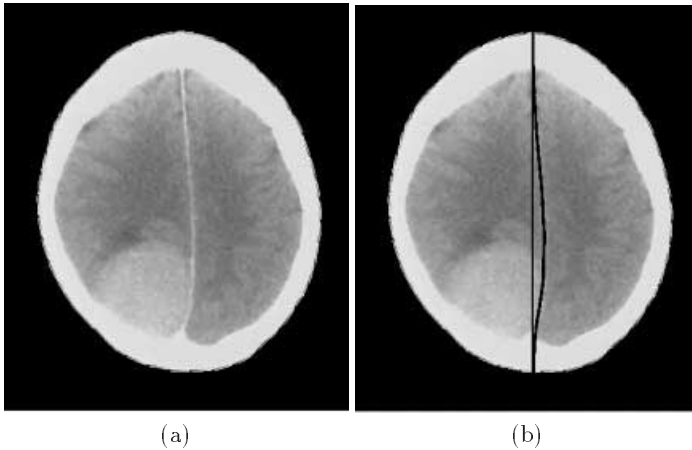
## 1 Introduction

Healthy human brains exhibit an approximate bilateral symmetry with respect to the interhemispheric (longitudinal) fissure plane bisecting the brain, known as the **midsagittal plane** (MSP). However, human brains are almost never perfectly symmetric [4,5,6]. Pathological brains, in particular, often depart drastically from reflectional symmetry. For effective pathological brain image alignment and comparison (e.g. [4,10,11]) it is most desirable to define a *plane of reference* that is invariant for symmetrical as well as asymmetrical brain images and to develop algorithms that capture this reference plane robustly.

We define an **ideal midsagittal plane (iMSP)** as a virtual geometric plane about which the given 3D brain image presents maximum bilateral symmetry. Computationally, this plane is determined by taking the majority votes from both axial and coronal 2D slices based on a sound geometric analysis (Section 2.1). Factors that challenge the robustness of an iMSP algorithm include: (1) the intrinsic factor: the brains being imaged can be either bilaterally symmetric or drastically asymmetric; (2) the extrinsic factor(s): anisotropism, under-sampling,

initial transformation errors and artifacts/noise can be introduced during the imaging process.

The well known Talairach framework is an anatomical landmark-based approach to define a 3D brain coordinate system [18]. Patient image to Talairach framework registration is difficult to achieve automatically since it relies on identifying 3D anatomical features that may not be obvious in the image. Furthermore, when the interhemispheric sagittal plane no longer lies on a flat surface due to normal or pathological deformation (Figure 1(a)), the interhemispheric medial plane is ill defined. In contrast, the iMSP is based on global geometry of the head and can be found using low-level image processing techniques. Furthermore, it remains well-defined in pathological cases, forcing a virtual left-right separation consistent with the location where an ideal midsagittal plane would be if not for the presence of local brain deformation (Figure 1(b)).



**Fig. 1.** (a) An axial brain slice, the midline is deformed due to a space occupying tumor. (b) The intersection of the extracted iMSP with the same 2D brain slice (straight line), and the deformed midline (curved line) captured by a “snake” active contour.

Designing a robust algorithm that deals with real clinical images originates from our desire to facilitate on-line clinical image database indexing and retrieval for real-time medical consultation [10,11,12,13]. We have developed a simple yet robust algorithm that can extract the iMSP of a brain from clinical CT or MR images (Section 2.2). The algorithm has been applied on more than 100 3D clinical images and tested on both synthetic and real images with computed ground truth. Breakdown points of the iMSP extraction algorithm are found by varying brain orientation, lesion size, and noise level, and are compared against a maximization of mutual information method (Section 3). We also consider “ground truth” generated by human experts, and find no significant difference

between the orientations estimated by our iMSP algorithm and those hand-picked by two neuroradiologists (Section 3).

The goal of many existing MSP detection algorithms [1,2,3,7,19] is to locate the plane of reflection of a roughly symmetrical brain image. Tolerance of these algorithms to asymmetry is reported to be low [3,7]. The MSP algorithm developed in [15] is tested on simulated PET images to show its insensitivity to focal asymmetries. More recently, Smith and Jenkinson [17] presented an algorithm for finding symmetry axes in partially damaged images of various modalities. However, no quantitative evaluations have yet been given and the computation is expensive.

## 2 Ideal Midsagittal Plane Extraction

We define an *ideal head coordinate system* centered in the brain with positive  $X_0, Y_0$  and  $Z_0$  axes pointing in the right, anterior and superior directions respectively (Figure 2, white coordinate axes). With respect to this coordinate system, the iMSP of the brain is defined as the plane  $X_0 = 0$ . Ideally, a set of *axial (coronal)* slices is cut perpendicular to the  $Z_0(Y_0)$  axis, and the intersection of the MSP with each slice appears as a vertical line on the slice<sup>1</sup>.

In clinical practice, however, the imaging coordinate system XYZ (Figure 2(a), black coordinate axes) differs from the ideal coordinates due to unintentional positioning errors and/or deliberate realignments introduced so that a desired volume can be better imaged. The orientation of the imaging coordinate system differs from the ideal coordinate system by three rotation angles, pitch, roll and yaw, about the  $X_0, Y_0$  and  $Z_0$  axes, respectively. The imaging coordinate system can also be offset (Figure 2(a)). The goal of an iMSP algorithm is to find the transformation between the two planes:  $X_0 = 0$  and  $X = 0$ .

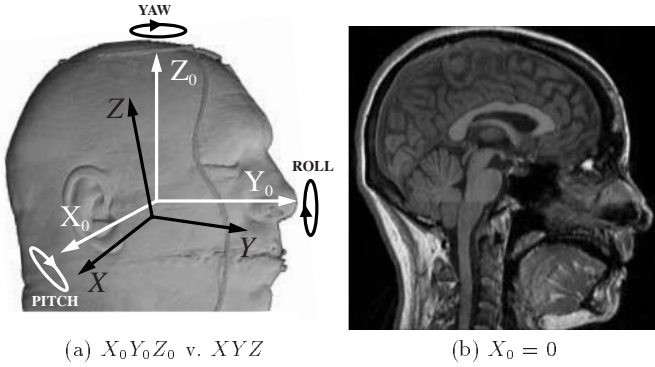
### 2.1 Geometry of the Ideal Midsagittal Plane

Under the *imaging coordinate system*, the iMSP can be represented as

$$aX + bY + cZ + d = 0 \tag{1}$$

where  $(a, b, c)$  is a vector describing the plane normal. For the rest of this section we assume a nonzero scaling such that  $\sqrt{a^2 + b^2} = 1$ . Now consider the  $i$ th axial slice, represented by the plane equation  $Z = Z_i$ . The symmetry axis of the  $i$ th slice is the intersection of the above two planes:  $aX + bY + (cZ_i + d) = 0$ . This is the equation of a 2D line  $(\theta_i, \rho_i)$  in the image XY plane, having line orientation  $\theta_i = \arctan(b/a)$  and perpendicular offset from the image origin  $\rho_i = cZ_i + d$ . By examining this line equation, we can make two immediate observations. First, the orientation angle  $\theta_i = \arctan(b/a)$  is the same for the symmetry axes of all slices regardless of their  $Z_i$  position. Secondly, the offset

<sup>1</sup> The analysis given to the axial slices from now on can be applied to coronal slices (cut along the Y axis) as well with corresponding symbols changed: ‘Z’ to ‘Y’.



**Fig. 2.** (a) Ideal head coordinate system  $X_0Y_0Z_0$  vs. the imaging coordinate system  $XYZ$ . The iMSP algorithm finds the transformation between planes  $X_0 = 0$  and  $X = 0$ . Rendered head courtesy of the Visible Human Project. (b) A midsagittal plane ( $X_0 = 0$ ) automatically extracted using our iMSP extraction algorithm.

$\rho_i$  of the symmetry axis on slice  $Z = Z_i$  is linearly related to  $Z_i$  as a function of plane parameters  $c$  and  $d$ . Therefore, given the translational offset of at least two symmetry axes on different slices, we can estimate  $c$  and  $d$  by solving a set of linear equations. These observations form the basis of the iMSP extraction algorithm.

Under the ideal coordinate system, the iMSP passes through the origin and has normal vector  $(1, 0, 0)$ . Due to the scanning geometry, points in the ideal coordinate system are reoriented into the observed imaging coordinate by an unknown rotation  $\mathcal{R} = \mathbf{yaw}(\theta)\mathbf{roll}(\phi)\mathbf{pitch}(\omega)$  and displaced by an unknown translation  $\Delta X_0$ ,  $\Delta Y_0$ , and  $\Delta Z_0$ . Precisely, points in the ideal coordinate system are mapped into the imaging coordinate system by the transformation matrix

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} c\phi c\theta c\theta s\omega s\phi - c\omega s\theta c\omega c\theta s\phi + s\omega s\theta \Delta X_0 \\ c\phi s\theta c\omega c\theta + s\omega s\phi s\theta c\omega s\phi s\theta - c\theta s\omega \Delta Y_0 \\ -s\phi & c\phi s\omega & c\omega c\phi \Delta Z_0 \end{bmatrix} \begin{bmatrix} X_0 \\ Y_0 \\ Z_0 \end{bmatrix}$$

where  $c\theta \equiv \cos \theta$ ,  $s\theta \equiv \sin \theta$ , and so on. After some algebraic manipulation, the iMSP  $X_0 = 0$  can be rewritten in terms of the imaging coordinate system as

$$\cos \phi \cos \theta X + \cos \phi \sin \theta Y - \sin \phi Z - (n \cdot \Delta) = 0 \quad (2)$$

where  $n = (\cos \phi \cos \theta, \cos \phi \sin \theta, -\sin \phi)^T$  is the unit normal vector of the plane and  $\Delta = (\Delta X_0, \Delta Y_0, \Delta Z_0)^T$ . Scaling appropriately, and comparing with (1), we find by inspection that

$$a = \cos \theta \quad b = \sin \theta \quad c = -\tan \phi \quad d = -(n \cdot \Delta) / \cos \phi . \quad (3)$$

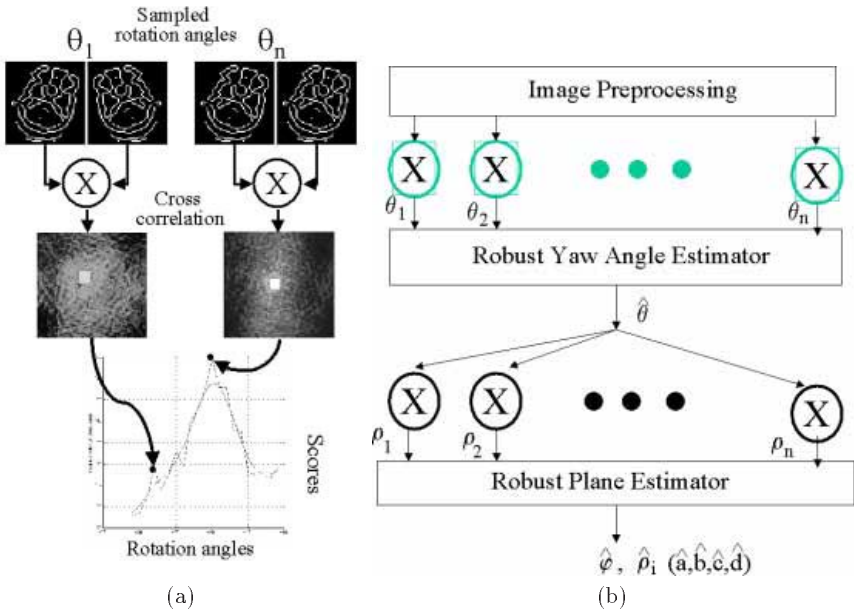
That is, the shared angle  $\theta = \theta_i = \arctan(b/a)$  of each axial slice is actually the yaw angle of the head's imaging coordinate system. Furthermore, the roll angle

$\phi$  can be determined from the offsets of the 2D symmetry axes on the set of slices by solving a linear system of equations  $\rho_i = cZ_i + d$ . Note from this equation and equation (3) that when the roll angle  $\phi$  is zero,  $c = 0$ , and thus all 2D symmetry axes have the same offset  $\rho_i = d$ ; otherwise  $\rho_i$  varies linearly from slice to slice. Finally, the quantity  $(-d \cos \phi)$  measures the displacement of the imaging coordinate system in the direction normal to the symmetry plane.

In summary, if we can extract the 2D axes of reflection symmetry from a set of axial slices, we can completely determine the geometric equation  $aX + bY + cZ + d = 0$  of the ideal MSP. Furthermore, we can infer from this equation some of the 3D pose parameters of the patient’s head with respect to the ideal head coordinate system, namely the yaw angle  $\theta$ , roll angle  $\phi$  and the translational offset along the  $X_0$  axis.

## 2.2 Midsagittal Plane Extraction Algorithm

The geometric results from the previous section have been used to develop an algorithm for automatically detecting the iMSP of a neural brain scan.



**Fig. 3.** (a) Using pairs of edge images (original image and its rotated reflection w.r.t.  $X = 0$  plane) to find the best correlation value for each given rotation angle. The brightest point indicates the highest correlation score. (b) A flow chart of the MSP extraction algorithm, where “X” with a circle around means 2D cross correlation, and with the addition of a square means multiple cross correlations of different rotated images.

Input: a set of brain scans in axial (or coronal) format.

Output: head yaw and roll angles  $\hat{\theta}$ ,  $\hat{\phi}$ , and translational offset of the iMSP from the  $X_0 = 0$  plane.

### iMSP Extraction Algorithm<sup>2</sup>

1. isolate the head region and compute binary edge images  $S_i$ .
2. find an estimated initial rotation error  $\theta_{init}$  from one of the lowest 2D brain slices: for each  $S_i$ , construct  $S'_i = S_i$  reflected w.r.t.  $X = 0$  plane.  
 $\theta_{init} = \arg \max \{C_i(S_i, \text{rot}(S'_i, \theta))\}$  where  $C_i$  is the cross correlation of  $S_i$  and rotated  $S'_i$ ,  $\theta$  is sampled in the range of  $[-90^\circ, 90^\circ]$  or  $[-180^\circ, 180^\circ]$  if necessary.
3. find symmetry axis orientation  $\theta_i$  on each  $S_i$  (Figure 3(a)):  
 for each 2D slice  $S_i$ ,  
 for  $j = -10$  to  $10$  step 1 (degrees),  $C_i(S_i, \text{rot}(S'_i, \theta_{init} + j))$  end;  
 $\theta_i = \arg \max \{C_i\}$ .  
 end;
4. compute the common yaw (or roll) angle (Figure 3(b)):  
 $\hat{\theta} = \text{robust}(\theta_1, \dots, \theta_n)$ , where function *robust* eliminates outliers [20] and finds the median from weighted inliers.
5. compute image offsets  $t_i$  by finding the maximum cross correlation value of each yaw (roll)-angle-corrected 2D slice and its vertical reflection.
6. robust estimation of image offsets  $\rho_i$ : taking out outliers from  $t_i$  using least median of squares [16] and fit a plane to the inliers using  $\rho_i = cZ_i + d$ .
7. compute all plane parameters (Equation (3)).

The algorithm is implemented on an SGI O2 R10000, using a mixture of MATLAB and C subroutines. Total time for all algorithmic steps is roughly 7 minutes. No special attention has yet been paid to speeding up the code, except for using the fast Fourier transform for cross correlation computation. The algorithm has been applied to over 100 3D image sets (Table 1) with varying modalities.

One strategy used to increase robustness to large orientation errors is to use both axial and coronal slices simultaneously to estimate the yaw and roll angles (usually one of these sets of slices is measured directly, and the other is created by resampling the image volume). This is done because the accuracy of symmetry axis offset detection degrades when axial (coronal) slices have a roll (yaw) angle beyond 20 degrees. However, there is no such angular limit to estimating yaw (roll) angles from axial (coronal) slices, as these are in-plane rotations. Figures 4 and 5 show examples of extracted symmetry axes when there are obvious asymmetries in the head.

## 3 Evaluation

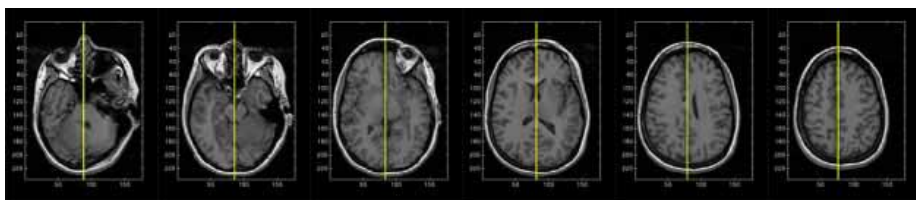
No obvious mishaps have been observed when applying the iMSP extraction algorithm to over 100 image sets with varying modalities and scan geometries. In this section we report a series of experiments that are carried out to test the

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<sup>2</sup> For further details of the algorithm see [9]

**Table 1.** A Sample of Input 3D Image Data

Set	Modality	Form	Matrix	Voxel (mm <sup>3</sup> )	Pathology
5	MR (T1)	coron	256x256x123	0.9375x0.9375x1.5	Normal
17	CT	axial	686x550x9	0.5x0.5x10	Right thalamic acute bleed
58	CT	axial	678x542x17	0.5x0.5x5 (1-9) 0.5x0.5x10 (10-17)	Frontal astrocytoma high grade glial tumor
109	CT	axial	512x512x21	0.4395x0.4395x5 (1-10) 0.4395x0.4395x8 (11-21)	Left parietal infarct
110	CT	axial	512x512x24	0.4297x0.4297x5	Normal

**Fig. 4.** The symmetry axes extracted from a set of axial slices with a 15 degree roll angle (out of plane rotation).

robustness of the iMSP algorithm. Two ground truth image test sets are created from datasets 5 and 110 respectively (Table 1), one is a sparse, axial CT volume and the other is a dense, coronal MR volume. Each ground truth test set is formed by finding the midsagittal plane by hand, then reflecting one half of the head volume about this midsagittal plane to overlay the other half, producing a perfectly symmetrical volume. Since the constructed test set is perfectly symmetric, the ground truth iMSP is known.

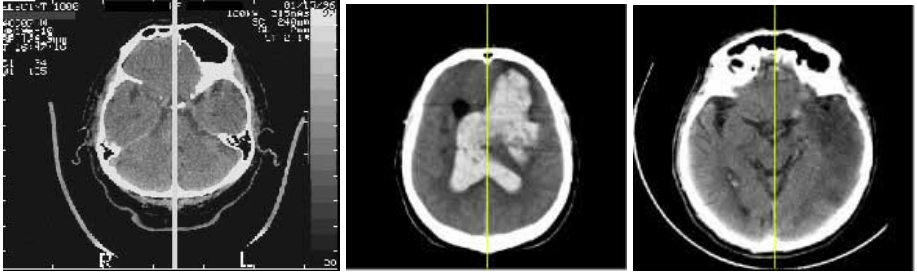
#### Tolerance to initial offset errors

To evaluate the accuracy of computed roll and yaw angles, the MR test image set was resampled using trilinear interpolation to artificially vary the yaw (roll) angles from -90 to 90 degrees in 5 degree intervals. The algorithm was then run on these sets to determine an estimated yaw and roll angle. In all cases, the error between estimated and actual angles is less than one degree. Given the image sampling interval, these errors are negligible.

#### Tolerance to asymmetry

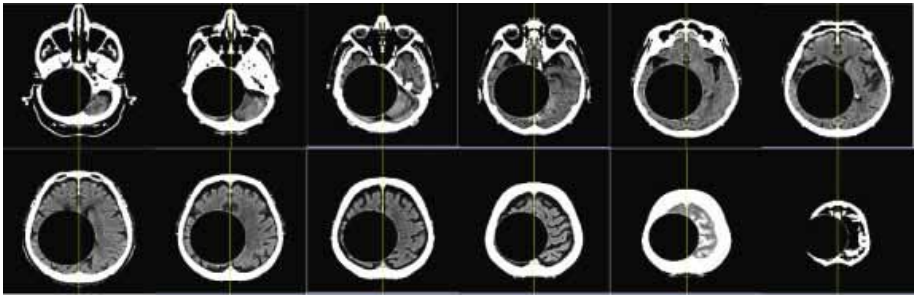
The algorithm is tested by superimposing spherical “lesions” of varying density, size and position into the CT test image. The lesions are offset from the midline, resulting in pathological asymmetry of the brain. The MSP algorithm’s performance starts to decline when the tumor radius reaches 200 pixels (85.94mm),





**Fig. 5.** The symmetry axes extracted from different CT scans where obvious asymmetry is present. Left to right: normal, acute blood, infarct.

and totally fails when the lesion radius reaches 250 pixels (107.4mm) (Figures 6 and 7).



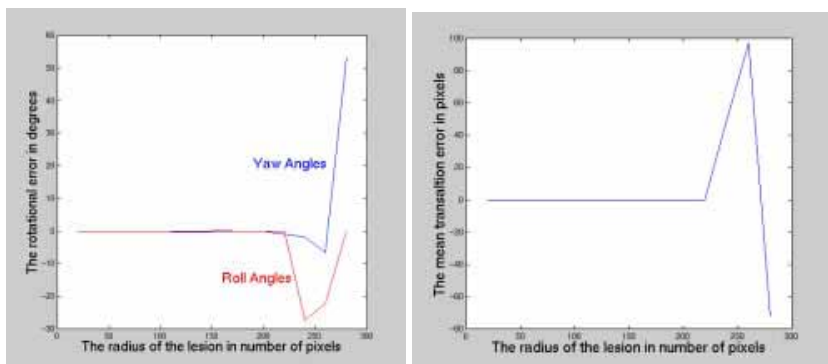
**Fig. 6.** The iMSP algorithm performs successfully when presented with an artificially grown lesion of 100 pixels (42.97mm) radius.

### Tolerance to noise and asymmetry

To study the effects of noise and asymmetry on the iMSP extraction algorithm, we have tested the algorithm on the MR ground truth dataset. The data is artificially degraded by adding different levels of zero-mean Gaussian noise, and by inserting spherical lesions of varying diameters. The algorithm breaking point is determined by incrementally adding noise until the algorithm fails to detect the correct symmetry plane. Each incremental addition of noise corresponds to a loss of 6.02dB of SNR, or roughly 1 bit of information.<sup>3</sup> Figure 8 shows representative slices, and iMSPs extracted by the algorithm. Naturally, the algorithm is more robust to noise when no lesion is present (Figure 8(d)). But the algorithm can handle very large levels of noise (up to SNR = -10.8dB when no lesion is

<sup>3</sup> SNR or Signal to Noise Ratio is defined as  $10 * \log(\text{var}(\text{signal})/\text{var}(\text{noise}))$ . An SNR of less than 0 means that the noise has a higher variance than the signal.





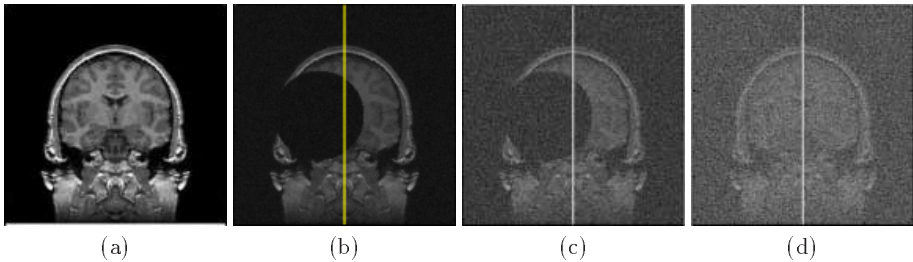
**Fig. 7.** Yaw and roll angle errors (Left) and translational offset errors (Right) versus the radius of an artificial lesion, in pixels (1 pixel = 0.4297 mm). The spherical lesion is centered at 3D location  $X = 310; Y = 210; Z = 350$ . The MSP algorithm’s performance starts to decline when the tumor radius reaches 225 pixels (96.68 mm), and totally fails when the lesion radius reaches 250 pixels (107.43mm).

present), as well as large lesions (we tested with lesions of radius up to 60 pixels = 56.25mm).

### Comparison with a mutual information maximization method

For comparison, an implementation of midsagittal plane extraction based on a general mutual information volume registration algorithm [14] was also tested. Volume registration can be used to identify an iMSP by finding the rigid transformation that best registers a volume with a version of itself reflected about the  $X = 0$  plane. The geometry underlying iMSP extraction in this case is analogous to that described in Section 2.2. We choose to compare a volume registration algorithm based on mutual information due to its intensity-based nature, in contrast to our edge-based method. The experimental results show that iMSP extraction based on mutual information registration breaks down at a lower level of noise than our algorithm, as shown in Figure 8. The volume registration algorithm had to be tested on the dense MR dataset, since it could not directly handle sparse, unisotropic clinical CT data.

**Comparison with human experts** To compare the algorithm with human performance, we had two neuroradiologists (one has 20 years experience, one is an intern) hand-draw the ideal midline on each 2D slice of several randomly chosen brain scans. The radiologists were allowed to view the whole set of the 2D slices from one volumetric image for reference while using a mouse to click on a computer screen directly. Although scan geometry tells us the angles of the symmetry axes on each axial slice should be the same (Section 2.1), there is a variation in the angles determined by the human expert. The standard deviation of the human measurement error on different sets of slices varies from 0.55 to 2.37 degrees (Table 2).



**Fig. 8.** Sample results on images artificially degraded with lesions and noise, to determine algorithm breaking points. (a) one slice from original dataset with no noise, SNR = 43.35dB. (b) result from iMSP extraction based on mutual information registration, on a dataset with lesion plus noise. SNR of breaking point is 13.25dB. (c) result from our algorithm, on a dataset with lesion plus noise. SNR of breaking point is -4.82dB. (d) result from our algorithm when run on a dataset with added noise only (no lesion). SNR of breaking point is -10.84dB.

**Table 2.** Comparison of human vs. computer-estimated yaw angles (in degrees)

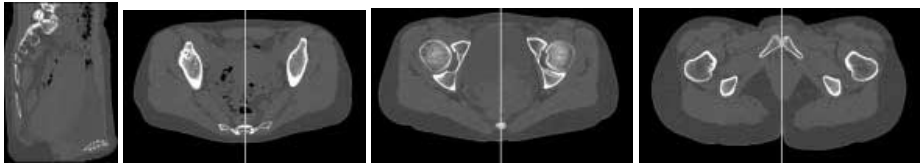
Label	Pathology	# Slices	Expert 1	Expert 2	Expert 1	Expert 2	Computed Yaw $\hat{\theta}$
			Mean( $\theta_i$ )	Mean( $\theta_i$ )	STD( $\theta_i$ )	STD( $\theta_i$ )	
CMU121	infarct	17	1.6208	1.5730	1.0290	0.9972	0.8202
CMU126	blood	21	7.1404	6.2472	2.3678	0.5595	6.0347
CMU129	infarct	10	-2.0248	-1.8201	1.1141	1.6304	-2.2318
CMU130	blood	21	1.3257	0.6829	0.9091	0.8967	1.3216
CMU170	normal	20	-4.3187	-4.5296	1.2781	2.0080	-4.5109
CMU171	normal	22	-1.3028	-1.7582	1.0626	1.1963	-1.0129

## 4 Discussion and Future Work

In this paper, we have presented an iMSP extraction algorithm that is capable of finding the ideal MSP from coarsely sampled, asymmetrical neural images, without compromising accuracy on symmetrical ones. We have observed that iMSP computation using our algorithm is not adversely affected by lesions, mass effects, or noise in the images. This may seem strange since cross-correlation is used as a measure for the best matching of two images. It is natural to ask why the algorithm works so well on drastically asymmetrical images. We can provide the following relevant observations: 1. **Majority rules:** For a 3D pathological brain, a lesion only resides on a relatively small number of 2D slices, thus when the iMSP is fit to the whole set of 2D slices, normal slices with prominent bilateral symmetry dominate the iMSP’s position. 2. **Edge features:** By using edge features rather than the original intensity images directly, the effect of strong density concentration around lesions is much reduced. 3. **Lower brain slice stability:** Lower brain slices are relatively stable due to the bilateral struc-

ture of the skull. In practice, the lower brain slices are given more weight when determining the orientation of the iMSP. 4. **Robust estimators:** Robust estimation techniques are used to remove outliers from computed measurements before combining them to determine plane parameters.

We are currently exploring how to use the iMSP extraction algorithm to facilitate registration of pathological images with other modalities (PET, SPECT), and comparison of brain images (e.g. schizophrenia, acute infarct). Computing similarity among diverse brain images is part of an ongoing effort to study how symmetry-based features can be used for classification and retrieval of medically relevant cases [10,11,12,13]. We have also begun to apply the method on 3D pelvis images, to establish a common coordinate system for cross patient comparison, set an initial position for X-ray/CT registration [8], and evaluate left-right abnormality (Figure 9).



**Fig. 9.** Results from applying the MSP algorithm to pelvis CT images. Leftmost image is the midsagittal plane automatically extracted.

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