

Rupture Directivity of the 2019 ML 6.3 Xiulin (Taiwan) Earthquake Estimated by Near-Field Seismograms: Implications for Source Scaling During Faulting

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Research Article

Keywords: 2018 Hualien earthquake, 2019 Xiulin earthquake, Rupture directivity, Rupture velocity, Static stress drop

Posted Date: February 28th, 2023

DOI: <https://doi.org/10.21203/rs.3.rs-2622549/v1>

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Additional Declarations:

No competing interests reported.

Tables are available in Supplementary Files section.

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3 **Scaling During Faulting**

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37 Pure and Applied Geophysics (PAGEOPH)

38 Submitted on February 24, 2023

40 **Abstract**

41 This study deconvolved regional seismograms to derive the azimuth-dependent
42 source time functions for the 2019 Xiulin earthquake in Hualien, Taiwan. Then, rupture
43 directivity analysis was used to estimate the fault parameters, and the results revealed a
44 rupture length of 11.5 km, a source duration of 7.37 s, and a rupture velocity (V_r) of
45 1.56 km/s, approximately 0.4 times the value of the crustal S-wave velocity.
46 Furthermore, the multiple-event analysis indicated two subruptures during the
47 earthquake. Notably, the average rupture and the subrupture shared the same product of
48 $\Delta\sigma_s V_r^3$ ($\Delta\sigma_s$: static stress drop) and thus obeyed a specific source-scaling relationship.
49 In short, the 2019 Xiulin earthquake had a relatively low V_r and a relatively high $\Delta\sigma_s$.
50 We noted similarities between the 2018 Hualien and 2019 Xiulin earthquakes when
51 comparing the fault parameters; rupture directivity analysis revealed that the two events
52 occurred on a west-dipping plane with a similar strike. Therefore, the 2019 Xiulin
53 earthquake likely constituted the remaining energy release of the 2018 Hualien
54 earthquake.

55

56 **Keywords:** 2018 Hualien earthquake; 2019 Xiulin earthquake; Rupture directivity;
57 Rupture velocity; Static stress drop.

58

59 **1. Introduction**

60 After an M_L 6.2 (M_W 6.4) earthquake struck the city of Hualien in 2018 and caused
61 severe destruction (called the 2018 Hualien earthquake; Rau & Tseng 2019), high
62 seismicity persisted in eastern Taiwan. Approximately 14 months later, on April 19,
63 2019, the Central Weather Bureau (CWB) reported an M_L 6.3 earthquake in the Xiulin
64 region of Hualien. The 2019 event had a depth of approximately 20 km, greater than
65 the 6.3-km depth of the 2018 event, and occurred 18 km to its southwest. The fault-
66 plane solutions indicated that the two events both had a west-dipping plane with a strike
67 of approximately 217° (Fig. 1). Hwang (2018) analyzed the rupture directivity of the
68 2018 Hualien earthquake to suggest that the west-dipping plane was the fault plane.
69 When we superimposed the location of the 2019 Xiulin earthquake on the finite-fault
70 model of the 2018 event (Huang & Huang 2018; Lee et al. 2019), the 2019 event
71 appeared to occur on the 2018 event's fault plane, where it had failed to rupture.
72 Therefore, the data indicated that the two events occurred in the same fault system. This
73 study investigated whether the 2019 Xiulin earthquake originated from the release of
74 the remaining energy of the 2018 Hualien earthquake.

75 Lee et al. (2020) derived the finite-fault model of the 2019 event and calculated a
76 rupture velocity (V_r) of up to 4.0 km/s (i.e., a supershear rupture event) and a static
77 stress drop ($\Delta\sigma_s$) of 3.27 MPa. These calculations differed from those of Lin et al.

78 (2022), who measured V_r values of 2.58 and 3.16 km/s and $\Delta\sigma_s$ values of 13.7 and
79 23.4 MPa for two strong motion generation areas (SGMAs). The conflicting results of
80 the two studies imply an anticorrelation between V_r and $\Delta\sigma_s$; namely, an increase in
81 V_r coincides with a decrease in $\Delta\sigma_s$, and vice versa. Ye et al. (2016) noted that $\Delta\sigma_s V_r^3$
82 remained approximately constant for a given earthquake in finite-fault inversions
83 (Kanamori & Rivera, 2004). Hwang et al. (2020) also proposed an inverse relationship
84 between V_r and $\Delta\sigma_s$ and further derived the product $\Delta\sigma_s V_r^3 = 29.3 \text{ MPa}\cdot\text{km}^3\text{s}^{-3}$
85 from the observations of moderate-to-large earthquakes in Taiwan. Hence, we also
86 investigated whether the 2019 Xiulin earthquake obeyed the conclusion of Hwang et al.
87 (2020).

88 This study analyzed the kinematic and dynamic source parameters of the 2019
89 Xiulin earthquake and compared them with those of the 2018 Hualien earthquake
90 (Huang & Huang 2018; Hwang 2018; Lee et al. 2019; Hwang et al. 2019, 2020, 2022).
91 We first used rupture directivity analysis (e.g., Ben-Menahen 1961; Chung & Kanamori
92 1976; Velasco et al. 1994, 2004; Hwang et al. 2012) to investigate the kinematic source
93 parameters, including rupture length, source duration, and V_r through the azimuth-
94 dependent source time functions (e.g., Ammon et al. 2006; Vallée 2007; Hwang et al.
95 2019). In addition, we also employed multiple-event analysis to determine the dynamic
96 source parameters, including radiated seismic energy, scaled energy, and $\Delta\sigma_s$ (Hwang

97 et al. 2019).

98

99 **2. Data**

100 We used vertical-component acceleration seismograms from the Broadband Array
101 in Taiwan for Seismology (BATS; IES 1996) and the CWB Geophysical Data
102 Management System (CWB 2012) to analyze the azimuth-dependent STFs using a
103 nonnegative time-domain deconvolution technique (Hwang et al. 2019). Only
104 seismograms with epicentral distances of less than 50 km were analyzed to reduce the
105 effect of structural complexity in wave propagation, where the structure can be regarded
106 as a half-space region (Kanamori 1990). Fig. 1 illustrates the available stations around
107 the epicenter. Before retrieving the STFs, we removed the instrument responses,
108 converted the accelerograms into displacement, and filtered the waveforms between
109 0.05 and 0.33 Hz. Finally, for the follow-up deconvolution, we extracted a 35-s-long
110 waveform, which began during the first 5 s of the P-wave arrival and ended during the
111 last 30 s of the P-wave arrival (Figs 2 and 3).

112

113 **3. Analysis and results**

114 **3.1 Source time functions (STFs)**

115 The nonnegative time-domain deconvolution was employed to solve $g(t) *$

116 $s(t) = b(t)$ for retrieving the STF, with $b(t)$ as the observed waveform, $g(t)$ as the
 117 empirical Green's function (EGF), $s(t)$ as the STF, and '*' representing the
 118 convolution operator. The time domain convolution can be written in linear matrix form
 119 as $GS = B$, where G is the EGF matrix arranged according to the convolution
 120 operation, S is the STF matrix with the unknown parameters to be solved, and B is
 121 the observed waveform matrix. The damped least-squares method with nonnegative
 122 constraint (i.e., $S \geq 0$) was applied to the linear inversion (Lawson & Hanson 1974;
 123 Menke 2012) by minimising $E + \lambda^2 L$, where $E = ||B - GS||^2$, $L = ||WS||$, damping
 124 $= \lambda^2$, and W = matrix smoothness to yield the following solution:

$$125 \quad S = (G^T G + \lambda^2 W^T W)^{-1} G^T B \quad (1)$$

126 Details regarding the nonnegative time-domain deconvolution can be found in the
 127 work of Hwang et al. (2019). We used synthetic seismograms without source duration
 128 as the EGFs, created using the wavenumber integration technique (Herrmann 2013) in
 129 a half-space model with a P-wave velocity of 6.47 km/s, an S-wave velocity of 3.76
 130 km/s, and a density of 2.80 g/cm³. To generate the EGFs also needed a focal mechanism,
 131 provided by the BATS CMT (Central Moment Tensor) catalogue (IES 1996) (Fig. 1).
 132 Fig. 2 provides an example of deconvolution for station WUSB.

133 Fig. 3 presents the apparent STFs (aSTF) with duration variations according to the
 134 station azimuths. A relatively longer duration occurred at stations located south of the

135 epicenter (e.g., EGC, ESL, and SHUL); by contrast, a relatively shorter duration
 136 dominated the stations situated north of the epicenter (e.g., ETLH, NACB, ENA, NNS,
 137 NNSB, and EWT). The apparent source duration variation with station azimuth formed
 138 a shape approximating a cosine or sine wave (Fig. 3), revealing unilateral rupture
 139 (Hwang 2014). This feature indicated that the 2019 Xiulin earthquake was a unilateral-
 140 faulting event with a northward rupture. We next implemented rupture directivity
 141 analysis to investigate the rupture propagation of the 2019 Xiulin earthquake.

142

143 **3.2 Rupture directivity analysis**

144 The apparent source duration (T_{ASD}) for an event with unilateral faulting (Fig. 4a)
 145 due to the rupture directivity effect can be written as follows:

$$146 \quad T_{ASD} = t_0 - \frac{l}{v} \cos \delta \quad (2)$$

147 where v is the wave velocity (P- or S-wave) at the source area, l is the rupture length,
 148 and t_0 is the source duration (corresponding to l/V_r) observed at the station azimuth
 149 that is perpendicular to the rupture direction. Because the STF is derived primarily from
 150 the S-wave (Fig. 2), v in Equation 2 is the S-wave velocity (3.76 km/s in this study).

151 In Equation 2, $\cos \delta$ can be expressed below (Chung & Kanamori 1976):

$$152 \quad \cos \delta = \cos i_d \cos \theta + \sin \theta \sin i_d \cos(AZ - \phi)$$

153 where δ is the angle between the rupture direction and a ray taking off from the

154 hypocentre, i_d is the take-off angle of the wave ray, AZ is the station azimuth, ϕ is
155 the horizontal rupture azimuth measured clockwise from the north, and θ is the
156 vertical rupture angle measured upward from the vertically downward axis (see Fig.
157 4a). For θ larger than 90° , the event ruptures upward; for θ less than 90° , the event
158 ruptures downward. When searching for a series of ϕ and θ , we obtained an
159 appropriate pair of (ϕ, θ) constructing an optimal linear relationship between t_{ASD}
160 and $\cos \delta$. Therefore, the intercept denotes the average source duration (t_0 in Equation
161 2), and the slope represents the propagation time ($\frac{l}{v}$ in Equation 6) used to obtain the
162 rupture length (l) when v at the source area is known. Finally, we derived the average
163 rupture velocity from l and t_0 .

164 Fig. 4 shows the rupture directivity analysis of the 2019 Xiulin earthquake. The
165 optimal pair of (ϕ, θ) , identified by searching for ϕ and θ between 0° and 180°
166 with an interval of 1° , was $(5^\circ, 76^\circ)$, indicative of a slightly downward rupture along
167 the azimuth of N5°E (Fig. 4b). The optimal linear relationship between T_{ASD} and
168 $\cos \delta$, as illustrated in Fig. 4c, had a rupture length (l) of 11.5 km and a source duration
169 of 7.37 s, resulting in a V_r of 1.56 km/s, about 0.4β (β is the S-wave velocity as 3.36
170 km/s). Unlike the results of Lee et al. (2019), which demonstrated a high V_r of 4.0
171 km/s for the Xiulin earthquake, the low V_r of this study is similar to the estimated V_r
172 (1.85 km/s) of the 2018 Hualien earthquake (Hwang 2018; Hwang et al. 2020).

173 The angle between the optimal rupture direction and the vertically downward axis
174 was 76° , analogous to the take-off angle (Fig. 4b). We projected the optimal rupture
175 direction ($\phi = 5^\circ$, $\theta = 76^\circ$) to the focal mechanism (i.e., beachball; BATS CMT) as
176 illustrated with a solid blue circle in Fig. 4d. The solid blue circle is closer to the red
177 arc than the other arc; we thus verified that the west-dipping plane with a strike of 217°
178 (from BATS CMT with the best double couple of $217^\circ/61^\circ/81^\circ$ and $55^\circ/30^\circ/105^\circ$) was
179 the fault plane (red arc) of the 2019 Xiulin earthquake.

180 The derived source parameters are also comparable with several empirical
181 relationships. When using $M_0 = 3 \times 10^{18}$ Nm (Table 1), the source duration (7.37 s)
182 from this study agrees with that (7.4 s) calculated by an empirical relationship between
183 M_0 and T as $M_0 = 0.74 \times 10^{16} T^3$ (M_0 = seismic moment in Nm and T = source
184 duration in s) (Hwang et al. 2020); however, the derived rupture length (11.5 km) is
185 slightly shorter than that (14.4 km) estimated by $\log_{10} L = (1/2) \log_{10} M_0 - 8.08$ for
186 $M_0 < 10^{20}$ Nm (L = rupture length in km; Yen & Ma 2011).

187

188 **3.3 Multiple-event analysis**

189 Because station WUSB with azimuth is approximately perpendicular to the rupture
190 direction, we used the aSTF deconvolved from WUSB as the STF of the 2019 Xiulin
191 earthquake (Fig. 2). Through multiple-event analysis of the STF (cf. Hwang 2013;

192 Hwang et al. 2019), the mainshock comprised at least three subevents, each of which
 193 had its own isosceles triangle and source duration (Table 1 and Fig. 2). Then, the seismic
 194 moment (M_0) of each subevent was calculated from the area of the isosceles triangle
 195 STF, and the radiated seismic energy (E_s) of each subevent was estimated from M_0
 196 and its own source duration (cf. Vassiliou & Kanamori 1982). The total M_0 and E_s
 197 were 3.0×10^{18} Nm (M_w 6.3) and 1.2×10^{14} Nm, respectively; these measurements
 198 were somewhat larger than those calculated by several institutes (United States
 199 Geological Survey, USGS; Global Centroid-Moment-Tensor, GCMT; BATS, and CWB)
 200 and by Lee et al. (2020). From Table 1 and Fig. 2, our results revealed that the largest
 201 subevent with M_w 6.1 occurred about 3 s later than the initiation. The E_s/M_0 ratio of
 202 3.4×10^{-5} also resembled the global average (3.0×10^{-5} ; Ide & Beroza 2001) and was
 203 comparable with that of the 2018 Hualien earthquake (2.72×10^{-5} ; Hwang et al. 2019).
 204 We also estimated the $\Delta\sigma_s$ of each subevent following circular cracks (Brune 1970)
 205 using $\Delta\sigma_s = \frac{7M_0}{16} \left(\frac{2\pi f_c}{2.34\beta} \right)^3$ with $f_c = \frac{2}{\pi T_{rup}}$ (Godano et al. 2015), where β is the S-
 206 wave velocity at the source area, and f_c is the corner frequency determined by the
 207 rupture time (T_{rup}), which is about 0.85 times the value of the source duration (cf.
 208 Vassiliou & Kanamori 1982; Heaton 1990). From the multiple-event analysis, the
 209 average $\Delta\sigma_s$ was measured to be 8.82 MPa using weighted M_0 (cf. Kanamori &
 210 Heaton 2000). In addition, from the E_s/M_0 ratio, the apparent stress (σ_a) was 1.35

211 MPa using $\sigma_a = \mu E_s/M_0$ (μ : rigidity; Wyss & Brune 1968). Because $\sigma_a/\Delta\sigma_s < 0.5$,
212 the frictional overshoot model, in which the frictional stress is lower than the final stress
213 on the fault plane, can be used to interpret the 2019 Xiulin earthquake rupture (Savage
214 & Wood 1971; Zúñiga 1993; Kanamori & Rivera 2006). Table 1 lists the source
215 parameters of the three subevents composing the 2019 Xiulin earthquake.

216 According to Fig. 3, the aSTF at several stations may be divided into two groups,
217 G1 and G2. G1 consists of the first two subevents, and G2 consists of the last subevent
218 (see Table 1). We assumed that G1 and G2 occurred along the optimal rupture direction
219 of $(5^\circ, 76^\circ)$, as measured in Fig. 4. Fig. 5a shows the rupture directivity analysis of G1
220 based on the optimal rupture direction of $(5^\circ, 76^\circ)$ to obtain a V_r of 1.61 km/s, a rupture
221 length of 7.26 km, and a source duration of 4.50 s. Next, subtracting the rupture length
222 and source duration of G1 from the entire rupture length and source duration, we
223 obtained a V_r of 1.48 km/s, a rupture length of 4.24 km, and a source duration of 2.87
224 s for G2 (Fig. 5b). The rupture from G1 to G2 revealed a slight deceleration.

225

226 **3.4 Static stress drop**

227 As mentioned in the preceding section, using multiple-events analysis, the average
228 $\Delta\sigma_s$ was estimated at 8.82 MPa (Table 1). However, a standard method of calculating
229 $\Delta\sigma_s$ is to use the rupture area (A) as: $\Delta\sigma_s = \frac{7M_0}{16} \left(\frac{\pi}{A}\right)^{3/2}$ (cf. Kanamori & Anderson,

230 1975). Here, we attempted to calculate the rupture area of the 2019 Xiulin earthquake
231 by the rupture length and width. The rupture width using the aftershock distribution and
232 the fault dip was calculated. As shown in Fig. 1, aftershocks with $M_L \geq 3.0$ appeared at
233 depths of 18–25 km with an approximately 7-km-depth range. In addition, the focal
234 mechanisms from GCMT, USGS, BATS, CWB, and Lee et al. (2020) indicated fault
235 dips of 60° , 46° , 61° , 69° , and 63° , respectively. The rupture widths were then estimated
236 to be 8.08, 9.73, 8.00, 7.50, and 7.85 km, respectively, yielding an average rupture width
237 of 8.23 km. Hence, the rupture area is 94.65 km^2 ($11.5 \text{ km} \times 8.23 \text{ km}$) for the 2019
238 Xiulin earthquake. Assuming a circular fault (Kanamori & Anderson 1975), through the
239 rupture area, the 2019 Xiulin earthquake had a $\Delta\sigma_s = 7.94 \text{ MPa}$, similar to the
240 measurement (8.82 MPa) obtained through multiple-event analysis. In any case, the two
241 results were relatively higher than that (3.27 MPa) estimated by Lee et al. (2020) but
242 comparable with the single SMGA $\Delta\sigma_s$ of Lin et al. (2022). Through the rupture area,
243 the average dislocation slip (D) for the 2019 Xiulon earthquake is about 0.8 m by $M_0 =$
244 μDA (Aki, 1966).

245

246 **4. Discussion**

247 The results of the rupture directivity analysis based on azimuth-dependent STFs
248 (Figs 3 and 4) verified the fault plane to be a west-dipping plane with a strike of 217°

249 (BATS CMT). Such results were similar to the rupture directivity analysis of the 2018
250 Hualien earthquake (Hwang 2018); therefore, the two events seemingly occurred in the
251 same fault system (Fig. 1). Furthermore, the 2018 M_W 6.4 Hualien and the 2019 M_L 6.3
252 Xiulin earthquakes shared additional common features. First, the two events had
253 relatively slow average V_r values, with 1.85 km/s (0.55 β , β : S-wave velocity) for the
254 2018 event and 1.56 km/s (0.4 β) for the 2019 event. Second, the two earthquakes had
255 a similar E_S/M_0 , which also corresponds to the global value of 3×10^{-5} (Ide & Beroza
256 2001). Third, both events could be interpreted using the frictional overshoot model, i.e.,
257 the final stress on the fault plane is larger than the frictional stress (cf. Kanamori and
258 Rivera, 2006). Fourth, even though the $\Delta\sigma_s$ of the 2019 event was larger than that of
259 the 2018 event, the two events had a similar product $\Delta\sigma_s V_r^3$, a finding that closely
260 agrees with the suggestion of Hwang et al. (2020), i.e., $\Delta\sigma_s V_r^3 = 29.3 \text{ MPa}\cdot\text{km}^3/\text{s}^3$ for
261 Taiwan's moderate-to-large earthquakes (Fig. 6). Fifth, the 2019 event seemingly
262 occurred on an unruptured area of the 2018 event's fault plane when superimposed on
263 the finite-fault models of Huang and Huang (2018) and Lee et al. (2020). From these,
264 a high level of similarities is evident between the 2018 and 2019 events. Hence, the
265 2019 event likely originated from the release of the remaining energy of the 2018 event.
266 Table 2 lists the source parameters of the 2018 and 2019 events for comparison.

267 In addition, we investigated whether the subruptures during faulting corresponded

268 to the proposed source-scaling relationship, having $\Delta\sigma_s V_r^3 = 29.3 \text{ MPa}\cdot\text{km}^3/\text{s}^3$
 269 (Hwang et al. 2020). As shown in Table 1 and Fig. 5, the subrupture of G1 had a V_r of
 270 1.61 km/s and a $\Delta\sigma_s$ of 8.11 MPa, resulting in $\Delta\sigma_s V_r^3 = 33.85 \text{ Mpa}\cdot\text{km}^3/\text{s}^3$; the
 271 subrupture of G2 had a V_r of 1.48 km/s and a $\Delta\sigma_s$ of 10.77 MPa, leading to $\Delta\sigma_s V_r^3 =$
 272 34.91 $\text{MPa}\cdot\text{km}^3/\text{s}^3$ (Fig. 5b). Both subruptures also had the similar $\Delta\sigma_s V_r^3$ to obey the
 273 source-scaling relationship proposed by Hwang et al. (2020).

274 Unlike a high V_r (4.0 km/s) obtained by Lee et al. (2020) using the rupture
 275 wavefront of their finite-fault model, our study derived a relatively slow V_r (1.56 km/s).
 276 In order to investigate the validity of the derived V_r , we implemented a parameter called
 277 radiation efficiency (η_R), generally defined as $\eta_R = E_s/E_{s0} = E_s/(E_s + E_g)$, where
 278 the available energy $E_{s0} = (\frac{1}{2})\Delta\sigma_s DA$, and E_g is the fracture energy (D : dislocation
 279 slip; A : rupture area) (cf. Venkataraman & Kanamori 2004; Kanamori & Rivera 2006;
 280 Wang 2006). For subshear earthquakes with $V_r < \beta$ (β : S-wave velocity), then $\eta_R <$
 281 1; for supershear earthquakes with $V_r > \beta$, then η_R is possibly close to 1.0 (Kanamori
 282 2004). For a frictional overshoot model, E_{s0} might be overestimated; then the original
 283 E_{s0} must be reduced to $0.6E_{s0}$ for $V_r = 0.9\beta$ and $0.7E_{s0}$ for $V_r = 0.6\beta$
 284 (Madariaga 1976). In addition, η_R can also be estimated by V_r . For model III crakes,
 285 we have $\eta_R = 1 - \sqrt{(1 - V_r/\beta)/(1 + V_r/\beta)}$ in the subshear case (Husseini &
 286 Randall 1976; Husseini 1977). From E_s and $\Delta\sigma_s$ estimated in this study, we obtained

287 $\eta_R = 0.31$; in addition, using the derived V_r to yield $\eta_R = 0.35$. The two estimations
288 are close to each other. Because the 2019 Xiulin earthquake rupture belongs to the
289 frictional overshoot, the value of η_R might be increased to 0.4–0.5, comparable with
290 the η_R of the 2018 Hualien earthquake (Hwang et al. 2022). Here, whether η_R is
291 estimated from E_S and $\Delta\sigma_S$ or V_r , η_R is always less than 1.0. Therefore, we suggest
292 that the 2019 Xiulin earthquake should have a slow V_r , indicating a subshear
293 earthquake rather than a supershear one.

294

295 **6. Conclusions**

296 The rupture directivity analysis of the 2019 Xiulin earthquake from the azimuth-
297 dependent STFs, deconvolved from regional seismograms, indicated a relatively slower
298 rupture velocity (~0.4 times the crustal S-wave velocity) and verified a west-dipping
299 plane to be the fault plane. Observations from the average rupture and the subrupture
300 both obeyed the proposed source-scaling relationship (i.e., $\Delta\sigma_S V_r^3 = \text{constant}$; Hwang
301 et al. 2020). In addition, we noted similarities in the source parameters of the 2018
302 Hualien and 2019 Xiulin earthquakes. Therefore, our findings indicate that the 2019
303 Xiulin event was likely the remaining energy of the 2018 Hualien earthquake.

304

305 **Acknowledgements** We first thank the Central Weather Bureau (CWB) and the

306 Institute of Earth Sciences(IES), Academia Sinica, Taiwan, for permitting the use of
307 their earthquake catalog and seismograms. The National Science Council, ROC,
308 financially supported this study under Grant No. MOST110-2116-M-034-004.

309

310 **Authors' contributions**

311 RD contributed to the conception and design of the study, conducted the analyses, and
312 drafted the manuscript. YL contributed to the discussion and interpretation and revised
313 the manuscript. WY contributed to the discussion and interpretation. CY and CY drew
314 the part of the figures. All authors read and approved the final manuscript.

315

316 **Competing interests**

317 The authors declare that they have no competing interests.

318

319 **Data Availability**

320 The seismograms were acquired from the Broadband Array in Taiwan for
321 Seismology (BATS; <https://bats.earth.sinica.edu.tw>) and the Central Weather Bureau
322 Geophysical Data Management System (CWB GDMS; <https://gdmsn.cwb.gov.tw>). The
323 earthquake catalog and focal mechanisms were from the CWB GDMS and BATS.

324

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456

457 **Figure Captions**

458 **Figure 1.** Locations of the 2019 Xiulin earthquake and its aftershocks in eastern
459 Taiwan. Also included is the 2018 Hualien earthquake. The stars indicate the
460 epicenters of the two mainshocks. The blue and red circles indicate the aftershocks
461 within one month for the Xiulin and Hualien earthquakes, respectively. Aftershock
462 distributions with depths are illustrated in two profiles, AA' along the strike and BB'
463 vertical to the strike. Focal mechanisms are from the BATS CMT catalogue. The
464 triangles represent the seismic stations used in this study.

465 **Figure 2.** Nonnegative time-domain deconvolution for station WUSB. From top to
466 bottom, the blue and red lines denote the observed and reconstructed P-waves; the
467 black line is the empirical Green's function (EGF), which was created from a half-
468 space velocity model. The bottom line is the deconvolved source time function
469 (STF), and the blue shading represents the multiple-event analysis.

470 **Figure 3.** (Left) The stations used for deconvolution. The yellow and purple triangles
471 denote the stations from the CWB and the BATS. The star is the epicenter of the
472 mainshock. (Middle) The source time functions (STFs) were obtained through
473 nonnegative time-domain deconvolution. The dashed lines represent two
474 subruptures (also see Fig. 5). (Right) Comparison of the observed (blue lines) and
475 reconstructed (red lines) P-waves.

476 **Figure 4.** (A) A coordinate system for a source rupture in space. O is the hypocentre, R
477 is the termination of the rupture, \overrightarrow{OR} is the rupture direction, and l is the rupture
478 length. ϕ and θ are the angles that describe the rupture in space, where ϕ is the
479 horizontal rupture azimuth measured clockwise from the north and θ is the vertical
480 rupture angle measured upward from the Z-axis. In addition, i_d is the take-off angle
481 of a wave ray, AZ is the station azimuth, and δ is the angle between the rupture
482 direction and a ray taking off from the hypocentre and controls the rupture directivity
483 of the source. (B) Rupture directivity analysis to search for the optimal rupture
484 azimuth (θ , ϕ), which is (5° , 76°). (C) A plot of T_{ASD} versus $\cos\delta$ in accordance
485 with the optimal rupture azimuth in (B). (D) The optimal rupture azimuth is projected
486 on the equal-area net to indicate the fault plane (red arc) from the fault-plane
487 solutions of the BATS CMT.

488 **Figure 5.** (A) Rupture directivity analysis for the first subrupture (G1) following the
489 optimal rupture azimuth of (5° , 76°). Please also see Fig. 4. (B) Schematic of the
490 subruptures G1 and G2 and their corresponding rupture parameters. The rupture
491 length and duration of G2 were obtained by subtracting the values of G1 from the
492 total rupture length and duration.

493 **Figure 6.** Log-log plot of rupture velocity (V_r) and static stress drop ($\Delta\sigma_s$) for Taiwan's
494 moderate-to-large earthquakes. Excluding the squares from this study, the data

495 plotted are from Hwang et al. (2020). G1 and G2 represent the two subruptures of

496 the 2019 Xiulin earthquake (also see Fig. 5).

497

Figures

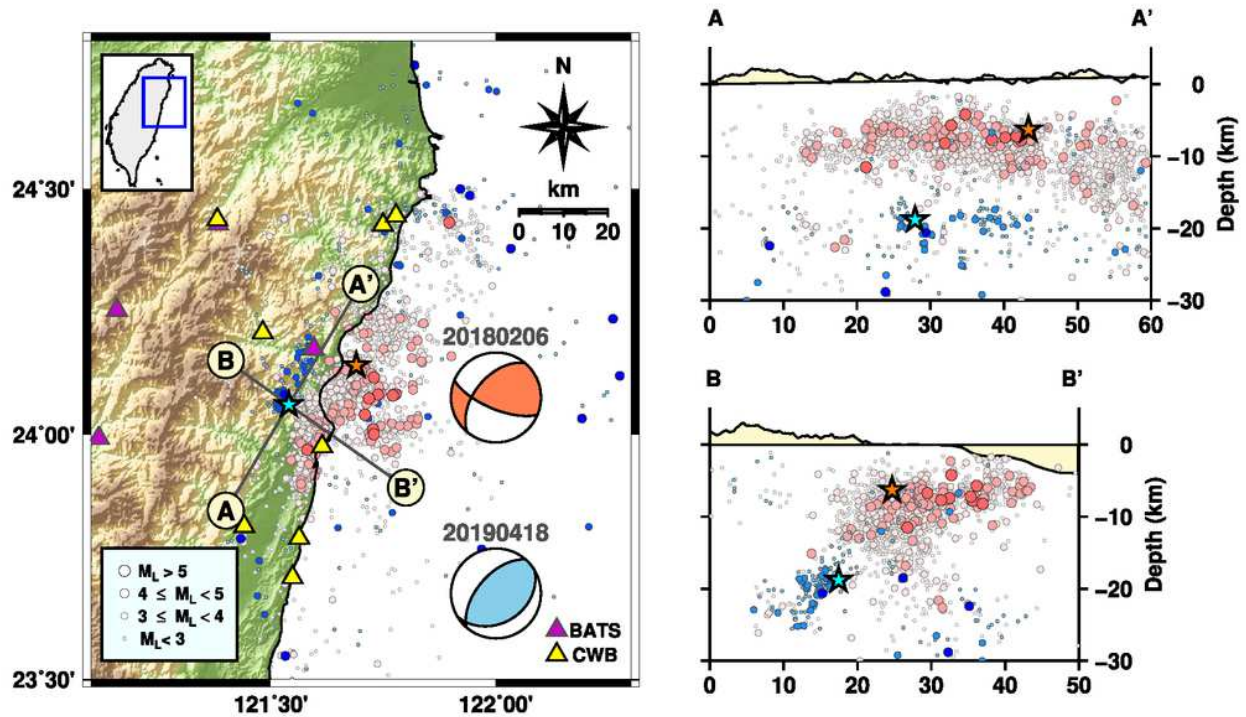


Figure 1 (Hwang et al., 2023)

Figure 1

Locations of the 2019 Xiulin earthquake and its aftershocks in eastern Taiwan. Also included is the 2018 Hualien earthquake. The stars indicate the epicenters of the two mainshocks. The blue and red circles indicate the aftershocks within one month for the Xiulin and Hualien earthquakes, respectively. Aftershock distributions with depths are illustrated in two profiles, AA' along the strike and BB' vertical to the strike. Focal mechanisms are from the BATS CMT catalogue. The triangles represent the seismic stations used in this study.

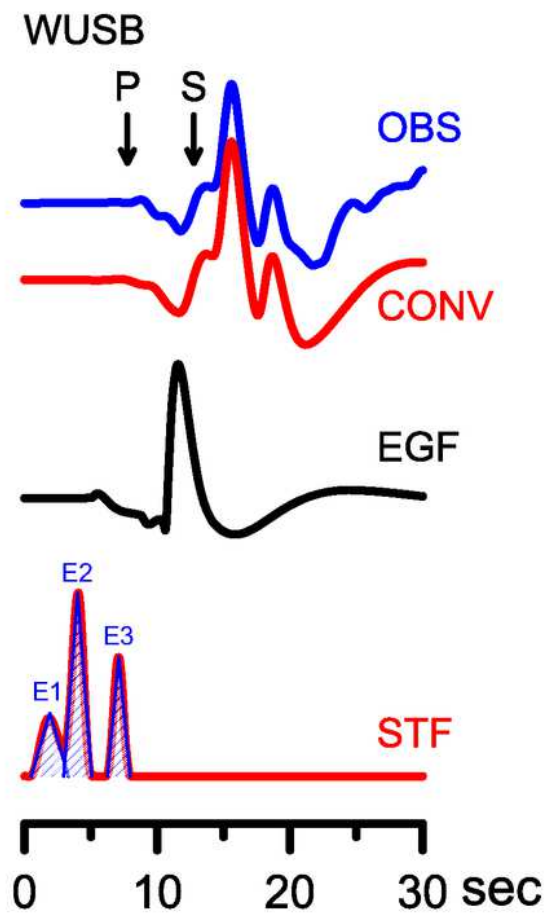


Figure 2 (Hwang et al., 2023)

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Nonnegative time-domain deconvolution for station WUSB. From top to bottom, the blue and red lines denote the observed and reconstructed P-waves; the black line is the empirical Green's function (EGF), which was created from a half-space velocity model. The bottom line is the deconvolved source time function (STF), and the blue shading represents the multiple-event analysis.

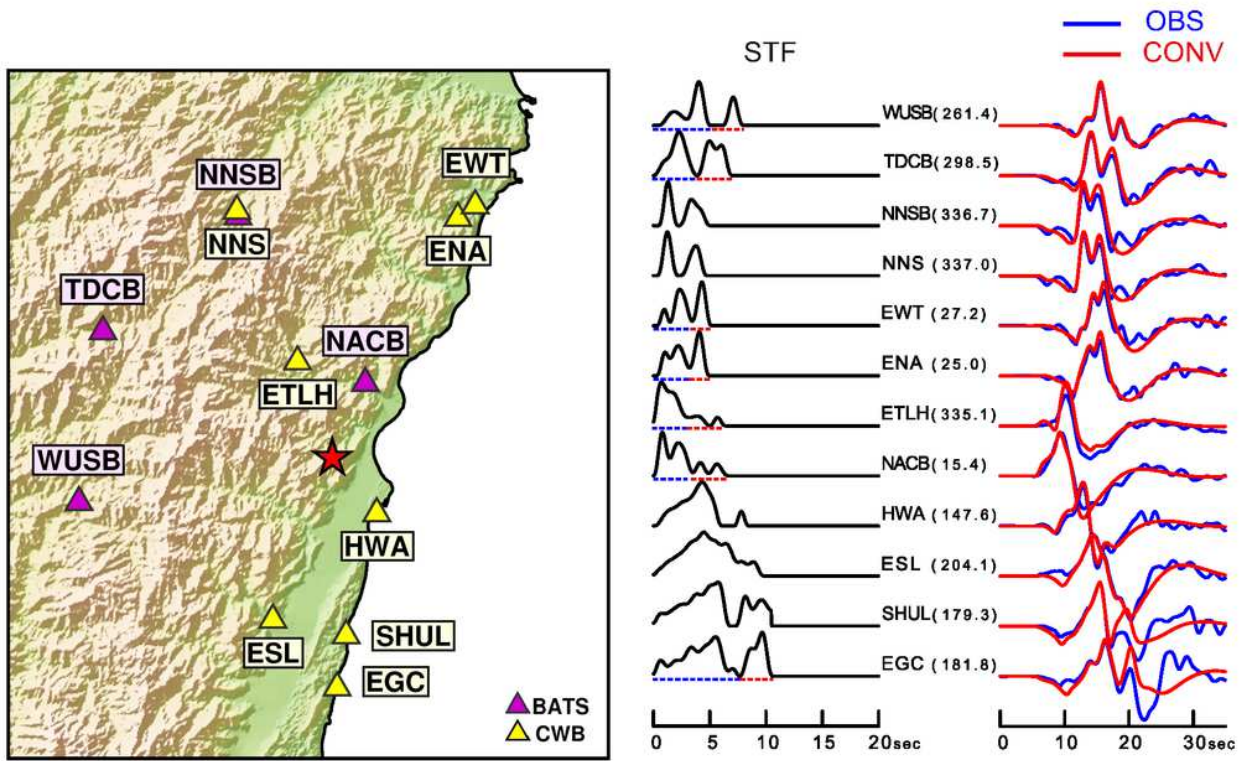


Figure 3 (Hwang et al., 2023)

Figure 3

(Left) The stations used for deconvolution. The yellow and purple triangles denote the stations from the CWB and the BATS. The star is the epicenter of the mainshock. (Middle) The source time functions (STFs) were obtained through nonnegative time-domain deconvolution. The dashed lines represent two subruptures (also see Fig. 5). (Right) Comparison of the observed (blue lines) and reconstructed (red lines) P-waves.

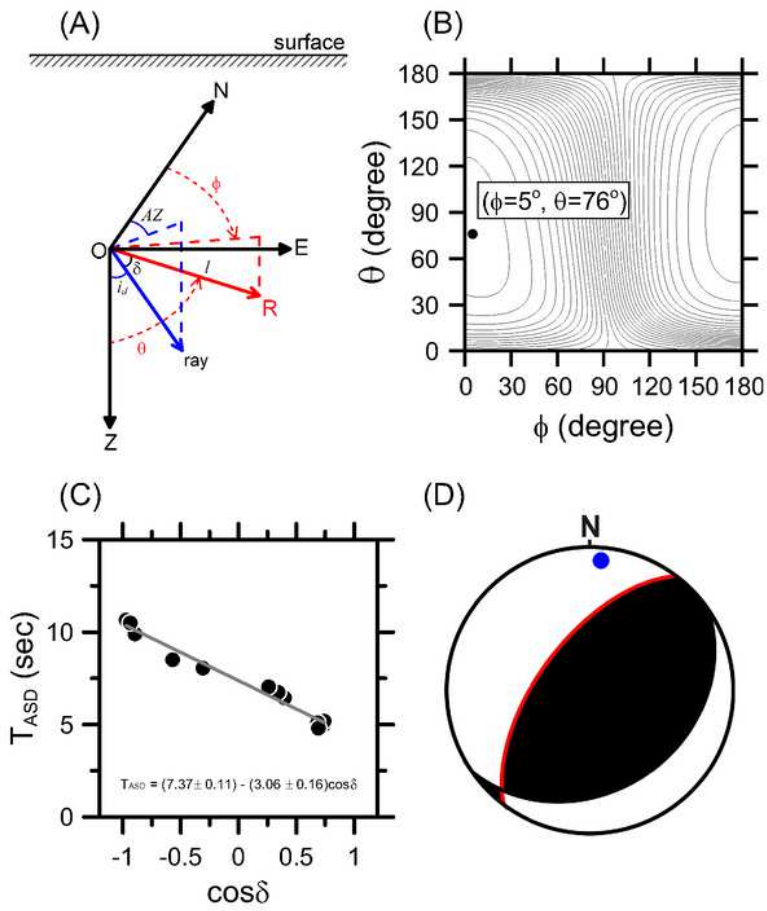


Figure 4 (Hwang et al., 2023)

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Figure 4

See image above for figure legend

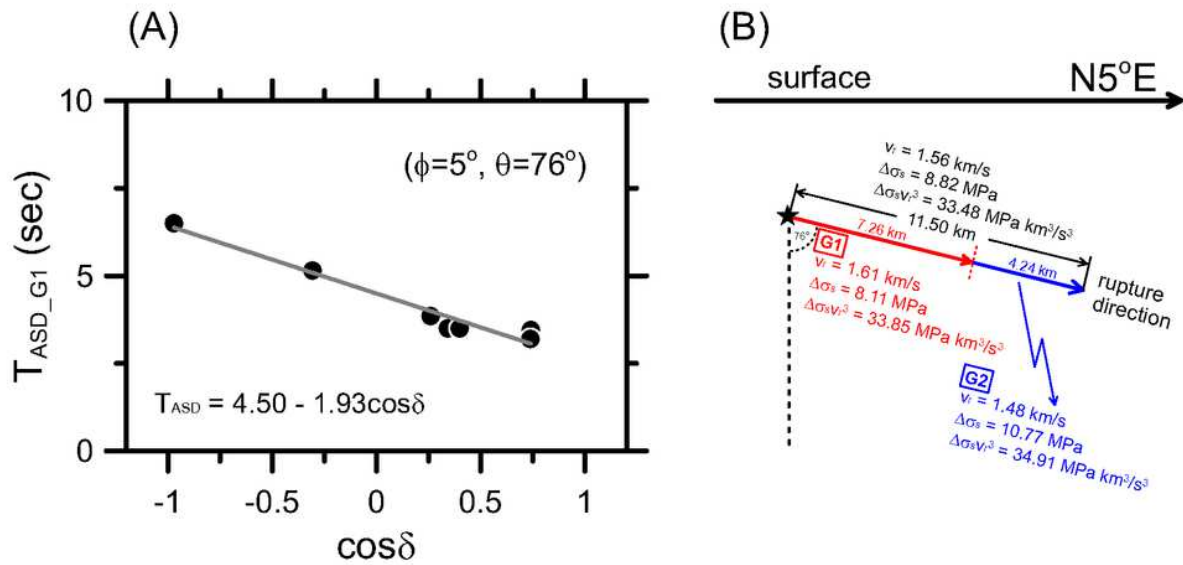


Figure 5 (Hwang et al., 2023)

Figure 5

(A) Rupture directivity analysis for the first subrupture (G1) following the optimal rupture azimuth of (5° , 76°). Please also see Fig. 4. (B) Schematic of the subruptures G1 and G2 and their corresponding rupture parameters. The rupture length and duration of G2 were obtained by subtracting the values of G1 from the total rupture length and duration.

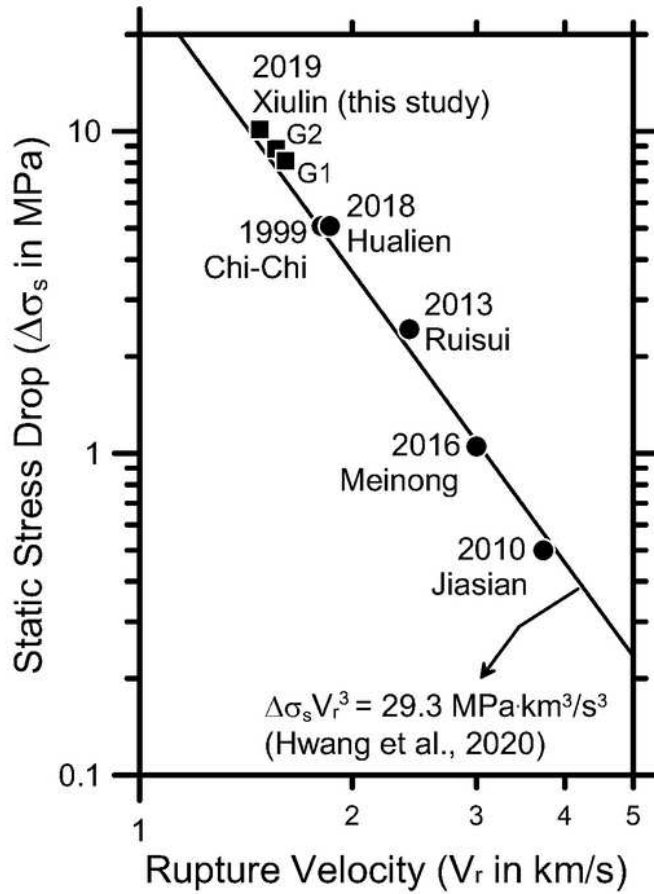


Figure 6 (Hwang et al., 2023)

Figure 6. Log-log plot of rupture velocity (V_r) and static stress drop ($\Delta\sigma_s$) for Taiwan's moderate-to-large earthquakes. Excluding the squares from this study, the data plotted are from Hwang et al. (2020). G1 and G2 represent the two subruptures of the 2019 Xiulin earthquake (also see Fig. 3).

Figure 6

See image above for figure legend

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